

#### Problem A. Alien Sunset

Source file name: alien.c, alien.cpp, alien.java, alien.py

Input: Standard Output: Standard

Following tremendous advances in space flight control software and equally impressive innovations in reality TV crowdfunding, humans have successfully settled a number of planets, moons, asteroids, and various other kinds of funny-shaped rocks across our solar system.

To celebrate, the Galactic President has elected to create a new holiday called "Solar Night". At the crux of the event, she decrees, every settlement will simultaneously launch colourful fireworks into the darkness of night.



Twitter: @RedProgramacion

Night, like most things, is a difficult problem in space. Every spacebound object has its own day length and period of rotation. Thankfully all of the settlements did, at least, start their clocks at the same moment. Settlements may have started in daylight or darkness and so it is possible that the first recorded sunrise can be either before or after the first hour of sunset.

By convention, the President's term lasts for exactly 1825 days as measured by the planet with the longest period of rotation. The celebration needs to happen within that time or it will not serve its intended purpose.

Determine how many hours must pass for us to find a suitable time to celebrate Solar Night.

#### Input

- One line containing the integer N ( $1 \le N \le 20$ ), the number of settlements.
- N lines, each containing three integers:
  - -H ( $2 \le H \le 100$ ), the number of hours in this settlement's solar day.
  - -R and T ( $0 \le R, T \le H-1, R \ne T$ ), the hours of sunrise and sunset respectively.

At sunrise and sunset, a settlement is in darkness. At times strictly in between sunrise and sunset, a settlement is in daylight.

## Output

Output the number of hours that must pass from when the settlement clocks began until each settlement is in darkness. If no suitable time occurs in the first 1825 days, output impossible.



Input	Output
2	6
24 7 19	
24 18 6	
3	12
10 8 2	
15 5 10	
20 15 10	
2	impossible
6 4 2	
12 7 5	
2	5
10 5 6	
10 6 5	



## Problem B. Breaking Biscuits

Source file name: biscuits.cp, biscuits.java, biscuits.py

Input: Standard Output: Standard

This year, Walter's workplace resolved to try something radically different: they're going to change the weekly order of biscuits for the break room to a whole other brand.

Biscuits come in many shapes and sizes, but the particular brand they settled on has two special qualities:

- It is completely planar (two-dimensional);
- It is perfectly polygon-shaped.

However, disaster struck immediately: the available mugs in the break room are too narrow for Walter to be able to dunk these new biscuits into, no matter what combination of rotations along the three axes he tries.

There is only one thing for it: Walter will need to order another mug.

Before taking this drastic step, it is vital to know how wide the diameter of this mug will need to be in order to successfully accommodate a (possibly rotated) biscuit of the new brand.

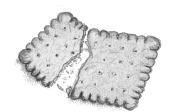
#### Input

- One line containing an integer N ( $3 \le N \le 100$ ), the number of vertices in the biscuit.
- Each of the following N lines contains two space-separated integers  $X_i$  and  $Y_i$  ( $-10^5 \le X_i, Y_i \le 10^5$ ), the coordinates of the *i*-th vertex.

Vertices are always given in anti-clockwise order. Also, as anyone can tell you, biscuits never self-intersect and always have positive area.

## Output

Output the minimum possible diameter of the new mug, in order that it can fit the new kind of biscuit fully inside in at least one orientation. The output must be accurate to an absolute or relative error of at most  $10^{-6}$ .



Twitter: @RedProgramacion



Input	Output
4	2.0
0 0	
5 0	
5 2	
0 2	
6	1224.7089450046291
81444 14017	
80944 13517	
81127 12834	
81810 12651	
82310 13151	
82127 13834	
8	28.816782
197 239	
208 246	
221 241	
250 254	
220 265	
211 258	
198 268	
163 256	



#### Problem C. Cued In

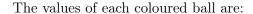
Source file name: cued.c, cued.cpp, cued.java, cued.py

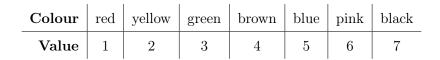
Input: Standard Output: Standard

Snooker is a cue sport played by two players on a rectangular table. The players take turns to pot a series of balls of varying colours, where each colour represents a distinct point value for potting the ball.

A player may pot any ball on the table initially, however any subsequent shots must follow a pattern: if the previous ball was red, the next ball must be another colour; otherwise, if there are still red balls left, the next ball must be red.

Balls of any colour other than red are initially replaced on the table every time they are potted, and may be used again to score more points. The balls stop being replaced once all of the red balls have been potted.





Snooker players are respected universally for their prowess in mental arithmetic. One sweeping glance across the table is enough to tell an experienced contestant how much they could score.

For newer players, however, this is a challenge. Write a program to help calculate a score for a given list of balls remaining on the table.

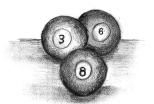
#### Input

- one line containing the integers N ( $1 \le N \le 21$ ), the number of balls remaining on the table.
- N further lines, each containing the colour of one of the balls on the table.

The list of balls will not be ordered in any way and will contain at most one of each of yellow, green, brown, blue, pink and black.

## Output

Output the largest possible score the player can make.



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Input	Output
5	37
red	
black	
pink	
red	
red	
3	18
blue	
black	
pink	
8	34
yellow	
green	
brown	
red	
2	1
red	
red	



## Problem D. Deranging Hat

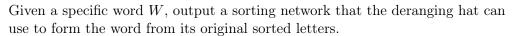
Source file name: deranging.c, deranging.cpp, deranging.java, deranging.py

Input: Standard Output: Standard

In the wizarding world of security, there are two kinds of researcher: the idealist arranging hat and the mercenary deranging hat.

As we learned last year, an arranging hat carefully sorts out any list of letters given to it into ascending order. However, a deranging hat performs the exact opposite function: putting a sorted string of letters back into its original order.

The tool of choice for today's discerning headwear is a sorting network: a sequence of instructions represented by a list of pairs of numbers  $A_i$  and  $B_i$ , meaning that if at step i the A-th item in the string is not already smaller than the B-th item, they should be swapped immediately.





#### Input

One line containing one string of lowercase Latin letters ('a'-'z'), S, containing at most 1000 characters.

## Output

Output at most 10000 lines, each containing two integers  $A_i$  and  $B_i$  ( $1 \le A_i, B_i \le |S|$ ) giving the *i*-th operation to perform.

Input	Output
bab	2 1
dude	4 3
	3 2



#### Problem E. Education

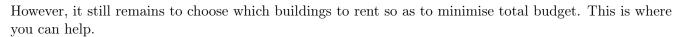
Source file name: education.cpp, education.java, education.py

Input: Standard Output: Standard

Seeking to cash in on the lucrative private education business, EduCorp recently established the prestigious "Bootcamp Academy of Economics" and, counter to their early projections, is growing rapidly.

So rapidly, in fact, that the student body is already overflowing the small (but prestigious) campus building and now needs to be contained somewhere else while more new (and prestigious) buildings are built.

Each department will sell off its original space and then move into its own new rented building. As departments are deeply territorial, buildings must not be shared. Because this is an economics academy, the capacities and rents of each of all the local available buildings were easy to find by disguising the task as homework.



## Input

- one line containing the integers n and m ( $1 \le n \le m \le 5000$ ), the number of departments and buildings respectively.
- one line containing n integers  $s_1 \dots s_n$  ( $1 \le s_i \le 1000$  for each i), where  $s_i$  is the number of students in department i.
- one line containing m integers  $p_1 \dots p_m$   $(1 \le p_i \le 1000 \text{ for each } i)$ , where  $p_i$  is the capacity of building i.
- one line containing m integers  $r_1 \dots r_m$   $(1 \le r_i \le 1000 \text{ for each } i)$ , where  $r_i$  is the yearly rental cost of building i.

## Output

If it is not possible to rent enough buildings for all the departments, output impossible.

Otherwise, output n unique, space-separated integers  $v_1 \dots v_n$ , where the i-th number is the building to be rented by the i-th department so as to minimise the total spend on rent. If there are multiple equally good answers, you may print any.





Input	Output
2 5	2 3
40 200	
1000 199 201 10 50	
600 300 400 200 800	
3 5	5 3 1
10 20 30	
30 25 20 15 10	
30 25 20 15 10	
1 1	impossible
20	
10	
1	



## Problem F. Flipping Coins

Source file name: flipping.c, flipping.cpp, flipping.java, flipping.py

Input: Standard Output: Standard

Here's a jolly and simple game: line up a row of N identical coins, all with the heads facing down onto the table and the tails upwards, and for exactly K times take one of the coins, toss it into the air, and replace it as it lands either heads-up or heads-down. You may keep all of the coins that are face-up by the end.

Being, as we established last year, a ruthless capitalist, you have resolved to play optimally to win as many coins as you can. Across all possible combinations of strategies and results, what is the maximum expected (mean average) amount you can win by playing optimally?



#### Input

- One line containing two space-separated integers:
  - -N ( $1 \le N \le 400$ ), the number of coins at your mercy;
  - -K ( $1 \le K \le 400$ ), the number of flips you must perform.

#### Output

Output the expected number of heads you could have at the end, as a real number. The output must be accurate to an absolute or relative error of at most  $10^{-6}$ .

Input	Output
2 1	0.5
2 2	1
2 3	1.25
6 10	4.63476563
6 300	5.5



## Problem G. GentleBots

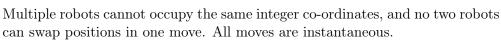
Source file name: gentlebots.c, gentlebots.cpp, gentlebots.java, gentlebots.py

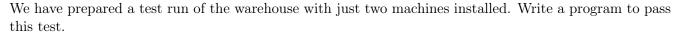
Input: Standard Output: Standard

Rainforest Inc. is opening a large new automated warehouse in the far Northern reaches of the UK—some place they call "Walthamstow".

The robotic worker drones inside will operate in not just one or two, but three dimensions, and can move in any one of the 6 cardinal dimensions in steps of 1 metre at a time. For example, a robot looking to move from position  $(X_1,Y_1,Z_1)$  to position  $(X_2,Y_2,Z_2)$  will, assuming no obstacles, need to take  $(|X_2-X_1|+|Y_2-Y_1|+|Z_2-Z_1|)$  steps in total.

Since this warehouse is in Britain, and because every stereotype is true, the robotic denizens are all impeccably polite. When two robots travelling in opposite directions meet, they wordlessly negotiate for one of the robots to step aside somehow so the other can pass.







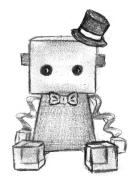
Two lines, one for each robot, each containing six space-separated integers  $(X_0Y_0Z_0)$  and  $(X_\infty Y_\infty Z_\infty)$ , the intended start and end locations of a robot respectively  $(-1000 \le X, Y, Z \le 1000)$ .

The robots will start in different places from each other, and will also end in different places from each other.

## Output

Output up to 7000 lines, giving one possible list of locations of the robots over time. The position of both robots at time T must be given as bracketed space-separated (X, Y, Z) co-ordinate tuples on line T.

Co-ordinates must not exceed an absolute value of  $10^6$ .





Input	Output
0 0 0 2 2 2	(0 0 0) (1 1 2)
1 1 2 0 0 0	(1 0 0) (1 1 1)
	(1 1 0) (0 1 1)
	(1 1 1) (0 1 0)
	(1 1 2) (0 0 0)
	(1 2 2) (0 0 0)
	(2 2 2) (0 0 0)
-2 0 0 1 0 0	(-2 0 0) (3 0 0)
3 0 0 -1 0 0	(-1 0 0) (2 0 0)
	(0 0 0) (1 0 0)
	(1 0 0) (1 0 -1)
	(1 0 0) (0 0 -1)
	(1 0 0) (-1 0 -1)
	(1 0 0) (-1 0 0)
0 0 0 1 0 0	(0 0 0) (1 0 0)
1 0 0 0 0 0	(0 1 0) (0 0 0)
	(1 1 0) (0 0 0)
	(1 0 0) (0 0 0)



## Problem H. Hiker Safety

Source file name: hiker.c, hiker.cpp, hiker.java, hiker.py

Input: Standard Output: Standard

Times are hard at the Association of Chartered Mountaineers.

The growth of their pedestrian sport has slowed to a crawl. Instead of taking up mountaineering, younger potentials are gravitating towards warmer indoor activities such as snooker, musical chairs, and programming contests.

To win over more members, the Association is going to organise a series of new time trial orienteering events next year. The route for the first race will be a short run through the Cairngorms, with every contestant following the same route designated by marker points but all starting at different times.



Because hiking can be dangerous, and many of the contestants will be inexperienced, the competition committee drew up two rules:

- Every contestant needs to keep a specific maximum distance away from the next-closest contestant, in either direction, at all times.
- Every contestant should be given personal space. If a contestant needs a personal space of *D* metres, nobody else should ever come closer than that at any time. This distance varies according to level of experience.

The hardest part of orienteering is the pathfinding; once a contestant knows where to go next, they can get there in almost no time (for the purposes of this problem, instantaneously).

In fact, while the inaugural ACM "Icy-Cold Peak Contest" is already underway, pathfinding is turning out to be a problem: nobody is sure whether they can move next without breaking any of the conditions on minimum and maximum distance.

Help the runners reach the end of their route by computing a list of who should move to the next goal point, and at what time.

## Input

- One line containing an integer B ( $1 \le B \le 50000$ ), the maximum separation allowed between any two runners.
- One line containing an integer P ( $3 \le P \le 1000$ ), the number of marker points along the route.
- One line containing P unique space-separated integers  $d_1 \dots d_P$  i  $(0 \le d_P \le 10^6)$ , with  $d_i$  being the distance of the i-th vertex from the starting point  $d_1 = 0$ .
- One line containing an integer K ( $2 \le K \le 1000$ ), the number of hikers on the landscape.
- K further lines, each containing the pair of space-separated integers  $A_i$  and  $V_i$   $(1 \le A_i \le 10^6; 1 \le V_i \le P)$ , the minimum separation distance and current marker position respectively for the *i*-th person.

The initial configuration of hikers will be legal according to the minimum and maximum distance rules. The hikers will be given in increasing order of distance from the start.



#### Output

If it is not possible to get everyone to the end of the route without breaking minimum or maximum distance requirements, output impossible.

Otherwise, output a space-separated list of moves on one line, each describing which person should make the next move.

If anyone falls off the landscape, your answer will not be judged as correct. However, once someone has arrived at the end of their journey they cease to count towards any rule violations.

Input		
3		
8		
0 1 2 3 4 5 6 7		
2		
2 1		
2 4		
Output		
1 2 1 2 1 2 1 1 1		
Input		
10		
10		
0 1 3 6 10 14 17 19 20 21		
3		
3 1		
1 3		
3 5		
Output		
2 1 1 3 2 1 3 2 1 3 3 2 1 3 2 2 1 2 1 1 1		
Input		
5		
5		
0 2 5 9 14		
2		
2 1		
2 2		
Output		
impossible		



## Problem I. I Work All Day

Source file name: work.c, work.cpp, work.java, work.py

Input: Standard Output: Standard

Michael is a lumberjack, and a pretty OK one at that. However, automation is making fast (if polite) inroads to his business, and he needs to stay ahead to remain competitive.

To this end, he has invented a machine called the *Flannelmaster GTX*. This is a fearsome tree-cutting contraption, powered by logarithms, which swings an axe horizontally from a specified height above the ground. Each impact of its electronic axe cuts the tree cleanly into two parts, the stump rolling away and the remainder of the tree falling down into the same place.

This continues until the remaining height is too small to cut any more, at which point any irregular-sized stump is discarded as waste and the remaining lumber of the same length as the setting is neatly packaged and sold on automatically.

What setting should Michael use for the height in order to minimise loss?



#### Input

- One line containing the integer N ( $2 \le N \le 10$ ), the number of settings;
- One line containing N distinct integers  $H_i$  ( $1 \le H \le 500$ ), the possible settings;
- One line containing the integer T ( $1 \le T \le 3000$ ), the height of the tree.

#### Output

Output the best setting to use so that tree waste will be minimal. If there are multiple settings that yield equally small waste, you may print any one of them.

Input	Output
3	6
5 6 8 103	
103	
4	7
7 3 5 13	
1366	



## Problem J. Just A Minim

Source file name: minim.c, minim.cpp, minim.java, minim.py

Input: Standard Output: Standard

Listening to music is a good way to take one's mind off the monotony of typing out solution after correct solution.

However, it can be very annoying to start listening to a tune and then for time to run out early, cutting the listening short. How much more satisfying it would be if you could choose tunes to fit the time available!

With this in mind, you have found a way to code musical scores into simple lists of numbers representing the length of the notes in each tune as follows:



Code	Name	Length
0	breve	2 notes
1	semibreve	1 notes
2	minim	$\frac{1}{2}$ note
4	crotchet	$\frac{1}{4}$ note
8	quaver	$\frac{1}{8}$ note
16	semiquaver	$\frac{1}{16}$ note

Given such a list of numbers, calculate the length of the tune in notes.

## Input

- One line containing the integer N ( $1 \le N \le 2000$ ), the number of values in the tune.
- ullet one line containing N integers each representing the length of a value using the codes above.

## Output

Output the length of the tune, as a real number of notes. The output must be accurate to an absolute or relative error of at most  $10^{-6}$ .

Input	Output
4	5
1 1 1 0	
10	4.3125
1 2 2 2 1 4 4 8 8 16	



## Problem K. Knightsbridge Rises

Source file name: rises.c, rises.cpp, rises.java, rises.py

Input: Standard Output: Standard

High-rise buildings in the wealthy retail district of Knightsbridge are usually built with exotic hoisting machines known, in construction circles, as *cranes*.

While it is common to mount these devices on the ground, it's not always ideal—for example, a skyscraper building would need an equally tall crane. In these cases, the clever solution the industry has developed is for a smaller crane to be mounted directly on top of the tower.

However, this solution presents another challenge: how can such heavy equipment be brought to the summit in the first place? The industry's solution is to simply use a smaller crane to lift the main crane up. And if that smaller crane is still too massive, find another smaller still, and so on, until said device fits inside a pocket and can be carried up by some enterprising engineer.



Once on top of the building, whether by being carried up, or by being lifted up by another crane capable of holding its weight, a crane can be used to lift others up onto its tower. Once raised, it is not possible to transfer a crane anywhere else.

We have several construction projects in progress at the moment, each with its own requirements on how heavy the loads eventually lifted from the ground need to be. Find an assignment of cranes to buildings that can satisfy these requirements.

## Input

- One line containing an integer N ( $1 \le N \le 100$ ), the number of types of cranes under our command.
- N further lines, each containing a pair of space-separated integers  $W_i$  and  $L_i$  ( $0 \le W_i, L_i \le 10^6$ ), the weight and maximum lifting weight of the *i*-th crane in kilograms.
- One line containing an integer M ( $1 \le M \le 100$ ), the number of tower blocks.
- One line containing the M space-separated integers  $T_i$   $(1 \le T_i \le 10^6)$ ,  $T_i$  being the weight we need to be able to lift from the top of the i-th building by the end.

#### Output

If it is not possible to supply all of the buildings, output impossible.

Otherwise, output M lines. The *i*-th line should contain a list of space-separated integers  $x_1 \dots x_k$   $(1 \le x \le N)$ , describing the order in which cranes should be raised onto the *i*-th building from the input.



Input	Output
5	5 3 4
0 1	1 2
1 2	
2 3	
3 4	
0 2	
2	
4 2	
7	3 5
0 1	1 2
1 4	4 7 6
0 3	
0 1	
2 5	
2 5	
1 2	
3	
5 4 5	
2	impossible
0 1	
5 3	
2	
2 1	



## Problem L. Lounge Lizards

Source file name: lounge.c, lounge.cpp, lounge.java, lounge.py

Input: Standard Output: Standard

Monitor lizards are a kind of reptile known mainly for their cold-bloodedness and addiction to computer screens. Due to their love for digital displays, these scaly creatures spend most of their time at home glued to a small television in the lounge.

Conflict has arisen at one particular reptile house. The audience here has grown so large that not everyone will be able to see the screen at once any more; specifically, a lizard will only be able to see enough if it is strictly taller than all of the lizards sitting exactly along the straight line from itself to the television.



Monitor lizards aren't particularly picky about the actual contents of the screen or being able to see it obliquely (or even from the front)—they just want to be able to keep an eye on it.

The lizards don't want to move, however. It's possible to chase a monitor lizard away in order for the ones behind it to see, or leave it alone, but re-homing somewhere else in the room is unthinkable.

Assuming lizards are removed optimally, how many at most can remain and still see the screen?

## Input

- one line containing the space-separated integers  $T_X$  and  $T_Y$  ( $-10^6 \le T_X, T_Y \le 10^6$ ), the co-ordinates of the television.
- one line containing the integer N ( $1 \le N \le 10^6$ ), the number of lizards.
- N further lines, each containing three space-separated integers  $X_iY_iH_i$   $(-10^6 \le X,Y \le 10^6;1 \le H \le 10^6)$ , the co-ordinates and height respectively of one lizard.

The co-ordinates of all televisions and lizards will be distinct.

## Output

Output the maximum number of lizards that can stay and watch television at once.



Input	Output
50 50	2
2	
60 50 1	
65 50 2	
50 50	2
3	
60 55 1	
70 60 1	
40 45 1	
-100 0	4
6	
-99 1 2	
-98 2 4	
-97 3 3	
-96 4 4	
0 100 3	
100 0 7	