2.
$$\frac{\partial^2 u}{\partial t^2} = c^2 \frac{\partial^2 u}{\partial x^2}$$
 for $u(x,t) = \chi(x,T(t))$

$$X_{11}-X_{12}=X_{11}-(-\nu_{5})X=X_{11}+\nu_{5}X=0$$

Let
$$\chi(x) = a \sin(ux) + b \cos(ux)$$

$$X'(x) = a u cos(ux) - b u sin(ux)$$

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$$X_{11}(x) = a n cos(nx) - p ns cos(nx) =$$

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$$x'''(x) = -\alpha \nu^2 \sin(\nu x) + \beta \cos(\nu x) = -\nu^2 \chi(x)$$

...
$$\chi(x) = a xin (\mu x) + b coo(\mu x) u notation.$$

Checking boundary Conditions of

$$y(0,t) = \chi(0) = 0 = a \sin(0) + b \cos(0) = 0 = b \cdot 1 = 0 = b$$
 $y(0,t) = \lambda \sin(\mu x)$
 $y(x) = a \sin(\mu x)$

(a) · Soy Principle of superposition, we have the family of Solutions .

Solutions.
$$U_{N}(x,t) = \sum_{n=1}^{\infty} \sin\left(\frac{n \cdot T}{L} \cdot x\right) \cdot b_{N} \cos\left(\frac{n \cdot T}{L} \cdot t\right)$$

with period on to p= 2th-L = 2L and

common period 2L.

For
$$T \subset f(x) = u(x, 0) = \sum_{n=1}^{\infty} b_n \sin(\frac{n \cdot \pi}{r} \cdot x)$$

$$f(x) = \begin{cases} \frac{2H}{L} \cdot x & \text{if } 0 < x < \frac{L}{2} \\ \frac{2M}{L} (L-x) & \text{if } \frac{L}{2} < x < \frac{L}{2} \end{cases}$$

$$b_n = \int_0^{1/2} \frac{2M \cdot \chi}{L} \cdot \sin\left(\frac{n \cdot \pi}{L} \cdot \chi\right) d\chi + \int_{-\frac{1}{2}}^{\frac{1}{2}} \frac{2M \left(L - \chi\right) \sin\left(\frac{n \cdot \pi}{L} \cdot \chi\right) d\chi}{L}$$

by using Maple, we arrive to:
$$bn = 8. M \sin \left(\frac{n\pi}{2}\right) \quad assumins \ h>0 \ , \ n, integer$$

of our great robution is of
$$(n \cdot T \cdot x) \cdot \cos(n \cdot T \cdot t)$$

$$u_n(x,t) = \sum_{n=1}^{8} \frac{8 \cdot M \cdot \sin(n \cdot T)}{(\pi n)^2} \cdot \sin(n \cdot T \cdot x) \cdot \cos(n \cdot T \cdot t)$$

$$2 \cdot \frac{1}{\pi n} \cdot \frac{1$$

of period in t,
$$p = \frac{2\pi}{n \cdot T} \cdot L = \frac{2L}{n}$$