

∇ ∇^* g

Dual connection ∇^* coupled to (∇, g) :

$$Xg(Y, Z) = g(\nabla_X Y, Z) + g(Y, \nabla_X^* Z)$$

Statistical structure (∇, g) : torsion-free connection ∇

$$(\nabla_X g)(Y, Z) - (\nabla_Y g)(X, Z) = -g(T^\nabla(X, Y), Z)$$

Statistical structure of constant curvature κ :

$$\nabla R(X, Y)Z = \kappa(g(Y, Z)X - g(X, Z)Y)$$

Hessian structure of constant curvature c :

$$(\nabla_X K^{(\nabla, g)})(Y, Z) := (\nabla K^{(\nabla, g)})(Y, Z; X) = -\frac{c}{2}\{g(X, Y)Z + g(X, Z)Y\}$$

Difference tensor field:

$$K(X, Y) := \nabla_X Y - \nabla_X^g Y$$