

2.(a)

$\sin(x)$

By Euler's formula : $e^{ix} = \cos(x) + i \sin(x)$
 $e^{-ix} = \cos(x) - i \sin(x)$

$$\begin{aligned}\Rightarrow e^{ix} - e^{-ix} &= \cancel{\cos(x)} + i \sin(x) - \cancel{\cos(x)} + i \sin(x) \\ e^{ix} - e^{-ix} &= 2 \cdot i \cdot \sin(x) \\ \sin(x) &= \frac{e^{ix} - e^{-ix}}{2 \cdot i}\end{aligned}$$

$$\text{Since } \frac{1}{i} = \frac{1}{i} \cdot \frac{i}{i} = \frac{i}{-1} = -i$$

$$\therefore \sin(x) = -i \cdot \left(\frac{e^{ix} - e^{-ix}}{2} \right)$$

2.b

$$\begin{aligned}e^{ix} + e^{-ix} &= \cos(x) + i \cancel{\sin(x)} + \cos(x) - i \cancel{\sin(x)} \\ &= 2 \cos(x)\end{aligned}$$

$$\therefore \cos(x) = \frac{e^{ix} + e^{-ix}}{2}$$