Tutorial on How to Fit Latent Factor Models

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This paper describes how you can fit latent factor models (e.g., [1, 2, 3]) using the open source package developed in Yahoo! Labs.

Stable repository: https://github.com/yahoo/Latent-Factor-Models
Development repository: https://github.com/beechung/Latent-Factor-Models

1 Preparation

Before you can use this code to fit any model, you need to install R (with R version $\geq 2.10.1$) and compile the C/C++ code in this package.

1.1 Install R

Before installing R, please make sure that you have C/C++ and Fortran compilers (e.g., gcc and gfortran) installed on your machine.

To install R, go to http://www.r-project.org/. Click CRAN on the left panel. Pick a CRAN mirror. Then, install R from the R source code. The fact that you are able to build R from source would ensure that you can compile the C/C++ code in this package.

Alternatively, you can install R using linux's package management software. In this case, please install r-base, r-base-core, r-base-dev, r-recommended.

After installing R, enter R by simply typing R and install the following R packages: Matrix and glmnet. Notice that these two packages are not required if you do not need to handle sparse feature vectors or matrices. To install these R packages, use the following commands in R.

```
> install.packages("Matrix");
> install.packages("glmnet");
```

Make sure that you can run R by simply typing R. Otherwise, please use alias to point R to your R executable file. This is required for make to work properly.

1.2 Be Familiar with R

This tutorial assumes that you are familiar with R, at least comfortable reading R code. If not, please read

http://cran.r-project.org/doc/manuals/R-intro.pdf.

1.3 Compile C/C++ Code

This is extremely simple. Just type make in the top-level directory (i.e., the directory that contains LICENSE, README, Makefile, Makevars, etc.).

2 Bias-Smoothed Tensor Model

The bias-smoothed tensor (BST) model [2] includes the regression-based latent factor model (RLFM) [1] and regular matrix factorization models as special cases. In fact, the BST model presented here is more general than the model presented in [2]. In the following, I demonstrate how to fit such a model and its special cases. The R code of this section can be found in src/R/examples/tutorial-BST.R.

2.1 Model

We first specify the model in its most general form and then describe special cases. Let y_{ijkpq} denote the response (e.g., rating) that source node i (e.g., user i) gives destination node j (e.g., item j) in context (k, p, q), where the context is specified by a three dimensional vector:

- Edge context k specifies the context when the response occurs on the edge from node i to node j; e.g., the rating on the edge from user i to item j was given when i saw j on web page k.
- Source context p specifies the context (or mode) of the source node i when this node gives the response; e.g., p represents the category of item j, meaning that user i are in different modes when rating items in different categories.
- Destination context q specifies the context (or mode) of the destination node j when this node receives the response; e.g., q represents the user segment that user i belongs to, meaning that the response that an item receives depends on the segment that the user belongs to.

Notice that the context (k, p, q) is assumed to be given and each individual response is assumed to occur in a single context. Also note that when modeling a problem, we may not always need all the three components in the three dimensional context vector.

Because i always denotes a source node (e.g., a user), j always denotes a destination node (e.g., an item) and k always denotes an edge context, we slightly abuse our notation by using x_i to denote the feature vector of source node i, x_j to denote the feature vector of destination node j, x_k to denote the feature vector of edge context k, and x_{ijk} to denote the feature vector associated with the occasion when i gives j the response in context k.

Response model: For numeric response, we use the Gaussian response model; for binary response, we use the logistic response model.

$$y_{ijkpq} \sim \mathcal{N}(\mu_{ijkpq}, \sigma_y^2)$$
 or $y_{ijkpq} \sim Bernoulli((1 + \exp(-\mu_{ijkpq}))^{-1}),$

where $\mu_{ijkpq} = \mathbf{x}'_{ijk}\mathbf{b} + \alpha_{ip} + \beta_{jq} + \gamma_k + \langle \mathbf{u}_i, \mathbf{v}_j, \mathbf{w}_k \rangle$. Note that $\langle \mathbf{u}_i, \mathbf{v}_j, \mathbf{w}_k \rangle = \sum_{\ell} \mathbf{u}_i[\ell] \mathbf{v}_j[\ell] \mathbf{w}_k[\ell]$ is a form of the tensor product of three vectors $\mathbf{u}_i, \mathbf{v}_j$ and \mathbf{w}_k , where $\mathbf{u}_i[\ell]$ denotes the ℓ th element in vector \mathbf{u}_i . For ease of exposition, we use the following notation to represent both the Gaussian and logistic models.

$$y_{ijkpq} \sim \boldsymbol{x}'_{ijk}\boldsymbol{b} + \alpha_{ip} + \beta_{jq} + \gamma_k + \langle \boldsymbol{u}_i, \boldsymbol{v}_j, \boldsymbol{w}_k \rangle,$$
 (1)

where \boldsymbol{b} is the regression coefficient vector on feature vector \boldsymbol{x}_{ijk} ; α_{ip} is the latent factor of source node i in source context p; β_{jq} is the latent factor of destination node j in destination context q; γ_k is the latent factor of edge context k; \boldsymbol{u}_i , \boldsymbol{v}_j and \boldsymbol{w}_k are the latent factor vectors of source node i, destination node j and edge context k, respectively. Note that these latent factors and regression coefficients will be learned from data.

Regression Priors: The priors of the latent factors are specified in the following:

$$\alpha_{ip} \sim \mathcal{N}(\mathbf{g}_p' \mathbf{x}_i + q_p \alpha_i, \ \sigma_{\alpha,p}^2), \quad \alpha_i \sim \mathcal{N}(0,1)$$
 (2)

$$\beta_{jq} \sim \mathcal{N}(\mathbf{d}_q' \mathbf{x}_j + r_q \beta_j, \ \sigma_{\beta,q}^2), \quad \beta_j \sim \mathcal{N}(0,1)$$
 (3)

$$\gamma_k \sim \mathcal{N}(\mathbf{h}' \mathbf{x}_k, \, \sigma_\gamma^2 I),$$
 (4)

$$\boldsymbol{u}_i \sim \mathcal{N}(G'\boldsymbol{x}_i, \sigma_u^2 I), \quad \boldsymbol{v}_j \sim \mathcal{N}(D'\boldsymbol{x}_j, \sigma_v^2 I), \quad \boldsymbol{w}_k \sim \mathcal{N}(H'\boldsymbol{x}_k, \sigma_w^2 I),$$
 (5)

where g_p , q_p , d_q , r_q , G, D and H are regression coefficient vectors and matrices. These regression coefficients will be learned from data and provide the ability to make predictions for users or items that do not appear in training data. The factors of these new users or items will be predicted based on their features through regression.

2.2 Toy Dataset

In the following, we describe a toy dataset. You can put your data in the same format to fit the model to your data. This toy dataset is in the following directory:

test-data/multicontext_model/simulated-mtx-uvw-10K

Please read the README file there to better understand this dataset, which was created by running the following R script. Please do not rerun this R script.

src/unit-test/multicontext_model/create-simulated-data-1.R

This is a simulated dataset; i.e., the response values y_{ijkpq} are generated according to a ground-truth model. To see the ground-truth, run the following commands in R.

```
> load("test-data/multicontext_model/simulated-mtx-uvw-10K/ground-truth.RData");
> str(factor);
> str(param);
```

Response Data: The response data, also called observation data, is in obs-train.txt and obs-test.txt. Each file has six columns:

- 1. src_id : Source node ID (e.g., user i).
- 2. dst_id : Destination node ID (e.g., item j).
- 3. $src_context$: Source context ID (e.g., source context p).
- 4. dst_context: Destination context ID (e.g., destination context q).
- 5. ctx_id : Edge context ID (e.g., edge context k).
- 6. y: Response (e.g., the rating that user i gives item j in context (k, p, q)).

Note that all of the above IDs can be numbers or character strings. To read obs-train.txt, run the following commands in R.

```
> input.dir = "test-data/multicontext_model/simulated-mtx-uvw-10K"
> obs.train = read.table(paste(input.dir,"/obs-train.txt",sep=""),
    sep="\t", header=FALSE, as.is=TRUE);
> names(obs.train) = c("src_id", "dst_id", "src_context",
    "dst_context", "ctx_id", "y");
```

It is important to note that the **column names** of an observation table have to be exactly **src_id**, **dst_id**, **src_context**, **dst_context**, **ctx_id** and **y**. The model fitting code does not recognize other names.

Source, Destination and Context Features: The features vectors of source nodes (x_i) , destination nodes (x_j) , edge contexts (x_k) and training and test observations (x_{ijk}) are in

```
type-feature-user.txt,
type-feature-item.txt,
type-feature-ctxt.txt,
```

where type = "dense" for the dense format and type = "sparse" for the sparse format.

For the dense format, take dense-feature-user.txt for example. The first column is src_id (the src_id column in the observation table refers to this column to get the feature vector of the source node for each observation). It is important to note that the name of the first column has to be exactly src_id. The rest of the columns specify the feature values and the column names can be arbitrary.

For the sparse format, take <code>sparse-feature-user.txt</code> for example. It has three columns:

1. src_id: Source node ID

- 2. index: Feature index (starting from 1, not 0)
- 3. value: Feature value

It is important to note that the **column names** have to be exactly **src_id**, **index** and **value**.

```
dense-feature-user.txt
sparse-feature-user.txt
SPARSE FORMAT
                       <=> DENSE FORMAT
src_id index
                            src_id
                                     feature_1 feature_2 feature_3
               value
   15
           2 -0.978
                                             0
                                                   -0.978
                                                               0.031
                                15
   15
           3
              0.031
```

Observation Features: The features vectors of training and test observations (x_{ijk}) are in

```
type-feature-obs-train.txt,
type-feature-obs-test.txt,
```

where type = "dense" for the dense format and type = "sparse" for the sparse format.

For the dense format, take dense-feature-obs-train.txt for example. The *n*th line specifies the feature vector of observation on the *n*th line of obs-train.txt. Since there is a line-by-line correspondence, there is no need to have an ID column. Each column in this file represents a feature and the column names can be arbitrary.

For the sparse format, take sparse-feature-obs-train.txt for example. It has three columns:

- 1. obs_id: Line number in obs-train.txt (starting from 1, not 0)
- 2. index: Feature index (starting from 1, not 0)
- 3. value: Feature value

It is important to note that the **column names** have to be exactly **src_id**, **index** and **value**.

```
obs_id index value  # MEANING
     9     1     0.14     # 1st feature of line     9 in obs-train.txt = 0.14
     9     2     -0.93     # 2nd feature of line     9 in obs-train.txt =-0.93
     10     1     -0.91     # 1st feature of line 10 in obs-train.txt =-0.91
```

2.3 Quick Start

In this section, we describe how to fit BST models using this package without much need for familiarity of R or deep understanding of the code. Before you run the sample code, please make sure you are in the top-level directory of the installed code, i.e. by using Linux command 1s, you should be able to see files "LICENSE" and "README".

Step 1: Read training and test observation tables (obs.train and obs.test), their corresponding observation feature tables (x_obs.train and x_obs.test), the source feature table (x_src), the destination feature table (x_dst) and the edge context feature table (x_ctx) from the corresponding files. Note that if you replace these tables with your data, you must not change the column names. Assuming we use the dense format of the feature files, a sample code can be

```
>input.dir = "test-data/multicontext_model/simulated-mtx-uvw-10K"
obs.train = read.table(paste(input.dir, "/obs-train.txt", sep=""),
            sep="\t", header=FALSE, as.is=TRUE);
names(obs.train) = c("src_id", "dst_id", "src_context",
                     "dst_context", "ctx_id", "y");
x_obs.train = read.table(paste(input.dir,"/dense-feature-obs-train.txt",
              sep=""), sep="\t", header=FALSE, as.is=TRUE);
obs.test = read.table(paste(input.dir,"/obs-test.txt",sep=""),
           sep="\t", header=FALSE, as.is=TRUE);
names(obs.test) = c("src_id", "dst_id", "src_context",
                    "dst_context", "ctx_id", "y");
x_obs.test = read.table(paste(input.dir,"/dense-feature-obs-test.txt",
             sep=""), sep="\t", header=FALSE, as.is=TRUE);
x_src = read.table(paste(input.dir,"/dense-feature-user.txt",sep=""),
        sep="\t", header=FALSE, as.is=TRUE);
names(x_src)[1] = "src_id";
x_dst = read.table(paste(input.dir,"/dense-feature-item.txt",sep=""),
        sep="\t", header=FALSE, as.is=TRUE);
names(x_dst)[1] = "dst_id";
x_ctx = read.table(paste(input.dir,"/dense-feature-ctxt.txt",sep=""),
        sep="\t", header=FALSE, as.is=TRUE);
names(x_ctx)[1] = "ctx_id";
```

Step 2: We start fitting the model by loading the function fit.bst in src/R/BST.R.
>source("src/R/BST.R");

Then we run a simple latent factor model using the following command

```
>ans = fit.bst(obs.train=obs.train, obs.test=obs.test, x_obs.train=x_obs.train,
x_obs.test=x_obs.test, x_src=x_src, x_dst=x_dst, x_ctx=x_ctx,
out.dir = "/tmp/unit-test/simulated-mtx-uvw-10K",
model.name="uvw", nFactors=3, nIter=10);
```

Basically we put all the loaded data sets as input of the function, specify the output directory prefix as /tmp/unit-test/simulated-mtx-uvw-10K, and run model uvw. Note that the model name is quite arbitrary, and the final output directory for model uvw is /tmp/unit-test/simulated-mtx-uvw-10K_uvw. For model uvw, we use 3 factors and run 10 EM iterations.

Step 3: Once Step 2 is finished, we have the predicted values of the response variable y, since we have the test data as input of the function (If we do not have test data, we can simply omit the obs.test and x.obs.test option, and

the final output would only have model parameters without prediction results). Check out the file prediction inside the output directory (In our example, $/tmp/unit-test/simulated-mtx-uvw-10K_uvw/prediction$ is the filename). The file has two columns: the original observed y and the predicted y (the pred_y column). Standard metrics such as complete data log-likelihood and RMSE (root mean squared error) have been generated in the file summary. Check Section ?? for more details.

Please note that the predicted values of y for model uvw can also be found at anspred.yuvw. Run multiple models simultaneously: We actually are

able to run multiple BST models simultaneously using the following command

```
>ans = fit.bst(obs.train=obs.train, obs.test=obs.test, x_obs.train=x_obs.train,
x_obs.test=x_obs.test, x_src=x_src, x_dst=x_dst, x_ctx=x_ctx,
out.dir = "/tmp/unit-test/simulated-mtx-uvw-10K",
model.name=c("uvw1", "uvw2"), nFactors=c(1,2), nIter=10);
```

Here we are able to run two models: uvw1 and uvw2 simultaneously by setting the model.name and nFactors as 2-dimensional vectors, i.e. model uvw1 uses 1 factor, and model uvw2 uses 2 factors. They both do 10 EM iterations and unfortunately for fair comparison between sibling models we do not allow running environment parameters such as nIter to be different among different models. Plus, we do have the model parameters for each EM iteration saved in the output directory of each model. Please check out each model's output directory for model summary and prediction files.

Basic parameters: The meaning of basic parameters of function fit.bst are listed as follows:

- code.dir is the top-level directory of where code get installed. If you are already in the directory, the default which is the empty string can be used.
- obs.train, obs.test, x.obs.train, x.obs.test, x_src, x_dst, x_ctx are the data. Please check Section ?? for more details. Note that only obs.train is required to run this code; everything else is optional depends on the problem you have.
- out.dir is the output directory prefix. The final output directory is out.dir_model.name.
- model.name is the names of models to run. It can be any arbitrary string or a vector of strings. Default is "model".
- nFactors specifies the number of factors for each model. It can be either a scalar value or a vector of numbers with length equal to the number of models.
- nIter specifies the number of EM iterations. All the models share the same number of iterations.

- nSamplesPerIter specifies the number of Gibbs samples per E-step. It can be either a scalar which means every EM iteration share the same nSamplesPerIter, or it can be a vector with length equal to nIter, i.e. each EM iteration has their own values of nSamplesPerIter. Note that all models share the same nSamplesPerIter.
- is.logistic specifies whether we want to use logistic link function for our models on binary response data. Default is FALSE. It can be either a boolean value that is shared by all models, or a vector of boolean values with length equal to the number of models.
- src.dst.same: Whether source nodes and destination nodes refer to the same set of entities. For example, if source nodes represent users and destination nodes represents items, src.dst.same should be set to FALSE. However, if both source and destination nodes represent users (e.g., users rate other users) and $src_id = A$ refers to the same user A as $dst_id = A$, the src.dst.same should be set to TRUE. Regarding to modeling, when src.dst.same is TRUE, $\langle u_i, v_j, w_k \rangle$ in the model specified in Eq 1 will be replaced by $\langle v_i, v_j, w_k \rangle$. The default of src.dst.same is FALSE.
- control has a list of more advanced parameters that will be introduced later.

Advanced parameters: control=fit.bst.control(...) contains the following advanced parameters:

- rm.self.link: Whether to remove self-edges. If src.dst.same=TRUE, you can choose to remove observations with src_id = dst_id by setting rm.self.link=FALSE. Otherwise, rm.self.link should be set to FALSE. The default of rm.self.link is FALSE.
- add.intercept: Whether you want to add an intercept to each feature matrix. If add.intercept=TRUE, a column of all 1s will be added to every feature matrix. The default of add.intercept is TRUE.
- has.gamma specifies whether to include γ_k in the model specified in Eq 1 or not. If has.gamm=FALSE, γ_k will be disabled or removed from the model. For the default, has.gamma is set as FALSE unless the training response data obs.train do not have any source or destination context, but have edge context.
- reg.algo and reg.control specify how the regression priors will to be fitted. If they are set to NULL (default), R's basic linear regression function lm will be used to fit the prior regression coefficients g, d, h, G, D and H. Currently, we only support two other algorithms "GLMNet" and "RandomForest". Therefore, reg.algo can only have three types of values: NULL, "GLMNet" and "RandomForest" (both are strings). Notice that if "RandomForest" is used, the regression priors become nonlinear; see [3] for more information.

- nBurnin is the number of burn-in samples per E-step. The default is 10% of nSamplesPerIter.
- init.params is a list of the initial values of all the variance component parameters. The default values of init.params is

The details of the meanings of these parameters can be found at Section ??

• random.seed is the random seed for the model fitting procedure.

2.4 Model Fitting Details

See Example 1 in src/R/examples/tutorial-BST.R for the R script. For succinctness, we ignore some R commands in the following description.

Step 1: Read training and test observation tables (obs.train and obs.test), their corresponding observation feature tables (x_obs.train and x_obs.test), the source feature table (x_src), the destination feature table (x_dst) and the edge context feature table (x_ctx) from the corresponding files. Note that if you replace these tables with your data, you must not change the column names.

```
input.dir = "test-data/multicontext_model/simulated-mtx-uvw-10K"
obs.train = read.table(paste(input.dir,"/obs-train.txt",sep=""),
            sep="\t", header=FALSE, as.is=TRUE);
names(obs.train) = c("src_id", "dst_id", "src_context",
                     "dst_context", "ctx_id", "y");
x_obs.train = read.table(paste(input.dir,"/dense-feature-obs-train.txt",
              sep=""), sep="\t", header=FALSE, as.is=TRUE);
obs.test = read.table(paste(input.dir,"/obs-test.txt",sep=""),
           sep="\t", header=FALSE, as.is=TRUE);
names(obs.test) = c("src_id", "dst_id", "src_context",
                    "dst_context", "ctx_id", "y");
x_obs.test = read.table(paste(input.dir,"/dense-feature-obs-test.txt",
             sep=""), sep="\t", header=FALSE, as.is=TRUE);
x_src = read.table(paste(input.dir,"/dense-feature-user.txt",sep=""),
        sep="\t", header=FALSE, as.is=TRUE);
names(x_src)[1] = "src_id";
x_dst = read.table(paste(input.dir,"/dense-feature-item.txt",sep=""),
        sep="\t", header=FALSE, as.is=TRUE);
names(x_dst)[1] = "dst_id";
x_ctx = read.table(paste(input.dir,"/dense-feature-ctxt.txt",sep=""),
        sep="\t", header=FALSE, as.is=TRUE);
names(x_ctx)[1] = "ctx_id";
```

Step 2: Index the training and test data. Functions indexData and indexTestData (defined in rc/R/model/multicontext_model_utils.R) convert the input data tables into the right data structure. In particular, they replace the original IDs (src_id, dst_id, src_context, dst_context and ctx_id) by consecutive index numbers, and convert feature tables (data frames) into feature matrices.

```
data.train = indexData(
    obs=obs.train, src.dst.same=FALSE, rm.self.link=FALSE,
    x_obs=x_obs.train, x_src=x_src, x_dst=x_dst, x_ctx=x_ctx,
    add.intercept=TRUE
);
data.test = indexTestData(
    data.train=data.train, obs=obs.test,
    x_obs=x_obs.test, x_src=x_src, x_dst=x_dst, x_ctx=x_ctx
):
```

We then describe some input parameters to function indexData.

- src.dst.same: Whether source nodes and destination nodes refer to the same set of entities. For example, if source nodes represent users and destination nodes represents items, src.dst.same should be set to FALSE. However, if both source and destination nodes represent users (e.g., users rate other users) and src_id = A refers to the same user A as dst_id = A, the src.dst.same should be set to TRUE.
- rm.self.link: Whether to remove self-edges. If src.dst.same=TRUE, you can choose to remove observations with src_id = dst_id by setting rm.self.link=FALSE. Otherwise, rm.self.link should be set to FALSE
- add.intercept: Whether you want to add an intercept to each feature matrix. If add.intercept=TRUE, a column of all 1s will be added to every feature matrix.

Because data.train is passed into indexTestData, the above parameters do not need to be passed into indexTestData and the parameter setting used to create the test data will be the same as the setting used to create the training data.

The output of indexData and indexTestData primarily consists of the following three components:

- obs: This is the observation table (data frame) with the new numeric index IDs. The columns are: src.id, dst.id, src.context, dst.context, edge.context and y, where src.id corresponds to src_id, etc., and edge.context corresponds to ctx_id.
- IDs: This list of vectors contains the mapping from new numeric index IDs to the original IDs.
- feature: This is a list of four feature matrices. x_obs , x_src , x_dst and x_cctx correspond to x_{ijk} , x_i , x_j and x_k , respectively.

For example, assume the mth row of data.train\$obs is

```
src.id dst.id src.context dst.context edge.context y i \quad j \quad p \quad q \quad k \quad y_{ijkpq}
```

Then, we have the following correspondence:

- data.train\$IDs\$SrcIDs[i] is the original source node ID of this observation. Similarly, DstIDs[j], SrcContexts[p], DstContexts[q] and CtxIDs[k] are the original IDs of the destination node, source context, destination context, edge context of this observation.
- data.train\$feature\$x_obs[m,] is the observation feature vector of this observation. Similarly, x_src[i,], x_dst[j,] and x_ctx[k,] are the feature vectors of the source node, destination node and edge context of this observation.

Step 3: Fit the model(s). We first specify the settings of the models to be fitted.

```
setting = data.frame(
                  = c("uvw1", "uvw2"),
   name
                  = c(
   nFactors
                         1,
                                   2).
                  = c(TRUE,
                                TRUE).
   has.11
                  = c( FALSE,
                               FALSE).
   has.gamma
                         Ο,
   nLocalFactors = c(
                                   0).
    is.logistic
                = c( FALSE,
```

In the above example, we specify two models to be fitted.

- name specifies the name of the model, which should be unique.
- nFactors specifies the number of interaction factors per node; i.e., the number of dimensions of v_j , which is the same as the numbers of dimensions of u_i and w_k . If you want to disable or remove $\langle u_i, v_j, w_k \rangle$ from the model specified in Eq 1, set nFactors = 0.
- has.u specifies whether to use $\langle u_i, v_j, w_k \rangle$ in the model specified in Eq 1 or replace this term by $\langle v_i, v_j, w_k \rangle$ (more examples will be given later). Notice that the latter does not have factor vector u_i ; thus, it corresponds to has.u=FALSE. It is important to note that if has.u=FALSE, you must set src.dst.same=TRUE when calling indexData in Step 2.
- has.gamma specifies whether to include γ_k in the model specified in Eq 1 or not. If has.gamm=FALSE, γ_k will be disabled or removed from the model.
- nLocalFactors should be set to 0 for most cases. Do not set it to other numbers unless you know what you are doing.

• is.logistic specifies whether to use the logistic response model or not. If is.logistic=FALSE, the Gaussian response model will be used.

In the following, we demonstrate a few different example settings and their corresponding models.

• The original BST model defined in [2]: Set has.u=FALSE, has.gamma=FALSE, and set all the context columns to be the same in the input data; i.e., before Step 2, set the input observation tables obs.train and obs.test so that the following holds.

```
obs.train$src_context = obs.train$dst_context = obs.train$ctx_id
obs.test$src_context = obs.test$dst_context = obs.test$ctx_id
```

This setting gives the following model:

$$y_{ijk} \sim \boldsymbol{x}'_{ijk}\boldsymbol{b} + \alpha_{ik} + \beta_{jk} + \langle \boldsymbol{v}_i, \boldsymbol{v}_j, \boldsymbol{w}_k \rangle$$

Notice that since all the context columns are the same, there is no need for using a three dimensional context vector (k,p,q); instead, it is sufficient to just use k to index the context in the above equation. Also note that you must set $\mathtt{src.dst.same=TRUE}$ when calling $\mathtt{indexData}$ in Step 2.

• The RLFM model defined in [1]: Set has.u=TRUE, has.gamma=FALSE, and before Step 2, set:

```
obs.train$src_context = obs.train$dst_context = obs.train$ctx_id = NULL;
obs.test$src_context = obs.test$dst_context = obs.test$ctx_id = NULL;
x_ctx = NULL;
```

This setting gives the following model:

$$y_{ij} \sim \boldsymbol{x}'_{ij}\boldsymbol{b} + \alpha_i + \beta_j + \boldsymbol{u}'_i\boldsymbol{v}_j$$

Notice that setting the context-related objects to NULL disables the context-specific factors in the model.

Step 4: Run the model fitting procedure.

```
out.dir = "/tmp/unit-test/simulated-mtx-uvw-10K";
ans = run.multicontext(
    obs=data.train$obs,
                                # training observation table
    feature=data.train$feature, # training feature matrices
    setting=setting, # setting specified in Step 3
                    # number of Gibbs samples in each E-step
   nSamples=200.
   nBurnIn=20,
                     # number of burn-in samples for the Gibbs sampler
   nIter=10,
                     # number of EM iterations
    test.obs=data.test$obs,
                                   # test observation table (optional)
    test.feature=data.test$feature, # test feature matrices (optional)
    reg.algo=NULL,
                     # regression algorithm; see below
```

```
reg.control=NULL, # control parameters for the regression algorithm
IDs=data.test$IDs, # ID mappings (optional)
out.level=1,
                   # see below
out.dir=out.dir,
                 # output directory
out.overwrite=TRUE, # whether to overwrite the output directory
# initialization parameters (the default setting usually works)
var_alpha=1, var_beta=1, var_gamma=1,
var_v=1, var_u=1, var_w=1, var_y=NULL,
relative.to.var_y=FALSE, var_alpha_global=1, var_beta_global=1,
# others
verbose=1,
                # overall verbose level: larger -> more messages
verbose.M=2,
               # verbose level of the M-step
rnd.seed.init=0, rnd.seed.fit=1 # random seeds
```

Most input parameters to run.multicontext are described in the above code piece. We make the following additional notes:

- nSamples, nBurnIn and nIter determine how long the procedure will run. In the above example, the procedure runs 10 EM iterations. In each iteration, it draws 220 Gibbs samples, where the first 20 samples are burnin samples (which are thrown away) and the rest 200 samples are used to compute the Monte Carlo means in the E-step of this iteration. In our experience, 10-20 EM iterations with 100-200 samples per iteration are usually sufficient.
- reg.algo and reg.control specify how the regression priors will to be fitted. If they are set to NULL, R's basic linear regression function 1m will be used to fit the prior regression coefficients g, d, h, G, D and H. Currently, we only support two other algorithms GLMNet and RandomForest. Notice that if RandomForest is used, the regression priors become nonlinear; see [3] for more information.

```
paste(out.dir, "_", setting$name[m], sep="")
```

In this example, the output directories of the two models specified in the setting table are:

```
/tmp/unit-test/simulated-mtx-uvw-10K_uvw1
/tmp/unit-test/simulated-mtx-uvw-10K_uvw2
```

If out.level=1, the fitted models are stored in files model.last and model.minTestLoss in the output directories, where model.last contains the model obtained at the end of the last EM iteration and model.minTestLoss

contains the model at the end of the EM iteration that gives the minimum loss on the test observation. model.minTestLoss exists only when test.obs is not NULL. If the fitting procedure stops (e.g., the machine reboots) before it finishes all the EM iteration, the latest fitted models will still be saved in these two files. If out.level=2, the model at the end of the mth EM iteration will be saved in model.m for each m. We describe how to read the output in Section 2.5.

2.5 Output

The two main output files in an output directory are summary and model.last.

Summary File: It records a number of statistics for each EM iteration. To read a summary file, use the following R command.

```
read.table(paste(out.dir,"_uvw2/summary",sep=""), header=TRUE);
```

Explanation of the columns are in the following:

- Iter specifies the iteration number.
- nSteps records the number of Gibbs samples drawn in the E-step of that iteration.
- CDlogL, TestLoss, LossInTrain and TestRMSE record the complete data log likelihood, loss on the test data, loss on the training data and RMSE (root mean squared error) on the test data for the model at the end of that iteration. For the Gaussian response model, the loss is defined as RMSE. For the logistic response model, the loss is defined as negative average log likelihood per observation.
- TimeEStep, TimeMStep and TimeTest record the numbers of seconds used to compute the E-step, M-step and predictions on test data in that iteration.

Sanity Check:

- Check CDlogL to see whether it increases sharply during the first few iterations and then oscillates at the end.
- Check TestLoss to see whether it converges. If not, more EM iterations are needed.
- Check TestLoss and LossInTrain to see whether the model overfits the data; i.e., TestLoss goes up, while LossInTrain goes down. If so, try to simplify the model by reducing the number of factors and parameters.

You can monitor the summary file when the code is running. When you see TestLoss converges, kill the running process.

Model File: The fitted models are saved in model.last and model.minTestLoss, which are R data binary files. To load the models, run the following command.

```
load(paste(out.dir,"_uvw2/model.last",sep=""));
```

After loading, the fitted prior parameters are in object param and the fitted latent factors are in object factor. Also, the object IDs contains the ID mappings described in Step 2 of Section 2.4.

2.6 Prediction

To make predictions, use the following function.

```
pred = predict.multicontext(
    model=list(factor=factor, param=param),
    obs=data.test$obs, feature=data.test$feature, is.logistic=FALSE
);
```

Now, pred\$pred.y contains the predicted response for data.test\$obs. Notice that the test data data.test was created by call indexTestData in Step 2 of Section 2.4.

2.7 Other Examples

In src/R/examples/tutorial-BST.R, we also provide a number of additional examples.

- Example 2: In this example, we demonstrate how to fit the same models as those in Example 1 with sparse features and the glmnet algorithm.
- Example 3: In this example, we demonstrate how to add more EM iterations to an already fitted model.
- Example 4: In this example, we demonstrate how to fit RLFM models with sparse features and the glmnet algorithm. Note that RLFM models do not fit this toy dataset well.

References

- D. Agarwal and B.-C. Chen. Regression-based latent factor models. In KDD, 2009.
- [2] B.-C. Chen, J. Guo, B. Tseng, and J. Yang. User reputation in a comment rating environment. In KDD, 2011.
- [3] L. Zhang, D. Agarwal, and B. Chen. Generalizing matrix factorization through flexible regression priors. In *RecSys*, 2011.