

# Algorithms for Bioinformatics - lect 4

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Till now, we have talked about global sequence alignment (NW algorithm) and local sequence Alignment (SW algorithm). In both cases we want to minimize a score,  $M_{i,j}$ .

Until now the alphabet we have seen is limited to the DNA (ATCG),  $match = 1$   $mismatch = -1$  independently from the actual letters. Both algorithm that we have seen so far are correct, we actually find the maximum score.

1. solve practical problems (so far we are here, NW and SW)
2. modeling a biological phenomenon
3. understanding the computation done by the biological system.

## 1 Modeling a biological phenomenon

<http://xaktly.com/GeneticCode.html> here we can see the abbreviations for the aminoacid, this means that so far we use only one alphabet but we could use even the aminoacid one.

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AUG AUU GGU  
AUG AUU GGC

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this seems different but due to the fact that the last triplet represents the same aminoacid the actual difference is 0. With this alphabet we don't expect that the match-mismatch model works in the same optimal way.

### 1.1 Substitution matrices

1. PAM (1978) [https://en.wikipedia.org/wiki/Point\\_accepted\\_mutation](https://en.wikipedia.org/wiki/Point_accepted_mutation) Percent Accepted Mutation.
2. BLOSUM

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AAU  
AAA

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1. Generation

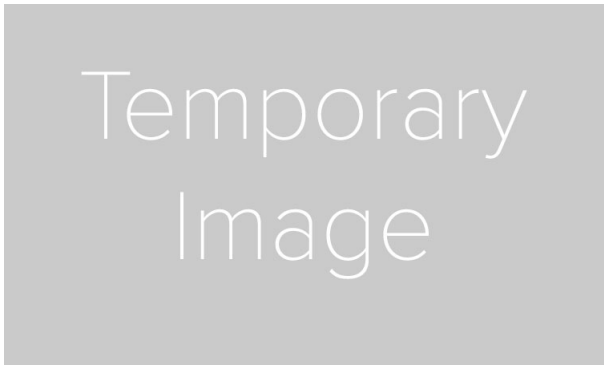


Figure 1: For each aminoacid we have the probability of be substituted by another aminoacid, basically a markov chain.

Table 1: accepted point mutation

	A	B	C	D	G	H	I	J
A			1	1				
B			1	1				
C	1	1						
D	1	1						
G								
H								
I								
J								

2. Conservation (acceptation)

Let's assume we have this kind of sequence

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ACGH	DBGH	ADIJ	CBIJ
(ACGH)–ABGH–(DBGH)	(ADIJ)–ABIJ–(CBIJ)		
(ABGH)–AB**–(ABIJ)			

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$$A_{jk} = \frac{1}{nT} \sum_T A_{jk}^T$$

$$P_{jk}^{(1)} = m_j \frac{A_{jk}}{\sum_{h \neq j} A_{jh}}$$

$$P_{jj}^{(1)} = 1 - m_j$$

$$m_j = \frac{1}{np_j z} \frac{\sum_{l \neq j} A_{jl}}{\sum_h \sum_{l \neq h} A_{hl}}$$

1.  $m_j$  = the mutability of the amminoacid  $j$
2.  $z$  is a normalizing factor s.t.=  $\sum_{ji}(P_j \mu_j) = \frac{1}{100}$

The steps we needed were, find probabilities and find the scores.

$$q_{jk}^{(n)} = P_j p_{jk}^{(n)}$$

$$S_{[j,k]}^n = \lambda \log \frac{q_{jk}}{P_j P_k} = \lambda \log \frac{P_{jk}^{(n)}}{P_k}$$

j and k are aminoacid, p their propabilities, q is the probability that j mutated in a certain way, the score is the comparison.

$$S_{[j,k]}^{(n)} \neq S_{[k,j]}^{(n)}$$

the PAM100 matrix represents 100% change, the PAM250 matrix represents 250% change. They were determined by the global alignment of sequences that differ by less than 85%. One PAM represents a 1% change in all residues or one Point Accepted Mutation per 100 residues