

$$9. \sin(t) \cos(t) = \frac{\sin(2t)}{2}$$

$$p = \frac{2\pi}{L} = \pi$$

$$\text{General form of Fourier Series: } A_0 + \sum_{n=1}^{\infty} \left(A_n \cos\left(\frac{2\pi nx}{p}\right) + B_n \sin\left(\frac{2\pi nx}{p}\right) \right)$$

$$\text{let } A_0 = 0 = A_n \forall n. \quad \text{let } B_1 = \frac{1}{2}, \quad B_n = 0 \quad \forall n, n > 1$$

$$p = \pi$$

$$\text{then } \sin(t) \cos(t) = B_1 \cdot \sin(2t) = \frac{1}{2} \sin(2t) \checkmark$$

Fourier series for $\cos(t) \sin(t)$