

```
> de:=diff(M(t), t)=r*M(t)-P;
r:=0.06;
```

$$de := \frac{d}{dt} M(t) = 0.06 M(t) - P$$

$$r := 0.06$$

(1)

```
> sol:=dsolve( {de, M(0)=500000}, M(t));
```

$$sol := M(t) = \frac{50 P}{3} + e^{\frac{3t}{50}} \left(500000 - \frac{50 P}{3} \right)$$

(2)

```
> eq:=eval(rhs(sol), t=30.0) =0;
```

$$eq := -84.16079103 P + 3.024823732 \times 10^6 = 0$$

(3)

```
> annualpayment := solve(eq, P);
```

$$annualpayment := 35941.00881$$

(4)

```
> r:=0.06/365;
```

```
P:=35941.00881/12;
```

$$r := 0.0001643835616$$

$$P := 2995.084068$$

(5)

```
> dayspermonth:=[31,28,31,30,31,30,31,31,30,31,30,31];
```

$$dayspermonth := [31, 28, 31, 30, 31, 30, 31, 31, 30, 31, 30, 31]$$

(6)

```
> M:=500000;
```

```
for y to 30 do
```

```
for m in dayspermonth do
```

```
for d to m do M:= M + r*M; od:
```

```
M:=M-P;
```

```
od;
```

```
od:
```

```
M;
```

$$M := 500000$$

$$7005.001342$$

(7)

```
> M:=500000;
```

```
for y to 30 do
```

```
for m in dayspermonth do
```

```
for d to m do
```

```
M:=M + r*M;
```

```
if d=15 then M:= M-P; fi;
```

```
od:
```

```
od;
```

```
od:
```

```
M;
```

$$M := 500000$$

$$-648.9168967$$

(8)

```
>
```

```
> with(plots):
```

```
M := 500000:
```

```
r := 0.06/365:
```

```
P := 35941.00881/12:
```

```
dayspermonth := [31,28,31,30,31,30,31,31,30,31,30,31]:
```

```
pts := [[0,M]]:
```

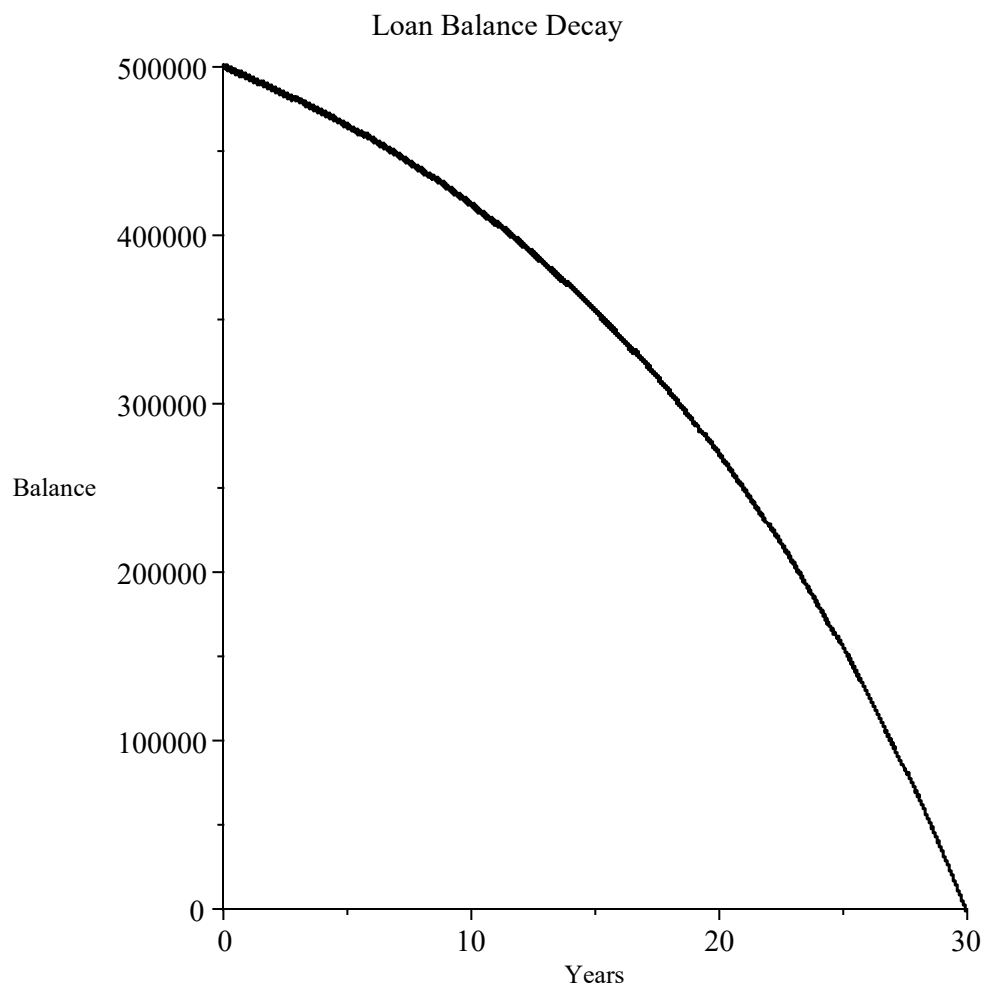
```

t := 0:

for y to 30 do
  for m in dayspermonth do
    for d to m do
      M := M + r*M;
      if d=15 then
        M := M - P;
      end if;
      t := t+1;
      pts := [op(pts), [t/365., M]]; |
    end do;
  end do;
end do:

listplot(pts, labels=["Years","Balance"], title="Loan Balance Decay");

```



>