



$$\begin{aligned}
 S_F(\theta_1; \theta_2) &= \int_0^1 ds^2(\gamma(t)) dt \\
 &= \int_0^1 ds^2(\gamma^*(t)) dt \\
 &= S_{F^*}(\eta_1; \eta_2)
 \end{aligned}$$

$$\begin{aligned}
 S_F(\theta_1; \theta_2) &= B_F(\theta_1 : \theta_2) + B_F(\theta_2 : \theta_1) \\
 &= (\theta_2 - \theta_1)^\top (\eta_2 - \eta_1) = S_{F^*}(\eta_1; \eta_2)
 \end{aligned}$$

$$\begin{aligned}
 \theta(\gamma(t)) &= \theta(p) + t(\theta(q) - \theta(p)) \\
 \eta(\gamma^*(t)) &= \eta(p) + t(\eta(q) - \eta(p))
 \end{aligned}$$