

$$\sum_{n=0}^{\infty} x^n = \frac{1}{1-x} \quad x \in (-1, 1)$$

$$\sum_{n=0}^{\infty} \frac{x^n}{n!} = e^x \quad x \in \mathbb{R}$$

$$\sum_{n=0}^{\infty} (-1)^n \frac{x^{2n+1}}{(2n+1)!} = \sin x$$

$$\sum_{n=0}^{\infty} (-1)^n \frac{x^{2n}}{(2n)!} = \cos x$$

$$\frac{1}{1+x} = 1 - x + x^2 - x^3 + \dots = \sum_{n=0}^{\infty} (-1)^n x^n$$

$$\ln(1+x) = x - \frac{x^2}{2} + \frac{x^3}{3} - \frac{x^4}{4} + \dots = \sum_{n=0}^{\infty} (-1)^n \frac{x^{n+1}}{n+1} \quad x \in (-1, 1]$$

$$\oint_{\Sigma} P dy dz + Q dx dz + R dx dy$$

$$= \iint_{\Omega} \left(\frac{\partial P}{\partial x} + \frac{\partial Q}{\partial y} + \frac{\partial R}{\partial z} \right) dx dy dz$$

$$\oint_L P dx + Q dy + R dz = \iint_{\Sigma} \begin{vmatrix} dy dz & dx dz & dx dy \\ \frac{\partial}{\partial x} & \frac{\partial}{\partial y} & \frac{\partial}{\partial z} \\ P & Q & R \end{vmatrix} = \iint_{\Sigma} \begin{vmatrix} \cos \alpha & \cos \beta & \cos \gamma \\ \frac{\partial}{\partial x} & \frac{\partial}{\partial y} & \frac{\partial}{\partial z} \\ P & Q & R \end{vmatrix} d\omega$$

$$\oint_L P dx + Q dy = \iint_{\Sigma} \left(\frac{\partial Q}{\partial x} - \frac{\partial P}{\partial y} \right) dx dy$$

$$\text{点到面: } d = \frac{|Ax_0 + By_0 + Cz_0 + D|}{\sqrt{A^2 + B^2 + C^2}}$$

$$\text{点到线: } d = \frac{|\vec{m} \times \vec{s}|}{|\vec{s}|}$$

$$\frac{x-x_0}{a} = \frac{y-y_0}{b} = \frac{z-z_0}{c}$$



$$\text{线到线: } d = \frac{|\vec{m}_1 \cdot (\vec{s}_1 \times \vec{s}_2)|}{|\vec{s}_1 \times \vec{s}_2|}$$

连续偏导数 \rightarrow 可微 \rightarrow 可偏导

方向导数存在

$$f(x_0 + \Delta x, y_0 + \Delta y) - f(x_0, y_0) = f'_x(x_0, y_0) \Delta x + f'_y(x_0, y_0) \Delta y$$

$$\lim_{\Delta x \rightarrow 0, \Delta y \rightarrow 0}$$

$$\frac{\sqrt{\Delta x^2 + \Delta y^2}}{\rho}$$

$$\Delta z = z_x(x_0, y_0) \Delta x + z_y(x_0, y_0) \Delta y$$

$$y' + p(x)y = f(x)$$

$$y = e^{-\int p(x) dx} (c + \int f(x) e^{\int p(x) dx} dx)$$

$$y'' + p(x)y' + q(x)y = 0.$$

用多项式 / 指数法

$$y_2 = y_1 \int \frac{1}{y_1^2} e^{-\int p(x) dx} dx.$$

$$y'' + py' + qy = P_n(x) e^{\lambda x}.$$

$$\frac{1}{a^2 + x^2} = \left(\frac{1}{a} \arctan \frac{x}{a} \right)'$$

$$\frac{1}{a^2 - x^2} = \frac{1}{2a} \ln \left| \frac{a+x}{a-x} \right|$$

$$\frac{1}{\sqrt{a^2 - x^2}} = \arcsin \frac{x}{a}$$

$$\frac{1}{\sqrt{x^2 \pm a^2}} = \ln |x + \sqrt{x^2 \pm a^2}|$$

$$\tan x \sim -\ln |\cos x|$$

$$\frac{1}{\cos^2 x} \sim \tan x.$$

$$\frac{1}{\sin^2 x} \sim \frac{-1}{\tan x}$$

$$f(x) = \frac{a_0}{2} + \sum_{n=1}^{\infty} (a_n \cos nx + b_n \sin nx)$$

$$a_0 = \int_{-\pi}^{\pi} f(x) dx$$

$$a_n = \frac{1}{\pi} \int_{-\pi}^{\pi} f(x) \cos nx \, dx$$

$$b_n = \frac{1}{\pi} \int_{-\pi}^{\pi} f(x) \sin nx \, dx.$$