Spectral decomposition of a symmetric matrix (assume all eigenvalues are distinct)

Matrix
$$M$$

 $M \in \operatorname{Sym}(d, \mathbb{R})$

$$\lambda_1 v_1 v_1^{\top} \lambda_2 v_2 v_2^{\top}$$

$$M v_i = \lambda_i v_i \qquad \lambda_{d-1} v_{d-1} v_{d-1}^{\top}$$

$$M = \sum_{i=1}^{d} \lambda_i v_i v_i^{\top}$$

$$P_i = v_i v_i^{\top}, P_i P_j = 0 (i \neq j), \sum_{i=1}^{d} P_i = I$$