

# A Modular Monadic Framework for Abstract Interpretation

## (Draft)

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### Abstract

The design and implementation of static analyses is a difficult process. Verifying the correctness of an implementation is often the most painful step. We present Monadic AAM—an extension of the Abstracting Abstract Machines methodology introduced by Van Horn and Might [?]-which captures a large class of both automatically derivable and correct by construction abstract interpreters. Monadic AAM is part methodology and part toolkit. In the methodology, semantics are designed in a monadic extension of traditional AAM. Once designed, a large class of known analyses can be automatically recovered using our language agnostic toolkit. Both the computational and correctness properties of our framework are realized through a restricted class of monad transformers. Our framework enjoys the benefits of being highly compositional and placing a minimal burden of proof on the analysis designer.

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