Data Structures & Algorithms 1 Topic 7 - Stacks and Queues 1

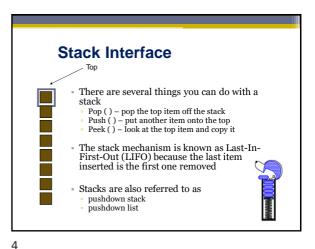
Abstract Data Types (ADTs)

- Stacks and queues are abstract data types they are more conceptual in nature than concrete data types such as arrays
- The ideas of stacks and queues is described by their interface we're not interested in how they're actually implemented
- Underlying mechanism is typically not visible to the user

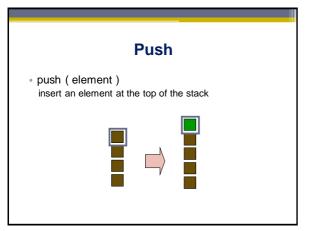
 we just want to know how to use them

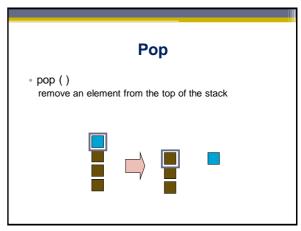
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Other Stack Operations

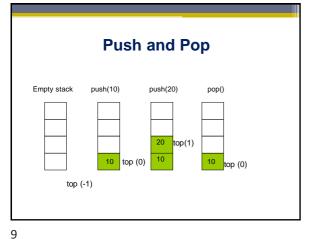
- MakeEmpty()
 - Remove all items from the stack
- IsEmpty()
 - True if stack is empty, false otherwise
- IsFull()
 - True if stack is full, false otherwise

Array-based Stack

- · A simple way of implementing the Stack ADT uses an array
- · We add elements from left to right
- · A variable keeps track of the index of the top element



7



Array-based Stack (cont.)

- · The array storing the stack elements may become full
- A push operation will then throw a FullStackException
 - Limitation of the array-based implementation
 - Not intrinsic to the Stack ADT

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Implementing a Stack

- Stack object will need several instance fields
 - maxSize to store the size of the array
 - an array of numbers stackArray to store the stack
 - a variable called top to track where the top of the stack
- · Constructor will take in size of array, initialize it and set top to -1 since there's nothing in the stack to start with

Java Implementation

```
public class Stack{
  private int maxSize;
                          // size of stack array
  private long[] stackArray;
private int top;
                          // top of stack
public Stack(int s) {
                         // constructor
    // no items yet
    top = -1;
```

11 12

Methods

```
public void push(long j) {
                             // put item on top of stack
       stackArray[top] = j;
                            // increment top, insert item
public long pop() {
                             // take item from top of stack
      return stackArray[top--]; //access item, decrement top
public long peek() {
                             // peek at top of stack
      return stackArray[top];
```

Methods

```
public boolean isEmpty() { // true if stack is empty
    return (top == -1);
public boolean isFull() {
                       // true if stack is full
    return (top == maxSize-1);
top=-1;
```

13 14

Result

Stack theStack = new Stack(10); // make new stack theStack.push(20); // push items onto stack theStack.push(40); theStack.push(60); theStack.push(80); while (!theStack.isEmpty()) { System.out.println(theStack.pop());

• Output would be: 80 60 40 20

Stack Structures

- · In which of the following situations could you feasibly use a stack?
 - Storing fruit
- Storing milk cartonsStoring cans
- Can you think of anything else using a stack structure?
 Web browsers

 - Undo sequence in a text editor
 - Java Virtual Machine

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Method Stack in the JVM

- The Java Virtual Machine (JVM) keeps track of the chain of active methods with a stack
- When a method is called, the JVM pushes on the stack a frame containing
 - Local variables and return value Program counter, keeping track of the statement being executed
- When a method ends, its frame is popped from the stack and control is passed to the method on top of the stack
- main() { foo(int j) {
 - m = 6 foo i = 5k = 6 main

What can we use stacks for?

- The LIFO principle can be used in reversing a word
- If we push "h", "e", "I", "o" and then pop the contents of the stack
- Output is "o", "I", "I", "e", "h"

17 18

Checking for palindromes · The LIFO principle can be used to check if a word is a palindrome · Say we have a word like redder · Push the the word onto the stack е · Pop it off the stack d · It has now been reversed - check if it is the same as the original е

Parentheses Matching

- Each "(", "{", or "[" must be paired with a matching ")", "}", or "["
- Correct: ()(())(([()]))
 correct: ((())(()){([()])})
 incorrect: (([)))
 incorrect: (([]))
 incorrect: (([]))

- Start from the beginning of the sequence
- Opening brackets are placed on a stack
- When the program comes across a closing bracket it pops from the 'opening bracket stack' and this should match
- When the program comes to the end, the 'opening bracket stack' must be empty

19 20

Performance and Limitations

- Performance
- Let n be the number of elements in the stack
- The space used is **O**(**n**)
- Each operation runs in time **O**(1) (e.g. pop, push)
- · Limitations for array-based stacks
 - The maximum size of the stack must be defined a priori and cannot be changed
 - Trying to push a new element into a full stack causes an implementation-specific exception

Queues

· A queue means to line up for something



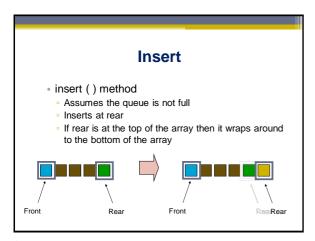
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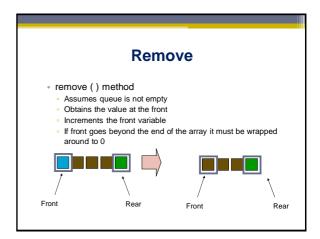
Queues

- · Queues use the First-In-First-Out system (FIFO)
- · Rather than piling items up, the one that has been in the queue the longest is the one that is popped
- · Insertions are made at one end, the back of the queue
- · Deletions take place at the other end, the front of the
- So, the last one added is always the last one available for deletion

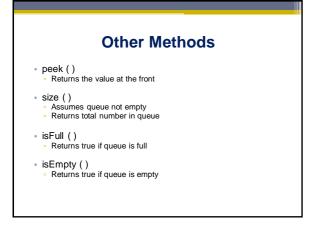
Queues Queues are used everywhere e.g. printer queue, · Push () is called insert, put, add or enqueue! · Pop () is called remove, delete, get or dequeue! The front and back of the queue are called the front and rear Front Rear

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Variables

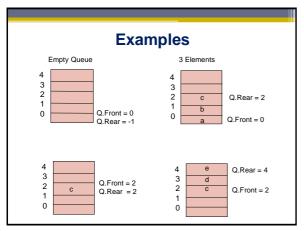
• We need to maintain some variables with our queue class
• Size of the array
• The array itself
• Variables for tracking front and rear

• Empty Queue:
• Front = 0, Rear = -1

• 3 items in queue:
• Front = 0, Rear = 2

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Array-based Queue • Use an array of size N in a circular fashion • Two variables keep track of the front and rear front index of the front element rearindex of the last element normal configuration Q variables variables keep track of the front and rear front index of the front element vearindex of the last element

public class Queue{ private int maxSize; private long[] queArray; private int front; private int rear; private int rear; private int nItems; public Queue(int s) { // constructor maxSize = s; queArray = new long[maxSize]; front = 0; rear = -1; nItems = 0; }

31 32

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```
        Operation insert(5)
        Output front <- Q <- rear (5)</th>

        insert(5)
        - (5)

        insert(3)
        - (5, 3)

        remove()
        5 (3)

        insert(7)
        - (3, 7)

        remove()
        3 (7)

        front()
        7 (7)

        remove()
        7 (7)

        remove()
        "error"
        0

        isEmpty()
        true
        0

        insert(7)
        - (9, 7)
        (9, 7)

        size()
        2 (9, 7)
        (9, 7, 3)

        insert(5)
        - (9, 7, 3, 5)
        (7, 3, 5)

        remove()
        9 (7, 3, 5)
        (7, 3, 5)
```

Performance and Limitations

- Performance
- Let **n** be the number of elements in the queue
- The space used is **O**(**n**)
- Each operation runs in time O(1)
- · Limitations for array-based queues
 - The maximum size of the queue must be defined a priori and cannot be changed
 - Trying to insert a new element into a full queue causes an implementation-specific exception

35 36

Deque

- · A deque is a double-ended queue
- This means you can insert items at either end and delete them at either end
- Essentially, there is no longer a front and rear, simply two ends
- Use methods called
 - insertLeft()
 - insertRight()
 - removeLeft()
 - removeRight()

Deques, Stacks and Queues

- · A stack is actually a deque with only the methods
- insertRight()
- removeRight()
- · A queue is a deque with only the methods
 - insertRight()
 - removeLeft()
- A deque is actually a more versatile data structure than either a stack or a queue but is not used as often

37 38

Priority Queue



- A priority queue is a queue where items don't just join at the rear, they are slotted into the queue according to their priority
- Imagine a stack of mail which are sorted according to priority
 - Each time a new letter is added, you slot it in according to its
 - Every time you pick up a letter to read, you are picking the most important one of the pile

What's Different?

- Don't really need to track front and rear as the rear always stays put at slot 0
- It looks kind of similar to a stack because we only need to track the top - would be better named as a "priority stack"
- We shift elements up to make space rather than just putting the element at the rear
- Insert method has a for loop that shifts elements up
- Remove method simply removes the top (highest priority) element

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Priority Queue Insert ()

Priority Queue

- Insertion is O(n) while deletion is O(1)
- What output do we get following from the following (assuming lower numbers have highest priority?)

```
PQ thePQ = new PQ(10); // make new priority queue
thePQ.insert(60); // slot items into queue
thePQ.insert(20);
thePQ.insert(80);
thePQ.insert(40);
while (!thePQ.isEmpty()) {
    System.out.println(thePQ.remove());
}
20     40     60     80
```

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