

$$[con] \quad (\widehat{C}, \widehat{\rho}) \models c^\ell \text{ always}$$

$$[var] \quad (\widehat{C}, \widehat{\rho}) \models x^\ell \text{ iff } \widehat{\rho}(x) \subseteq \widehat{C}(\ell)$$

$$[fn] \quad (\widehat{C}, \widehat{\rho}) \models (fn \ x \Rightarrow e_0)^\ell \text{ iff } \{fn \ x \Rightarrow e_0\} \subseteq \widehat{C}(\ell)$$

$$[fun] \quad (\widehat{C}, \widehat{\rho}) \models (fun \ f \ x \Rightarrow e_0)^\ell \text{ iff } \{fun \ f \ x \Rightarrow e_0\} \subseteq \widehat{C}(\ell)$$

$$\begin{aligned}
 [app] \quad (\widehat{C}, \widehat{\rho}) \models (t_1^{\ell_1} \ t_2^{\ell_2})^\ell \\
 \text{iff } & (\widehat{C}, \widehat{\rho}) \models t_1^{\ell_1} \wedge (\widehat{C}, \widehat{\rho}) \models t_2^{\ell_2} \wedge \\
 & (\forall (fn \ x \Rightarrow t_0^{\ell_0}) \in \widehat{C}(\ell_1) : \\
 & \quad (\widehat{C}, \widehat{\rho}) \models t_0^{\ell_0} \wedge \\
 & \quad \widehat{C}(\ell_2) \subseteq \widehat{\rho}(x) \wedge \widehat{C}(\ell_0) \subseteq \widehat{C}(\ell)) \wedge \\
 & (\forall (fun \ f \ x \Rightarrow t_0^{\ell_0}) \in \widehat{C}(\ell_1) : \\
 & \quad (\widehat{C}, \widehat{\rho}) \models t_0^{\ell_0} \wedge \\
 & \quad \widehat{C}(\ell_2) \subseteq \widehat{\rho}(x) \wedge \widehat{C}(\ell_0) \subseteq \widehat{C}(\ell) \wedge \\
 & \quad \{fun \ f \ x \Rightarrow t_0^{\ell_0}\} \subseteq \widehat{\rho}(f))
 \end{aligned}$$

$$\begin{aligned}
 [if] \quad (\widehat{C}, \widehat{\rho}) \models (if \ t_0^{\ell_0} \text{ then } t_1^{\ell_1} \text{ else } t_2^{\ell_2})^\ell \\
 \text{iff } & (\widehat{C}, \widehat{\rho}) \models t_0^{\ell_0} \wedge \\
 & (\widehat{C}, \widehat{\rho}) \models t_1^{\ell_1} \wedge (\widehat{C}, \widehat{\rho}) \models t_2^{\ell_2} \wedge \\
 & \widehat{C}(\ell_1) \subseteq \widehat{C}(\ell) \wedge \widehat{C}(\ell_2) \subseteq \widehat{C}(\ell)
 \end{aligned}$$

$$\begin{aligned}
 [let] \quad (\widehat{C}, \widehat{\rho}) \models (let \ x = t_1^{\ell_1} \text{ in } t_2^{\ell_2})^\ell \\
 \text{iff } & (\widehat{C}, \widehat{\rho}) \models t_1^{\ell_1} \wedge (\widehat{C}, \widehat{\rho}) \models t_2^{\ell_2} \wedge \\
 & \widehat{C}(\ell_1) \subseteq \widehat{\rho}(x) \wedge \widehat{C}(\ell_2) \subseteq \widehat{C}(\ell)
 \end{aligned}$$

$$[op] \quad (\widehat{C}, \widehat{\rho}) \models (t_1^{\ell_1} \ op \ t_2^{\ell_2})^\ell \text{ iff } (\widehat{C}, \widehat{\rho}) \models t_1^{\ell_1} \wedge (\widehat{C}, \widehat{\rho}) \models t_2^{\ell_2}$$