

## Full Length Article

C<sub>60</sub> surface-supported TM@Si<sub>16</sub> (TM = Ti, Zr, Hf) superatoms as self-assembled photocatalystsLijun Shi<sup>a</sup>, Ping Guo<sup>a,\*</sup>, Jiming Zheng<sup>b</sup>, Pujun Zhao<sup>a</sup>, Zhenyi Jiang<sup>c</sup>, Lei Shen<sup>d,e,\*</sup><sup>a</sup> School of Physics, Northwest University, Xi'an 710069, China<sup>b</sup> Institute of Photonics & Photon-Technology, Northwest University, Xi'an 710069, China<sup>c</sup> Institute of Modern Physics, Northwest University, Xi'an 710069, China<sup>d</sup> Department of Mechanical Engineering, National University of Singapore, 117575, Singapore<sup>e</sup> Engineering Science Programme, National University of Singapore, 117575, Singapore

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## ABSTRACT

Nanocluster assembly is a very promising approach for developing new functional materials. In order to obtain efficient photocatalysts, we investigated photocatalytic properties of two-dimensional (2D) heterostructures self-assembled by superatomic TM@Si<sub>16</sub> (TM = Ti, Zr, Hf) and C<sub>60</sub> clusters using density functional theory. Our results show that the TM@Si<sub>16</sub>/C<sub>60</sub> heterostructures are expected to be direct Z-scheme photocatalysts for overall water splitting. Gibbs free energy studies show that the TM@Si<sub>16</sub>/C<sub>60</sub> heterostructures indeed reduce the energy barrier of water splitting to 0.09 eV for the hydrogen evolution reaction (HER) and 0.40 eV for oxygen evolution reaction (OER) at PH = 0 under solar light.

## 1. Introduction

Due to the low efficiency of solar energy absorption and conversion of existing photocatalytic materials, the wide application of photocatalytic technology is greatly limited [1–3]. The mechanism of photocatalysis is as follows: when a photocatalyst is irradiated by solar, its valence band (VB) electrons will be excited to its conduction band (CB), generating photogenerated electrons in CB and leaving photogenerated holes in VB. These electrons and holes are unstable, with strong reduction and oxidation, and they can react with the electron acceptors and electron donors on the surface of the material, respectively, to promote the corresponding chemical reaction. According to the above physical process, an ideal photocatalyst should meet the following basic conditions: i) a suitable band gap to ensure efficient absorption of sunlight; ii) proper band edge positions to catalyze specific chemical reactions. iii) effective separation of photogenerated carriers to avoid their recombination, ensuring high catalytic efficiency [4]. However, due to inappropriate band gap and rapid recombination of photogenerated carriers, the catalytic efficiency of most single-phase photocatalysts is low, which is difficult to meet the application requirements [2,5].

Many strategies have been developed to modify the existing photocatalysts and attempt to design new photocatalysts [6–10]. Among which constructing 2D heterostructures is recognized as the most

effective way to improve photocatalytic performance [8,9]. Because heterostructures can not only broaden the solar absorption spectrum, but also effectively separate photogenerated electrons and holes at two sides of the heterostructure [8]. Based on the band structure relationship, two different materials can form three heterostructures: type-I with straddling gap, type-II with staggered gap, and type-III with broken gap. Only type-II heterostructures are suitable for photocatalysis because of their regulated charge transfer mechanism [11].

There is a type-II heterostructure called direct Z-scheme heterojunction, composed of oxidation photocatalyst (OP) and reduction photocatalyst (RP). In the process of photocatalysis, the useless conduction band electrons of the OP and the valence band hole of the RP tend to recombine, effectively preventing the recombination of photogenerated electrons and holes for catalysis [9,12,13]. In such a Z-scheme heterojunction, the large interface built-in electric field can promote the recombination of useless electrons and holes, and improve the photocatalytic efficiency. Yu et al. proposed that adjusting the Fermi level position of the two materials can induce the energy band bending of the interface, so as to improve the built-in electric field, and renamed the modified heterostructure as S-scheme heterostructure [14]. As promising high-efficiency photocatalysts, Janus 2D material itself has strong internal electric field induced by intrinsic dipole moments and spatial separation of photogenerated electrons and holes, leading to a

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reduction in the electron-hole recombination rate [15]. Recently, Gao et al. argued that the proper selection of 2D *polar* materials to form Dipole-scheme (D-scheme) heterostructures can realize the desired charge transfer, without sacrificing half of the photogenerated carriers as in Z-scheme or S-scheme photocatalysts [16]. However, regardless of the direct Z-scheme, S-scheme or D-scheme heterostructures, the variety of 2D materials with proper band gaps, intrinsic p-type, and self-polarization that can form them is very limited, greatly hindering the practical application of photocatalysis. Therefore, it is very interesting to find new ways to design and synthesize efficient photocatalytic materials.

The rapid development of nanotechnology makes it possible to select suitable building blocks to construct new functional materials [17]. The experimentally synthesized 2D layered biphenylene network (BPN) has been proved by theoretical studies to be composed of three rings of tetragon, hexagon and octagon [18]. As attractive building blocks, Nanoclusters have rich physical and chemical properties, which can be adjusted by changing their size, shape, and composition so on [19–21]. Cluster-assembled materials with tunable building blocks and assembly ways exhibit the advantage of being precisely tailored in properties [22]. As a building block,  $C_{60}$  cluster has received much attention since its discovery and has been assembled into a variety of materials with novel properties [23–27], and recently a  $C_{60}$  monolayer with notable in-plane anisotropic conductivity has been experimentally synthesized [27]. In order to construct a photocatalytic material, it is necessary to select highly stable cluster building blocks, with suitable highest occupied molecular orbital (HOMO) and lowest unoccupied molecular orbital (LUMO) energy gaps, ensuring that they can maintain their own structure and chemical properties during assembly [28].

As a class of potential building units, the transition metal (TM)-encapsulated silicon cage cluster has attracted widespread attention because its properties can be precisely regulated by only changing one transition metal atom [29–38].  $TM@Si_{16}$  cluster has received more experimental and theoretical attention [32–38]. Experimentally,  $TMSi_{16}$  (TM = Sc, Ti, V, Ta, Zr, Hf, etc.) can be synthesized on a large scale [32] and well characterized [33]. In 2014,  $Ta@Si_{16}$  clusters deposited on the surface of  $C_{60}$ -terminated highly oriented pyrolytic graphite (HOPG) exhibit good thermal stability and uniformity [34], mainly because  $Ta@Si_{16}$  clusters form dimers one-to-one with  $C_{60}$ , where  $C_{60}$  acts as a template to disperse and fix  $Ta@Si_{16}$  [19,35]. The  $Ta@Si_{16}$  self-assembled 2D systems on  $C_{60}$  surface have been demonstrated to exhibit excellent magnetic and potential photocatalytic properties [36].  $TM@Si_{16}$  clusters have two low-lying stable isomers, one is Frank-Kasper (FK) polyhedron structure with approximate  $T_d$  symmetry, and the other is fullerene (f) structure with  $D_{4d}$  symmetry [37]. The FK structures of  $TM@Si_{16}$  (TM = Ti, Zr, Hf) clusters have a HOMO-LUMO gap of about 2.0 eV and can absorb sunlight efficiently [38].

In this work, we investigate the structural, electronic and photocatalytic properties of 2D heterostructures composed of FK- structure  $TM@Si_{16}$  (TM = Ti, Zr, Hf) monolayer and  $C_{60}$  monolayer by first-principles calculations. The  $TM@Si_{16}$  monolayer and  $C_{60}$  monolayer can be respectively used as RP and OP for photocatalytic water splitting, forming a typical direct Z-scheme heterostructure. The interfacial built-in electric field from  $TM@Si_{16}$  to  $C_{60}$  promotes the recombination of useles photoelectrons from the OP- $C_{60}$  layer and photoholes from the RP- $TM@Si_{16}$  layer, effectively retaining the photoholes of OP- $C_{60}$  layer and the photoelectrons of RP- $TM@Si_{16}$  layer to participate in the catalytic reaction, exhibiting a highly efficient photocatalysis for overall water splitting. The overpotentials of water splitting were evaluated by calculating the Gibbs free energies, when PH = 0 only 0.09 eV for the HER and 0.4 eV for the OER under illumination, respectively. These values are substantially better than most conventional photocatalysts [39]. This work paves a new way for the design and construction of high-performance photocatalysts.

## 2. Computational methods

Our calculation mainly used Vienna *ab initio* simulation package (VASP) [40,41] and Amsterdam Density Functional (ADF) [42,43] based on density functional theory (DFT). By using the ADF program, we can draw the molecular orbital diagram to show the superatomic properties of monomer clusters, and calculate the excited states by using the time-dependent density functional (TDDFT) [44–46] to obtain the electron absorption spectra of monomer clusters. The VASP program can be widely used to calculate the electronic structure of clusters and periodic materials, and it is much faster. When  $TM@Si_{16}$  and  $C_{60}$  clusters as well as their dimers are studied by VASP package, they are respectively put into a sufficiently large cubic box ( $30 \text{ \AA} \times 30 \text{ \AA} \times 30 \text{ \AA}$  for the monomer, and  $30 \text{ \AA} \times 30 \text{ \AA} \times 35 \text{ \AA}$  for the dimer) and the sampling of k points in the Brillouin zone only considers the  $\Gamma$  point. For the 2D periodic structures, a vacuum layer of about 15  $\text{\AA}$  was set along the vertical direction of plane, which is sufficient to avoid image interactions between surfaces. The  $\Gamma$ -centered k-point mesh of  $3 \times 3 \times 1$  and  $5 \times 5 \times 1$  was used to sample the Brillouin zone (BZ) by the Monkhorst–Pack (MP) for structural relaxation and electronic structure calculations, respectively. The conjugate gradient method was adopted to optimize the geometry without any symmetry constraint. The generalized gradient approximation (GGA) of Perdew, Burke, and Ernzerhof (PBE) [47] and the projected augmented wave (PAW) [48] method were used for the exchange correlation potential and the ion-electron interaction, and the cut-off energy of the corresponding plane wave was set to 450 eV. Considering the strong Coulomb interaction of d electrons, GGA+U method was adopted for TM atoms [49–51], and the effective U values of Ti, Zr and Hf are set to 2.5 eV adopted from the reference [52]. Considering the weak interaction between  $TM@Si_{16}$  layer and  $C_{60}$  layer, the vdW-DF<sub>2</sub> functional [53] was adopted in our calculations. The Heyd-Scuseria-Ernzerh (HSE06) hybrid functional was used to calculate the accurate energy band structures [54].

To test the reliability of our methods, we firstly examined the electronic properties of free  $TM@Si_{16}$  (TM = Ti, Zr, Hf) and  $C_{60}$  clusters. The results show the HOMO-LUMO gaps of  $TM@Si_{16}$  and  $C_{60}$  are well agreed with the previous calculation [55–57]. The band gap of the qHP  $C_{60}$  monolayer is also agreed with the results obtained by the other method [58]. In addition, we performed a first-principles molecular dynamics (FPMD) simulation [59] to study the thermodynamic stability of the self-assembled  $TM@Si_{16}/C_{60}$  2D heterostructures. Considering the cost of calculation, we only investigated the stability at room temperature 300 K, and the simulation time is 10 ps with a time step of 2 fs.

## 3. Results and discussion

In response to the requirements of ideal photocatalytic materials, we first studied the electronic and optical properties of  $TM@Si_{16}$  (TM = Ti, Zr, Hf) and  $C_{60}$  clusters. Then the geometric, electronic and photocatalytic properties of  $TM@Si_{16}-C_{60}$  dimers were evaluated. Finally, 2D  $TM@Si_{16}/C_{60}$  heterostructures were constructed based on the low-lying dimers and their photocatalytic properties were further investigated in detail. The properties of photocatalytic water splitting are mainly evaluated from three aspects: i) determine the solar energy utilization rate by the optical absorption spectrum; ii) determine whether the system can catalyze the water splitting reaction by the band edge positions of VB and CB; For the photocatalytic water splitting reaction, the CB and VB of the ideal photocatalyst should span the reduction and oxidation potential (−4.44 eV and −5.67 eV) of water to provide electrons and holes for the photocatalytic overall water splitting; iii) determine the reaction mechanism by the charge transfer during photocatalysis water splitting. Besides, we also investigated the possibility of photocatalytic water splitting of all 3d, 4d, and 5d transition metal-doped  $Si_{16}$  cage clusters.

### 3.1. TM@Si<sub>16</sub> monomers

Two low-lying isomers of TM@Si<sub>16</sub> (TM = Ti, Zr, Hf) clusters are shown in Fig. 1. The optimized geometric parameters and energies are listed in Table 1. The lowest-energy structure of Ti@Si<sub>16</sub> and Zr@Si<sub>16</sub> are the FK isomer and the *f* isomer, respectively [38], while the FK and *f* isomers of Hf@Si<sub>16</sub> are nearly degenerate in energy [60]. The HOMO-LUMO gaps of the FK isomers are generally larger than that of the *f* isomers. The superatomicity of FK Ti@Si<sub>16</sub> isomers can be characterized by its valence electron molecular orbital diagram. As seen from Fig. 2, these orbitals are similar to the atomic s, p, d, f and g orbitals, so they are recognized as the S, P, D, F and G orbitals of the cluster, and the electron configuration of the Ti@Si<sub>16</sub> cluster is 1S<sup>2</sup>1P<sup>6</sup>1D<sup>10</sup>1F<sup>14</sup>2S<sup>2</sup>1G<sup>2</sup>2P<sup>6</sup>1G<sup>16</sup>2D<sup>10</sup>.

The electronic absorption spectra of the monomers were calculated by TDDFT method. The FK isomers mainly absorb sunlight in the range of 240–540 nm [Fig. S.1(a)], and the *f* isomer mainly absorbs sunlight in the range of 600–900 nm [Fig. S.1(b) and S.1(c)], while C<sub>60</sub> molecule has a HOMO-LUMO gap of 1.65 eV, and it mainly absorbs sunlight in the range of 260–480 nm [56,57] as shown in Fig. S.1(d). To evaluate whether these monomers can catalyze water splitting reactions, we compared their HOMO and LUMO energy levels with the redox potential of water splitting. Both the HOMO and LUMO of C<sub>60</sub> cluster are lower than the reduction potential for water splitting, indicating the C<sub>60</sub> monomer is suitable for OP (Figure S.2). The FK isomers of Ti@Si<sub>16</sub>, Zr@Si<sub>16</sub> and Hf@Si<sub>16</sub> are more suitable for RP than the *f* isomers, because their LUMO levels are significantly higher than the reduction potential (−4.44 eV) of water splitting, so we try to combine the FK isomers with C<sub>60</sub> molecules to check whether they can form a Z-scheme heterostructure.

### 3.2. TM@Si<sub>16</sub>-C<sub>60</sub> dimers

There are 28 triangles on TM@Si<sub>16</sub> surface, 12 hexagons and 20 pentagons on C<sub>60</sub> surface. According to the structural characteristics of FK-TM@Si<sub>16</sub> clusters and C<sub>60</sub> molecules, we designed various possible TM@Si<sub>16</sub>-C<sub>60</sub> heterodimers. Taking Ti@Si<sub>16</sub>-C<sub>60</sub> dimer as an example, the following connection ways are considered: face-to-face connection (eg: Face3-5, Face3-6), edge-to-edge connection (eg: Line-line), dot-to-surface connection (eg: Dot-5, Dot-6), dot-to-dot connection (eg: Dot-dot), as shown in Fig. 3. “Face3-5” means the connection between the triangles of Ti@Si<sub>16</sub> clusters and the pentagons of C<sub>60</sub>; “Dot-5” means that a Si atom of the Ti@Si<sub>16</sub> cluster is connected to a pentagonal face of C<sub>60</sub>; “Line-line” means that a Si-Si bond is connected with a C-C bond, while “Dot-dot” refers to the connection between a Si atom and a C atom. The optimized dimers can maintain the original framework and connection mode of Ti@Si<sub>16</sub> and C<sub>60</sub>, and the minimum distance between Ti@Si<sub>16</sub> and C<sub>60</sub> clusters is greater than 3.47 Å, indicating a relatively weak interaction and a relatively small binding energy (*E<sub>b</sub>* ≈ 0.2 eV) between Ti@Si<sub>16</sub> and C<sub>60</sub>. As seen from Table 2, these dimers are

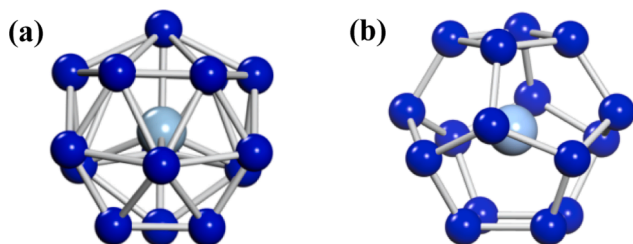


Fig. 1. Two low-lying isomers of TM@Si<sub>16</sub> (TM = Ti, Zr, Hf): (a) C<sub>3v</sub> symmetry Frank – Kasper (FK) structure and (b) D<sub>4d</sub> symmetry fullerene (*f*) structure. The central TM and Si atoms are in cyan and blue, respectively. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

Table 1

The energy of HOMO and LUMO, HOMO-LUMO (H-L) gaps, and the range of TM-Si distance (*d<sub>TM-Si</sub>*) and Si-Si distance (*d<sub>Si-Si</sub>*) of the FK and *f* isomers of TM@Si<sub>16</sub> (TM = Ti, Zr, Hf) clusters. All the units of energy here are eV and all of the bond lengths are Å units.

Structures	<i>d<sub>TM-Si</sub></i> (Å)	<i>d<sub>Si-Si</sub></i> (Å)	HOMO (eV)	LUMO (eV)	H-L Gap (eV)
FK-Ti@Si <sub>16</sub>	2.60–2.84	2.38–2.66	−5.79	−3.49	2.31
FK-Zr@Si <sub>16</sub>	2.70–2.87	2.41–2.73	−6.13	−3.71	2.39
FK-Hf@Si <sub>16</sub>	2.69–2.86	2.41–2.73	−5.99	−3.53	2.42
<i>f</i> -Ti@Si <sub>16</sub>	2.88–2.89	2.28–2.36	−5.53	−4.12	1.41
<i>f</i> -Zr@Si <sub>16</sub>	2.92–2.93	2.31–2.39	−5.92	−4.38	1.53
<i>f</i> -Hf@Si <sub>16</sub>	2.91–2.92	2.30–2.38	−5.85	−4.32	1.54
C <sub>60</sub>			−6.14	−4.49	1.65

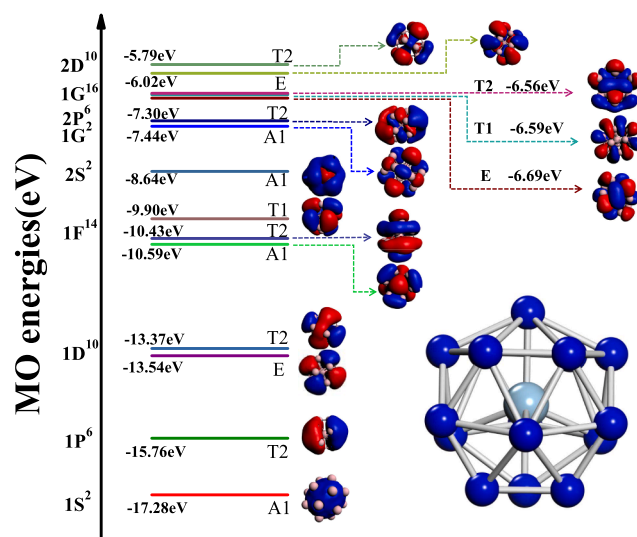


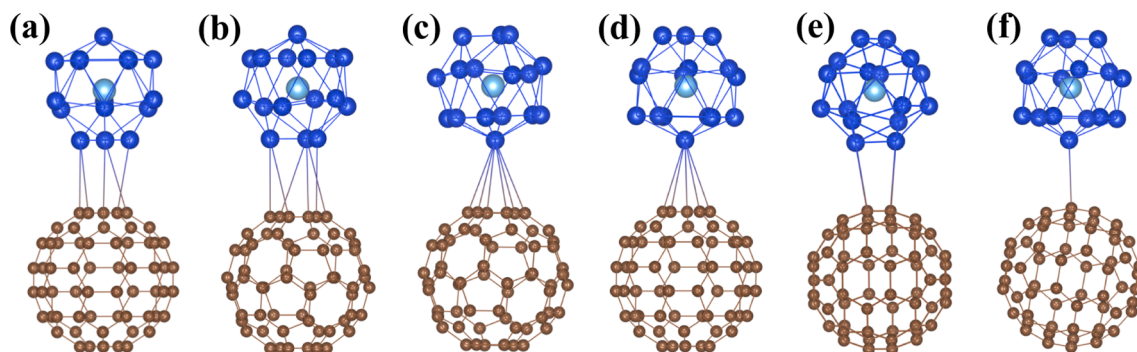
Fig. 2. Valence electron molecular orbital diagram of the Ti@Si<sub>16</sub> cluster with the C<sub>3v</sub> symmetry.

arranged in order of energy from low to high as follows: Face3-5, Face3-6, Dot-6, Dot-5, Line-line, Dot-dot, and the three most stable structures (Face3-5, Face3-6 and Dot-6) are considered for TM@Si<sub>16</sub>-C<sub>60</sub> (TM = Zr, Hf) dimers. Similar to Ti@Si<sub>16</sub>-C<sub>60</sub> dimer, both TM@Si<sub>16</sub> (TM = Zr, Hf) and C<sub>60</sub> also can maintain their framework and connection mode in the dimer, and the spacing between TM@Si<sub>16</sub> and C<sub>60</sub> clusters is greater than 3.48 Å.

Bader charge analysis indicates that the charges transfer from TM@Si<sub>16</sub> to C<sub>60</sub> in the dimer, meaning that there may be a built-in electric field from TM@Si<sub>16</sub> to C<sub>60</sub>. Under illumination, this built-in electric field promotes the recombination of the photoelectrons of C<sub>60</sub> and the photoholes of TM@Si<sub>16</sub>, leaving the photoholes of C<sub>60</sub> and the photoelectrons of TM@Si<sub>16</sub> to catalyze the water splitting reaction. This heralds their potential to assemble into efficient direct Z-scheme photocatalytic heterostructures.

### 3.3. TM@Si<sub>16</sub>/C<sub>60</sub> heterostructures

In this section, the self-assembled 2D TM@Si<sub>16</sub>/C<sub>60</sub> heterostructure were constructed mainly using the low-lying Face3-5 and Face3-6 dimers as building blocks. The Dot-6 2D heterostructure has been assembled and its thermodynamic stability has been proved, especially its PBE electronic structure and light absorption are very similar to that of the Face3-5 heterostructure (Figure S.3). So the electronic and photocatalytic properties of 2D heterostructures were mainly demonstrated by the Face3-5 structure.



**Fig. 3.** Several typical structures of the Ti@Si<sub>16</sub>-C<sub>60</sub> dimers:(a) Face3-5 ; (b) Face3-6 ; (c) Dot-6; (d) Dot-5; (e) Line-Line; (f) Dot-Dot. The Ti, Si and C atoms are shown in cyan, blue and brown, respectively. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

**Table 2**

The distance range of TM-Si bond ( $d_{\text{TM-Si}}$ ) and adjacent Si – Si bond ( $d_{\text{Si-Si}}$ ) in TM@Si<sub>16</sub> clusters, the vertical distance ( $d_{\perp}$ ) and binding energies ( $E_b$ ) between TM@Si<sub>16</sub> and C<sub>60</sub> cluster in the TM@Si<sub>16</sub>-C<sub>60</sub> (TM = Ti, Zr, Hf) dimers.

Dimers	Structures	$d_{\text{TM-Si}}$ (Å)	$d_{\text{Si-Si}}$ (Å)	$d_{\perp}$ (Å)	$E_b$ (eV)
Ti@Si <sub>16</sub> -C <sub>60</sub>	Face 3-5	2.68–2.89	2.42–2.75	3.62	0.243
	Face 3-6	2.68–2.88	2.22–2.76	3.88	0.238
	Dot-6	3.68–2.89	2.42–2.74	3.58	0.228
	Dot-5	2.67–2.89	2.42–2.73	3.57	0.222
	Line-line	2.68–2.89	2.42–2.75	3.47	0.217
	Dot-dot	2.67–2.89	2.42–2.73	3.48	0.187
Zr@Si <sub>16</sub> -C <sub>60</sub>	Face 3-5	2.80–2.94	2.46–2.89	3.66	0.246
	Face 3-6	2.80–2.93	2.47–2.84	3.83	0.238
	Dot-6	2.79–2.94	2.47–2.82	3.48	0.224
Hf@Si <sub>16</sub> -C <sub>60</sub>	Face 3-5	2.79–2.96	2.46–2.96	3.70	0.252
	Face 3-6	2.79–2.93	2.46–2.83	3.84	0.238
	Dot-6	2.78–2.93	2.46–2.81	3.49	0.224

Fig. 4 shows the crystal structure of the 2D Face3-5 Ti@Si<sub>16</sub>/C<sub>60</sub> heterostructure, its cohesive energy ( $E_c$ ) is about 1.23 eV/unit, indicating that the Ti@Si<sub>16</sub>-C<sub>60</sub> system prefers to form a periodic 2D heterostructure, the distance between Ti@Si<sub>16</sub> layer and C<sub>60</sub> layer is 3.62 Å. As shown in Figure S.4, the oscillations of temperature and energy tend to converge with time, which proves that the system is thermodynamically stable.

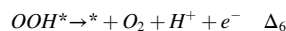
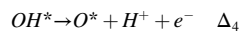
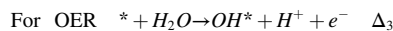
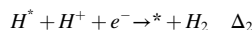
The photocatalytic properties of the 2D Ti@Si<sub>16</sub>/C<sub>60</sub> heterostructure were analyzed by the light absorption, band structure, work function (Figure S.5) and charge transfer. As shown in Fig. 5(a), the study started with absorption spectra, and the light absorption range (50–650 nm) and intensity of Ti@Si<sub>16</sub>/C<sub>60</sub> heterostructure is exactly consistent with the superposition of light absorption of Ti@Si<sub>16</sub> monolayer and C<sub>60</sub> monolayer respectively. This is a very efficient utilization of solar energy. Both the Ti@Si<sub>16</sub> and C<sub>60</sub> monolayer are semiconductors with band gaps of 2.51 eV and 1.72 eV as show in Fig. 5(b) and 5(c), while the 2D Face3-5 Ti@Si<sub>16</sub>/C<sub>60</sub> system is a type-II heterostructure with a direct band gap of 1.68 eV [Fig. 5(d)], its VBM and CBM are provided by Ti@Si<sub>16</sub> and C<sub>60</sub> layer, respectively.

Then let's analyze the band edge positions and charge transfer between interfaces. As show in Fig. 6(a), the CBM and VBM of C<sub>60</sub> layer are respectively lower than the reduction and oxidation potentials of water splitting, while the CBM and VBM of the Ti@Si<sub>16</sub> layer span the reduction and oxidation potentials of the water redox reaction. This means that the C<sub>60</sub> layer is suitable as OP for water splitting, while the Ti@Si<sub>16</sub> layer can be used as both OP and RP. After considering the overpotential and the built-in electric field between the interfaces, the Ti@Si<sub>16</sub> layer is actually more suitable for RP. The differential charge density [Fig. 6(b)]

shows that the electron transfer is from the Ti@Si<sub>16</sub> layer to the C<sub>60</sub> layer, resulting a built-in electric field from Ti@Si<sub>16</sub> to C<sub>60</sub>.

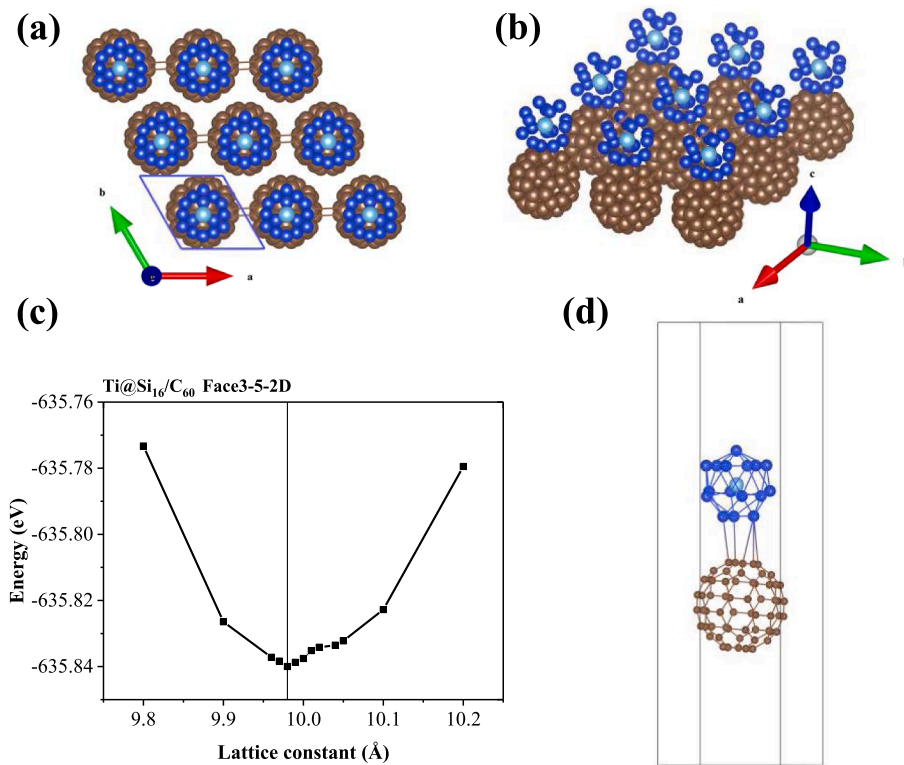
Now we analyze the possible charge transfer during photocatalysis. When the Face3-5 heterostructure is irradiated by sunlight, the Ti@Si<sub>16</sub> layer and C<sub>60</sub> layer absorb sunlight, respectively, and electrons transition from their respective VB to CB, generating photogenerated electrons and holes. The built-in electric field, energy band bending and Coulomb force will jointly drive the useless photoelectrons of the C<sub>60</sub> layer to combine with the useless photoholes of the Ti@Si<sub>16</sub> layer. In this way, the electron-hole recombination of C<sub>60</sub> and Ti@Si<sub>16</sub> itself is greatly suppressed, thus retaining the photoholes of C<sub>60</sub> and the photoelectrons of Ti@Si<sub>16</sub> to participate in oxidation and reduction reactions, which is the electron transfer characteristic of direct Z-scheme heterostructure, suggesting that the Face3-5 2D heterostructure is a promising photocatalysts for photocatalytic overall water splitting. The Face3-6 heterostructures also have similar electronic structures and possible photocatalytic properties[Fig. S.6(a)].

Finally, we examined the photocatalytic water splitting properties of the Ti@Si<sub>16</sub>/C<sub>60</sub> heterostructure by comparing the overpotentials of HER and OER with and without light addition. The water splitting reaction is a non-spontaneous reaction with increasing Gibbs free energy ( $2\text{H}_2\text{O} \rightarrow 2\text{H}_2 + \text{O}_2$ ,  $\Delta G_0 = 237 \text{ kJ}\cdot\text{mol}^{-1}$ ) [61]. Therefore, external energy must be injected into the system for this reaction to occur. The adsorption behavior of H<sub>2</sub>O molecules on the Ti@Si<sub>16</sub>/C<sub>60</sub> heterostructures was firstly studied, and the adsorption energies ( $E_{\text{ads}}$ ) [ $E_{\text{ads}} = E_{\text{TiSi}_{16}/\text{C}_{60}+\text{H}_2\text{O}} - (E_{\text{TiSi}_{16}/\text{C}_{60}} + E_{\text{H}_2\text{O}})$ ] of different adsorption configurations (Figure S.7) are all negative, indicating that H<sub>2</sub>O molecules can be spontaneously adsorbed on the surface [58]. Water splitting reaction include the HER and OER, the typical HER has two steps and the OER has four steps:

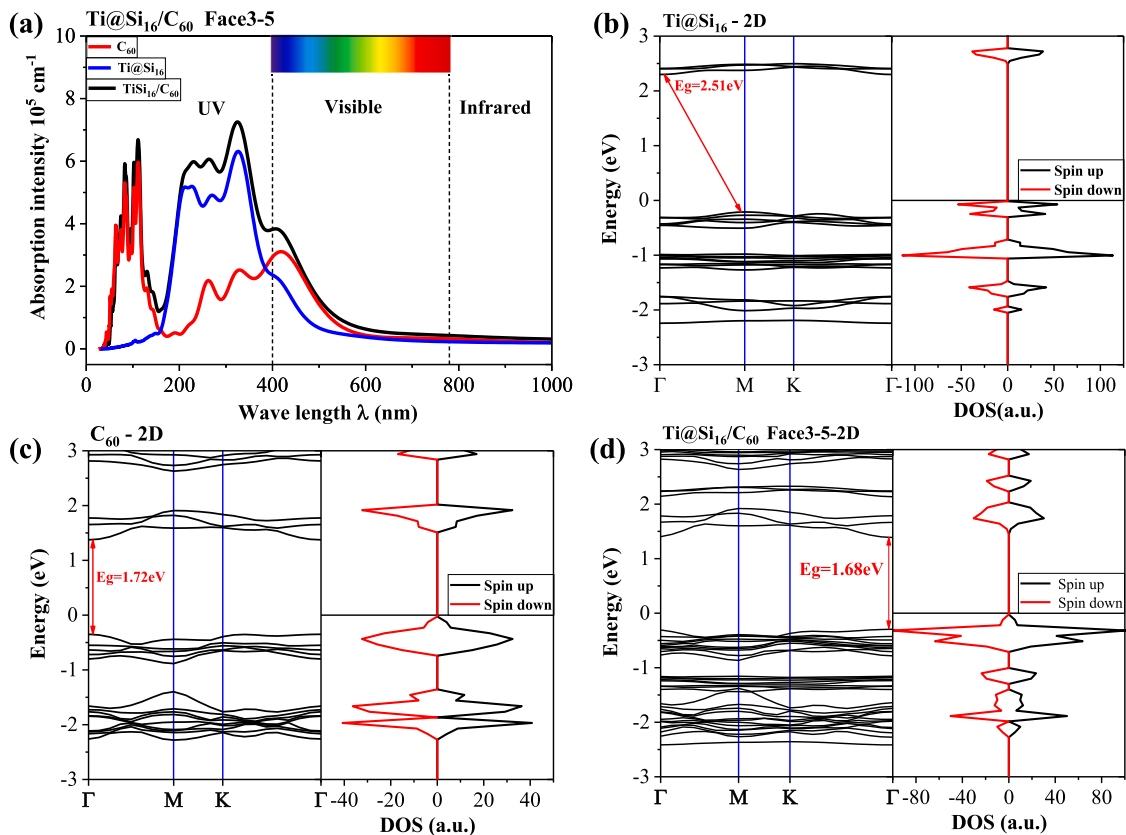


where \* represents photocatalytic materials (*i.e.*, Ti@Si<sub>16</sub>/C<sub>60</sub> heterostructure), and O\*, OH\*, OOH\* and H\* represent the adsorbed intermediates during the redox reactions. The corresponding Gibbs free energy changes for each step are denoted as  $\Delta_i$  ( $i = 1$  and 2 for HER, and  $i = 3, 4, 5$  and 6 for OER), respectively. Theoretically, the ultimate criterion for a good photocatalyst is to have small HER and OER

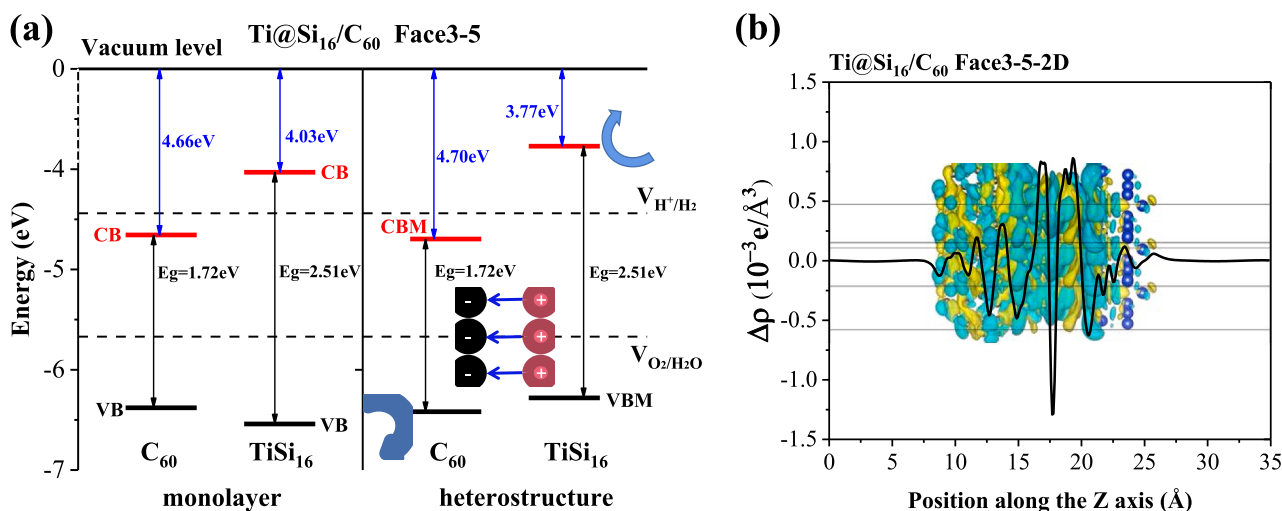




**Fig. 4.** (a) Top-view and (b) Side-view crystal structure of the Face3-5 Ti@Si<sub>16</sub>/C<sub>60</sub> heterostructure, its equilibrium lattice constant is 9.98 Å. (c) Energy as a function of the lattice constant and (d) geometry structure of the Face3-5 Ti@Si<sub>16</sub>/C<sub>60</sub> unit. The Ti, Si and C atoms are shown in cyan, blue and brown, respectively. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)



**Fig. 5.** (a) The absorption spectra of the C<sub>60</sub>, Ti@Si<sub>16</sub> and Face3-5 Ti@Si<sub>16</sub>/C<sub>60</sub> heterostructure. Energy band structure (left) and density of states (right) of (b) Ti@Si<sub>16</sub> monolayer, (c) C<sub>60</sub> monolayer and (d) Face3-5 Ti@Si<sub>16</sub>/C<sub>60</sub> heterostructure.

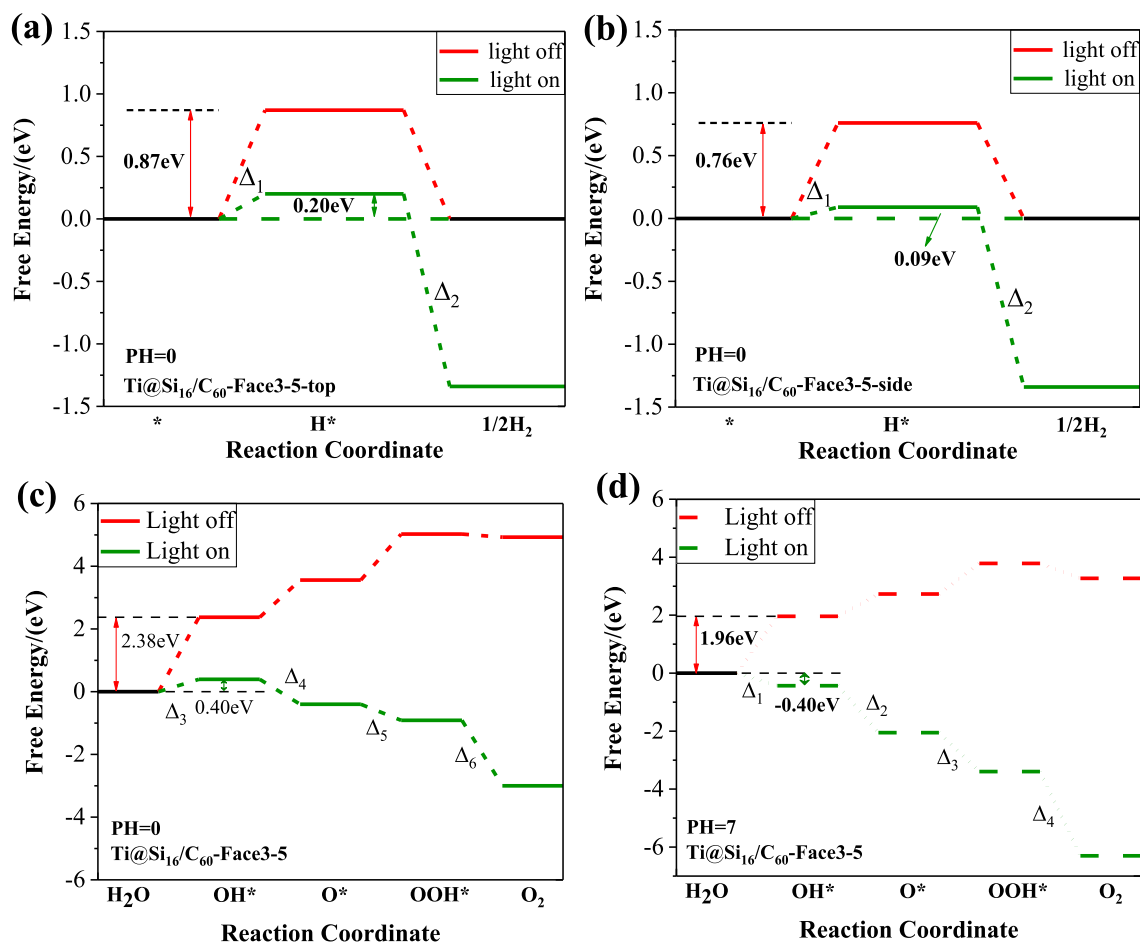


**Fig. 6.** (a) Diagram of the band edge positions and (b) charge density difference together with the averaged plane charge density of the Face3-5  $\text{Ti@Si}_{16}/\text{C}_{60}$  heterostructure.

overpotentials, which can be obtained by calculating the Gibbs free energy change ( $\Delta G$ ) of the rate-determining step in the HER and OER processes.

The first step of HER, adsorption of H, is the rate-determining step. H atoms tend to be adsorbed on the top and side site of  $\text{Ti@Si}_{16}$  as shown in Figure S.8, and the side-site is more stable than the top-site. As shown in

Fig. 7(a) and 7(b), under  $\text{pH} = 0$  and without light conditions, the  $\Delta_1$  is 0.76 eV for the side-site adsorption structures. Under light irradiation, an external potential of  $U_e = 0.67 \text{ eV}$  is supplied by the photogenerated electrons, which reduces  $\Delta_1$  to 0.09 eV (The  $\Delta_1$  of the top-site is reduced to 0.20 eV). This overpotentials is superior to Janus  $\text{PtSsSe}$  (0.34 eV),  $\text{PtTe}$  (0.22 eV), and  $\text{PtSeTe}$  (0.29 eV) [4].



**Fig. 7.** The Gibbs free energy steps of (a and b) the HER processes at  $\text{pH} = 0$ , (c) the OER processes at  $\text{pH} = 0$  and (d) the OER processes at  $\text{pH} = 7$  on the Face3-5  $\text{Ti@Si}_{16}/\text{C}_{60}$  heterostructure.

As shown in Fig. 7(c), the  $\Delta_3$ ,  $\Delta_4$ , and  $\Delta_5$  of OER are all positive at pH = 0 and no light, and the  $\Delta_3$  is already as high as 2.38 eV, indicating that OER is difficult to perform on the  $C_{60}$  surface. When exposed to sunlight, the photogenerated holes can provide an external potential of  $U_h = 1.98$  eV, which reduces  $\Delta_3$  to 0.40 eV. Especially when pH = 7, the external potential  $U_h$  can reach 2.39 eV [62], so that OER can occur spontaneously as shown in Fig. 7(d). The same case is for the Face-3–6 Ti@Si<sub>16</sub>/C<sub>60</sub> heterostructure (Figure S.9). The above studies show that the Ti@Si<sub>16</sub>/C<sub>60</sub> 2D heterostructures are indeed expected to be efficient photocatalysts.

Using the same methods and steps, we investigated the electronic structure and photocatalytic properties of Zr@Si<sub>16</sub>/C<sub>60</sub> and Hf@Si<sub>16</sub>/C<sub>60</sub> heterostructures, and the corresponding energy level structures were shown in Fig. S.5(b) and S.5(c). Similar to the Ti@Si<sub>16</sub>/C<sub>60</sub> heterostructures, the  $E_c$  of the Zr@Si<sub>16</sub>/C<sub>60</sub> and Hf@Si<sub>16</sub>/C<sub>60</sub> 2D heterostructures is also about 1.25 eV. Bader charge analysis shows that the charge transfer between the interfaces is still from TM@Si<sub>16</sub> to C<sub>60</sub>, forming a built-in electric field from TM@Si<sub>16</sub> to C<sub>60</sub>. The charge transfer analysis of photocatalytic water splitting shows that both Zr@Si<sub>16</sub>/C<sub>60</sub> and Hf@Si<sub>16</sub>/C<sub>60</sub> heterostructures can form direct Z-scheme photocatalysts.

The built-in electric field plays an important role in the formation of the direct Z-scheme heterostructure. To get a large built-in electric field, we systematically investigated the charge transfer in all TM@Si<sub>16</sub>/C<sub>60</sub> (TM = 3d, 4d, 5d transition metals) heterostructures and found that several TM@Si<sub>16</sub> (TM = Sc, Zn, Y, Pd and Cd)/C<sub>60</sub> interfaces may be more promising for water splitting photocatalysts because more charge transfer from the TM@Si<sub>16</sub> clusters to the C<sub>60</sub> surface, they are expected to have better photocatalytic performance for water splitting reaction. Furthermore, appropriate modifications to the above systems, such as doping a halogen (Cl atom) in the center of the C<sub>60</sub> cage, can greatly increase the electron affinity of C<sub>60</sub> (from 2.68 eV to 4.38 eV [63]), thereby increasing the charge transfer and the built-in electric field between the interfaces. The charge transfer increase from 0.03e/unit to 0.12e/unit for the Face-3–5 Ti@Si<sub>16</sub>/C<sub>60</sub> heterostructure. We hope this work will stimulate further theoretical and experimental studies to discover more self-assembled heterostructures with superatomic clusters and explore the photocatalytic properties in these types of unique 2D bottom-up systems, which may lead to practical photocatalytic applications.

#### 4. Conclusions

In summary, given the low efficiency of solar energy conversion of existing photocatalytic materials, TM@Si<sub>16</sub> (TM = Ti, Zr, Hf) superatomic clusters were selected to assemble with C<sub>60</sub> molecules to form 2D heterostructures. Their electronic structures and photocatalytic water splitting properties were investigated using the first-principles DFT calculations. The photocatalytic properties of TM@Si<sub>16</sub> and C<sub>60</sub> monomers, TM@Si<sub>16</sub>-C<sub>60</sub> dimers as well as TM@Si<sub>16</sub>/C<sub>60</sub> interfaces were evaluated respectively. The result shows that the C<sub>60</sub> monomer is suitable for OP to catalyze the water splitting reaction and the FK isomers of TM@Si<sub>16</sub> monomers are more suitable for RP, and the TM@Si<sub>16</sub>-C<sub>60</sub> dimers have better photocatalytic properties compared with their monomers. TM@Si<sub>16</sub>/C<sub>60</sub> heterostructures exhibit the characteristics of direct Z-scheme photocatalysts, which are expected to realize the efficient photocatalytic overall water splitting reaction. By calculating the  $\Delta G$  of HER and OER for water splitting on the Ti@Si<sub>16</sub>/C<sub>60</sub> heterostructure, it is proved that this system can indeed effectively reduce the overpotential of the photocatalytic water splitting reaction.

#### CRediT authorship contribution statement

**Lijun Shi:** Conceptualization, Data curation, Investigation, Writing – original draft. **Ping Guo:** Conceptualization, Supervision, Project administration, Writing – review & editing. **Jiming Zheng:**

Methodology, Visualization. **Puju Zhao:** Data curation, Investigation. **Zhenyi Jiang:** Investigation, Supervision. **Lei Shen:** Conceptualization, Formal analysis, Supervision.

#### Declaration of Competing Interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

#### Data availability

Data will be made available on request.

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#### Appendix A. Supplementary data

Supplementary data to this article can be found online at <https://doi.org/10.1016/j.apsusc.2023.156465>.

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