>
$$bn := \frac{1}{int\left(\sin^2\left(\frac{n \cdot \text{Pi} \cdot x}{L}\right), x = 0 ... L\right)} \left(int\left(\frac{2 \cdot M \cdot x}{L} \cdot \sin\left(\frac{n \cdot \text{Pi} \cdot x}{L}\right), x = 0 ... \frac{L}{2}\right) + int\left(\frac{2 \cdot M \cdot (L - x)}{L} \cdot \sin\left(\frac{n \cdot \text{Pi} \cdot x}{L}\right), x = \frac{L}{2} ... L\right)\right) \text{assuming}(L > 0, n, integer) :$$

> $bn := simplify(bn)$

 $\rightarrow bn := simplify(bn)$

$$bn := \frac{8 M \sin\left(\frac{n\pi}{2}\right)}{n^2 \pi^2} \tag{1}$$

$$\Rightarrow$$
 phi := $\sin\left(\frac{n \cdot \text{Pi} \cdot x}{L}\right)$

$$\phi := \sin\left(\frac{n\,\pi\,x}{L}\right) \tag{2}$$

- $psum := subs(M=1, L=10, sum(bn \cdot phi, n=1..100))$:
- plot(psum, x = 0..10):
- with(plots):
- $psum := subs \left(M = 1, L = 10, sum \left(bn \cdot \sin \left(\frac{n \cdot \text{Pi} \cdot x}{L} \right) \cdot \cos \left(\frac{n \cdot \text{Pi} \cdot t}{L} \right), n = 1..200 \right) \right) :$
- \rightarrow animate(psum, x = 0..10, t = 0..20):
 - $curves := [seq(subs(t=2\cdot m, psum), m=0..10)]:$
- > plot(curves, x = 0..10, thickness = [1, 2, 3, 4, 5], color = blue)

