

Primitive Root Modulo n

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Hey folks,

Today we are going to talk about the concept of *primitive root modulo n* and a [codeforces problem](#) on it.

Definition

x is a primitive root modulo of a number n if

for all ' a ' such that ' a ' is coprime to ' n ' there exist a ' k ' for which the following condition holds true.

$$x^k = a \pmod{n}$$

Actually the above condition can also be written in simpler words like :

let A is a set of all numbers coprime to ' n ' and are less than ' n '

then for every ' x ' in A if [multiplicative order](#) of ' x ' is equal to the [euler_totient function\(\$n\$ \)](#) then ' x ' is primitive root modulo ' n '.

Example

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Example.

if $n=14$ then $A = \{1, 3, 5, 9, 11, 13\}$

$x \ x, \ x^2, \ x^3, \ \dots \pmod{14}$

1 : 1

3 : 3, 9, 13, 11, 5, 1

5 : 5, 11, 13, 9, 3, 1

9 : 9, 11, 1

11 : 11, 9, 1

13 : 13, 1

only $x = 3$ and 5 satisfied the given condition so they are primitive root modulo n .

Note : It is possible that there is no primitive root modulo n for example there is no primitive root modulo n for 15 .

Finally , the no of primitive root modulo n of a give number are

$\text{euler_totient_function}(\text{euler_totient_function}(n))$

the problem on codeforces is also the same in which we have to calculate the no of primitive root modulo n .

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return 42;

May 2012

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