

Question 1

[20 marks]

- 1 Write a Java program that outputs the 10,001st prime number. Provide comments which explain how the algorithm works.

```
public class Q1 {
    public static void main (String args[]) {
        int count = 0;
        int number = 2;
        // Find the nTH Prime number
        while(count < 10001) {
            if(isPrime(number)) count++;
            number++;
        }
        /* When go out the loop, return the previous number,
        that is the answer */
        number--;
        System.out.println(number);
    }

    //Check whether the number is Prime
    public static boolean isPrime(int number) {
        if (number <= 1) return false;

        for(int i = 2; i < number; i++) {
            if(number % i == 0) return false;
        }

        return true;
    }
}
```

Question 2

[20 marks]

- 2 Write a Java program that uses a stack to check if an inputted String is a palindrome or not (i.e. a word that reads the same forwards as backwards, such as 'radar'). Write the Java Stack class for it to use. Provide comments which explain how the algorithm works.

```
import java.util.Stack;

public class Q2 {
    public static void main (String args[]) {
        System.out.println(isPalindrome("acca"));
        System.out.println(isPalindrome("abc"));
    }

    public static boolean isPalindrome(String input) {
        Stack<Character> stack = new Stack<Character>();
        //Convert String into char Array
        char charArray[] = input.toCharArray();
        //Push each char into the Stack
        for(char c : charArray) stack.push(c);
        //Pop each char out of the Stack and compare
        for(char c : charArray) {
            if(stack.pop() != c) return false;
        }
        return true;
    }
}
```

Question 3

[20 marks]

- 3 Write a Java method that takes in a reference to the head of a single-ended doubly-linked list and deletes every third link, starting with the deletion of the head. Provide comments which explain how the algorithm works.

```
class Node {
    int data;
    Node next;
    Node prev;

    public Node(int data) {
        this.data = data;
        this.next = null;
        this.prev = null;
    }
}

class SingleEndedDoublyLinkedList {
    Node head;

    /* Method to delete every third link in a single-ended
       doubly-linked list */
    public void deleteEveryThirdLink() {
        Node current = head;
        int count = 0;

        while (current != null) {
            count++;

            // Check if the current link is the third one
            if (count % 3 == 0) {
                Node prevNode = current.prev;
                Node nextNode = current.next;

                // Update links to skip the current node
                if (prevNode != null) {
                    prevNode.next = nextNode;
                }
                // If current node is the head, update head
            }
            current = current.next;
        }
    }
}
```

```

    } else {
        head = nextNode;
    }

    if (nextNode != null) {
        nextNode.prev = prevNode;
    }

    // Move to the next node (skip the deleted one)
    current = nextNode;
} else {
    // Move to the next node
    current = current.next;
}
}
}
}

```

Question 4

[20 marks]

- 4 Write a Java method that takes in an array of strings and sorts them, preferably in $O(n \log n)$ time, by length, or alphabetically where strings have the same length. Provide comments which explain how the algorithm works. For example, the set of strings below would be sorted as follows:

```
pear
plum
apple
grape
mango
melon
banana
orange
```

```
import java.util.Scanner;
import java.util.Comparator;
import java.util.LinkedList;
import java.util.Collections;

public class Q4 {
    public static void main (String args[]) {
        Scanner sc = new Scanner (System.in);
        LinkedList<String> list = new LinkedList<String>();

        //Input the String, ends by empty String
        while(true) {
            String inputLine = sc.nextLine();
            if(inputLine.isEmpty()) {
                sc.close();
                break;
            }
            list.add(inputLine);
        }
    }
}
```

```

//The sort method is in O(nlogn) time
Collections.sort(list, new Comparator<String>() {
    @Override
    public int compare(String o1, String o2) {
        // 1 - short String has priority
        if(o1.length() != o2.length()) {
            return o1.length()-o2.length();
        }
        // 2 - Alphabetically
        else {
            return o1.compareTo(o2);
        }
    }
});

//Print out the sorted String
for(String s: list) {
    System.out.println(s);
}

}

}

```

Question 5

[20 marks]

- 5 Write a Java program that uses a Monte Carlo algorithm to calculate the probability that next week's lottery draw won't have any consecutive pairs of numbers. Six numbers are drawn from 1 to 45. Provide comments which explain how the algorithm works.

```
import java.util.Set;
import java.util.TreeSet;

public class Q5 {
    public static void main (String args[]) {
        //Monte Carlo Simulation
        int N = 1000000;
        int count = 0;

        MONTECARLO:
        for(int i = 0; i < N; i++) {
            /* Create a lottery to store 6 numbers drawn from 1 to 45
               drawn from 1 to 45, and sort them! */
            Set<Integer> lottery = new TreeSet<>();
            while(lottery.size() < 6) {
                int draw = (int) (45 * Math.random()) + 1;
                lottery.add(draw);
            }

            //Convert TreeSet to Array
            Integer[] lotteryArray = lottery.toArray(
                new Integer[lottery.size()]);

            //Check whether lottery has consecutive pairs of numbers
            for(int j = 1; j < lotteryArray.length; j++) {
                if(lotteryArray[j] == lotteryArray[j-1] + 1 ) {
                    // If has consecutive pairs of numbers, go to next loop
                    continue MONTECARLO;
                }
            }
            // If does not have consecutive pairs of numbers, count it.
            count++;
        }
    }
}
```

```
// Print out the probability, retain 2 digits
double probability = (double)(100 * count) / (double)N;
System.out.printf("Probability of Lottery: %.2f", probability);

    }
}
```