Hopcroft Karp

```
int N,M,D[MAXV],Pair[MAXV],Q[MAXV];
bool BFS(){
   int u,v,i,f =0,izq=0,der=0;
   FORR(i,N+M) D[i] = 0;
   FOR(i,N)
      if(Pair[i]==-1)
         Q[der++] = i;
   while (izq < der){
      u = Q[izq++];
      for(i=last[u];i ;i=edges[i].next){
         v = edges[i].v;
         if (D[v + N]) continue;
         D[v + N] = D[u] + 1;
         if (Pair[v + N] != -1){
            D[Pair[v + N]] = D[v + N] + 1;
            Q[der++] = Pair[v + N];
         }else f = 1;
      }
   }
   return f;
}
int DFS(int u){
   for(int v,i = last[u]; i; i=edges[i].next){
      v = edges[i].v;
      if (D[v+N] != D[u]+1) continue;
      D[v + N] = 0;
      if (Pair[v + N]==-1 || DFS(Pair[v + N])){
         Pair[u] = v;
         Pair[v + N] = u;
         return 1;
      }
   }
   return 0;
}
int Hopcroft_Karp(){
   int flow=0;
   FORR(i,N+M) Pair[i] = -1;
   while (BFS())
      FOR(i,N)
         if (Pair[i]==-1 &&DFS(i))
            flow++;
   return flow; }
```

Hungarian

```
const ll oo = 1e18;
ll M[16][16]; int n;
// Para minimizar - M[i][j] < 0
ll Hungarian(){
   int p,q;
   ll xx,yy;
   vector<ll> fx(n,oo),fy(n,0);
   vector<int> x(n,-1),y(n,-1);
   for(int i=0;i<n;){
      vector<int> t(n,-1),s(n+1,i);
      for(p=q=0;p<=q && x[i]<0;++p)
         for(int k=s[p],j=0;j<n && x[i]<0;++j)
            if(fx[k]+fy[j]== M[k][j] && t[j]<0){
               s[++q]=y[j],t[j]=k;
               if(s[q]<0)
                  for(p=j;p>=0;j=p)
                     y[j] = k = t[j],
                     p = x[k],x[k]=j;
            }
      if(x[i]<0){
         yy = oo;
         FOR(k,q+1) FOR(j,n)
            if(t[j]<0)
              yy=min(yy,(fx[s[k]]+fy[j]-
                         M[s[k]][j]));
         FOR(j,n)
            fy[j] += (t[j]<0 ? 0:yy);
         FOR(k,q+1) fx[s[k]] -=yy;
      } else i++;
   }
   xx = 0;
   FOR(i,n)
      xx += M[i][x[i]];
   return -xx;
}
```

Max Flow Min Cost

```
int F[MAXV],Prev[MAXE];
ll D[MAXV],Phi[MAXV];
backEdge ( cap=0,cost = -cost )
Phi[i] = 0
bool Dikjstra()
   F[i] = D[s] = 0
```

```
   F[s] = D[i] = oo
   D[u] > D[v] + edges[i].cost + Phi[v] - Phi[u]
      F[u] = min(F[v] , edges[i].cap)
      Prev[u] = i

ll MAX_FLOW_MIN_COST(){
   ll cost = 0,flujo = 0; int i;
   while(Dikjstra()){
      cost += (D[t] + Phi[t]) * F[t];
      flujo += F[t];
      FOR(i,n)
         if(F[i])
            Phi[i] += D[i];
      for(i = t; i != s; i = edges[Prev[i]].src){
         edges[Prev[i]].cap  -= F[t];
         edges[Prev[i]^1].cap+= F[t];
      }
   }
   return cost;
}
```

Kth Shortest Path

```
int n, d[MAXN]; bool marcas[MAXN];
Graph g,gt;
int k_shortestPath(int s, int t, int k){
   int i,u,v,p,pv;
   for(i=0;i<n;i++)
      d[i]=oo, marcas[i]=0;
   d[t] = 0;
   priority_queue<Arco> Q;
   Q.push(Arco(t, t, 0));
   while (!Q.empty()) {
      v = Q.top().u; Q.pop();
      if (marcas[v]) continue;
      marcas[v] = 1;
      for(i=gt[v].size()-1;i>=0;i--){
         u =gt[v][i].u;
         p = gt[v][i].p;
         if (d[u] > d[v] + p) {
            d[u] = d[v] + p;
            Q.push(Arco(v, u, d[u]));
         }
      }
   }
   int l = 0;
   Q.push(Arco(-1,s,0));
   while (!Q.empty()) {
      v = Q.top().u;
      pv = Q.top().p;  Q.pop();
      if (v == t && ++l == k)
        return pv + d[s];
      for(i=g[v].size()-1;i>=0;i--){
         u = g[v][i].u;
         p = g[v][i].p;
         Q.push(Arco(v,u,pv+p-d[v]+d[u]));
      }
   }
   return -1;
}
```

Puntos Articulacion y CompBiConexas

```
int ndfs[MAXN], low[MAXN], pila[MAXN], top;
bool Art[MAXN];
vector<vector<int> > bi;

void Tarjan(int v, int cnt) {
   int part = cnt > 1, u,i;
   pila[top++] = v;
   ndfs[v] = low[v] = cnt;
   for(i=last[v];i ;i=edges[i].next) {
      if (!ndfs[ u = edges[i].v ]) {
         Tarjan(u, cnt + 1);
         low[v] = min(low[v], low[u]);
         if (low[u] >= ndfs[v]) {
            Art[v] = ++part == 2;
            vector<int> A;
            A.push_back(v);
            pila[top]=0;
            while(pila[top]!= u)
               A.push_back(st[--top]);
            bi.push_back(A);
         }
      } else if (ndfs[u] != ndfs[v] - 1)
         low[v] = min(low[v], ndfs[u]);
   }
}
void ArtPoint_CompBiconex(int N) {
   FOR(i,N)
```

```
      Art[i] = ndfs[i] = low[i] = 0;
   bi.clear();
   top=0; FOR(i,N)
      if (!ndfs[i])
         Tarjan(i, 1);
}
```

Bridges y CompBiconexas

```
int num[MAXN], inS[MAXN];
vector< pair<int,int> > brdg;
vector< vector<int> > tecomp;
int S[MAXN],roots[MAXN];
int n,ndfs,topS,topR;
int i,m;

void visit(int v, int u) {
   inS[v] = num[v] = ++ndfs;
   S[topS++] = roots[topR++] = v;
   for(int i=last[v];i;i=edges[i].next){
      int w = edges[i].v;
      if (!num[w])
         visit(w, v);
      else if (u != w && inS[w])
         while (num[roots[topR-1]] > num[w])
            topR--;
   }
   if (v == roots[topR - 1]) {
      brdg.push_back(make_pair(u,v));
      tecomp.push_back(vector<int>());
      while (1) {
         int w = S[--topS];
         inS[w] = false;
         tecomp.back().push_back(w);
         if (v == w) break;
      } topR--;
   }
}
void Bridges_CompBiCnx() {
   FOR(i,n)
      num[i] =inS[i] = 0;
   topS = topR = 0;
   brdg.clear(); tecomp.clear();
   ndfs = 1;
   FOR(i,n) if (!num[i]) {
      visit(i, n);
      brdg.pop_back();
   }
}
```

LCA

```
// T[i] - Padre de i
int N,T[MAXN], P[MAXN][20],L[MAXN];
void Preprocesar(int *T){
   FOR(i,N)
      for(int j=0; 1<<j < N;j++)
         P[i][j] = -1;
   FOR(i,N) P[i][0] = T[i];
   for(int j = 1; 1<<j <N; j++)
      FOR(i,N)
         if(P[i][j - 1]!= -1)
            P[i][j]=P[P[i][j-1] ][j-1];
}

int QUERY(int p, int q){
   int log=1;
   if(L[p] < L[q]) swap(p,q);
   while(1<<log <= L[p]) log++;
   log--;
   FORR(i,log)
      if (L[p] - (1 << i) >= L[q])
         p = P[p][i];
   if (p == q) return p;
   FORR(i,log)
      if (P[p][i] != -1 && P[p][i] != P[q][i])
         p = P[p][i], q = P[q][i];
   return T[p];
}
```

SCC

```
bool visit[MAXV], mark[MAXV];
int lowlink[MAXV],vlink[MAXV],ndfs, pila[MAXV],top;
void Tarjan(int u){
   vlink[u]=lowlink[u]=ndfs;
   visit[u]=mark[u]=ndfs++;
   pila[top++] = u;
   for(int v,i=last[u];i ;i=edges[i].next)
      if(!visit[ v = edges[i].v]){
         Tarjan( v );
         lowlink[u] = min(lowlink[u],lowlink[v]);
```

```
      } else
         if (mark[ v ])
            lowlink[u] = min(lowlink[u],vlink[v]);
      // Componente X
   while(vlink[u] == lowlink[u]){
      int v = pila[--top];
      mark[v] = false;
      if(v == u) break;
   }
}
void SCC(){
   ndfs = top = 1;
   FOR(i,N)
      visit[i]= false;
   FOR(i,N)
      if (!visit[i])
         Tarjan(i);
}
```

GCD Extendido

```
ll GCDext(ll a, ll b, ll &x, ll &y){
   ll g = a; x = 1 ; y = 0;
   if (b != 0){
      g = GCDext(b, a % b, y, x);
      y -= (a / b) * x;
   }
   return g;
}
```

Inverso Modular

```
ll invMod(ll a, ll m, ll &inv) {
   ll x, y;
   if (GCDext(a, m, x, y) != 1)
         return 0 ; // noSolucion
   inv = (x + m) % m;
   return 1;
}
```

Teorema del Resto Chino

```
// x = a[i] mod m[i]
// if GCD(m[i],m[j]) != 1 -> noSolucion
int RestoChino(int n,ll *a,ll *m,ll *x){
   ll K = 1, inverso;  *x = 0;
   FOR(i,n) K *= m[i];
   FOR(i,n){
      invMod(K/m[i],m[i],inverso);
      *x += a[i]* K/m[i]* inverso;
   }
   *x %= K;
   return 1; // Tiene sol
}
```

Euler Totient Function

```
ll Euler_Totient_Function(ll n){
   ll ans = n;
   for(ll i=2;i*i<= n;i++){
      if(n %i==0) ans -= ans/i;
      while(n%i==0) n/=i;
   }
   if(n>1) ans -=ans/n;
   return ans;
}
```

Hungarian Extendido

```
int N,M,cx[MAX],cy[MAX],w[MAX][MAX];
// T[i][j] = cant de x para y
// w[i][j] = -w[i][j] para Minimizar
int T[MAX][MAX];
int lx[MAX],ly[MAX];
int S[MAX],SX[MAX],P[MAX];
void Inicializar(){
   FOR(i,N){
      lx[i]= -oo;
        FOR(j,M){
         if(lx[i]<w[i][j])
            lx[i]= w[i][j];
         T[i][j]= 0;
        }
   }
   FOR(i,M) ly[i]= 0;
}
int HungarianExt(){ // 1
   Inicializar();
   int delta,f,j;
   bool found,vx[MAX],vy[MAX];
   FOR(u,N) while(cx[u]){ // 2
      FOR(i,N) vx[i]=0, P[i] = -1;
      FOR(i,M){ // 3
         vy[i]=0 , SX[i]=u;
         S[i] = lx[u]+ ly[i] -w[u][i];
      } // 3
```

```
      while(vx[u] = 1){ // 4
         delta = oo,found = 0;
         FOR(i,M) if(!vy[i]){ // 5
            delta = min(S[i],delta);
            if(S[i] == 0){ // 6
               vy[i] = 1;
               if(cy[i]){ // 7
                  f = min(cx[u],cy[i]);
                  for(j=SX[i];P[j]!=-1;j =SX[P[j]])
                     f= min(f, T[j][P[j]]);
                  cx[u] -=f, cy[i] -=f;
                  j= i; while(j!=-1){ // 8
                     T[SX[j]][j] += f;
                     if(P[SX[j]] != -1)
                        T[SX[j]][P[SX[j]]] -=f;
                     j= P[SX[j]];
                  } // 8
                  found = 1;
               }else  // 7
                 FOR(j,N)
                   if(!vx[j] && T[j][i]){ // 9
                     P[j]=i,vx[j]= 1;
                     FOR(k,M) if (!vy[k])
                      if(S[k]>lx[j]+ly[k]-w[j][k]){
                         S[k]= lx[j]+ly[k]-w[j][k];
                         SX[k]= j;
                       }
                    } // 9
         break;}  } // 6 5
         if(found) break;
         if(delta){
            FOR(i,N) if(vx[i]) lx[i] -=delta;
            FOR(i,M) if(vy[i]) ly[i] +=delta;
            else
               S[i] -=delta;
         }
   }  } // 4 2
   delta = 0;
   FOR(i,N) FOR(j,M)
      delta -= T[i][j]*w[i][j];
   return delta;
}
```

Sieve Atkin

```
void Sieve_Atkin(int N) {
   FAB(x,1,sqrtN+1) FAB(y,1,sqrtN+1){
         int n = 4*x*x + y*y;
         if (n<=N && (n%12==1||n%12==5))
            isprime[n] ^= 1;
         n =3*x*x +y*y;
         if(n<=N && n%12==7)  isprime[n] ^= 1;
         n = 3*x*x - y*y;
         if (n<=N && x > y && n%12==11)
            isprime[n] ^= 1;
      } isprime[2] = isprime[3] = true;
   for(int k,n=5; n <= sqrtN; ++n)
      if(isprime[n]) while((k+=n*n)<=N)
            isprime[k] = false;
}
```

Edmons

```
int n, NewBase,Start, match[MAXN];// match[i]!=0
int izq,der,Q[MAXN],P[MAXN], C[MAXN];
bool marcas[MAXN] , X[MAXN];
int LCA(int u, int v) {
   memset(X,0,sizeof(X));
   while (true) {
      u = C[u], X[u] = 1;
      if (u == Start) break;
      u = P[match[u]];
   }
   while (1)
      if(X[v = C[v]]) break;
      else v = P[match[v]];
   return v;
}
void ResetTrace(int u) {
   while (C[u] != NewBase) {
      int v = match[u];
      X[C[u]] = X[C[v]] = 1;
      u = P[v];
      if(C[u] != NewBase)   P[u] = v;
   }
}
void BlossomContract(int u, int v) {
   NewBase = LCA(u, v);
   memset(X, 0, sizeof(X));
```

```
   ResetTrace(u), ResetTrace(v);
   if (C[u] != NewBase) P[u] = v;
   if (C[v] != NewBase) P[v] = u;
   for(u = 1; u <= n; u++)
      if (X[C[u]]) {
         if (!marcas[u]) Q[der++]=u;
         marcas[u] = C[u] = NewBase;
      }
}
int FindPath() {
   izq=0,der=0;
   for(int u=1; u<=n;u++)
      C[u]=u, marcas[u] =P[u]=0;
   marcas[Start] = 1;
   Q[der++]=Start;
   while (izq<der) {
      int u = Q[izq++];
      for(int i=last[u];i ;i=edges[i].next){
         int v =edges[i].v;
         if(C[u] !=C[v]&& match[u]!=v)
         if(v==Start ||(match[v] &&P[match[v]]))
            BlossomContract(u, v);
         else if (!P[v]) {
            P[v] = u;
            if (!match[v]) return v;
            marcas[ match[v] ] = 1;
            Q[der++]=march[v];
         }
      }
   }
   return 0;
}
void Aumentar(int u) {
   int v, w; while (u) {
      v = P[u], w = match[v];
      match[v] = u,match[u] = v;
      u = w;
   }
} void Edmonds() {
   memset(match, 0, sizeof(match));
   for(Start= 1;Start<= n;Start++)
      if (!match[Start])
         Aumentar( FindPath() );
}
```

Newton Raphson

```
double NewtonRaphson(double n){
   double x = 1, nx;
   while (true) {
      nx = (x + n / x) / 2;
      if (fabs(x-nx) < EPS) break;
      x = nx;
   }
   return x;
}

int NewtonRaphson(int n){
   int a = 1; bool low = 0;
   while(1) {
      int nx=(a+n/a)/2;
      if (a==nx || (nx>a &&low))
         break;
      low =nx<a, a=nx;
   }
   return a;
}
```

Index Permutation

```
ll fact[21];
int alpha[30]; // Ya Normalizado
ll IndexPermutation(int *per,int n,int dif){
   //n=len, dif -elems diferentes
   memset(alpha,0,sizeof(alpha));
   FOR(i,n) alpha[per[i]]++;
   ll sol = 0, par;
   FOR(i,n-1){
      FAB(j,1,per[i]){
         if(!alpha[j]) continue;
            par = fact[n-i-1];
            for(int k=1;k <= dif;k++)
               par /=fact[alpha[k]-(k==j)];
            sol += par;
      }
      --alpha[per[i]];
   }
   return sol;
}
```

Complex

```
inline P operator*(const P b)
   {return P(x*b.x-y*b.y , x*b.y + y*b.x );}

inline P operator/(const P b){
   P s = P( x*b.x + y*b.y , y*b.x-x*b.y);
   s.x /=  ( b.x*b.x + b.y*b.y);
   s.y /=  ( b.x*b.x + b.y*b.y);
   return s;
}
```

```
int Combinatoria (int n, int k) {
   double res = 1;
   for (int i = 1; i <= k; + + i)
      res = res * (n - k + i) / i;
   return (int) (res + 0,01);
}
```

Tiling Dominoes

```
double res = 1;
for(double i = 1;i<=n;i++)
   for(double j = 1;j<=k;j++){
      double x = 4*cos(PI*i/(n+1))*cos(PI*i/(n+1));
      x += 4*cos(PI*j/(k+1))*cos(PI*j/(k+1));
      res *= pow(x,0.25);
   }
(ll)(res+0.000001);
```

Digitos de N!, n > 3

```
0.5*log10(2*n*PI)+n*log10(n/M_E)+1;
```

Miller Rabin

```
ll multMOD(ll x,ll y,ll mod){ //(x*y)%mod
   ll rx = 0;  x %= mod, y %= mod;
   for (int bx = 0; y >> bx; bx++){
      if(bx) x = x + x;
      if(x >= mod) x -= mod;
      if((y >> bx) & 1) rx += x;
      if (rx >= mod) rx -= mod;
   }
   return rx;
}
ll powMOD(ll a,ll b,ll mod){//(x^y)%mod
   ll rx = 1;
   for(int bx = 0;b; b>>=1,bx++){
      if(bx) a = multMOD(a,a,mod);
      if (b & 1)
         rx = multMOD(rx,a,mod);
   }
   return rx;
}
ll f(ll x,ll mod){
   ll rx= multMOD(x,x,mod) + 123;
   while(rx >= mod) rx -= mod;
   if(!rx) rx = 2;
   return rx;
}
bool Miller_Rabin(ll n ,ll iter){
   ll m = n-1,b=2,z; int j,a=0;
   while(!(m&1)) m>>=1, ++a;
   while(iter--){
      j =0; z = powMOD(b,m,n);
      while(!(( !j && z==1)|| z==n-1))
         if((j > 0 && z==1)|| ++j==a)
            return 0;
         else z = powMOD(z,2,n);
      b = f(b,n);
   }
   return 1;
}
bool is_prime(ll n){
   if (n == 2) return true;
   return n>1 && (n & 1) && Miller_Rabin(n, 1);
}
```

Pollard_Rho

```
ll factores[70]; int nfactor;
ll  pollard_rho(ll c, ll num){
   ll x = rand() % num;
   ll i=1, k=2, y=x,comDiv;
   do { i++;
      if((x =multMOD(x, x, num)-c)<0)
         x += num;
      if(x == y) break;
      comDiv =GCD((y-x +num) %num,num);
```

```
      if(comDiv > 1 && comDiv < num )
         return comDiv;
      if(i ==k){
         y = x; k <<= 1;
      }
   }while ( true );
   return num;
}

void fFindFactor(ll num){
   if ( is_prime(num) ){
      factores[nfactor++] = num;
      return;
   }
   ll factor = num + 1;
   while(factor >= num)
      factor= pollard_rho(rand()%(num-1)+ 1,num);
   fFindFactor(factor);
   fFindFactor(num / factor);
}
```

Stable Matching

```
vector<int> stable_matching () {
   vector<vector<int> > aux(N,vector<int>(N+1,N));
   vector<int> matchW(N,N),proposedM(N);
   FOR(i,N)FOR(j,N)
      aux[i][orderW[i][j]]=j;
   FOR(i,N) FAB(j,i,N){
     int w=orderM[j][proposedM[j]++ ];
     if(aux[w][j] <aux[w][matchW[w]])
       swap(j,matchW[w]);
   }
   return matchW;
}
```

Geometria Computacional

```
const double EPS = 1e-8;
const double oo = 1e12;
const double PI = 3.141592653589793;
#define X real()
#define Y imag()
typedef complex<double> P;
typedef vector<P> Pol;

struct circle{
   P p; double r;
   circle(){}
   circle(P x,double rr){
      p=x, r = rr;
   }
};
struct L: public vector <P>{ //Linea
   L (P a, P b){
      push_back(a); push_back(b);
 }};
inline bool operator<(const P a, const P b){
   return a.X!=b.X ?a.X<b.X :a.Y <b.Y;
}
double cross(P a, P b){//1
   return imag(conj(a) * b);
}
double dot(P a, P b){//2
   return (conj(a)*b).X;
}
//Orientacion de 3 puntos
int ccw(P a, P b, P c){ //3,1 2
   b-=a; c-=a;
   if(cross(b,c)>0) return +1;
   if(cross(b,c)<0) return -1;
   if(dot(b,c)<0) return +2;//c-a-b line
   if(norm(b)<norm(c)) return -2;//a-b-c line
   return 0;
}
//Interseccion de 2 rectas
bool intersectLL (L l, L m){//4,1
      //non-parallel
   return abs(cross(l[1]-l[0], m[1]-m[0])) > EPS
         || abs(cross(l[1]-l[0], m[0]-l[0])) < EPS;
} //same-line

//Punto interseccion recta recta
P crosspoint(L l, L m){ //5,1
   double A = cross( l[1]-l[0], m[1]-m[0]);
   double B = cross( l[1]-l[0], l[1]-m[0]);
   if(abs(A)<EPS && abs(B)<EPS)
      return m[0]; //Same line
   if(abs(A)<EPS) return P(0,0);//parallels
   return m[0] + B / A * (m [1] - m [0]);
```

```
}
//Interseccion recta y segmento
bool intersectLS (L l, L s){//6, 1
      //s[0] is left of l
   return cross(l[1]-l[0], s[0]-l[0]) *
      cross(l[1]-l[0],s[1]-l[0])<EPS;
} //s[1] is right of l

//Interseccion recta y punto
bool intersectLP (L l, P p){//7,1
   return abs(cross(l[1]-p, l[0]-p))<EPS;
}
//Interseccion de 2 segmento
bool intersectSS (L s, L t){//8,3
   FOR(i,2)FOR(j,2) if(abs(s[i]-t[j])<EPS)
      return 1;  // same point
 return ccw(s[0],s[1],t[0])*ccw(s[0],s[1],t[1])<=0
    && ccw(t[0],t[1],s[0])*ccw(t[0],t[1],s[1])<=0;
}

//Interseccion segmento y punto
bool intersectSP (L s,P p){//9
   double a=abs(s[0]-p)+abs(s[1]-p);
   return a-abs(s[1]-s[0])<EPS;
}
//Interseccion circulo circulo
pair<P, P> intersectCC(circle a,circle b) {
   P x= b.p - a.p;
   P A= conj(x), C = a.r*a.r*(x);
   P B= (b.r*b.r-a.r*a.r-(x)*conj(x));
   P D= B*B-4.0*A*C;
   P z1= (-B+sqrt(D)) / (2.0*A) +a.p;
   P z2= (-B-sqrt(D)) / (2.0*A) +a.p;
   return pair<P, P>(z1, z2);
}
//Proyeccion punto recta
P projection(L l,P p){//10,2
  double t=dot(p-l[0], l[0]-l[1])/norm(l[0]-l[1]);
  return l[0] + t*(l[0]-l[1]);
}

//Reflexion punto recta
P reflection(L l, P p){//11, 10
   return p +(P(2,0) *(projection(l,p)-p));
}

//Distancia recta punto
double distanceLP(L l,P p){//12, 10
   return abs(p - projection(l,p));
}

//Distancia recta recta
double distanceLL(L a, L b){//13,4 12
   if(intersectLL(a,b)) return 0;
   return distanceLP(a,b[0]);
}
//Distancia recta segmento
double distanceLS(L l, L s){//14,7 12
  if(intersectLS(l,s)) return 0;
  return
min(distanceLP(l,s[0]),distanceLP(l,s[1]));
}

//Distancia segmento punto
double distanceSP(L s, P p){//15, 10 9
   const P r = projection(s,p);
   if (intersectSP(s,r)) return abs(r-p);
   return min( abs(s[0]-p), abs(s[1]-p) );
}

//distancia segmento segmento
double distanceSS (L s, L t) {//16,8 15
   if (intersectSS(s, t)) return 0;
   double a=oo,b=oo;
   FOR(i,2) a=min(a, distanceSP(s,t[i]));
   FOR(i,2) b=min(b, distanceSP(t,s[i]));
   return min(a,b);
}

//Centro de circunferencia dado 3 puntos
P circunferenceCenter(P a, P b, P c){//17
   P x =1.0/conj(b-a), y=1.0/conj(c-a);
   return (y-x)/(conj(x)*y-x*conj(y)) +a;
}
double anguloEjeX(P a){//18,1 2
   P b = P(1,0);
   if(dot(b,a)/(abs(a)*abs(b))==1) return 0;
   if(dot(b,a)/(abs(a)*abs(b))==-1) return PI;
```

```
   double aux=asin(cross(b,a)/(abs(a)*abs(b)));
   if(a.X<0 && a.Y>0) aux+=PI/2;
   if(a.X<0 && a.Y<0) aux-=PI/2;
   if(aux<0) aux += 2*PI;
   return aux;
}

double anguloEntreVectores(P a, P b){//19,18
   double aa = anguloEjeX(a);
   double bb = anguloEjeX(b);
   double r = bb - aa;
   if (r<0) r+=2*PI;
   return r;
}

double anguloEntre3Puntos(P a, P b, P c){//20,19
   a-=b; c-=b;
   return anguloEntreVectores(a,b);
}

Pol convexHull(Pol ps){//21,3
  int t,i,n = ps.size(), k=0;
  if (n < 3) return ps;
  sort(ps.begin(), ps.end());
  Pol ch (2*n);
  for(i=0;i<n;ch[k++]=ps[i++]) //lower
  while(k>=2 && ccw(ch[k-2],ch[k-1],ps[i])<=0) --k;
  for(i=n-2,t=k+1 ;i>=0; ch[k++]=ps[i--])// upper
 while(k>=t && ccw(ch[k-2],ch[k-1], ps[i])<=0) --k;
  ch.resize(k-1);
  return ch;
}

int pointInPolygon(Pol pol, P p){//22, 1 2
   bool in = false; int n=pol.size();
   FOR(i,n){
      P a= pol[i] - p, b= pol[(i+1)%n]-p;
        if(a.Y > b.Y) swap(a,b);
        if(a.Y<=0 && 0 < b.Y)
          if (cross(a,b)<0) in = !in;
          if(abs(cross(a,b))<=EPS &&dot(a,b)<=0)
            return true; // ON
   }
   return in; // IN | OUT
}
pair <P,P> closestPair (Pol p) {//23
   int i,n = p.size(), s=0, t=1, m=2;
   vector<int> S(n);  S[0]=0, S[1]=1;
   sort(p.begin(), p.end());
   double d = norm(p[s]-p[t]);
   for(i =2;i<n; S[m++]=i++)
      FOR(j,m){
         if(norm(p[S[j]]-p[i])<d)
            d=norm(p[s=S[j]]-p[t = i]);
         if(p[S[j]].X < p[i].X-d)
            S[j--] = S[--m];
   }
   return make_pair( p[s], p[t] );
}

//max distance pair points, O(n)
double diameter(Pol pt) {//24, 1
   int is=0,js=0, n=pt.size();
   FAB(i,1,n){
      if(pt[i].Y >pt[is].Y) is=i;
      if(pt[i].Y <pt[js].Y) js=i;
   }
   double maxd=norm(pt[is]-pt[js]);
   int i,maxi,j,maxj;
   i = maxi = is;  j = maxj = js;
   do {
     if(cross(pt[(i+1)%n]-pt[i],
              pt[(j+1)%n]-pt[j])>=0)
       j=(j+1)%n; else i=(i+1)%n;
      if (norm(pt[i]-pt[j])>maxd){
         maxd =norm(pt[i]-pt[j]);
         maxi=i; maxj=j;
  } }while(i!=is || j!=js);
   return maxd;
}
double area(Pol pol) {//25, 1
   double A=0; int n=pol.size();
   FOR(i,n)
      A+=cross(pol[i],pol[(i+1)%n]);
   return A/2;
}
```

```
struct KDtree {
   struct Node {
      P p; Node *l, *r; Node(P pp){
         p=pp,l=r =NULL;
   }} *root;
   KDtree(){ root = NULL; }
   #define cmp(d,p,q) (d ? p.X<q.X :p.Y<q.Y)
   void insert(P p)
   {   root=insert(root,0,p); }
   void search(P ld,P ru,vector<P> &out)
   {   search(root, 0 , ld, ru, out); }

   Node *insert(Node *t,int d,P p) {
      if (t == NULL)
         return new Node(p);
      if(t->p == p) return t; // Rep
      if (cmp(d,p,t->p))
         t->l = insert(t->l, !d, p);
      else t->r = insert(t->r, !d, p);
      return t;
   }
  void search(Node *t,int d,P ld,P ru,
              vector<P> &out){
      if (t== NULL) return;
      P p = t->p;
      if(ld.X <= p.X && p.X <= ru.X)
         if(ld.Y <= p.Y && p.Y <= ru.Y)
            out.push_back(p);
      if(!cmp(d,p,ld))
         search(t->l, !d, ld, ru, out);
      if(!cmp(d,ru,p))
         search(t->r, !d, ld, ru, out);
   } };
```

Minimal Enclosing Circle

```
double distSqr(P &p1, P &p2){
   return (p1.X-p2.X)*(p1.X-p2.X) +
          (p1.Y-p2.Y)*(p1.Y-p2.Y);
}
bool contain(circle c,P p){
   return distSqr(c.p,p)<= c.r*c.r;
}
circle findCircle(P a,P b){
   P p( real(a+b)/2.0 , imag(a+b)/2.0);
   return circle( p, sqrt(distSqr(a,p)));
}
circle findCircle(P pa,P pb,P pc) {
   double a,b,c,x,y,r,d;
   c = sqrt(distSqr(pa , pb));
   b = sqrt(distSqr(pa , pc));
   a = sqrt(distSqr(pb , pc));
   if (b==0 || c==0 || a*a>= b*b+c*c)
      return findCircle(pb,pc);
   if (b*b >= a*a+c*c)
      return findCircle(pa,pc);
   if (c*c >= a*a+b*b)
      return findCircle(pa,pb);
   d = real(pb-pa)*imag(pc-pa);
   d = 2 * (d - imag(pb-pa)*real(pc-pa));
   x = (imag(pc-pa)*c*c-imag(pb-pa)*b*b)/d;
   y = (real(pb-pa)*b*b-real(pc-pa)*c*c)/d;
   x += real(pa), y += imag(pa);
   r= sqrt(pow(real(pa)-x,2)+ pow(imag(pa)-y,2));
   return circle(P(x,y),r);
}

P points[MAXN], R[3];
circle sed(int n,int nr){
   circle c;
   if(nr == 3)
      c = findCircle(R[0],R[1],R[2]);
   else if (n == 0 && nr==2)
      c = findCircle(R[0], R[1]);
   else if(n==1 && nr == 0)
      c = circle(points[0],0);
   else if(n == 1 && nr == 1)
      c = findCircle(R[0],points[0]);
   else{
      c = sed(n-1, nr);
      if(!contain(c,points[n-1])){
         R[nr++] = (points[n-1]);
         c = sed(n-1, nr);
      }
   }
   return c;
}
```

Range Minimum Query

```
int DP[ MAXN ][20];
void RMQ(){
   int i,j,k;
   FOR(i,N) DP[i][0] = i;
   for(j=1;(1<<j)<=N;j++)
      for(i=0;i+(1<<j)-1<N;i++){
         k=DP[i+(1 << (j-1))][j-1];
         if (A[DP[i][j-1]]< A[k])
            k = DP[i][j-1];
         DP[i][j]= k;
      }
}
int QUERY(int a,int b){
   int k,m; if(a==b) return A[a-1];
   for(k=0;(1<<k)<(b-a+1);k++);
   k--; a--; b--;
   m = DP[b-(1<<k)+1][k];
   return min(A[DP[a][k]],A[m]);
}
```

Salto del Caballo

```
ll SaltoCaballo(ll x1,ll y1,ll x2,ll y2){
      ll dx =abs(x2-x1);
      ll dy =abs(y2-y1);
      ll lb= max(dx+1 , dy + 1)/2;
      lb = max(lb, (dx + dy + 2)/3);
      while((lb % 2) != (dx+ dy)%2) lb++;
      if(abs(dx)==1 && !dy) return 3;
      if(abs(dy)==1 && !dx) return 3;
      if(abs(dx)==2 && abs(dy)==2) return 4;
      return lb;
}
```

Day Of Week

```
int DayOfWeek(int d, int m, int y){
   if(m<3) y--, m+=10; else m -=2;
   int c= y/100; y %= 100;
   c =y- 2 * c+ d+ y/4 +c/4;
   return((int)(2.6*m-0.2)+c+7)%7;
}
```

Catalan

```
C[n] => FOR(k=0,n-1) C[k] * C[n-1-k]
C[n] => Comb(2*n,n) / (n + 1)
C[n] => 2*(2*n-3)/n * C[n-1]
```

Fact Mod

```
int factMod (int n, int p) {
   int res = 1,i;
   while (n > 1) {
      if ((n/p) & 1)
      res = (res * (p-1)) % p;
      for (i=n%p; i > 1;i--)
         res = (res * i) % p;
      n /= p;
   }
   return res % p;
}
```

Fibonacci

-Sumatoria de F[1..n]=F[n+2]-1.
- Si n es divisible por m entonces Fn es divisible por Fm
- Los nmeros consecutivos de Fibonacci son primos entre si.
- Si N es Fibonacci => (5*N*N + 4 || 5*N*N 4) es un cuadrado
- Suma de n terminos partiendo del k-simo + k = F[k+n+1]
- gcd(F[p], F[n]) = F[gcd(p,n)] = F[1] = 1
- Cantidad num fibonacci hasta n
  floor((log10(n)+ (log10(5)/2))/log10(1.6180));

```
//      _    _ ^ n    _                  _
//a b | 0 1 | = |fib(n-1) fib(n)    |
//c d |_0 1_|   |_fib(n)  fib(n+1)_|

struct matrix{
ll a, b, c, d;
   matrix(ll a, ll b, ll c, ll d) :
      a(a), b(b), c(c), d(d) {}
   const matrix operator*(const matrix &t){
      ll A =a*t.a+ b*t.c;
      ll B =a*t.b+ b*t.d;
      ll C =c*t.a+ d*t.c;
      ll D =c*t.b+ d*t.d;
      return matrix(A,B,C,D);
```

```
    }
};
matrix pow(const matrix &p, int n){
    if (n == 1) return p;
    matrix k = pow(p, n/2);
    matrix ans = k*k;
    if (n & 1) ans = ans * p;
    return ans;
}
```

Kth Permutacion

```
int N; // N grupos
char grupo[22];//caract del grupo
int cantgrupo[22], quitar;
//FOR(i,N) quitar *= fac[cantgrupo[i]]
void KthPermutacion(int k,int quedan){
    if (quedan == 0) return;
    int total = fact[quedan - 1];
    int inicio = 0, fin = 0;
    FOR(i,N){
        if (cantgrupo[i] == 0) continue;
        fin += (cantgrupo[i] * total) / quitar;

        if (fin > k){
            quitar /= cantgrupo[i]--;
            cout << grupo[i];
            KthPermutacion(k-inicio,quedan-1);
        }
        else inicio = fin;
    }
}
```

TREAP

```
srand( time( 0 ) );
#define size(r) buff[r].ch[2]
#define hijo(r,i) buff[r].ch[i]
#define PR(r) buff[r].ch[4]
#define key(r) buff[r].ch[3]
struct Treap {
    struct Nodo {
        int ch[5];
        Nodo() {}
        Nodo( int key ){
            ch[0]=ch[1]=0, ch[4]=rand();
            ch[2]=1, ch[3]=key;
        }
    } buff[MAXNODES];
    int root, nodes;
    void update_size( int root ) {
        size(root) = 1 +
        size(hijo(root,0))+ size(hijo(root,1));
    }
    void rotate(int &root,bool dir) {
        int tmp = hijo(root,dir);
        hijo(root,dir)= hijo(tmp,1 - dir);
        hijo(tmp,1-dir)= root;
        update_size(root);
        update_size(tmp);
        root = tmp;
    }
    void insert(int &root,int val){
        if ( root == 0 ) {
            buff[root= ++nodes]=Nodo(val);
            return;
        }
        if (val == key(root)) return;
        bool dir = !( val < key(root) );
        insert( hijo(root,dir), val );
        if(PR(root) >PR(hijo(root,dir)))
            rotate( root, dir );
        update_size( root );
    }

void erase(int &root,int val){
        if (root==0 ) return;
        if ( val != key(root)) {
        bool dir= !(val<key(root));
        erase( hijo(root,dir), val );
    } else {
        int L = hijo(root,0);
        int R = hijo(root,1);
        if (L) if(R)
            rotate(root, PR(L)>PR(R));
        else rotate(root,0);
        else if(R) rotate(root,1);
        else { root = 0; return ; }
        erase( root, val );
```

```
      }
      update_size( root );
   }
   int countLessThan(int root,int val){
      int cant = 0;
      while(root) {
         bool dir= !(val<key(root));
         if( dir ) {
            cant+=size(hijo(root,0));
            if(val<=key(root))
               return cant;
            cant++;
         }
         root = hijo(root,dir);
      }
      return cant;
   }
   int findKth( int root, int kth ) {
      while(root) {
         int v=hijo(root,0);
         if(kth< size(v)) root=v;
         else {
            kth -=size(v)+ 1;
            if(kth <0) return key(root);
            root=hijo(root,1);
         }
      }
      return -1;
   }
};
```

KMP

```
int pi[MAXN]; // prefix function
void PreKMP(char *P,int n){
   int q,k=0; pi[1] = 0;
   for(q =2;q <=n; pi[q++] =k){
      while(k && (P[k]!=P[q-1]))
         k=pi[k];
      if(P[k]==P[q-1]) k++;
   }
}
void KMP(char *T,int n,char *P,int m){
   int i,q=0; PreKMP(P,m);
   for(i=1;i <= n;i++){
      while((q>0) && (P[q]!=T[i-1]))
         q = pi[q];
      if(P[q]==T[i-1]) q++;
      if(q==m) q = pi[q];//found
   }

}
```

Manacher

```
int rad[2*MAX];
void Manacher(char *s,int n){
   int i=0,j=0,k;
   while(i < 2 * n - 1 ) {
      while(i >= j && i+j+1< 2*n &&
         s[(i-j)/ 2]==s[(i+j+1)/2])
         j++;
      rad[i] = j, k = 1;
        while(k <=rad[i] && rad[i-k]!=rad[i]-k){
         rad[i+k ]=min(rad[i-k],rad[i]-k);
             k++;
        }
      j = max(j-k,0),i +=k;
   }
}
```

ZAlgorithm

```
int Z[MAX]; // Z[i]=SA[i]%SA[0]
void zAlgorithm(char *S,int n){
   int g=0,f=0; Z[0] = n;
   FAB(i,1,n)
      if(i<g && Z[i-f]!=(g-i))
         Z[i]=min(Z[i-f],g-i);
      else{
         g = max(g, f = i);
         while(g<n && S[g]==S[g-f]) g++;
         Z[i] = g - f;
      }
}
```

Suffix Array

```
int wa[MAXN], wb[MAXN], we[MAXN], wv[MAXN];
int SA[MAXN];
int cmp(int *r,int a,int b,int l){
   return r[a]==r[b] && r[a+l]==r[b+l];
}
void SuffixArray(char *cad, int N) {
```

```
   N++; int j, p, *x=wa, *y=wb,range=256;
   memset(we, 0, range*sizeof(int));
   FOR(i,N) we[x[i]=cad[i]]++;
   FAB(i,1,range) we[i]+=we[i-1];
   FORR(i,N-1) SA[--we[x[i]]]=i;
   for(j=p=1; p<N; j<<=1, range = p) {
      p=0; FAB(i,N-j,N) y[p++]=i;
      FOR(i,N) if (SA[i]>=j)
         y[p++]=SA[i]-j;
      FOR(i,N) wv[i]=x[y[i]];
      memset(we, 0, range*sizeof(int));
      FOR(i,N) we[wv[i]]++;
      FAB(i,1,range) we[i] +=we[i-1];
      FORR(i,N-1) SA[--we[wv[i]]]= y[i];
      swap(x, y);
      x[SA[0]]=0, p = 1;
      FAB(i,1,N)
         if(cmp(y,SA[i],SA[i-1],j))
            x[SA[i]]= p-1;
         else x[SA[i]]=p++;
   } N--;
}
int rank[MAXN], lcp[MAXN];
void findLCP(char *cad,int N) {
   int j, k=0;
   FAB(i,1,N+1) rank[SA[i]] = i;
   FOR(i,N){
      if(k) k--; j=SA[rank[i]-1];
      while(cad[i+k]==cad[j+k]) k++;
      lcp[rank[i]]=k;
}}
```

SDAWG

```
const int alfa = 27;
struct SDAWG{
   struct state {
      int length, edges[alfa],suf;
      bool solid[alfa];
      state() { length = suf = 0;
         memset(edges,0,sizeof(edges));
         memset(solid,0,sizeof(solid));
      }
   };
   vector<state> aut;
void setedge(int a, int b, int ch, int solid) {
   aut[a].edges[ch] = b;
   aut[a].solid[ch] = solid;
   if (aut[b].length <= aut[a].length)
      aut[b].length = aut[a].length + 1;
}
SDAWG(char* s) {
   aut.push_back(state());
   aut.push_back(state());
   int i=-1,current = 1, sink = 1,newsink;
   int newnode, v, w, a;
   aut[1].suf = aut[0].suf = 0;
   while(s[++i]) {
      a = Convertir(s[i]);
      newsink = ++current;
      aut.push_back(state());
      setedge(sink, newsink, a, 1);
      w = aut[sink].suf;
      while (w && aut[w].edges[a] == 0) {
         setedge(w, newsink, a, 0);
         w = aut[w].suf;
      }
      v = aut[w].edges[a];
      if (w == 0)
         aut[newsink].suf = 1;
      else if (aut[w].solid[a])
         aut[newsink].suf = v;
      else {
         newnode = ++current;
         aut.push_back(state());
               FOR(j,alfa){
        aut[newnode].edges[j] =aut[v].edges[j];
            setedge(w, newnode, a, 1);
            w = aut[w].suf;
            aut[newnode].suf = aut[v].suf;
        aut[newsink].suf = aut[v].suf = newnode;
         while(w && !aut[w].solid[a]){
           setedge(w,newnode,a,aut[w].solid[a]);
           w =aut[w].suf;
          }
        }
        sink = newsink;
      }
   }
```

```
    }
    int FDM(char *s) {
       int best= 0,len= 0,i=-1,w= 1;
       while(s[++i]) {
          int a = Convertir(s[i]);
          if (aut[w].edges[a])
             len++, w= aut[w].edges[a];
          else {
             while (true) {
                w= aut[w].suf;
                if(w== 0||aut[w].edges[a])
                            break;
             }
             if (w== 0) len= 0,w= 1;
             else {
                len= aut[w].length + 1;
                w= aut[w].edges[a];
             }
          }
          if(len >best) best=len;
       }
       return best;
    }
};
```

Aho Corasick

```
#define F(x,y) T[x].next[y]
const int alfa = 27;
struct Aho_Corasick{
   struct PMA {
      int suf,next[alfa],accept;
      PMA() {accept=-1;
         memset(next,0,sizeof(next));suf = 0;}
   };
   int root,size,father[MAXN],Q[MAXN];
   vector<PMA> T;
   Aho_Corasick(){
      T.push_back(PMA());
      T.push_back(PMA());
      root = size = 1;
   }
   void Add(char *p,int id){
      int t = root,i = -1;
      while( p[++i]){
         int c = Convertir(p[i]);
         if (F(t,c) == 0 )
            F(t,c) = ++size, T.push_back(PMA());
         t = F(t,c);
      }
      if(T[t].accept != -1 )
         father[id] = T[t].accept;
      else
         T[t].accept = father[id] = id;
   }
   void buildPMA() {
      T.push_back(PMA());
      int izq= 0,der= 0,c= 0;
      while(++c<alfa)
         if (F(root,c)) {
            F( F(root,c) ,0) = root;
            Q[der++] = F(root,c);
         } else
            F(root,c) = root;

      while (izq < der){
         int t = Q[izq++];
         for ( c = 1 ; c < alfa ; ++c)
            if (F(t,c)) {
               Q[der++] = F(t,c);
               int r = F(t,0);
               while (!F(r,c)) r =F(r,0);
               F(F(t,c),0)= F(r,c);
               if (T[F(F(t,c),0)].accept != -1)
                  T[F(t,c)].suf =F(F(t,c),0);
               else
               T[F(t,c)].suf =T[F(F(t,c),0)].suf;
            }
      }
   }
   void match(char *S,int *cant) {
      int v = root,i = -1;
      while (S[++i]){
         int c = Convertir(S[i]);
         while (!F(v,c)) v = F(v,0);
         v = F(v,c);
         if(T[v].accept != - 1)
            cant[T[v].accept]++;
         for (int u= T[v].suf; u; u= T[u].suf)
```

```
            if(T[u].accept != - 1)
               cant[T[u].accept]++;
      }
   }
};
```

Joseph

```
int joseph (int n, int k) {
   int res = 0;
   for (int i=1; i<=n; ++i)
      res = (res + k) % i;
   return res + 1;
}
```

Expresiones

```
import javax.script.*;
ScriptEngineManager manager = new
ScriptEngineManager();
ScriptEngine motor = manager.getEngineByName("js");
motor.put("VARIABLE", valor);
motor.eval(Expresion);
```

Expresiones Regulares

```
import java.util.regex.*;
Pattern pattern = Pattern.compile(expresion);
Matcher matcher = pattern.matcher(patron);
if (matcher.matches())

[abc] -> a, b, or c (simple class)
[^abc] -> Any character except a, b, or c
(negation)
[a-zA-Z]  -> a hasta z or A hasta Z, inclusive
(range)
[a-d[m-p]] -> a hasta d, or m hasta p: [a-dm-p]
(union)
[a-z&&[def]] ->  d, e, or f (intersection)
[a-z&&[^bc]] ->  a through z, except for b and c:
[ad-z] (subtraction)
[a-z&&[^m-p]] -> a through z, and not m through p:
[a-lq-z](subtraction)

.  -> Any character
\d -> A digit: [0-9]
\D -> A non-digit: [^0-9]
\s -> A whitespace character: [ \t\n\x0B\f\r]
\S -> A non-whitespace character: [^\s]
\w -> A word character: [a-zA-Z_0-9]
\W -> A non-word character: [^\w]

\p{Punct} -> One of !"#$%&'()*+,-
./:;<=>?@[\]^_`{|}~
\p{Lower} -> A lower-case alphabetic character: [a-
z]
\p{Upper} -> An upper-case alphabetic character:[A-
Z]
\p{Alpha} -> An alphabetic character
\p{Digit} -> A decimal digit: [0-9]
\p{Alnum}  -> An alphanumeric
character:[\p{Alpha}\p{Digit}]
\p{XDigit}  -> A hexadecimal digit: [0-9a-fA-F]
\p{Space}  -> A whitespace character: [
\t\n\x0B\f\r]
X?    -> X, once or not at all
X*    -> X, zero or more times
X+    -> X, one or more times
X{n}  -> X, exactly n times
X{n,} -> X, at least n times
X{n,m}-> X, at least n but not more than m times
X|Y   ->  Either X or Y
```

Paint

```
Path2D.Double p = new Path2D.Double();
//Crear path
p.moveTo(x1, 0);
p.lineTo(x1, y);
p.lineTo(x2, y);
p.lineTo(x2, 0);
p.lineTo(x1, 0);
p.closePath();
//Compilar
Area area = new Area(p);

//Sacar
PathIterator iter = area.getPathIterator(null);
while (!iter.isDone()) {
  double[] buf = new double[6];
  switch (iter.currentSegment(buf)) {
    case PathIterator.SEG_MOVETO:
```

```
     case PathIterator.SEG_LINETO:
    points.add(new Point2D.Double(buf[0],buf[1]));
      break;
     case PathIterator.SEG_CLOSE:
       totArea += computePolygonArea(points);
       points.clear();
       break;
     }
     iter.next();
}
```

Area de Rectangulos

```
struct Event{
   int x,y1,y2,v;
   Event(){}
   Event(int vv,int ww,int mm,int nn)
   {x=vv;y1=ww;y2=mm;v=nn;}
   bool operator<(const Event& a) const{
      return x < a.x;}
} E[MAXN * 2];
int n,c,d,v,V[1000000],A[1000000];
void update(int index,int a,int b){
   if(a > d || b < c) return;
   if(a >= c && b <= d) {
      V[index] += v; A[index] = 0;
      if(V[index] > 0) A[index] =b-a+1;
      else if(a != b)
         A[index]=A[2*index]+A[2*index+1];
      return;
   }
   update(2*index,a,(a+b)/2);
   update(2*index+1,(a+b)/2+1,b);
   A[index]=0;
   if(V[index]>0) A[index]=b-a+1;
   else if(a != b)
      A[index]=A[2*index]+A[2*index+1];
}
int x1,x2,y1,y2,ptr,sol;
   scanf("%d",&n);
   for(int i=0;i<n;i++) {
   scanf("%d%d%d%d",&x1,&y1,&x2,&y2);++y1;++y2;
   E[ptr++] = Event(x1,y1,y2, 1);
   E[ptr++] = Event(x2,y1,y2,-1);
   }
   sort(E,E+(2*n));
   for(int i=0;i<2*n;i++) {
      if(i!=0)
         sol += A[1] * (E[i].x - E[i-1].x);
         c = E[i].y1 + 1;
         d = E[i].y2;
         v = E[i].v;
         update(1,1,30001);
      }
   printf("%lld\n",sol);
```

```
void output_tandem(string s, int shift, bool left,
                   int cntr, int l, int l1, int l2)
{  int pos;
   if (left) pos = cntr-l1;
   else pos = cntr-l1-l2-l1+1;
   cout<<"["<<shift+pos<<".."<<shift+pos+2*l-1;
   cout << "] = " << s.substr (pos, 2*l) << endl;
}
void output_tandems(string s,int shift,bool left,
                    int cntr,int l,int k1,int k2){
   for (int l1=1; l1<=l; ++l1) {
      if (left && l1 == l)  break;
      if (l1 <= k1 && l-l1 <= k2)
 output_tandem (s,shift,left, cntr,l,l1,l-l1);
   }
}
int get_z(vector<int> & z, int i) {
   return 0<=i && i<(int)z.size() ? z[i] :0;}
void find_tandems (string s, int shift =0) {
   int n=(int) s.length();
   if (n == 1) return;
   int nu = n/2,  nv = n-nu;
   string u = s.substr (0, nu),
   v = s.substr (nu);
   string ru = string (u.rbegin(), u.rend()),
   rv = string (v.rbegin(), v.rend());
   find_tandems (u, shift);
   find_tandems (v, shift + nu);
   vector<int> z1 = z_function (ru),
   z2 =z_function(v + '#' + u),
   z3 =z_function(ru + '#' + rv),
   z4 =z_function(v);
   for (int cntr=0; cntr<n; ++cntr) {
      int l, k1, k2;
```

```
      if (cntr < nu) {  l = nu - cntr;
         k1 = get_z (z1, nu-cntr);
         k2 = get_z (z2, nv+1+cntr);
      }else { l = cntr - nu + 1;
         k1 = get_z (z3, nu+1 + nv-1-(cntr-nu));
         k2 = get_z (z4, (cntr-nu)+1);
      }
      if (k1 + k2 >= l)
output_tandems(s,shift,cntr<nu,cntr,l,k1,k2);
   } }
```

Digit Count

```
void DigitCount(int n,ll *sol){
   ll aux=n, sum=0,p=1,d;
   while(aux){
      d = aux % 10, aux /= 10;
      sol[d] += ((n%p)+1);
      for(int i=0;i<d;i++) sol[i]+=p;
      for(int i=0;i<10;i++)
      sol[i] += sum*d;
      sol[0] -= p;
      sum = p + 10 * sum;
      p *= 10;
   }
}

int LIS(int n,int *a){
   int i,l, r, c, p[MAXN], b[MAXN], m = 1;
   for (b[0]=0,i=1; i < n; i++){
      if (a[b[m-1]] < a[i]){
         p[i] = b[m-1];
         b[m++] = i;
         continue;
      }
      l = 0, r = m - 1;
      while (l < r){
         c = (l + r) / 2;
         if (a[b[c]] < a[i])
         l =c+1;
         else r =c;
      }
      if (a[i] < a[b[l]]) {
         p[i] = (l > 0)? b[l-1] : -1;
         b[l] = i;
      } else
         p[i] = -1;
   }
   return m;
}
```

Triangle Counting - TJU

```
inline bool upper(pnt a) {
   return imag(a)>0 ||(imag(a)== 0&& eal(a)>0);
}

inline bool compare_angle(pnt a, pnt b) {
   if (upper(a) && !upper(b)) return true;
   if (!upper(a) && upper(b)) return false;
   return cross(a,b) > 0;
}
inline bool same_half(pnt a, pnt b) {
   ll cr = cross(b,a);
   if(cr < 0) return 1;
   if(cr == 0 && dot(b,a) > 0) return 1;
   return 0;
}

int n;
pnt arr[100001];

int main() {
   scanf("%d",&n);
   for(int i=0;i<n;i++)

scanf("%lld%lld",&arr[i].real(),&arr[i].imag());
   sort(arr, arr+n, compare_angle);
   ll sol = ll(n) * (n - 1) / 2 * (n - 2) / 3;
   for(int i = 0, j = 0;i < n;i++) {
      while((j + 1)%n != i &&
            same_half(arr[i],arr[(j+1)%n]))
         j = (j + 1)%n;
      ll cc = (j - i + n)%n;
      sol -= cc*(cc-1)/2;
      if(i == j) ++j;
   }
   cout << sol << endl;
   return 0;
```

FFT

```
void fft (P *a, int n,bool invert) {
   for (int i=1, j=0; i<n; ++i) {
      int bit = n >> 1;
      for (; j>=bit; bit>>=1)
         j -= bit;
      j += bit;
      if (i < j) swap (a[i], a[j]);
   }
   for (int len=2; len <= n; len <<= 1) {
      double ang = 2*PI/len * (invert ? -1 : 1);
      P wlen (cos(ang), sin(ang));
      for (int i=0; i<n; i += len) {
         P w (1,0);
         for (int j=0; j<len/2; ++j) {
            P u = a[i+j],  v = a[i+j+len/2] * w;
            a[i+j] = u + v;
            a[i+j+len/2] = u - v;
            w = w * wlen;
         }
      }
   }
   if (invert)
      for (int i=0; i<n; ++i)
         a[i].x /= n, a[i].y /= n;
}

int n1[MAXN], n2[MAXN], sol[MAXN],
ln1,ln2,lsol,lfa,lfb;
P fa[MAXN], fb[MAXN];

void multiply () {
   int n = 1,i, x; lfa = lfb = 0;
   for(i=0;i<ln1;i++)
      fa[lfa++] = P(n1[i],0);
   for(i=0;i<ln2;i++)
      fb[lfb++] = P(n2[i],0);
   n=4<<(int)(log((double)max(ln1,ln2))/log(2.0));
   while(lfa < n || lfb < n){
      if (lfa < n) fa[lfa++] = P(0,0);
      if (lfb < n) fb[lfb++] = P(0,0);
   }
   lfa = lfb = n;
   fft (fa,n, false),  fft (fb,n, false);
   for (i=0; i<n; ++i)
      fa[i] = fa[i] * fb[i];
   fft (fa,n, true);
   for (x=i=0, lsol=-1; i<n; ++i){
      sol[i] = x + int (fa[i].x + 0.5);
      x = sol[i] / 10;
      sol[i] %= 10;
      if (sol[i]) lsol = i;
   }
}
```

Fast Input

```
const int bz = 10240;
char bf[bz + 1], *ppp = bf;
int ch, sg, bt = 0;
#define GET(c) { \
   if(ppp-bf==bt && (bt==0 || bt==bz)) {  \
      bt = fread(bf,1,bz,stdin); ppp=bf; }\
   if(ppp-bf==bt && (bt>0 && bt<bz)) {    \
      bf[0] = 0; ppp=bf; }                \
   c = *ppp++; \
}
#define number(n) { \
   n=sg=0; do { GET(ch); }   \
      while(!isdigit(ch) && ch!='-'); \
   if(ch=='-') { sg=1; GET(ch); } \
   while(isdigit(ch)){n=10*n+ch-48;GET(ch); } \
   if(sg){ n= -n;} \
}
```

Grirar Grilla 45 grados

```
r = (max(col, filas) << 1) + 10;
c = (max(col, filas) << 1) + 10;
xx = x + y + 5;
yy = x - y + filas + 5;
```

Karp Rabin

```
#define REHASH(a,b,h) ((((h)-(a)*d)<<1)+(b))
void KR(char *x, int m, char *y, int n) {
   int d, hx, hy, i, j = 0;
   /* Preprocessing */
   /* computes d = 2^(m-1) with
   the left-shift operator */
   for (d = i = 1; i < m; ++i)
```

```
      d = (d<<1);
   for (hy = hx = i = 0; i < m; ++i) {
      hx = ((hx<<1) + x[i]);
      hy = ((hy<<1) + y[i]);
   }
   /* Searching */
   while (j <= n-m) {
      if (hx == hy && memcmp(x, y + j, m) == 0)
         OUTPUT(j);
      hy = REHASH(y[j], y[j + m], hy);
      ++j;
   }
}
```

Teoria de Numeros

```
N=p^a*q^b*r^c
CantDiv = D = (a+1)*(b+1)*(c+1)
SumaDiv = FOR(i,k)
   sum*=(prim[i]^(cant[i]+1)-1)/(prim[i]-1)
ProdDiv = P = N^(D/2)=Sqrt(N^D)
```

Cant de Palindromes de <= N Digitos

```
a(n) = 2 *(10^(n/2) -1) si n es par
a(n) = 11*(10^(n-1)/2)-2 si n es impar
```

Rotar Punto

```
P RotarPunto(P p,double ang){
   double x=p.x*cos(pi*ang)-p.y*sin(pi*ang);
   double y=p.x*sin(pi*ang)+p.y*cos(pi*ang);
   return P(x,y)
}
```

LCS

```
struct node {
   int value;
   node *next;
   node(int v,node *n) :
      value(v), next(n) { }
};
#define index_of(as, x) \
distance(as.begin(),lower_bound(as.begin(),as.end()
,x))
const int oo = 99999999 ;
vector<int> lcs_hs( vector<int> a, vector<int> b) {
   int n = a.size(), m = b.size();
   map< int , vector< int > > M;
   for (int j= m-1 ;j >= 0; --j)
      M[b[j]].push_back(j);
   vector<int> xs(n+ 1, oo); xs[ 0 ] = -oo;
   vector<node*> link(n+1);
   for (int i = 0;i<n;++i)
      if (M.count(a[i])) {
         vector< int > ys = M[a[i]];
         for (int j = 0;j< ys.size(); ++j) {
            int k =index_of(xs, ys[j]);
            xs[k] =ys[j];
            link[k]=new node(b[ ys[j]], link[k-1]);
         }
   }
   vector<int> c;
   int l =index_of(xs, oo - 1 ) - 1 ;
   for (node *p= link[l]; p; p=p->next)
      c.push_back(p->value);
   reverse(c.begin(), c.end());
   return c;
}
```