

### 35.1-4

- (1) Compute  $depth(v)$  for each vertex  $v \in V$ .
- (2) Use integer-sort to sort all vertices in  $V$  according to their depths by decreasing order.
- (3) for each  $v \in V$   
     $color[v] \leftarrow \text{white};$   
    for each  $v \in V$   
        if ( $color[v] = \text{white}$ ) and ( $parent[v] \neq \text{null}$ ) then  
             $color[parent[v]] = \text{black};$   
    Answer: those vertices  $v$  with  $color[v] = \text{black}$

Time analysis:

- (1)  $O(n)$
- (2)  $O(n)$
- (3)  $O(n)$

So total time complexity =  $O(n)$

Correctness:

- (1) If a vertex  $v$  is not chosen, we'll choose  $v$ 's parent (if exists) to cover that edge.
- (2) All leaves are not chosen by the algorithm.  
    Instead, we choose leaves' parents, which makes better situation compared to choosing leaves.

PS:

如果每次都選最大 degree 的 node，這是不對的。

以下圖為例，如果一開始就選了紅色的點(degree 最大)，那至少還要選另外四個藍色點才能 cover 所有的 edge，但最少可以只要四個白色點就夠了。

