

- 1 1. The power of simulating data: a tool to design experiments,  
2 understand data limitations and improve scientific reasoning
- 3 2. Between noise and patterns: the power of data simulation  
4 in science to overcome perception biases
- 5 3. The power of simulating data: a tool for scientists from  
6 designing experiments to drawing/reaching reasonable  
7 conclusions
- 8 4. Between noise and patterns: Overcoming perception biases  
9 through data simulation

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## 12 Abstract

13 What's the Problem, what do we want to save and what's the solution

14 - Werwolf: p-values, 'sloppy', simplified stats, over-interpretation of patterns that emerge by chance

15 - Baby: scientific standards, correct conclusions, knowing the potential and limits of a dataset

16 - Silverbullet: Data simulation through formulation of a mathematical model and playing with the  
17 parameters and the replication

18 Science continuously tries to explain patterns in nature that appear in data, hidden by the noise of  
19 variation caused by thousands of influencing factors. Statistics provide us with a tool to separate noise  
20 from a real pattern that is unlikely to have occurred simply by chance. At the same time however,  
21 some statistical measures have left us overconfident to find this hidden 'treasures' and our minds seem  
22 not to be trained enough to judge the difference in many cases. In fact it turns out that humans are  
23 really bad in capturing the amount of variation that can be expected.

## 24 Introduction

25 A renowned researcher once explained to me the progression of a curve deriving from a dendrometer

26 - a device attached to the bark of a tree that stood beside us. As we observed the graph on the  
27 screen extending in real-time, he provided a passionate and insightful explanation on water relations  
28 and plant physiology. However, moments later, the responsible technician entrusted me with the fact,  
29 that the device hasn't yet recorded anything meaningful and that all data displayed couldn't possibly  
30 depict anything biologically relevant. This example - and I think most of us can share similar stories -  
31 shows the incredible ability of our minds to make sense of patterns that underpin our current beliefs  
32 or argument. But it also underpins our blindness of how randomness or noise can look like. However,  
33 separating noise from a pattern is perhaps the most important skill of any researcher.

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We all manage to go through this world with the help of models in our minds. Most of the time we are not aware of this fact but their implications are all around us. For instance when we wait for a bus we expect the waiting time to be lets say around  $7 \pm 3$  min or when we readjust our expected travel time after an incidence and add the variable 'traffic jam' to our internal model. In short, whenever we have an intuitive understanding of how the world works, our brain suggests basic models - mostly oversimplified and with increasing bias as soon as we enter non-linear relationships. - In many practical cases we get the chance to recalibrate our internal model (or lets call it intuition). For example when the bus after 10 min is still not there and we start realizing that we need to incorporate the variable 'traffic jam'. But in many cases we don't get this kind of feedback or at least not in an informative way because it is too complex to grasp for our minds. While daily life is arguably not a big drawback to this issue, in science it can be.

## Current challenges with data interpretation in science

Famous examples of data overinterpretation or drawing wrong conclusions.

## Replication crisis is not over

Too many studies are still caried out with simply too few replicates. Especially when drawing conclusions based on interactions.

## Problems associated with p-values, associated thresholds and biases in reporting of relevant findings

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Although Fisher's concept of the p-value and the associated threshold value date back more than a century, they are still the standard in many scientific disciplines, institutes and research groups.

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## Modern statistics departs from p-values

problem with p values, many scientists continue using them, despite the ban of p-values and words like "significant" by some journals. Language change. Introduce Bayesian stats.

Here it would be nice to show a graph with the inreased usage of Bayesian approaches over time for different science fields and journals or the appearance of words like 'p-value' and 'Bayesian' or? over time to underpin that Bayesian stats is on the rise.

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## Simulating data as an integral part of conducting science

Beyond that many Bayesian statisticians see themselves not only as simply using a different method but rather as a new philosophy of conducting science that starts already prior to an experiment or way

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76 before looking at some real data.

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78 We think it is time to highlight the advantages of one, in our opinion the most important step of the  
79 Bayesian approach to conduct science. And I am convinced that this step benefits to all scientists, no  
80 matter which way they proceed. In fact, we believe it would be most beneficial for students through all  
81 academic stages and should become an integral part of statistical teaching as it allows to convincingly  
82 self assess the potential of a particular dataset and to evaluate its suitability to answer a specific  
83 question of interest.

84 This paper aims to bridge frequentists and Bayesian ways of thinking by encouraging the usage of data  
85 simulation to check assumptions, evaluate replication, define hypothesis and to assess model suitability.

## 86 What does data simulation imply?

87 Simulating data is not a new idea and there are excellent books demonstrating their usefulness and  
88 power as an integral approach to make statistical inference (do you know some examples beside ROS?).  
89 However, this approach still hasn't been considered/adopted by most researchers particular in some  
90 science fields and most concerning has not entered statistical teaching at most universities.

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92 Fake data simulation is a great way to overcome these issues. Because it forces and allows us to:

- 93 - think about our currently existing model of how we see the world, clarifying our expectations
- 94 - get feedback in a valuable way so that we can calibrate our model (in this case this means our  
95 mathematical model but also our general understanding)
- 96 - get a better sense and intuition of natural variability
- 97 - think more carefully about the design of an experiment

98 Fake data simulation is not about directly generating the y-variable of interest with a certain distribu-  
99 tion in mind. It is more complex but more interesting and meaningful: We think about what factors  
100 (that are truly relevant) are influencing the y-variable of interest in which way. This is important  
101 because at this point we already clarify the mathematical relationship between explanatory variables  
102 and y. These are parameters (e.g. intercept and slope). Because real data are never exactly on a line  
103 (in that case) we need to think about introducing a meaningful amount of noise and how we expect its  
104 distribution. - In other words simulating data means we have to think about a mathematical function  
105 and define our parameters so that we can produce y-values that match our expectations including a  
106 realistic amount of noise.

## 107 Examples

108 here we would provide some code to simulate data to give an example of how many replicates would  
109 be needed to get consistent results with a given effect size etc. or show that we can get a whole  
110 distribution of p-values if we repeat our simulation enough

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