

4. By Euler's formula :

$$i = \underbrace{\cos\left(\frac{\pi}{2}\right)}_0 + i \underbrace{\sin\left(\frac{\pi}{2}\right)}_{i \cdot 1} = e^{i\frac{\pi}{2}}$$

$$\Rightarrow i = e^{i\frac{\pi}{2}}, \quad i^i = \left(e^{i\frac{\pi}{2}}\right)^i = e^{-\pi/2}$$

$$\text{then } i^i = e^{-\pi/2} \text{ is real! (crazy!) } \quad i^i = \frac{1}{e^{\pi/2}}$$