

Sum of Two Integers

Calculate the sum of two integers a and b , but you are **not allowed** to use the operator `+` and `-`.

Example:

Given $a = 1$ and $b = 2$, return 3.

Credits:

Special thanks to [@fujiaozhu](#) for adding this problem and creating all test cases.

Solution 1

I have been confused about bit manipulation for a very long time. So I decide to do a summary about it here.

"&" AND operation, for example, $2 (0010) \& 7 (0111) \Rightarrow 2 (0010)$

"^" XOR operation, for example, $2 (0010) \wedge 7 (0111) \Rightarrow 5 (0101)$

"~" NOT operation, for example, $\sim 2(0010) \Rightarrow -3 (1101)$ what??? Don't get frustrated here. It's called two's complement.

1111 is -1, in two's complement

1110 is -2, which is $\sim 2 + 1$, $\sim 0010 \Rightarrow 1101$, $1101 + 1 = 1110 \Rightarrow -2$

1101 is -3, which is $\sim 3 + 1$

so if you want to get a negative number, you can simply do $\sim x + 1$

Reference:

https://en.wikipedia.org/wiki/Two%27s_complement

<https://www.cs.cornell.edu/~tomf/notes/cps104/twoscomp.html>

For this, problem, for example, we have $a = 1$, $b = 3$,

In bit representation, $a = 0001$, $b = 0011$,

First, we can use "and"("&") operation between a and b to find a carry.

$\text{carry} = a \& b$, then $\text{carry} = 0001$

Second, we can use "xor" ("^") operation between a and b to find the different bit, and assign it to a,

Then, we shift carry one position left and assign it to b, $b = 0010$.

Iterate until there is no carry (or $b == 0$)

```

// Iterative
public int getSum(int a, int b) {
    if (a == 0) return b;
    if (b == 0) return a;

    while (b != 0) {
        int carry = a & b;
        a = a ^ b;
        b = carry << 1;
    }

    return a;
}

// Iterative
public int getSubtract(int a, int b) {
    while (b != 0) {
        int borrow = (~a) & b;
        a = a ^ b;
        b = borrow << 1;
    }

    return a;
}

// Recursive
public int getSum(int a, int b) {
    return (b == 0) ? a : getSum(a ^ b, (a & b) << 1);
}

// Recursive
public int getSubtract(int a, int b) {
    return (b == 0) ? a : getSubtract(a ^ b, (~a & b) << 1);
}

// Get negative number
public int negate(int x) {
    return ~x + 1;
}

```

written by [zhaolz](#) original link [here](#)

Solution 2

test cases all pass

0 ms

```
public int getSum(int a, int b) {  
    if(b == 0){// 没有进为的时候完成运算  
        return a;  
    }  
    int sum,carry;  
    sum = a^b;// 完成第一步加发的运算  
    carry = (a&b)<<1;// 完成第二步进位并且左移运算  
    return getSum(sum,carry);  
}
```

written by [lido04](#) original link [here](#)

Solution 3

```
class Solution {
public:
    int getSum(int a, int b) {
        int sum = a;

        while (b != 0)
        {
            sum = a ^ b; //calculate sum of a and b without thinking the carry
            b = (a & b) << 1; //calculate the carry
            a = sum; //add sum(without carry) and carry
        }

        return sum;
    }
};
```

written by [vdrvdd](#) original link [here](#)

From [LeetCoder](#).