

Hand in to Frank Thursday 17 October:

33. Suppose that a group  $G$  has an element  $x$  with exactly *three* distinct conjugates. Show that  $G$  is not simple.

Prove the same result if  $G$  has an element  $x$  with exactly *four* distinct conjugates.

Fact: This result remains true if  $G$  has an element with exactly five conjugates.

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Hand in for the grader Thursday 17 October:

34. How many elements of order seven are there in a simple group of order 168?
35. Let  $p$  be a prime number and  $C$  a subgroup of the symmetric group  $S_p$  of order  $p$ . Use the orbit-stabilizer theorem to determine the cardinality of the normalizer in  $S_p$  of  $C$ .
36. Show that no group of order 72 is simple.
37. Show that no group of order 192 is simple.