

Input: A set $\{p_i = (p_i^1, \dots, p_i^d)\}_{i \in [n]}$ of n categorical distributions belonging to the $(d-1)$ -dimensional probability simplex Δ_{d-1} . T : The number of CCCP iterations

Output: An approximation $^{(T)}\bar{p}$ of the Jensen-Shannon centroid \bar{p} minimizing $\frac{1}{n} \sum_{i=1}^n D_{\text{JS}}(c, p_i)$

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/* Convert the categorical distributions to their natural parameters by dropping
   the last coordinate */
 $\theta_i^j = p_i^j$  for  $j \in \{1, \dots, d-1\}$ ;
/* Initialize the Jensen-Shannon centroid */
 $t \leftarrow 0$ ;
 $^{(0)}\bar{\theta} = \frac{1}{n} \sum_{i=1}^n \theta_i$ ;
/* Convert the initial natural parameter of the JS centroid to a categorical
   distribution */
 $^{(0)}\bar{p}^j = ^{(0)}\bar{\theta}^j$  for  $j \in \{1, \dots, d-1\}$ ;  $^{(0)}\bar{p}^d = 1 - \sum_{i=1}^d ^{(0)}\bar{p}^i$ ;
/* Perform the ConCave-Convex Procedure (CCCP) */
while  $t \leq T$  do
    /* Use  $\nabla F(\theta) = \left[ \log \frac{\theta_i}{1 - \sum_{j=1}^d \theta_j} \right]_i$  and  $\nabla F^{-1}(\eta) = \frac{1}{1 + \sum_{j=1}^d \exp(\eta_j)} [\exp(\eta_i)]_i$  */
     $^{(t+1)}\theta = (\nabla F)^{-1} \left( \frac{1}{n} \sum_i \nabla F \left( \frac{\theta_i + ^{(t)}\theta}{2} \right) \right)$ ;
     $t \leftarrow t + 1$ ;
end
/* Convert back the natural parameter to the categorical distribution of the
   approximated Jensen-Shannon centroid */
 $^{(T)}\bar{p}^j = ^{(T)}\bar{\theta}^j$  for  $j \in \{1, \dots, d-1\}$ ;  $^{(T)}\bar{p}^d = 1 - \sum_{i=1}^d ^{(T)}\bar{p}^i$ ;
return  $^{(T)}\bar{p}$ ;

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