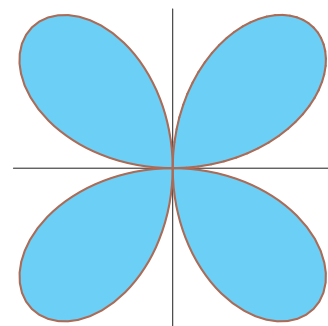
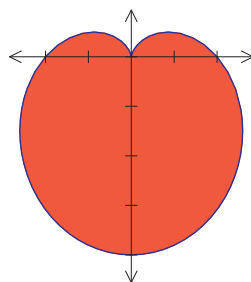


1. Evaluate the following improper integrals.

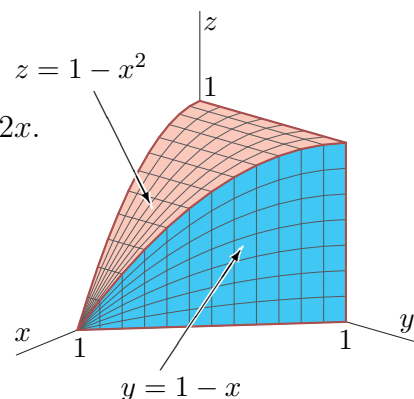
$$(a) \int_{-\infty}^{\infty} x^2 e^{-x^2} dx \quad \text{and} \quad (b) \int_{-\infty}^{\infty} \sqrt{x} e^{-x} dx.$$

2. Electric charge is distributed over the disk  $x^2 + y^2 \leq 2$  with charge density  $\sigma(x, y) = 1 + x^2 + y^2$ . Find the total charge on the disk.
3. A lamina (thin sheet of material) occupies the region inside the circle  $x^2 + y^2 = 2y$  but outside the unit circle  $x^2 + y^2 = 1$ . Find its center of mass if the density at any point is inversely proportional to its distance to the origin.
4. A lamina has shape that part of the disk  $x^2 + y^2 \leq 4$  that lies in the first quadrant. Suppose that its mass density is proportional to the square of the distance to the origin,  $\rho(x, y) = k(x^2 + y^2)$ . Find its center of mass.
5. Suppose that a lamina is in the shape of the rectangle  $D = \{(x, y) \mid 0 \leq x \leq 2, 0 \leq y \leq 3\}$  with mass density  $\rho(x, y) = \pi y$ . Find its center of mass.
6. Find the three moments of inertial  $I_x$ ,  $I_y$ , and  $I_0$  of the lamina from each of the previous two problems.
7. Suppose that a lamina is in the shape of the cardioid  $r = 2 - 2\sin(\theta)$  with constant mass density. Find its centroid and three moments of inertial  $I_x$ ,  $I_y$ , and  $I_0$ .
8. Repeat the previous exercise, but for the first loop (in the positive quadrant) of the four-leaved rose  $r = 2\sin(2\theta)$ . (Use symmetry to reduce your workload.)
9. Repeat the previous exercise, but for the full area enclosed by the four-leaved rose  $r = 2\sin(2\theta)$ . (Again, use symmetry.)



10. Evaluate the iterated integral  $\int_0^3 \int_0^{\sqrt{9-x^2}} \int_0^x yz \, dy \, dz \, dx$ .
11. Compute  $\iiint_E xy \, dV$  where  $E$  is the tetrahedron with vertices  $(0, 0, 0)$ ,  $(3, 0, 0)$ ,  $(0, 2, 0)$ ,  $(0, 0, 1)$ .
12. Compute  $\iiint_E xy \, dV$  where  $E$  is the solid bounded by the parabolic cylinder  $y = x^2$  and the planes  $x = z$ ,  $x = y$ , and  $z = 0$ .
13. Express  $\iiint_E f(x, y, z) \, dV$  as an iterated integral in six different ways, where  $E$  is the solid bounded by  $z = 0$ ,  $x = 0$ ,  $y = 2$ , and  $z = y - 2x$ .
14. The figure shows the region of integration for the integral

$$\int_0^1 \int_0^{1-x^2} \int_0^{1-x} f(x, y, z) \, dy \, dz \, dx.$$



Rewrite this as an equivalent iterated integral in the five other ways.