

Progression

Double derivative $u(x)$, multiply by -1

$$u(x) = 1 - (1 - e^{-10})x - e^{-10x}$$

$$\begin{aligned} u'(x) &= [1]' - [(1 - e^{-10})x]' - [e^{-10x}]' \\ &= - (1 - e^{-10}) - (e^{-10x} \times [-10x]') \\ &= - (1 - e^{-10}) + 10 e^{-10x} \end{aligned}$$

$$\begin{aligned} u''(x) &= [-(1 - e^{-10})]' + [10 e^{-10x}]' \\ &= 10 e^{-10x} \times [-10x]' \\ &= -100 e^{-10x} = -f(x) \end{aligned}$$

Further:

$$f(x) = -u''(x) = -\frac{d^2u}{dx^2} \quad \text{qed.}$$