

Federal University of Santa Catarina
Department of Automation and Systems Engineering
DAS-410047: Introduction to Algorithms

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Mid-Term Exercises – Given Results

```
1  # names: Felipe, Thays and Ivan
2  # Introduction to Algorithms list : Insertion Sort
3
4  import numpy as np
5
6  def insertion_sort(A):
7      for j in range(1, len(A)):
8          key = A[j]
9          i = j-1
10         while i >= 0 and A[i] < key:
11             A[i+1] = A[i]
12             i = i-1
13         A[i+1] = key
14
15
16  if __name__ == '__main__':
17
18      C = np.random.randint(1, 99, 20)
19      print(f'without order')
20      print(C)
21      insertion_sort(C)
22      print(f'ordered')
23      print(C)
```

Insertion Sort Algorithm

```

1  # names: Felipe, Thays and Ivan
2  # Introduction to Algorithms list : Merge Sort
3  import numpy as np
4
5  def merge_sort(A) :
6      B = A
7      if len(B) > 1:
8          mid_point = len(B)//2
9          left = B[:mid_point]
10         right = B[mid_point:]
11         left_2 = merge_sort(left)
12         right_2 = merge_sort(right)
13         B = merge(left_2, right_2)
14
15     return B
16
17 def merge(L,R) :
18     merged = []
19     i=j=0
20     while i<len(L) and j<len(R) :
21         if L[i]<R[j]:
22             merged.append(L[i])
23             i+=1
24         else:
25             merged.append(R[j])
26             j+=1
27
28     if i != len(L) :
29         for element in L[i:]:
30             merged.append(element)
31     else:
32         for element in R[j:]:
33             merged.append(element)
34     return merged
35
36
37 if __name__ == '__main__':
38
39     A = np.random.randint(1, 99, 21).tolist()
40     print(f'without order')
41     print(A)
42     B = merge_sort(A)
43     print(f'ordered')
44     print(B)

```

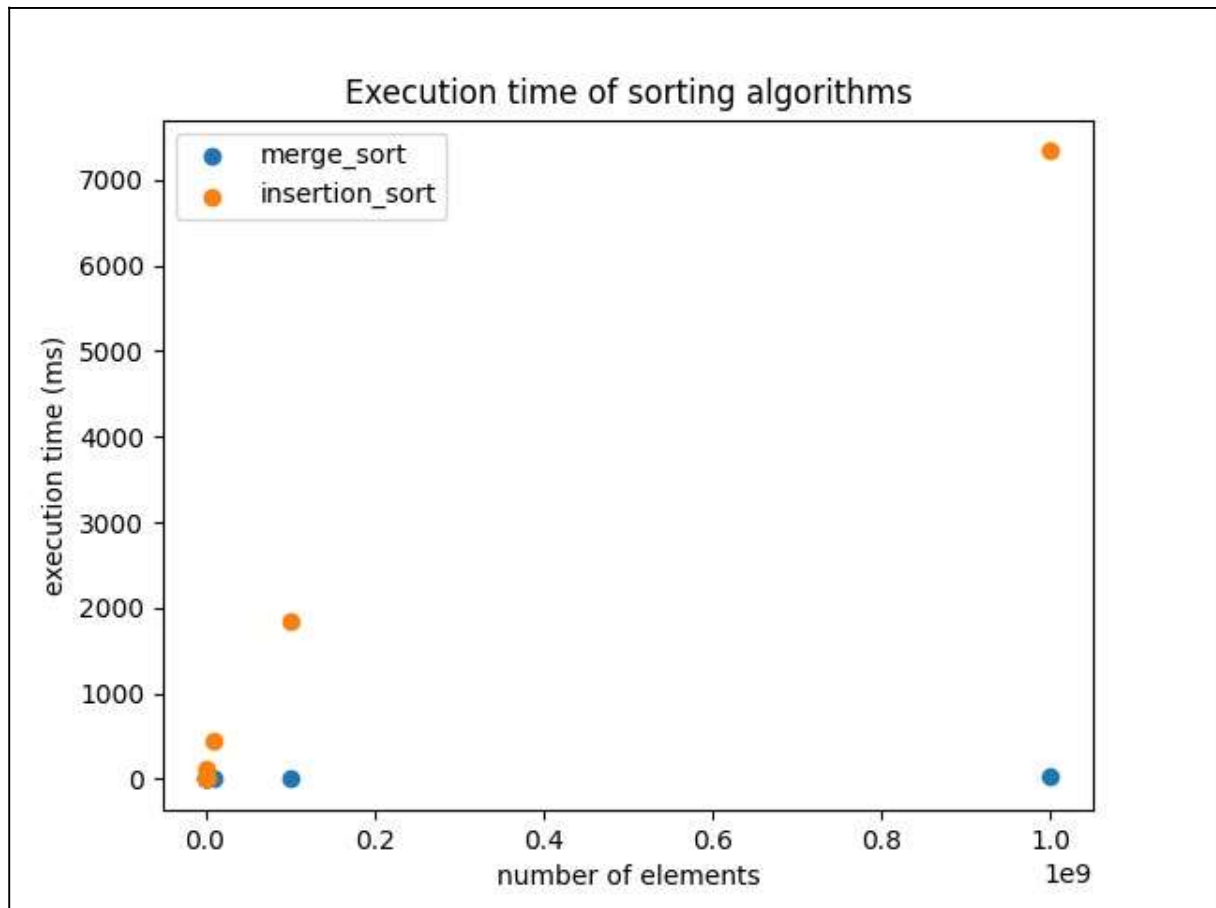
Merge Sort Algorithm

```

49 if __name__ == '__main__':
50
51     exec_time_merge = []
52     exec_time_insertion = []
53     elements = []
54     size_list = 10
55
56     for i in range (10):
57         size_list = size_list*2
58         list_merge = np.random.randint(low=0,high=10**3,size=size_list)
59         start = time.time()
60         merge_sort(list_merge)
61         final = 1000*(time.time() - start)
62         exec_time_merge.append(final)
63         elements.append(10**i)
64
65     size_list = 10
66     for i in range (10):
67         size_list = size_list*2
68         list_insertion = np.random.randint(low=0,high=10**3,size=size_list)
69         start = time.time()
70         insertion_sort(list_insertion)
71         final = 1000*(time.time() - start)
72         exec_time_insertion.append(final)
73         #elements.append(10**i)
74
75     plt.scatter(elements, exec_time_merge, label='merge_sort')
76     plt.scatter(elements, exec_time_insertion, label='insertion_sort')
77     plt.legend(['merge_sort', 'insertion_sort'])
78     plt.ylabel('execution time (ms)')
79     plt.xlabel('number of elements')
80     plt.title('Execution time of sorting algorithms')
81     plt.show()

```

Algorithm for performance comparison using inputs from $n = 20$ to $n = 1 \times 10^9$



Plotting execution time results using Insertion Sort and Merge Sort