$$f_p(x) = \begin{cases} \frac{1}{p} & x = p\\ \frac{\frac{1}{p-(1-x)\frac{1}{2}}}{\sqrt{1-p}\cos(x-p)} & x \neq p \end{cases}$$