

# Formal methods - ch 05 symbolic CTL model Checking

Francesco Penasa

March 25, 2020

2020 03 24

## 1 Symbolic representation of systems part 2

### 1.1 Symbolic representation of systems

**Symbolic representation** a set of state as their characteristic function (boolean formula). **Example** three state variables  $x_1, x_2, x_3$ : 000, 001, 010, 011 represented as  $\neg x$ .  $\xi(s)$  is the formula representing the state  $s \in S$

### 1.2 Pre-image

The most important slide: the symbolic representation of the pre-image.

Theoretic view:

$$PreImage(P, R) := \{s | \text{forsomes}' \in P, (s, s') \in R\}$$

Logical view:

$$\xi(PreImage(P, R)) := \exists V'. (\xi(P)[V'] \wedge \xi(R)[V, V'])$$

**Symbolic CTL model checking**  $\xi([\phi_i])$  computed directly, without computing  $[\phi_i]$  explicitly!

$$PreImage(X) \rightarrow \exists V'. (X[V'] \wedge \xi(R)[V, V'])$$

$$Check\_EG(X) \rightarrow Y' = Y \wedge PreImage(Y);$$

$$Check\_EU(X_1, X_2) \rightarrow Y' = X_2 \rightarrow Y' = Y \vee (X_1 \wedge PreImage(Y));$$