## Francisco Moyet Vargas Final Exam ISE 560

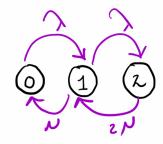
## Problem 1

(a)

The state space  $S=\{0,1,2\}$ .

(b)

Let  $\{X(t), t \ge 0\}$  . X: # of calls in the system



(c)

$$R = \begin{cases} i|j & 0 & 1 & 2 \\ 0 & 0 & \lambda & 0 \\ 1 & \mu & 0 & \lambda \\ 2 & 0 & 2\mu & 0 \end{cases}$$

(d)

Arrival rate $\lambda$ and Service rate $\mu$	Values of $r_i = \Sigma_{j=0}^2 r_{i,j}$	System of Equations
$\lambda = \frac{9}{hr}; \mu = \frac{5}{hr}$	$r_0 = \lambda = 9$ $r_1 = \mu + \lambda = 14$ $r_2 = 2\mu = 10$	$p_{0} + p_{1} + p_{2} = 1$ $p_{0}r_{0} = p_{1}\mu$ $p_{1}r_{1} = p_{0}\lambda + p_{2}2\mu$ $p_{2}r_{2} = p_{1}\lambda$

Using MATLAB to compute the steady state probabilities for state 0,1,and 2:

 $p_0 = 0.2262$ 

 $p_1 = 0.4072$ 

 $p_2 = 0.3665$ 

## Code:

```
lambda=9;
mu=5;
B=[1;0;0]
A = [1,1,1;lambda,-mu,0;-lambda,(mu+lambda),-2*mu]
p=A\B|
```

- (e) Utilization of the 2 technicians is 0.57. That means, we are using 57% of the system capacity.
- (f) The probability that both technicians are idle is P0=0.226.
- (g) The probability that a caller receives a busy signal is the same as the probability of both technicians busy = 0.367.

Then the probability that both technicians are busy at 12:00 pm the same day is 0.3665 Code attached after exercise (i).

(i) The long run expected number of calls in the system is L = 1.14 calls.