$$\nabla\text{-geodesic }\gamma_{\nabla}(P,Q;t) = (PQ)^{\nabla}(t)$$

$$(PQ)^{\nabla}(t) = \begin{pmatrix} M_{\mathrm{id}}(\theta(P),\theta(Q);1-t,t) \\ M_{\nabla F^*}(\eta(P),\eta(Q);1-t,t) \end{pmatrix}$$

$$\nabla^*\text{-geodesic }\gamma_{\nabla^*}(P,Q;t) = (PQ)^{\nabla^*}(t)$$

$$(M,g,\nabla,\nabla^*) \qquad (PQ)^{\nabla^*}(t) = \begin{pmatrix} M_{\nabla F}(\theta(P),\theta(Q);1-t,t) \\ M_{\mathrm{id}}(\eta(P),\eta(Q);1-t,t) \end{pmatrix}$$