

Let  $P = \{p_1, \dots, p_n\}$  be a point set, and  $\bar{x} = \frac{1}{n} \sum_i p_i = c(P)$  the centroid of  $P$ . A coreset  $Q \subset P$  for the centroid performs  $\frac{2}{\epsilon^2}$  iterations: Choose  $c_1 = x_1$ , let  $i_t = \arg \min \langle c_t - \bar{x}, x_i - \bar{x} \rangle$ , and

$$c_{t+1} = \frac{t-1}{t} c_t + \frac{1}{t} x_{i_t}$$

Let  $Q_t = \{x_{i_1}, \dots, x_{i_t}\}$  denote the coreset.

$$|c(Q_{\frac{2}{\epsilon^2}}) - c(P)| \leq \epsilon$$