

## 1. Regular Languages

- (a) [5] What are the two techniques to prove a language is regular?
- (b) [10] Use these two techniques to prove the language of all strings with an even number of 0's and an odd number of 1's is regular

## 2. [15] Pumping lemma (PDA)

- (a) Show that  $L = \{a^n b^m \mid n > m, m \geq 0\}$  is not regular
- (b) Show that  $L = \{a^n b^m \mid n \leq m, n \geq 0\}$  is not regular
- (c) Prove or disprove the following statement: If  $L_1$  and  $L_2$  are nonregular languages, then  $L_1 \cup L_2$  is also nonregular

## 3. Consider the decimal integer system. The first digit cannot be a 0 unless its value is zero.

- (a) [5] Write down the regular expression that generates the language  $L$  of all decimal integer numbers.
- (b) [10] Use Thompson's construction to find its NFA that accepts  $L(G)$   
Note: Must follow the Thompson's construction algorithm to build NFA
- (c) [10] Convert the NFA to a DFA  
Note: must use the subset construction algorithm
- (d) [5] Minimize the DFA

4. [15] Is it possible to find a DFA that accepts the same language as the PDA  $M$ ?

$$M = (\{q_0, q_1\}, \{a, b\}, \{z\}, \delta, q_0, z, \{q_1\})$$

with

$$\delta(q_0, a, z) = \{(q_1, z)\}$$

$$\delta(q_0, b, z) = \{(q_0, z)\}$$

$$\delta(q_1, a, z) = \{(q_1, z)\}$$

$$\delta(q_1, b, z) = \{(q_0, z)\}$$

## 5. [10] Eliminate left recursion from the grammar

$$E \rightarrow E \text{ sub } E$$

$$E \rightarrow E \text{ sup } E$$

$$E \rightarrow E \text{ sub } E \text{ sup } E$$

$$E \rightarrow \text{id}$$

6. Consider the following grammar  $G$ 

$$\text{exp} \rightarrow \text{atom} \mid \text{list}$$

$$\text{atom} \rightarrow \text{num} \mid \text{id}$$

$$\text{list} \rightarrow (\text{exp-list})$$

$$\text{exp-list} \rightarrow \text{exp-list exp} \mid \text{exp}$$

- (a) [5] Remove the left recursion
- (b) [5] Write down the FIRST and FOLLOW sets for all nonterminals of  $G$
- (c) [5] Show the predictive parsing table of  $G$
- (d) [5] Show the process of parsing the string "( a ( b ( 2 ) ) ( c ) )" by the predictive parser