# Esercizi - 2022-10-10

Business Intelligence per i Servizi Finanziari 2022-2023

Antonio Candelieri

#### Excercise #1

Assume you have invested 100 € on Italy Government bonds. The security has a 4% annual interest rate, a semiannual frequency of payment of interests and a maturity at 5 years.

▶ What is the payoff of the investement at the maturity date?

And what is the profit?

▶ 10 Minutes to solve...



## Excercise #1 - Solution

- Remind the formula for the payoff:  $P_n = P_0 (1+r/m)^{nm}$
- ▶ Data:  $P_0 = 100 \in r = 0.04$ ; m = 2; n = 5
- ► Then, the <u>payoff</u> is:

$$P_{5-years} = P_0 (1 + 0.04 / 2)^{5x2} = 100 \in (1 + 0.02)^{10} = 100 \in (1.02)^{10} = 121.90 \in (1.02)^{10}$$

▶ Then, **profit** is simply the payoff discounted of the principal  $P_0$ :

$$P_{5\text{-vears}} - P_0 = 121.90 \notin -100 \notin = 21.90 \notin$$

#### Excercise #2

- Now, compare the previous investment with the following one:
  - ≥ 200 € on France Government bonds,
  - ▶ 3.6% annual interest rate (instead of 4%),
  - a querterly (instead of semiannual) frequency of payment of interests
  - ▶ and a maturity at 5 years (as in the previous case).
- ▶ Which is the investment with the highest profit?
- ▶ 10 Minutes to solve...



## Excercise #2 - Solution

- ▶ Data:  $P_0 = 200 \in r = 0.036; m = 4; n = 5$
- ▶ Then, the <u>payoff</u> of the investment on French bonds is:

$$P_{5\text{-}vears} = P_0 \; (1 + 0.036 \; / \; 4)^{5 \times 4} = 200 \; \notin \; (\; 1 + 0.009 \;)^{20} = 200 \; \notin \; (1.1962)^{20} = \underline{\textbf{239.25}} \; \in \; (1.1962)^{20} = \underline{\textbf{239$$

While the profit is

$$P_{5-years}$$
 -  $P_0$  = 239.25 € - 200 € = **39.25** €

The profit is higher in this case (39.25 € vs 21.90 €), but be carefull! you need 200 € to invest as principal!

If you have 200 € you could invest twice in italian bonds and obtain 2 x 21.90 € = 43.80 €!!!

## Excercise #3

- Now, assume you have invested in stocks and obtained a profit of 10 € after 1 year
- ► Has this investment a profit higher than 100 € invested on the italian bonds?
- ► And than 200 € invested on the french bonds?
- What if the profit from stocks is 3.50 € in 6 months?
- ▶ 10 Minutes to solve...



## Excercise #3 - Solution

- ▶ Remind the formula for continuous compounding, that is  $P_{\tau} = P_0 e^{r \tau}$
- Data:

$$P_0^{IT} = 100$$
 €;  $r^{IT} = 0.04$ ;  $\tau = 1$   
 $P_0^{FR} = 200$  €;  $r^{FR} = 0.036$ ;  $\tau = 1$   
stocks profit after 1 year 10 €

► Then, the continuously compounded **profits** for bonds are:

$$P_{1y}^{IT} - P_0^{IT} = 100$$
 €  $e^{0.04 \times 1} - 100$  €  $= 4.08$  €  $P_{1y}^{FR} - P_0^{FR} = 200$  €  $e^{0.036 \times 1} - 200$  €  $= 7.33$  €

We have not information about the investment for buying the stocks, but looking only at the profits, the highest one is provided by stocks

## Excercise #3 - Solution

Data:

$$P_0^{IT} = 100 \; \text{\ensuremath{\notin}}; \; r^{IT} = 0.04; \; \underline{\tau = 1/2}$$
 $P_0^{FR} = 200 \; \text{\ensuremath{\notin}}; \; r^{FR} = 0.036; \; \underline{\tau = 1/2}$ 
stocks profit after 6 months 3.5 \ensuremath{\infty}

► Then, the continuously compounded **profits** for bonds are:

$$P_{1y}^{IT} - P_0^{IT} = 100$$
 €  $e^{0.04 \times 0.5} - 100$  €  $= 2.02$  €  $P_{1y}^{FR} - P_0^{FR} = 200$  €  $e^{0.036 \times 0.5} - 200$  €  $= 3.63$  €

Looking only at the profits, the highest one, in this case, is provided by french bonds.

Remind that, having 200 € to invest in french bonds means that you could invest twice in italian bonds, obtaining a profit of 4.04 € at 6 months, that is higher that 3.5 €