DIGITAL DESIGN AND COMPUTER ARCHITECTURE (252-0028-00L), SPRING 2023 OPTIONAL HW 5: BRANCH PREDICTION, VLIW, AND SYSTOLIC ARRAYS

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1 Branch Prediction I

Assume the following piece of code that iterates through a large array populated with **completely (i.e., truly) random** positive integers. The code has four branches (labeled B1, B2, B3, and B4). When we say that a branch is *taken*, we mean that the code *inside* the curly brackets is executed.

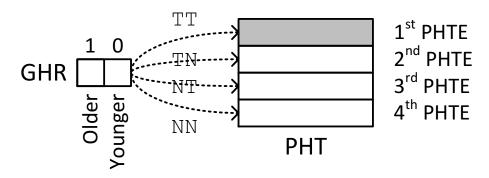
```
for (int i=0; i<N; i++) { /* B1 */
                        /* TAKEN PATH for B1 */
  val = array[i];
  if (val % 2 == 0) {
                        /* B2 */
                      /* TAKEN PATH for B2 */
    sum += val;
  }
  if (val % 3 == 0) { /* B3 */
                      /* TAKEN PATH for B3 */
    sum += val;
  }
  if (val % 6 == 0) {
                       /* B4 */
    sum += val;
                      /* TAKEN PATH for B4 */
  }
}
```

(a) Of the four branches, list all those that exhibit *local correlation*, if any.

(b) Which of the four branches are *globally correlated*, if any? Explain in less than 20 words.

Now assume that the above piece of code is running on a processor that has a global branch predictor. The global branch predictor has the following characteristics.

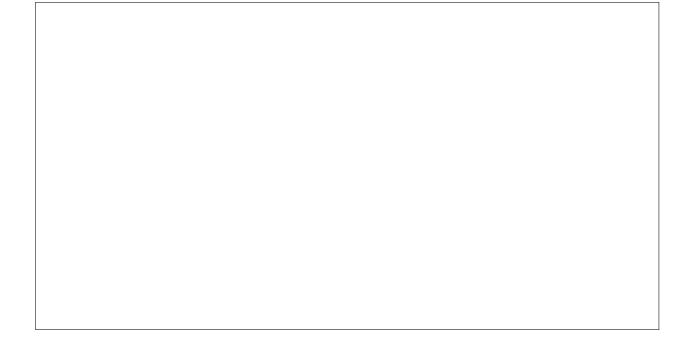
- Global history register (GHR): 2 bits.
- Pattern history table (PHT): 4 entries.
- Pattern history table entry (PHTE): 11-bit signed saturating counter (possible values: -1024-1023)
- Before the code is run, all PHTEs are initially set to 0.
- As the code is being run, a PHTE is incremented (by one) whenever a branch that corresponds to that PHTE is taken, whereas a PHTE is decremented (by one) whenever a branch that corresponds to that PHTE is not taken.



(c) After 120 iterations of the loop, calculate the **expected** value for only the first PHTE and fill it in the shaded box below. (Please write it as a base-10 value, rounded to the nearest one's digit.)

Hint. For a given iteration of the loop, first consider, what is the probability that both B1 and B2 are taken? Given that they are, what is the probability that B3 will increment or decrement the PHTE? Then consider...

Show your work.



2 Branch Prediction II

Assume a machine with a two-bit global history register (GHR) shared by all branches, which starts with Not Taken, Not Taken (2'b00). Each pattern history table entry (PHTE) contains a 2-bit saturating counter. The saturating counter values are as follows:

- 00 Strongly Not Taken
- 01 Weakly Not Taken

Show your work here.

- 10 Weakly Taken
- 11 Strongly Taken

Assume the following piece of code runs on this machine. The code has two branches (labeled B1 and B2). When we say that a branch is taken, we mean that the code inside the curly brackets is executed. For the following questions, assume that this is the only block of code that will ever be run, and the loop-condition branch (B1) is resolved first in the iteration before the if-condition branch (B2).

(a) Is it possible to observe that the branch predictor mispredicts 100% of the time in the first 5 iterations of the loop? If yes, fill in the table below with all possible initial values each entry can take. We represent Not Taken with N, and Taken with T.

Table 1: PHT

PHT Entry	Value
TT	
TN	
NT	
NN	

(b)	At steady-state, we observe the following pattern which repeats over time: TTTNTN, with T representing Taken, and N representing Not Taken. When GHR pattern equals to NT or TT, the predictor will observe that the branch outcome will be either T or N. Therefore, no matter what the initial values for these two entries are in the pattern history table (PHT), only one of the branches can be predicted correctly. Thus prediction accuracy will never reach 100%. Explain how using local history registers instead of the global history register will help bring the prediction accuracy up to 100% during the steady state, by showing what will each PHTE saturate to.				

3 Branch Prediction III

A processor implements an *in-order* pipeline with multiple stages. Each stage completes in a single cycle. The pipeline stalls upon fetching a conditional branch instruction and resumes execution once the condition of the branch is evaluated. There is no other case in which the pipeline stalls.

3.1 Part I: Microbenchmarking

You create a microbenchmark as follows to explore the pipeline characteristics:

The microbenchmark takes one input value R1 and runs until it is killed (e.g., via an external interrupt).

You carefully run the microbenchmark using three different input values as summarized in Table 2. You terminate the microbenchmark using an external interrupt such that each run is guaranteed to execute the same number of *dynamic instructions*. Unfortunately, your testing infrastructure does *not* give you the actual number of instructions executed.

Initial R1 Value	Number of Cycles Taken
4	51
8	63
16	87

Table 2: Microbenchmark results.

Using this information, you need to determine the following three experiment characteristics. Clearly show all work to receive full points!

- 1. How many dynamic instructions are executed?
- 2. How many stages are in the pipeline?
- 3. For how many cycles does a conditional branch instruction cause a stall?

3.2 Part II: Performance Enhancement

To improve performance, the architects add a *mystery* branch prediction mechanism. They keep the rest of the design exactly the same as before. You re-run the microbenchmark for the same number of total dynamic instructions with the new design, and you find that with R1 = 4, the microbenchmark executes in 48 cycles.

Based on this given information, determine which of the following branch prediction mechanisms could be the *mystery* branch predictor implemented in the new version of the processor. For each branch prediction mechanism below, you should circle the configuration parameters that makes it match the performance of the mystery branch predictor.

(a)	Static Branch Predictor Could this be the mystery branch predictor: YES NO If YES, for which configuration below is the answer YES? Pick an option for each configuration parameter. I) Static Prediction Direction				
	Always taken	Always not taken			
	Explain:				
(b)	Last Time Branch Pred Could this be the mystery b				
	YES	NO			
	If YES, for which configura	tion is the answer YES ? Pick an option for each configuration parameter.			
	I) Initial Prediction Direction	etion			
	Taken	Not taken			
	II) Local for each branch	instruction (PC-based) or global (shared among all branches) history?			
	Local	Global			
	Explain:				

YES		NO	
Expl	lain:		
Forv	ward taken, Bac	ckwards not t	taken (FTBN)
Coul	ld this be the mys	tery branch pr	redictor?
YES		NO	
Expl	lain:		
Coul	o-bit Counter Ba	tery branch pr	ion (using saturating arithmetic) redictor?
			,
Coul	ld this be the mys	tery branch pr NO	,
Coul	ld this be the mys	tery branch pr NO figuration is the	redictor?
Coul	ld this be the mys ES, for which conf	NO figuration is the Direction ot taken)	redictor?
Could YES If YI I)	ES, for which conf Initial Prediction 00 (Strongly no 10 (Weakly take	NO figuration is the Direction ot taken) en)	edictor? e answer YES ? Pick an option for each configuration parameter. O1 (Weakly not taken)
Could YES If YI I)	ES, for which conf Initial Prediction 00 (Strongly no 10 (Weakly take	NO figuration is the Direction ot taken) en)	e answer YES? Pick an option for each configuration parameter. 01 (Weakly not taken) 11 (Strongly taken) ion (i.e., PC-based, without any interference between different

4 Branch Prediction IV

Consider the following high level language code segment:

```
int array[1000] = { /* random values */ };
int sum1 = 0, sum2 = 0, sum3 = 0, sum4 = 0;
for (i = 0; i < 1000; i ++)
                               // Branch 1: Loop Branch
    // Branch 1: Taken
    if (i % 2 == 0)
                                // Branch 2: If Condition 1
        // Branch 2: Taken
        if (i \% 3 == 0)
                                // Branch 3: If Condition 2
            sum1 += array[i];
                                // Branch 3: Taken
        else
            sum2 += array[i];
    else
        if (i \% 4 == 0)
                                // Branch 4: If Condition 3
                                // Branch 4: Taken
            sum3 += array[i];
        else
            sum4 += array[i];
}
```

(a) What is the prediction accuracy for each of the four branches using a per-branch last-time predictor (assume that every per-branch counter starts at "not-taken")? Please show all of your work.

Branch 1:



Branch 2:

Branch 3:
Branch 4:
What is the prediction accuracy for each of the four branches when a per-branch 2-bit saturating counter-based predictor is used (assume that every per-branch counter starts at "strongly not-taken")? Please show all of your work. Branch 1:
Branch 2:

(b)

Branch 3:	
Branch 4:	
Branch 2 (i):	nd (ii) "weakly taken"?
Branch 2 (ii):	

Branch 3 (i):		
Branch 3 (ii):		

5 VLIW I

Explain the motivation for VLIW in one sentence.						

You are the human compiler for a VLIW machine whose specifications are as follows:

- There are 3 fully pipelined functional units (ALU, MU and FPU).
- Integer Arithmetic Logic Unit (ALU) has a 1-cycle latency.
- Memory Unit (MU) has a 2-cycle latency.
- Floating Point Unit (FPU) has a 3-cycle latency, and can perform either FADD or FMUL (floating point add / floating point multiply) on floating point registers.
- This machine has **only** 4 integer registers (r1 .. r4) and 4 floating point registers (f1 .. f4)
- The machine does not implement hardware interlocking or data forwarding.
- (a) For the given assembly code on the next page, fill **Table 3** (on the next page) with the appropriate VLIW instructions for only one iteration of the loop (The C code is also provided for your reference). Provide the VLIW instructions that lead to the **best** performance. Use the minimum number of VLIW instructions. Table 3 should **only** contain instructions provided in the assembly example. For all the instruction tables, show the NOP instructions you may need to insert. Note that BNE is executed in the **ALU**.

The base addresses for A, B, C are stored in r1, r2, r3 respectively. The address of the last element in the array C[N-1] is stored in r4, where N is an integer multiplier of 10! (read: 10 factorial).

C Code Assembly Code

```
float A[N];
                                                            loop: LD
                                                                       f1, 0 (r1)
float C[N];
                                                                       f2, 0 (r2)
                                                                  LD
int B[N];
                                                                  FMUL f1, f1, f1
\dots // code to initialize A and B
                                                                  FADD f1, f1, f2
for (int i=0; i<N; i++)</pre>
                                                                  ADDI r3, r3, 4
    C[i] = A[i] * A[i] + B[i];
                                                                       f1, -4, (r3)
                                                                  ADDI r1, r1, 4
                                                                  ADDI r2, r2, 4
                                                                  BNE r3, r4, loop
```

VLIW Instruction	ALU	MU	FPU
1			
2			
3			
4			
5			
6			
7			
8			
9			
10			
11			
12			
13			
14			
15			
16			
17			
18			
19			
20			
21			
22			
23			
24			
25			

Table 3

What is the performance in Ops/VLIW instruction (Operations/VLIW instruction) for this design? An operation here refers to an instruction (in the Assembly Code), excluding NOPs.

(b) Assume now we decide to unroll the loop once. Fill **Table 4** with the new VLIW instructions. You should optimize for latency first, then instruction count. **You can choose to use different offsets, immediates and registers, but you may not use any new instructions**.

VLIW Instruction	ALU	MU	FPU
1			
2			
3			
4			
5			
6			
7			
8			
9			
10			
11			
12			
13			
14			
15			
16			
17			
18			
19			
20			
21			
22			
23			
24			
25			

Table 4

What is the perform	nance in Ops/vLIW	instruction for this	s design?	

(c)	Assume now we have unlimited registers and the loop is fully optimized (unrolled to the best performance possible). What is the performance in Ops/cycle for this design? Show your work and explain clearly how you arrived at your answer. You are not required to draw any tables, but you may choose to do so to aid your explanation. (Hint: trace the dependent instructions)

6 VLIW II

You are using a tool that transforms machine code that is written for the MIPS ISA to code in a VLIW ISA. The VLIW ISA is identical to MIPS except that multiple instructions can be grouped together into one VLIW instruction. Up to N MIPS instructions can be grouped together (N is the machine width, which depends on the particular machine). The transformation tool can reorder MIPS instructions to fill VLIW instructions, as long as loads and stores are not reordered relative to each other (however, independent loads and stores can be placed in the same VLIW instruction).

You give the tool the following MIPS program (we have numbered the instructions for reference below):

```
(01) lw
            $t0 \leftarrow 0($a0)
(02) lw
            t2 \leftarrow 8(a0)
(03) lw
            t1 \leftarrow 4(a0)
(04) add
            $t6 ← $t0, $t1
(05) lw
            t3 \leftarrow 12(a0)
(06) sub
            $t7 ← $t1, $t2
(07) lw
            $t4 \leftarrow 16($a0)
            t5 \leftarrow 20(a0)
(08) lw
(09) srlv $s2 \leftarrow $t6, $t7
(10) sub
            $s1 ← $t4, $t5
(11) add
            $s0 \leftarrow $t3, $t4
(12) sllv \$s4 \leftarrow \$t7, \$s1
(13) srlv $s3 \leftarrow $t6. $s0
(14) sllv $s5 \leftarrow $s0, $s1
(15) add
            $s6 ← $s3, $s4
(16) add
            $s7 ← $s4, $s6
(17) srlv $t0 \leftarrow $s6, $s7
(18) srlv $t1 \leftarrow $t0, $s7
```

(a) Draw the dataflow graph of the program. Represent instructions as numbered nodes (01 through 18) and flow dependencies as directed edges (arrows).

the MIPS is value of Netion, choose	V. When	there is		the cod	o ob ovo)					
s value of l	V. When	there is		the cod	a abarra)					
			more tha	3.4						
		struction							ed into a	VLIW
						-		-		
	MIPS	MIPS	MIPS	MIPS	MIPS	MIPS	MIPS	MIPS	MIPS	MIPS
	Instr	Instr	Instr	Instr	Instr	Instr	Instr	$\operatorname{Instr}_{\mathbf{N}_{\mathbf{S}}}$	Instr	Instr
W Instr 1.	NO	NO	NO	NO	NO	NO	NO	NO	NO	No
V Instr.4:										
V Instr.5:										
V Instr.6:										
V Instr.7:										
V Instr.8:										
V Instr.9:										
	V Instr.5: V Instr.6: V Instr.7: V Instr.8: V Instr.9:	Instr No V Instr.1: V Instr.2: V Instr.3: V Instr.4: V Instr.5: V Instr.6: V Instr.7: V Instr.8: V Instr.9: Ind that the code is	Instr No	Instr Instr No	Instr Instr No No No	Instr Instr Instr No No No No	Instr Instr Instr Instr No No No No No No No N	Instr Instr Instr Instr Instr No No No No No No No N	Instr Instr Instr Instr Instr No No No No No No No N	Instr No No No Instr Instr No No No No No No No N

(e) Write the MIPS instruction numbers corresponding to each VLIW instruction, for this optimal value of N. Again, as in part (c) above, pack instructions such that when more than one instruction can be placed in a given VLIW instruction, the instruction that comes first in the original MIPS code is chosen.

	MIPS Instr No									
VLIW Instr.1:										
VLIW Instr.2:										
VLIW Instr.3:										
VLIW Instr.4:										
VLIW Instr.5:										
VLIW Instr.6:										
VLIW Instr.7:										
VLIW Instr.8:										
VLIW Instr.9:										

(f)	A competing processor design company builds an in-order superscalar processor with the same machine-width N as the width you found above in part(b). The machine has the same clock frequency as the VLIW processor. When you run the original MIPS program on this machine, you find that it executes slower than the corresponding VLIW program on the VLIW machine in part (b). Why could this be the case?
(g)	When you run some other program on this superscalar machine, you find it runs faster than the corresponding VLIW program on the VLIW machine. Why could this be the case?

7 VLIW III

Consider a VLIW (very long instruction word) CPU that uses the long instruction format shown in Table 5. Each long instruction is composed of four short instructions, but there are restrictions on which type of instruction may go in which of the four slots.

MEMORY	INTEGER	CONTROL	FLOAT

Table 5: VLIW instruction format.

Table 6 provides a detailed description of the available short instructions and the total execution latency of each type of short instruction. Each short instruction execution unit is fully pipelined, and its result is available on the cycle given by the latency, e.g., a CONTROL instruction's results (if any) are available for other instructions to use in the next cycle.

Category	$rac{ ext{Latency}}{ ext{(cycles)}}$	Instruction(s)	Description	Functionality
CONTROL	1	BEQ LABEL, Rs1, Rs2 NOP	Branch IF equal No operation	IF Rs1 == Rs2: PC = LABEL PC = Next PC
MEMORY	3	LD Rd, [Rs]	Memory load	Rd = MEM[Rs]
INTEGER	2	IADD Rd, Rs1, Rs2	Integer add	Rd = Rs1 + Rs2
FLOAT	4	FADD Rd, Rs1, Rs2	Floating-point add	Rd = Rs1 + Rs2

Table 6: Instruction latencies and descriptions.

Consider the piece of code given in Table 7. Unfortunately, it is written in terms of short instructions that cannot be directly input to the VLIW CPU.

	Instruction		Notes
	< Initialize RO-R2 >		RO-R2 point to valid memory
	LOOP:		
1	LD	RO, [RO]	RO <- MEM[RO]
2	LD	R1, [R1]	R1 <- MEM[R1]
3	IADD	R4, R0, R1	R4 <- R0 + R1
4	FADD	R5, R0, R4	R5 <- R0 + R4
5	LD	R6, [R2]	R6 <- MEM[R2]
6	LD	R2, [R0]	R2 <- MEM[RO]
7	FADD	R3, R1, R6	R3 <- R1 + R6
8	IADD	R4, R2, R4	R4 <- R2 + R4
9	IADD	R5, R5, R4	R5 <- R5 + R4
10	IADD	RO, R6, R2	RO <- R6 + R2
11	IADD	RO, RO, R3	RO <- RO + R3
12	BEQ	LOOP, RO, R5	GOTO LOOP if RO == R5

Table 7: Proposed code for calculating the results of the next Swiss referendum.

- (a) Warm-up: which of the following are goals of VLIW CPU design (circle all that apply)?
 - (I) Simplify code compilation.
 - (II) Simplify application development.
 - (III) Reduce overall hardware complexity.
 - (IV) Simplify hardware inter-instruction dependence checking.

- (V) Reduce processor fetch width.
- (b) Your task is to determine the optimal VLIW scheduling of the short instructions by hand. Fill in the following table with the highest performance (i.e., fewest number of execution cycles) instruction sequence that may be directly input into the VLIW CPU and have the same functionality as the code in Table 7. Where possible, you may write instruction IDs corresponding to the numbers given in Table 7 and leave any NOP instructions as blank slots.

Consider **only one loop iteration** (including the BEQ instruction), **ignore initialization** and any cross-iteration optimizations (e.g., loop unrolling), and **do not** optimize the code by removing or changing existing instructions.

Cycle	MEMORY	INTEGER	CONTROL	FLOAT
1				
2				
3				
4				
5				
6				
7				
8				
9				
10				
11				
12				
13				
14				
15				
16				
17				
18				
19				
20				

Hint: you should not require more than 20 cycles.

ilization of the instr slots throughout ex	slots (computed	as the ratio of utiliz	zed slots to
	slots (computed	as the ratio of utiliz	zed slots to

8 Systolic Arrays I

Figure 1 shows a systolic array processing element.

Each processing element takes in two inputs, M and N, and outputs P and Q. Each processing element also contains an "accumulator" R that can be read from and written to. The initial value of the "accumulator" is 0.

Figure 2 shows a systolic array composed of 9 processing elements. The smaller boxes are the inputs to the systolic array and the larger boxes are the processing elements. You will program this systolic array to perform the following calculation:

$$\begin{bmatrix} c_{00} & c_{01} & c_{02} \\ c_{10} & c_{11} & c_{12} \\ c_{20} & c_{21} & c_{22} \end{bmatrix} = \begin{bmatrix} a_{00} & a_{01} & a_{02} \\ a_{10} & a_{11} & a_{12} \\ a_{20} & a_{21} & a_{22} \end{bmatrix} \times \begin{bmatrix} b_{00} & b_{01} & b_{02} \\ b_{10} & b_{11} & b_{12} \\ b_{20} & b_{21} & b_{22} \end{bmatrix}$$

In each time cycle, each processing element will take in its two inputs, perform any necessary actions, and write on its outputs. The time cycle labels on the input boxes determine which time cycle the inputs will be fed into their corresponding processing elements. Any processing element input that is not driven will default to 0, and any processing element that has no output arrow will have its output ignored.

After all the calculations finish, each processing element's "accumulator" will hold one element of the final result matrix, arranged in the correct order.

(a) Please describe the operations that each individual processing element performs, using mathe-matical equations and the variables M, N, P, Q and R.

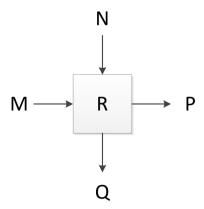


Figure 1: A systolic array processing element



(b) Please fill in all 30 input boxes in Figure 2 so that the systolic array computes the correct matrix multiplication result described on the previous page. (Hint: Use a_{ij} and b_{ij} .)

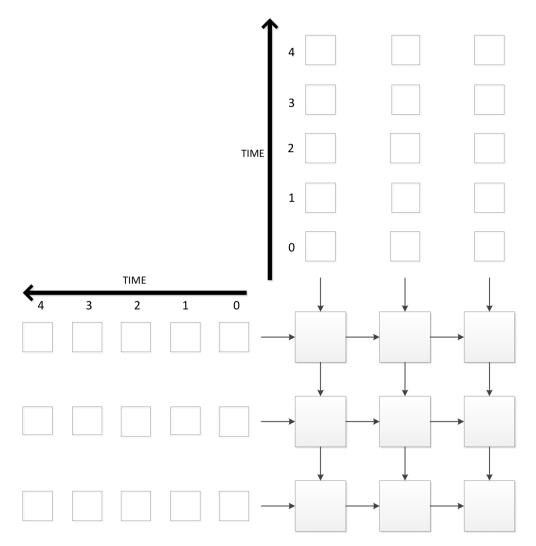


Figure 2: A systolic array

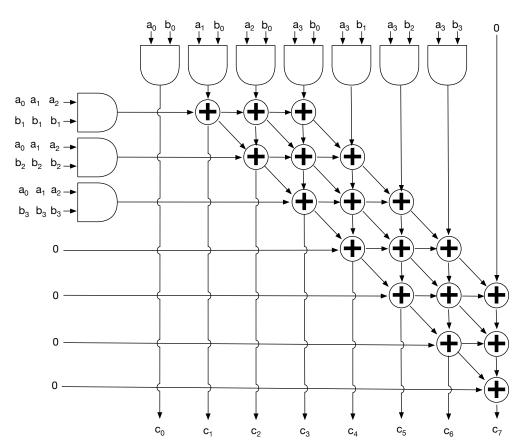
9 Systolic Arrays II

The following diagram is a systolic array that performs the multiplication of two 4-bit binary numbers (**a** and **b**). For example, if $\mathbf{a}=1110$ and $\mathbf{b}=1011$, the result of the multiplication is $\mathbf{c}=10011010$:

$$\begin{array}{r}
1011 \\
\times 1110 \\
\hline
0000 \\
1011 \\
1011 \\
+ 1011 \\
\hline
10011010
\end{array}$$
(1)

The input to the systolic arrays is through the AND gates. The figure shows which bits of the two numbers \mathbf{a} and \mathbf{b} are inserted into each AND gate. However, the figure does *not* indicate in which cycle each input is issued. Make the following assumptions:

- The latency of each adder is one cycle.
- Vertical arrows propagate the sum to the next adder.
- Diagonal arrows propagate the carry to the next adder.
- Horizontal arrows propagate the output of the AND gates in each row.
- An adder adds the value of its three inputs (vertical, diagonal and horizontal inputs)
- An adder can hold a value for only one cycle.



ar	ow many cycles does it take to perform <i>one</i> multiplication of two 4-bit binary numbers in this systolic ray? Indicate 1) in which cycle each bit is inputted in the systolic array and 2) in which cycle each t of the result is produced.
	ow many cycles does it take to perform N consecutive multiplications of two 4-bit binary numbers this systolic array?

EXTRA EXERCISES ON DELAYED BRANCHING

We did not cover delayed branching in detail in lecture, so these two questions are for your benefit and learning solely.

10 Delayed Branching I (Extra)

A machine has a five-stage pipeline consisting of fetch, decode, execute, mem and write-back stages. The machine uses delay slots to handle control dependences. Jump targets, branch targets and destinations are resolved in the execute stage.

)	Wha	at is the number of delay slots needed to ensure correct operation?
	the r	ch instruction(s) in the assembly sequences below would you place in the delay slot(s), assuming number of delay slots you answered for part(a)? Clearly rewrite the code with the appropriate ruction(s) in the delay slot(s).
	(I)	ADD R5 <- R4, R3 OR R3 <- R1, R2 SUB R7 <- R5, R6 J X Delay Slots LW R10 <- (R7) ADD R6 <- R1, R2 X:
		Solution:

(II)	ADD R5 <- R4, R3 OR R3 <- R1, R2 SUB R7 <- R5, R6 BEQ R5 <- R7, X Delay Slots LW R10 <- (R7) ADD R6 <- R1, R2 X: Solution:
(III)	ADD R2 <- R4, R3 OR R5 <- R1, R2 SUB R7 <- R5, R6 BEQ R5 <- R7, X Delay Slots LW R10 <- (R7) ADD R6 <- R1, R2 X: Solution:

(c)	Can you modify the pipeline to reduce the number of delay slots (without introducing branch prediction)? Clearly state your solution and explain why.

11 Delayed Branching II (Extra)

You are designing an ISA that uses delayed branch instructions. You are trying to decide how many instructions to place into the branch delay slot. How many branch delay slots would you need for the following different implementations? Explain your reasoning briefly.

(a)	An in-order processor where conditional branches resolve during the 4th stage
(b)	An out-of-order processor with 64 unified reservation station entries where conditional branches resolve during the 2nd cycle of branch execution. The processor has 15 pipeline stages until the start of the execution stages

EXTRA EXERCISES FOR PRACTICING

The following exercises are old exam questions that are conceptually similar to the ones above, but with slight alterations. We do not expect or recommend you to solve all of them, unless you think you are struggling with a particular concept, or would like to do practice runs on these old exam questions.

12 Branch Prediction (Extra)

Assume a processor that implements an ISA with eight registers (R0-R7). In this ISA, the main memory is byte-addressable and each word contains 4 bytes. The processor employs a branch predictor to reduce the overhead of the branches. The ISA implements the instructions given in the following table:

Instructions	Description
la R_i , Address	load the effective $Address$ into R_i
move R_i , R_j	$R_i \leftarrow R_j$
move R_i , (R_j)	$R_i \leftarrow \operatorname{Memory}[R_j]$
move (R_i) , R_j	$Memory[R_i] \leftarrow R_j$
li R_i , Imm	$R_i \leftarrow \text{Imm}$
add R_i, R_j, R_k	$R_i \leftarrow R_j + R_k$
addi R_i, R_j, Imm	$R_i \leftarrow R_j + \operatorname{Imm}$
$\operatorname{cmp} R_i, R_j$	Compare: Set sign flag, if $R_i < R_j$; set zero flag, if $R_i = R_j$
$\operatorname{cmp} R_i, (R_j)$	Compare: Set sign flag, if R_i < Memory $[R_j]$; set zero flag, if R_i = Memory $[R_j]$
cmpi R_i , Imm	Compare: Set sign flag, if R_i < Imm; set zero flag, if R_i = Imm.
jg label	Jump to the target address if both of sign and zero flags are zero.
jnz label	Jump to the target address if zero flag is zero.
halt	Stop executing instructions.

The processor executes the following program. Answer the questions below related to the accuracy of the branch predictors that the processor can potentially implement.

```
la RO, Array
           move R6, R0
2
           li R1, 4
3
           move R5, R1
           move R7, R1
           move R2, R0
6
           addi R2, R2, 4
   Loop:
           move R3, (R2)
9
           cmp R3, (R0)
10
           jg Next_Iteration
           move R4, (R0)
12
           move (RO), R3
13
           move (R2), R4
14
   Next_Iteration:
15
           addi RO, RO, 4
16
           addi R2, R2, 4
17
           addi R1, R1, -1
18
           cmpi R1, 0
19
           jnz Loop
20
           move R1, R7
21
           addi R5, R5, -1
22
           move RO, R6
23
           move R2, R0
24
           addi R2, R2, 4
25
           cmpi R5, 0
26
           jnz Loop
27
           halt
28
29
   . data
   Array: word 5, 20, 1, -5, 34
```

13 Systolic Arrays (Extra)

A systolic array consist of 3x4 Processing Elements (PEs), interconnected as shown in Figure 3. The inputs of the systolic array are labeled as H0, H1, H2 and V0,V1,V2,V3. Figure 4 shows the PE logic, which performs a multiply and accumulate operation (MAC), and it saves the result in an internal register (reg). Figure 4 also shows how each PE propagates its inputs. We make the following assumptions:

- The latency of each MAC is one cycle.
- The propagation of the values from i_0 to o_0 , and from i_1 to o_1 , takes one cycle.
- The initial value of all registers is zero.
- You can input a value more than once in the systolic array.

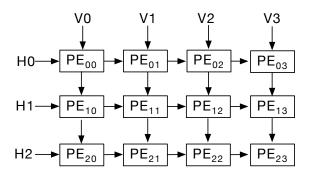


Figure 3: PE array

Processing Element (PE)

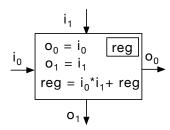


Figure 4: Processing Element (PE)

Your goal is to use this systolic array to perform the convolution of a 3x3 image (matrix I) with three 2x2 filters (matrices F, G, and H), to obtain three outputs (matrices O, U, and E):

As an example, the convolution of the matrix I with the filter F is computed as follows:

- $O_{00} = I_{00} * F_{00} + I_{01} * F_{01} + I_{10} * F_{10} + I_{11} * F_{11}$
- $O_{01} = I_{01} * F_{00} + I_{02} * F_{01} + I_{11} * F_{10} + I_{12} * F_{11}$
- $O_{10} = I_{10} * F_{00} + I_{11} * F_{01} + I_{20} * F_{10} + I_{21} * F_{11}$
- $O_{11} = I_{11} * F_{00} + I_{12} * F_{01} + I_{21} * F_{10} + I_{22} * F_{11}$

You should compute the three convolutions in the minimum possible amount of cycles. Fill the following table with:

- 1. The input values (matrices I, F, G, and H) in the correct input ports of the systolic array (the values can be repeated).
- 2. The output values and the corresponding PE where the outputs (matrices $O,\,U,\,and\,E)$ are generated.

Fill the gaps only with relevant information.

cycle	H 0	H1	H2	$\mathbf{V0}$	V1	V2	V3	PE_{00}	PE_{01}	PE_{02}	PE_{03}	PE_{10}	PE_{11}	PE_{12}	PE_{13}	PE_{20}	PE_{21}	PE_{22}	PE_{23}
0																			
1																			
2																			
3																			
4																			
5																			
6																			
7																			
8																			
9																			
10																			
11																			
12																			
13																			
14																			
15																			