

Final Report

Physics of Complex Networks: Structure and Dynamics



UNIVERSITÀ
DEGLI STUDI
DI PADOVA

Areas of physics by complexity



Newton's
Mechanics

Electro-
Magnetism

Special
Relativity

Quantum Mechanics
General Relativity

Quantum
Field Theory

Complexity
Science

Project # X:

Aquistapace Tagua, Franco

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1 | Song-Havlin-Makse self-similar model

Task leader(s): *Franco Aquistapace Tagua*

1.1 | Introduction and methods

The work by Song, Havlin and Makse [1] aims to explain the characteristic features of empirical scale-free fractal and non-fractal networks by means of a single growth model, that has the concept of renormalisation at its core. More specifically, the growth mechanism works as the inverse of the renormalisation procedure. The goal of this task is then to reproduce their growth and renormalisation procedures, and to recover the characteristic behaviour of fractal and non-fractal networks through relevant descriptors.

The renormalisation of a network was done as described in the source material, by covering its N nodes with $N_B(L_B)$ boxes, where the maximum shortest path between any two nodes in a box must be L_B . This is done algorithmically as follows:

1. Initialise a box with a randomly picked node.
2. For every remaining node i , add it to the box if $\max_{j \in B} d(i, j) \leq L_B$, where B contains the nodes currently in the box, and $d(i, j)$ is the shortest path between nodes i and j .
3. Repeat steps 1. and 2. with the remaining available nodes until all nodes are assigned to a box.

On the opposite hand, when performing the growth process of a network, each existing node is considered as a future hub. For a node with degree k , mk offspring nodes are attached to it at each growth step. Then, each edge between two of the original nodes is removed with probability e , and replaced by an edge between two of their offspring. Thus, parameter e represents hub-hub attraction / repulsion, with $e \rightarrow 1$ being hub-hub attraction, and $e \rightarrow 0$ being hub-hub repulsion.

1.2 | Results and discussion

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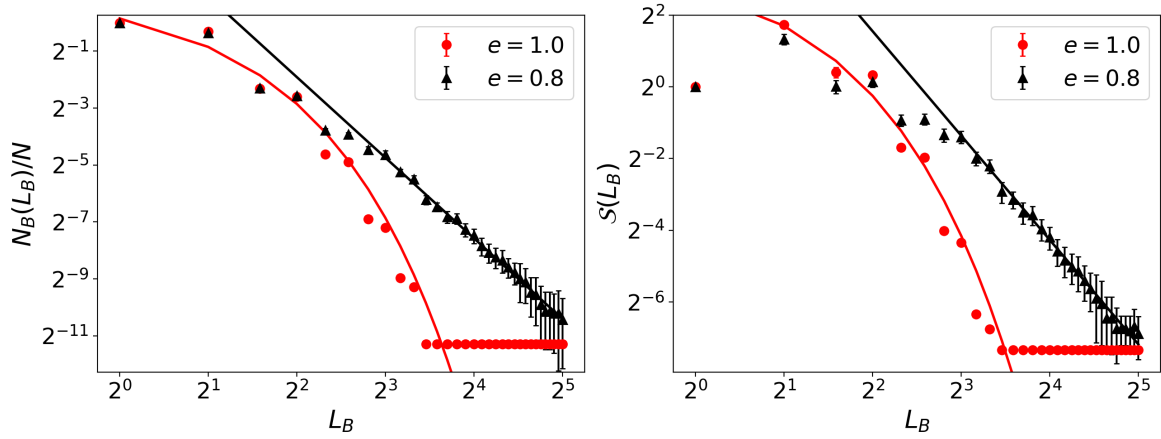


Figure 1.1: Caption.

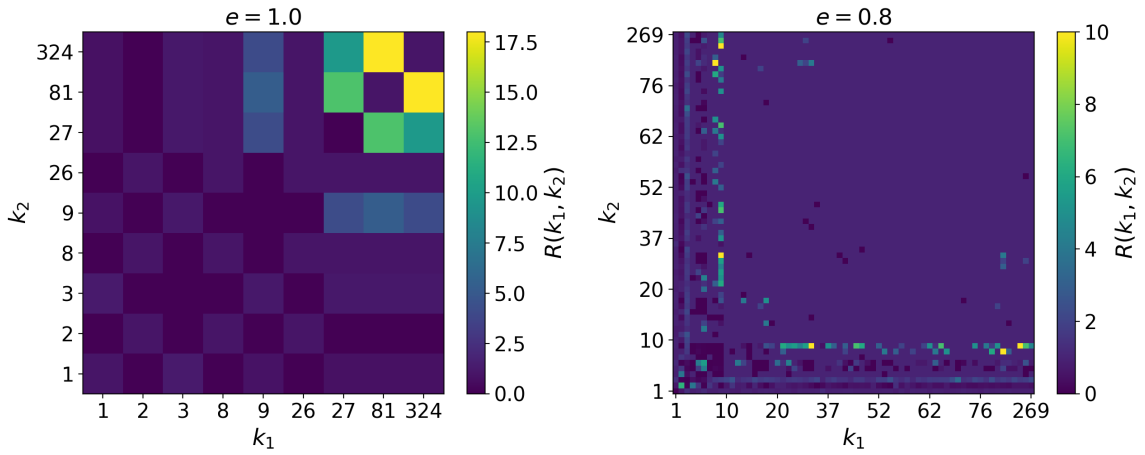


Figure 1.2: Caption.

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2 | Task title...

Task leader(s): *Author name(s)...*

Structure as¹:

- *A short (max 1 page) explanation of the task, including references. Include mathematical concepts.*
- *Max 2 pages for the whole task (including figures)*
- *It is possible to use appendices for supplementary material, at the end of the report. Max 5 pages per task*

A total of 3 pages + 5 supplementary pages per task

2.1 | A section...

Reference examples:

2.2 | Another section...

¹Remove this part from the report

3 | Task title...

Task leader(s): *Author name(s)...*

Structure as¹:

- *A short (max 1 page) explanation of the task, including references. Include mathematical concepts.*
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3.1 | A section...

Reference examples:

3.2 | Another section...

¹Remove this part from the report

4 | Supplementary material

Task leader(s): *Franco Aquistapace Tagua*

4.1 | Song-Havlin-Makse self-similar model

Reference examples:

4.2 | Another section...

5 | Bibliography

- [1] Chaoming Song, Shlomo Havlin, and Hernán A Makse. Origins of fractality in the growth of complex networks. *Nature physics*, 2(4):275–281, 2006.