

B

(i) 答案卷第一張正面為封面。第一張正、反兩面不要寫任何答案。

(ii) 依空格號碼順序在第二張正面寫下所有填充題答案，不要寫計算過程。

(iii) 依計算題之題號順序在第二張反面以後寫下演算過程與答案，每題從新的一頁寫起。

Note: $k = 9.0 \times 10^9 \text{ N} \cdot \text{m}^2 \cdot \text{C}^{-2}$, $\epsilon_0 = (4\pi k)^{-1} = 8.85 \times 10^{-12} \text{ C}^2 \cdot \text{N}^{-1} \cdot \text{m}^{-2}$ **Part I. Filling the blank (4 points per blank)**• The electric field of two point charges q and Q is represented by the right figure.The ratio $Q/q =$ [1].• The work to move a $50 \mu\text{C}$ charge against a 12 V potential difference is [2] J.• Four point charges, each of charge q , are assembled to form a square of side a . The electrostatic energy of this charge distribution is [3].• A thin ring of radius R carries charge $5Q$ distributed uniformly over $3/4$ of its circumference, and $-Q$ over the rest. The potential at the ring's center is [4].• A wire has a resistance of R_1 . The resistance of another wire, made of the same material, that is half as long and has half the diameter, is R_2 . The ratio R_2/R_1 is [5].• The capacitance of a parallel-plate capacitor is C_0 when the space between the plates is empty. If the space is filled with two dielectrics (dielectric constants κ_1 and κ_2) of equal size, as shown in the figure, the capacitance is [6] C_0 .• A 35Ω electric stove burner consumes 1.5 kW of power. At what voltage does it operate? [7] V.• A capacitor consists of a conducting sphere of radius a surrounded by a concentric (同心) conducting shell of radius b . The capacitance is [8].• The equivalent capacitance of the four identical capacitors in the figure, measured between A and B is [9] C.• A conductor has a hollow cavity. There is a point charge $3q/2$ inside the cavity. In the space far from conductor the electric field is $\vec{E} = \frac{kQ}{r^2} \hat{r}$. The charge on the outer surface of the conductor is [10].• You have a typical resistance of $100 \text{ k}\Omega$. How much current could a 12 V car battery pass through you? [11] mA.

$$\frac{4kq^2}{a} + \frac{\sqrt{2}kq^2}{a}$$

$$(4+\sqrt{2})kq^2$$

$$W = \frac{1}{2} \times 50 \times 10^{-6} \times 12 = 3 \times 10^{-4} \text{ J}$$

$$U = \frac{kq^2}{4R} + \frac{3kq^2}{4R} = \frac{4kq^2}{4R} = \frac{kq^2}{R}$$

$$V = \frac{kQ}{R}$$

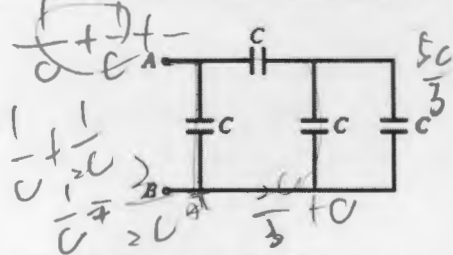
$$\frac{1}{13\pi} \times \frac{4\pi R}{R} = \frac{4}{13}$$

$$\frac{L}{4\pi r} \times \frac{1}{L}$$

$$C = \kappa \epsilon_0 \frac{A}{d}$$

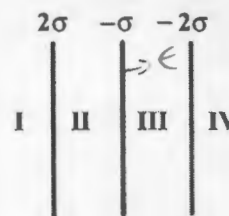
$$V = IR \Rightarrow R = \frac{V}{I} = \frac{120}{15} = 8 \Omega$$

$$C = 2\pi\epsilon_0 \ln\left(\frac{b}{a}\right)$$



$$I = \frac{V}{R} = \frac{12}{100000} = 1.2 \times 10^{-4} \text{ A}$$

- Three infinite sheets are charged with uniform surface charge density 2σ , $-\sigma$, and -2σ , shown in the right figure. The magnitude of electric field in region III is **[12]**.

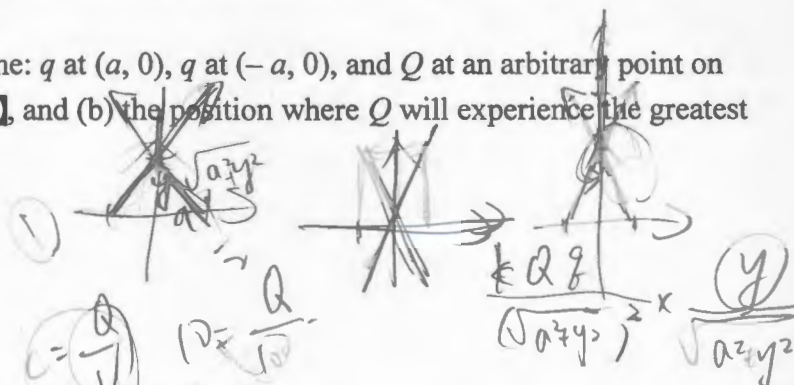


$$E = \frac{\sigma}{\epsilon_0}$$

- A uniformly charged wire of line charge density λ forms a rectangle of sides a and b . The electric field at the center of rectangle is **[13]** V/m.

- A cube of side L has one corner at $(0, 0)$ and its sides lie along the x , y , and z axes, respectively. There is an electric field given by $\vec{E} = (a + by)\hat{j}$. The net charge enclosed by the cube surface is **[14]**.

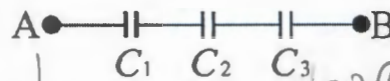
- Three positive point charges locate on the x - y plane: q at $(a, 0)$, q at $(-a, 0)$, and Q at an arbitrary point on the y -axis $(0, y)$. (a) The electric force on Q is **[15]**, and (b) the position where Q will experience the greatest force is **[16]**.



Part II Problems (10 points per problem)

1.

In the figure, three capacitors are connected in series where $C_1 = 10 \mu\text{F}$, $C_2 = 20 \mu\text{F}$, and $C_3 = 25 \mu\text{F}$. If no capacitor can resist a potential difference of more than 100 V, what is the maximum safe potential difference between the terminals A and B?



2.

A sphere of radius R carries charge Q distributed uniformly over its surface. Calculate the electric energy stored in the electric field and express your result in terms of Q , R , and k .

$$\left(\frac{kQ}{R^2}\right)^2 = \frac{1}{4\pi k} \times \frac{kQ}{R^2} = \frac{kQ^2}{4\pi R^2}$$

3.

An infinitely long rod of radius R carries a charge density $\rho(r) = Ar$, where r is the distance from the rod axis and A is a constant. Find the electric field strengths outside and inside the rod.

AY

4.

SK

A rod of length L has a charge Q uniformly distributed along its length. (a) Calculate the potential at a distance a from one end along the axis of the rod, as shown in the figure. (b) Find the electric \vec{E} field from (a).

