

$$\sin(2x) = 2 \sin x \cos x$$

$$\cos(2x) = 2 \cos^2 x - 1$$

$$\cos x = 2 \cos^2\left(\frac{1}{2}x\right) - 1$$

$$\sin x = \frac{\sin(2x)}{2 \cos(x)}$$

$$\sqrt{\frac{\cos x + 1}{2}} = \cos \frac{1}{2} x$$

$$\text{ex: } \cos 30^\circ = \frac{\sqrt{3}}{2}$$

$$\cos 15^\circ = \sqrt{\frac{\frac{\sqrt{3}}{2} + 1}{2}} = \sqrt{\frac{\sqrt{3} + 2}{4}} \quad \checkmark$$

$$\boxed{\cos \frac{1}{2} x = \sqrt{\frac{\cos x + 1}{2}}}$$

$$\sin \frac{1}{2} x =$$

$$\sin x = 2 \sin \frac{1}{2}x \cos \frac{1}{2}x$$

$$\Rightarrow \sin \frac{1}{2}x = \frac{\sin x}{2 \cos \frac{1}{2}x} \quad \checkmark$$

$$= \frac{\sin x}{2 \sqrt{\frac{\cos x + 1}{2}}} = \frac{\sin x}{\sqrt{2} \sqrt{(\cos x + 1)}}$$

$$\sin 30^\circ = \frac{1}{2}$$

$$\cos 30^\circ = \frac{\sqrt{3}}{2}$$

$$\sin 15^\circ = \frac{1/2}{\sqrt{2} \sqrt{(\frac{\sqrt{3}}{2} + 1)}} = \frac{0,25}{0,259} \checkmark$$

$$\boxed{\sin \frac{1}{2}x = \frac{\sqrt{2} \sin x}{2 \sqrt{1 + \cos x}}}$$