# Exploring type-directed, test-driven development

A case study using FizzBuzz

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June 7, 2014 Pittsburgh TechFest 2014

#### Abstract

An expressive static type system is one of the most joyful and powerful tools for prototyping, designing, and maintaining programs. In this performance-theatrical presentation, I will provide a taste of how to use types, in conjunction with tests, to drive iterative development of a particular program, the famous FizzBuzz problem. We will solve generalizations of this problem, changing and adding requirements, to illustrate the pleasures and benefits of "type thinking".

The Scala language will be used as the vehicle for this demonstration, but the techniques apply immediately to any industrial-strength statically typed language, such as Haskell, OCaml, F#, Rust, and most recently, Swift.

(Note: this presentation will use live human volunteers to play the roles of various programming concepts.)

# Outline

#### Outline

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1	1 ,	Goals
1.	т ,	Godis
$\mathbf{G}$	oals	of this presentation
	• G	ive a taste of a <i>practical</i> software development <i>process</i> that is:
		- test-driven
		- type-directed
	• Sl	how everything for real (using Scala):
		- project build process
		- testing frameworks
		- all the code
	<b>T</b> T	
	• U	se FizzBuzz because:
		– problem: easy to understand
		– modifications: easy to understand
		- fun!
	17	ncourage you to explore a modern typed language

- This Monday, Apple ditched Objective C for its new language Swift!



- Complete Swift code will shown at the end; looks a lot like Scala.

# 1.2 Test-driven development (TDD)

# Test-driven development (TDD)

- Think.
- Write a test that fails.
- Write code until test succeeds.
- Repeat, and refactor as needed.

#### Is TDD dead?

Short answer: No.

# 1.3 Type systems

# Type systems

#### What is a type system?

A syntactic method to prove that bad things can't happen.

# "Debating" types "versus" tests?

- Let's use both types and tests!
- But: use a *good* type system, not a bad one.

# Some decent practical typed languages

- OCaml: 20 years old
- Haskell: 20 years old
- Scala: 10 years old
- Swift: 5 days old
- Rust (still in progress)

# Poor versus decent type systems

# Poor type systems

- (Developed using 1960s-1970s knowledge)
- C, C++, Objective C
- Java

# Decent type systems

- (Developed using 1980s-1990s knowledge)
- ML (Standard ML, OCaml, F#): I first used for work in 1995
- Haskell: I first used for work in 1995
- Scala: first released in 2004
- Swift: announced by Apple on June 2, 2014!
- Rust: not yet version 1.0

# 2 Original FizzBuzz problem

# 2.1 Original FizzBuzz problem

#### Original FizzBuzz problem

#### FizzBuzz defined

Write a program that prints the numbers from 1 to 100.

But for multiples of three, print "Fizz" instead of the number.

And for the multiples of five, print "Buzz".

For numbers which are multiples of both three and five, print "FizzBuzz".

# 2.2 Starter code: main driver

# Starter code: main driver



Scala: a modern object-oriented and functional language.

```
object Main extends App {
   // Will not compile yet!
   runToSeq(1, 100).foreach(println)
}
```

- Type-directed design: separate out effects (such as printing to terminal) from the real work.
- Type-directed feedback: compilation fails when something is not implemented yet.

# 2.3 The joys of continuous compilation and testing

The joys of continuous compilation and testing

# sbt

SBT: build tool supporting Scala, Java...

# Winning features

- Source file changes trigger smart recompilation!
- Source file changes trigger rerun of the tests that depend on changed code!

```
$ sbt
> ~testQuick
[info] Compiling 1 Scala source to ...
[error] ...Main.scala:16: not found: value runToSeq
[error] runToSeq(1, 100) foreach println
[error] ^
[error] one error found
```

#### Write type-directed stub

```
object Main extends App {
  runToSeq(1, 100).foreach(println)

def runToSeq(start: Int, end: Int): Seq[String] = {
    ???
  }
}
```

# Write wanted type signature

??? is convenient for stubbing.

- In Scala standard library
- Just performs: throw new NotImplementedError

# 2.4 Write acceptance test (simplified)

Write acceptance test (simplified)



Specs2: a fine testing framework for Scala, Java...

```
class MainSpec extends Specification { def is = s2"""
    ${Main.runToSeq(1, 16) ==== 'strings for 1 to 16'}
    """

val 'strings for 1 to 16' = Seq(
    "1", "2", "Fizz", "4", "Buzz", "Fizz",
    "7", "8", "Fizz", "Buzz", "11", "Fizz",
    "13", "14", "FizzBuzz", "16"
    )
}
```

A realistic acceptance test would involve handling I/O, but an elegant technique for modularizing that, scalaz-stream, is outside the scope of this presentation.

#### TDD in Swift

```
class MainSpec: XCTestCase {
  func test1to16() {
    let expected: [String] = [
        "1", "2", "Fizz", "4", "Buzz", "Fizz",
        "7", "8", "Fizz", "Buzz", "11", "Fizz",
        "13", "14", "FizzBuzz", "16"
    ]

    XCTAssert(Main.runToSeq(1, 16) == expected)
  }
}
```

# Test passes type check, but fails

Incremental compilation/testing kicks in:

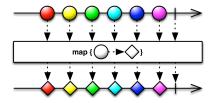
```
Waiting for source changes... (press enter to interrupt)
[info] MainSpec
[info] x Main.runToSeq(1, 16) ==== 'strings for 1 to 16
[error] an implementation is missing (Main.scala:19)
```

#### Outside-in: for a FizzBuzz unit

Types are shapes to assemble logically.

```
def runToSeq(start: Int, end: Int): Seq[String] = {
   start.to(end).map(FizzBuzz.evaluate)
}
```

- start.to(end): Seq[Int], where Seq[\_] is a type constructor that, given a type A, returns a type of Seq[A].
- For any value of type Seq[A], map:  $(A \Rightarrow B) \Rightarrow Seq[B]$ .



• Therefore: need to implement function FizzBuzz.evaluate: Int => String.

#### Swift version of driver

```
func runToSeq(i: Int, j: Int) -> [String] {
  return Array(i...j).map(Defaults.fizzBuzzer)
}
```

# 2.5 Test-driven units

# Implement new FizzBuzz module

A failing acceptance test drives discovery of

- A unit, FizzBuzz
- A function with a particular type, Int => String

```
object FizzBuzz {
  type Evaluator = Int => String

val evaluate: Evaluator = { i =>
    ???
  }
}
```

# Types are better than comments as documentation!

Comments are not checkable, unlike types and tests.

# First part of unit test: example-based

Manually write some examples.

```
class FizzBuzzSpec extends Specification { def is = s2"""
    ${FizzBuzz.evaluate(15) ==== "FizzBuzz"}
    ${FizzBuzz.evaluate(20) ==== "Buzz"}
    ${FizzBuzz.evaluate(6) ==== "Fizz"}
    ${FizzBuzz.evaluate(17) ==== "17"}
    """
}
```

# 2.6 Property-based tests

The joy of property-based tests



ScalaCheck: a framework for writing property-based tests.

```
class FizzBuzzSpec extends Specification
  with ScalaCheck { def is = s2"""
  ${'Multiple of both 3 and 5 => "FizzBuzz"'} """
  def 'Multiple of both 3 and 5 => "FizzBuzz"' =
    prop { i: Int => (i % 3 == 0 && i % 5 == 0) ==>
        { FizzBuzz.evaluate(i) ==== "FizzBuzz" }
    }
}
```

#### Winning features

- Auto-generates random tests for each property (100 by default).
- Type-driven: here, generates random Int values.

# Property-based testing for Swift?

I hope someone writes a property-based testing framework for Swift!

# Property-based tests (continued)

The other three properties of interest:

```
def 'Multiple of only 5 => "Buzz"' =
  prop { i: Int => (i % 3 != 0 && i % 5 == 0) ==>
      { FizzBuzz.evaluate(i) ==== "Buzz" }
}

def 'Not a multiple of either 3 or 5 => number' =
  prop { i: Int => (i % 3 != 0 && i % 5 != 0) ==>
      { FizzBuzz.evaluate(i) ==== i.toString }
}
```

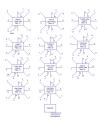
# 2.7 Solving the FizzBuzz problem

# A buggy and ugly solution

```
// Buggy and ugly!
val evaluate: Evaluator = { i =>
   if (i % 3 == 0)
     "Fizz"
   else if (i % 5 == 0)
     "Buzz"
   else if (i % 3 == 0 && i % 5 == 0)
     "FizzBuzz"
   else
     i.toString
}
```

#### Booleans are evil!

Maze of twisty little conditionals, all different



- Too easy to write incorrect sequences of nested, combined conditionals.
- Overuse of Booleans is a type smell.

#### Why booleans are evil

# No help from type system

- Conditions can be arbitrary: depend on any combination of data.
- Multiple conditions: combinatorial explosion (two conditions led to four cases).
- Possibly overlapping conditions: order dependency subtleties.
- Possibly duplicated checking of the some condition.

#### Pattern matching organizes information

```
val evaluate: Evaluator = { i =>
  (i % 3 == 0, i % 5 == 0) match {
    case (true, false) => "Fizz"
    case (false, true) => "Buzz"
    case (true, true) => "FizzBuzz"
    case (false, false) => i.toString
  }
}
```

#### Winning features

- Visual beauty and clarity.
- No duplicated conditionals.
- No ordering dependency.
- Type checker verifies full coverage of cases.

#### Example of non-exhaustive pattern matching

```
val evaluate: Evaluator = { i =>
  (i % 3 == 0, i % 5 == 0) match {
   case (true, false) => "Fizz"
   case (false, true) => "Buzz"
   case (true, true) => "FizzBuzz"
   // case (false, false) => ???
}
```

# Swift digression: pattern matching

The same solution, in Swift:

```
typealias Evaluator = Int -> String

let evaluate: Evaluator = { i in
   switch (i % 3 == 0, i % 5 == 0) {
   case (true, false): return "Fizz"
   case (false, true): return "Buzz"
   case (true, true): return "FizzBuzz"
   case (false, false): return String(i)
   }
}
```

# Acceptance test passes

```
[info] MainSpec
[info] + Main.runToSeq(1, 16) ==== 'strings for 1 to 16
```

#### Done?

No. Client wants more features.

# 3 FizzBuzz 2: user configuration

# 3.1 Adding new features

Adding new features

Client wants to:

- $\bullet$  Choose two arbitrary divisors in place of 3 and 5
  - such as 4 and 7
- Choose other arbitrary words in place of "Fizz" and "Buzz"
  - such as "Moo" and "Quack"

# 3.2 Type-driven refactoring

Type-driven refactoring

Types mean: refactoring is much more fun!

- Add new tests.
- Change types and code: to make new tests type check.

- Refactor original code and tests: use new APIs.
- Keep passing the *old* tests.
- Delay writing code for new features.

#### More features means more types

Change FizzBuzz.evaluate to Defaults.fizzBuzzer:

```
def runToSeq(start: Int, end: Int): Seq[String] = {
   start.to(end).map(Defaults.fizzBuzzer)
}
```

Add new types to FizzBuzz module:

# Extract original default configuration

```
object Defaults {
  val fizzBuzzerConfig: Config =
    Config(3 -> "Fizz", 5 -> "Buzz")

val fizzBuzzer: Evaluator =
    FizzBuzz.compile(fizzBuzzerConfig)

// Useful to keep old implementation
val oldFizzBuzzer: Evaluator = { i =>
    (i % 3 == 0, i % 5 == 0) match {
    case (true, false) => "Fizz"
    case (false, true) => "Buzz"
    case (true, true) => "FizzBuzz"
    case (false, false) => i.toString
    }
}
```

#### More types means more tests

Write new property-based test over arbitrary user configurations:

```
val arbitraryConfig: Arbitrary[Config] = Arbitrary {
   for {
      (d1, d2, w1, w2) <-
        arbitrary[(Int, Int, String, String)]
   } yield Config(d1 -> w1, d2 -> w2)
}

def 'Arbitrary pair of divisors: divisible by first' =
   arbitraryConfig { config: Config =>
      val evaluate = FizzBuzz.compile(config)
   val Config((d1, w1), (d2, _)) = config
   prop { i: Int => (i % d1 == 0 && i % d2 != 0) ==>
      { evaluate(i) ==== w1 }
   }
}
```

# 3.3 Refining types

Problem: coarse Config type

```
[info] ! Arbitrary divisor/word pair fizzBuzzers
[error] ArithmeticException: :
    A counter-example is 'Config((0,),(0,))':
    java.lang.ArithmeticException: / by zero
    (after 0 try) (FizzBuzzSpec.scala:58)
```

- 0 as a divisor *crashes*!
- We discovered client's underspecification.
- Client says: meant to allow only divisors within 2 and 100.

We need to:

- Add runtime *validation* when *constructing* Config.
- Refine Config random generator.

#### 3.4 Validation

#### Add (runtime) validation

Runtime precondition contract: Scala's require (throws exception on failure):

#### A note on exceptions and types

- Exceptions are evil because they escape the type system.
- In real life, I prefer to use a principled type-based validation system, such as Scalaz.
- Note: Swift does not have exceptions, so expect some type-based libraries to emerge!

#### Data validation can be critical!

#### Digression: two ways to prevent Heartbleed

- Instead of C: use a dependently typed safe systems language such as ATS for compile-time TDD.
- Even with C: use good validation and testing practices.
  - A weaker type system is not an excuse to skip write tedious validation code or tests!

#### Improve Config random generator

```
val arbitraryConfig: Arbitrary[Config] =
   Arbitrary {
    for {
        d1 <- choose(DIVISOR_MIN, DIVISOR_MAX)
        d2 <- choose(DIVISOR_MIN, DIVISOR_MAX)
        w1 <- arbitrary[String]
        w2 <- arbitrary[String]</pre>
```

```
} yield Config(d1 -> w1, d2 -> w2)
}
```

#### New test runs further, stills fails

Refactor old code to FizzBuzz.compile, to pass old tests and new test.

# 4 FizzBuzz 3: FizzBuzzPop and beyond

# 4.1 Generalize to more than two divisors

Generalizing to more than two divisors

Client wants FizzBuzzPop!

- Given three divisors (such as 3, 5, 7).
- Given three words (such as "Fizz", "Buzz", "Pop").
- Compile to evaluator that given an integer prints:
  - either a string combining a subset of the three words, or
  - a numerical string if the integer is not a multiple of any of the three divisors
- Example: 21 should output "FizzPop".

#### Thought-driven development

Software development is not primarily about coding, but thinking.

- Deep fact: solving a more general problem is often easier than solving the specific problem.
- There are four important numbers in the Universe:
  - 0 emptiness
  - 1 existence
  - 2 other (relationship)

many community

# 4.2 More features means more tests and types (again)

#### More features means more tests

Write new tests for new Defaults.fizzBuzzPopper:

```
def is = s2"""
${Defaults.fizzBuzzPopper(2) ==== "2"}
${Defaults.fizzBuzzPopper(21) ==== "FizzPop"}
${Defaults.fizzBuzzPopper(9) ==== "Fizz"}
${Defaults.fizzBuzzPopper(7) ==== "Pop"}
${Defaults.fizzBuzzPopper(35) ==== "BuzzPop"}
"""
```

Change configuration: to Seq of pairs, instead of just two:

```
val fizzBuzzPopperConfig: Config =
   Config(Seq(
      3 -> "Fizz", 5 -> "Buzz", 7 -> "Pop"
   ))
val fizzBuzzPopper: Evaluator =
   FizzBuzz.compile(fizzBuzzPopperConfig)
```

#### More tests means more (or changed) types

```
[error] ...Defaults.scala:29: not enough arguments for
  method apply:
    (pair1: (Int, String), pair2: (Int, String))
    com.franklinchen.FizzBuzz.Config in object Config
[error] Unspecified value parameter pair2.
[error] Config(Seq(
[error] ^
```

Change type Config to allow a sequence of pairs:

```
case class Config(pairs: Seq[(Int, String)]) {
   pairs.foreach(validatePair)
}
```

Note how our iterative development process promotes *reuse* (here, of validation logic).

# Fix remaining type errors

Refactoring reveals need to implement case of more than two divisors.

```
val compile: Compiler = {
  case Config(Seq((d1, w1), (d2, w2))) =>
    val w = w1 + w2

    { i =>
        (i % d1 == 0, i % d2 == 0) match {
        case (true, false) => w1
        case (false, true) => w2
        case (true, true) => w
        case (false, false) => i.toString
    }
    }
    case _ => // TODO handle more than 2
    { i => ??? }
}
```

#### General observations

- Return a sum of a subset of the configured words, if there is any divisor match.
- If there is *no* divisor match, return the numerical string.

#### More computation means more types

Compile each divisor to a "rule" that awaits input.

```
type Rule = Int => String

val buildRule: ((Int, String)) => Rule = {
  case (n, word) => { i =>
    if (i % n == 0) word else ""
  }
}
```

# FizzBuzz demo time!

- Two volunteers: each to play role of Rule.
- One "manager" to combine two sub-results.

#### 4.3 Demo

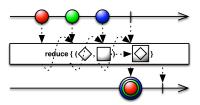
# Demo explanation

• Given a sequence of rules and an integer: apply all the rules to the integer, then combine the partial results.

# Assemble the types

# A note on reduce

For any value of type Seq[A], reduce:  $((A, A) \Rightarrow B) \Rightarrow B$ .



Example: for Seq[String], reduction with string concatenation + returns the concatenation of all the strings in the sequence.

# Test failure: coarse types again

```
nfo] x Arbitrary pair of divisors: divisible by first rror] A counter-example is 'Config(List((8,), (32,)))' (after 0 try) rror] A counter-example is '32405464' (after 0 try - shrinked ('1150076488' -> '32405464')) rror] '32405464' is not equal to '' (FizzBuzzSpec.scala:71)
```

#### Demo time!

```
• Configuration: Seq(3 -> "", 5 -> "Buzz")
```

```
• Input: 9 (note: divisible by 3)
```

• Output: should be "" (because of the part divisible by 3)

• Output was: "9"

# Property-based testing rescued us again!

Be honest: would you have caught this bug manually?

- I didn't.
- I never wrote FizzBuzzPop examples testing empty strings.
- Property-based testing reveals unexpected corner cases.

```
- (Empty "fizz" and "buzz" word strings).
```

# 4.4 Option[A] type

An empty string is not equivalent to no string

Presence of something "empty" is *not* equivalent to no thing. Sending someone an empty email versus not sending any email.

Many programming languages get this wrong.

# Option[A] type

Option[A] is one of two possibilities:

- None
- Some(a) wraps a value a of type A.

For example, Some("") is not the same as None.

```
val fizzFor3 = Some("") // multiple of 3
val buzzFor3 = None // not multiple of 5
val fizzbuzzFor3 = Some("") // fizzed ""

val fizzFor2 = None // not multiple of 3
val buzzFor2 = None // not multiple of 5
val fizzbuzzFor2 = None // not multiple of any
```

# Cleaning up the types

```
// was: type Rule = Int => String
type Rule = Int => Option[String]
```

# Useful type errors:

```
und : String
quired: Option[String]
    word
    ^
und : String("")
quired: Option[String]
    ""
    ^
und : Seq[Option[String]]
quired: Seq[String]
    val words: Seq[String] = rules map { rule => rule(i) }
    ^
```

#### Fix the type errors: our rule builder

```
type Rule = Int => Option[String]

val buildRule: ((Int, String)) => Rule = {
  case (n, word) => { i =>
      (i % n == 0).option(word)
  }
}
```

#### Demo time!

• (Instructions: for result Some(s), hold up the string, else don't hold up anything)

```
Configuration: Seq(3 -> "", 5 -> "Buzz")
Input: 9
```

• Output: now correctly is ""

# Fix the type errors: our compiler

```
val compile: Compiler = { case Config(pairs) =>
  val rules: Seq[Rule] = pairs map buildRule

{ i =>
   val wordOptions: Seq[Option[String]] =
      rules.map { rule => rule(i) }
  val combinedOption: Option[String] =
      wordOptions.reduce(addOption)
      combinedOption.getOrElse(i.toString)
  }
}
```

- We need to write: addOption
- Scala standard library provides: getOrElse

# "Addition" for Option[String]

```
def addOption(a1: Option[String], a2: Option[String]):
    Option[String] = (a1, a2) match {
    case (Some(s1), None) => Some(s1)
    case (None, Some(s2)) => Some(s2)
    case (Some(s1), Some(s2)) => Some(s1 + s2)
    case (None, None) => None
}
```

#### Getting A back out of Option[A]

# Do not lose information! getOrElse inspects the

and either

- returns the value v inside a Some(v),
- or else returns the specific default value.

#### Swift has two option types

Swift calls them "optionals".

# Normal optional type

- A? is a type for each type A.
- Must unwrap explicitly.

# Implicit unwrapped optional type

- A! is a type for each type A.
- Unfortunate type hole:

If you try to access an implicitly unwrapped optional when it does not contain a value, you will trigger a runtime error.

#### The same thing, in Swift

```
func addOption(a1: String?, a2: String?) -> String? = {
   switch (a1, a2) {
   case (let .Some(s1), .None): return .Some(s1)
   case (.None, let .Some(s2)): return .Some(s2)
   case (let .Some(s1), let .Some(s2)): return .Some(s1+s2)
   case (.None, .None): return .None
   }
}
```

# 4.5 Transform information; don't destroy it

#### Transform information; don't destroy it

Did you notice? Our new code no longer uses if.

#### Bug cause: destroying information, using if

- Building a rule: if (i % n == 0) word else ""
- Obtaining a final string answer: if (combined == "") i.toString else combined

#### Transforming information

- To Option[String]: (i % n == 0).option(word)
- To String: combinedOption.getOrElse(i.toString)

# Type-directed design tip

We could have saved trouble *up front*, by using precise *types*.

- Avoid if, when possible.
- Avoid String (but required at I/O boundaries of program).

#### Bonus: the final code in Swift

# 5 Parallel FizzBuzz

#### Parallelism

- Use of map: parallelizable; there are high-performance parallel collections for Scala.
- Use of *reduce*: parallelizable because of the monoid property:

# Option[String] is a Monoid

- There is an identity element (None).
- There is a binary associative operator (addOption).
- Fantastically important in practice!

#### Final demo!

#### Demo time!

- Configuration: Seq(3 -> "Fizz", 5 -> "Buzz", 7 -> "Pop", 2 -> "Boom")
- Tree of volunteers to simulate concurrency:
  - Four at leaves.
  - Two "middle managers" each handling two leaves.

- One top-level manager handling two middle managers.

```
• Input: 42
```

• Output: "FizzPopBoom"

# Final parallelized code

```
val parallelCompile: Compiler = { case Config(pairs) =>
  val rules = pairs.
    toArray.
    toPar.
    map(buildRule)

{ i: Int => rules.
    map { rule => rule(i) }.
    reduce(addOption).
    getOrElse(i.toString)
  }
}
```

# Coding style tip

This level of conciseness is not always best: maybe too "clever"?

#### Parallelism for Swift?

I expect people to develop libraries for parallelism in Swift.

#### Parallelism summary

We discovered a theoretical speedup for generalized FizzBuzz:

- Sequential: O(n)
- $\bullet$  Parallel:  $O(\log n)$  (given  $\log n$  processors, and omitting some technical subtleties)

Also, driver outer loop can be sped up:

- Sequential loop on 1 to m: O(m)
- Parallel loop: O(1) (given m processors)

#### Future work

- Asynchronous
- Real-time
- Interactive

# 6 Conclusion

#### Conclusion

- Tests are great.
- *Types* are great.
- Tests and types work hand in hand, driving design and program evolution.
- Modern typed languages such as Scala promote fun, correct programming!
- It's a great time to be learning and using a modern typed language: Apple ditched Objective C for Swift.

#### Code, slides, article

- Go to https://github.com/franklinchen/talk-on-type-directed-tdd-using-fizzbuzz
- The article has more detail omitted in the presentation.
- The hyperlinks in all provided PDFs are clickable.
- $\bullet \ \ The \ Swift \ code: \ https://github.com/franklinchen/fizzbuzz-swift \\$

# Appendix

# Some free online courses on modern typed functional programming

- Using Scala: Functional Programming Principles in Scala on Coursera, taught by Martin Odersky (inventor of Scala)
- Using Haskell: Introduction to Functional Programming on EdX, taught by Erik Meijer (Haskell hero)