

HW1

1. (8%) What is the exact number of bits in a system that contains (a) 16M byte and (b) 8.3G byte?

$$\begin{aligned} \text{(a) 16M Byte} &= 16 * 2^{20} * 2^8 \Rightarrow 134,217,728 \\ \text{(b) 8.3G Byte} &= 8.3 * 2^{30} * 2^8 (71,296,457,113.6) \Rightarrow 71,296,457,114 \end{aligned}$$

2. (24%) Convert the following numbers from the given base to other three bases listed in the table:

| Decimal | Binary | Octal | Hexadecimal |
|----------|----------------|----------|-------------|
| 384.57 | 110000000.1001 | 600.4436 | 180.91EB |
| 26.625 | 11010.101 | 32.5 | 1A.A |
| 30.53125 | 11110.10001 | 36.42 | 1E.88 |
| 249.25 | 11111001.01 | 371.2 | F9.4 |

$(384.57)_{10} \rightarrow \text{binary}$

$$\begin{array}{l} 384/2 = 192 \dots 0 \\ 192/2 = 96 \dots 0 \\ 96/2 = 48 \dots 0 \\ 48/2 = 24 \dots 0 \\ 24/2 = 12 \dots 0 \\ 12/2 = 6 \dots 0 \\ 6/2 = 3 \dots 0 \\ 3/2 = 1 \dots 1 \\ 1/2 = 0 \dots 1 \end{array} \quad \begin{array}{l} 0.57 \times 2 = 1.14 \\ 0.14 \times 2 = 0.28 \\ 0.28 \times 2 = 0.56 \\ 0.56 \times 2 = 1.12 \\ 0.12 \times 2 = 0.24 \\ 0.24 \times 2 = 0.48 \\ 0.48 \times 2 = 0.96 \\ 0.96 \times 2 = 1.92 \\ 0.92 \times 2 = 1.84 \\ 0.84 \times 2 = 1.68 \\ 0.68 \times 2 = 1.36 \\ 0.36 \times 2 = 0.72 \\ 0.72 \times 2 = 1.44 \\ 0.44 \times 2 = 0.88 \\ 0.88 \times 2 = 1.76 \\ 0.76 \times 2 = 1.52 \end{array}$$

110000000.1001

$(384.57)_{10} \rightarrow \text{octal}$

$$\begin{array}{ccccccc} 110000000.100100011110 \\ \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow \\ 600.4436 \end{array}$$

$(384.57)_{10} \rightarrow \text{hexadecimal}$

$$\begin{array}{ccccccc} 000110000000.1001000111101011 \\ \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow \\ 180.91EB \end{array}$$

$(11010.101)_2 \rightarrow \text{decimal}$

$$11010.101 \Rightarrow 1 \times 2^4 + 1 \times 2^3 + 0 \times 2^2 + 1 \times 2^1 + 0 \times 2^0 + 1 \times 2^{-1} + 0 \times 2^{-2} + 1 \times 2^{-3} = 26.625$$

$(11010.101)_2 \rightarrow \text{octal}$

$$\begin{array}{ccc} 011010.101 \\ \downarrow \downarrow \downarrow \downarrow \\ 32.5 \end{array}$$

$(11010.101)_2 \rightarrow \text{hexadecimal}$

$$\begin{array}{cccc} 00011010.1010 \\ \downarrow \downarrow \downarrow \downarrow \\ 1A.A \end{array}$$

$(36.42)_8 \rightarrow \text{binary}$

$$\begin{array}{l} 36/2 = 18 \dots 0 \\ 18/2 = 9 \dots 0 \\ 9/2 = 4 \dots 1 \\ 4/2 = 2 \dots 0 \\ 2/2 = 1 \dots 0 \\ 1/2 = 0 \dots 1 \end{array} \quad \begin{array}{l} 0.42 \times 2 = 0.84 \\ 0.84 \times 2 = 1.68 \\ 0.68 \times 2 = 1.36 \\ 0.36 \times 2 = 0.72 \\ 0.72 \times 2 = 1.44 \\ 0.44 \times 2 = 0.88 \end{array}$$

011110.100010

$(36.42)_8 \rightarrow \text{decimal}$

$$\Rightarrow 3 \times 8^1 + 6 \times 8^0 + 4 \times 8^{-1} + 2 \times 8^{-2} = 30.53125$$

$(36.42)_8 \rightarrow \text{hexadecimal}$

$$\begin{array}{ccc} 011110.100010 \\ \downarrow \downarrow \downarrow \downarrow \\ 1E.88 \end{array}$$

$(F9.4)_{16} \rightarrow \text{binary}$

$$\begin{array}{ccc} F & 9 & .4 \\ 1111 & 1001 & .0100 \end{array}$$

$(F9.4)_{16} \rightarrow \text{decimal}$

$$\Rightarrow 15 \times 16^1 + 9 \times 16^0 + 4 \times 16^{-1} = 249.25$$

$(F9.4)_{16} \rightarrow \text{octal}$

$$\begin{array}{cccc} 01111001.0100 \\ \downarrow \downarrow \downarrow \downarrow \\ 371.2 \end{array}$$

3. (16%) Perform the subtraction with the following unsigned binary numbers by taking the 2's complement of the subtrahend. (a) $0111 - 0110$, (b) $10010 - 1010$, (c) $1010110 - 1111010$, (d) $101101 - 110$.

| | |
|--------------------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------|
| <p>(a)</p> $\begin{array}{r} \text{00 0111} \\ + 11 1010 \\ \hline 00 0001 \end{array}$ | <p>(b)</p> $\begin{array}{r} \text{001 0010} \\ + 111 0110 \\ \hline 000 1000 \end{array}$ |
| <p>(c)</p> $\begin{array}{r} \text{00101 0110} \\ + 11000 0110 \\ \hline 11101 1100 \end{array}$ | <p>(d)</p> $\begin{array}{r} \text{00101101} \\ + 11111010 \\ \hline 00100111 \end{array}$ |

4. (16%) Convert decimal +47 and +38 to binary, using the signed-2's-complement representation and enough digits to accommodate the numbers. Then, perform the binary equivalent of $(+47)+(-38)$ and $(-47)+(-38)$ using addition. Convert the answers back to decimal and verify that they are correct.

| | |
|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| $47_{(10)} = 0010_1111_{(2)}$ $38_{(10)} = 0010_0110_{(2)}$ | $-47_{(10)} = 1101_0001_{(2)}$ $-38_{(10)} = 1101_1010_{(2)}$ |
| $\begin{array}{r} \text{0010 1111 } 47_{(10)} \\ + 1101 1010 -38_{(10)} \\ \hline \text{10000 1001 } 9_{(10)} \end{array}$ <p>carry out w/o overflow sum is correct</p> | $\begin{array}{r} \text{1101 0001 } -47_{(10)} \\ + 1101 1010 -38_{(10)} \\ \hline \text{11010 1011 } -85_{(10)} \end{array}$ <p>carry out w/o overflow sum is correct</p> |

5. (10%) Write the word "Logic" in ASCII using an eight-bit code including the space. Treat the leftmost bit of each character as a parity bit. Each 8-bit code should have even parity.

↓---- parity bit

L : 1100 1100
o : 0110 1111
g : 1110 0111
i : 0110 1001
c : 0110 0011

6. (8%) For an 8-bit sequence is 1101 0111. What is its content if it represents (a) two **decimal digits** in BCD? (b) two **decimal number** in the Excess-3 code? (c) an 8-bit unsigned number? (d) an 8-bit signed number?

a. $1101_{(2)} = \text{unused}_{(10)}$ $0111_{(2)} = 7_{(10)}$

b. $1101_{(2)} = \text{unused}_{(10)}$ $0111_{(2)} = 4_{(10)}$

c. $1101\ 0111_{(2)} = 215_{(10)}$

d. $1101\ 0111_{(2)} = -41_{(10)}$

7. (6%) If you have 27 books and want to give each book a unique id with a binary number. If we want to use as least as possible the number of bits as the id, how many bits do you need?

27 unique IDs which means the number of bits you need could at least represent 27 unique numbers .

$$2^5 > 27 > 2^4$$

Ans : 5 bits

8. (12%) Find the Gray code sequence of 12 code words.

| | | | |
|-------------------------|-------------------|-------------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| $M = 2^k = 12, k = 6$ | | | |
| D | $d_3 d_2 d_1 d_0$ | $g_3 g_2 g_1 g_0$ | $\left\{ \begin{array}{l} g_3 = 0 \text{ (MSB = 0)} \\ g_2 = d_3 \oplus d_2 = 0 \oplus 0 = 0 \\ g_1 = d_2 \oplus d_1 = 0 \oplus 0 = 0 \\ g_0 = d_1 \oplus d_0 = 0 \oplus 0 = 0 \end{array} \right.$ |
| 0 | 0 0 0 0 | → 0 0 0 0 | |
| 1 | 0 0 0 1 | → 0 0 0 1 | |
| 2 | 0 0 1 0 | → 0 0 1 1 | |
| 3 | 0 0 1 1 | → 0 0 1 0 | |
| 4 | 0 1 0 0 | → 0 1 1 0 | |
| 5 | 0 1 0 1 | → 0 1 1 1 | |
| For the rest half codes | | | |
| 6 | 0 1 1 0 | → 1 1 1 1 | set MSB = 1 |
| 7 | 0 1 1 1 | → 1 1 1 0 | then copy in reverse order of |
| 8 | 1 0 0 0 | → 1 0 1 0 | first half part! |
| 9 | 1 0 0 1 | → 1 0 1 1 | |
| 10 | 1 0 1 0 | → 1 0 0 1 | |
| 11 | 1 0 1 1 | → 1 0 0 0 | |