

Q2:

integration $F_1 = \int_0^1 x^3 = \frac{x^4}{4} \Big|_0^1 = \frac{1}{4}$

$$F_2 = \int 1 = x$$

$$U \sim \text{uniform}(0, 1)$$

if $U < \frac{1}{3}$

invert F_1

solve $U = \frac{x^4}{4}$, with $3U = x^4$
 $x = (3U)^{1/4}$

else

invert method for F_2

$$U = x$$