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**Appendix A. Supporting information**

**Resolving CO<sub>2</sub> activation and hydrogenation pathways over iron  
carbides from DFT investigation**

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## Method

In this work, periodic spin-polarized density functional theory (DFT) calculations were performed using the Vienna ab initio simulation package (VASP) [1-4]. The projected augmented wave (PAW)[5] pseudopotentials were used to describe the interactions between valence and core electrons. The exchange correlation energy of the electrons was treated with the Perdew, Burke, and Ernzerhof (PBE)[6] functional within the generalized gradient approximation (GGA) [7]. The solution of the Kohn–Sham equations was expanded in a plane wave basis set with a cutoff energy of 400 eV, and the sampling of the Brillouin zone was performed using the Monkhorst–Pack scheme [8,9]. Electron smearing was employed via the Methfessel–Paxton technique with a smearing width consistent to 0.2 eV. The TS were searched by combining the climbing image nudged elastic band (CI-NEB) method [10] with the dimer method [11]. The dimer separation was set to 0.01 Å, and the force convergence on each atom was less than 0.05 eV/Å. All vibrational analysis for the adsorbates and transition states were calculated to confirm the reliability of the calculated values (Table S13-S20). Bader charge analysis and charge density difference analysis were performed using the code developed by Henkelman and co-workers [12,13].

The surface energy ( $E_{surf}$ ) was determined by equation (Eq) 1:

$$E_{surf} = (E_{slab} - N \times E_{bulk}) / 2A \dots\dots\dots (1)$$

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where  $E_{slab}$  and  $E_{bulk}$  are the total energies of the supercell slab and one bulk unit cell, respectively,  $N$  is the number of bulk units in the slab, and  $A$  is the surface area of the slab.

The adsorption energy ( $E_{ads}$ ) was defined as Eq2:

$$E_{ads} = E_{(adsorbates + slab)} - (E_{slab} + E_{adsorbates}) \quad \dots\dots\dots (2)$$

where  $E_{(adsorbates + slab)}$  is the total energy of the slab with adsorbates,  $E_{slab}$  is the total energy of the corresponding bare slab, and  $E_{adsorbates}$  is the total energy of free adsorbates. Hence, a negative (positive) value indicates an exothermic (endothermic) adsorption. In principle, the more negative the  $E_{ads}$ , the stronger the binding.

The reaction energy ( $E_r$ ) and barrier ( $E_a$ ) were calculated by Eq3 and 4:

$$E_r = E_{FS} - E_{IS} \quad \dots\dots\dots (3)$$

$$E_a = E_{TS} - E_{IS} \quad \dots\dots\dots (4)$$

where  $E_{IS}$ ,  $E_{TS}$  and  $E_{FS}$  are the total energy of the corresponding initial state (IS), IS state (TS) and final state (FS), respectively.

The d-band center ( $\epsilon_d$ ) was used to correlate the catalytic properties with the electronic structure of the catalyst. It was calculated using Eq5:

$$\epsilon_d = \frac{\int_{-\infty}^{+\infty} \rho_d(E) E dE}{\int_{-\infty}^{+\infty} \rho_d(E) dE} \quad \dots\dots\dots (5)$$

where  $E$  is the energy with respect to the Fermi energy, and  $\rho_d(E)$  is the density of states projected onto the metal atom's d-band at energy  $E$ .

## Model

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Bulk  $\chi$ -Fe<sub>5</sub>C<sub>2</sub> (Fig. 1(a)) is a monoclinic crystal and shows a C2/c crystallographic symmetry including 20 Fe and 8 C atoms per unit cell. Bulk  $\theta$ -Fe<sub>3</sub>C (Fig. 1(b)) is an orthorhombic crystal and exhibits a Pnma crystallographic symmetry containing 12 Fe and 4 C atoms per unit cell. The bulk structure of  $\chi$ -Fe<sub>5</sub>C<sub>2</sub> ( $\theta$ -Fe<sub>3</sub>C) was optimized with a  $3 \times 5 \times 5$  ( $9 \times 7 \times 9$ ) Monkhorst–Pack k-point mesh. The optimized lattice parameters were in good agreement with previous experimental and theoretical values, as shown in Table S1.

## Results

Surface energies of typical low Miller index facets and the specific high Miller index facets were calculated as shown in Table S2. The surface energies of the high Miller index (510) facet for  $\chi$ -Fe<sub>5</sub>C<sub>2</sub> (510) and (031) for  $\theta$ -Fe<sub>3</sub>C are the lowest among the calculated ones, indicating that  $\chi$ -Fe<sub>5</sub>C<sub>2</sub> (510) and  $\theta$ -Fe<sub>3</sub>C (031) are the most thermodynamically stable facets. This is consistent with previous experimental and theoretical results [14,15]. Thus, in this work, the supercell of p ( $1 \times 1$ ) for  $\chi$ -Fe<sub>5</sub>C<sub>2</sub> (510) surface including 8 layers of carbon and 20 layers of iron and a p ( $1 \times 1$ ) for  $\theta$ -Fe<sub>3</sub>C (031) slab with 4 layers of carbon and 12 layers of iron were constructed to represent the iron carbide catalysts. A vacuum gap spacing of 10.5 Å was used to avoid interaction between the repeating slabs. The validity of slab models had been verified (Table S4, S5 and S6).

For the  $\chi$ -Fe<sub>5</sub>C<sub>2</sub> (510) model, the bottom 11 Fe layers and 5 C layers (11Fe + 5C)

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were fixed at their bulk positions, while the top 12 layers (9Fe + 3C) and adsorbates were allowed to relax. As for  $\theta$ -Fe<sub>3</sub>C (031) slab, the top 7 layers (6Fe + 1C) and adsorbates were allowed to relax, while the bottom 9 layers (6Fe + 3C) were constrained at the bulk positions. A k-space mesh of  $3 \times 1 \times 1$  within the Monkhorst–Pack scheme was used to sample the Brillouin zone of the surface. The test of Monkhorst–Pack meshes is given in Table S7. For isolated molecules and atoms, calculations were carried out in a  $10 \text{ \AA} \times 10 \text{ \AA} \times 10 \text{ \AA}$  box with a  $1 \times 1 \times 1$  Monkhorst-Pack k-point mesh. Spin-polarized calculations were performed considering the ferromagnetic nature of Fe.

In addition, charge analysis of surface atoms was performed to predict and interpret the adsorption position of reactants (Fig. S1). The iron atoms within the flat trapezoid-type and the ridge-type sites exhibit strong electron transport capabilities, thus could be effective sites for CO<sub>2</sub> adsorption and activation. These potential active sites are abundant on both  $\chi$ -Fe<sub>5</sub>C<sub>2</sub> (510) and  $\theta$ -Fe<sub>3</sub>C (031) surfaces, suggesting the comparability and reactivity of two surfaces. The surface site represents the position of CO<sub>2</sub> before optimization. For instance, 3F<sup>1</sup> represents the first 3-fold hollow site; 4F<sup>1</sup> represents the first 4-fold hollow site; Cs<sup>1</sup> represents the first surface carbon site; Fe<sup>1</sup> represents the surface iron atom site.

We first examined CO<sub>2</sub> adsorption on  $\chi$ -Fe<sub>5</sub>C<sub>2</sub> (510) and  $\theta$ -Fe<sub>3</sub>C (031), which are identified as the active phases of Fe-based catalysts. Starting from the energetically stable adsorption configurations, CO<sub>2</sub> activation pathways were subsequently

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investigated to elucidate the mechanism of CO<sub>2</sub> hydrogenation over the two iron carbides.

On  $\chi$ -Fe<sub>5</sub>C<sub>2</sub> (510) facet, CO<sub>2</sub> adsorption at the 3F<sup>5</sup> site is the most stable (Fig. S2(b)). The C atom resides on the bridge between Fe<sup>5</sup> and Fe<sup>6</sup>; the O<sup>1</sup> and O<sup>2</sup> of CO<sub>2</sub> form O-Fe bonds with Fe<sup>6</sup> and Fe<sup>5</sup>, respectively. The bond lengths of C-O<sup>1</sup> and C-O<sup>2</sup> are both 1.25 Å, with an O-C-O bond angle of 138.8° (For gas phase CO<sub>2</sub> in comparison, the C-O bond lengths are 1.18 Å and the O-C-O bond angle is 180.0°), indicating initial activation of CO<sub>2</sub> upon adsorption.

On  $\theta$ -Fe<sub>3</sub>C (031) facet, CO<sub>2</sub> adsorption at the 3F<sup>4</sup> site is the most stable (Fig. S6(b)). The C atom is on the top of Fe<sup>5</sup>, while the O<sup>2</sup> of CO<sub>2</sub> bonds with Fe<sup>4</sup> and Fe<sup>6</sup> on the bridge site, and O<sup>1</sup> on the top of Fe<sup>5</sup>. The bond lengths of C-O<sup>1</sup> and C-O<sup>2</sup> in the adsorbed-state CO<sub>2</sub> are elongated to 1.23 Å and 1.33 Å, respectively. The O-C-O bond angle bends to 130.8° in the adsorbed state. Configurations of the adsorbed state CO<sub>2</sub> enormously deviates from molecular CO<sub>2</sub> in the gas phase, suggesting initial activation of the molecule upon adsorption.

As for CO<sub>2</sub> direct dissociation over  $\chi$ -Fe<sub>5</sub>C<sub>2</sub> (510) surface, the easiest is at 3F<sup>4</sup> site with CO<sub>2</sub> adsorption of -0.52 eV (Fig. 2(a)). In the TS, the bond length of C and O<sup>2</sup> elongated to 1.66 Å. C in CO<sub>2</sub> migrates to the top of Fe<sup>6</sup> and O<sup>2</sup> is located at the bridge site between Fe<sup>3</sup> and Fe<sup>5</sup>. In addition, the O-C-O angle bends from 131.1° to 115.1° in the TS. Whereas, CO<sub>2</sub> direct dissociation  $\theta$ -Fe<sub>3</sub>C (031) facets at the 3F<sup>3</sup> site is most favorable with CO<sub>2</sub> adsorption energy of -0.58 eV (Fig. 2(b)). In the TS, the

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angle of O-C-O reduces to  $114.9^\circ$  and the C-O<sup>2</sup> bond length elongated to 1.68 Å from 1.34 Å in the IS. The C dissociated from \*CO<sub>2</sub> transfers to the Fe<sup>5</sup> top site with a C-Fe bond length of 1.90 Å with O<sup>1</sup>.

CO<sub>2</sub> activation can undergo hydrogen assisted pathway except for the direct dissociation. The stability of \*HCOO \*COOH and \*CO and \*OH intermediates on  $\chi$ -Fe<sub>5</sub>C<sub>2</sub> (510) facet were verified as the first FS and the second IS. And to compare inclination of activation pathway with CO<sub>2</sub> direct dissociation, the C-O bond breakage with H assistance was taken into consideration. It is found that the activation energy barrier is mainly focus on the first TS.

In the TS of \*CO and \*OH in one step pathway on  $\chi$ -Fe<sub>5</sub>C<sub>2</sub> (510) facet (Fig. 3(a)), C-O<sup>2</sup> bond is elongated to 1.73 Å accompanied by C adatom from Fe<sup>3</sup> and Fe<sup>5</sup> bridge site migrates to Fe<sup>4</sup>. In the final state, the H adatom transfers to Fe<sup>5</sup> and Fe<sup>6</sup> bridge site and then combines with O<sup>2</sup> with a bond length of 0.98 Å, additionally, \*CO<sup>1</sup> settles in inclined top of Fe<sup>3</sup>.

For the \*COOH intermediate pathway on  $\chi$ -Fe<sub>5</sub>C<sub>2</sub> (510) facet (Fig. 3(b)), in the first transition state (TS1), adsorbed H transfers towards O of \*CO<sub>2</sub> and the distance between them reduces to 1.45 Å from 2.67 Å in the IS. The formed \*COOH configuration is mono-dentate. The \*COOH intermediate then disintegrates into \*CO and \*OH with an energy barrier of 0.34 eV. In the second transition state (TS2), the C-O<sup>2</sup> bond length of \*CO<sub>2</sub> is enlarged to 1.35 Å from 1.34 Å, and the O-C-O angle increases to  $112.9^\circ$  from  $111.4^\circ$ . In the second final state (FS2), \*CO<sup>1</sup> is adsorbed at 4F<sup>1</sup>

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site and the  $^*\text{O}^2\text{H}$  migrates to  $3\text{F}^2$  site.

For the  $^*\text{HCOO}$  intermediate pathway on  $\chi\text{-Fe}_5\text{C}_2$  (510) facet (Fig. 3(c)), in TS1, adsorbed H transfers towards C of  $^*\text{CO}_2$  and the distance between them reduces to 1.69 Å from 2.90 Å in the IS. The O-C-O angle decreases to  $126.1^\circ$  from  $131.8^\circ$ . In addition, the  $^*\text{CO}_2$  configuration becomes bi-dentate from mono-dentate in the IS. The formed  $^*\text{HCOO}$  intermediate then disintegrates into  $^*\text{HCO}$  and  $^*\text{O}$  with an energy barrier of 0.57 eV. In the TS2,  $\text{O}^2$  of  $^*\text{CO}_2$  transfers to the bridge site between  $\text{Fe}^4$  and  $\text{Fe}^6$  from the bridge site between  $\text{Fe}^3$  and  $\text{Fe}^6$  and the distance is enlarged to 2.81 Å between C and  $\text{O}^2$ . C migrates to the bridge site between  $\text{Fe}^6$  and  $\text{Fe}^8$  from  $\text{Fe}^6$  top site. In the FS2,  $\text{O}^2$  is adsorbed at  $4\text{F}^1$  site and C transfers to the bridge site between  $\text{Fe}^5$  and  $\text{Fe}^8$ .

For the  $^*\text{COOH}$  intermediate pathway on  $\theta\text{-Fe}_3\text{C}$  (031) facet (Fig. 4(b)), in TS1, adsorbed H transfers towards  $\text{O}^2$  of  $^*\text{CO}_2$  and the distance between them reduces to 1.49 Å from 2.73 Å in the IS. The  $^*\text{COOH}$  configuration is mono-dentate. The  $^*\text{COOH}$  intermediate then disintegrates into  $^*\text{CO}$  and  $^*\text{OH}$  with an energy barrier of 0.56 eV. In the TS2, the distance between  $\text{O}^2$  and C is enlarged to 1.37 Å from 1.34 Å and the O-C-O angle increases to  $114.7^\circ$  from  $111.6^\circ$ . In the FS2,  $^*\text{CO}^1$  migrates to the top site of  $\text{Fe}^5$ ,  $^*\text{O}^2\text{H}$  transfers to the bridge site between  $\text{Fe}^6$  and  $\text{Fe}^8$ .

In the TS of  $^*\text{CO}$  and  $^*\text{OH}$  in one step pathway on  $\theta\text{-Fe}_3\text{C}$  (0 31) facet (Fig. 4(a)), adsorbed H transfers towards  $\text{O}^2$  of  $^*\text{CO}_2$  and the distance is shortened to 1.41 Å from 2.58 Å in the IS. C of  $^*\text{CO}_2$  moves to  $\text{Fe}^3$  accompanied by  $\text{O}^1$  and the C- $\text{O}^2$  bond length is stretched to 2.94 Å, indicating the completely broken C-O bond. In FS,



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156 \*O<sup>2</sup>H is adsorbed at bridge site between Fe<sup>4</sup> and Fe<sup>6</sup> and \*CO<sup>1</sup> is trapped at 3F<sup>3</sup> site.

157 As for \*HCOO intermediate pathway on  $\theta$ -Fe<sub>3</sub>C (031) facet (Fig. 4(c)), in the

158 first transition state (TS1), adsorbed H transfers towards C of \*CO<sub>2</sub> and the distance

159 between them reduces to 1.42 Å from 2.02 Å in the IS. And then formed \*HCOO

160 intermediate disintegrates into \*HCO and \*O with an energy barrier of 0.1 eV. In the

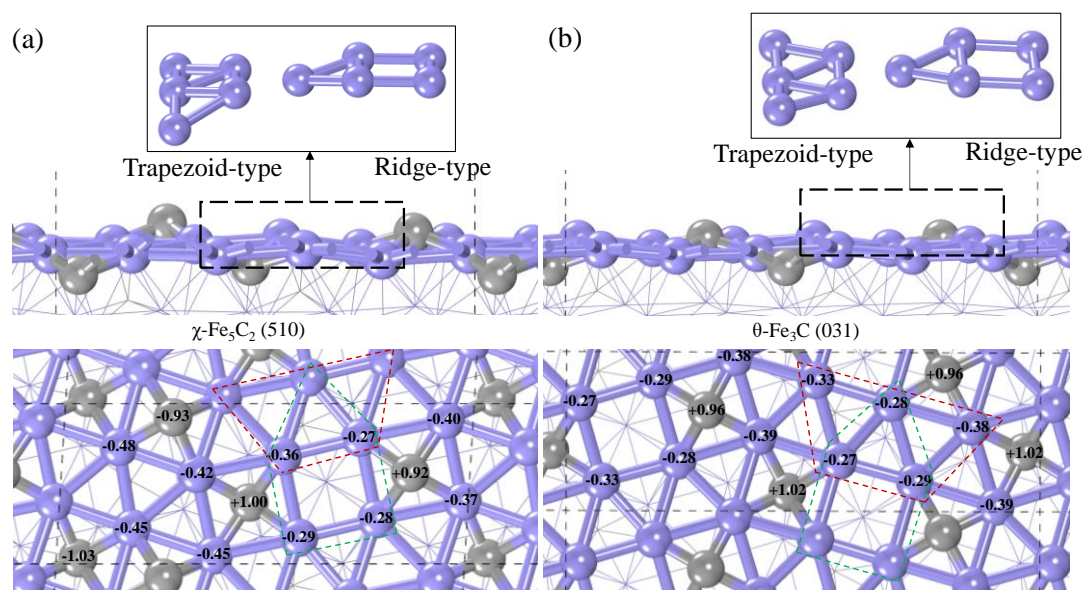
161 second transition state (TS2), O<sup>1</sup> of \*CO<sub>2</sub> transfers from Fe<sup>3</sup> to bridge site between

162 Fe<sup>3</sup> and Fe<sup>4</sup>; O<sup>2</sup> migrates to 4F<sup>1</sup> site from the bridge site between Fe<sup>4</sup> and Fe<sup>6</sup>. The

163 C-O<sup>2</sup> bond length is enlarged from 1.36 Å to 2.74 Å.

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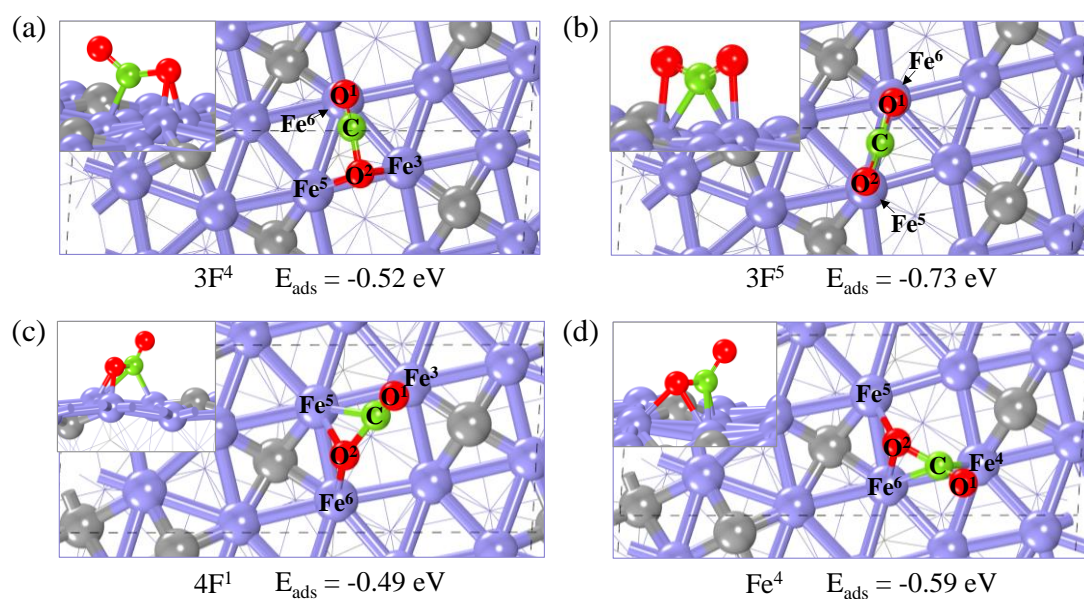
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167 Fig. S1. Charge analysis for surface atoms of (a)  $\chi$ -Fe<sub>5</sub>C<sub>2</sub> (510) and (b)  $\theta$ -Fe<sub>3</sub>C (031).

168 (Fe atoms in purple; C atoms in gray.)

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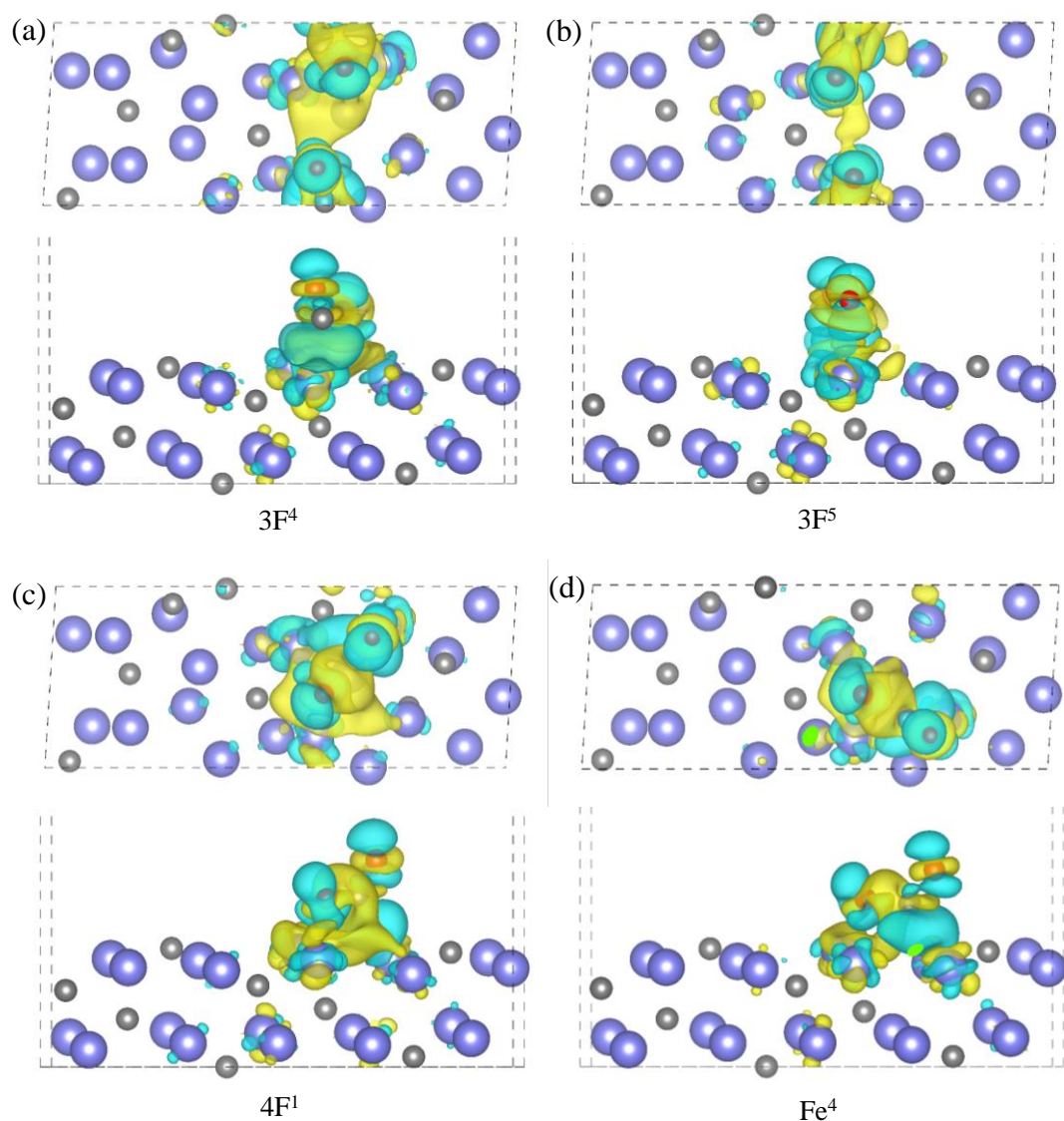
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172 Fig. S2. Stable  $\text{CO}_2$  adsorption configurations and the corresponding adsorption

173 energies on  $\chi\text{-Fe}_5\text{C}_2$  (510) surface. (Fe atoms in purple, C atoms of  $\chi\text{-Fe}_5\text{C}_2$  in gray, C

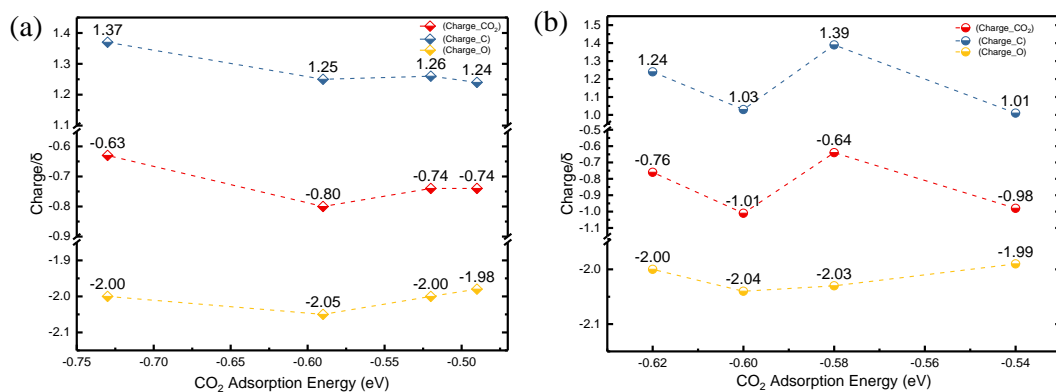
174 atoms of  $\text{CO}_2$  in green, O atoms of  $\text{CO}_2$  in red.)

175



178 Fig. S3. Top and side views of charge densities for stable CO<sub>2</sub> adsorption structure on  
 179  $\chi$ -Fe<sub>5</sub>C<sub>2</sub> (510). (Fe atoms in purple; O atoms in red; C atoms in gray.) Yellow and cyan  
 180 isosurfaces represent the charge accumulation (i.e. a gain of electron density) and  
 181 depletion (i.e. a loss of electron density) in the system, respectively.

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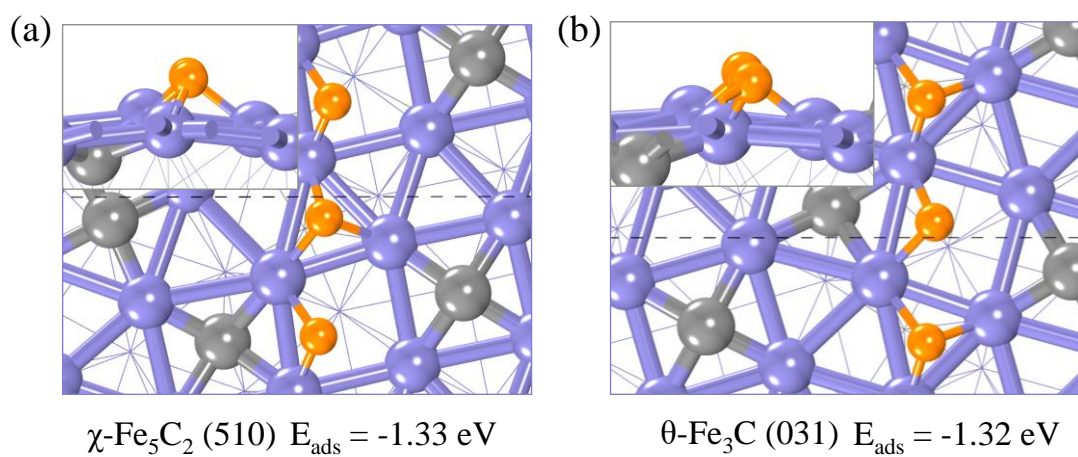


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185 Fig. S4. The relationship between the stable adsorption energies and the number of

186 electrons transferred over (a)  $\chi$ -Fe<sub>5</sub>C<sub>2</sub> (510) and (b)  $\theta$ -Fe<sub>3</sub>C (031) surfaces.

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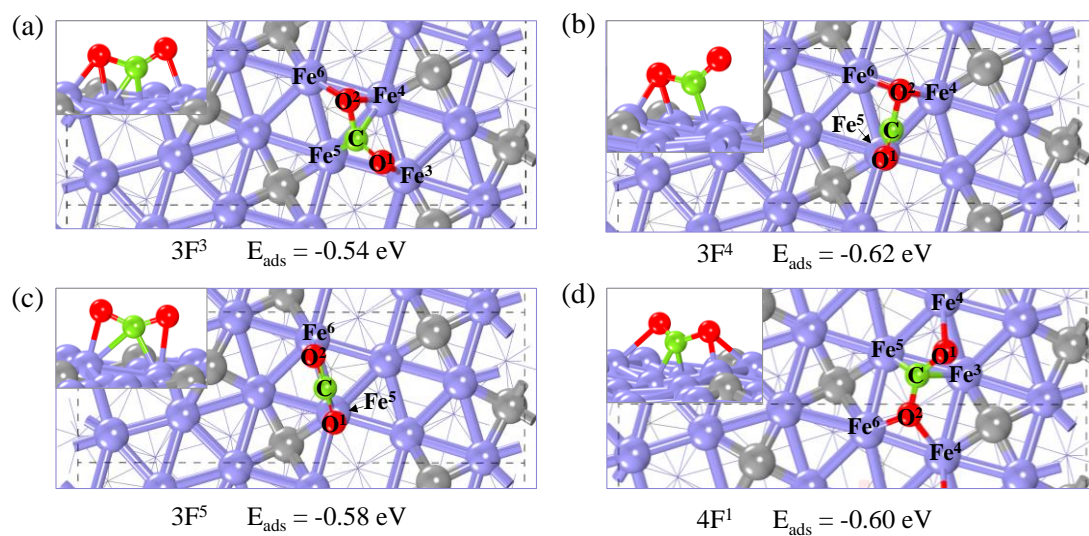
190 Fig. S5. Optimized structures of  $\text{H}_2$  adsorption and dissociation on (a)  $\chi\text{-Fe}_5\text{C}_2$  (510)

191 and (b)  $\theta\text{-Fe}_3\text{C}$  (031) surfaces. (Fe atoms in purple; O atoms in red; H atoms in orange.)

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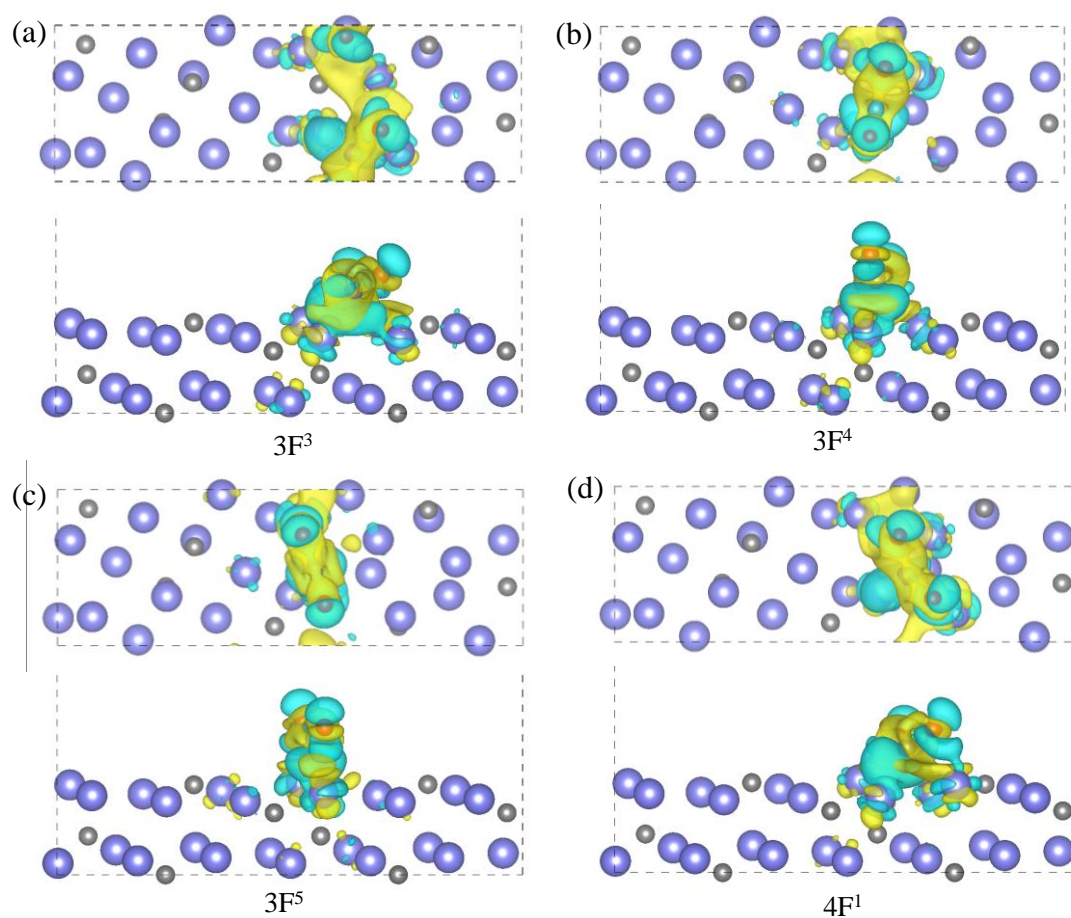
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195 Fig. S6. Stable  $\text{CO}_2$  adsorption configurations and the corresponding adsorption  
 196 energies on  $\theta\text{-Fe}_3\text{C}$  (031) surface. (Fe atoms in purple, C atoms of  $\theta\text{-Fe}_3\text{C}$  (031) in  
 197 gray, C atoms of  $\text{CO}_2$  in green, O atoms of  $\text{CO}_2$  in red.)

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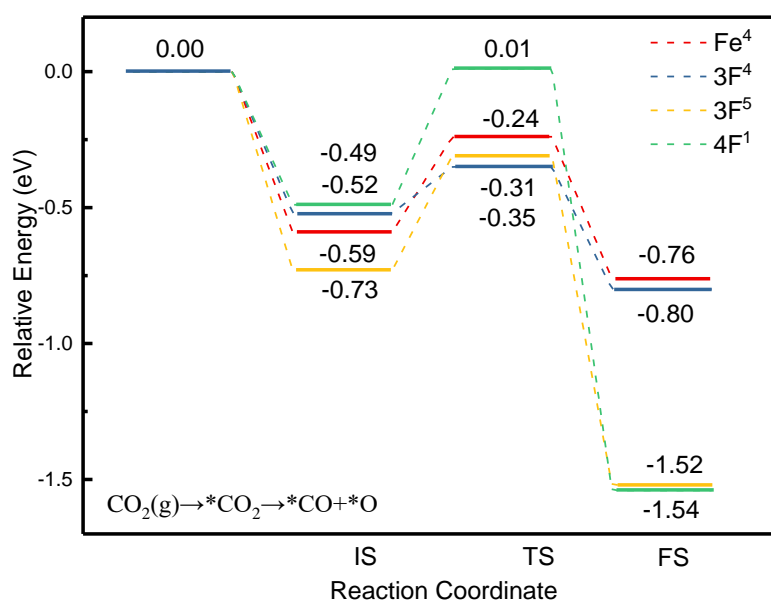
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201 Fig. S7. Top and side views of charge densities for stable CO<sub>2</sub> adsorption structure on  
 202  $\chi$ -Fe<sub>5</sub>C<sub>2</sub> (510). (Fe atoms in purple; O atoms in red; C atoms in gray.) Yellow and cyan  
 203 isosurfaces represent the charge accumulation (i.e. a gain of electron density) and  
 204 depletion (i.e. a loss of electron density) in the system, respectively.

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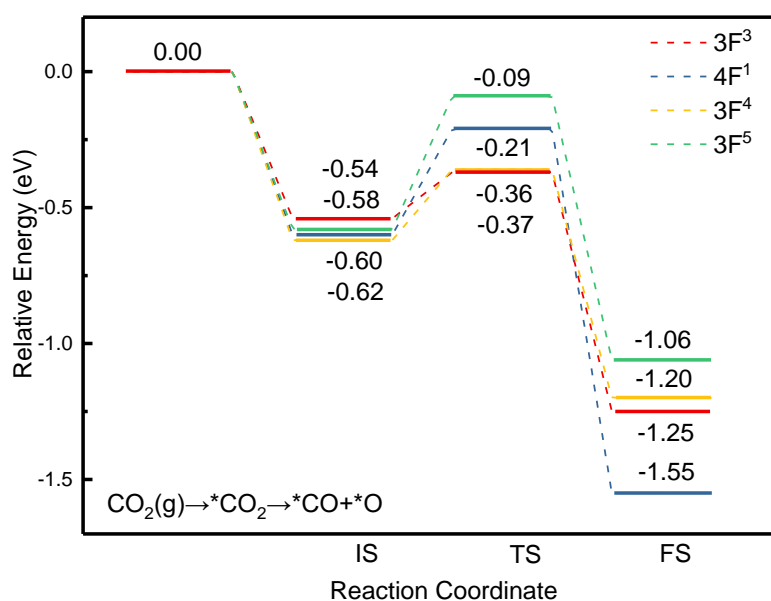
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208 Fig. S8. Potential energy profiles of CO<sub>2</sub> direct dissociation for different configurations

209 on χ-Fe<sub>5</sub>C<sub>2</sub> (510) surface.

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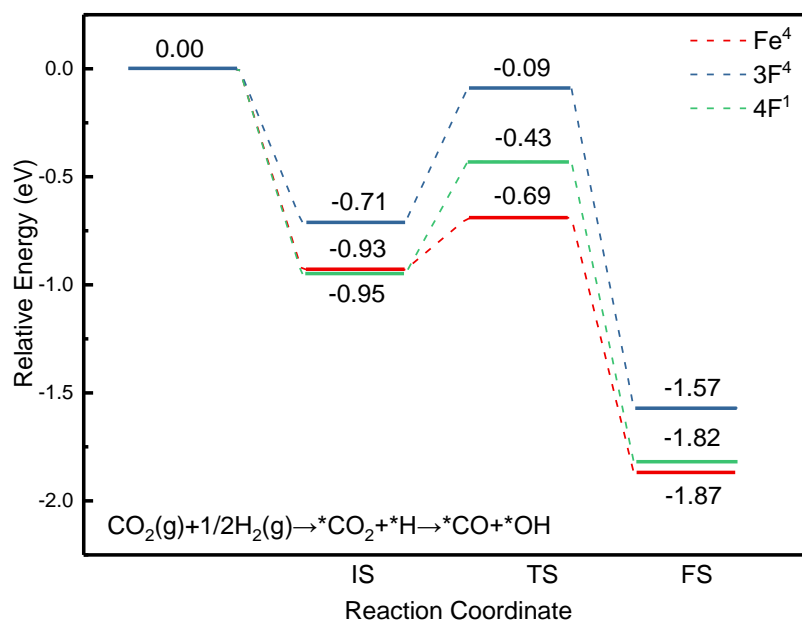
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213 Fig. S9. Potential energy profiles of CO<sub>2</sub> direct dissociation for different configurations

214 on θ-Fe<sub>3</sub>C (031) surface.

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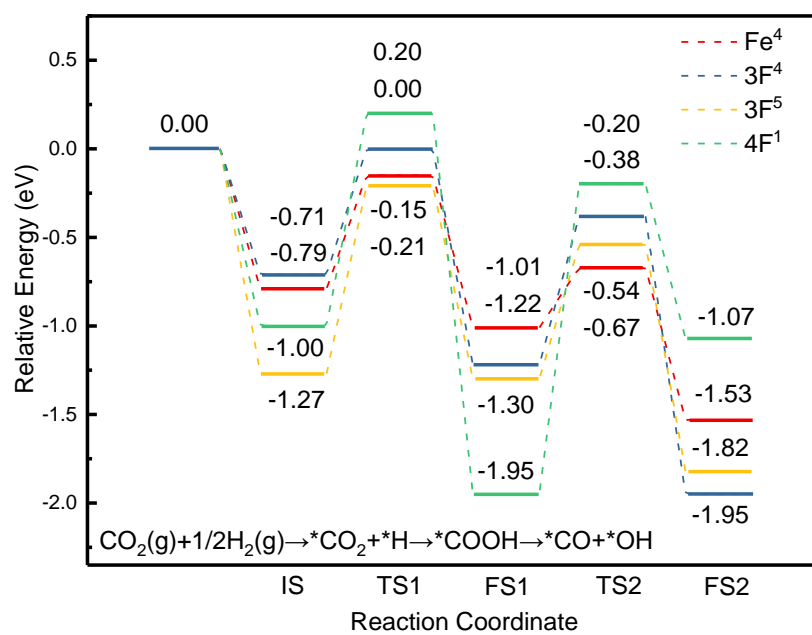
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218 Fig. S10. Potential energy profiles of CO<sub>2</sub> dissociation with H assistance (\*CO and  
219 \*OH pathway) for different configurations on  $\chi$ -Fe<sub>5</sub>C<sub>2</sub> (510) surface.

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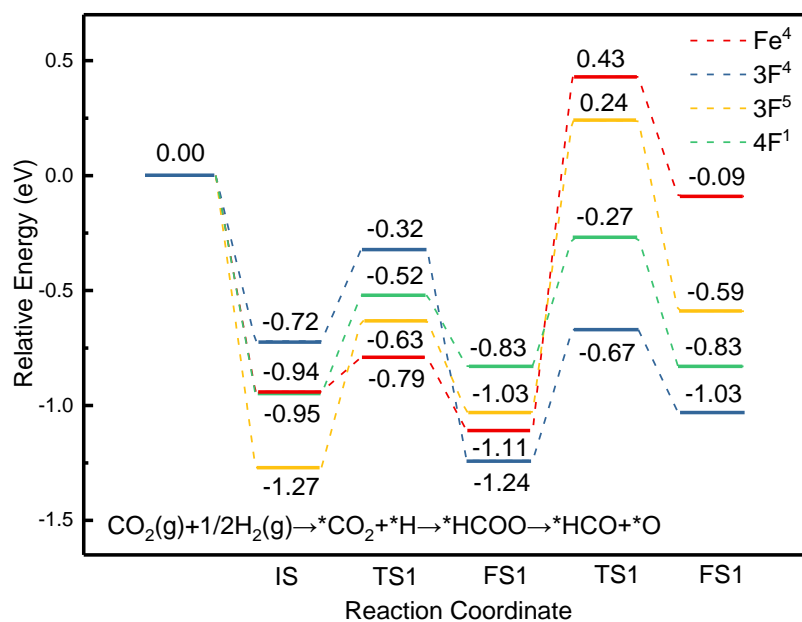


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223 Fig. S11. Potential energy profiles of CO<sub>2</sub> dissociation with H assistance (\*COOH224 pathway) for different configurations on  $\chi$ -Fe<sub>5</sub>C<sub>2</sub> (510) surface.

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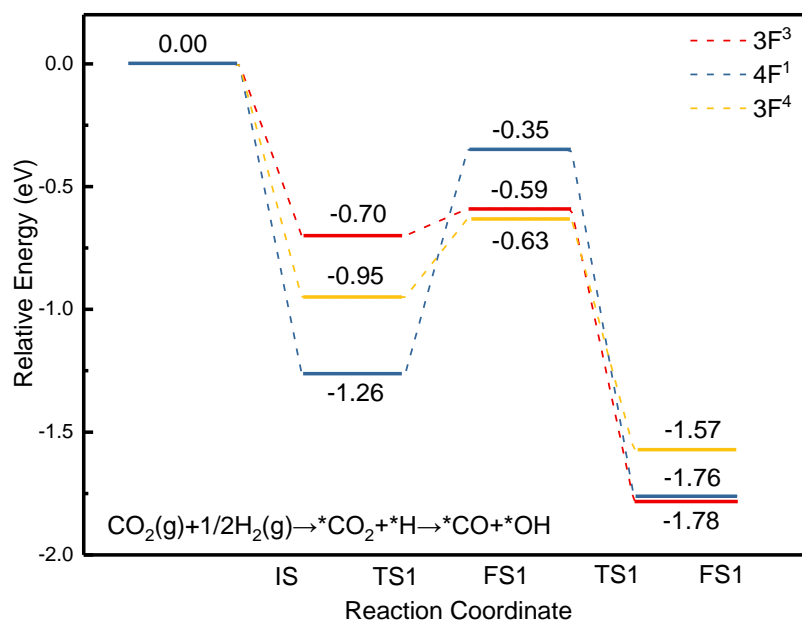


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228 Fig. S12. Potential energy profiles of CO<sub>2</sub> dissociation with H assistance (\*HCOO

229 pathway) for different configurations on  $\chi$ -Fe<sub>5</sub>C<sub>2</sub> (510) surface.

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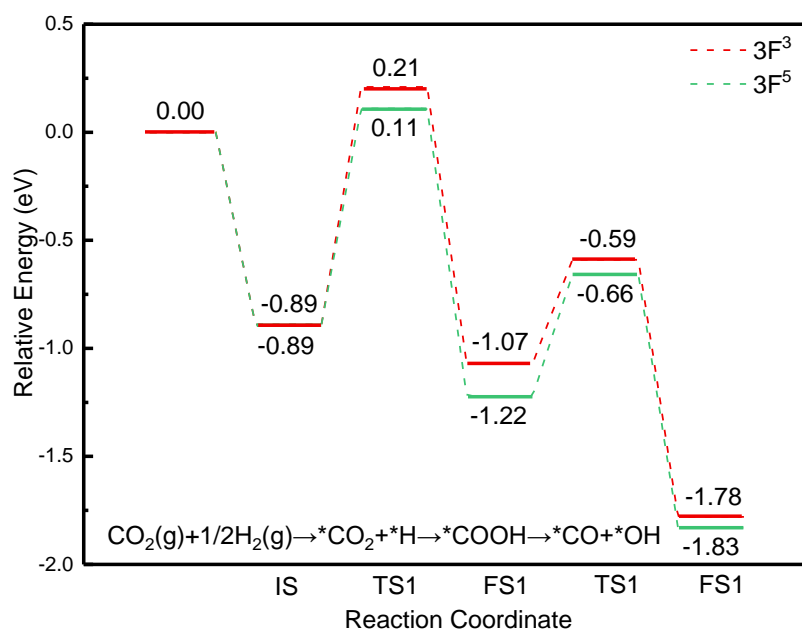


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233 Fig. S13. Potential energy profiles of CO<sub>2</sub> dissociation with H assistance (\*CO and

234 \*OH pathway) for different configurations on θ-Fe<sub>3</sub>C (031) surface.

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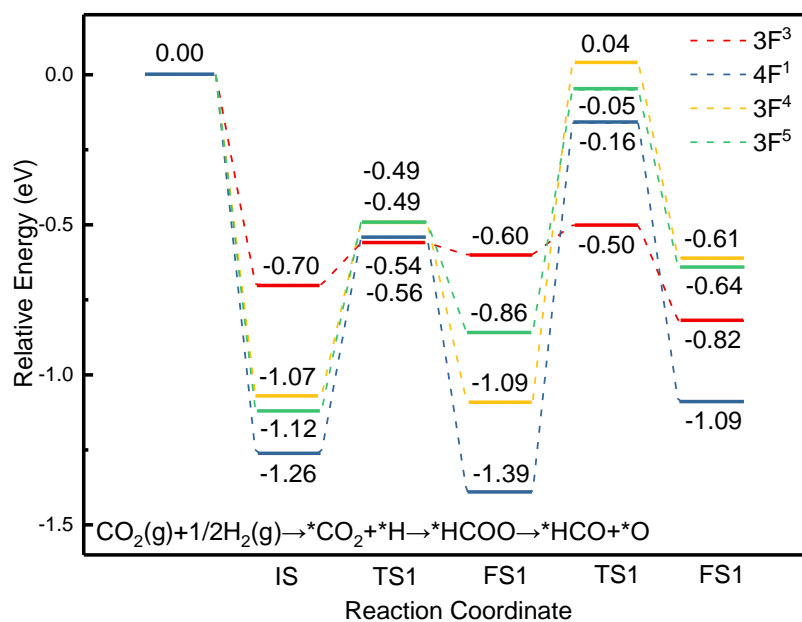
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238 Fig. S14. Potential energy profiles of CO<sub>2</sub> dissociation with H assistance (\*COOH

239 pathway) for different configurations on  $\theta$ -Fe<sub>3</sub>C (031) surface.

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243 Fig. S15. Potential energy profiles of CO<sub>2</sub> dissociation with H assistance (\*HCOO

244 pathway) for different configurations on  $\theta\text{-Fe}_3\text{C}$  (031) surface.

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Table S1. The lattice parameters of  $\chi$ -Fe<sub>5</sub>C<sub>2</sub> and  $\theta$ -Fe<sub>3</sub>C catalysts in this work and in literatures.

| Catalysts                              | Method | a(Å)  | b(Å) | c(Å) | $\alpha(^{\circ})$ | $\beta(^{\circ})$ | $\gamma(^{\circ})$ | ref       |
|--|--------|-------|------|------|--------------------|-------------------|--------------------|-----------|
| $\chi$ -Fe <sub>5</sub> C <sub>2</sub> | Expt.  | 11.59 | 4.58 | 5.06 | 90.00              | 97.75             | 90.00              | [16]      |
|  | PBE    | 11.55 | 4.50 | 4.98 | 90.00              | 97.62             | 90.00              | [17]      |
|  | PBE    | 11.58 | 4.51 | 4.99 | 90.00              | 96.64             | 90.00              | [18]      |
|  | PBE    | 11.56 | 4.51 | 4.99 | 90.00              | 97.67             | 90.00              | This work |
| $\theta$ -Fe <sub>3</sub> C            | Expt.  | 5.09  | 6.74 | 4.52 | 90.00              | 90.00             | 90.00              | [19]      |
|  | PBE    | 5.00  | 6.40 | 4.36 | 90.00              | 90.00             | 90.00              | [14]      |
|  | PBE    | 5.03  | 6.73 | 4.48 | 90.00              | 90.00             | 90.00              | [20]      |
|  | PBE    | 5.03  | 6.73 | 4.48 | 90.00              | 90.00             | 90.00              | This work |

Table S2. Calculated surface energies of different facets of  $\chi$ -Fe<sub>5</sub>C<sub>2</sub> and  $\theta$ -Fe<sub>3</sub>C catalysts.

| Phase                                  | Surface | Surface energy (J/m <sup>2</sup> ) |
|--|---------|------------------------------------|
| $\chi$ -Fe <sub>5</sub> C <sub>2</sub> | 001     | 2.72                               |
|  | 010     | 3.44                               |
|  | 100     | 3.37                               |
|  | 011     | 3.01                               |
|  | 101     | 3.28                               |
|  | 110     | 3.17                               |
|  | 111     | 2.80                               |
|  | 510     | 1.78                               |
| $\theta$ -Fe <sub>3</sub> C            | 001     | 2.51                               |
|  | 010     | 2.56                               |
|  | 100     | 2.86                               |
|  | 011     | 2.68                               |
|  | 101     | 2.51                               |
|  | 110     | 2.50                               |
|  | 111     | 2.36                               |
|  | 031     | 2.27                               |

Table S3. The surface energies of different termination for  $\chi$ -Fe<sub>5</sub>C<sub>2</sub> (510) and  $\theta$ -Fe<sub>3</sub>C (031) surfaces

| Surface                                      | Surface termination | Surface energy(J/m <sup>2</sup> ) |
|--|---------------------|-----------------------------------|
| $\chi$ -Fe <sub>5</sub> C <sub>2</sub> (510) | Mixed termination   | 1.78                              |
|  | C-termination       | 2.43                              |
|  | Fe-termination      | 2.43                              |
|  | Mixed termination   | 2.27                              |
| $\theta$ -Fe <sub>3</sub> C (031)            | C-termination       | 2.81                              |
|  | Fe-termination      | 2.81                              |

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Table S4. Influence of slab thickness on CO adsorption energy.

| Surface                                      | Thickness (Å) | $E_{ads}$ (eV) | $\Delta E_{ads}$ (eV) |
|--|---------------|----------------|-----------------------|
| $\chi$ -Fe <sub>5</sub> C <sub>2</sub> (510) | 3.93          | -2.07          | 0.01                  |
|  | 5.89          | -2.06          |                       |
| $\theta$ -Fe <sub>3</sub> C (031)            | 4.01          | -2.05          | 0.02                  |
|  | 6.02          | -2.07          |                       |

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Table S5. Influence of vacuum heights on CO adsorption energy.

| Surface                                      | Thickness (Å) | $E_{ads}$ (eV) | $\Delta E_{ads}$ (eV) |
|--|---------------|----------------|-----------------------|
| $\chi$ -Fe <sub>5</sub> C <sub>2</sub> (510) | 10.5          | -2.06          | 0.00                  |
|  | 12.0          | -2.06          |                       |
| $\theta$ -Fe <sub>3</sub> C (031)            | 10.5          | -2.05          | 0.01                  |
|  | 12.0          | -2.06          |                       |

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Table S6. Influence of supercell sizes on CO and CO<sub>2</sub> adsorption energies.

|  | Supercell size | $E_{ads}$ (eV) | $\Delta E_{ads}$ (eV) |
|--|----------------|----------------|-----------------------|
| $\chi$ -Fe <sub>5</sub> C <sub>2</sub> (510) |                |                |                       |
| CO   | p(1 × 1)       | -2.08          | 0.00                  |
|  | p(2 × 1)       | -2.08          |                       |
| CO <sub>2</sub>                              | p(1 × 1)       | -0.73          | 0.00                  |
|  | p(2 × 1)       | -0.73          |                       |
| $\theta$ -Fe <sub>3</sub> C (031)            |                |                |                       |
| CO   | p(1 × 1)       | -2.05          | 0.05                  |
|  | p(2 × 1)       | -2.10          |                       |
| CO <sub>2</sub>                              | p(1 × 1)       | -0.62          | 0.03                  |
|  | p(2 × 1)       | -0.65          |                       |

Table S7. Influence of Monkhorst–Pack meshes on CO adsorption energy.

| Surface                            | M-P meshes            | $E_{ads}(\text{eV})$ | $\Delta E_{ads}(\text{eV})$ |
|------------------------------------|-----------------------|----------------------|-----------------------------|
| $\chi\text{-Fe}_5\text{C}_2$ (510) | $3 \times 1 \times 1$ | -2.06                | 0.00                        |
|                                    | $5 \times 3 \times 1$ | -2.06                |                             |
| $\theta\text{-Fe}_3\text{C}$ (031) | $3 \times 1 \times 1$ | -2.05                | 0.03                        |
|                                    | $5 \times 3 \times 1$ | -2.08                |                             |

Tables S8. Adsorption energy and geometric parameters for CO<sub>2</sub> adsorbed on  $\chi$ -Fe<sub>5</sub>C<sub>2</sub> (510) facet.

| Sites            | $E_{ads}$ | Angle | $d_{C-O}$ |      | $d_{C-Fe}$ |      | $d_{O-Fe}$ |      | $d_{C-C}$ |      |    |
|------------------|-----------|-------|-----------|------|------------|------|------------|------|-----------|------|----|
|                  | (eV)      | (°)   | (Å)       |      | (Å)        |      |            | (Å)  |           | (Å)  |    |
| Fe <sup>1</sup>  | -0.22     | 140.6 | 1.24      | 1.25 | 1.99       | 2.33 | --         | 2.11 | 2.18      | --   | -- |
| Fe <sup>2</sup>  | -0.21     | 137.0 | 1.24      | 1.26 | 2.05       | 2.24 | --         | 2.04 | 2.28      | --   | -- |
| Fe <sup>3</sup>  | -0.72     | 125.5 | 1.30      | 1.30 | 1.94       | 2.09 | --         | 1.96 | 2.03      | --   | -- |
| Fe <sup>4</sup>  | -0.59     | 126.5 | 1.23      | 1.34 | 2.03       | 2.23 | --         | 2.00 | 2.11      | --   | -- |
| Fe <sup>5</sup>  | -0.25     | 179.4 | 1.17      | 1.18 | --         | --   | --         | 2.27 | --        | --   | -- |
| Fe <sup>6</sup>  | -0.71     | 137.6 | 1.25      | 1.26 | 1.96       | 2.24 | --         | 2.05 | 2.16      | --   | -- |
| Fe <sup>7</sup>  | -0.39     | 132.6 | 1.22      | 1.30 | 2.01       | --   | --         | 1.92 | --        | --   | -- |
| Fe <sup>8</sup>  | -0.29     | 130.2 | 1.22      | 1.31 | 2.03       | --   | --         | 1.89 | --        | --   | -- |
| Fe <sup>9</sup>  | -0.16     | 179.9 | 1.18      | 1.18 | --         | --   | --         | --   | --        | --   | -- |
| Fe <sup>10</sup> | -0.16     | 179.5 | 1.18      | 1.18 | --         | --   | --         | --   | --        | --   | -- |
| 3F <sup>1</sup>  | 0.09      | 140.1 | 1.23      | 1.25 | 2.04       | 2.28 | --         | 2.08 | 2.28      | --   | -- |
| 3F <sup>2</sup>  | -0.50     | 123.1 | 1.31      | 1.31 | 1.92       | 2.27 | 2.28       | 2.00 | 2.18      | 2.24 | -- |
| 3F <sup>3</sup>  | -0.55     | 123.4 | 1.30      | 1.32 | 1.93       | 2.19 | --         | 2.01 | 2.04      | --   | -- |
| 3F <sup>4</sup>  | -0.52     | 131.1 | 1.23      | 1.32 | 1.92       | --   | --         | 2.05 | 2.        | --   | -- |
| 3F <sup>5</sup>  | -0.73     | 138.8 | 1.25      | 1.25 | 2.00       | 2.14 | --         | 2.04 | 2.09      | --   | -- |



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|                             |       |       |      |      |      |      |    |      |      |    |      |
|-----------------------------|-------|-------|------|------|------|------|----|------|------|----|------|
| 3F <sup>6</sup>             | -0.32 | 139.7 | 1.24 | 1.26 | 1.94 | --   | -- | 2.04 | 2.29 | -- | --   |
| 3F <sup>7</sup>             | -0.22 | 125.2 | 1.30 | 1.30 | 1.92 | 2.29 | -- | 2.16 | 2.25 | -- | --   |
| 3F <sup>8</sup>             | -0.14 | 179.9 | 1.18 | 1.18 | --   | --   | -- | --   | --   | -- | --   |
| 3F <sup>9</sup>             | -0.22 | 137.0 | 1.24 | 1.26 | 2.04 | 2.24 | -- | 2.04 | 2.28 | -- | --   |
| 3F <sup>10</sup>            | -0.17 | 136.8 | 1.24 | 1.26 | 2.04 | 2.23 | -- | 2.04 | 2.27 | -- | --   |
| 4F <sup>1</sup>             | -0.49 | 128.3 | 1.22 | 1.34 | 2.04 | 2.17 | -- | 2.03 | 2.06 | -- | --   |
| 4F <sup>2</sup>             | -0.32 | 126.4 | 1.21 | 1.36 | 2.01 | --   | -- | 2.01 | 2.08 | -- | --   |
| 4F <sup>3</sup>             | -0.17 | 140.7 | 1.24 | 1.24 | 1.99 | 2.30 | -- | 2.11 | 2.18 | -- | --   |
| C <sub>S</sub> <sup>1</sup> | 0.34  | 126.1 | 1.21 | 1.39 | --   | --   | -- | 2.08 | 2.14 | -- | 1.52 |
| C <sub>S</sub> <sup>2</sup> | -0.06 | 123.4 | 1.21 | 1.39 | --   | --   | -- | 2.00 | 2.15 | -- | 1.51 |

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Tables S9. Adsorption energy and geometric parameters for CO<sub>2</sub> adsorbed on  $\theta$ -Fe<sub>3</sub>C (031) facet.

| Sites           | $E_{ads}$ | Angle | $d_{C-O}$ |      | $d_{C-Fe}$ |      | $d_{O-Fe}$ |      | $d_{C-C}$ |      |
|-----------------|-----------|-------|-----------|------|------------|------|------------|------|-----------|------|
|                 | (eV)      | (°)   | (Å)       |      | (Å)        |      | (Å)        |      | (Å)       |      |
| Fe <sup>1</sup> | -0.42     | 138.1 | 1.24      | 1.26 | 1.96       | 2.28 | --         | 2.04 | 2.23      | --   |
| Fe <sup>2</sup> | -0.36     | 138.7 | 1.24      | 1.26 | 1.98       | 2.31 | --         | 2.03 | 2.23      | --   |
| Fe <sup>3</sup> | -0.49     | 122.6 | 1.30      | 1.34 | 1.94       | 2.07 | --         | 2.04 | 2.09      | 2.14 |
| Fe <sup>4</sup> | -0.56     | 125.1 | 1.30      | 1.30 | 1.95       | 2.10 | --         | 1.96 | 2.02      | --   |
| Fe <sup>5</sup> | -0.58     | 137.2 | 1.25      | 1.26 | 1.98       | 2.22 | --         | 2.05 | 2.17      | --   |
| Fe <sup>6</sup> | -0.54     | 138.6 | 1.24      | 1.26 | 1.97       | 2.20 | --         | 2.05 | 2.18      | --   |
| Fe <sup>7</sup> | -0.42     | 138.0 | 1.24      | 1.26 | 1.97       | 2.26 | --         | 2.04 | 2.22      | --   |
| Fe <sup>8</sup> | -0.36     | 138.8 | 1.24      | 1.26 | 1.97       | 2.33 | --         | 2.03 | 2.24      | --   |
| 3F <sup>1</sup> | 0.05      | 138.8 | 1.24      | 1.25 | 2.02       | 2.29 | --         | 2.09 | --        | --   |
| 3F <sup>2</sup> | -0.32     | 124.0 | 1.27      | 1.35 | 1.90       | 2.28 | 2.30       | 2.07 | 2.10      | 2.11 |
| 3F <sup>3</sup> | -0.54     | 122.5 | 1.29      | 1.34 | 1.91       | 2.16 | --         | 2.02 | 2.05      | 2.16 |
| 3F <sup>4</sup> | -0.62     | 130.8 | 1.23      | 1.33 | 1.93       | --   | --         | 2.06 | 2.10      | --   |
| 3F <sup>5</sup> | 0.58      | 136.9 | 1.25      | 1.26 | 1.99       | 2.21 | --         | 2.05 | 2.17      | --   |
| 3F <sup>6</sup> | -0.42     | 138.0 | 1.24      | 1.26 | 1.96       | 2.27 | --         | 2.04 | 2.23      | --   |
| 4F <sup>1</sup> | -0.60     | 122.4 | 1.30      | 1.34 | 1.91       | 2.17 | --         | 2.02 | 2.22      | 2.28 |
| 4F <sup>2</sup> | -0.34     | 136.9 | 1.23      | 1.27 | 1.98       | --   | --         | 1.99 | --        | --   |

|  |                 |      |       |      |      |    |    |    |      |    |    |      |
|--|-----------------|------|-------|------|------|----|----|----|------|----|----|------|
|  |                 |      |       |      |      |    |    |    |      |    |    |      |
|  | Cs <sup>1</sup> | 0.36 | 127.4 | 1.22 | 1.34 | -- | -- | -- | 1.92 | -- | -- | 1.54 |

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Table S10. The adsorption properties of reaction intermediates on  $\chi$ -Fe<sub>5</sub>C<sub>2</sub> (510) and  $\theta$ -Fe<sub>3</sub>C (031) surfaces.

| COOH                      |  |                                   |
|---------------------------|--|-----------------------------------|
| Facet                     | $\chi$ -Fe <sub>5</sub> C <sub>2</sub> (510) | $\theta$ -Fe <sub>3</sub> C (031) |
| E <sub>ads</sub> (eV)     | -3.16  | -2.86                             |
| Bader charge ( $\delta$ ) | 0.62   | 0.50                              |
| C-Fe bond length (Å)      | 1.91   | 1.90                              |
| O-Fe bond length (Å)      | 1.99   | 2.03                              |
| C-O bond length (Å)       | 1.33;1.34                                    | 1.29;1.35                         |
| O-H bond length (Å)       | 0.99   | 0.98                              |
| O-C-O angle (°)           | 111.9  | 113.9                             |
| Configuration             | mono-dentate                                 | mono-dentate                      |
| HCOO                      |  |                                   |
| Facet                     | $\chi$ -Fe <sub>5</sub> C <sub>2</sub> (510) | $\theta$ -Fe <sub>3</sub> C (031) |
| E <sub>ads</sub> (eV)     | -6.40  | -7.18                             |
| Bader charge ( $\delta$ ) | 0.89   | 0.62                              |
| C-Fe bond length (Å)      | 2.15;2.29;2.33                               | --                                |
| O-Fe bond length (Å)      | 1.92;1.96                                    | 1.95;2.00                         |
| C-O bond length (Å)       | 1.31;1.32                                    | 1.27;1.28                         |
| C-H bond length (Å)       | 1.19   | 1.11                              |

|                           |  |                                   |
|---------------------------|--|-----------------------------------|
| O-C-O angle (°)           | 122.5  | 126.5                             |
| Configuration             | bi-dentate                                   | bi-dentate                        |
| HCO                       |  |                                   |
| Facet                     | $\chi$ -Fe <sub>5</sub> C <sub>2</sub> (510) | $\theta$ -Fe <sub>3</sub> C (031) |
| E <sub>ads</sub> (eV)     | -3.06  | -3.11                             |
| Bader charge ( $\delta$ ) | 0.72   | 0.73                              |
| C-Fe bond length (Å)      | 1.89;2.15                                    | 1.89;2.11                         |
| O-Fe bond length (Å)      | 1.96;2.18                                    | 1.98;2.08                         |
| C-O bond length (Å)       | 1.34   | 1.35                              |
| C-H bond length (Å)       | 1.11   | 1.11                              |
| CO                        |  |                                   |
| Facet                     | $\chi$ -Fe <sub>5</sub> C <sub>2</sub> (510) | $\theta$ -Fe <sub>3</sub> C (031) |
| E <sub>ads</sub> (eV)     | -2.09  | -2.08                             |
| Bader charge ( $\delta$ ) | 0.42   | 0.32                              |
| C-Fe bond length (Å)      | 1.78   | 1.94;2.04;2.05                    |
| C-O bond length (Å)       | 1.18   | 1.20                              |
| OH                        |  |                                   |
| Facet                     | $\chi$ -Fe <sub>5</sub> C <sub>2</sub> (510) | $\theta$ -Fe <sub>3</sub> C (031) |
| E <sub>ads</sub> (eV)     | -3.72  | -4.02                             |
| Bader charge ( $\delta$ ) | 0.57   | 0.58                              |

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|                      |                |                |
|----------------------|----------------|----------------|
| O-Fe bond length (Å) | 1.97;2.00;2.04 | 1.99;2.00;2.05 |
| O-H bond length (Å)  | 0.98           | 0.97           |

| Tables S11. *CO <sub>2</sub> dissociation on $\chi$ -Fe <sub>5</sub> C <sub>2</sub> (510) facet. |                 |         |                |                |
|--|-----------------|---------|----------------|----------------|
| $\chi$ -Fe <sub>5</sub> C <sub>2</sub> (510)   | Site            | Pathway | E <sub>a</sub> | E <sub>r</sub> |
|  | Fe <sup>4</sup> | *CO+*O  | 0.35           | -0.17          |
|  |                 | *COOH   | 0.64           | -0.74          |
|  |                 | *HCOO   | 1.37           | 0.85           |
|  |                 | *CO+*OH | 0.24           | -0.94          |
|  | 3F <sup>4</sup> | *CO+*O  | 0.17           | -0.28          |
|  |                 | *COOH   | 0.71           | -1.24          |
|  |                 | *HCOO   | 0.40           | -0.31          |
|  |                 | *CO+*OH | 0.62           | -0.86          |
|  | 3F <sup>5</sup> | *CO+*O  | 0.42           | -0.79          |
|  |                 | *COOH   | 1.06           | -0.55          |
|  |                 | *HCOO   | 1.51           | -0.68          |
|  |                 | *CO+*OH | --             | --             |
|  | 4F <sup>1</sup> | *CO+*O  | 0.50           | -1.05          |
|  |                 | *COOH   | 1.20           | -0.07          |
|  |                 | *HCOO   | 0.68           | 0.12           |
|  |                 | *CO+*OH | 0.52           | -0.87          |

Tables S12. \*CO<sub>2</sub> dissociation on  $\theta$ -Fe<sub>3</sub>C (031) facet.

|                                   | Site            | Pathway | $E_a$ | $E_r$ |
|-----------------------------------|-----------------|---------|-------|-------|
| $\theta$ -Fe <sub>3</sub> C (031) | 3F <sup>3</sup> | *CO+*O  | 0.17  | -0.71 |
|                                   |                 | *COOH   | 1.10  | -0.89 |
|                                   |                 | *HCOO   | 0.20  | -0.12 |
|                                   |                 | *CO+*OH | 0.11  | -1.08 |
|                                   | 3F <sup>4</sup> | *CO+*O  | 0.26  | -0.58 |
|                                   |                 | *COOH   | --    | --    |
|                                   |                 | *HCOO   | 1.11  | 0.46  |
|                                   |                 | *CO+*OH | 0.32  | -0.62 |
|                                   | 3F <sup>5</sup> | *CO+*O  | 0.49  | -0.48 |
|                                   |                 | *COOH   | 1.00  | -0.94 |
|                                   |                 | *HCOO   | 1.07  | 0.48  |
|                                   |                 | *CO+*OH | --    | --    |
|                                   | 4F <sup>1</sup> | *CO+*O  | 0.39  | -0.95 |
|                                   |                 | *COOH   | --    | --    |
|                                   |                 | *HCOO   | 1.10  | 0.17  |
|                                   |                 | *CO+*OH | 0.91  | -0.50 |



Table S13. The vibrational frequencies for CO<sub>2</sub> direct dissociation on  $\chi$ -Fe<sub>5</sub>C<sub>2</sub> (510) surface

| Initial state (IS)    |                         |                         |                         |                         |
|-----------------------|-------------------------|-------------------------|-------------------------|-------------------------|
| Site                  | Fe <sup>4</sup>         | 3F <sup>4</sup>         | 3F <sup>5</sup>         | 4F <sup>1</sup>         |
| 1f=                   | 1605.43cm <sup>-1</sup> | 1614.99cm <sup>-1</sup> | 1710.49cm <sup>-1</sup> | 1654.57cm <sup>-1</sup> |
| 2f=                   | 947.64cm <sup>-1</sup>  | 1071.60cm <sup>-1</sup> | 1158.43cm <sup>-1</sup> | 936.28cm <sup>-1</sup>  |
| 3f=                   | 678.32cm <sup>-1</sup>  | 691.90cm <sup>-1</sup>  | 677.34cm <sup>-1</sup>  | 673.04cm <sup>-1</sup>  |
| 4f=                   | 389.65cm <sup>-1</sup>  | 392.23cm <sup>-1</sup>  | 428.98cm <sup>-1</sup>  | 414.26cm <sup>-1</sup>  |
| 5f=                   | 297.41cm <sup>-1</sup>  | 339.18cm <sup>-1</sup>  | 302.60cm <sup>-1</sup>  | 292.44cm <sup>-1</sup>  |
| 6f=                   | 158.29cm <sup>-1</sup>  | 165.37cm <sup>-1</sup>  | 237.35cm <sup>-1</sup>  | 178.29cm <sup>-1</sup>  |
| 7f=                   | 148.17cm <sup>-1</sup>  | 145.78cm <sup>-1</sup>  | 110.44cm <sup>-1</sup>  | 151.91cm <sup>-1</sup>  |
| 8f=                   | 93.51cm <sup>-1</sup>   | 87.00cm <sup>-1</sup>   | 98.67cm <sup>-1</sup>   | 133.50cm <sup>-1</sup>  |
| 9f=                   | 53.75cm <sup>-1</sup>   | 55.46cm <sup>-1</sup>   | 56.20cm <sup>-1</sup>   | 92.38cm <sup>-1</sup>   |
| Transition state (TS) |                         |                         |                         |                         |
| 1f=                   | 1848.59cm <sup>-1</sup> | 1844.70cm <sup>-1</sup> | 1757.99cm <sup>-1</sup> | 1872.02cm <sup>-1</sup> |
| 2f=                   | 606.6cm <sup>-1</sup>   | 641.28cm <sup>-1</sup>  | 682cm <sup>-1</sup>     | 601.02cm <sup>-1</sup>  |
| 3f=                   | 428.11cm <sup>-1</sup>  | 445.07cm <sup>-1</sup>  | 512.60cm <sup>-1</sup>  | 437.47cm <sup>-1</sup>  |
| 4f=                   | 372.76cm <sup>-1</sup>  | 416.86cm <sup>-1</sup>  | 416.96cm <sup>-1</sup>  | 387.75cm <sup>-1</sup>  |
| 5f=                   | 284.70cm <sup>-1</sup>  | 299.86cm <sup>-1</sup>  | 316.60cm <sup>-1</sup>  | 270.17cm <sup>-1</sup>  |
| 6f=                   | 219.01cm <sup>-1</sup>  | 258.14cm <sup>-1</sup>  | 250.41cm <sup>-1</sup>  | 207.66cm <sup>-1</sup>  |

|                  |                         |                         |                         |                         |
|------------------|-------------------------|-------------------------|-------------------------|-------------------------|
| 7f=              | 147.68cm <sup>-1</sup>  | 99.25cm <sup>-1</sup>   | 153.98cm <sup>-1</sup>  | 131.30cm <sup>-1</sup>  |
| 8f=              | 70.03cm <sup>-1</sup>   | 37.37cm <sup>-1</sup>   | 40.89cm <sup>-1</sup>   | 67.46cm <sup>-1</sup>   |
| 9f/i=            | 387.95cm <sup>-1</sup>  | 381.95cm <sup>-1</sup>  | 139.95cm <sup>-1</sup>  | 418.48cm <sup>-1</sup>  |
| Final state (FS) |                         |                         |                         |                         |
| 1f=              | 1626.12cm <sup>-1</sup> | 1996.99cm <sup>-1</sup> | 1894.12cm <sup>-1</sup> | 1623.15cm <sup>-1</sup> |
| 2f=              | 460.86cm <sup>-1</sup>  | 579.1cm <sup>-1</sup>   | 442.48cm <sup>-1</sup>  | 463.12cm <sup>-1</sup>  |
| 3f=              | 440.25cm <sup>-1</sup>  | 426.75cm <sup>-1</sup>  | 437.36cm <sup>-1</sup>  | 443.75cm <sup>-1</sup>  |
| 4f=              | 284.89cm <sup>-1</sup>  | 416.84cm <sup>-1</sup>  | 386.59cm <sup>-1</sup>  | 286.01cm <sup>-1</sup>  |
| 5f=              | 270.54cm <sup>-1</sup>  | 390.45cm <sup>-1</sup>  | 361.70cm <sup>-1</sup>  | 274.30cm <sup>-1</sup>  |
| 6f=              | 238.71cm <sup>-1</sup>  | 379.37cm <sup>-1</sup>  | 284.95cm <sup>-1</sup>  | 249.08cm <sup>-1</sup>  |
| 7f=              | 209.88cm <sup>-1</sup>  | 207.83cm <sup>-1</sup>  | 268.20cm <sup>-1</sup>  | 220.36cm <sup>-1</sup>  |
| 8f=              | 153.83cm <sup>-1</sup>  | 66.41cm <sup>-1</sup>   | 92.07cm <sup>-1</sup>   | 149.29cm <sup>-1</sup>  |
| 9f=              | 129.41cm <sup>-1</sup>  | 58.30cm <sup>-1</sup>   | 57.17cm <sup>-1</sup>   | 113.82cm <sup>-1</sup>  |

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Table S14. The vibrational frequencies for CO<sub>2</sub> direct dissociation on  $\theta$ -Fe<sub>3</sub>C (031) surface

| IS   |                         |                         |                         |                         |
|------|-------------------------|-------------------------|-------------------------|-------------------------|
| Site | 3F <sup>3</sup>         | 3F <sup>4</sup>         | 3F <sup>5</sup>         | 4F <sup>1</sup>         |
| 1f=  | 1298.84cm <sup>-1</sup> | 1620.03cm <sup>-1</sup> | 1679.35cm <sup>-1</sup> | 1295.10cm <sup>-1</sup> |
| 2f=  | 1056.96cm <sup>-1</sup> | 1060.75cm <sup>-1</sup> | 1156.98cm <sup>-1</sup> | 1038.93cm <sup>-1</sup> |
| 3f=  | 693.71cm <sup>-1</sup>  | 686.43cm <sup>-1</sup>  | 681.93cm <sup>-1</sup>  | 684.75cm <sup>-1</sup>  |
| 4f=  | 441.26cm <sup>-1</sup>  | 388.91cm <sup>-1</sup>  | 425.59cm <sup>-1</sup>  | 404.79cm <sup>-1</sup>  |
| 5f=  | 344.86cm <sup>-1</sup>  | 344.11cm <sup>-1</sup>  | 309.43cm <sup>-1</sup>  | 341.10cm <sup>-1</sup>  |
| 6f=  | 267.58cm <sup>-1</sup>  | 190.32cm <sup>-1</sup>  | 209.2cm <sup>-1</sup>   | 242.16cm <sup>-1</sup>  |
| 7f=  | 193.11cm <sup>-1</sup>  | 152.34cm <sup>-1</sup>  | 119.85cm <sup>-1</sup>  | 200.39cm <sup>-1</sup>  |
| 8f=  | 163.05cm <sup>-1</sup>  | 93.37cm <sup>-1</sup>   | 97.15cm <sup>-1</sup>   | 152.88cm <sup>-1</sup>  |
| 9f=  | 149.02cm <sup>-1</sup>  | 80.57cm <sup>-1</sup>   | 67.10cm <sup>-1</sup>   | 123.59cm <sup>-1</sup>  |
| TS   |                         |                         |                         |                         |
| 1f=  | 1828.76cm <sup>-1</sup> | 1816.32cm <sup>-1</sup> | 1809.80cm <sup>-1</sup> | 1802.41cm <sup>-1</sup> |
| 2f=  | 633.33cm <sup>-1</sup>  | 635.41cm <sup>-1</sup>  | 627.65cm <sup>-1</sup>  | 618.84cm <sup>-1</sup>  |
| 3f=  | 433.05cm <sup>-1</sup>  | 433.03cm <sup>-1</sup>  | 445.01cm <sup>-1</sup>  | 395.74cm <sup>-1</sup>  |
| 4f=  | 411.79cm <sup>-1</sup>  | 407.95cm <sup>-1</sup>  | 425.24cm <sup>-1</sup>  | 364.47cm <sup>-1</sup>  |
| 5f=  | 303.53cm <sup>-1</sup>  | 304.62cm <sup>-1</sup>  | 297.27cm <sup>-1</sup>  | 309.69cm <sup>-1</sup>  |
| 6f=  | 261.54cm <sup>-1</sup>  | 260.32cm <sup>-1</sup>  | 261.99cm <sup>-1</sup>  | 264.92cm <sup>-1</sup>  |

|       |                        |                        |                        |                        |
|-------|------------------------|------------------------|------------------------|------------------------|
| 7f=   | 102.39cm <sup>-1</sup> | 109.98cm <sup>-1</sup> | 100.21cm <sup>-1</sup> | 127.90cm <sup>-1</sup> |
| 8f=   | 46.25cm <sup>-1</sup>  | 72.63cm <sup>-1</sup>  | 52.64cm <sup>-1</sup>  | 53.08cm <sup>-1</sup>  |
| 9f/i= | 401.62cm <sup>-1</sup> | 403.49cm <sup>-1</sup> | 422.67cm <sup>-1</sup> | 430.21cm <sup>-1</sup> |

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|     |                         |                         |                         |                         |
|-----|-------------------------|-------------------------|-------------------------|-------------------------|
| 1f= | 1910.73cm <sup>-1</sup> | 1952.32cm <sup>-1</sup> | 1884.99cm <sup>-1</sup> | 1912.14cm <sup>-1</sup> |
| 2f= | 550.75cm <sup>-1</sup>  | 460.83cm <sup>-1</sup>  | 504.36cm <sup>-1</sup>  | 531.80cm <sup>-1</sup>  |
| 3f= | 486.66cm <sup>-1</sup>  | 451.98cm <sup>-1</sup>  | 431.92cm <sup>-1</sup>  | 449.89cm <sup>-1</sup>  |
| 4f= | 418.56cm <sup>-1</sup>  | 431.82cm <sup>-1</sup>  | 385.94cm <sup>-1</sup>  | 403.04cm <sup>-1</sup>  |
| 5f= | 386.99cm <sup>-1</sup>  | 398.58cm <sup>-1</sup>  | 372.42cm <sup>-1</sup>  | 364.68cm <sup>-1</sup>  |
| 6f= | 361.37cm <sup>-1</sup>  | 333.29cm <sup>-1</sup>  | 314.35cm <sup>-1</sup>  | 329.30cm <sup>-1</sup>  |
| 7f= | 317.85cm <sup>-1</sup>  | 266.17cm <sup>-1</sup>  | 246.36cm <sup>-1</sup>  | 305.25cm <sup>-1</sup>  |
| 8f= | 157.49cm <sup>-1</sup>  | 92.82cm <sup>-1</sup>   | 73.40cm <sup>-1</sup>   | 97.70cm <sup>-1</sup>   |
| 9f= | 48.01cm <sup>-1</sup>   | 64.84cm <sup>-1</sup>   | 48.06cm <sup>-1</sup>   | 49.35cm <sup>-1</sup>   |

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Table S15. The vibrational frequencies for CO<sub>2</sub> dissociation with H assistance (\*CO and \*OH pathway) on  $\chi$ -Fe<sub>5</sub>C<sub>2</sub> (510) surface

| IS   |                         |                         |                 |                         |
|------|-------------------------|-------------------------|-----------------|-------------------------|
| Site | Fe <sup>4</sup>         | 3F <sup>4</sup>         | 3F <sup>5</sup> | 4F <sup>1</sup>         |
| 1f=  | 1581.15cm <sup>-1</sup> | 2751.75cm <sup>-1</sup> | --              | 1672.57cm <sup>-1</sup> |
| 2f=  | 1389.24cm <sup>-1</sup> | 1617.55cm <sup>-1</sup> | --              | 1221.45cm <sup>-1</sup> |
| 3f=  | 995.21cm <sup>-1</sup>  | 1087.78cm <sup>-1</sup> | --              | 1029.02cm <sup>-1</sup> |
| 4f=  | 958.29cm <sup>-1</sup>  | 694.19cm <sup>-1</sup>  | --              | 939.26cm <sup>-1</sup>  |
| 5f=  | 672.57cm <sup>-1</sup>  | 626.05cm <sup>-1</sup>  | --              | 822.26cm <sup>-1</sup>  |
| 6f=  | 442.90cm <sup>-1</sup>  | 549.31cm <sup>-1</sup>  | --              | 669.61cm <sup>-1</sup>  |
| 7f=  | 333.97cm <sup>-1</sup>  | 388.15cm <sup>-1</sup>  | --              | 407.40cm <sup>-1</sup>  |
| 8f=  | 277.29cm <sup>-1</sup>  | 335.58cm <sup>-1</sup>  | --              | 291.14cm <sup>-1</sup>  |
| 9f=  | 136.74cm <sup>-1</sup>  | 159.23cm <sup>-1</sup>  | --              | 184.01cm <sup>-1</sup>  |
| 10f= | 122.35cm <sup>-1</sup>  | 140.23cm <sup>-1</sup>  | --              | 150.68cm <sup>-1</sup>  |
| 11f= | 108.37cm <sup>-1</sup>  | 83.46cm <sup>-1</sup>   | --              | 118.93cm <sup>-1</sup>  |
| 12f= | 68.59cm <sup>-1</sup>   | 54.36cm <sup>-1</sup>   | --              | 89.75cm <sup>-1</sup>   |
| TS   |                         |                         |                 |                         |
| 1f=  | 1808.96cm <sup>-1</sup> | 1985.02cm <sup>-1</sup> | --              | 1976.79cm <sup>-1</sup> |
| 2f=  | 1392.89cm <sup>-1</sup> | 1285.37cm <sup>-1</sup> | --              | 967.53cm <sup>-1</sup>  |
| 3f=  | 947.40cm <sup>-1</sup>  | 823.79cm <sup>-1</sup>  | --              | 630.14cm <sup>-1</sup>  |

|        |                        |                         |    |                        |
|--------|------------------------|-------------------------|----|------------------------|
| 4f=    | 608.75cm <sup>-1</sup> | 499.23cm <sup>-1</sup>  | -- | 567.07cm <sup>-1</sup> |
| 5f=    | 427.54cm <sup>-1</sup> | 430.17cm <sup>-1</sup>  | -- | 470.02cm <sup>-1</sup> |
| 6f=    | 409.49cm <sup>-1</sup> | 425.12cm <sup>-1</sup>  | -- | 445.46cm <sup>-1</sup> |
| 7f=    | 375.86cm <sup>-1</sup> | 405.32cm <sup>-1</sup>  | -- | 429.49cm <sup>-1</sup> |
| 8f=    | 281.58cm <sup>-1</sup> | 350.55cm <sup>-1</sup>  | -- | 372.98cm <sup>-1</sup> |
| 9f=    | 209.35cm <sup>-1</sup> | 248.93cm <sup>-1</sup>  | -- | 274.06cm <sup>-1</sup> |
| 10f=   | 151.49cm <sup>-1</sup> | 114.88cm <sup>-1</sup>  | -- | 101.25cm <sup>-1</sup> |
| 11f=   | 77.08cm <sup>-1</sup>  | 66.45cm <sup>-1</sup>   | -- | 60.78cm <sup>-1</sup>  |
| 12f/i= | 392.45cm <sup>-1</sup> | 1591.85cm <sup>-1</sup> | -- | 650.85cm <sup>-1</sup> |

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FS

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|      |                         |                         |    |                         |
|------|-------------------------|-------------------------|----|-------------------------|
| 1f=  | 3685.79cm <sup>-1</sup> | 3682.58cm <sup>-1</sup> | -- | 3684.89cm <sup>-1</sup> |
| 2f=  | 1934.44cm <sup>-1</sup> | 1925.28cm <sup>-1</sup> | -- | 1901.78cm <sup>-1</sup> |
| 3f=  | 637.82cm <sup>-1</sup>  | 744.95cm <sup>-1</sup>  | -- | 739.19cm <sup>-1</sup>  |
| 4f=  | 578.02cm <sup>-1</sup>  | 585.56cm <sup>-1</sup>  | -- | 578.06cm <sup>-1</sup>  |
| 5f=  | 465.64cm <sup>-1</sup>  | 463.06cm <sup>-1</sup>  | -- | 458.03cm <sup>-1</sup>  |
| 6f=  | 450.96cm <sup>-1</sup>  | 449.41cm <sup>-1</sup>  | -- | 457.40cm <sup>-1</sup>  |
| 7f=  | 395.60cm <sup>-1</sup>  | 427.78cm <sup>-1</sup>  | -- | 412.07cm <sup>-1</sup>  |
| 8f=  | 362.50cm <sup>-1</sup>  | 416.76cm <sup>-1</sup>  | -- | 377.57cm <sup>-1</sup>  |
| 9f=  | 261.03cm <sup>-1</sup>  | 319.79cm <sup>-1</sup>  | -- | 292.42cm <sup>-1</sup>  |
| 10f= | 169.71cm <sup>-1</sup>  | 260.83cm <sup>-1</sup>  | -- | 167.93cm <sup>-1</sup>  |

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|     |      |                        |                        |    |                       |
|-----|------|------------------------|------------------------|----|-----------------------|
|     | 11f= | 100.81cm <sup>-1</sup> | 117.55cm <sup>-1</sup> | -- | 91.90cm <sup>-1</sup> |
|     | 12f= | 42.40cm <sup>-1</sup>  | 50.22cm <sup>-1</sup>  | -- | 38.15cm <sup>-1</sup> |
| 277 |      |                        |                        |    |                       |
| 278 |      |                        |                        |    |                       |

Table S16. The vibrational frequencies for CO<sub>2</sub> dissociation with H assistance (\*COOH pathway) on  $\chi$ -Fe<sub>5</sub>C<sub>2</sub> (510) surface

| IS   |                         |                         |                         |                         |
|------|-------------------------|-------------------------|-------------------------|-------------------------|
| Site | Fe <sup>4</sup>         | 3F <sup>4</sup>         | 3F <sup>5</sup>         | 4F <sup>1</sup>         |
| 1f=  | 1669.91cm <sup>-1</sup> | 2751.75cm <sup>-1</sup> | 1724.36cm <sup>-1</sup> | 1672.57cm <sup>-1</sup> |
| 2f=  | 1390.81cm <sup>-1</sup> | 1617.55cm <sup>-1</sup> | 1178.70cm <sup>-1</sup> | 1221.45cm <sup>-1</sup> |
| 3f=  | 936.47cm <sup>-1</sup>  | 1087.78cm <sup>-1</sup> | 1168.07cm <sup>-1</sup> | 1029.02cm <sup>-1</sup> |
| 4f=  | 866.68cm <sup>-1</sup>  | 694.19cm <sup>-1</sup>  | 1055.61cm <sup>-1</sup> | 939.26cm <sup>-1</sup>  |
| 5f=  | 683.92cm <sup>-1</sup>  | 626.05cm <sup>-1</sup>  | 800.58cm <sup>-1</sup>  | 822.26cm <sup>-1</sup>  |
| 6f=  | 629.46cm <sup>-1</sup>  | 549.31cm <sup>-1</sup>  | 675.01cm <sup>-1</sup>  | 669.61cm <sup>-1</sup>  |
| 7f=  | 461.44cm <sup>-1</sup>  | 388.15cm <sup>-1</sup>  | 440.88cm <sup>-1</sup>  | 407.40cm <sup>-1</sup>  |
| 8f=  | 313.37cm <sup>-1</sup>  | 335.58cm <sup>-1</sup>  | 296.20cm <sup>-1</sup>  | 291.14cm <sup>-1</sup>  |
| 9f=  | 194.83cm <sup>-1</sup>  | 159.23cm <sup>-1</sup>  | 235.51cm <sup>-1</sup>  | 184.01cm <sup>-1</sup>  |
| 10f= | 193.77cm <sup>-1</sup>  | 140.23cm <sup>-1</sup>  | 114.00cm <sup>-1</sup>  | 150.68cm <sup>-1</sup>  |
| 11f= | 158.64cm <sup>-1</sup>  | 83.46cm <sup>-1</sup>   | 97.31cm <sup>-1</sup>   | 118.93cm <sup>-1</sup>  |
| 12f= | 68.47cm <sup>-1</sup>   | 54.36cm <sup>-1</sup>   | 79.89cm <sup>-1</sup>   | 89.75cm <sup>-1</sup>   |
| TS1  |                         |                         |                         |                         |
| 1f=  | 1445.47cm <sup>-1</sup> | 1481.95cm <sup>-1</sup> | 1590.53cm <sup>-1</sup> | 1461.04cm <sup>-1</sup> |
| 2f=  | 1106.77cm <sup>-1</sup> | 1174.87cm <sup>-1</sup> | 1176.26cm <sup>-1</sup> | 1318.87cm <sup>-1</sup> |
| 3f=  | 982.05cm <sup>-1</sup>  | 1004.06cm <sup>-1</sup> | 1078.21cm <sup>-1</sup> | 1106.11cm <sup>-1</sup> |



|        |                         |                         |                         |                         |
|--------|-------------------------|-------------------------|-------------------------|-------------------------|
| 4f=    | 699.84cm <sup>-1</sup>  | 708.27cm <sup>-1</sup>  | 689.02cm <sup>-1</sup>  | 676.04cm <sup>-1</sup>  |
| 5f=    | 603.92cm <sup>-1</sup>  | 532.91cm <sup>-1</sup>  | 614.74cm <sup>-1</sup>  | 533.32cm <sup>-1</sup>  |
| 6f=    | 388.26cm <sup>-1</sup>  | 411.72cm <sup>-1</sup>  | 360.67cm <sup>-1</sup>  | 389.23cm <sup>-1</sup>  |
| 7f=    | 306.16cm <sup>-1</sup>  | 339.34cm <sup>-1</sup>  | 302.08cm <sup>-1</sup>  | 298.40cm <sup>-1</sup>  |
| 8f=    | 258.97cm <sup>-1</sup>  | 277.47cm <sup>-1</sup>  | 287.13cm <sup>-1</sup>  | 201.62cm <sup>-1</sup>  |
| 9f=    | 179.71cm <sup>-1</sup>  | 153.41cm <sup>-1</sup>  | 119.08cm <sup>-1</sup>  | 164.19cm <sup>-1</sup>  |
| 10f=   | 112.78cm <sup>-1</sup>  | 89.16cm <sup>-1</sup>   | 113.16cm <sup>-1</sup>  | 118.92cm <sup>-1</sup>  |
| 11f=   | 108.13cm <sup>-1</sup>  | 66.59cm <sup>-1</sup>   | 70.41cm <sup>-1</sup>   | 37.87cm <sup>-1</sup>   |
| 12f/i= | 1363.26cm <sup>-1</sup> | 1345.82cm <sup>-1</sup> | 1326.56cm <sup>-1</sup> | 1453.00cm <sup>-1</sup> |

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FS1

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|      |                         |                         |                         |                         |
|------|-------------------------|-------------------------|-------------------------|-------------------------|
| 1f=  | 3598.51cm <sup>-1</sup> | 3570.70cm <sup>-1</sup> | 3566.77cm <sup>-1</sup> | 3648.43cm <sup>-1</sup> |
| 2f=  | 1315.03cm <sup>-1</sup> | 1308.02cm <sup>-1</sup> | 1310.78cm <sup>-1</sup> | 1302.17cm <sup>-1</sup> |
| 3f=  | 1202.76cm <sup>-1</sup> | 1204.39cm <sup>-1</sup> | 1202.64cm <sup>-1</sup> | 1198.11cm <sup>-1</sup> |
| 4f=  | 1081.59cm <sup>-1</sup> | 1078.98cm <sup>-1</sup> | 1084.23cm <sup>-1</sup> | 1076.14cm <sup>-1</sup> |
| 5f=  | 680.01cm <sup>-1</sup>  | 692.31cm <sup>-1</sup>  | 695.73cm <sup>-1</sup>  | 672.37cm <sup>-1</sup>  |
| 6f=  | 559.60cm <sup>-1</sup>  | 686.34cm <sup>-1</sup>  | 691.21cm <sup>-1</sup>  | 523.69cm <sup>-1</sup>  |
| 7f=  | 462.80cm <sup>-1</sup>  | 469.08cm <sup>-1</sup>  | 465.82cm <sup>-1</sup>  | 422.18cm <sup>-1</sup>  |
| 8f=  | 317.68cm <sup>-1</sup>  | 350.43cm <sup>-1</sup>  | 351.29cm <sup>-1</sup>  | 311.60cm <sup>-1</sup>  |
| 9f=  | 246.75cm <sup>-1</sup>  | 261.01cm <sup>-1</sup>  | 260.15cm <sup>-1</sup>  | 239.58cm <sup>-1</sup>  |
| 10f= | 174.28cm <sup>-1</sup>  | 161.65cm <sup>-1</sup>  | 161.84cm <sup>-1</sup>  | 184.78cm <sup>-1</sup>  |

|      |                        |                        |                        |                        |
|------|------------------------|------------------------|------------------------|------------------------|
| 11f= | 154.45cm <sup>-1</sup> | 114.03cm <sup>-1</sup> | 104.06cm <sup>-1</sup> | 134.44cm <sup>-1</sup> |
| 12f= | 59.07cm <sup>-1</sup>  | 76.46cm <sup>-1</sup>  | 79.60cm <sup>-1</sup>  | 83.97cm <sup>-1</sup>  |

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TS2

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|        |                         |                         |                         |                         |
|--------|-------------------------|-------------------------|-------------------------|-------------------------|
| 1f=    | 3609.14cm <sup>-1</sup> | 3488.03cm <sup>-1</sup> | 3518.65cm <sup>-1</sup> | 3534.52cm <sup>-1</sup> |
| 2f=    | 1384.27cm <sup>-1</sup> | 1557.85cm <sup>-1</sup> | 1552.49cm <sup>-1</sup> | 1671.53cm <sup>-1</sup> |
| 3f=    | 1190.60cm <sup>-1</sup> | 1070.24cm <sup>-1</sup> | 1197.69cm <sup>-1</sup> | 903.82cm <sup>-1</sup>  |
| 4f=    | 1095.83cm <sup>-1</sup> | 845.08cm <sup>-1</sup>  | 1014.41cm <sup>-1</sup> | 709.67cm <sup>-1</sup>  |
| 5f=    | 687.40cm <sup>-1</sup>  | 573.36cm <sup>-1</sup>  | 617.74cm <sup>-1</sup>  | 611.45cm <sup>-1</sup>  |
| 6f=    | 580.37cm <sup>-1</sup>  | 520.58cm <sup>-1</sup>  | 530.70cm <sup>-1</sup>  | 434.22cm <sup>-1</sup>  |
| 7f=    | 464.81cm <sup>-1</sup>  | 304.16cm <sup>-1</sup>  | 345.59cm <sup>-1</sup>  | 366.36cm <sup>-1</sup>  |
| 8f=    | 337.01cm <sup>-1</sup>  | 232.69cm <sup>-1</sup>  | 227.92cm <sup>-1</sup>  | 266.35cm <sup>-1</sup>  |
| 9f=    | 250.18cm <sup>-1</sup>  | 142.92cm <sup>-1</sup>  | 106.29cm <sup>-1</sup>  | 192.81cm <sup>-1</sup>  |
| 10f=   | 160.19cm <sup>-1</sup>  | 102.90cm <sup>-1</sup>  | 81.49cm <sup>-1</sup>   | 93.16cm <sup>-1</sup>   |
| 11f=   | 94.98cm <sup>-1</sup>   | 53.98cm <sup>-1</sup>   | 56.02cm <sup>-1</sup>   | 67.81cm <sup>-1</sup>   |
| 12f/i= | 184.51cm <sup>-1</sup>  | 193.68cm <sup>-1</sup>  | 129.90cm <sup>-1</sup>  | 242.70cm <sup>-1</sup>  |

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FS2

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|     |                         |                         |                         |                         |
|-----|-------------------------|-------------------------|-------------------------|-------------------------|
| 1f= | 3526.96cm <sup>-1</sup> | 3740.15cm <sup>-1</sup> | 3724.18cm <sup>-1</sup> | 3746.58cm <sup>-1</sup> |
| 2f= | 1589.90cm <sup>-1</sup> | 1922.14cm <sup>-1</sup> | 1704.18cm <sup>-1</sup> | 1688.28cm <sup>-1</sup> |
| 3f= | 673.66cm <sup>-1</sup>  | 591.54cm <sup>-1</sup>  | 626.60cm <sup>-1</sup>  | 656.37cm <sup>-1</sup>  |
| 4f= | 581.94cm <sup>-1</sup>  | 516.60cm <sup>-1</sup>  | 554.77cm <sup>-1</sup>  | 564.90cm <sup>-1</sup>  |

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|      |                        |                        |                        |                        |
|------|------------------------|------------------------|------------------------|------------------------|
| 5f=  | 420.75cm <sup>-1</sup> | 449.76cm <sup>-1</sup> | 430.87cm <sup>-1</sup> | 442.67cm <sup>-1</sup> |
| 6f=  | 390.47cm <sup>-1</sup> | 437.15cm <sup>-1</sup> | 381.14cm <sup>-1</sup> | 314.53cm <sup>-1</sup> |
| 7f=  | 313.98cm <sup>-1</sup> | 429.08cm <sup>-1</sup> | 318.15cm <sup>-1</sup> | 278.55cm <sup>-1</sup> |
| 8f=  | 278.51cm <sup>-1</sup> | 409.15cm <sup>-1</sup> | 293.02cm <sup>-1</sup> | 245.74cm <sup>-1</sup> |
| 9f=  | 244.51cm <sup>-1</sup> | 293.54cm <sup>-1</sup> | 275.88cm <sup>-1</sup> | 217.09cm <sup>-1</sup> |
| 10f= | 226.36cm <sup>-1</sup> | 262.89cm <sup>-1</sup> | 249.96cm <sup>-1</sup> | 183.97cm <sup>-1</sup> |
| 11f= | 166.77cm <sup>-1</sup> | 65.59cm <sup>-1</sup>  | 136.37cm <sup>-1</sup> | 132.84cm <sup>-1</sup> |
| 12f= | 133.53cm <sup>-1</sup> | 45.97cm <sup>-1</sup>  | 126.06cm <sup>-1</sup> | 108.39cm <sup>-1</sup> |

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Table S17. The vibrational frequencies for CO<sub>2</sub> dissociation with H assistance (\*HCOO pathway) on  $\chi$ -Fe<sub>5</sub>C<sub>2</sub> (510) surface

| IS   |                         |                         |                         |                         |
|------|-------------------------|-------------------------|-------------------------|-------------------------|
| Site | Fe <sup>4</sup>         | 3F <sup>4</sup>         | 3F <sup>5</sup>         | 4F <sup>1</sup>         |
| 1f=  | 1651.15cm <sup>-1</sup> | 1628.50cm <sup>-1</sup> | 1724.36cm <sup>-1</sup> | 1656.00cm <sup>-1</sup> |
| 2f=  | 1270.17cm <sup>-1</sup> | 1227.66cm <sup>-1</sup> | 1178.70cm <sup>-1</sup> | 1219.87cm <sup>-1</sup> |
| 3f=  | 1084.96cm <sup>-1</sup> | 1066.13cm <sup>-1</sup> | 1168.07cm <sup>-1</sup> | 1025.77cm <sup>-1</sup> |
| 4f=  | 994.61cm <sup>-1</sup>  | 985.33cm <sup>-1</sup>  | 1055.61cm <sup>-1</sup> | 994.69cm <sup>-1</sup>  |
| 5f=  | 749.96cm <sup>-1</sup>  | 688.57cm <sup>-1</sup>  | 800.58cm <sup>-1</sup>  | 672.21cm <sup>-1</sup>  |
| 6f=  | 670.46cm <sup>-1</sup>  | 646.73cm <sup>-1</sup>  | 675.01cm <sup>-1</sup>  | 652.93cm <sup>-1</sup>  |
| 7f=  | 460.11cm <sup>-1</sup>  | 381.59cm <sup>-1</sup>  | 440.88cm <sup>-1</sup>  | 409.91cm <sup>-1</sup>  |
| 8f=  | 287.89cm <sup>-1</sup>  | 329.62cm <sup>-1</sup>  | 296.20cm <sup>-1</sup>  | 282.08cm <sup>-1</sup>  |
| 9f=  | 216.92cm <sup>-1</sup>  | 187.16cm <sup>-1</sup>  | 235.51cm <sup>-1</sup>  | 174.56cm <sup>-1</sup>  |
| 10f= | 154.39cm <sup>-1</sup>  | 141.58cm <sup>-1</sup>  | 114.00cm <sup>-1</sup>  | 151.83cm <sup>-1</sup>  |
| 11f= | 123.02cm <sup>-1</sup>  | 94.83cm <sup>-1</sup>   | 97.31cm <sup>-1</sup>   | 118.09cm <sup>-1</sup>  |
| 12f= | 77.03cm <sup>-1</sup>   | 34.95cm <sup>-1</sup>   | 79.89cm <sup>-1</sup>   | 100.71cm <sup>-1</sup>  |
| TS1  |                         |                         |                         |                         |
| 1f=  | 1735.5cm <sup>-1</sup>  | 1784.70cm <sup>-1</sup> | 1794.99cm <sup>-1</sup> | 2472.45cm <sup>-1</sup> |
| 2f=  | 1384.51cm <sup>-1</sup> | 1400.44cm <sup>-1</sup> | 1403.77cm <sup>-1</sup> | 1311.43cm <sup>-1</sup> |
| 3f=  | 1092.89cm <sup>-1</sup> | 1100.35cm <sup>-1</sup> | 1100.36cm <sup>-1</sup> | 1173.90cm <sup>-1</sup> |

|        |                        |                        |                        |                         |
|--------|------------------------|------------------------|------------------------|-------------------------|
| 4f=    | 836.19cm <sup>-1</sup> | 687.39cm <sup>-1</sup> | 722.86cm <sup>-1</sup> | 1086.78cm <sup>-1</sup> |
| 5f=    | 809.66cm <sup>-1</sup> | 589.73cm <sup>-1</sup> | 665.15cm <sup>-1</sup> | 801.16cm <sup>-1</sup>  |
| 6f=    | 636.54cm <sup>-1</sup> | 522.15cm <sup>-1</sup> | 520.66cm <sup>-1</sup> | 627.47cm <sup>-1</sup>  |
| 7f=    | 367.84cm <sup>-1</sup> | 335.94cm <sup>-1</sup> | 332.14cm <sup>-1</sup> | 337.29cm <sup>-1</sup>  |
| 8f=    | 285.08cm <sup>-1</sup> | 296.59cm <sup>-1</sup> | 303.62cm <sup>-1</sup> | 323.98cm <sup>-1</sup>  |
| 9f=    | 245.14cm <sup>-1</sup> | 190.38cm <sup>-1</sup> | 180.34cm <sup>-1</sup> | 300.09cm <sup>-1</sup>  |
| 10f=   | 207.45cm <sup>-1</sup> | 153.82cm <sup>-1</sup> | 162.57cm <sup>-1</sup> | 161.68cm <sup>-1</sup>  |
| 11f=   | 68.67cm <sup>-1</sup>  | 128.42cm <sup>-1</sup> | 130.56cm <sup>-1</sup> | 106.71cm <sup>-1</sup>  |
| 12f/i= | 152.47cm <sup>-1</sup> | 609.68cm <sup>-1</sup> | 714.85cm <sup>-1</sup> | 142.01cm <sup>-1</sup>  |

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FS1

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|      |                         |                         |                         |                         |
|------|-------------------------|-------------------------|-------------------------|-------------------------|
| 1f=  | 2960.80cm <sup>-1</sup> | 3028.33cm <sup>-1</sup> | 2828.91cm <sup>-1</sup> | 2985.31cm <sup>-1</sup> |
| 2f=  | 1677.98cm <sup>-1</sup> | 1274.43cm <sup>-1</sup> | 1316.58cm <sup>-1</sup> | 1306.68cm <sup>-1</sup> |
| 3f=  | 1321.40cm <sup>-1</sup> | 1175.16cm <sup>-1</sup> | 1243.59cm <sup>-1</sup> | 1265.29cm <sup>-1</sup> |
| 4f=  | 1115.73cm <sup>-1</sup> | 1066.81cm <sup>-1</sup> | 1148.53cm <sup>-1</sup> | 1107.69cm <sup>-1</sup> |
| 5f=  | 988.69cm <sup>-1</sup>  | 820.63cm <sup>-1</sup>  | 848.91cm <sup>-1</sup>  | 807.14cm <sup>-1</sup>  |
| 6f=  | 719.59cm <sup>-1</sup>  | 613.92cm <sup>-1</sup>  | 622.06cm <sup>-1</sup>  | 604.83cm <sup>-1</sup>  |
| 7f=  | 328.52cm <sup>-1</sup>  | 475.15cm <sup>-1</sup>  | 446.28cm <sup>-1</sup>  | 417.46cm <sup>-1</sup>  |
| 8f=  | 248.83cm <sup>-1</sup>  | 386.72cm <sup>-1</sup>  | 386.88cm <sup>-1</sup>  | 376.20cm <sup>-1</sup>  |
| 9f=  | 181.57cm <sup>-1</sup>  | 301.39cm <sup>-1</sup>  | 229.86cm <sup>-1</sup>  | 262.16cm <sup>-1</sup>  |
| 10f= | 110.36cm <sup>-1</sup>  | 228.03cm <sup>-1</sup>  | 131.57cm <sup>-1</sup>  | 171.76cm <sup>-1</sup>  |

|        |                         |                         |                         |                         |
|--------|-------------------------|-------------------------|-------------------------|-------------------------|
| 11f=   | 48.14cm <sup>-1</sup>   | 126.91cm <sup>-1</sup>  | 115.56cm <sup>-1</sup>  | 141.85cm <sup>-1</sup>  |
| 12f=   | 17.58cm <sup>-1</sup>   | 90.84cm <sup>-1</sup>   | 87.93cm <sup>-1</sup>   | 108.38cm <sup>-1</sup>  |
| TS2    |                         |                         |                         |                         |
| 1f=    | 2965.27cm <sup>-1</sup> | 2939.69cm <sup>-1</sup> | 2989.81cm <sup>-1</sup> | 2875.97cm <sup>-1</sup> |
| 2f=    | 1242.80cm <sup>-1</sup> | 1214.93cm <sup>-1</sup> | 1318.68cm <sup>-1</sup> | 1424.94cm <sup>-1</sup> |
| 3f=    | 1111.92cm <sup>-1</sup> | 1195.09cm <sup>-1</sup> | 1147.58cm <sup>-1</sup> | 1177.43cm <sup>-1</sup> |
| 4f=    | 765.34cm <sup>-1</sup>  | 672.40cm <sup>-1</sup>  | 842.76cm <sup>-1</sup>  | 702.90cm <sup>-1</sup>  |
| 5f=    | 526.28cm <sup>-1</sup>  | 525.00cm <sup>-1</sup>  | 705.86cm <sup>-1</sup>  | 558.07cm <sup>-1</sup>  |
| 6f=    | 426.30cm <sup>-1</sup>  | 489.13cm <sup>-1</sup>  | 487.16cm <sup>-1</sup>  | 519.53cm <sup>-1</sup>  |
| 7f=    | 322.74cm <sup>-1</sup>  | 456.54cm <sup>-1</sup>  | 353.50cm <sup>-1</sup>  | 468.23cm <sup>-1</sup>  |
| 8f=    | 272.15cm <sup>-1</sup>  | 367.61cm <sup>-1</sup>  | 307.48cm <sup>-1</sup>  | 304.73cm <sup>-1</sup>  |
| 9f=    | 239.02cm <sup>-1</sup>  | 297.16cm <sup>-1</sup>  | 164.88cm <sup>-1</sup>  | 258.48cm <sup>-1</sup>  |
| 10f=   | 221.16cm <sup>-1</sup>  | 199.06cm <sup>-1</sup>  | 120.61cm <sup>-1</sup>  | 171.80cm <sup>-1</sup>  |
| 11f=   | 196.69cm <sup>-1</sup>  | 144.00cm <sup>-1</sup>  | 74.67cm <sup>-1</sup>   | 143.83cm <sup>-1</sup>  |
| 12f/i= | 176.47cm <sup>-1</sup>  | 158.24cm <sup>-1</sup>  | 344.63cm <sup>-1</sup>  | 172.38cm <sup>-1</sup>  |
| FS2    |                         |                         |                         |                         |
| 1f=    | 3034.81cm <sup>-1</sup> | 3740.15cm <sup>-1</sup> | 2890.53cm <sup>-1</sup> | 2921.68cm <sup>-1</sup> |
| 2f=    | 1241.56cm <sup>-1</sup> | 1922.14cm <sup>-1</sup> | 1277.56cm <sup>-1</sup> | 1181.88cm <sup>-1</sup> |
| 3f=    | 986.18cm <sup>-1</sup>  | 591.54cm <sup>-1</sup>  | 1179.62cm <sup>-1</sup> | 1162.12cm <sup>-1</sup> |
| 4f=    | 801.58cm <sup>-1</sup>  | 516.60cm <sup>-1</sup>  | 688.52cm <sup>-1</sup>  | 684.90cm <sup>-1</sup>  |

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|      |                        |                        |                        |                        |
|------|------------------------|------------------------|------------------------|------------------------|
| 5f=  | 643.88cm <sup>-1</sup> | 449.76cm <sup>-1</sup> | 508.95cm <sup>-1</sup> | 544.31cm <sup>-1</sup> |
| 6f=  | 423.01cm <sup>-1</sup> | 437.15cm <sup>-1</sup> | 491.27cm <sup>-1</sup> | 508.74cm <sup>-1</sup> |
| 7f=  | 417.37cm <sup>-1</sup> | 429.08cm <sup>-1</sup> | 378.42cm <sup>-1</sup> | 405.96cm <sup>-1</sup> |
| 8f=  | 393.68cm <sup>-1</sup> | 409.15cm <sup>-1</sup> | 375.29cm <sup>-1</sup> | 362.35cm <sup>-1</sup> |
| 9f=  | 277.26cm <sup>-1</sup> | 293.54cm <sup>-1</sup> | 262.51cm <sup>-1</sup> | 343.36cm <sup>-1</sup> |
| 10f= | 266.87cm <sup>-1</sup> | 262.89cm <sup>-1</sup> | 194.11cm <sup>-1</sup> | 316.99cm <sup>-1</sup> |
| 11f= | 217.44cm <sup>-1</sup> | 65.59cm <sup>-1</sup>  | 133.54cm <sup>-1</sup> | 275.17cm <sup>-1</sup> |
| 12f= | 160.00cm <sup>-1</sup> | 45.97cm <sup>-1</sup>  | 89.73cm <sup>-1</sup>  | 215.64cm <sup>-1</sup> |

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Table S18. The vibrational frequencies for CO<sub>2</sub> dissociation with H assistance (\*CO and \*OH pathway) on  $\theta$ -Fe<sub>3</sub>C (031) surface

| IS   |                         |                         |                 |                         |
|------|-------------------------|-------------------------|-----------------|-------------------------|
| Site | 3F <sup>3</sup>         | 3F <sup>4</sup>         | 3F <sup>5</sup> | 4F <sup>1</sup>         |
| 1f=  | 1523.09cm <sup>-1</sup> | 1672.13cm <sup>-1</sup> | --              | 1312.70cm <sup>-1</sup> |
| 2f=  | 1356.58cm <sup>-1</sup> | 1528.09cm <sup>-1</sup> | --              | 1258.23cm <sup>-1</sup> |
| 3f=  | 1072.61cm <sup>-1</sup> | 1092.36cm <sup>-1</sup> | --              | 1066.51cm <sup>-1</sup> |
| 4f=  | 950.52cm <sup>-1</sup>  | 847.05cm <sup>-1</sup>  | --              | 972.02cm <sup>-1</sup>  |
| 5f=  | 694.49cm <sup>-1</sup>  | 676.54cm <sup>-1</sup>  | --              | 789.26cm <sup>-1</sup>  |
| 6f=  | 575.39cm <sup>-1</sup>  | 495.94cm <sup>-1</sup>  | --              | 688.48cm <sup>-1</sup>  |
| 7f=  | 468.92cm <sup>-1</sup>  | 345.06cm <sup>-1</sup>  | --              | 437.69cm <sup>-1</sup>  |
| 8f=  | 316.21cm <sup>-1</sup>  | 337.12cm <sup>-1</sup>  | --              | 344.56cm <sup>-1</sup>  |
| 9f=  | 274.03cm <sup>-1</sup>  | 236.30cm <sup>-1</sup>  | --              | 253.09cm <sup>-1</sup>  |
| 10f= | 204.89cm <sup>-1</sup>  | 179.18cm <sup>-1</sup>  | --              | 205.56cm <sup>-1</sup>  |
| 11f= | 188.68cm <sup>-1</sup>  | 125.09cm <sup>-1</sup>  | --              | 160.78cm <sup>-1</sup>  |
| 12f= | 131.97cm <sup>-1</sup>  | 76.40cm <sup>-1</sup>   | --              | 133.51cm <sup>-1</sup>  |
| TS   |                         |                         |                 |                         |
| 1f=  | 1916.02cm <sup>-1</sup> | 1958.99cm <sup>-1</sup> | --              | 1863.86cm <sup>-1</sup> |
| 2f=  | 1324.54cm <sup>-1</sup> | 1026.60cm <sup>-1</sup> | --              | 1353.61cm <sup>-1</sup> |
| 3f=  | 562.82cm <sup>-1</sup>  | 740.47cm <sup>-1</sup>  | --              | 594.96cm <sup>-1</sup>  |



|        |                         |                         |    |                         |
|--------|-------------------------|-------------------------|----|-------------------------|
| 4f=    | 522.90cm <sup>-1</sup>  | 541.63cm <sup>-1</sup>  | -- | 508.25cm <sup>-1</sup>  |
| 5f=    | 453.85cm <sup>-1</sup>  | 460.27cm <sup>-1</sup>  | -- | 424.68cm <sup>-1</sup>  |
| 6f=    | 383.94cm <sup>-1</sup>  | 433.36cm <sup>-1</sup>  | -- | 316.10cm <sup>-1</sup>  |
| 7f=    | 367.23cm <sup>-1</sup>  | 400.95cm <sup>-1</sup>  | -- | 299.61cm <sup>-1</sup>  |
| 8f=    | 360.85cm <sup>-1</sup>  | 351.23cm <sup>-1</sup>  | -- | 262.87cm <sup>-1</sup>  |
| 9f=    | 188.00cm <sup>-1</sup>  | 249.22cm <sup>-1</sup>  | -- | 202.26cm <sup>-1</sup>  |
| 10f=   | 102.89cm <sup>-1</sup>  | 105.00cm <sup>-1</sup>  | -- | 79.51cm <sup>-1</sup>   |
| 11f=   | 55.01cm <sup>-1</sup>   | 68.62cm <sup>-1</sup>   | -- | 58.68cm <sup>-1</sup>   |
| 12f/i= | 1263.16cm <sup>-1</sup> | 1092.97cm <sup>-1</sup> | -- | 1355.81cm <sup>-1</sup> |

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FS

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|      |                         |                         |    |                         |
|------|-------------------------|-------------------------|----|-------------------------|
| 1f=  | 3464.11cm <sup>-1</sup> | 3674.25cm <sup>-1</sup> | -- | 3582.12cm <sup>-1</sup> |
| 2f=  | 1708.89cm <sup>-1</sup> | 1935.76cm <sup>-1</sup> | -- | 1784.47cm <sup>-1</sup> |
| 3f=  | 801.54cm <sup>-1</sup>  | 755.55cm <sup>-1</sup>  | -- | 696.28cm <sup>-1</sup>  |
| 4f=  | 769.08cm <sup>-1</sup>  | 629.77cm <sup>-1</sup>  | -- | 659.07cm <sup>-1</sup>  |
| 5f=  | 504.95cm <sup>-1</sup>  | 468.95cm <sup>-1</sup>  | -- | 489.76cm <sup>-1</sup>  |
| 6f=  | 441.74cm <sup>-1</sup>  | 434.68cm <sup>-1</sup>  | -- | 444.86cm <sup>-1</sup>  |
| 7f=  | 334.38cm <sup>-1</sup>  | 417.92cm <sup>-1</sup>  | -- | 348.98cm <sup>-1</sup>  |
| 8f=  | 309.95cm <sup>-1</sup>  | 409.88cm <sup>-1</sup>  | -- | 322.62cm <sup>-1</sup>  |
| 9f=  | 280.57cm <sup>-1</sup>  | 295.02cm <sup>-1</sup>  | -- | 252.25cm <sup>-1</sup>  |
| 10f= | 235.11cm <sup>-1</sup>  | 241.18cm <sup>-1</sup>  | -- | 205.63cm <sup>-1</sup>  |

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|      |                        |                       |    |                        |
|------|------------------------|-----------------------|----|------------------------|
| 11f= | 120.20cm <sup>-1</sup> | 98.72cm <sup>-1</sup> | -- | 108.96cm <sup>-1</sup> |
| 12f= | 98.55cm <sup>-1</sup>  | 56.79cm <sup>-1</sup> | -- | 75.77cm <sup>-1</sup>  |

Table S19. The vibrational frequencies for CO<sub>2</sub> dissociation with H assistance (\*COOH pathway) on  $\theta$ -Fe<sub>3</sub>C (031) surface

| IS   |                         |                 |                         |                 |
|------|-------------------------|-----------------|-------------------------|-----------------|
| Site | 3F <sup>3</sup>         | 3F <sup>4</sup> | 3F <sup>5</sup>         | 4F <sup>1</sup> |
| 1f=  | 1330.14cm <sup>-1</sup> | --              | 1717.94cm <sup>-1</sup> | --              |
| 2f=  | 1321.51cm <sup>-1</sup> | --              | 1160.33cm <sup>-1</sup> | --              |
| 3f=  | 1075.61cm <sup>-1</sup> | --              | 962.77cm <sup>-1</sup>  | --              |
| 4f=  | 919.11cm <sup>-1</sup>  | --              | 786.31cm <sup>-1</sup>  | --              |
| 5f=  | 761.73cm <sup>-1</sup>  | --              | 663.32cm <sup>-1</sup>  | --              |
| 6f=  | 706.32cm <sup>-1</sup>  | --              | 582.58cm <sup>-1</sup>  | --              |
| 7f=  | 431.41cm <sup>-1</sup>  | --              | 443.01cm <sup>-1</sup>  | --              |
| 8f=  | 340.55cm <sup>-1</sup>  | --              | 288.69cm <sup>-1</sup>  | --              |
| 9f=  | 270.41cm <sup>-1</sup>  | --              | 204.57cm <sup>-1</sup>  | --              |
| 10f= | 196.89cm <sup>-1</sup>  | --              | 124.58cm <sup>-1</sup>  | --              |
| 11f= | 166.38cm <sup>-1</sup>  | --              | 102.67cm <sup>-1</sup>  | --              |
| 12f= | 78.93cm <sup>-1</sup>   | --              | 73.82cm <sup>-1</sup>   | --              |
| TS1  |                         |                 |                         |                 |
| 1f=  | 1243.12cm <sup>-1</sup> | --              | 1484.42cm <sup>-1</sup> | --              |
| 2f=  | 1215.22cm <sup>-1</sup> | --              | 1183.74cm <sup>-1</sup> | --              |
| 3f=  | 1084.41cm <sup>-1</sup> | --              | 1098.87cm <sup>-1</sup> | --              |

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|        |                         |    |                         |    |
|--------|-------------------------|----|-------------------------|----|
| 4f=    | 686.54cm <sup>-1</sup>  | -- | 712.51cm <sup>-1</sup>  | -- |
| 5f=    | 677.02cm <sup>-1</sup>  | -- | 504.00cm <sup>-1</sup>  | -- |
| 6f=    | 408.96cm <sup>-1</sup>  | -- | 432.36cm <sup>-1</sup>  | -- |
| 7f=    | 339.99cm <sup>-1</sup>  | -- | 332.49cm <sup>-1</sup>  | -- |
| 8f=    | 238.15cm <sup>-1</sup>  | -- | 251.09cm <sup>-1</sup>  | -- |
| 9f=    | 175.01cm <sup>-1</sup>  | -- | 153.16cm <sup>-1</sup>  | -- |
| 10f=   | 171.23cm <sup>-1</sup>  | -- | 102.85cm <sup>-1</sup>  | -- |
| 11f=   | 68.98cm <sup>-1</sup>   | -- | 59.81cm <sup>-1</sup>   | -- |
| 12f/i= | 1401.78cm <sup>-1</sup> | -- | 1315.68cm <sup>-1</sup> | -- |

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FS1

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|      |                         |    |                         |    |
|------|-------------------------|----|-------------------------|----|
| 1f=  | 3529.63cm <sup>-1</sup> | -- | 3579.35cm <sup>-1</sup> | -- |
| 2f=  | 1288.01cm <sup>-1</sup> | -- | 1295.40cm <sup>-1</sup> | -- |
| 3f=  | 1219.35cm <sup>-1</sup> | -- | 1203.33cm <sup>-1</sup> | -- |
| 4f=  | 1038.82cm <sup>-1</sup> | -- | 1060.75cm <sup>-1</sup> | -- |
| 5f=  | 656.52cm <sup>-1</sup>  | -- | 682.85cm <sup>-1</sup>  | -- |
| 6f=  | 615.44cm <sup>-1</sup>  | -- | 671.03cm <sup>-1</sup>  | -- |
| 7f=  | 446.13cm <sup>-1</sup>  | -- | 478.70cm <sup>-1</sup>  | -- |
| 8f=  | 357.02cm <sup>-1</sup>  | -- | 353.43cm <sup>-1</sup>  | -- |
| 9f=  | 254.55cm <sup>-1</sup>  | -- | 270.29cm <sup>-1</sup>  | -- |
| 10f= | 169.41cm <sup>-1</sup>  | -- | 183.88cm <sup>-1</sup>  | -- |

|        |                         |    |                         |    |
|--------|-------------------------|----|-------------------------|----|
| 11f=   | 151.17cm <sup>-1</sup>  | -- | 140.61cm <sup>-1</sup>  | -- |
| 12f=   | 86.60cm <sup>-1</sup>   | -- | 81.47cm <sup>-1</sup>   | -- |
| TS2    |                         |    |                         |    |
| 1f=    | 3531.94cm <sup>-1</sup> | -- | 3687.68cm <sup>-1</sup> | -- |
| 2f=    | 1564.85cm <sup>-1</sup> | -- | 1178.07cm <sup>-1</sup> | -- |
| 3f=    | 1130.39cm <sup>-1</sup> | -- | 1123.78cm <sup>-1</sup> | -- |
| 4f=    | 888.19cm <sup>-1</sup>  | -- | 972.93cm <sup>-1</sup>  | -- |
| 5f=    | 613.72cm <sup>-1</sup>  | -- | 666.33cm <sup>-1</sup>  | -- |
| 6f=    | 554.53cm <sup>-1</sup>  | -- | 442.99cm <sup>-1</sup>  | -- |
| 7f=    | 443.27cm <sup>-1</sup>  | -- | 359.73cm <sup>-1</sup>  | -- |
| 8f=    | 297.88cm <sup>-1</sup>  | -- | 221.01cm <sup>-1</sup>  | -- |
| 9f=    | 237.78cm <sup>-1</sup>  | -- | 197.99cm <sup>-1</sup>  | -- |
| 10f=   | 94.40cm <sup>-1</sup>   | -- | 127.04cm <sup>-1</sup>  | -- |
| 11f=   | 54.34cm <sup>-1</sup>   | -- | 66.13cm <sup>-1</sup>   | -- |
| 12f/i= | 100.25cm <sup>-1</sup>  | -- | 591.83cm <sup>-1</sup>  | -- |
| FS2    |                         |    |                         |    |
| 1f=    | 3641.25cm <sup>-1</sup> | -- | 3682.46cm <sup>-1</sup> | -- |
| 2f=    | 1719.00cm <sup>-1</sup> | -- | 1890.51cm <sup>-1</sup> | -- |
| 3f=    | 756.56cm <sup>-1</sup>  | -- | 676.58cm <sup>-1</sup>  | -- |
| 4f=    | 651.22cm <sup>-1</sup>  | -- | 560.21cm <sup>-1</sup>  | -- |

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|      |                        |    |                        |    |
|------|------------------------|----|------------------------|----|
| 5f=  | 405.39cm <sup>-1</sup> | -- | 446.98cm <sup>-1</sup> | -- |
| 6f=  | 392.94cm <sup>-1</sup> | -- | 425.27cm <sup>-1</sup> | -- |
| 7f=  | 291.09cm <sup>-1</sup> | -- | 412.72cm <sup>-1</sup> | -- |
| 8f=  | 252.04cm <sup>-1</sup> | -- | 383.58cm <sup>-1</sup> | -- |
| 9f=  | 208.63cm <sup>-1</sup> | -- | 244.21cm <sup>-1</sup> | -- |
| 10f= | 159.12cm <sup>-1</sup> | -- | 164.83cm <sup>-1</sup> | -- |
| 11f= | 148.45cm <sup>-1</sup> | -- | 67.02cm <sup>-1</sup>  | -- |
| 12f= | 47.45cm <sup>-1</sup>  | -- | 50.88cm <sup>-1</sup>  | -- |

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Table S20. The vibrational frequencies for CO<sub>2</sub> dissociation with H assistance (\*HCOO pathway) on  $\theta$ -Fe<sub>3</sub>C (031) surface

| IS   |                         |                         |                         |                         |
|------|-------------------------|-------------------------|-------------------------|-------------------------|
| Site | 3F <sup>3</sup>         | 3F <sup>4</sup>         | 3F <sup>5</sup>         | 4F <sup>1</sup>         |
| 1f=  | 1523.09cm <sup>-1</sup> | 1627.67cm <sup>-1</sup> | 1699.40cm <sup>-1</sup> | 1312.70cm <sup>-1</sup> |
| 2f=  | 1356.58cm <sup>-1</sup> | 1166.11cm <sup>-1</sup> | 1170.45cm <sup>-1</sup> | 1258.23cm <sup>-1</sup> |
| 3f=  | 1072.61cm <sup>-1</sup> | 1096.68cm <sup>-1</sup> | 1163.5cm <sup>-1</sup>  | 1066.51cm <sup>-1</sup> |
| 4f=  | 950.52cm <sup>-1</sup>  | 1089.95cm <sup>-1</sup> | 1056.56cm <sup>-1</sup> | 972.02cm <sup>-1</sup>  |
| 5f=  | 694.49cm <sup>-1</sup>  | 769.13cm <sup>-1</sup>  | 789.41cm <sup>-1</sup>  | 789.26cm <sup>-1</sup>  |
| 6f=  | 575.39cm <sup>-1</sup>  | 687.20cm <sup>-1</sup>  | 675.40cm <sup>-1</sup>  | 688.48cm <sup>-1</sup>  |
| 7f=  | 468.92cm <sup>-1</sup>  | 394.65cm <sup>-1</sup>  | 433.82cm <sup>-1</sup>  | 437.69cm <sup>-1</sup>  |
| 8f=  | 316.21cm <sup>-1</sup>  | 331.41cm <sup>-1</sup>  | 302.40cm <sup>-1</sup>  | 344.56cm <sup>-1</sup>  |
| 9f=  | 274.03cm <sup>-1</sup>  | 171.84cm <sup>-1</sup>  | 209.89cm <sup>-1</sup>  | 253.09cm <sup>-1</sup>  |
| 10f= | 204.89cm <sup>-1</sup>  | 144.89cm <sup>-1</sup>  | 121.90cm <sup>-1</sup>  | 205.56cm <sup>-1</sup>  |
| 11f= | 188.68cm <sup>-1</sup>  | 101.70cm <sup>-1</sup>  | 92.11cm <sup>-1</sup>   | 160.78cm <sup>-1</sup>  |
| 12f= | 131.97cm <sup>-1</sup>  | 71.00cm <sup>-1</sup>   | 77.00cm <sup>-1</sup>   | 133.51cm <sup>-1</sup>  |
| TS1  |                         |                         |                         |                         |
| 1f=  | 1788.19cm <sup>-1</sup> | 1766.54cm <sup>-1</sup> | 1780.38cm <sup>-1</sup> | 1847.98cm <sup>-1</sup> |
| 2f=  | 1289.36cm <sup>-1</sup> | 1394.21cm <sup>-1</sup> | 1395.91cm <sup>-1</sup> | 1278.50cm <sup>-1</sup> |
| 3f=  | 1015.31cm <sup>-1</sup> | 1098.15cm <sup>-1</sup> | 1100.22cm <sup>-1</sup> | 1130.98cm <sup>-1</sup> |

|        |                        |                        |                        |                         |
|--------|------------------------|------------------------|------------------------|-------------------------|
| 4f=    | 794.38cm <sup>-1</sup> | 724.20cm <sup>-1</sup> | 726.36cm <sup>-1</sup> | 1057.76cm <sup>-1</sup> |
| 5f=    | 685.26cm <sup>-1</sup> | 662.13cm <sup>-1</sup> | 664.28cm <sup>-1</sup> | 982.74cm <sup>-1</sup>  |
| 6f=    | 557.03cm <sup>-1</sup> | 512.40cm <sup>-1</sup> | 513.49cm <sup>-1</sup> | 638.37cm <sup>-1</sup>  |
| 7f=    | 322.40cm <sup>-1</sup> | 332.96cm <sup>-1</sup> | 336.55cm <sup>-1</sup> | 355.34cm <sup>-1</sup>  |
| 8f=    | 300.27cm <sup>-1</sup> | 280.37cm <sup>-1</sup> | 277.72cm <sup>-1</sup> | 282.26cm <sup>-1</sup>  |
| 9f=    | 236.33cm <sup>-1</sup> | 181.66cm <sup>-1</sup> | 185.62cm <sup>-1</sup> | 241.50cm <sup>-1</sup>  |
| 10f=   | 205.04cm <sup>-1</sup> | 157.35cm <sup>-1</sup> | 160.52cm <sup>-1</sup> | 169.49cm <sup>-1</sup>  |
| 11f=   | 146.64cm <sup>-1</sup> | 125.77cm <sup>-1</sup> | 127.36cm <sup>-1</sup> | 124.39cm <sup>-1</sup>  |
| 12f/i= | 467.16cm <sup>-1</sup> | 727.46cm <sup>-1</sup> | 718.27cm <sup>-1</sup> | 304.67cm <sup>-1</sup>  |

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FS1

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|      |                         |                         |                         |                         |
|------|-------------------------|-------------------------|-------------------------|-------------------------|
| 1f=  | 1840.86cm <sup>-1</sup> | 3009.53cm <sup>-1</sup> | 2873.33cm <sup>-1</sup> | 3043.66cm <sup>-1</sup> |
| 2f=  | 1280.84cm <sup>-1</sup> | 1306.77cm <sup>-1</sup> | 1314.82cm <sup>-1</sup> | 1296.56cm <sup>-1</sup> |
| 3f=  | 1234.69cm <sup>-1</sup> | 1238.07cm <sup>-1</sup> | 1248.35cm <sup>-1</sup> | 1179.45cm <sup>-1</sup> |
| 4f=  | 984.27cm <sup>-1</sup>  | 1115.12cm <sup>-1</sup> | 1147.78cm <sup>-1</sup> | 1090.17cm <sup>-1</sup> |
| 5f=  | 954.53cm <sup>-1</sup>  | 832.04cm <sup>-1</sup>  | 835.65cm <sup>-1</sup>  | 806.47cm <sup>-1</sup>  |
| 6f=  | 610.30cm <sup>-1</sup>  | 635.18cm <sup>-1</sup>  | 622.52cm <sup>-1</sup>  | 627.99cm <sup>-1</sup>  |
| 7f=  | 342.87cm <sup>-1</sup>  | 449.66cm <sup>-1</sup>  | 446.65cm <sup>-1</sup>  | 465.41cm <sup>-1</sup>  |
| 8f=  | 321.64cm <sup>-1</sup>  | 365.20cm <sup>-1</sup>  | 386.27cm <sup>-1</sup>  | 367.26cm <sup>-1</sup>  |
| 9f=  | 305.96cm <sup>-1</sup>  | 253.11cm <sup>-1</sup>  | 213.62cm <sup>-1</sup>  | 305.55cm <sup>-1</sup>  |
| 10f= | 231.03cm <sup>-1</sup>  | 191.60cm <sup>-1</sup>  | 117.76cm <sup>-1</sup>  | 276.64cm <sup>-1</sup>  |



|        |                         |                         |                         |                         |
|--------|-------------------------|-------------------------|-------------------------|-------------------------|
| 11f=   | 162.94cm <sup>-1</sup>  | 114.16cm <sup>-1</sup>  | 105.07cm <sup>-1</sup>  | 217.61cm <sup>-1</sup>  |
| 12f=   | 145.06cm <sup>-1</sup>  | 101.89cm <sup>-1</sup>  | 76.16cm <sup>-1</sup>   | 124.56cm <sup>-1</sup>  |
| TS2    |                         |                         |                         |                         |
| 1f=    | 2983.00cm <sup>-1</sup> | 3009.97cm <sup>-1</sup> | 3014.75cm <sup>-1</sup> | 2976.54cm <sup>-1</sup> |
| 2f=    | 1406.93cm <sup>-1</sup> | 1202.86cm <sup>-1</sup> | 1236.30cm <sup>-1</sup> | 1290.53cm <sup>-1</sup> |
| 3f=    | 1169.10cm <sup>-1</sup> | 1164.71cm <sup>-1</sup> | 1193.62cm <sup>-1</sup> | 1170.07cm <sup>-1</sup> |
| 4f=    | 915.98cm <sup>-1</sup>  | 872.18cm <sup>-1</sup>  | 880.73cm <sup>-1</sup>  | 745.58cm <sup>-1</sup>  |
| 5f=    | 508.08cm <sup>-1</sup>  | 535.68cm <sup>-1</sup>  | 555.61cm <sup>-1</sup>  | 497.85cm <sup>-1</sup>  |
| 6f=    | 464.74cm <sup>-1</sup>  | 520.13cm <sup>-1</sup>  | 506.52cm <sup>-1</sup>  | 449.71cm <sup>-1</sup>  |
| 7f=    | 420.38cm <sup>-1</sup>  | 377.46cm <sup>-1</sup>  | 362.04cm <sup>-1</sup>  | 382.62cm <sup>-1</sup>  |
| 8f=    | 299.27cm <sup>-1</sup>  | 296.57cm <sup>-1</sup>  | 312.45cm <sup>-1</sup>  | 312.51cm <sup>-1</sup>  |
| 9f=    | 296.77cm <sup>-1</sup>  | 209.23cm <sup>-1</sup>  | 264.07cm <sup>-1</sup>  | 279.45cm <sup>-1</sup>  |
| 10f=   | 213.78cm <sup>-1</sup>  | 176.60cm <sup>-1</sup>  | 173.23cm <sup>-1</sup>  | 200.92cm <sup>-1</sup>  |
| 11f=   | 142.79cm <sup>-1</sup>  | 95.72cm <sup>-1</sup>   | 99.21cm <sup>-1</sup>   | 171.52cm <sup>-1</sup>  |
| 12f/i= | 326.91cm <sup>-1</sup>  | 386.35cm <sup>-1</sup>  | 411.81cm <sup>-1</sup>  | 234.31cm <sup>-1</sup>  |
| FS2    |                         |                         |                         |                         |
| 1f=    | 2861.08cm <sup>-1</sup> | 2954.60cm <sup>-1</sup> | 2863.82cm <sup>-1</sup> | 2931.93cm <sup>-1</sup> |
| 2f=    | 1460.47cm <sup>-1</sup> | 1183.69cm <sup>-1</sup> | 1306.30cm <sup>-1</sup> | 1191.72cm <sup>-1</sup> |
| 3f=    | 1163.18cm <sup>-1</sup> | 1118.65cm <sup>-1</sup> | 1181.01cm <sup>-1</sup> | 1063.72cm <sup>-1</sup> |
| 4f=    | 742.81cm <sup>-1</sup>  | 735.35cm <sup>-1</sup>  | 735.18cm <sup>-1</sup>  | 725.83cm <sup>-1</sup>  |

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|      |                        |                        |                        |                        |
|------|------------------------|------------------------|------------------------|------------------------|
| 5f=  | 579.12cm <sup>-1</sup> | 572.43cm <sup>-1</sup> | 507.77cm <sup>-1</sup> | 520.92cm <sup>-1</sup> |
| 6f=  | 389.88cm <sup>-1</sup> | 570.00cm <sup>-1</sup> | 490.42cm <sup>-1</sup> | 481.77cm <sup>-1</sup> |
| 7f=  | 329.44cm <sup>-1</sup> | 383.85cm <sup>-1</sup> | 373.14cm <sup>-1</sup> | 466.84cm <sup>-1</sup> |
| 8f=  | 273.55cm <sup>-1</sup> | 370.10cm <sup>-1</sup> | 340.49cm <sup>-1</sup> | 409.82cm <sup>-1</sup> |
| 9f=  | 243.84cm <sup>-1</sup> | 277.60cm <sup>-1</sup> | 245.76cm <sup>-1</sup> | 366.54cm <sup>-1</sup> |
| 10f= | 195.76cm <sup>-1</sup> | 221.32cm <sup>-1</sup> | 166.83cm <sup>-1</sup> | 335.55cm <sup>-1</sup> |
| 11f= | 155.51cm <sup>-1</sup> | 162.95cm <sup>-1</sup> | 141.65cm <sup>-1</sup> | 288.83cm <sup>-1</sup> |
| 12f= | 43.61cm <sup>-1</sup>  | 137.75cm <sup>-1</sup> | 75.43cm <sup>-1</sup>  | 231.89cm <sup>-1</sup> |

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Table S21. Catalytic performance of iron-based catalysts

| Catalysts                        | Rate (CO <sub>2</sub> ) [moleculeCO <sub>2</sub> /nm <sup>2</sup> Fe/h] |
|----------------------------------|---|
| Fe <sub>3</sub> O <sub>4</sub>   | 4.29  |
| χ-Fe <sub>5</sub> C <sub>2</sub> | 48.23   |
| θ-Fe <sub>3</sub> C              | 22.50   |

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