



Assignment 3

Mandelbulb Set

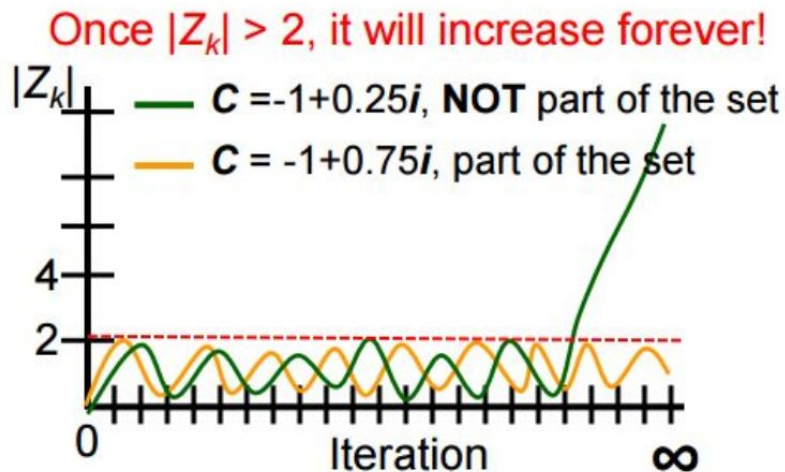
Parallel Programming
2025/10/17



Mandelbrot Set

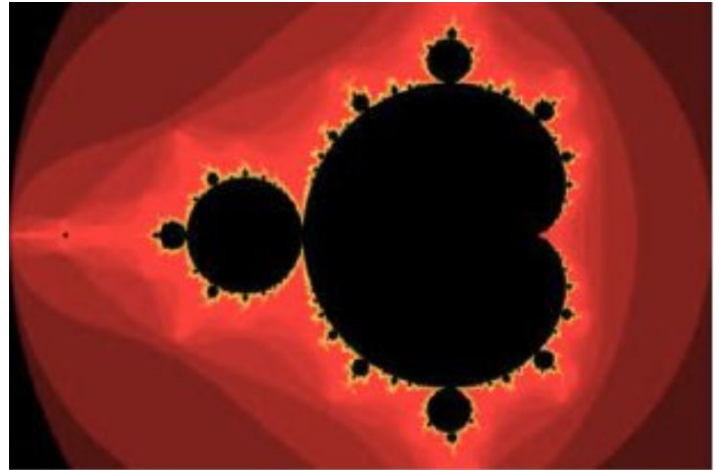
A set of complex numbers \mathbb{C}

- for every complex number $c \in \mathbb{C}$, under iterations of quadratic map $Z_{k+1} = (Z_k)^2 + c$ remain bounded
 - $Z_0 = c$
 - $Z_{k+1} = (Z_k)^2 + c$
 - $|Z_k| \leq 2$
- if $|Z_k| \leq 2$ for any k , c belongs to the Mandelbrot Set



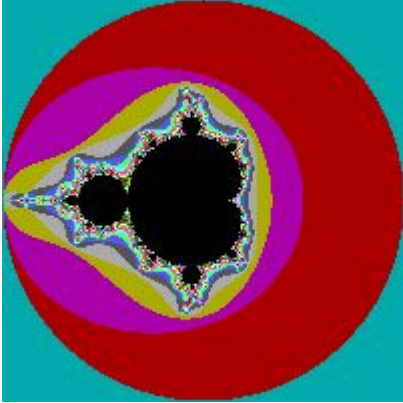
Mandelbrot Set Visualization

- Convert each pixel to the corresponding coordinates on the complex plane
- Plug into the equation repeatedly until $|Z_k| > 2$
- Color the pixel according to the iteration count
- <https://www.youtube.com/watch?v=IrYfMfUURYM>

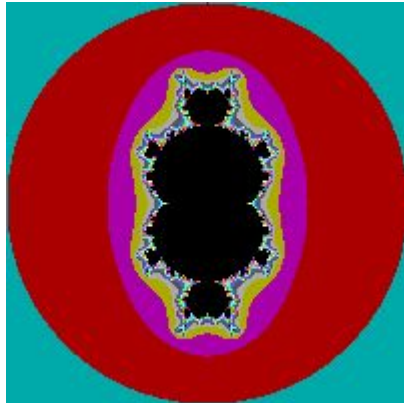


Powers of Mandelbrot Set

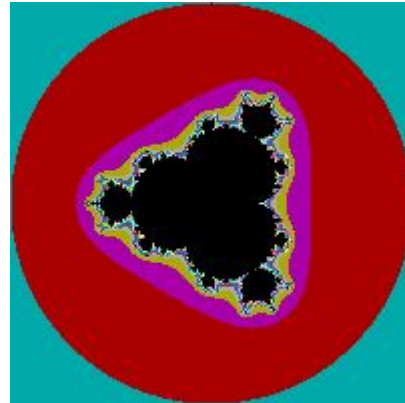
$$Z_{k+1} = (Z_k)^2 + c$$



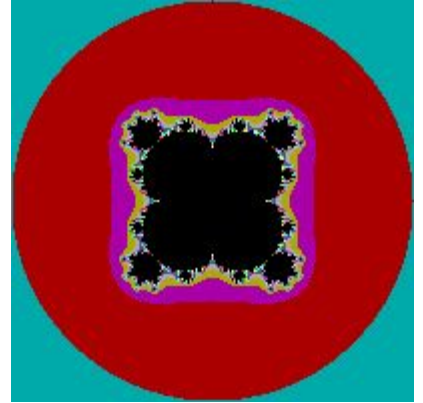
$$Z_{k+1} = (Z_k)^3 + c$$



$$Z_{k+1} = (Z_k)^4 + c$$



$$Z_{k+1} = (Z_k)^5 + c$$



Mandelbulb

- 3D fractal using spherical coordinates (Quaternion, 四元數).
- In this assignment, we refer to power-8 mandelbulb
- https://youtu.be/BLmAV6O_ea0

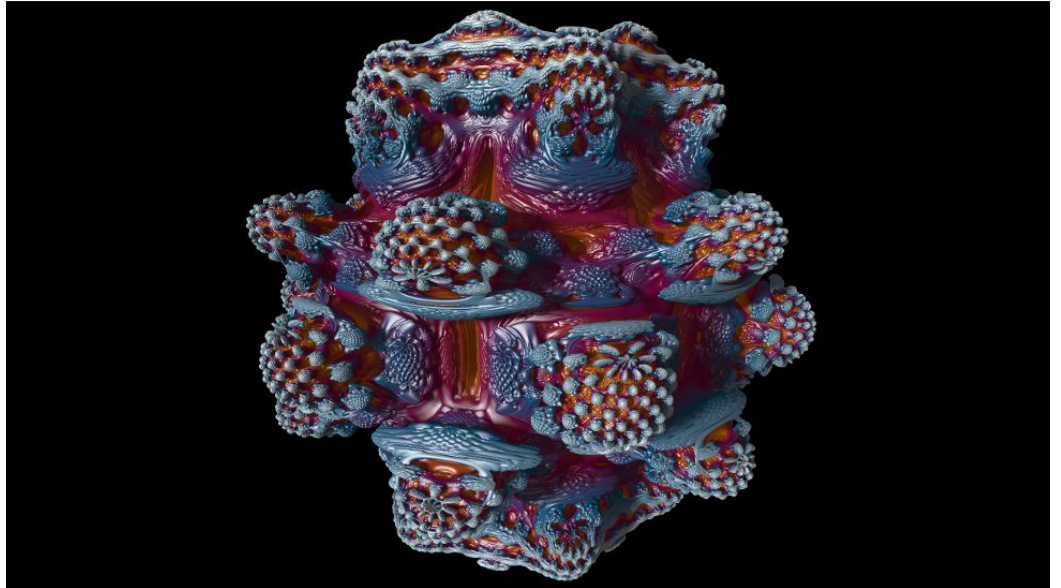
$$v_{k+1} = v_k^8 + C$$

$$v = \langle x, y, z \rangle \text{ in } \mathbb{R}^3, v^n := r^n \langle \cos(n\theta) \cos(n\phi), \cos(n\phi) \sin(n\theta), -\sin(\phi) \rangle$$

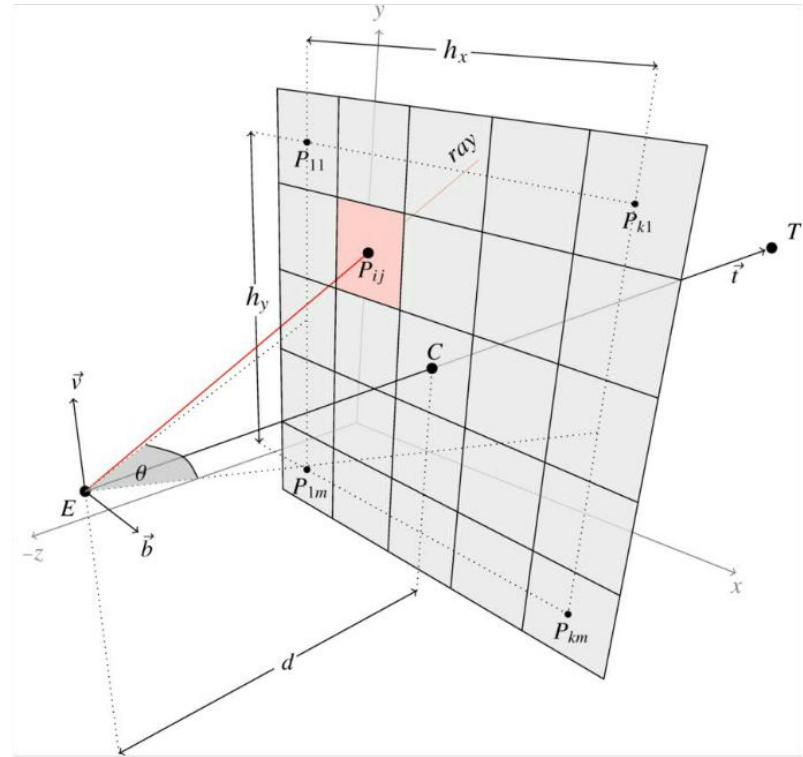
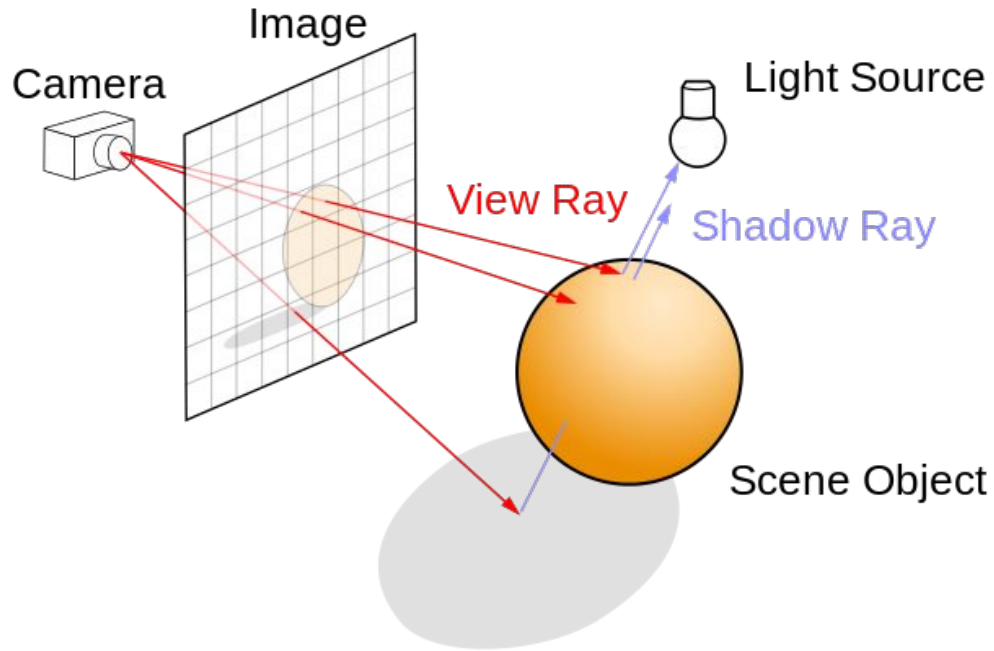
$$\begin{aligned} &\bullet r = \sqrt{x^2 + y^2 + z^2}, \theta = \arctan\left(\frac{y}{x}\right), \phi = \arctan\left(\frac{z}{r}\right) \\ &x = r \sin(\phi) \cos(\theta), y = r \sin(\phi) \sin(\theta), z = r \cos(\phi) \end{aligned}$$

Mandelbulb Visualization

- Generate 3D images by ray tracing
- We use ray marching algorithm



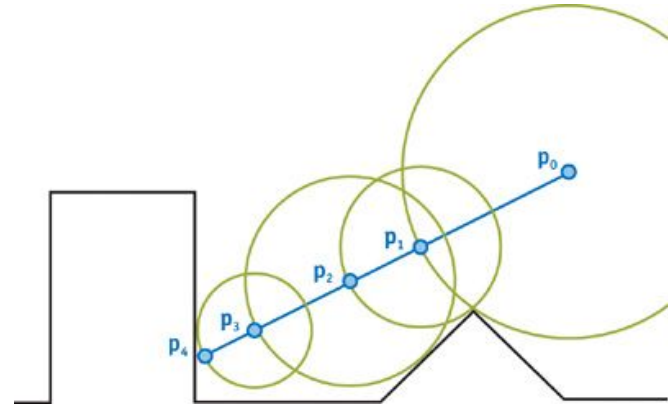
Ray Tracing



Ray Marching

Often used for 3D fractal rendering

1. Start at the “beginning” of the ray
2. Evaluate the **distance function** to estimate how close is to the object
3. Keep moving forward, the step should be short enough to not tunnel through the surface



Distance Function for Ray Marching

The approximate distance function of the mandelbulb is:

$$DE = \frac{0.5r \ln(r)}{dr}$$

Where $r = |v_k|$ and $dr = |v'_k|$.

We can get dr by scalar derivative $dr_{k+1} = n|v_k|^{n-1}dr_k + 1$ and $dr_0 = 1$

Goal

- We provide a sequential version of sample code named `hw3_cpu.cpp`
- You are asked to accelerate it with GPU
- Learn how to write a cuda program
- Understand the importance of **Load Balancing**

Input

```
./executable $x1 $y1 $z1 $x2 $y2 $z2 $width $height $filename
```

- \$x1 double camera position x
- \$y1 double camera position y
- \$z1 double camera position z
- \$x2 double camera target position x
- \$y2 double camera target position y
- \$z2 double camera target position z
- \$width unsigned int width of the image
- \$height unsigned int height of the image
- \$filename string filename of the output PNG image

Output

- Save the result to `$filename`
- The output image should be a 32bit PNG image with RGBA channels

Resources

- `/work/b10502010/pp25/hw3/`
 - `hw3_cpu.cpp` # sequential version
 - `Makefile`
 - `glm/` # vector arithmetic
 - `lodepng/` # png i/o
 - `testcases/`

Environment Setting

- `module load cuda`
- Run your program with `slurm` on 1 GPU

Execute

- Check `testcases/xx.txt`

- `00.txt`:

- `pos` = -0.522 2.874 1.340
- `tarpos` = 0 0 0
- `width` = 64
- `height` = 64
- `timelimit` = 5

```
srun -N 1 -n 1 --gpus-per-node 1 -A ACD114118 -t 3 \  
./hw3_cpu -0.522 2.874 1.340 0 0 0 64 64 00.png
```

- It may take a few hours to run large cases using sequential code. Please start with small cases first and remember to set a time limit.
- Remember to **terminate your process** when finished to avoid wasting resources

Judge

- hw3-judge
- Scoreboard:
<http://140.112.187.55:7771/scoreboard/hw3>
- Remember there is a 10-minute cooldown between judges, please don't abuse the judge system : (
- Accuracy: 97%

Report

- Please refer to the [spec](#)

Submission

- Due: **Fri, 2025/10/31 23:59**
- Place the following files into a directory named <studentID>, archive it and submit to NTU Cool:
 - b1xxxxxxx\
 - hw3.cu
 - report.pdf
 - Makefile (optional)
- **Please note that the first character of your studentID must be lowercase.**

Q & A

Feel free to ask if you have any questions.

Good luck :)

