MATHEMATICS FORM ONE NOTES



CHAPTER ONE

Specific Objectives

By the end of the topic the learner should be able to:

- a.) Identify, read and write natural numbers in symbols and words;
- b.) Round off numbers to the nearest tens, hundreds, thousands, millions and billions;
- c.) Classify natural numbers as even, odd or prime;
- d.) Solve word problems involving natural numbers.

Content

- a.) Place values of numbers
- b.) Rounding off numbers to the nearest tens, hundreds, thousands, millions and billions
- c.) Odd numbers
- d.) Even numbers
- e.) Prime numbers
- f.) Word problems involving natural numbers

Introduction

Place value

A digit have a different value in a number because of its position in a number. The position of a digit in a number is called its place value.

Total value

This is the product of the digit and its place value.

Example

Number	Hundred Millions	Ten Millions	Millions	Hundred Thousands	Ten Thousands	Thousands	Hundred	Tens	ones
345,678,901	3	4	5	6	7	8	9	0	1
769,301,854	7	6	9	3	0	1	8	5	4
902,350,409	9	0	2	3	5	0	4	0	9

A place value chart can be used to identify both place value and total value of a digit in a number. The place value chart is also used in writing numbers in words.

Example

- ✓ Three hundred and forty five million, six hundred and seventy eight thousand, nine hundred and one.
- ✓ Seven hundred and sixty nine million, Three hundred and one thousand, eight hundred and fifty four

Billions

A billion is one thousands million, written as 1, 000, 000,000. There are ten places in a billion.

Example

What is the place value and total value of the digits below?

- a.) 47,397,263,402 (place value 7 and 8).
- b.) 389,410,000,245 (place 3 and 9)

Solution

- a.) The place value for 6 is ten thousands. Its total value is 60,000.
- b.) The place value of 3 is hundred billions. Its total value is 300,000,000,000.

Rounding off

When rounding off to the nearest ten, the ones digit determines the ten i.e. if the ones digit is 1, 2, 3, or 4 the nearest ten is the ten number being considered. If the ones digit is 5 or more the nearest ten is the next ten or rounded up.

Thus 641 to the nearest ten is 640, 3189 to the nearest is 3190.

When rounding off to the nearest 100, then the last two digits or numbers end with 1 to 49 round off downwards. Number ending with 50 to 99 are rounded up.

Thus 641 to the nearest hundred is 600, 3189 is 3200.

Example

Rounding off each of the following numbers to the nearest number indicated in the bracket:

- a.) 473,678 (100)
- b.) 524,239 (1000)
- c.) 2,499 (10)

Solution

- a.) 473,678 is 473,700 to the nearest 100.
- b.) 524,239 is 524,000 to the nearest 1000
- c.) 2,499 is 2500 to the nearest 10.

Operations on whole Numbers

Addition

Example

Find out:

```
a.) 98 + 6734 + 348b.) 6349 + 259 +7954
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Solution

Arrange the numbers in vertical forms

98

6734

+ 348

7180

6349

259

+ 79542

86150

Subtracting

Example

Find: 73469 – 8971

Solution

73469

- <u>8971</u> _64498

Multiplication

The product is the result of two or more numbers.

Example

Work out: 469 x 63

Solution

469

29547

Division

When a number is divided by the result is called the quotient. The number being divided is the divided and the number dividing is the divisor.

Example

Find: 6493 ÷ 14

Solution

We get 463 and 11 is the remainder

Note:

$$6493 = (463 \times 14) + 11$$

In general, dividend = quotient x division + remainder.

Operation	Words	
Addition	sum plus added more increased by	han
Subtraction		rom han by by
Multiplication	product multiply times twice thrice	of

Division	quotient of divided by
	equal to result is
1	result is

Word problem

In working the word problems, the information given must be read and understood well before attempting the question.

The problem should be broken down into steps and identify each other operations required.

Example

Otego had 3469 bags of maize, each weighing 90 kg. He sold 2654 of them.

- a.) How many kilogram of maize was he left with?
- b.) If he added 468 more bags of maize, how many bags did he end up with?

Solution

```
a.) One bag weighs 90 kg. 3469 bags weigh 3469 x 90 = 312,210 kg
2654 bags weigh 2654 x 90 = 238,860 kg
Amount of maize left = 312,210 - 238,860 = 73,350 kg.
b.) Number of bags = 815 + 468
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=1283

Even Number

A number which can be divided by 2 without a remainder E.g. 0,2,4,6 0 or 8

3600, 7800, 806, 78346

Odd Number

Any number that when divided by 2 gives a remainder. E.g. 471,123, 1197,7129. The numbers ends with the following digits 1, 3, 5,7 or 9.

Prime Number

A prime number is a number that has only two factors one and the number itself.

For example, 2, 3, 5, 7, 11, 13, 17 and 19.

Note:

- i.) 1 is not a prime number.
- ii.) 2 is the only even number which is a prime number.

End of topic

Did you understand everything?

If not ask a teacher, friends or anybody and make sure you understand before going to sleep!

Past KCSE Questions on the topic

- 1.) Write 27707807 in words
- 2.) All prime numbers less than ten are arranged in descending order to form a number
- a.) Write down the number formed
- b.) What is the total value of the second digit?
- c.) Write the number formed in words.

CHAPTER TWO

FACTORS

Specific Objectives

By the end of the topic the learner should be able to:

- a.) Express composite numbers in factor form;
- b.) Express composite numbers as product of prime factors;
- c.) Express factors in power form.

Content

- a.) Factors of composite numbers.
- b.) Prime factors.
- c.) Factors in power form
- d.)

Introduction

Definition

A factor is a number that divides another number without a remainder.

Number	Factors
12	1,2,3,4,6,12
16	1,2,4,8,16
39	1 ,3,13,39

A natural number with only two factors, one and itself is a prime number. Or any number that only can be divided by 1 and itself. Prime numbers have exactly $\underline{2}$ different factors.

Prime Numbers up to 100.

2	3	5	7	11
13	17	19	23	29
31	37	41	43	47
53	59	61	67	71
73	79	83	89	97

Composite numbers

Any number that has more factors than just itself and 1. They can be said to be natural number other than 1 which are not prime numbers. They can be expressed as a product of two or more prime factors.

$$9 = 3 \times 3$$

$$12 = 2 \times 2 \times 3$$

$$105 = 3 \times 5 \times 7$$

The same number can be repeated several times in some situations.

$$32 = 2 \times 2 \times 2 \times 2 \times 2 = 2^5$$

$$72 = 2 \times 2 \times 2 \times 3 \times 3 = 2^3 \times 3^2$$

To express a number in terms of prime factors, it is best to take the numbers from the smallest and divide by each of them as many times as possible before going to the next.

Example

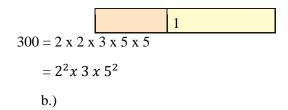
Express the following numbers in terms of their prime factors

- a.) 300
- b.) 196

Solution

a.)

2	300
2	150
3	75
5	25
5	5



2	196
2	98
7	49
7	7
	1

$$196 = 2 \times 2 \times 7 \times 7$$
$$= 2^{2} \times 7^{2}$$

Exceptions

The numbers 1 and 0 are neither prime nor composite. 1 cannot be prime or composite because it only has one factor, itself. 0 is neither a prime nor a composite number because it has infinite factors. All other numbers, whether prime or composite, have a set number of factors. 0 does not follow the rules.

End of topic

Did you understand everything?

If not ask a teacher, friends or anybody and make sure you understand before going to sleep!

Past KCSE Questions on the topic

1.) Express the numbers 1470 and 7056, each as a product of its prime factors. Hence evaluate: 1470^2

$$\sqrt{7056}$$

Leaving the answer in prime factor form

- 2.) All prime numbers less than ten are arranged in descending order to form a number
 - (a) Write down the number formed
 - (b) What is the total value of the second digit?



Specific Objectives

By the end of the topic the learner should be able to:

The learner should be able to test the divisibility of numbers by 2, 3, 4, 5, 6, 8, 9, 10 and 11.

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Content

Divisibility test of numbers by 2, 3, 4, 5, 6, 8, 9, 10 and 11

Introduction

Divisibility test makes computation on numbers easier. The following is a table for divisibility test.

Divisibility Tests	Example
A number is divisible by 2 if the last digit is 0, 2, 4, 6 or 8.	168 is divisible by 2 since the last digit is 8.
A number is divisible by 3 if the sum of the digits is divisible by 3.	168 is divisible by 3 since the sum of the digits is 15 (1+6+8=15), and 15 is divisible by 3.
A number is divisible by 4 if the number formed by the last two digits is divisible by 4.	316 is divisible by 4 since 16 is divisible by 4.
A number is divisible by 5 if the last digit is either 0 or 5.	195 is divisible by 5 since the last digit is 5.
A number is divisible by 6 if it is divisible by 2 AND it is divisible by 3.	168 is divisible by 6 since it is divisible by 2 AND it is divisible by 3.

A number is divisible by 8 if the number formed by the last three digits is divisible by 8.	7,120 is divisible by 8 since 120 is divisible by 8.
A number is divisible by 9 if the sum of the digits is divisible by 9.	549 is divisible by 9 since the sum of the digits is 18 (5+4+9=18), and 18 is divisible by 9.
A number is divisible by 10 if the last digit is 0.	1,470 is divisible by 10 since the last digit is 0.
A number is divisible by 11 if the sum of its digits in the odd positons like 1 st , 3 rd , 5 th , 7 th Positions, and the sum of its digits in the even position like 2 nd , 4 th , 6 th , 8 th positions are equal or differ by 11, or by a multiple of 11	2+0+3=5;

End of topic

Did you understand everything?

If not ask a teacher, friends or anybody and make sure you understand before going to sleep!

Past KCSE Questions on the topic

CHAPTER FOUR

GREATEST COMMON DIVISOR

Specific Objectives

By the end of the topic the learner should be able to:

- a.) Find the GCD/HCF of a set of numbers.
- b.) Apply GCD to real life situations.

Content

- a.) GCD of a set of numbers
- b.) Application of GCD/HCF to real life situations

Introduction

A Greatest Common Divisor is the largest number that is a factor of two or more numbers.

When looking for the Greatest Common Factor, you are only looking for the COMMON factors contained in both numbers. To find the G.C.D of two or more numbers, you first list the factors of the given numbers, identify common factors and state the greatest among them.

The G.C.D can also be obtained by first expressing each number as a product of its prime factors. The factors which are common are determined and their product obtained.

Example

Find the Greatest Common Factor/GCD for 36 and 54 is 18.

Solution

The prime factorization for 36 is 2 x 2 x 3 x 3.

The prime factorization for 54 is 2 x 3 x 3 x 3.

They both have in common the factors 2, 3, 3 and their product is 18.

That is why the greatest common factor for 36 and 54 is 18.

Example

Find the G.C.D of 72, 96, and 300

Solution

I	72	96	300
2	36	48	150
2	18	24	75



End of topic

Did you understand everything?

If not ask a teacher, friends or anybody and make sure you understand before going to sleep!

Past KCSE Questions on the topic

- 1.) Find the greatest common divisor of the term. $144x^3y^2$ and $81xy^4$ b) Hence factorize completely this expression $144x^3y^2-81xy^4$ (2 marks)
- **2.)** The GCD of two numbers is 7and their LCM is 140. if one of the numbers is 20, find the other number
- **3.)** The LCM of three numbers is 7920 and their GCD is 12. Two of the numbers are 48 and 264. Using factor notation find the third number if one of its factors is 9

CHAPTER FIVE

LEAST COMMON MULTIPLE

Specific Objectives

By the end of the topic the learner should be able to:

- a.) List multiples of numbers.
- b.) Find the L CM of a set of numbers.
- c.) Apply knowledge of L CM in real life situations.

Content

- a.) Multiples of a number
- b.) L CM of a set of numbers
- c.) Application of L CM in real life situations.

Introduction

Definition

LCM or LCF is the smallest multiple that two or more numbers divide into evenly i.e. without a remainder. A multiple of a number is the product of the original number with another number.

Some multiples of 4 are 4, 8, 12, 16, 20, 24, 28, 32, 36, 40, 44, 48, 52, 56 ...

Some multiples of 7 are 7, 14, 21, 28, 35, 42, 49, 56 ...

A Common Multiple is a number that is divisible by two or more numbers. Some common multiples of 4 and 7 are 28, 56, 84, and 112.

When looking for the Least Common Multiple, you are looking for the smallest multiple that they both divide into evenly. The least common multiple of 4 and 7 is 28.

Example

Find the L.C.M of 8, 12, 18 and 20.(using tables)

Solution

		8	18	20
	2	4	6	10
l	2	2	3	5
	2	1	3	5

3	1	1	5
3	1	1	5
5	1	1	1

The L.C.M is the product of all the divisions used.

Therefore, L.C.M. of 8, 12, 18 and
$$20 = 2 \times 2 \times 2 \times 3 \times 3 \times 5$$

$$= 2^3 x 3^2 x 5$$

= 360

Note:

Unlike the G.C.D tables, if the divisor /factor does not divide a number exactly, then the number is retained, e.g., 2 does not divide 9 exactly, therefore 9 is retained. The last row must have all values 1.

End of topic

Did you understand everything?

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Past KCSE Questions on the topic

- **4.)** Find the L.C.M of $x^2 + x$, $x^2 1$ and $x^2 x$.
- **5.)** Find the least number of sweets that can be packed into polythene bags which contain either 9 or 15 or 20 or 24 sweets with none left over.
- **6.)** A number n is such that when it is divided by 27, 30, or 45, the remainder is always 3. Find the smallest value of n.
- 7.) A piece of land is to be divided into 20 acres or 24 acres or 28 acres for farming and Leave 7 acres for grazing. Determine the smallest size of such land.
- **8.)** When a certain number x is divided by 30, 45 or 54, there is always a remainder of 21. Find the least value of the number x.

A number **m** is such that when it is divided by 30, 36, and 45, the remainder is always 7. Find the smallest possible value of **m**.



Specific Objectives

By the end of the topic the learner should be able to:

- a.) Define integers
- b.) Identify integers on a number line
- c.) Perform the four basic operations on integers using the number line.
- d.) Work out combined operations on integers in the correct order
- e.) Apply knowledge of integers to real life situations.

Content

- a.) Integers
- b.) The number line
- c.) Operation on integers
- d.) Order of operations
- e.) Application to real life situations

Introduction

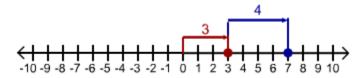
The Number Line

Integers are whole numbers, negative whole numbers and zero. Integers are always represented on the number line at equal intervals which are equal to one unit.

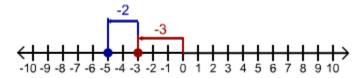
Operations on Integers Addition of Integers

Addition of integers can be represented on a number line .For example, to add

+3 to 0, we begin at 0 and move 3 units to the right as shown below in red to get +3, Also to add +4 to +3 we move 4 units to the right as shown in blue to get +7.



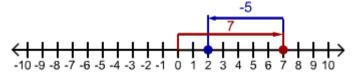
To add -3 to zero we move 3 units to the left as shown in red below to get -3 while to add -2 to -3 we move 2 steps to the left as shown in blue to get -5.



Note:

- ✓ When adding positive numbers we move to the right.
- ✓ When dealing with negative we move to the left.

Subtraction of integers.



Example

$$(+7) - (0) = (+7)$$

To subtract +7 from 0 ,we find a number n which when added to get 0 we get +7 and in this case n = +7 as shown above in red.

Example

$$(+2) - (+7) = (-5)$$

Start at +7 and move to +2. 5 steps will be made towards the left. The answer is therefore -5.

Example

$$-3 - (+6) = -9$$



We start at +6 and moves to -3. 9 steps to the left, the answer is -9.

Note:

✓ In general positives signs can be ignored when writing positive numbers i.e. +2 can be written as 2 but negative signs cannot be ignored when writing negative numbers -4 can only be written s -4.

$$4 - (+3) = 4 - 3$$

= 1

$$-3-(+6)=3-6$$

= -3

✓ Positive integers are also referred to as natural numbers. The result of subtracting the negative of a number is the same as adding that number.

$$2 - (-4) = 2 + 4$$

$$= 6$$

$$(-5) - (-1) = -5 + 2$$

$$= -3$$

✓ In mathematics it is assumed that that the number with no sign before it has appositive sign.

Multiplication

In general

- i.) (a negative number) x (appositive number) = (a negative number)
- ii.) (a positive number) x (a negative number) = (a negative number)
- iii.) (a negative number) x (a negative number) = (a positive number)

Examples

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-6 \times 5 = -30
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$$7 \times -4 = -28$$

$$-3 \times -3 = 9$$

$$-2 \times -9 = 18$$

Division

Division is the inverse of multiplication. In general

- i.) (a positive number) \div (a positive number) = (a positive number)
- ii.) (a positive number) \div (a negative number) = (a negative number)
- iii.) (a negative number) ÷ (a negative number) = (a positive number)
- iv.) (a negative number) \div (appositive number) = (a negative number)

Note:

For multiplication and division of integer:

- ✓ Two like signs gives positive sign.
- ✓ Two unlike signs gives negative sign
- ✓ Multiplication by zero is always zero and division by zero is always zero.

Order of operations

BODMAS is always used to show as the order of operations.

- B Bracket first.
- O Of is second.
- D Division is third.
- M Multiplication is fourth.
- A Addition is fifth.
- S Subtraction is considered last.

Example

$$6 \times 3 - 4 \div 2 + 5 + (2 - 1) =$$

Solution

Use **BODMAS**

(2-1) = 1 we solve brackets first

 $(4 \div 2) = 2$ we then solve division

 $(6 \times 3) = 18$ next is multiplication

Bring them together

18 - 2 + 5 + 1 = 22 we solve addition first and lastly subtraction

18 + 6 - 2 = 22

End of topic

Did you understand everything?

If not ask a teacher, friends or anybody and make sure you understand before going to sleep!

Past KCSE Questions on the topic

- 1.) The sum of two numbers exceeds their product by one. Their difference is equal to their product less five. Find the two numbers. (3mks)
- 2.) 3x 1 > -4

$$2x + 1 \le 7$$

3.) Evaluate $\frac{-12 \div (-3) \times 4 - (-15)}{}$

$$-5 \times 6 \div 2 + (-5)$$

4.) Without using a calculator/mathematical tables, evaluate leaving your answer as a simple fraction

$$(-4)(-2) + (-12) \div (+3) + -20 + (+4) + -6)$$

-9 - (15) 46- (8+2)-3

5.) Evaluate $-8 \div 2 + 12 \times 9 - 4 \times 6$

56 ÷7 x 2

6.) Evaluate without using mathematical tables or the calculator 1.9×0.032

20 x 0.0038

CHAPTER SEVEN



Specific Objectives

By the end of the topic the learner should be able to:

- a.) Identify proper and improper fractions and mixed number.
- b.) Convert mixed numbers to improper fractions and vice versa.
- c.) Compare fractions;
- d.) Perform the four basic operations on fractions.
- e.) Carry out combined operations on fractions in the correct order.
- f.) Apply the knowledge of fractions to real life situations.
- g.)

Content

- a.) Fractions
- b.) Proper, improper fractions and mixed numbers.
- c.) Conversion of improper fractions to mixed numbers and vice versa.
- d.) Comparing fractions.
- e.) Operations on fractions.
- f.) Order of operations on fractions
- g.) Word problems involving fractions in real life situations.

Introduction

A fraction is written in the form $\frac{a}{b}$ where a and b are numbers and b is not equal to 0. The upper number is called the numerator and the lower number is the denominator.

$$\frac{a \to numerator}{b \to denominator}$$

Proper fraction

In proper fraction the numerator is smaller than the denominator. E.g.

$$\frac{2}{3}$$
, $\frac{1}{4}$

Improper fraction

The numerator is bigger than or equal to denominator. E.g.

$$\frac{7}{3}$$
, $\frac{15}{6}$, $\frac{9}{2}$

Mixed fraction

An improper fraction written as the sum of an integer and a proper fraction. For example

$$\frac{7}{3} = 2 + \frac{1}{3}$$
$$= 2\frac{1}{3}$$

Changing a Mixed Number to an Improper Fraction

Mixed number – $4\frac{2}{3}$ (contains a whole number and a fraction)

Improper fraction - $\frac{14}{3}$ (numerator is larger than denominator)

Step 1 – Multiply the denominator and the whole number

Step 2 – Add this answer to the numerator; this becomes the new numerator

Step 3 – Carry the original denominator over

Example

$$3\frac{1}{8} = 3 \times 8 + 1 = 25$$

$$=\frac{25}{8}$$

Example

$$4 \quad \frac{4}{9} = 4 \times 9 + 4 = 40$$

$$=\frac{40}{9}$$

Changing an Improper Fraction to a Mixed Number

Step 1– Divide the numerator by the denominator

Step 2– The answer from step 1 becomes the whole number

Step 3– The remainder becomes the new numerator

Step 4— The original denominator carries over

Example

$$\frac{47}{5} = 47 \div 5 \quad \text{or}$$

$$5)47 = 5)47 = 9\frac{2}{5}$$

2

Example

$$\frac{9}{2} = 2 \overline{\smash{\big)}\!9} = 2 \overline{\smash{\big)}\!9} = 4 \frac{1}{2}$$

Comparing Fractions

When comparing fractions, they are first converted into their equivalent forms using the same denominator.

Equivalent Fractions

To get the equivalent fractions, we multiply or divide the numerator and denominator of a given fraction by the same number. When the fraction has no factor in common other than 1, the fraction is said to be in its simplest form.

Example

Arrange the following fractions in ascending order (from the smallest to the biggest):

1/2 1/4 5/6 2/3

Step 1: Change all the fractions to the same denominator.

Step 2: In this case we will use 12 because 2, 4, 6, and 3 all go into i.e. We get 12 by finding the L.C.M of the denominators. To get the equivalent fractions divide the denominator by the L.C.M and then multiply both the numerator and denominator by the answer,

For $\frac{1}{2}$ we divide $12 \div 2 = 6$, then multiply both the numerator and denominator by 6 as shown below.

Step3: The fractions will now be:

Step 4: Now put your fractions in order (smallest to biggest.)

Step 5: Change back, keeping them in order.

You can also use percentages to compare fractions as shown below.

Example

Arrange the following in descending order (from the biggest)

Solution

$$\frac{5}{12}$$
 X 100 = 41.67%

$$\frac{7}{3}$$
 X 100 = 233.3%

$$\frac{11}{5}$$
 X 100 = 220%

$$\frac{9}{4}$$
 X 100 = 225%

Operation on Fractions

Addition and Subtraction

The numerators of fractions whose denominators are equal can be added or subtracted directly.

Example

$$2/7 + 3/7 = 5/7$$

$$6/8 - 5/8 = 1/8$$

When adding or subtracting numbers with different denominators like:

$$5/4 + 3/6 = ?$$

$$2/5 - 2/7 = ?$$

Step 1- Find a common denominator (a number that both denominators will go into or L.C.M)

Step 2– Divide the denominator of each fraction by the common denominator or L.C.M and then multiply the answers by the numerator of each fraction

Step 3– Add or subtract the numerators as indicated by the operation sign

Step 4 – Change the answer to lowest terms

Example

$$\frac{1}{2} + \frac{7}{8}$$
 = Common denominator is 8 because both 2 and 8 will go into 8

$$\frac{1}{2} + \frac{7}{8} = \frac{4+7}{8}$$

$$\frac{11}{8}$$
 Which simplifies to $1\frac{3}{8}$

Example

$$4\frac{3}{5} - \frac{1}{4} =$$
 Common denominator is 20 because both 4 and 5 will go into 20

$$4\frac{3}{5} = 4\frac{12}{20}$$
$$-\frac{1}{4} = \frac{5}{20}$$
$$4\frac{7}{20}$$

Or

$$4\frac{3}{5} - \frac{1}{4} = 4\frac{12-5}{20} = 4\frac{7}{20}$$

Mixed numbers can be added or subtracted easily by first expressing them as improper fractions.

Examples

$$5\frac{2}{3}+1\frac{4}{5}$$

Solution

$$5\frac{2}{3} + 1\frac{4}{5} = 5 + \frac{2}{3} + 1 + \frac{4}{5}$$

$$= (5+1) + \frac{2}{3} + \frac{4}{5}$$

$$=6+\frac{10+12}{15}$$

$$= 6 + \frac{22}{15}$$
$$= 6 + 1\frac{7}{15} = 7\frac{7}{15}$$

Example

Evaluate
$$\frac{-2}{3} + \frac{-1}{5}$$

Solution

$$\frac{-2}{3} + \frac{-1}{5} = \frac{-16 - 3}{24} = \frac{-19}{24}$$

Multiplying Simple Fractions

Step 1– Multiply the numerators

Step 2– Multiply the denominators

Step 3– Reduce the answer to lowest terms by dividing by common divisors

Example

$$\frac{1}{7} \times \frac{4}{6} = \frac{4}{42}$$
 which reduces to $\frac{2}{21}$

Multiplying Mixed Numbers

Step 1– Convert the mixed numbers to improper fractions first

Step 2— Multiply the numerators

Step 3– Multiply the denominators

Step 4– Reduce the answer to lowest terms

Example

$$2\frac{1}{3} \times 1\frac{1}{2} = \frac{7}{3} \times \frac{3}{2} = \frac{21}{6}$$

Which then reduces to $3\frac{1}{2}$

Note:

When opposing numerators and denominators are divisible by a common number, you may reduce the numerator and denominator before multiplying. In the above example, after converting the mixed numbers to improper fractions, you will see that the 3 in the numerator and the opposing 3 in the denominator could have been reduced by dividing both numbers by 3, resulting in the following reduced fraction:

$$\frac{7}{18} \times \frac{31}{2} = \frac{7}{2} = 3\frac{1}{2}$$

Dividing Simple Fractions

Step 1– Change division sign to multiplication

Step 2– Change the fraction following the multiplication sign to its reciprocal (rotate the fraction around so the old denominator is the new numerator and the old numerator is the new denominator)

Step 3- Multiply the numerators

Step 4- Multiply the denominators

Step 5– simplify the answer to lowest terms

Example

$$\frac{1}{8} \div \frac{2}{3}$$
 = becomes $\frac{1}{8} \times \frac{3}{2}$ which when solved is $\frac{3}{16}$

Dividing Mixed Numbers

Step 1 – Convert the mixed number or numbers to improper fraction.

Step 2 – Change the division sign to multiplication.

Step 3– Change the fraction following the multiplication sign to its reciprocal (flip the fraction around so the old denominator is the new numerator and the old numerator is the new denominator)

Step 4- Multiply the numerators.

Step 5– Multiply the denominators.

Step 6– Simplify the answer to lowest form.

Example

$$3\frac{3}{4} \div 2\frac{5}{6} = \text{ becomes } \frac{15}{4} \div \frac{17}{6} \text{ becomes } \frac{15}{4} \times \frac{6}{17} =$$

Which when solved is
$$\frac{15}{24} \times \frac{63}{17} = \frac{45}{34}$$
 which simplifies to $1\frac{11}{34}$

Order of operations on Fractions

The same rules that apply on integers are the same for fractions

BODMAS

Example

$$15 \div \frac{1}{4}$$
 of $12 = 15 \div \left(\frac{1}{4} \times 12\right)$ (we start with of then division)
= $15 \div 3$

$$=5$$

Example

$$\frac{1}{6} + \frac{1}{2} x \left\{ \frac{3}{8} + \left(\frac{1}{3} - \frac{1}{4} \right) \right\} =$$

Solution

$$1/3 - 1/4 = \frac{4-1}{12} = \frac{1}{12}$$
 (we start with bracket)

$$\left\{\frac{3}{8} + \frac{1}{12}\right\} = \frac{11}{21}$$
 (We then work out the outer bracket)

$$\frac{1}{6} + \frac{1}{2} \times \frac{11}{48} = \frac{1}{6} + \frac{11}{48}$$
 (We then work out the multiplication)

$$\frac{1}{6} + \frac{11}{48} = \frac{19}{48}$$
 (Addition comes last here)

Example

Evaluate
$$\frac{\frac{1}{2} + \frac{1}{3}}{\frac{1}{7} of(\frac{2}{5} - \frac{1}{6})} + \frac{1}{2}$$

Solution

We first work out this first
$$\frac{\frac{1}{2} + \frac{1}{3}}{\frac{1}{7} of \left(\frac{2}{5} - \frac{1}{6}\right)}$$

$$\frac{1}{2} + \frac{1}{3} = \frac{3+2}{6} = \frac{5}{6}$$

$$\frac{1}{7} \text{ of } \left(\frac{2}{5} - \frac{1}{6}\right) = \frac{1}{7} x \frac{7}{30} = \frac{1}{30}$$

$$\frac{5}{6} \times 30 = 25$$

Therefore
$$\frac{\frac{1}{2} + \frac{1}{3}}{\frac{1}{7} of \left(\frac{2}{5} - \frac{1}{6}\right)} + \frac{1}{2} = 25 + \frac{1}{2}$$

$$= 25 \frac{1}{2}$$

Note:

Operations on fractions are performed in the following order.

- ✓ Perform the operation enclosed within the bracket first.
- ✓ If (of) appears, perform that operation before any other.

Example

Evaluate:
$$\frac{1}{2} \left\{ \frac{3}{5} + \frac{1}{4} \left(\frac{7}{3} - \frac{3}{7} \right) \text{ of } 1 \frac{1}{2} \div 5 \right\} =$$

Solution

=

$$\frac{1}{2} \left\{ \frac{3}{5} + \frac{1}{4} \left(\frac{40}{21} \right) \text{ of } 1\frac{1}{2} \div 5 \right\}$$
$$= \frac{1}{2} \left\{ \frac{3}{5} + \frac{1}{4} x \frac{40}{21} x \frac{3}{2} \div 5 \right\}$$

$$= \frac{1}{2} \left(\frac{3}{5} + \frac{10}{21} x \frac{3}{2} \div 5 \right)$$

$$= \frac{1}{2} \left(\frac{3}{5} + \frac{5}{35} \right)$$

$$= \frac{1}{2} \left(\frac{21+5}{35} \right) = \frac{1}{2} x \frac{26}{35} = \frac{13}{35}$$

Example

Two pipes **A** and **B** can fill an empty tank in 3hrs and 5hrs respectively. Pipe **C** can empty the tank in 4hrs. If the three pipes **A**, **B** and **C** are opened at the same time find how long it will take for the tank to be full.

Solution

$$1/3 + 1/5 - 1/4 = \underline{20 + 12 - 15}$$

$$60$$

$$= 17/60$$

$$17/60 = 1 \text{hr}$$

$$1 = 1 \times 60/17$$

$$60/17 = 3.5294118$$

$$= 3.529 \text{ hrs.}$$

End of topic

Did you understand everything?

If not ask a teacher, friends or anybody and make sure you understand before going to sleep!

Past KCSE Questions on the topic

1. Evaluate without using a calculator.

$$\frac{\left(1\frac{3}{7} - \frac{5}{8}\right) \times \frac{2}{3}}{\frac{3}{4} + 1\frac{5}{7} \div \frac{4}{7} \text{ of } 2\frac{1}{3}}$$

2. A two digit number is such that the sum of the ones and the tens digit is ten. If the digits are reversed, the new number formed exceeds the original number by 54.

Find the number.

3. Evaluate
$$\frac{3}{8}$$
 of $\left\{7\frac{3}{5} - \frac{1}{3}\left(1\frac{1}{4} + 3\frac{1}{3}\right) \times 2\frac{2}{5}\right\}$

- 4. Convert the recurring decimal 12.18 into fraction
- 5. Simplify $(0.00243)^{-\frac{2}{5}} \times (0.0009)^{\frac{1}{2}}$ without using tables or calculator
- 6. Evaluate without using tables or calculators

$$\frac{6}{7} of \frac{14}{3} \div 80 \times -\frac{20}{3} \\ -2 \times 5 + (14 \div 7) \times 3$$

- 7. Mr. Saidi keeps turkeys and chickens. The number of turkeys exceeds the number of chickens by 6. During an outbreak of a disease, ½ of the chicken and ½ of the turkeys died. If he lost total of 30 birds, how many birds did he have altogether?
- 9. Work out $\frac{8 \div 2 + 12 \times 9 4 \times 6}{56 \div 7 \times 2}$

10. Evaluate
$$-4 \text{ of } (-4 + -5 \div 15) + -3 - 4 \div 2)$$

$$84 \div -7 + 3 - -5$$

11. Write the recurring decimal 0.3 Can as Fraction

12. Evaluate
$$\frac{\frac{5}{6}of\left(4\frac{1}{3} - 3\frac{5}{6}\right)}{\frac{5}{12} \times \frac{3}{25} + 1\frac{5}{9} \div 2\frac{1}{3}}$$
 without using a calculator.

13. Without using tables or calculators evaluate.

$$\frac{35 \div 5 + 2 \times -3}{-9 + 14 \div 7 + 4}$$

14. Without using tables or calculator, evaluate the following.

$$\frac{-8 + (-13) \times 3 - (-5)}{}$$

$$^{-}1 + (^{-}6) \div 2 \times 2$$

15. Express
$$1.93 + 0.25$$
 as a single fraction

16. Simplify
$$\frac{\frac{1}{2} \text{ of } 3\frac{1}{2} + \frac{1}{2} (2\frac{1}{2} - \frac{2}{3})}{\frac{3}{4} \text{ of } 2\frac{1}{2} \div \frac{1}{2}}$$

17. Evaluate:

$$\frac{^{2}/_{5} \div \frac{1}{2} \text{ of } ^{4/_{9}} - 1^{1}/_{10}}{^{1}/_{8} - ^{1}/_{6} \text{ of } 3/_{8}}$$

18. Without using a calculator or table, work out the following leaving the answer as a mixed number in its simplest form:-

$$\frac{{}^{3/4} + 1^{2/7} \div {}^{3/7} \text{ of } 2^{1/3}}{(9/7^{-3}/8) \text{ x }^{2/3}}$$

19. Work out the following, giving the answer as a mixed number in its simplest form.

$$\frac{\frac{2}{5} \div \frac{1}{2} \text{ of } 4/9 - 1^{-1}/10}{\frac{1}{8} - \frac{1}{16} \times \frac{3}{8}}$$

20. Evaluate;

$$^{3}/_{8}$$
 of $\left(7^{3}/_{5} - ^{1}/_{3} \, 1\% + 3^{1}/_{3} \times 2^{2}\right)_{5}$

23. Without using a calculator, evaluate:

$$\frac{1^4/_5 \text{ of } 25/_{18} \div 1^2/_3 \times 24}{2^1/_3 - \frac{1}{4} \text{ of } 12 \div \frac{5}{3}}$$
 leaving the answer as a fraction in its simplest form

24. There was a fund-raising in Matisse high school. One seventh of the money that was raised was used to construct a teacher's house and two thirds of the remaining money was used to construct classrooms. If shs.300, 000 remained, how much money was raised

CHAPTER EIGHT



Specific Objectives

By the end of the topic the learner should be able to:

- a.) Convert fractions into decimals and vice versa
- b.) Identify recurring decimals
- c.) Convert recurring decimals into fractions
- d.) Round off a decimal number to the required number of decimal places
- e.) Write numbers in standard form
- f.) Perform the four basic operations on decimals
- g.) Carry our operations in the correct order
- h.) Apply the knowledge of decimals to real life situations.

Content

- a.) Fractions and decimals
- b.) Recurring decimals
- c.) Recurring decimals and fractions
- d.) Decimal places
- e.) Standard form
- f.) Operations on decimals
- g.) Order of operations
- h.) Real life problems involving decimals.

Introduction

A fraction whose denominator can be written as the power of 10 is called a decimal fraction or a decimal. E.g. 1/10, 1/100, 50/1000.

A decimal is always written as follows 1/10 is written as 0.1 while 5/100 is written as 0.05. The dot is called the decimal point.

Numbers after the decimal points are read as single digits e.g. 5.875 is read as five point eight seven five. A decimal fraction such 8.3 means 8 + 3/10. A decimal fraction which represents the sum of a whole number and a proper fraction is called a mixed fraction.

Place value chart

Ten thousands	Thousands	Hundreds	Tens	Ones	Decimal Point	Tenths	Hundredths	Thousandth s	Ten Thousandth s	Hundred Thousandth S
10,000	1,000	100	10	1		.1	.01	.001	.0001	.00001

Decimal to Fractions

To convert a number from fraction form to decimal form, simply divide the numerator (the top number) by the denominator (the bottom number) of the fraction.

Example:

5/8

$$8)$$
 5.000 ← Add as many zeros as needed.

48

20

<u>16</u>

40

<u>40</u>

0

Converting a decimal to a fraction

To change a decimal to a fraction, determine the place value of the last number in the decimal. This becomes the denominator. The decimal number becomes the numerator. Then reduce your answer.

Example:

.625 - the 5 is in the thousandths column, therefore,

$$.625 = \frac{625}{1000} = \text{reduces to } \frac{5}{8}$$

Note:

Your denominator will have the same number of zeros as there are decimal digits in the decimal number you started with - .625 has three decimal digits so the denominator will have three zero.

Recurring Decimals

These are decimal fractions in which a digit or a group of digits repeat continuously without ending.

$$\frac{1}{3} = 0.3333333$$

$$\frac{5}{11} = 0.454545454$$

We cannot write all the numbers, we therefore place a dot above a digit that is recurring. If more than one digit recurs in a pattern, we place a dot above the first and the last digit in the pattern.

E.g.

0.3333.....is written as 0.3

0.4545.....is written as $0.\dot{4}\dot{5}$

0.324324.....is written as 0.324

Any division whose divisor has prime factors other than 2 or 5 forms a recurring decimal or non-terminating decimal.

Example

Express each as a fraction

- a.) 0.6
- b.) 0.73
- c.) 0.15

Solution

$$r = \frac{6}{9}$$
$$= \frac{2}{3}$$

90r = 66
$$r = \frac{66}{90}$$

$$= \frac{11}{15}$$
c.) Let r = 0.151515 ------(I)
$$100r = 15.1515 ------(II)$$

$$99r = 15$$

$$r = \frac{15}{99}$$

$$= \frac{5}{33}$$

Decimal places

When the process of carrying out division goes over and over again without ending we may round off the digits to any number of required digits to the right of decimal points which are called decimal places.

Example

Round 2.832 to the nearest hundredth.

Solution

Step 1 – Determine the place to which the number is to be rounded is.

2.832

Step 2 – If the digit to the right of the number to be rounded is less than 5, replace it and all the digits to the right of it by zeros. If the digit to the right of the underlined number is 5 or higher, increase the underlined number by 1 and replace all numbers to the right by zeros. If the zeros are decimal digits, you may eliminate them.

$$2.832 = 2.830 = 2.83$$

Example

Round 43.5648 to the nearest thousandth.

Solution

$$43.5648 = 43.5650 = 43.565$$

Example

Round 5,897,000 to the nearest hundred thousand.

Solution

$$5,897,000 = 5,900,000$$

Standard Form

A number is said to be in standard form if it is expressed in form $A \times 10^n$, Where 1 < A < 10 and n is an integer.

Example

Write the following numbers in standard form.

Solution

- a.) $36/10 \times 10 = 3.6 \times 10^{1}$
- b.) $576/100 \times 100 = 5.76 \times 10^2$
- c.) $0.052 = 0.052 \times 100/100$

$$5.2 \times \frac{1}{100}$$
$$5.2 \times (\frac{1}{100})^{2}$$
$$5.2 \times 10^{-2}$$

Operation on Decimals

Addition and Subtraction

The key point with addition and subtraction is to line up the decimal points!

Example

Example

14.73 – 12.155 = 14.730 → again adding this 0 helps
$$- \frac{12.155}{2.575}$$

Example

$$127.5 + 0.127 = 327.500 + 0.127$$

327.627

Multiplication

When multiplying decimals, do the sum as if the decimal points were not there, and then calculate how many numbers were to the right of the decimal point in both the original numbers - next, place the decimal point in your answer so that there are this number of digits to the right of your decimal point?

Example

2.1 x 1.2.

Calculate $21 \times 12 = 252$. There is one number to the right of the decimal in each of the original numbers, making a total of two. We therefore place our decimal so that there are two digits to the right of the decimal point in our answer.

Hence $2.1 \times 1.2 = 2.52$.

Always look at your answer to see if it is sensible. $2 \times 1 = 2$, so our answer should be close to 2 rather than 20 or 0.2 which could be the answers obtained by putting the decimal in the wrong place.

Example

1.4 x 6

Calculate $14 \times 6 = 84$. There is one digit to the right of the decimal in our original numbers so our answer is 8.4

Check 1 x 6 = 6 so our answer should be closer to 6 than 60 or 0.6

Division

When dividing decimals, the first step is to write your numbers as a fraction. Note that the symbol / is used to denote division in these notes.

Hence 2.14 / 1.2 = 2.14

1.2

Next, move the decimal point to the right until both numbers are no longer decimals. Do this the same number of places on the top and bottom, putting in zeros as required.

Hence
$$\frac{2.14}{1.2}$$
 becomes $\frac{214}{120}$

This can then be calculated as a normal division.

Always check your answer from the original to make sure that things haven't gone wrong along the way. You would expect 2.14/1.2 to be somewhere between 1 and 2. In fact, the answer is 1.78.

If this method seems strange, try using a calculator to calculate 2.14/1.2, 21.4/12, 214/120 and 2140 / 1200. The answer should always be the same.

Example

$$4.36 / 0.14 = \underline{4.36} = \underline{436} = 31.14$$

$$0.14 \qquad 14$$

Example

$$27.93 / 1.2 = 27.93 = 2793 = 23.28$$
 1.2
 120

Rounding Up

Some decimal numbers go on forever! To simplify their use, we decide on a cutoff point and "round" them up or down.

If we want to round 2.734216 to two decimal places, we look at the number in the third place after the decimal, in this case, 4. If the number is 0, 1, 2, 3 or 4, we leave the last figure before the cut off as it is. If the number is 5, 6, 7, 8 or 9 we "round up" the last figure before the cut off by one. 2.734216 therefore becomes 2.73 when rounded to 2 decimal places.

If we are rounding to 2 decimal places, we leave 2 numbers to the right of the decimal.

If we are rounding to 2 significant figures, we leave two numbers, whether they are decimals or not.

Example

```
243.7684 = 243.77 (2 decimal places)
= 240 (2 significant figures)
1973.285 = 1973.29 (2 decimal places)
= 2000 (2 significant figures)
```

Order of operation

The same rules on operations is always the same even for decimals.

Examples

Evaluate

$$0.02 + 3.5 \times 2.6 - 0.1 (6.2 - 3.4)$$

Solution

$$0.02 + 3.5 \times 2.6 - 0.1 \times 2.8 = 0.02 + 0.91 - 0.28$$

= 8.84

End of topic

Did you understand everything?

If not ask a teacher, friends or anybody and make sure you understand before going to sleep!

Past KCSE Questions on the topic

1.) Without using logarithm tables or a calculator evaluate.

96.04

2.) Evaluate without using mathematical table

$$1000 \left(\sqrt{\frac{0.0128}{200}} \right)$$

3.) Express the numbers 1470 and 7056, each as a product of its prime factors. Hence evaluate: 1470^2

7056

Leaving the answer in prime factor form

4.)	Without	using mathematical tables or calculators, evaluate
		$\sqrt[3]{675 \times 135}$
		$\sqrt{2025}$

5.) Evaluate without using mathematical tables or the calculator

$$\frac{0.0625x\ 2.56}{0.25\ x\ 0.08}$$

CHAPTER NINE

SQUARE AND SQURE ROOTS

Specific Objectives

By the end of the topic the learner should be able to:

- a.) Find squares of numbers by multiplication
- b.) Find squares from tables
- c.) Find square root by factor method
- d.) Find square root from tables.

Content

- a.) Squares by multiplication
- b.) Squares from tables
- c.) Square roots by factorization
- d.) Square roots from tables.

Introduction

Squares

The square of a number is simply the umber multiplied by itself once. For example the square of 15 is 225. That is $15 \times 15 = 225$.

Square from tables

The squares of numbers can be read directly from table of squares. This tables give only approximate values of the squares to 4 figures. The squares of numbers from 1.000 to 9.999 can be read directly from the tables.

The use of tables is illustrated below

Example

Find the square of:

- a.) 4.25
- b.) 42.5
- c.) 0.425

Tables

a.) To read the square of 4.25, look for 4.2 down the column headed x. Move to the right along this row, up to where it intersects with the column headed 5. The number in this position is the square of 4.25

So $4.25^2 = 18.06$ to 4 figures

b.) The square of 4.25 lies between 40^2 and 50^2 between 1600 and 2500.

$$42.5^2 = (4.25 \times 10^1)^2$$

$$=4.25^2 \times 10^2$$

$$= 18.06 \times 100$$

= 1806

c.)
$$0.425^2 = (4.25 x \frac{1}{10})^2$$

$$=4.25^2 x(\frac{1}{10})^2$$

$$=18.06 \times 1/100$$

$$=0.1806$$

The square tables have extra columns labeled 1 to 9 to the right of the thick line. The numbers under these columns are called mean differences. To find 3.162, read 3.16 to get 9.986. Then read the number in the position where the row containing 9.986 intersects with the differences column headed 2. The difference is 13 and this should be added to the last digits of 9.986

9.986

9.999

56.129 has 5 significant figures and in order to use 4 figures tables, we must first round it off to four figures.

56.129 = 56.13 to 4 figures

$$56.13^2 = (5.613 \times 10^1)^2$$

$$= 31.50 \times 10^2$$

= 3150

Square Roots

Square roots are the opposite of squares. For example 5 x 5 = 25, we say that 5 is a square root of 25.

Any positive number has two square roots, one positive and the other negative . The symbol for the square root of a number is $\sqrt{\ }$.

A number whose square root is an integer is called a perfect square. For example 1, 4,9,25 and 36 are perfect squares.

Square roots by Factorization.

The square root of a number can also be obtained using factorization method.

Example

Find the square root of 81 by factorization method.

Solution

```
\sqrt{81} = \sqrt{3 \times 33 \times 3} (Find the prime factor of 81)
= (3x3)(3x3) (Group the prime factors into two identical numbers)
= 3x3 (Out of the two identical prime factors, choose one and find their product)
= 9
```

Note:

Pair the prime factors into two identical numbers. For every pair, pick only one number then obtain the product.

Example

Find $\sqrt{1764}$ by factorization.

Solution

$$\sqrt{1764} = \sqrt{2 \times 2 \times 3 \times 3 \times 7 \times 7}$$

= 2 x 3 x 7
= 42

Example

Find $\sqrt{441}$ by factorization

Solution

 $= 3 \times 7$

=21

$$\sqrt{441} = \sqrt{3 \times 3 \times 7 \times 7}$$

Square Root from tables

Square roots of numbers from 1.0 to 99.99 are given in the tables and can be read directly.

Examples

Use tables to find the square root of:

Solution

- a.) To read the square root of 1.86, look for 1.8 in the column headed x, move to the right along this row to where it intersects with the column headed 6. The number in this position is the square root of 1.86. Thus $\sqrt{1.86} = 1.364$ to 4 figures.
- b.) $\sqrt{42.57}$ Look for 42 in the column headed x and move along the row containing 42 to where it intersects with the column headed 5.Read the number in this position, which is 6.519. The difference for 7 from the difference column along this row is 6.The difference is added to 6.519 as shown below:

+0.006

6.525

Thus,
$$\sqrt{42.57} = 6.525$$
 to 4 figures.

For any number outside this range, it is necessary to first express it as the product of a number in this range and an even power of 10.

c.)
$$359 = 3.59 \times 10^2$$

$$= 1.895 \times 10$$

$$= 18.95 \text{ (four figures)}$$
d.) $0.8236 = 82.36 \times \left(\frac{1}{10}\right)^2$

$$\sqrt{0.8236} = \sqrt{(82.36 \times \frac{1}{100})}$$

$$= (9.072 + 0.004) \times \frac{1}{10}$$

$$= 0.9076 \text{ (4 figures)}$$

End of topic

Did you understand everything?

If not ask a teacher, friends or anybody and make sure you understand before going to sleep!

Past KCSE Questions on the topic

1.) Evaluate without using tables or calculators

$$\sqrt[3]{\frac{0.125 \times \sqrt{64}}{0.064 \times \sqrt{629}}}$$

2.) Evaluate using reciprocals, square and square root tables only.

$$\sqrt{\frac{\left(445.1\times10^{-1}\right)^2+1}{0.07245}}$$

3.) Using a calculator, evaluate $\frac{\sqrt{(4.652 \times 0.387)^2}}{0.8462}$

(Show your working at each stage)

4.) Use tables of reciprocals and square roots to evaluate

$$\sqrt{\frac{2}{o.5893} - \frac{1.06}{846.3}}$$

- 5.) Use tables to find;
 - a) I) 4.978²
 - ii) The reciprocal of 31.65
 - b) Hence evaluate to 4.S.F the value of

$$4.978^2 - \frac{1}{31.65}$$

6.) Use tables of squares, square roots and reciprocals to evaluate correct to 4 S.

$$\frac{3}{\sqrt{0.0136}} \frac{2}{(3.72)^2}$$

7. Without using mathematical tables or calculator, evaluate: $\underline{153 \times 1.8}$ giving your answer in standard form 0.68×0.32



Specific Objectives

By the end of the topic the learner should be able to:

- a.) Use letters to represent numbers
- b.) Write statements in algebraic form
- c.) Simplify algebraic expressions
- d.) Factorize an algebraic expressions by grouping
- e.) Remove brackets from algebraic expressions
- f.) Evaluate algebraic expressions by substituting numerical values
- g.) Apply algebra in real life situations.

Content

- a.) Letters for numbers
- b.) Algebraic fractions
- c.) Simplification of algebraic expressions
- d.) Factorization by grouping
- e.) Removal of brackets
- f.) Substitution and evaluation
- g.) Problem solving in real life situations.

Introduction

An algebraic expression is a mathematical expression that consists of variables, numbers and operations. The value of this expression can change Clarify the definitions and have students take notes on their graphic organizer.

Note:

- Algebraic Expression—contains at least one variable, one number and one operation. An example of an algebraic expression is n + 9.
- Variable—a letter that is used in place of a number. Sometimes, the variable will be given a value. This value will replace the variable in order to solve the equation. Other times, the variable is not assigned a value and the student is to solve the equation to determine the value of the variable.
- **Constant**—a number that stands by itself. The 9 in our previous vocabulary is an example of a constant.
- Coefficient—a number in front of and attached to a variable. For example, in the expression 5x + 3, the 5 is the coefficient.
- **Term**—each part of an expression that is separated by an operation. For instance, in our earlier example n + 9, the terms are n and 7.

Examples

Write each phrase as an algebraic expression.

Nine increased by a number $r \rightarrow 9 + r$

Fourteen decreased by a number $x \rightarrow 14 - x$

Six less than a number $t \rightarrow t - 6$

The product of 5 and a number $n \rightarrow 5 X n$ or 5n

Thirty-two divided by a number y $31 \div x$ or $\frac{31}{x}$

Example

An electrician charges sh 450 per hour and spends sh 200 a day on gasoline. Write an algebraic expression to represent his earnings for one day.

Solution: Let x represent the number of hours the electrician works in one day. The electrician's earnings can be represented by the following algebraic expression:

Solution

450x - 200

Simplification of Algebraic Expressions

Note:

Basic steps to follow when simplify an algebraic expression:

- ✓ Remove parentheses by multiplying factors.
- ✓ Use exponent rules to remove parentheses in terms with exponents.
- ✓ Combine like terms by adding coefficients.
- ✓ Combine the constants.

Like and unlike terms

Like terms have the same variable /letters raised to the same power i.e. 3 b + 2 b = 5 b or a + 5 a = 6 a and they can be simplified further into 5b and 6a respectively (a^2 and $3a^2$ are also like terms). While unlike terms have different variables i.e. 3 b + 2 c or 4 b + 2 x and they cannot be simplified further.

Example

3a+12b+4a-2b = 7a+10b (collect the lick terms)

$$2x - 5y + 3x - 7y + 3w = 5x - 12y + 3w$$

Example

Simplify: 2x - 6y - 4x + 5z - y

Solution

$$2x - 6y - 4x + 5z - y = 2x - 4x - 6y - y + 5z$$

$$= (2x - 4x) - (6y + y) + 5z$$
$$= -2x - 7y + 5z$$

Note:

$$-6y - y = -(6y + y)$$

Example

Simplify:
$$\frac{1}{2}a - \frac{1}{3}b + \frac{1}{4}a$$

Solution

The L.C.M of 2, 3 and 4 is 12.

Therefore
$$\frac{1}{2}a - \frac{1}{3}b + \frac{1}{4}a = \frac{6a - 4b + 3a}{12}$$

$$= \frac{6a + 3a - 4b}{12}$$
$$= \frac{9a - 4b}{12}$$

Example

Simplify:
$$\frac{a+b}{2} - \frac{2a-b}{3}$$

Solution

$$\frac{a+b}{2} - \frac{2a-b}{3} = \frac{3(a+b)-2(2a-b)}{6}$$

$$\frac{3a+3b-4a+2b}{6}$$

$$\frac{3a-4a+3b+2b}{6}$$

$$= \frac{-a+5b}{6}$$

Example

$$5x^2 - 2x^2 = 3x^2$$

$$4a^{2}bc - 2a^{2}bc = 2a^{2}bc$$

$$a^{2}b - 2b^{3}c + 3a^{2}b + b^{3}c = 4a^{2}b - b^{3}c$$

Note:

Capital letter and small letters are not like terms.

Brackets

Brackets serve the same purpose as they do in arithmetic.

Example

Remove the brackets and simplify:

a.)
$$3(a+b)-2(a-b)$$

b.)
$$1/3a + 3(5a + b - c)$$

c.)
$$2b + 3(3 - 2(a - 5))$$

Solution

a.)
$$3(a+b)-2(a-b) = 3a+3b-2a+2b$$

= $3a-2a+3b+2b$
= $a+5b$

b.)
$$1/3a + 3(5a + b - c) = 1/3a + 15a + 3b - 3c$$

= $15\frac{1}{3}a + 3b - 3c$

c.)
$$2b + a \{ 3 - 2 (a - 5) \} = 2b + a \{ 3 - 2a + 10 \}$$

= $2b + 3a - 2a^2 + 10a$
= $2b + 3a + 10 a - 2a^2$
= $2b + 13a - 2a^2$

The process of remaining the brackets is called expansion while the reverse process of inserting the brackets is called factorization.

Example

Factorize the following:

a.)
$$3m + 3n = 3 (m + n)$$
 (the common term is 3 so we put it outside the bracket)

b.)
$$ar^3 + ar^4 + ar^5$$

c.)
$$4x^2y + 20x^4y^2 - 36x^3y$$

Solution

b.)
$$ar^3 + ar^4 + ar^5 (ar^3 \text{ is common})$$

$$ar^3(1+r+r^2)$$

c.)
$$4x^2y + 20x^4y^2 - 36x^3y$$

 $4x^2y$ (Is common)
 $= 4x^2y(1 + 5x^2y - 9x)$

Factorization by grouping

When the terms of an expression which do not have a common factor are taken pairwise, a common factor can be found. This method is known as factorization by grouping.

Example

Factorize:

a.)
$$3ab + 2b + 3ca + 2c$$

b.)
$$ab + bx - a - x$$

Solution

a.)
$$3ab + 2b + 3ca + 2c = b (3a + 2) + c (3a + 2)$$

= $(3a + 2) (b + c)$

b.)
$$ab + bx - a - x = b (a + x) - 1 (a + x)$$

= $(a + x) (b - 1)$

Algebraic fractions

In algebra, fractions can be added and subtracted by finding the L.C.M of the denominators.

Examples

Express each of the following as a single fraction:

a.)
$$\frac{x-1}{2} + \frac{x+2}{4} + \frac{x}{5}$$

b.)
$$\frac{a+b}{b} - \frac{b-a}{a}$$

c.)
$$\frac{1}{3(a+b)} + \frac{3}{8(a+b)} + \frac{5}{12a}$$

Solution

a.)
$$\frac{x-1}{2} + \frac{x+2}{4} + \frac{x}{5} = \frac{10(x-1)+5(x+2)+4x}{12a}$$
 (10x -10 + 5x + 10 + 4x)
= $\frac{19x}{20}$

$$b.) \frac{a+b}{b} - \frac{b-a}{a} = \frac{b(a+b)-a(b-a)}{ab}$$
$$= \frac{a^2+b^2}{ab}$$

c.)
$$\frac{1}{3(a+b)} + \frac{3}{8(a+b)} + \frac{5}{12a}$$
 (find the L. C. M. of 3,8 and 12 which is 24,)
(find the L. C. M. of a and (a+b) is a(a+b))
(The L. C. M. of 3 (a+b),8 (a+b) and 12 is 24a (a+b))
 $\frac{1}{3(a+b)} + \frac{3}{8(a+b)} + \frac{5}{12a} = \frac{8a+9a+10a+10b}{24a(a+b)}$

$$= \frac{27a + 10b}{24a(a+b)}$$

Simplification by factorization

Factorization is used to simplify expressions

Examples

Simplify
$$\frac{p^2 - 2pq + q^2}{2p^2 - 3pq + q^2}$$

Solution

Numerator is solved first.

$$p^2 - Pq - pq + q^2$$

$$p(p-q) - q(p+q)$$
$$(p-q)^2$$

Then solve the denominator

$$2p^2-2pq - pq - q^2$$

(2p-q) (p-q)

$$\frac{(p-q)^2}{(2p-q)(p-q)} = \frac{p-q}{2p-q}$$

 $(p-q)^2 = (p-q)(p-q)$ hence it cancel with the denominator

Example

Simplify

$$\frac{16m^2 - 9n^2}{4m^2 - mn - 3n^2}$$

Solution

Num.
$$(4m - 3n) (4m + 3n)$$

Den.
$$4m^2 - 4mn + 3mn - 3n^2$$

$$(4m+3n)(m-n)$$

$$(4m-3n)(4m+3n)$$

$$(4m + 3n)(m - n)$$

$$4m-3n$$

$$m - n$$

Example

Simplify the expression.

$$\frac{18xy - 18xr}{9xr - 9xy}$$

Solution

Numerator

$$18x (y - r)$$

Denominator

$$9x(r-y)$$

Therefore
$$\frac{18x(y-r)}{9x(r-y)}$$

$$=\frac{(y-r)}{(r-y)}$$

Example

$$\frac{12x^2 + ax - 6a^2}{9x^2 - 4a^2}$$

Solution

$$\frac{(3x-2a)(4x+3a)}{}$$

$$\overline{(3x+2a)(3x-2a)}$$

$$=\frac{4x+3a}{3x+2a}$$

Example

Simplify the expression completely.

$$\frac{ay-ax}{bx-by}$$

Solution

$$\frac{a(y-x)}{b(x-y)} = \frac{a(y-x)}{-b(x-y)} = \frac{a}{-b} = \frac{-a}{b}$$

Note:

$$x - y = -(y - x)$$

Substitution

This is the process of giving variables specific values in an expression

Example

Evaluate the expression $\frac{x^2+y^2}{y+2}$ if x =2 and y = 1

Solution

$$\frac{x^2 + y^2}{y + 2} = \frac{2^2 + 1^2}{1 + 2} = \frac{4 + 1}{3}$$

$$=\frac{5}{3}=1\frac{2}{3}$$

End of topic

Did you understand everything?

If not ask a teacher, friends or anybody and make sure you understand before going to sleep!

Past KCSE Questions on the topic

- 1. Given that $y = \frac{2x z}{x + 3z}$ express x in terms of y and z
- 2. Simplify the expression

$$\underline{x-1}$$
 - $\underline{2x+1}$

x = 3x

Hence solve the equation

$$\underline{x-1} \quad - \quad \underline{2x+1} \quad = \underline{2}$$

x 3x

3. Factorize $a^2 - b^2$

Hence find the exact value of 2557² - 2547²

4. Simplify $p^2 - 2pq + q^2$

$$P^3 - pq^2 + p^2 q - q^3$$

5. Given that y = 2x - z, express x in terms of y and z.

Four farmers took their goats to a market. Mohammed had two more goats as Koech had 3 times as many goats as Mohammed, whereas Odupoy had 10 goats less than both Mohammed and Koech.

- (i) Write a simplified algebraic expression with one variable, representing the total number of goats.
- (ii) Three butchers bought all the goats and shared them equally. If each butcher got 17 goats, how many did odupoy sell to the butchers?
- 6. Solve the equation

$$\underline{1} = \underline{5} -7$$

7. Simplify

$$2(a+b)$$
 $2(a-b)$

8. Three years ago, Juma was three times as old. As Ali in two years time, the sum of their ages will be 62. Determine their ages

CHAPTER ELEVEN

RATES, RATIO, PROPORTION AND PERCENTAGE

Specific Objectives

By the end of the topic the learner should be able to:

- a.) Define rates
- b.) Solve problems involving rates
- c.) Define ratio
- d.) Compare two or more quantities using ratios
- e.) Change quantities in a given ratio
- f.) Compare two or more ratios
- g.) Represent and interpret proportional parts
- h.) Recognize direct and inverse proportions
- i.) Solve problems involving direct and inverse proportions
- j.) Convert fractions and decimals to percentages and vice-versa
- k.) Calculate percentage change in a given quantity
- 1.) Apply rates, ratios, percentages to real life situations and proportion.

Content

- a.) Rates
- b.) Solving problems involving rates
- c.) Ratio
- d.) Comparing quantities using ratio
- e.) Increase and decrease in a given ratio
- f.) Comparing ratios
- g.) Proportion: direct and inverse
- h.) Solve problems on direct and inverse proportions
- i.) Fractions and decimals as percentages
- i.) Percentage increase and decrease
- k.) Application of rates, ratios, percentages and proportion to real life situations.

Introduction

Rates

A rate is a measure of quantity, and comparing one quantity with another of different kind.

Example

If a car takes two hours to travel a distance of 160 km. then we will say that it is travelling at an average rate of 80 km per hour. If two kilograms of maize meal is sold for sh. 38.00, then we say that maize meal is selling at the rate of sh.19.00 per kilogram.

Example

What is the rate of consumption per day if twelve bags of beans are consumed in 120 days?

Solution.

Rate of consumption = number of bags/number of days

$$=\frac{12}{120}$$

=1/10 bags per day

Example

A laborer's wage is sh.240 per eight hours working day. What is the rate of payment per hour?

Solution

Rate = amount of money paid/number of hours

$$=\frac{240}{8}$$

=sh.30 per hour

Ratio

A ratio is a way of comparing two similar quantities. For example, if alias is 10 years old and his brother basher is 14 years old. Then alias age is 10/14 of Bashir's age, and their ages are said to be in the ratio of 10 to 14. Written, 10:14.

Alias age: Bashir's age =10:14

Bashir's age: alias age =14:10

In stating a ratio, the units must be the same. If on a map 2cm rep 5km on the actual ground, then the ratio of map distance to map distance is 2cm: 5x1 00 000cm, which is 2:500 000.

A ratio is expressed in its simplest form in the same way as a fraction,

E.g. 10/14 = 5/7, hence 10:14 = 5:7.

Similarly, $2:500\ 000 = 1:250\ 000$,

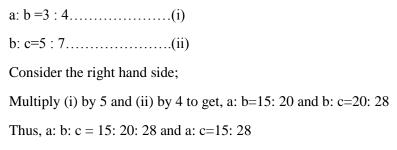
A proportion is a comparison of two or more ratios. If, example, a, b and c are three numbers such that a: b: c=2:3:5, then a, b, c are said to be proportional to 2, 3, 5 and the relationship should be interpreted to mean a/2 = b/3 = c/5.

Similarly, we can say that a: b = 2:3, b: c = 3:5 a: c = 2:5

Example 3

If a: b = 3: 4 and b: c = 5: 7 find a: c

Solution



Increase and decrease in a given ratio

To increase or decrease a quantity in a given ratio, we express the ratio as a fraction and multiply it by the quantity.

Example

Increase 20 in the ratio 4: 5

Solution

```
New value =5/4x20
=5x5
=25
```

Example

Decrease 45 in the ratio 7:9

Solution

```
New value =7/9 \text{ x}45
=7\text{x}5
=35
```

Example

The price of a pen is adjusted in the ratio 6:5. If the original price was sh.50. What is the new price?

Solution

```
New price: old price = 6.5
New price /old price = 6/5
New price = 6/5x50
= 8x + 60
```

Note:

When a ratio expresses a change in a quantity an increase or decrease , it is usually put in the form of new value: old value

Comparing ratios

In order to compare ratios, they have to be expressed as fractions first, ie., a:b=a/b . the resultant fraction can then be compared.

Example

Which ratio is greater, 2: 3 or 4: 5?

Solution 2:3 = 2/3, 4:5 = 4/5

$$2/3 = 10/15$$
, $4/5 = 12/15 = 4/5 > 2/3$

Thus, 4: 5 > 2: 3

Distributing a quantity in a given ratio

If a quantity is to be divided in the ratio a: b: c, the fraction of the quantity represented by:

(i) A will be
$$\frac{a}{a+b+c}$$

(ii) B will be
$$\frac{a}{a+b+c}$$

(iii) C will be
$$\frac{a}{a+b+c}$$

Example

A 72-hactare farm is to be shared among three sons in the ratio 2:3:4. What will be the sizes in hectares of the three shares?

Solution

Total number of parts is 2+3+4=9

The she shares are: $2/9 \times 72$ ha = 16ha

$$3/9 \times 72$$
ha= 24ha

$$4/9 \times 72$$
ha = 36ha

Direct and inverse proportion

Direct proportion

The table below shows the cost of various numbers of cups at sh. 20 per cup.

No. of cups	1	2	3	4	5
Cost (sh.)	20	40	60	80	100

The ratio of the numbers of cups in the fourth column to the number of cups in the second column is 4:2=2:1. The ratio of the corresponding costs is 80:40=2:1. By considering the ratio of costs in any two columns and the corresponding ratio and the number of cups, you should notice that they are always the same.

If two quantities are such that when the one increases (decreases) in particular ratio, the other one also increases (decreases) in the ratio,

Example

A car travels 40km on 5 litres of petrol. How far does it travel on 12 litres of petrol?

Solution

Petrol is increased in the ratio 12: 5

Distance= 40x 12/5 km

Example

A train takes 3 hours to travel between two stations at an average speed of 40km per hour. A t what average speed would it need to travel to cover the same distance in 2hours?

Solution

Time is decreased in the ratio 2:3 Speed must be increased in the ratio 3:2 average speed is $40 \times 3/2 \text{ km} = 60 \text{ km/h}$

Example

Ten men working six hours a day take 12 days to complete a job. How long will it take eight men working 12 hours a day to complete the same job?

Solution

Number of men decreases in the ratio 8:10

Therefore, the number of days taken increases in the ratio 10:8.

Number of hours increased in the ratio 12:6.

Therefore, number of days decreases in the ratio 6:12.

Number of days taken =
$$12 \times \frac{10}{8} \times \frac{6}{12}$$

Percentages

A percentage (%) is a fraction whose denominator is 100. For example, 27% means 27/100.

Converting fractions and decimals into percentages

To write a decimal or fraction as a %: multiply by 100 .For example

$$0.125 = 0.125 \times 100 = 12.5\%$$

$$\frac{2}{5}$$
 = $\frac{2}{5} \times 100$ (i.e. $\frac{2}{5}$ Of 100%) = 40%
Or $\frac{2}{5}$ = $2 \div 5 \times 100 = 40\%$

Example

Change 2/5 into percentage.

Solution

$$\frac{2}{5} = \frac{x}{100}$$

$$x = \frac{2}{5} \times 100$$

$$= 40\%$$

Example

Convert 0.67 into a percentage: solution

$$0.67 = \frac{67}{100}$$

As a percentage,
$$0.67 = \frac{67}{100} \times 100$$

Percentage increase and decrease

A quantity can be expressed as a percentage of another by first writing it as a fraction of the given quantity.

Example

A farmer harvested 250 bags of maize in a season. If he sold 200 bags, what percentage of his crops does this represent?

Let x be the percentage sold.

Then,
$$x/100 = \frac{200}{250}$$

So,
$$x = = \frac{200}{250} \times 100$$

Example

A man earning sh. 4 800 per month was given a 25% pay rise. What was his new salary?

Solution

Example

A dress which was costing sh. 1 200 now goes for sh. 960. What is the percentage decrease?

Solution

Decrease in cost is 1 200- 960= sh. 240

Percentage decrease = $240/1\ 200\ x\ 100$

=20%

Example

The ratio of john's earnings to muse's earnings is 5:3. If john's earnings increase by 12%, his new figure becomes sh. 5 600. Find the corresponding percentage change in muse's earnings if the sum of their new earnings is sh.9 600

Solution

John's earnings before the increase is $100/112 \times 5600 = \text{sh. } 5000$

John's earnings/muse's earnings = 5/3

Musa's earnings before the increase = $3/5 \times 5000$

$$= sh. 3 000$$

Musa's new earnings = 9 600 - 5 600=sh. 4 000 Musa's change in earnings = 4 000-1 000=sh. 3 000 Percentage change in muse's earnings = $1000/3000 \times 100$

 $=33\frac{1}{3}\%$

End of topic

Did you understand everything?

If not ask a teacher, friends or anybody and make sure you understand before going to sleep!

Past KCSE Questions on the topic

- 1. Akinyi bought and beans from a wholesaler. She then mixed the maize and beans in the ratio 4:3 she bought the maize at Kshs 21 per kg and the beans 42 per kg. If she was to make a profit of 30%. What should be the selling price of 1 kg of the mixture?
- 2. Water flows from a tap at the rate of 27 cm³ per second into a rectangular container of length 60 cm, breadth 30 cm and height 40 cm. If at 6.00 PM the container was half full, what will be the height of water at 6.04 pm?
- 3. Two businessmen jointly bought a minibus which could ferry 25 paying passengers when full. The fare between two towns A and B was Kshs 80 per passenger for one way. The minibus made three round trips between the two towns daily. The cost of fuel was Kshs 1500 per day. The driver and the conductor were paid daily allowances of Kshs 200 and Kshs 150 respectively.

A further Kshs 4000 per day was set aside for maintenance, insurance and loan repayment.

- (a) (i) How much money was collected from the passengers that day?
 - (ii) How much was the net profit?
- (b) On another day, the minibus was 80% full on the average for the three round trips, how much did each businessman get if the day's profit was shared in the ratio 2:3?
- 4. Wainaina has two dairy farms, A and B. Farm A produces milk with 3 ¼ percent fat and farm B produces milk with 4 ¼ percent fat.
 - (a) Determine
 - (i) The total mass of milk fat in 50 kg of milk from farm A and 30 kg of milk from farm B
 - (ii) The percentage of fat in a mixture of 50kg of milk A and 30kg of milk from B
 - (b) The range of values of mass of milk from farm B that must be used in a 50kg mixture so that the mixture may have at least 4 percent fat.
- 5. In the year 2001, the price of a sofa set in a shop was Kshs 12,000
 - (a) Calculate the amount of money received from the sales of 240 sofa sets that year.
 - (b) (i) In the year 2002 the price of each sofa set increased by 25% while the number of sets sold decreased by 10%. Calculate the percentage increase in the amount received from the sales
 - (ii) If the end of year 2002, the price of each sofa set changed in the ratio 16: 15, calculate the price of each sofa set in the year 2003.
 - (c) The number of sofa sets sold in the year 2003 was P% less than the number sold in the year 2001.
 - Calculate the value of P, given that the amounts received from sales if the two years were equal.

- 6. A solution whose volume is 80 litres is made up of 40% of water and 60% of alcohol. When x litres of water is added, the percentage of alcohol drops to 40%.
 - (a) Find the value of x
 - (b) Thirty litres of water is added to the new solution. Calculate the percentage of alcohol in the resulting solution
 - (c) If 5 litres of the solution in (b) above is added to 2 litres of the original solution, calculate in the simplest form, the ratio of water to that of alcohol in the resulting solution.
- 7. Three business partners, Asha, Nangila and Cherop contributed Kshs 60,000, Kshs 85,000 and Kshs 105,000 respectively. They agreed to put 25% of the profit back into business each year. They also agreed to put aside 40% of the remaining profit to cater for taxes and insurance. The rest of the profit would then be shared among the partners in the ratio of their contributions. At the end of the first year, the business realized a gross profit of Kshs 225,000.
 - (a) Calculate the amount of money Cherop received more than Asha at the end of the first year.
 - (b) Nangila further invested Kshs 25,000 into the business at the beginning of the second year. Given that the gross profit at the end of the second year increased in the ratio 10:9, calculate Nangila's share of the profit at the end of the second year.
- 8. Kipketer can cultivate a piece of land in 7 hrs while Wanjiku can do the same work in 5 hours. Find the time they would take to cultivate the piece of land when working together.
- 9. Mogaka and Ondiso working together can do a piece of work in 6 days. Mogaka working alone, takes 5 days longer than Onduso. How many days does it take Onduso to do the work alone.
- 10. A certain amount of money was shared among 3 children in the ratio 7:5:3 the largest share was Kshs 91. Find the
 - (a) Total amount of money
 - (b) Difference in the money received as the largest share and the smallest share.

CHAPTER TWELVE



Specific Objectives

By the end of the topic the learner should be able to:

- a.) State the units of measuring length
- b.) Convert units of length from one form to another
- c.) Express numbers to required number of significant figures
- d.) Find the perimeter of a plane figure and circumference of a circle.

Content

- a.) Units of length (mm, cm, m, km)
- b.) Conversion of units of length from one form to another
- c.) Significant figures
- d.) Perimeter
- e.) Circumference (include length of arcs)

Introduction

Length is the distance between two points. The SI unit of length is metres. Conversion of units of length.

1 kilometer (km) = 1000metres

1 hectometer (hm) =100metres

1 decameter (Dm) =10 metres

1 decimeter (dm) = 1/10 metres

1 centimeter (cm) = 1/100 metres

1 millimeter (mm) = 1/1000 metres

The following prefixes are often used when referring to length:

Mega - 1 000 000

Kilo - 1 000

Hecto - 100

Deca -10

Deci-1/10

Centi-1/100

Milli-1/1000

Micro-1/1 000 000

Significant figures

The accuracy with which we state or write a measurement may depend on its relative size. It would be unrealistic to state the distance between towns A and B as 158.27 km. a more reasonable figure is 158 km.158.27km is the distance expressed to 5 significant figures and 158 km to 3 significant figures.

Example

Express each of the following numbers to 5, 4, 3, 2, and 1 significant figures:

- (a) 906 315
- (b) 0.08564
- (c) 40.0089
- (d) 156 000

Solution

	number	5 s.f.	4s.f	3s.f	2s.f	1 s.f.
(a)	906 315	906 320	906 300	906 000	910 000	900 000
(b)	0.085641	0.085641	0.08564	0.0856	0.085	0.09
(c)	40.0089	40.009	40.01	40.0	40	40
(d)	156 000	156 000	156 000	156 000	160 000	200 000

The above example show how we would round off a measurement to a given number of significant figures

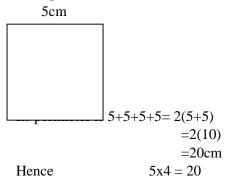
Zero may not be a significant. For example:

- (i) 0.085 zero is not significant therefore, 0.085 is a two- significant figure.
- (ii) 2.30 zero is significant. Therefore 2.30 is a three-significant figure.
- (iii) 5 000 –zero may or may not be significant figure. Therefore, 5 000 to three significant figure is 5 00 (zero after 5 is significant). To one significant figure is 5 000. Zero after 5 is not significant.
- (iv) 31.805 Or 305 zero is significant, therefore 31.805 is five significant figure. 305 is three significant figure.

Perimeter

The perimeter of a plane is the total length of its boundaries. Perimeter is a length and is therefore expressed in the same units as length.

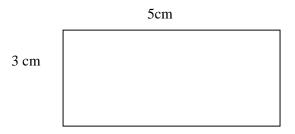
Square shapes



So perimeter of a square = Sides x 4

Rectangular shapes

Figure 12.2 is a rectangle of length 5cm and breadth 3cm.



Its perimeter is 5+3+5+3 = 2(5+3)cm

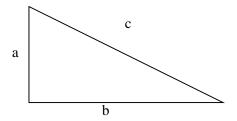
=2x8

= 16cm

Hence perimeter of a rectangle p=2(L+W)

Triangular shapes

To find the perimeter of a triangle add all the three sides.



Perimeter = (a + b + c) units, where a, b and c are the lengths of the sides of the triangle.

The circle

The circumference of a circle = $2 \pi r$ or πD

Example

- (a) Find the circumference of a circle of a radius 7cm.
- (b) The circumference of a bicycle wheel is 140 cm. find its radius.

Solution

(a) $C = \pi d$

 $=22/7 \times 7$

=44 cm

(b) $C=\pi d$

 $=2\pi r$

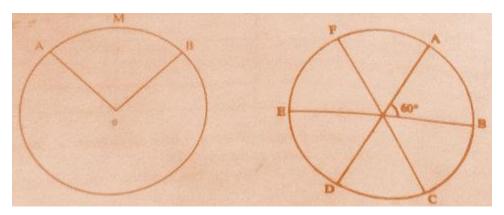
=2x22/7xr

 $=140 \div 44/7$

=22.27 cm

Length of an arc

An arc of a circle is part of its circumference. Figure 12.10 (a) shows two arcs AMB and ANB. Arc AMB, which is less than half the circumference of the circle, is called the minor arc, while arc ANB, which is greater half of the circumference is called the major arc. An arc which is half the circumference of the circle is called a semicircle.



Example

An arc of a circle subtends an angle 60 at the centre of the circle. Find the length of the arc if the radius of the circle is 42 cm. (π =22/7).

Solution

The length, l, of the arc is given by:

 $L = \theta/360 \times 2\pi r$.

 Θ =60, r=42 cm

Therefore, 1 = 60/360 x2 x 22/7 x 42

=44 cm

Example

The length of an arc of a circle is 62.8 cm. find the radius of the circle if the arc subtends an angle 144 at the centre, (take π =3.142).

Solution

 $L = \theta/360 \times 2\pi r = 62.8$ and $\theta = 144$

Therefore, $\frac{144}{360}x2 \ x \ 3.142 \ x \ r = 62.8$

$$R= 62.8 x \frac{360}{144} x 2 x 3.142$$

=24.98 cm

Example

Find the angle subtended at the centre of a circle by an arc of length 11cm if the radius of the circle is 21cm.

Solution

 $L=0/360 \times 2 \times \pi r = 11 \text{ cm} \text{ and } r = 21 \text{ m}$

L=0/360 x2x22/7x 21=11

Thus, $\theta = 11x360x7 / 2x22x21$

 $=30^{0}$

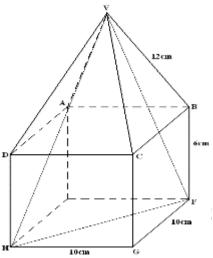
End of topic

Did you understand everything?

If not ask a teacher, friends or anybody and make sure you understand before going to sleep!

Past KCSE Questions on the topic

- 1.) Two coils which are made by winding copper wire of different gauges and length have the same mass. The first coil is made by winding 270 metres of wire with cross sectional diameter 2.8mm while the second coil is made by winding a certain length of wire with cross-sectional diameter 2.1mm. Find the length of wire in the second coil.
- 2. The figure below represents a model of a hut with HG = GF = 10cm and FB = 6cm. The four slanting edges of the roof are each 12cm long.



NEB, High School & Primary Notes 5657/0770195807

Calculate

Length DF.

Angle VHF

The height of the model hut.

The length of the projection of line VH on the plane EFGH.

The le	ngth VH	•			
The angle DF makes with the plane ABCD.					
3.		quare floor is fitted with rectangular tiles of perimeters 220 cm. each row (tile length wise) ries 20 less tiles than each column (tiles breadth wise). If the length of the floor is 9.6 m.			
	Calculate:				
	a. The dimensions of the tiles				
	b. The number of tiles needed				
	c. The cost of fitting the tiles, if tiles are sold in dozens at sh. 1500 per dozen and the lab cost is sh. 3000				

CHAPTER THIRTEEN



Specific Objectives

By the end of the topic the learner should be able to:

- a.) State units of area
- b.) Convert units of area from one form to another
- c.) Calculate the area of a regular plane figure including circles
- d.) Estimate the area of irregular plane figures by counting squares
- e.) Calculate the surface area of cubes, cuboids and cylinders.

Content

- a.) Units of area (cm₂, m₂, km₂, Ares, ha)
- b.) Conversion of units of area
- c.) Area of regular plane figures
- d.) Area of irregular plane shapes
- e.) Surface area of cubes, cuboids and cylinders

Introduction

Units of Areas

The area of a plane shape is the amount of the surface enclosed within its boundaries. It is normally measured in square units. For example, a square of sides 5 cm has an area of

$$5 \times 5 = 25 \text{ cm}$$

A square of sides 1m has an area of 1m, while a square of side 1km has an area of 1km

Conversion of units of area

```
1 m<sup>2</sup> =1mx 1m

= 100 cm x 100 cm

= 10 000 cm<sup>2</sup>

1 km<sup>2</sup> = 1 km x 1 km

= 1 000 m x 1 000 m

=1 000 000 m<sup>2</sup>

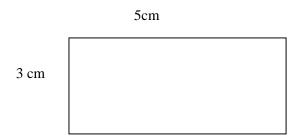
1 are = 10 m x 10 m

=100 m<sup>2</sup>
```

1 hectare (ha) = 100 Ares

 $=10\ 000\ m^2$

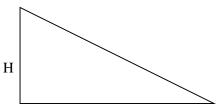
Area of a regular plane figures Areas of rectangle



Area, A = 5x3 cm = $15m^2$

Hence, the area of the rectangle, A =L X W square units, where l is the length and b breadth.

Area of a triangle



Area of a triangle

A = 1/2bh square units

Area of parallelogram

Area = 1/2bh + 1/2bh

=bh square units

Note:

This formulae is also used for a rhombus

Area of a trapezium

The figure below shows a trapezium in which the parallel sides are a units and b units, long. The perpendicular distance between the two parallel sides is h units.

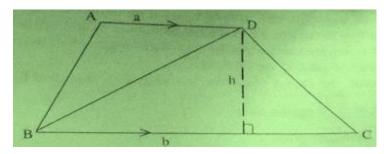
Area of a triangle ABD = 1/2 ah square units

Area of triangle DBC = $\frac{1}{2}$ bh square units

Therefore area of trapezium ABCD = 1/2 ah + 1/2 bh

= 1/2h (a + b) square units.

Thus, the area of a trapezium is given by a half the sum of the length of parallel sides multiplied by the perpendicular distance between them.



That is, area of trapezium $=\frac{1}{2}(a+b)h$

Area of a circle

The area A of a circle of radius r is given by: $A = \pi r^2$

The area of a sector

A sector is a region bounded by two radii and an arc.

Suppose we want to find the area of the shaded part in the figure below



The area of the whole circle is πr^2

The whole circle subtends 360at the centre.

Therefore, 360 corresponds to πr^2

1° corresponds to 1/360°x π r²

 60° corresponds to $60^{\circ}/360^{\circ}$ x π r²

Hence, the area of a sector subtending an angle θ at the centre of the circle is given by

$$A = \frac{\theta}{360^0} \times \pi r^2$$

Example

Find the area of the sector of a circle of radius 3cm if the angle subtended at the centre is 140 (take π =22/7)

Solution

Area A of a sector is given by

$$A = \frac{\theta}{360^0} x \pi r^2$$

Here, r = 3 cm and $\theta = 140^{\circ}$

Therefore,
$$A = \frac{140}{360^0} x \frac{22}{7} x 3 x 3$$

= 11 cm²

Example

The area of a sector of a circle is 38.5 cm². Find the radius of the circle if the angle subtended at the centre is 90° (Take $\pi=22/7$)

Solution

From the formula $a = \theta/360 \text{ x } \pi r^2$, we get $90/360 \text{ x } 22/7 \text{ x } r^2 = 38.5$

Therefore,
$$r^2 = \frac{38.5 \times 360 \times 7}{90 \times 22}$$

Thus, r = 7

Example

The area of a circle radius 63 cm is 4158 cm². Calculate the angle subtended at the centre of the circle. (Take $\pi = 22/7$)

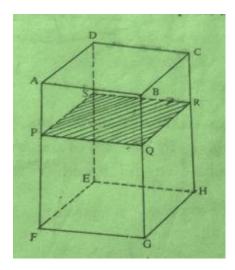
Using a = $\theta/360 \times \pi r^2$,

$$\Theta = \frac{4158 \, x \, 7 \, x \, 360}{22 \, x \, 63 \, x \, 63}$$

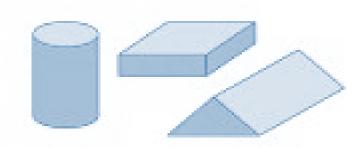
$$=120^{0}$$

Surface area of solids

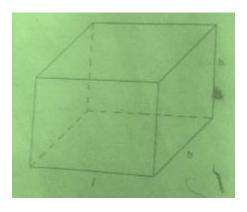
Consider a cuboid ABCDEFGH shown in the figure below. If the cuboid is cut through a plane parallel to the ends, the cut surface has the same shape and size as the end faces. PQRS is a plane. The plane is called the cross-section of the cuboid



A solid with uniform cross-section is called a prism. The following are some of the prisms. The following are some of the prisms.



The surface area of a prism is given by the sum of the area of the surfaces.



The figure below shows a cuboid of length l, breath b and height h. its area is given by;

A=21b+2bh+2h1

=2(lb. + bh + hl)

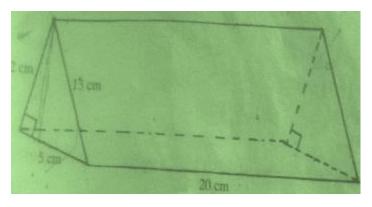
For a cube offside 2cm;

 $A = 2(3x2^2)$

 $=24 \text{ cm}^2$

Example

Find the surface area of a triangular prism shown below.



Area of the triangular surfaces = $\frac{1}{2}$ x5x12 x2cm²

 $=60 \text{ cm}^2$

Area of the rectangular surfaces=20 x13 +5 x 20 +12 x20

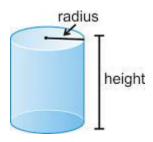
 $=260 + 100 + 240 = 600 \text{cm}^2$

Therefore, the total surface area= (60+600) cm²

 $=660 \text{ cm}^2$

Cylinder

A prism with a circular cross-section is called a cylinder, see the figure below.



If you roll a piece of paper around the curved surface of a cylinder and open it out, you will get a rectangle whose breath is the circumference and length is the height of the cylinder. The ends are two circles. The surface area S of a cylinder with base and height h is therefore given by;

$$S=2\pi rh + 2\pi r^2$$

Example

Find the surface area of a cylinder whose radius is 7.7 cm and height 12 cm.

Solution

$$S = 2 \pi (7.7) \times 12 + 2 \pi (7.7) \text{ cm}^2$$

=
$$2 \pi (7.7) \times 12 + (7.7) \text{ cm}^2$$

$$=2 \times 7.7 \pi (12 + 7.7) \text{ cm}^2$$

$$=2 \times 7.7 \times \pi (19.7) \text{ cm}^2$$

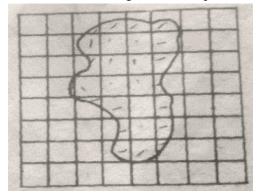
$$=15.4\pi (19.7) \text{ cm}^2$$

$$=953.48 \text{ cm}^2$$

Area of irregular shapes

The area of irregular shape cannot be found accurately, but it can be estimated. As follows;

(i) Draw a grid of unit squares on the figure or copy the figure on such a grid, see the figure below



- (ii) Count all the unit squares fully enclosed within the figure.
- (iii) Count all partially enclosed unit squares and divide the total by two, i.e., treat each one of them as half of a unit square.
- (iv) The sum of the numbers in (ii) and (ii) gives an estimate of the areas of the figure.

From the figure, the number of full squares is 9

Number of partial squares= 18

Total number of squares = 9 + 18/2

=18

Approximate area = 18 sq. units.

End of topic

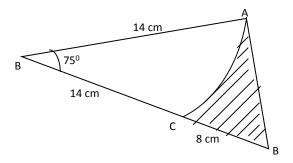
Did you understand everything?

If not ask a teacher, friends or anybody and make sure you understand before going to sleep!

Past KCSE Questions on the topic

1.) Calculate the area of the shaded region below, given that AC is an arc of a circle centre B.

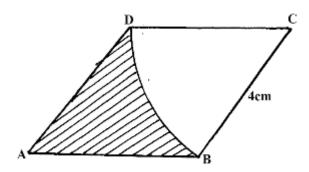
AB=BC=14cm CD=8cm and angle ABD = 75⁰ (4 mks)



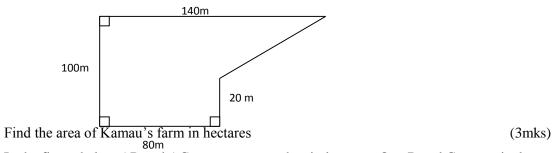
2.) The scale of a map is 1:50000. A lake on the map is 6.16cm². find the actual area of the lake in hactares.

(3mks)

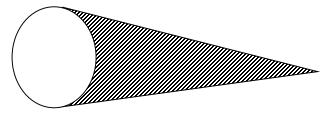
3.) The figure below is a rhombus ABCD of sides 4cm. BD is an arc of circle centre C. Given that $\angle ABC = 138^{\circ}$. Find the area of shaded region. (3mks)



4.) The figure below sows the shape of Kamau's farm with dimensions shown in meters

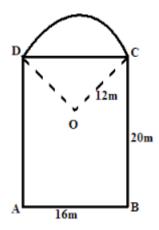


5.) In the figure below AB and AC are tangents to the circle centre O at B and C respectively, the angle $AOC = 60^{\circ}$



Calculate

- (a) The length of AC
- 6.) The figure below shows the floor of a hall. A part of this floor is in the shape of a rectangle of length 20m and width 16m and the rest is a segment of a circle of radius 12m. Use the figure to find:-



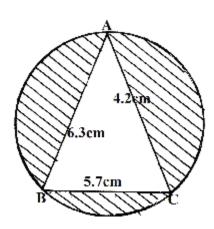
(a) The size of angle COD

(2mks)

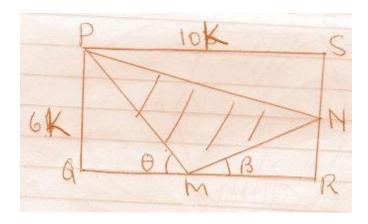
- (b) The area of figure DABCO (4mks)
- (c) Area of sector ODC (2mks)
- (d) Area of the floor of the house.

(2mks)

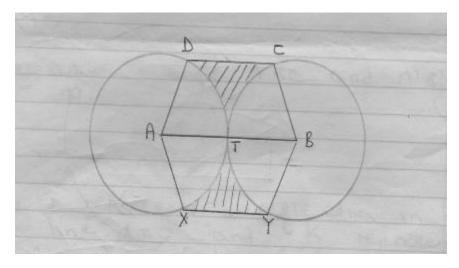
7.) The circle below whose area is 18.05cm^2 circumscribes a triangle ABC where AB = 6.3cm, BC = 5.7cm and AC = 4.8cm. Find the area of the shaded part



8.) In the figure below, PQRS is a rectangle in which PS=10k cm and PQ = 6k cm. M and N are midpoints of QR and RS respectively



- a) Find the are of the shaded region (4 marks)
- b) Given that the area of the triangle $MNR = 30 \text{ cm}^2$. find the dimensions of the rectangle (2 marks)
- Calculate the sizes of angles θ and β giving your answer to 2 decimal places (4 marks)
- 9.) The figure below shows two circles each of radius 10.5 cm with centres A and B. the circles touch each other at T



Given that angle XAD =angle YBC = 160^{0} and lines XY, ATB and DC are parallel, calculate the area of:

d) The minor sector AXTD

(2 marks)

e) Figure AXYBCD

(6marks)

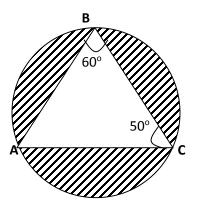
f) The shaded region

(2 marks)

10.) The floor of a room is in the shape of a rectangle 10.5 m long by 6 m wide. Square tiles of

length 30 cm are to be fitted onto the floor.

- (a) Calculate the number of tiles needed for the floor.
- (b) A dealer wishes to buy enough tiles for fifteen such rooms. The tiles are packed in cartons each containing 20 tiles. The cost of each carton is Kshs. 800. Calculate
 - (i) the total cost of the tiles.
 - (ii) If in addition, the dealer spends Kshs. 2,000 and Kshs. 600 on transport and subsistence respectively, at what price should he sell each carton in order to make a profit of 12.5% (Give your answer to the nearest Kshs.)
- 11.) The figure below is a circle of radius 5cm. Points **A**, **B** and **C** are the vertices of the triangle ABC in which \angle ABC = 60° and \angle ACB=50° which is in the circle. Calculate the area of \triangle ABC)



- 12.) Mr.Wanyama has a plot that is in a triangular form. The plot measures 170m, 190m and 210m, but the altitudes of the plot as well as the angles are not known. Find the area of the plot in hectares
- 13.) Three sirens wail at intervals of thirty minutes, fifty minutes and thirty five minutes.

 If they wail together at 7.18a.m on Monday, what time and day will they next wail together?

14.) A farmer decides to put two-thirds of his farm under crops. Of this, he put a quarter under maize and four-fifths of the remainder under beans. The rest is planted with carrots.

If 0.9 acres are under carrots, find the total area of the farm

CHAPTER FOURTEEN

VOLUME AND CAPACITY

Specific Objectives

By the end of the topic the learner should be able to:

- a.) State units of volume
- b.) Convert units of volume from one form to another
- c.) Calculate volume of cubes, cuboids and cylinders
- d.) State units of capacity
- e.) Convert units of capacity from one form to another
- f.) Relate volume to capacity
- g.) Solve problems involving volume and capacity.

Content

- a.) Units of volume
- b.) Conversion of units of volume
- c.) Volume of cubes, cuboids and cylinders
- d.) Units of capacity
- e.) Conversion of units of capacity
- f.) Relationship between volume and capacity

g.) Solving problems involving volume and capacity

Introduction

Volume is the amount of space occupied by a solid object. The unit of volume is cubic units.

A cube of edge 1 cm has a volume of 1 cm x 1 cm x 1 cm = 1 cm³.

Conversion of units of volume

A cube of side 1 m has a volume of 1 m³

But 1 m = 100 cm

1 m x 1 m x 1 m = 100 cm x 100 cm x 100 cm

Thus, $1 \text{ m} = (0.01 \text{ x } 0.01 \text{ x } 0.01) \text{ m}^3$

 $=0.000001 \,\mathrm{m}^3$

 $=1 \times 10^{-6} \text{m}^3$

A cube side 1 cm has a volume of 1 cm³.

But 1 cm=10mm

1 cm x 1 cm x 1 cm = 10 mm x 10 mm x 10 mm

Thus, 1 cm³= 1000mm³

Volume of cubes, cuboids and cylinders

Cube

A cube is a solid having six plane square faces in which the angle between two adjacent faces is a right-angle.

Volume of a cube= area of base x height

 $=l^2x l$

 $=l^3$

Cuboid

A cuboid is a solid with six faces which are not necessarily square.

Volume of a cuboid = length x width x height

=a sq. units x h

= ah cubic units.

Cylinder

This is a solid with a circular base.

```
Volume of a cylinder = area of base x height
=\pi r^2 x h
```

 $=\pi r^2 h$ cubic units

Example

Find the volume of a cuboid of length 5 cm, breadth 3 cm and height 4 cm.

Solution

```
Area of its base = 5x4 \text{ cm}^2
Volume = 5x4x3 \text{ cm}^3
```

 $= 60 \text{ cm}^3$

Example

Find the volume of a solid whose cross-section is a right- angled triangle of base 4 cm, height 5 cm and length 12 cm.

Solution

Area of cross-section = $1/2 \times 4 \times 5$

 $=10 \text{ cm}^2$

Therefore volume $=10 \times 12$

 $=120 \text{ cm}^3$

Example

Find the volume of a cylinder with radius 1.4 m and height 13 m.

Solution

Area of cross-section= 22/7 x 1.4 x 1.4

 $=6.16 \text{ m}^2$

Volume = 6.16×13

 $=80.08 \text{ m}^3$

In general, volume v of a cylinder of radius r and length l given by $v=\pi r^2 l$

Capacity

Capacity is the ability of a container to hold fluids. The SI unit of capacity is litre (l)

Conversion of units to capacity

1 centiliter (*cl*)=10 millilitre (*ml*)

1 decilitre dl = 10 centilitre (cl)

```
1 litre (l) =10 decilitres (dl)
1 Decalitre (Dl) = 10 litres (l)
1 hectolitre (Hl) =10 decalitre(Dl)
1 kilolitre (kl) =10 hectolitres (Hl)
1 kilolitre (kl)= 1000 litres (l)
1 litre (l) = 1000 millilitres (ml)
```

Relationship between volume and capacity

A cubed of an edge 10 cm holds 1 litre of liquid.

```
1 \text{ litre} = 10 \text{ cm} \times 10 \text{cm} \times 10 \text{cm}
             = 1~000~cm^3
1 \text{ m}^3 = 10^6 \text{ cm}^3
1 \text{ m}^3 = 10^3 \text{ litres}.
```

End of topic

Did you understand everything?

If not ask a teacher, friends or anybody and make sure you understand before going to sleep!

Past KCSE Questions on the topic

- 1.) All the water is poured into a cylindrical container of circular radius 12cm. If the cylinder has height 45cm, calculate the surface area of the cylinder which is not in contact with water.
- 2.) The British government hired two planes to airlift football fans to South Africa for the World cup tournament. Each plane took 10 ½ hours to reach the destination.
 - Boeng 747 has carrying capacity of 300 people and consumes fuel at 120 litres per minute. It makes 5 trips at full capacity. Boeng 740 has carrying capacity of 140 people and consumes fuel at 200 litres per minute. It makes 8 trips at full capacity. If the government sponsored the fans one way at the cost of 800 dollars per fan, calculate:
 - (a) The total number of fans airlifted to South Africa.

(2mks)

(b) The total cost of fuel used if one litre costs 0.3 dollars. (4mks)

(c) The total collection in dollars made by each plane. (2mks)

(d) The net profit made by each plane. (2mks)

- 3.) A rectangular water tank measures 2.6m by 4.8m at the base and has water to a height of 3.2m. Find the volume of water in litres that is in the tank
- 4.) Three litres of water (density1g/cm³) is added to twelve litres of alcohol (density 0.8g/cm³. What is the density of the mixture?
- 5.) A rectangular tank whose internal dimensions are 2.2m by 1.4m by 1.7m is three fifth full of milk.
 - (a) Calculate the volume of milk in litres
- (b) The milk is packed in small packets in the shape of a right pyramid with an equilateral base triangle of sides 10cm. The vertical height of each packet is 13.6cm. Full packets obtained are sold at shs.30 per packet. Calculate:
 - (i) The volume in cm³ of each packet to the nearest whole number
 - (ii) The number of full packets of milk
 - (iii) The amount of money realized from the sale of milk
 - 6.) An 890kg culvert is made of a hollow cylindrical material with outer radius of 76cm and an inner radius of 64cm. It crosses a road of width 3m, determine the density of the material ssused in its construction in Kg/m³ correct to 1 decimal place.

CHAPTER FIFTEEN

MASSS WEIGHT AND DENSITY

Specific Objectives

By the end of the topic the learner should be able to:

- a.) Define mass
- b.) State units of mass
- c.) Convert units of mass from one form to another
- d.) Define weight
- e.) State units of weight
- f.) Distinguish mass and weight
- g.) Relate volume, mass and density.

Content

- a.) Mass and units of mass
- b.) Weight and units of weight
- c.) Density
- d.) Problem solving involving real life experiences on mass, volume, density and weight.

Introduction

Mass

The mass of an object is the quantity of matter in it. Mass is constant quantity, wherever the object is, and matter is anything that occupies space. The three states of matter are solid, liquid and gas.

The SI unit of mass is the kilogram. Other common units are tone, gram and milligram.

The following table shows units of mass and their equivalent in kilograms.

Weight

The weight of an object on earth is the pull of the earth on it. The weight of any object varies from one place on the earth's surface to the other. This is because the closure the object is to the centre of the earth, the more the gravitational pull, hence the more its weight. For example, an object weighs more at sea level then on top of a mountain.

Units of weight

The SI unit of weight is newton. The pull of the earth, sun and the moon on an object is called the force of gravity due to the earth, sun and moon respectively. The force of gravity due to the earth on an object of mass 1kg is approximately equal to 9.8N. The strength of the earth's gravitational pull (symbol 'g') on an object on the surface of the earth is about 9.8N/Kg.

Weight of an object = mass of an object x gravitation

Weight N = mass kg x g N/kg

Density

The density of a substance is the mass of a unit cube of the substance. A body of mass (m)kg and volume (v) m^3 has:

- (i) Density (d) = mass (m)/density (d)
- (ii) Mass (m)= density (d) x volume (v)
- (iii) Volume (v) = mass (m) / density (d)

Units of density

The SI units of density is kg/m³. the other common unit is g/cm³

```
1 \text{ g/cm}^3 = 1 000 \text{kg/m}^3
```

Example

Find the mass of an ice cube of side 6 cm, if the density of the ice is 0.92 g/cm³.

Solution

```
Volume of cube = 6x6x6 = 216 \text{ cm}^3
```

```
Mass = density x volume
=216 x 0.92
=198.72 g
```

Example

Find the volume of cork of mass 48 g. given that density of cork is 0.24 g/cm³

Solution

```
Volume = mass/density
=48/0.24
=200 \text{cm}^3
```

Example

The density of iron is 7.9 g/cm³. what is this density in kg/m³

Solution

```
1 g/cm<sup>3</sup> = 1 000 kg/m<sup>3</sup>
7.9 g/cm<sup>3</sup> = 7.9 x 1000/1
= 7 900kg/m<sup>3</sup>
```

Example

A rectangular slab of glass measures 8 cm by 2 cm by 14 cm and has a mass of 610g. calculate the density of the glass in kg/m³

Solution

Volume of the slab = 8x 2x14

 $=224 \text{ cm}^3$ Mass of the slab = 610 g Density = 610/244 $= 2.5 \times 1000 \text{ kg} = 25000 \text{kg/m}^3$ End of topic

Did you understand everything? If not ask a teacher, friends or anybody and make sure you understand before going to sleep!

Past KCSE Questions on the topic

- 1.) A squared brass plate is 2mm thick and has a mass of 1.05kg. The density of brass is 8.4g/cm.

 Calculate the length of the plate in centimeters. (3mks)
- 2.) A sphere has a surface area 18cm². Find its density if the sphere has a mass of 100g. (3mks)
- 3.) Nyahururu Municipal Council is to construct a floor of an open wholesale market whose area is 800m^2 . The floor is to be covered with a slab of uniform thickness of 200mm. In order to make the slab, sand, cement and ballast are to be mixed such that their masses are in the ratio 3:2:3. The mass of dry slab of volume 1m^3 is 2000kg. Calculate
 - (a) (i) The volume of the slab

(2mks)

(ii) The mass of the dry slab.

(2mks)

(iii) The mass of cement to be used.

(2mks)

- (b) If one bag of the cement is 50kg, find the number of bags to be purchased. (1mk)
- (c) If a lorry carries 10 tonnes of ballast, calculate the number of lorries of ballast to be purchased.

(3mks)

4.) A sphere has a surface area of 18.0cm². Find its density if the sphere has a mass of 100 grammes.

(3 mks)

- 5.) A piece of metal has a volume of 20 cm³ and a mass of 300g. Calculate the density of the metal in kg/m³.
- 6.) 2.5 litres of water density 1g/cm³ is added to 8 litres of alcohol density 0.8g/cm³. Calculate the density of the mixture



TIME

Specific Objectives

By the end of the topic the learner should be able to:

- a.) Convert units of time from one form to another
- b.) Relate the 12 hour and 24 hour clock systems
- c.) Read and interpret travel time-tables
- d.) Solve problems involving travel time tables.

Content

- a.) Units of time
- b.) 12 hour and 24 hour clock systems
- c.) Travel time-tables
- d.) Problems involving travel time tables

Introduction

Units of time

1 week = 7 days

1 day = 24 hours

1 hour = 60 minutes

1 minutes = 60 seconds

Example

How many hours are there in one week?

Solution

1 week = 7 days

1 day = 24 hours

1 week = (7×24) hours

=168 hours

Example

Covert 3h 45 min into minutes

Solution

```
1 h = 60 min

3 h = (3x60) min

3h 45min =((60x3) + 45) min

=(180+45) min
```

 $=225 \min$

Example

Express 4h 15 min in sec

Solution

```
1 hour = 60 min

1 min= 60 sec

4h 15 min=(4x60+15) min

=240+15 min

=255 min

=255 x 60 sec

=15 300 sec.
```

The 12 and the 24 hour systems

In the 12 hour system, time is counted from midnight. The time from midnight to midday is written as am . while that from midday to midnight is written as pm.

In the 24 hour system, time is counted from midnight and expressed in hours.

Travel time table

Travel timetables shows the expected arrival and departure time for vehicles. Ships, aeroplanes, trains.

Example

The table below shows a timetable for a public service vehicle plying between two towns A and D via towns B and C.

Town	Arrival time	Departure time
A	10.40 P.M	8.20 A.M
B	2.30 P.M	11.00 A.M
C	4.00 P.M	2.50 P.M

- (a) What time does the vehicle leave town A?
- (b) At what time does it arrive in town D?
- (c) How long does it take to travel from town A to D.
- (d) What time does the vehicle takes to travel from town C to D?

Solution

- (a) 8.20 A.M
- (b) 4.00 P.M
- (c) Arrival time in town D was 4.00 p.m. it departure from town A was 8.20 a.m.

Time taken= (12.00-8.20 +4 h) =3 h 40 min +4 h

= 7 h 40 min

(d) The vehicle arrived in town D at 4.00 p.m. it departed from town C at 2.50 p.m.

Time taken = 4.00-2.50= 1 h 10 min

End of topic

Did you understand everything?

If not ask a teacher, friends or anybody and make sure you understand before going to sleep!

Past KCSE Questions on the topic

 A van travelled from Kitale to Kisumu a distance of 160km. The average speed of the van for the first 100km was 40km/h and the remaining part of the journey its average speed was 30km/h.
 Calculate the average speed for the whole journey.

(3 mks)

2.) A watch which looses a half-minute every hour was set to read the correct time at 0545h on Monday. Determine the time, in the 12 hour system, the watch will show on the following Friday at 1945h.

3.) The timetable below shows the departure and arrival time for a bus plying between two towns $\,$ M and $\,$ R, 300km apart $\,$ 0710982617

Town	Arrival	Departure
M		0830h
N	1000h	1020h
P	1310h	1340h
Q	1510h	1520h
R	1600h	

- (a) How long does the bus take to travel from town \mathbf{M} to \mathbf{R} ?
- (b) What is the average speed for the whole journey?

CHAPTER SEVENTEEN

LINEAR EQUATIONS

Specific Objectives

By the end of the topic the learner should be able to:

- a.) solve linear equations in one unknown
- b.) solve simultaneous linear equations by substitution and elimination
- c.) Linear equations in one and two unknown.

Content

- a.) Linear equations in one unknown
- b.) Simultaneous linear equations
- c.) Linear equations in one and two unknowns from given real life situations

Introduction

Linear equations are straight line equations involving one or two unknowns. In this chapter, we will deal with the formation and solving of such equations consider the following cases.

Example

Solve for the unknowns in each of the following equations

$$3x + 4 = 10$$

$$\frac{x}{3} - 2 = 4$$

$$\frac{p+5}{3} = 5/4$$

Solution

$$3x + 4 = 10$$

$$3x + 4 - 4 = 10 - 4$$
 (to make x the subject subtract 4 on both sides)

$$3x = 6$$

$$X = 2$$

$$\frac{x}{3} - 2 = 4$$

$$\frac{x}{3}$$
 - 2 + 2 = 4 + 2 (to make x the subject add 2 to both sides)

$$\frac{x}{3} = 6$$

$$X = 18$$

$$\frac{p+5}{3} = \frac{5}{4}$$

$$3 \times (\frac{p+5}{3}) = \frac{5}{4} \times 3$$

$$P+5=\frac{5}{4} x3$$

$$4(p+5) = \frac{5}{4} \chi 4$$

$$4p + 20 = 15$$

$$4p = -5$$

$$P = \frac{-5}{4}$$

$$= -1 \frac{1}{4}$$

Solving an equation with fractions or decimals, there is an option of clearing the fractions or decimals in order to create a simpler equation involving whole numbers.

- 1. To clear fractions, multiply both sides of the equation (distributing to all terms) by the LCD of all the fractions.
- 2. To clear decimals, multiply both sides of the equation (distributing to all terms) by the lowest power of 10 that will make all decimals whole numbers.

Steps for Solving a Linear Equation in One Variable:

- 1. Simplify both sides of the equation.
- 2. Use the addition or subtraction properties of equality to collect the variable terms on one side of the equation and the constant terms on the other.
- 3. Use the multiplication or division properties of equality to make the coefficient of the variable term equal to 1.
- 4. Check your answer by substituting your solution into the original equation.

Note:

All other linear equations which have only one solution are called conditional.

Example

Solve for the unknown in each in of the following equations

a.)
$$\frac{x+1}{2} - \frac{x-1}{3} = 1/8$$

b.) $\frac{3y}{2} - \frac{14y-3}{5} = \frac{y-1}{4}$
c.) $1 - \frac{y}{2} - 2\left(\frac{y-3}{2}\right) = 0$

Solution

a.)
$$\left(\frac{x+1}{2}\right)x24 - \left(\frac{x-1}{3}\right)x24 = 1/8 \times 24$$
 (multiply both sides by the L.C.M of 2,3 and 8) $12(x+1)-8(x-2)=3$ $12x+12-8x-16=3$

$$4x + 28 = 3$$

$$4x = -25$$

$$x = -6\frac{1}{4}$$

b.)
$$\frac{3y}{2}x20 - \frac{(14y-3)}{5}x20 = \left(\frac{y-1}{4}\right)x20$$
 (multiply both sides by the L.C.M of 2 5 and 4) 30y-4 (14y-3) = 5 (y-4)

$$-26 + 12 = 5y - 20$$

$$31 y = 32$$

$$y = \frac{32}{31} = 1\frac{1}{31}$$

c.)
$$(1 \times 2) - (\frac{y}{2} \times 2) - 2(\frac{y-3}{2}) \times 2 = 0 \times 2$$

 $2 - y - 2(y-3) = 0$

$$2 - y - 2y + 6 = 0$$
$$8 - 3y = 0$$

$$3y = \frac{8}{3} = 2\frac{2}{3}$$

Problems leading to Linear equations

Equations are very useful in solving problems. The basic technique is to determine what quantity it is that we are trying to find and make that the unknown. We then translate the problem into an equation and solve it. You should always try to minimize the number of unknowns. For example, if we are told that a piece of rope 8 metres long is cut in two and one piece is x metres, then we can write the remaining piece as (8 - x) metres, rather than introducing a second unknown.

Word problems

Equations arise in everyday life. For example Mary bought a number of oranges from Anita's kiosk. She then went to Marks kiosk and bought the same number of oranges. Mark them gave her three more oranges. The oranges from the two kiosks were wrapped in different paper bags. On reaching her house, she found that a quarter of the first Lot oranges and a fifth of the second were bad. If in total six oranges were bad, find how many oranges she bought from Anita's kiosk.

Solution

Let the number of oranges bought at Anita's kiosk be x.

Then, the number of oranges obtained from Marks kiosk will be x + 3.

Number of Bad oranges from Marks kiosk was $\frac{x+3}{5}$.

Total number of Bad oranges is equal to $=\frac{x}{4} + \frac{x+3}{5}$

Thus,
$$=\frac{x}{4} + \frac{x+3}{5} = 6$$

Multiply each term of the equation by 20 (L.C.M of 4 and 5) to get rid of the denominator.

$$=20 \times \frac{x}{4} + 20 \left(\frac{x+3}{5}\right) = 6 \times 20$$

$$5x + 4(x + 3) = 120$$

5x + 4x + 12 = 120 (Removing brackets)

Subtracting 12 from both sides.

$$9x = 108$$

$$X = 12$$

Thus, the number of oranges bought from Anita's kiosk was 12.

Note:

If any operation is performed on one side of an equation, it must also be performed on the other side.

Example

Solve for x in the equation:
$$\frac{x+3}{2} - \frac{x-4}{3} = 4$$

Solution

Eliminate the fractions by multiplying each term by 6 (L.C.M, of 2 and 3).

$$6x\left(\frac{x+3}{2}\right) - 6\left(\frac{x-4}{3}\right) = 4x6$$

$$3(x+3)-2(x-4)=24$$

3x + 9 - 2x + 8 = 24(note the change in sigh when the bracket are removed)

$$x + 17 = 24$$

$$x = 7$$

Linear Equations in Two Unknowns

Many problems involve finding values of two or more unknowns. These are often linked via a number of linear equations. For example, if I tell you that the sum of two numbers is 89 and their difference is 33, we can let the larger number be x and the smaller one y and write the given information as a pair of equations:

$$x + y = 89(1)$$

$$x - Y = 33.$$
 (2)

These are called simultaneous equations since we seek values of x and y that makes both equations true simultaneously. In this case, if we add the equations we obtain 2x = 122, so x = 61. We can then substitute this value back into either equation, say the first, then 61 + y = 89 giving y = 28.

Example

The cost of two skirts and three blouses is sh 600. If the cost of one skirt and two blouses of the same quality sh 350, find the cost of each item.

Solution

Let the cost of one skirt be x shillings and that of one blouse be y shillings. The cost of two skirts and three blouses is 2x + 3y shillings.

The cost of one skirt and two blouses is x + 2y shillings.

So,
$$2x + 3y = 600$$
....(I)

$$X + 2y = 350$$
(II)

Multiplying equation (II) by 2 to get equation (III).

$$2x + 4y = 700$$
 (III).

$$2x + 3y = 600...$$
 (I)

Subtracting equation (I) from (II), y = 100.

From equation (II),

$$X + 2y = 350$$
 but $y = 100$

$$X + 200 = 350$$

$$X = 150$$

Thus the cost of one skirt is 150 shillings and that of a blouse is 100 shillings.

In solving the problem above, we reduced the equations from two unknowns to a single unknown in y by eliminating. This is the elimination method of solving simultaneous equations.

Examples

a.)
$$a + b = 7$$

$$a - b = 5$$

b.)
$$3a + 5b = 20$$

$$6a - 5b = 12$$

c.)
$$3x + 4y = 18$$

$$5x + 6y = 28$$

Solutions

a.)

$$a + b = 7 - - - - - (i)$$

$$a - b = 5 - - - - - (ii)$$

Adding I to II

$$2a = 12 \rightarrow a = 6$$

Subtracting II from I;

$$2b = 2$$

$$b = 1$$

b.)
$$3a + 5b = 20 - - - - - (i)$$

$$6a - 5b = 12 - - - - - (ii)$$

To eliminate b, we simply add the two equations.

$$9a = 32$$

$$a = \frac{32}{9}$$

Find the value of b

c.)
$$3x + 4y = 18 - - - - - - - - (i)$$

 $5x + 6y = 28 - - - - - - - (ii)$

Here it is not easy to know the obvious unknown to be eliminated

To eliminate (I) by 5 and (II) by 3 to get (III) and (IV) respectively and subtracting (IV) from (III);

d.)
$$15x + 20y = 90 - - - - - - - - (iii)$$

 $15x + 18y = 84 - - - - - - - - (iv)$
 $2y = 6$

Therefore y = 3

Substituting y = 3 in (I);

$$3x + 12 = 18$$

Therefore x = 2

Note that the L.C.M of 3 and 5 is 15.

To eliminate y;

Multiplying (I) by 3, (II) by 2 to get (V) and (VI) and Subtracting (V) from (VI);

$$9x + 12y = 54 - - - - - - (v)$$

$$10x + 12y = 56 - - - - - - (vi)$$

Subtracting x = 2 in (ii);

$$10 + 6y = 28$$

$$6y = 18$$

Therefore y = 3.

Note:

- ✓ It is advisable to study the equation and decide which variable is easier to eliminate.
- ✓ It is necessary to check your solution by substituting into the original equations.

Solution by substitution

$$2x + 3y = 600 - - - - - - (i)$$

$$x + 2y = 350 - - - - - - - (ii)$$

Taking equation (II) alone;

$$x + 2y = 350$$

Subtracting 2y from both sides;

$$x = 350 - 2y - - - - - - - (iii)$$

Substituting this value of x in equation(i);

$$2(350 - 2y) + 3y = 600$$

$$700 - 4y + 3y = 600$$

$$Y = 100$$

Substituting this value of y in equation(iii);

$$x = 350 - 2y$$

$$=350-200$$

$$x = 150$$

This method of solving simultaneous equations is called the substitution method

End of topic

Did you understand everything?

If not ask a teacher, friends or anybody and make sure you understand before going to sleep!

Past KCSE Questions on the topic

- 1. A cloth dealer sold 3 shirts and 2 trousers for Kshs 840 and 4 shirts and 5 trousers for Kshs 1680 find the cost of 1 shirt and the cost of 1 trouser
- 2. Solve the simultaneous equations

$$2x - y = 3$$

$$x^2 - xy = -4$$

- 3. The cost of 5 skirts and blouses is Kshs 1750. Mueni bought three of the skirts and one of the blouses for Kshs 850. Find the cost of each item.
- 4. Akinyi bought three cups and four spoons for Kshs 324. Wanjiru bought five cups and Fatuma bought two spoons of the same type as those bought by Akinyi, Wanjiku paid Kshs 228 more than Fatuma. Find the price of each cup and each spoon.
- 5. Mary has 21 coins whose total value is Kshs. 72. There are twice as many five shillings coins as there are ten shilling coins. The rest one shillings coins. Find the number of ten shillings coins that Mary has. (4 mks)
- 6. The mass of 6 similar art books and 4 similar biology books is 7.2 kg. The mass of 2 such art books and 3 such biology books is 3.4 kg. Find the mass of one art book and the mass of one biology book
- 7. Karani bought 4 pencils and 6 biros pens for Kshs 66 and Tachora bought 2 pencils and 5 biro pens for Kshs 51.
- (a) Find the price of each item
- (b) Musoma spent Kshs. 228 to buy the same type of pencils and biro pens if the number of biro pens he bought were 4 more than the number of pencils, find the number of pencils bought.
- 8. Solve the simultaneous equations below

$$2x - 3y = 5$$

$$-x + 2y = -3$$

9. The length of a room is 4 metres longer than its width. Find the length of the room if its area is 32m^2

- 10. Hadija and Kagendo bought the same types of pens and exercise books from the same types of pens and exercise books from the same shop. Hadija bought 2 pens and 3 exercise books for Kshs 78. Kagendo bought 3 pens and 4 exercise books for Kshs 108. Calculate the cost of each item
- 11. In fourteen years time, a mother will be twice as old as her son. Four years ago, the sum of their ages was 30 years. Find how old the mother was, when the son was born.
- 12. Three years ago Juma was three times as old as Ali. In two years time the sum of their ages will be 62. Determine their ages.
- 13. Two pairs of trousers and three shirts costs a total of Kshs 390. Five such pairs of trousers and two shirts cost a total of Kshs 810. Find the price of a pair of trousers and a shirt.
- 14. A shopkeeper sells two- types of pangas type x and type y. Twelve x pangas and five type y pangas cost Kshs 1260, while nine type x pangas and fifteen type y pangas cost 1620. Mugala bought eighteen type y pangas. How much did he pay for them?

CHAPTER EIGHTEEN

COMMERCIAL ARITHMETIC

Specific Objectives

By the end of the topic the learner should be able to:

- a.) State the currencies of different countries
- b.) Convert currency from one form into another given the exchange rates
- c.) Calculate profit and loss
- d.) Express profit and loss as percentages
- e.) Calculate discount and commission
- f.) Express discount and commission as percentage.

Content

- a.) Currency
- b.) Current currency exchange rates
- c.) Currency conversion
- d.) Profit and loss
- e.) Percentage profit and loss
- f.) Discounts and commissions
- g.) Percentage discounts and commissions

Introduction

In commercial arithmetic we deal with calculations involving business transaction. The medium of any business transactions is usually called the currency. The Kenya currency consist of a basic unit called a shilling.100 cents are equivalent to one Kenyan shillings, while a Kenyan pound is equivalent to twenty Kenya shillings.

Currency Exchange Rates

The Kenyan currency cannot be used for business transactions in other countries. To facilitate international trade, many currencies have been given different values relative to another. These are known as exchange rates.

The table below shows the exchange rates of major international currencies at the close of business on a certain day in the year 2015. The buying and selling column represents the rates at which banks buy and sell these currencies.

Note

The rates are not always fixed and they keep on charging. When changing the Kenyan currency to foreign currency, the bank sells to you. Therefore, we use the selling column rate. Conversely when changing foreign currency to Kenyan Currency, the bank buys from you, so we use the buying column rate.

Currency	Buying	Selling	
DOLLAR		102.1472	102.3324
STG POUND		154.0278	154.3617
EURO		109.6072	109.8522
SA RAND		7.3332	7.3486
KES / USHS		33.0785	33.2363
KES / TSHS		20.9123	21.0481
KES / RWF		7.2313	7.3423
AE DIRHAM		27.8073	27.8653
CAN\$		77.6018	77.7661
JAPNESE YE	N	84.0234	84.1964
SAUDI RIYA	L	27.2284	27.2959
CHINESE YU	JAN	16.0778	16.1082
AUSTRALIA	N \$	71.8606	72.0420

Example

Convert each of the following currencies to its stated equivalent

- a.) Us \$305 to Ksh
- b.) 530 Dirham to euro

Solution

a.) The bank buys Us 1 at Ksh 102.1472 Therefore US \$ 305 = Ksh (102.1472 x 305)

= Ksh 31,154.896

= Ksh 31,154.00 (To the nearest shillings)

The bank buys 1 Dirham at Ksh 27.8073

Therefore 530 Dirham = Ksh (21.8073×530)

The bank sells 1 Euro at 109.8522

Therefore 530 Dirham = 11, 557/109.8522

= 105.170 Euros

Example

During a certain month, the exchange rates in a bank were as follows;

	Buying (Ksh.)	Selling (Ksh.)
1 US \$	91.65	91.80
1 Euro	103.75	103.93

A tourist left Kenya to the United States with Ksh.1 000,000.On the airport he exchanged all the money to dollars and spent 190 dollars on air ticket. While in US he spent 4500 dollars for upkeep and proceeded to Europe. While in Europe he spent a total of 2000 Euros. How many Euros did he remain with? (3marks)

Solution

$$\frac{1000000}{91.80} = 10,893.25$$

$$10,893.25 - (190 + 4500) = 6203.25$$

$$6203.25 \times 91.65 = 568,278.86$$

$$\frac{568,527.86}{103.93} = 5,470.30$$

$$5470.30 - 2000 = 3,470.30$$

Profit and Loss

The difference between the cost price and the selling price is either profit or loss. If the selling price is greater than the cost price, the difference is a profit and if the selling price is less than the total cost price, the difference is a loss.

Note

Selling price - cost price = profit

Percentage profit =
$$\frac{Profit}{Cost\ price} \times 100$$

Cost price - selling price = loss

Percentage loss =
$$\frac{Profit}{Cost \ price}$$
 x 100

Example

Ollie bought a cow at sh 18000 and sold it at sh 21000. What percentage profit did he make?

Solution

Selling price = $sh\ 21000$

Cost price = sh 18000

Profit = sh (21000 - 18, 000)

= sh 3000

Percentage profit = $\frac{3000}{18000}$ x 100

$$=16\frac{2}{3}\%$$

Example

Johnny bought a dress at 3500 and later sold it at sh.2800.what percentage loss did he incurs?

Cost price = sh 3500

Selling price = sh 2800

Loss = sh (3500 - 2800)

= Sh 700

Percentage loss = $\frac{700}{3500}$ x 100 = 20%

Discount

A shopkeeper may decide to sell an article at reduced price. The difference between the marked price and the reduced price is referred to as the discount. The discount is usually expressed as a percentage of the actual price.

Example

The price of an article is marked at sh 120.A discount is allowed and the article sold at sh 96.Calculate the percentage discount.

Solution

Actual price = sh 120.00

Reduced price = sh 96.00

Discount = sh (120.00 - 96.00)

=sh 24

Percentage discount = $24/120 \times 100$

= sh 20%

Commission

A commission is an agreed rate of payment, usually expressed as a percentage, to an agent for his services.

Example

Mr. Neasa, a salesman in a soap industry, sold 250 pieces of toilet soap at sh 45.00 and 215 packets of determining at sh 75.00 per packet. If he got a 5% commission on the sales, how much money did he get as commission?

Solution

Sales for the toilet soap was $250 \times 45 = \text{sh } 11250$

Sales for the detergent was $215 \times 75 = \text{sh } 16125$

Commission =
$$\frac{5}{100}$$
 (11250 + 16125)

$$\frac{5}{100}x\ 27375 = sh1368$$

Example

A salesman earns a basic salary of sh. 9,000 per month. In addition he is also paid a commission of 5% for sales above sh. 15,000. In a certain month he sold goods worth sh. 120,000 at a discount of 2½%. Calculate his total earnings that month.

[3 marks]

Solution

net after discount
$$\frac{97.5}{100} \times 120,000 = 17,000$$

sales above sh.
$$15,000 = 117,000 - 15,000$$

= kshs. 102,000 commission
$$\frac{5}{100} \times 102,000 = 5,100$$

totl earnings =
$$9,000 + 5,100$$

= kshs 14,100

End of topic

Did you understand everything?

If not ask a teacher, friends or anybody and make sure you understand before going to sleep!

Past KCSE Questions on the topic

- 1. The cash prize of a television set is Kshs 25000. A customer paid a deposit of Kshs 3750. He repaid the amount owing in 24 equal monthly installments. If he was charged simple interest at the rate of 40% p.a how much was each installment?
- 2. Mr Ngeny borrowed Kshs 560,000 from a bank to buy a piece of land. He was required to repay the loan with simple interest for a period of 48 months. The repayment amounted to Kshs 21,000 per month.

Calculate

- (a) The interest paid to the bank
- (b) The rate per annum of the simple interest
- 3. A car dealer charges 5% commission for selling a car. He received a commission of Kshs 17,500 for selling car. How much money did the owner receive from the sale of his car?
- 4. A company saleslady sold goods worth Kshs 240,000 from this sale she earned a commission of Kshs 4,000
 - (a) Calculate the rate of commission
 - (b) If she sold good whose total marked price was Kshs 360,000 and allowed
 - a discount of 2% calculate the amount of commission she received.
- 5. A business woman bought two bags of maize at the same price per bag. She discovered that one bag was of high quality and the other of low quality. On the high quality bag she made a profit by selling at Kshs 1,040, whereas on the low quality bag she made a loss by selling at Kshs 880. If the profit was three times the loss, calculate the buying price per bag.
- 6. A salesman gets a commission of 2. 4 % on sales up to Kshs 100,000. He gets an additional commission of 1.5% on sales above this. Calculate the commission he gets on sales worth Kshs 280,000.
- 7. Three people Koris, Wangare and Hassan contributed money to start a business. Korir contributed a quarter of the total amount and Wangare two fifths of the remainder. Hassan's contribution was one and a half times that of Koris. They borrowed the rest of the money from the bank which was Kshs 60,000 less than Hassan's contribution. Find the total amount required to start the business.
- 8. A Kenyan tourist left Germany for Kenya through Switzerland. While in Switzerland he bought a watch worth 52 deutsche Marks. Find the value of the watch in:
 - (a) Swiss Francs.
 - (b) Kenya Shillings

Use the exchange rtes below:

1 Swiss Franc = 1.28 Deutsche Marks.

1 Swiss Franc = 45.21 Kenya Shillings

9. A salesman earns a basic salary of Kshs. 9000 per month In addition he is also paid a commission of 5% for sales above Kshs 15000

In a certain month he sold goods worth Kshs. 120, 000 at a discount of $2\frac{1}{2}$ %. Calculate his total earnings that month

10. In this question, mathematical table should not be used

A Kenyan bank buys and sells foreign currencies as shown below

Buying Selling

(In Kenya shillings) In Kenya Shillings

1 Hong Kong dollar 9.74 9.77

1 South African rand 12.03 12.11

A tourists arrived in Kenya with 105 000 Hong Kong dollars and changed the whole amount to Kenyan shillings. While in Kenya, she pent Kshs 403 897 and changed the balance to South African rand before leaving for South Africa. Calculate the amount, in South African rand that she received.

11. A Kenyan businessman bought goods from Japan worth 2, 950 000 Japanese yen. On arrival in Kenya custom duty of 20% was charged on the value of the goods.

If the exchange rates were as follows

1 US dollar = 118 Japanese Yen

1 US dollar = 76 Kenya shillings

Calculate the duty paid in Kenya shillings

12. Two businessmen jointly bought a minibus which could ferry 25 paying passengers when full. The fare between two towns A and B was Kshs. 80 per passenger for one way. The minibus made three round trips between the two towns daily. The cost of fuel was Kshs 1500 per day. The driver and the conductor were paid daily allowances of Kshs 200 and Kshs 150 respectively.

A further Kshs 4000 per day was set aside for maintenance.

- (a) One day the minibus was full on every trip.
 - (i) How much money was collected from the passengers that day?
 - (ii) How much was the net profit?
- (b) On another day, the minibus was 80% on the average for the three round trips. How much did each business get if the days profit was shared in the ratio 2:3?

- 13. A traveler had sterling pounds 918 with which he bought Kenya shillings at the rate of Kshs 84 per sterling pound. He did not spend the money as intended. Later, he used the Kenyan shillings to buy sterling pound at the rate of Kshs. 85 per sterling pound. Calculate the amount of money in sterling pounds lost in the whole transaction.
- 14. A commercial bank buys and sells Japanese Yen in Kenya shillings at the rates shown below Buying 0.5024

Selling 0.5446

A Japanese tourist at the end of his tour of Kenya was left with Kshs. 30000 which he converted to Japanese Yen through the commercial bank. How many Japanese Yen did he get?

- 15. In the month of January, an insurance salesman earned Kshs. 6750 which was commission of 4.5% of the premiums paid to the company.
 - (a) Calculate the premium paid to the company.
 - (b) In February the rate of commission was reduced by 66²/₃% and the premiums reduced by 10% calculate the amount earned by the salesman in the month of February
- 16. Akinyi, Bundi, Cura and Diba invested some money in a business in the ratio of 7:9:10:14 respectively. The business realized a profit of Kshs 46800. They shared 12% of the profit equally and the remainder in the ratio of their contributions. Calculate the total amount of money received by Diba.
- 17. A telephone bill includes Kshs 4320 for a local calls Kshs 3260 for trank calls and rental charge Kshs 2080. A value added tax (V.A.T) is then charged at 15%, Find the total bill.
- 18. During a certain period. The exchange rates were as follows

1 sterling pound = Kshs 102.0

1 sterling pound = 1.7 us dollar

1 U.S dollar = Kshs 60.6

A school management intended to import textbooks worth Kshs 500,000 from UK. It changed the money to sterling pounds. Later the management found out that the books the sterling pounds to dollars. Unfortunately a financial crisis arose and the money had to be converted to Kenya shillings. Calculate the total amount of money the management ended up with.

19. A fruiterer bought 144 pineapples at Kshs 100 for every six pineapples. She sold some of them at Kshs 72 for every three and the rest at Kshs 60 for every two.

If she made a 65% profit, calculate the number of pineapples sold at Kshs 72 for every three.

CHAPTER TEN

COORDINATES AND GRAPHS

Specific Objectives

By the end of the topic the learner should be able to:

- a.) Draw and label the complete Cartesian plane
- b.) Locate and plot points on the Cartesian plane
- c.) Choose and use appropriate scale for a given data
- d.) Make a table of values for a given linear relation
- e.) Use values to draw a linear graph
- f.) Solve simultaneous linear equations graphically
- g.) Draw, read and interpret graphs.

Content

- a.) Cartesian plane
- b.) Cartesian co-ordinate
- c.) Points on the Cartesian plane
- d.) Choice of appropriate scale
- e.) Table of values for a given linear relation
- f.) Linear graphs
- g.) Graphical solutions of simultaneous linear equations
- h.) Interpretation of graphs.

Introduction

The position of a point in a plan is located using an ordered pair of numbers called co- ordinates and written in the form (x, y). The first number represents the distance along the x axis and is called the x co-ordinates. The second number represents distance along the y axis and it's called the y coordinates.

The x and y coordinates intersects at (0, 0) a point called the origin. The system of locating points using two axes at right angles is called Cartesian plan system.

To locate a point on the Cartesian plane, move along the *x*-axis to the number indicated by the *x*-coordinate and then along the *y*-axis to the number indicated by the *y*-coordinate. For example, to locate the point with coordinates (1, 2), move 1 unit to the right of the origin and then 2 units up

The Cartesian plan The Graph of a straight line

Consider the Linear equation y = 2x + 1. Some corresponding values of x and y are given in the table below. If we plot the points we notice that they all lie in a straight line.

Solution

Step 1 write the rule y = 2x + 1

Step 2 Draw a table and choose simple x values

Step 3 Use the rule to find each y value and enter then in the table.

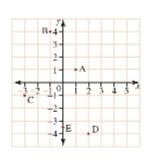
E.g. when x = -2, $y = 2 \times -2 + 1 = -3$.

when x = -1, $y = 2 \times -1 + 1 = -1$

step 4 Draw a Cartesian plan and plot the points.

Step 5 Join the points to form a straight line and label the graph

Write the Cartesian coordinates of the points A to E marked on the Cartesian plane at right.



THINK

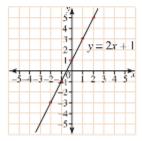
- Trace along the x-axis to find the first number, and then along the y-axis to find the second number.
 Point A is at 1 on the x-axis and 1 on the y-axis.
 Point B is at -1 on the x-axis and 4 on the y-axis.
 Point C is at -3 on the x-axis and -1 on the y-axis.
 Point D is at 2 on the x-axis and -4 on the y-axis.
 Point E is at 0 on the x-axis and -3½ on the y-axis.
- Write each point as a pair of coordinates.

A(1, 1) B(-1, 4) C(-3, -1)
D(2, -4) E(0,
$$-3\frac{1}{2}$$
)

WRITE

y = 2x + 1

x	-2	-1	0	1	2
у	-3	-l	1	3	5

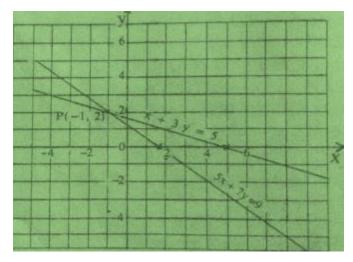


Note:

- ✓ Two points are sufficient to determine a straight line, but we use the third point as a check.
- ✓ It is advisable to choose points which can be plotted easily.

Graphing solutions of simultaneous linear equation

The graphs of the form ax + by = c represents a straight line. When two linear equations are represented on the same Cartesian plan, their graphs may or may not intersect. For example, in solving the simultaneous equations x + 3y = 5 and 5x + 7y = 9 graphically, the graphs of the two equation are drawn.



The two lines intersect at p (-1, 2). The solution to the simultaneous equations is, therefore, x = -1 and y = 2.

General graphs

Graphs are applied widely in science and many other fields. The graphs should theirfoe be drawn in a way that convey information easily and accurately. The most of important technique of drawing graphs is the choice of appropriate scale.

A good scale is one which uses most of the graph page and enables us to plot points and read off values easily and accurately.

Avoid scales which:

- ✓ Give tiny graphs.
- ✓ Cannot accommodate all the data in the table.

It is good practice to:

- ✓ Label the axes clearly.
- ✓ Give the title of the graph.

End of topic

Did you understand everything?

If not ask a teacher, friends or anybody and make sure you understand before going to sleep!

Revision Questions on the topic

1.) Copy and complete the table and hence draw the corresponding graph.

$$Y = 4x + 3$$

X	-2	-1	0	1	2
у					

- 2.) Draw the graph of the following:
 - a.) Y + 2x = 5
 - b.) y/2 + 2x = 5

CHAPTER TWENTY



Specific Objectives

By the end of the topic the learner should be able to:

- a.) Name and identify types of angles
- b.) Solve problems involving angles on a straight line
- c.) Solve problems involving angles at a point
- d.) Solve problems involving angles on a transversal cutting parallel lines
- e.) State angle properties of polygons
- f.) Solve problems involving angle properties of polygons
- g.) Apply the knowledge of angle properties to real life situations.

Content

- a.) Types of angles
- b.) Angles on a straight line
- c.) Angles at a point
- d.) Angles on a transversal (corresponding, alternate and allied angles)
- e.) Angle properties of polygons
- f.) Application to real life situations.

Introduction

A flat surface such as the top of a table is called a plane. The intersection of any two straight lines is a point.

Representation of points and lines on a plane

A point is represented on a plane by a mark labelled by a capital letter. Through any two given points on a plane, only one straight line can be drawn.

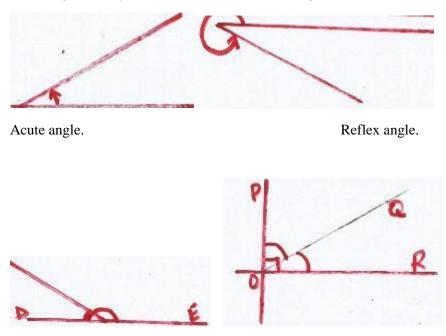


The line passes through points A and B and hence can be labelled line AB.

Types of Angles

Obtuse angle

When two lines meet, they form an angle at a point. The point where the angle is formed is called the vertex of the angle. The symbol < is used to denote an angle.



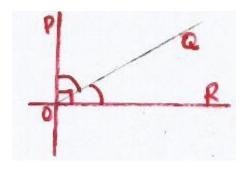
To obtain the size of a reflex angle which cannot be read directly from a protractor, the corresponding acute or obtuse angle is subtracted from 360° . If any two angles X and Y are such that:

i.) Angle X + angle Y =90 0 , the angles are said to be complementary angles. Each angle is then said to be the complement of the other.

Right angle

ii.) Angle X + angle Y = 180 0 , the angles are said to be supplementary angles. Each angle is then said to be the supplement of the other.

In the figure below < POQ and < ROQ are a pair of complementary angles.

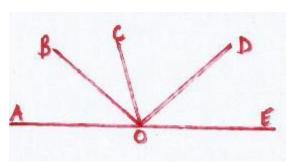


In the figure below <DOF and < FOE are a pair of supplementary angles.



Angles on a straight line.

The below shows a number of angles with a common vertex 0.AOE is a straight line.



Two angles on either side of a straight line and having a common vertex are referred to as adjacent angles.

In the figure above:

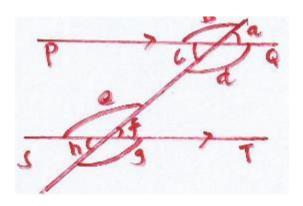
- < AOB is adjacent to <BOC
- < BOC is adjacent to <COD
- < COD is adjacent to <DOE

Angles on a straight line add up to 180° .

Angles at a point

Two intersecting straight lines form four angles having a common vertex. The angles which are on opposite sides of the vertex are called vertically opposite angles. Consider the following:





In the figure above < COB and < AOC are adjacent angles on a straight line. We can now show that a = c as follows:

 $a + b = 180^{\circ}$ (Angles on a straight line)

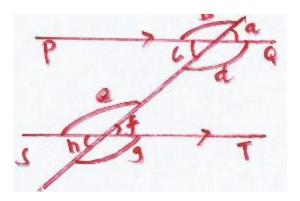
 $c + d = 180^{0}$ (Angles on a straight line)

So, $a + b + c + d = 180^{\circ} + 180^{\circ} = 360^{\circ}$

This shows that angles at a point add up to 360°

Angles on a transversal

A transversal is a line that cuts across two parallel lines.



In the above figure PQ and ST are parallel lines and RU cuts through them.RU is a transversal.

Name:

- i.) Corresponding angles are Angles b and e, c and h, a and f, d and g.
- ii.) Alternate angles a and c, f and h, b and d, e and g.
- iii.) Co-interior or allied angles are f and d, c and e.

Angle properties of polygons

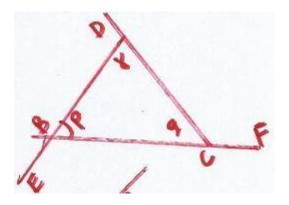
A polygon is a plan figure bordered by three or ore straight lines

Triangles

A triangle is a three sided plane figure. The sum of the three angles of a triangle add up to 180^o.triangles are classified on the basis of either angles sides.

- i.) A triangle in which one of the angles is 90° is called a right angled triangle.
- ii.) A scalene triangle is one in which all the sides and angles are not equal.
- iii.) An isosceles triangle is one in which two sides are equal and the equal sides make equal angles with the third side.
- iv.) An equilateral triangle is one in which all the side are equal and all the angles are equal

Exterior properties of a triangle



Angle DAB = p + q.

Similarly, Angle EBC = r + q and angle FCA = r + p.

But $p + q + r = 180^{0}$

But $p + q + r = 180^{0}$

Therefore angle DAB + angle EBC + angle FCA = 2p + 2q + 2r

$$=2(p + q + r)$$

$$= 2 \times 180^{0}$$

$$=360^{0}$$

In general the sum of all the exterior angles of a triangle is 360° .

Ouadrilaterals

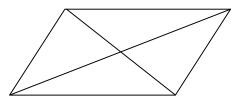
A quadrilateral is a four –sided plan figure. The interior angles of a quadrilateral add put 360° . Quadrilaterals are also classified in terms of sides and angles.

PROPERTIES OF QUADRILATERALS

Properties of Parallelograms

In a parallelogram,

- 1. The parallel sides are parallel by definition.
- 2. The opposite sides are congruent.
- 3. The opposite angles are congruent.
- 4. The diagonals bisect each other.
- 5. Any pair of consecutive angles are supplementary.



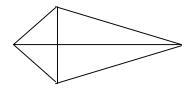
Properties of Rectangles

In a rectangle,

- 1. All the properties of a parallelogram apply by definition.
- 2. All angles are right angles.
- 3. The diagonals are congruent.

Properties of a kite

- 1. Two disjoint pairs of consecutive sides are congruent by definition.
- 2. The diagonals are perpendicular.
- 3. One diagonal is the perpendicular bisector of the other.
- 4. One of the diagonals bisects a pair of opposite angles.
- 5. One pair of opposite angles are congruent.

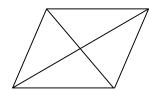


Properties of Rhombuses

In a rhombus,

- 1. All the properties of a parallelogram apply by definition.
- 2. Two consecutive sides are congruent by definition.
- 3. All sides are congruent.
- 4. The diagonals bisect the angles.
- 5. The diagonals are perpendicular bisectors of each other.
- 6. The diagonals divide the rhombus into four congruent right triangles.

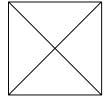
7.



Properties of Squares

In a square,

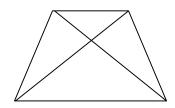
- 1. All the properties of a rectangle apply by definition.
- 2. All the properties of a rhombus apply by definition.
- 3. The diagonals form four isosceles right triangles.



Properties of Isosceles Trapezoids

In an isosceles trapezoid,

- 1. The legs are congruent by definition.
- 2. The bases are parallel by definition.
- 3. The lower base angles are congruent.
- 4. The upper base angles are congruent.
- 5. The diagonals are congruent.
- 6. Any lower base angle is supplementary to any upper base angle.



Proving That a Quadrilateral is a Parallelogram

Any one of the following methods might be used to prove that a quadrilateral is a parallelogram.

- 1. If both pairs of opposite sides of a quadrilateral are parallel, then it is a parallelogram (definition).
- 2. If both pairs of opposite sides of a quadrilateral are congruent, then it is a parallelogram.
- 3. If one pair of opposite sides of a quadrilateral are both parallel and congruent, then it is a parallelogram.
- 4. If the diagonals of a quadrilateral bisect each other, then the it is a parallelogram.
- 5. If both pairs of opposite angles of a quadrilateral are congruent, then it is a parallelogram.

Proving That a Quadrilateral is a Rectangle

One can prove that a quadrilateral is a rectangle by first showing that it is a parallelogram and then using either of the following methods to complete the proof.

- 1. If a parallelogram contains at least one right angle, then it is a rectangle (definition).
- 2. If the diagonals of a parallelogram are congruent, then it is a rectangle.

One can also show that a quadrilateral is a rectangle without first showing that it is a parallelogram.

3. If all four angles of a quadrilateral are right angles, then it is a rectangle.

Proving That a Quadrilateral is a Kite

To prove that a quadrilateral is a kite, either of the following methods can be used.

- 1. If two disjoint pairs of consecutive sides of a quadrilateral are congruent, then it is a kite (definition).
- 2. If one of the diagonals of a quadrilateral is the perpendicular bisector of the other diagonal, then it is a kite.

Proving That a Quadrilateral is a Rhombus

To prove that a quadrilateral is a rhombus, one may show that it is a parallelogram and then apply either of the following methods.

- 1. If a parallelogram contains a pair of consecutive sides that are congruent, then it is a rhombus (definition).
- 2. If either diagonal of a parallelogram bisects two angles of the parallelogram, then it is a rhombus. One can also prove that a quadrilateral is a rhombus without first showing that it is a parallelogram.
 - 3. If the diagonals of a quadrilateral are perpendicular bisectors of each other, then it is a rhombus.
 - 4.

Proving That a Quadrilateral is a Square

The following method can be used to prove that a quadrilateral is a square:

☐ If a quadrilateral is both a rectangle and a rhombus, then it is a square.

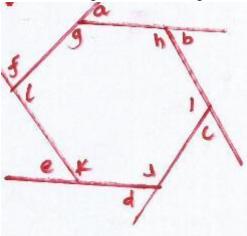
Proving That a Trapezoid is an Isosceles Trapezoid

Any one of the following methods can be used to prove that a trapezoid is isosceles.

- 1. If the nonparallel sides of a trapezoid are congruent, then it is isosceles (definition).
- 2. If the lower or upper base angles of a trapezoid are congruent, then it is isosceles.
- 3. If the diagonals of a trapezoid are congruent, then it is isosceles.

Note:

- \checkmark If a polygon has n sides, then the sum of interior angles (2n -4) right angles.
- ✓ The sum of exterior angles of any polygon is 360° .
- ✓ A triangle is said to be regular if all its sides and all its interior angles are equal.



The figure below is a hexagon with interior angles g, h, I, k and I and exterior angles a, b, c, d, e, and f.

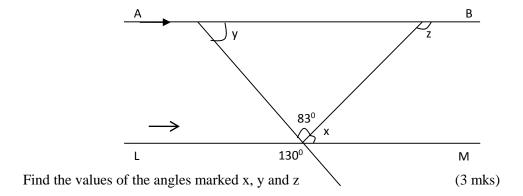
End of topic

Did you understand everything?

If not ask a teacher, friends or anybody and make sure you understand before going to sleep!

Past KCSE Questions on the topic

In the figure below, lines AB and LM are parallel.



CHAPTER ONE

GEOMETRIC CONSTRUCTIONS

Specific Objectives

By the end of the topic the learner should be able to:

- a.) Use a ruler and compasses only to:
- construct a perpendicular bisector of a line
- ✓ construct an angle bisector
- ✓ construct a perpendicular to a line from a given a point
- ✓ construct a perpendicular to a line through a given point on the line
- ✓ construct angles whose values are multiples of 7 ½ °
- ✓ construct parallel lines
- ✓ divide a line proportionally
- b.) Use a ruler and a set square to construct parallel lines, divide a line proportionally, and to construct perpendicular lines
- c.) Construct a regular polygon using ruler and compasses only, and ruler, compasses and protractor
- d.) Construct irregular polygons using a ruler, compasses and protractor.

Content

- a.) Construction of lines and angles using a ruler and compasses only
- b.) Construction of perpendicular and parallel lines using a ruler and a set square only
- c.) Proportional division of a line
- d.) Construction of regular polygons (up to a hexagon)
- e.) Construction of irregular polygons (up to a hexagon).

Introduction

Construction Instruments

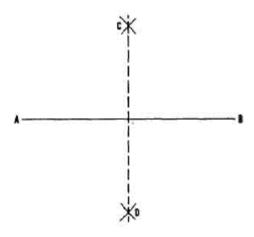
The following minimum set of instruments is required in order to construct good quality drawings:

- Two set squares.
- A protractor.
- o A 15cm or 150 mm ruler
- Compass
- Protractor
- Divider
- An eraser/rubber
- Two pencils a 2H and an HB, together with some sharpening device Razor blade or shaper.

Construction of Perpendicular Lines

Perpendicular lines

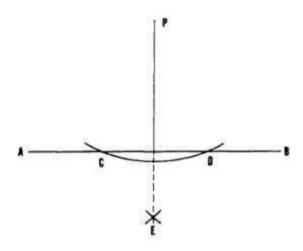
The figure below shows PQ as a perpendicular bisector of a given line AB.



To obtain the perpendicular bisector PQ

- ✓ With A and B as centre, and using the same radius,draw arcs on either side of AB to intersect at P and Q.
- ✓ Join P to Q.

The figure below shows PE, a perpendicular from a point P to a given line AB.



To construct a perpendicular line from a point

- ✓ To drop a perpendicular line from point P to AB.
- ✓ Set the compass point at P and strike an arc intersecting AB at C and D.
- ✓ With C and D as centres and any radius larger than one-half of CD,
- ✓ Strike arcs intersecting at E.

✓ A line from P through E is perpendicular to AB.

To construct a perpendicular line from a point

- ✓ Using P as centre and any convenient radius, draw arcs to intersect the lines at A and B.
- ✓ Using A as centre and a radius whose measure is greater than AP,draw an arc above the line.
- ✓ Using B as the centre and the same radius, draw an arc to interact the one in (ii) at point Q.
- ✓ Using a ruler ,draw PQ.

FIGUR 21.4

Construction of perpendicular lines using a set square.

Two edges of a set square are perpendicular. They can be used to draw perpendicular lines. When one of the edges is put along a line, a line drawn along the other one is perpendicular to the given line.

To construct a perpendicular from a point p to a line

- ✓ Place a ruler along the line.
- ✓ Place one of the edges of a set square which form a right angle along the ruler.
- ✓ Slide the set square along the ruler until the other edge reaches p.
- ✓ Hold the set square firmly and draw the line through P to meet the line perpendicularly.

Construction of Angles using a Ruler and a pair of compass only

The basic angle from which all the others can be derived from is the 60° , 45° and 90°

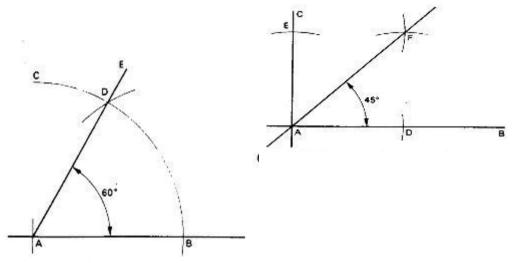
Construction of an Angle of 60⁰

- ✓ Let A be the apex of the angle
- ✓ With centre A draw an arc BC using a suitable radius.
- ✓ With b as the centre draw another arc to intersect arc BC at D.

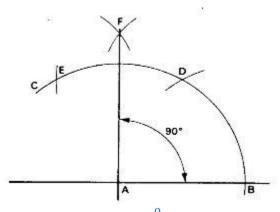
✓ Draw a line AE through D. The angle EAC is 60°

Construction of an Angle of 90⁰

- ✓ Let A be the apex of the angle.
- ✓ With centre A draw an arc BC of large radius.
- ✓ Draw an arc on BC using a suitable radius and mark it D.
- ✓ Using the same radius and point D as the centre draw an arc E.

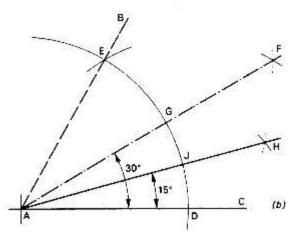


- ✓ BD and DE are of the same radius.
- ✓ With centre D draw any arc F.
- ✓ With centre E draw an arc equal in radius to DF.
- ✓ Join AF with a straight line. Angle BAF is 90°



Construction of an Angle of 45⁰

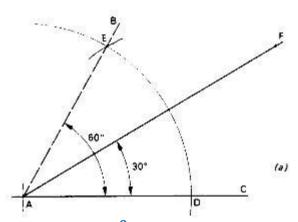
Draw AB and AC at right angles 45^0 to each other. With centre A and with large radius, draw an arc to cut AB at D and and AC at E. With centres E and D draw arcs of equal radius to intersect at Draw a straight line from A through Angle BAF is 45^0



Construction of angles of multiple of $7\frac{10}{2}$ 30°15°...

The bisection of 60° angle produces 30° and the successive bisection of this angle produces 15° which is bisected to produce $7\frac{10^{\circ}}{2}$ as shown below.

- \checkmark Draw AB and AC at 60° to each other as shown above.
- ✓ With centre A, and a large radius, draw an arc to cut AB at E and AC at D.
- ✓ With centres E and D draw arcs of equal radius to intersect at F.
- ✓ Draw a line from A through F.
- \checkmark Angle CAF is 30° half 60°.



To construct 15^0 $7\frac{1}{2}^0$

- \checkmark Draw AC and AF at 30° to each other as described above.
- ✓ With centres G and D draw arcs of equal radius to intersect at H
- ✓ Draw a line from A through H
- ✓ Angle CAH is 15° .
- ✓ With centres J and D a further bisection can be made to give $7\frac{1}{2}^{0}$

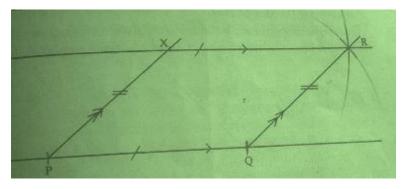
Construction of parallel lines

To construct a line through a given point and parallel to a given line, we may use a ruler and a pair of compass only, or a ruler and a set square.

Using a ruler and a pair of compass only

Parallelogram method

The line EP parallel to AC is constructed as follows:

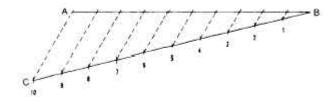


- ✓ With X as the centre and radius PQ, draw an arc.
- ✓ With Q as the centre and radius PX, draw another arc to cut the first arc at R.
- ✓ Join X to R.

v

Proportional Division of lines

Lines can be proportionately divided into a given number of equal parts by use of parallel lines.



To divide line AB

- ✓ Divide line AB into ten equal parts.
- ✓ Through b, draw a line CB of any convenient length at a suitable angle with AB.
- ✓ Using a pair of compasses, mark off, along BC, ten equal intervals as shown above.
- ✓ Join C to A.By using a set square and a ruler, draw lines parallel to CA.
- ✓ The line is therefore divided ten equal parts or intervals.

Construction of Regular Polygons

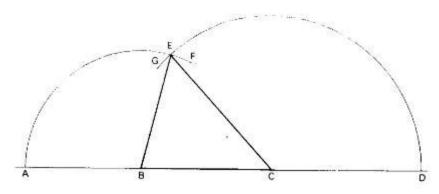
A polygon is regular if all its sides and angles are equal, otherwise it is irregular.

Note:

For a polygon of n sides,the sum of interior angles is (2n -4) right angles. The size of each interior angle of the regular polygon is therefore equal to $(\frac{2n-4}{n})90^{\circ}$.

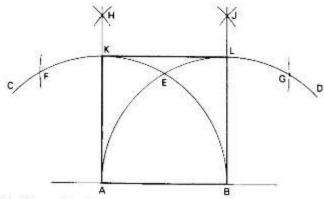
The sum of exterior angles of any polygon is 360^{0} . Each exterior angle of a regular polygon is therefore equal to $\frac{360^{0}}{n}$.

Construction of a regular Triangle



- 1. Draw AB, BC and CD equal in length to the sides of the required triangle
- 2. With centre B and radius AB draw the arc AF
- 3. With centre C and radius CD draw the arc DG
- 4. Where the arcs intersect at E is an apex of the triangle
- 5. Join BE and CE with straight lines to form the triangle BCE

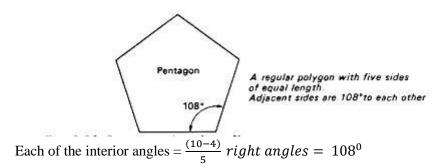
Construction of a regular Quadrilateral



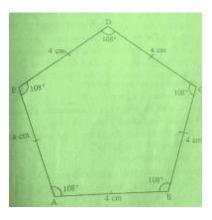
- 1. Mark off one side of the square AB on the base line
- 2. With centre 'A' and radius AB draw the arc BC
- 3. With centre B' and radius AB draw the arc AD
- 4. With centre 'E' and radius AB step off 'F' and 'G' on arcs BC and AD respectively
- 5. With centres 'E' and 'F' draw arcs of equal radius to intersect at H
- 6. With centres 'E' and 'G' draw arcs of equal radius to intersect at J
- 7. Erect perpendiculars AH and BJ
- 8. The arcs BC and AD cut the perpendiculars AH and BJ at 'K' and 'L' respectively
- 9. To complete the square join 'K' and 'L'

Construction of a regular pentagon.

To construct a regular pentagon ABCD of sides 4 cm.



- \checkmark Draw a line AB = 4 cm long.
- ✓ Draw angle ABC = 108° and BC = 4 cm
- ✓ Use the same method to locate points D and



Note:

Use the same procedure to construct other points.

Construction of irregular polygons

Construction of triangles

To construct a triangle given the length of its sides

- ✓ Draw a line and mark a point A on it.
- ✓ On the line mark off with a pair of compass a point B,3 cm from A.
- ✓ With B as the centre and radius 5 cm, draw an arc
- ✓ With A as the centre and radius 7 cm,draw another arc to intersect the arc in (iii) at C.Join A to C and B to C.

To construct a triangle, given the siz of two angles and length of one side.

Construct a triangle ABC in which < BAC = 60° , < ABC = 50° and BC = 4 cm. The sketch is shown below.

- ✓ Draw a line and mark a point B on it.
- ✓ Mark off a point C on the line, 4 cm from B.
- ✓ Using a protractor, measure an angle of = 50° and = 70° at B and C respectively.

To construct a triangle given two sides and one angle.

Given the lengths of two sides and the size of the included angle. Construct a triangle ABC, in which AB = 4 cm,BC = 5 cm and $< \text{ABC} = 60^{\circ}$. Draw a sketch as shown below.

- \checkmark Draw a line BC = 5 cm along
- ✓ Measure an angle of = 60° at B and mark off a point A, 4 cm from B.
- ✓ Join A to C.

To construct a trapezium.

The construction of a trapezium ABCD with $AB=8\ cm$, $BC=5\ cm$,CD=4cm and angle $ABC=60^0$ and $AB=8\ cm$

- \checkmark Draw a line AB = 8 cm.
- ✓ Construct an Angle of = 60° at B.

- ✓ Using B as the centre and radius of 5 cm, mark an arc to insect the line in (ii) at C.
- ✓ Through C, draw a line parallel to AB
- ✓ Using C as the centre and radius of 4 cm, Mark an arc to intersect the line in (iv) at D.
- ✓ Join D to A to form the trapezium.

End of topic

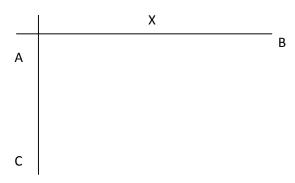
Did you understand everything?

If not ask a teacher, friends or anybody and make sure you understand before going to sleep!

Past KCSE Questions on the topic

- 1. Using a ruler and a pair of compasses only,
 - a) Construct a triangle ABC in which AB = 9cm, AC = 6cm and angle BAC = $37\frac{1}{2}^{0}$
 - a) Drop a perpendicular from C to meet AB at D. Measure CD and hence find the area of the triangle ABC
 - b) Point E divides BC in the ratio 2:3. Using a ruler and Set Square only, determine point E. Measure AE.

2.



On the diagram, construct a circle to touch line AB at X and passes through the point C.

(3 mks)

- 3. Using ruler and pair of compasses only for constructions in this question.
 - (a) Construct triangle ABC such that AB=AC=5.4cm and angle ABC=30^o. Measure BC

(4 mks)

- (b) On the diagram above, a point P is always on the same side of BC as A. Draw the locus of P such that angle BAC is twice angle BPC (2 mks)
- (c) Drop a perpendicular from A to meet BC at D. Measure AD (2 mks)
- (d) Determine the locus Q on the same side of BC as A such that the area of triangle

	$BQC = 9.4cm^2$		(2			
	mks)					
4.	(a) Without using a protractor or set square, construct a triangle ABC in which AB = 4cm,					
	BC = 6cm and \angle ABC = 67½. Take AB as	the base.	(3mks)			
	Measure AC.					
	(b) Draw a triangle A ¹ BC ¹ which is indirect	ly congruent to triangle ABC.	(3mks)			
5.	Construct triangle ABC in which $AB = 4.4$ cm, $BC = 6.4$ cm and $AC = 7.4$ cm. Construct an					
	escribed circle opposite angle ACB	(5 mks)				
	(a) Measure the radius of the circle		(1 mk)			
	(b) Measure the acute angle subtended at the centre of the circle by AB (1 mk)					
	(c) A point P moves such that it is always outside the circle but within triangle AOB, where O is					
	the centre of the escribed circle. Show by shading the region within which P lies.					
		(3 mks)				
6.	(a) Using a ruler and a pair of compasses or	nly, construct a parallelogram PQR	S in which PQ =			
	8cm, QR = 6cm and \angle PQR = 150 ⁰	(3 mks)				
	(b) Drop a perpendicular from S to meet PQ at B. Measure SB and hence calculate the area of the					
	parallelogram.	(5 mks)				
	(c) Mark a point A on BS produced such that the area of triangle APQ is equal to three quarters					
	the area of the parallelogram	(1 mk)				
	(d) Determine the height of the triangle.	(1 m	k)			
7.	Using a ruler and a pair of compasses only, 8cm and angle ABC = 45°. Drop a perpendi					
8.	a) Using a ruler and a pair of compasses on	y to construct a trapezium ABCD	(+IIIK3)			
	such that $AB = 12 cm$, $\angle DAB = 60^{\circ}$.	, $\angle ABC = 75^{\circ}$ and $AD = 7cm$	(5mks)			
	b)From the point D drop a perpendicular to	the line AB to meet the line at E. r.	neasure DE hence			
	calculate the area of the trapezium	(5mks)				
9.	Using a pair of compasses and ruler only; (a) Construct triangle ABC such that AB = (b) Measure the length of AC (c) Draw a circle that touches the vertices A (d) Measure the radius of the circle (e) Hence or otherwise, calculate the area of	A,B and C. f the circle outside the triangle.	(1 mark) (2 marks) (1 mark) (3 marks)			
10.	Using a ruler and a pair of compasses only,	•	en that angle APB =			
	60^{0} on the line AB = 5cm.	(4mks)				



- 11. Using a set square, ruler and pair of compases divide the given line into 5 equal portions. (3mks)
- 12. Using a ruler and a pair of compasses only, draw a parallelogram ABCD, such that angle DAB = 75° . Length AB = 6.0cm and BC = 4.0cm from point D, drop a perpendicular to meet line AB at N
 - a) Measure length DN
 - b) Find the area of the parallelogram

(10 mks)

- 13. Using a ruler and a pair of compasses only, draw a parallelogram ABCD in which AB = 6cm, BC = 4cm and angle $BAD = 60^{\circ}$. By construction, determine the perpendicular distance between the lines AB and CD
- 14. Without using a protractor, draw a triangle ABC where \angle CAB = 30°, AC = 3.5cm and AB = 6cm. measure BC
- 15. (a) Using a ruler and a pair of compass only, construct a triangle ABC in which angle ABC =37.5°, BC =7cm and BA = 14cm
 - (b) Drop a perpendicular from A to BC produced and measure its height
 - (c) Use your height in (b) to find the area of the triangle ABC
 - (d) Use construction to find the radius of an inscribed circle of triangle ABC
- 16. In this question use a pair of compasses and a ruler only
 - a) Construct triangle PQR such that PQ = 6 cm, QR = 8 cm and $< PQR = 135^{\circ}$
 - b) Construct the height of triangle PQR in (a) above, taking QR as the base
- 17. On the line AC shown below, point **B** lies above the line such that $\angle BAC = 52.5^{\circ}$ and AB = 4.2cm. (*Use a ruler and a pair of compasses for this question*)



- (a) Construct ∠BAC and mark point **B**
- (b) Drop a perpendicular from **B** to meet the line **AC** at point **F**. Measure **BF**

CHAPTER TWENTY TW0

SCALE DRAWING

Specific Objectives

By the end of the topic the learner should be able to:

- a.) Interpret a given scale
- b.) Choose and use an appropriate scale
- c.) Draw suitable sketches from given information
- d.) State the bearing of one point from another
- e.) Locate a point using bearing and distance
- f.) Determine angles of elevation and depression
- g.) Solve problems involving bearings elevations and scale drawing
- h.) Apply scale drawing in simple surveying.

Content

- a.) Types of scales
- b.) Choice of scales
- c.) Sketching from given information and scale drawing
- d.) Bearings
- e.) Bearings, distance and locating points
- f.) Angles of elevation and depression
- g.) Problems involving bearings, scale drawing, angles of elevation and depression
- h.) Simple surveying techniques.

Introduction

The scale

The ratio of the distance on a map to the actual distance on the ground is called the scale of the map. The ratio can be in statement form e.g. 50 cm represents 50,000 cm or as a representative fraction (R.F), 1:

$$5,000,000$$
 is written as $\frac{1}{5,000,000}$

Example

The scale of a map is given in a statement as 1 cm represents 4 km. convert this to a representative fraction (R.F).

Solution

One cm represents 4 x 100,000 cm. 1 cm represents 400, 000

Therefore, the ratio is 1: 400,000 and the R.F is
$$\frac{1}{400,000}$$

Example

The scale of a map is given as 1:250,000. Write this as a statement.

Solution

1:250,000 means 1 cm on the map represents 250,000 cm on the ground. Therefore, 1 cm represents $\frac{250,000}{100,000}$ km.

I.e. 1 cm represents 2.5 km.

Scale Diagram

When during using scale, one should be careful in choosing the right scale, so that the drawing fits on the paper without much details being left.

Bearing and Distances

Direction is always found using a compass point.



A compass has eight points as show above. The four main points of the compass are North, South, East, and West. The other points are secondary points and they include North East (NE), South East (SE), South West (SW) and North West (NW). Each angle formed at the centre of the compass is 45° the angle between N and E is 90° .

Compass Bearing

When the direction of a place from another is given in degrees and in terms of four main points of a compass. E.g. $N45^0\ W$, then the direction is said to be given in compass bearing. Compass bearing is measured either clockwise or anticlockwise from North or south and the angle is acute.

True bearing

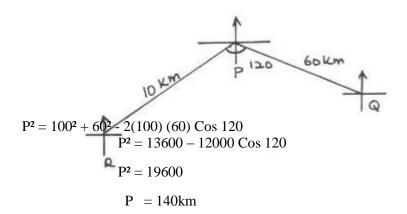
North East direction, written as $N45^0$ E can be given in three figures as 045^0 measured clockwise from True North. This three- figure bearing is called the true bearing.

The true bearings due north is given as 000° .Due south East as 135° and due North West as 315° .

Example

From town P, a town Q is 60km away on a bearing South 80° east. A third town R is 100km from P on the bearing South 40° west. A cyclist travelling at 20km/h leaves P for Q. He stays at Q for one hour and then continues to R. He stays at R for 1½ hrs. and then returns directly to P.

(a) Calculate the distance of Q from R.



(b) Calculate the bearing of R from Q.

$$\frac{140}{Sin\ 120} = \frac{100}{Sin\ Q}$$
 M1
$$Sin\ Q = \frac{100\ Sin\ 120}{140}$$
 M1
$$= 38.2^{\circ}$$
 A1
Bearing 270 – 38.2 = 241.8 B1

(c) What is the time taken for the whole round trip?

= 15hrs

Time from P to R =
$$\frac{60}{20} = 3hrs$$

Time from Q to R = $\frac{140}{20} = 7hrs$

B1 for all three correct

From R to P = $\frac{100}{20} = 5hrs$

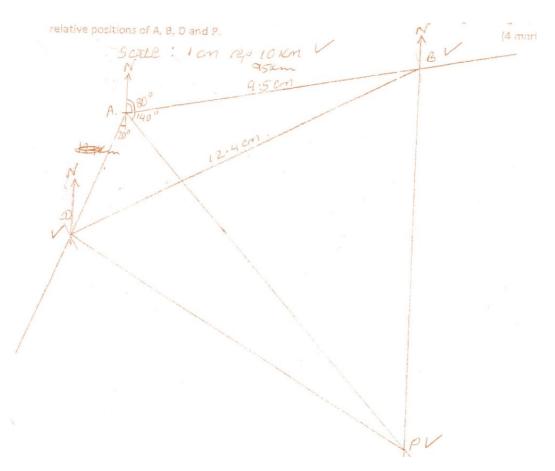
Taken travelling = $3 + 7 + 5$

M1

Example

A port B is on a bearing 080° from a port A and a distance of 95 km. A Submarine is stationed at a port D, which is on a bearing of 200° from A, and a distance of 124 km from B. A ship leaves B and moves directly Southwards to an Island P, which is on a bearing of 140° from A. The Submarine at D on realizing that the ship was heading to the Island P, decides to head straight for the Island to intercept the ship. Using a scale of 1 cm to represent 10 km, make a scale drawing showing the relative positions of A, B, D and P.

{4 marks}



Hence find:

b) The distance from A to D.

{2 marks}

 $4.6 \pm 0.1 \times 10 = 46 \text{ KM} \pm 1 \text{ KM}$

c) The bearing o the Submarine from the ship when the ship was setting off from B. {1 mark}

 $240^{\circ} \pm 1^{\circ}$ OR S 60° W $\pm 2^{\circ}$

d) The bearing of the Island P from D. {1 mark}

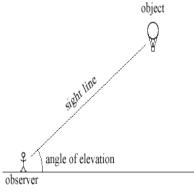
e) The distance the Submarine had to cover to reach the Island 127 \pm 1 KM {2 marks}

 $P127 \pm 0.1 \times 10 =$

Angle of Elevation and Depression

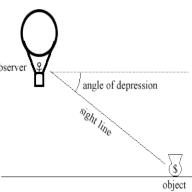
Angle of Elevation:

The angle above the horizontal that an observer must look to see an object that is higher than the observer. Example, a man looking at a bird.



Angle of Depression:

The angle below horizontal that an observer must look to see an object that is lower than the observer. Example, a bird looking down at a bug.



Angles of depression and elevation can be measured using an instrument called clinometer

To find the heights or the lengths we can use scale drawing.

Simple survey methods

This involves taking field measurements of the area so that a map of the area can be drawn to scale. Pieces of land are usually surveyed in order to:

- ✓ Fix boundaries
- ✓ For town planning
- ✓ Road construction
- ✓ Water supplies
- ✓ Mineral development

Areas of irregular shapes

Areas of irregular shape can be found by subdividing them into convenient geometrical shapes e.g. triangles, rectangles or trapezia.

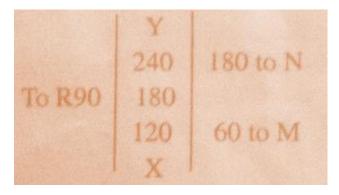
Example

The area in hectares of the field can be found by the help of a base line and offsets as shown.

Fig 22.26

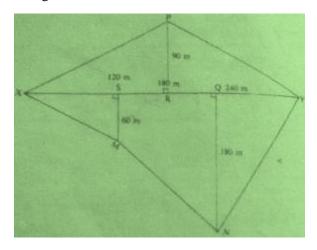
XY is the base line 360 m.SM,RP and QN are the offsets.

Taking X as the starting point of the survey, the information can be entred in a field book as follows.



The sketch is as follows:

Using a suitable scale.



The area of the separate parts is found then combined.

Area of:

```
Triangle XPR is \frac{1}{2} x180 x 90 = 8100 m^2

Triangle PRY is \frac{1}{2} x180 x 90 = 8100 m^2

Triangle XSM is \frac{1}{2} x120 x 60 = 3600 m^2

Triangle QNY is \frac{1}{2} x120 x 180 = 10800 m^2

Trapezium SQNM = \frac{1}{2}(QN + SM) x SQ m^2

\frac{1}{2} (180 + 60) x 120 m^2

= 14400m^2

Total area = 8100 + 8100 + 3600 + 10800 + 14400 = 45000m^2
```

End of topic

Did you understand everything?

If not ask a teacher, friends or anybody and make sure you understand before going to sleep!

Past KCSE Questions on the topic

A point B is on a bearing of 080⁰ from a port A and at a distance of 95 km. A submarine is stationed at a port D, which is on a bearing of 200⁰ from AM and a distance of 124 km from B.
 A ship leaves B and moves directly southwards to an island P, which is on a bearing of 140 from A.
 The submarine at D on realizing that the ship was heading fro the island P, decides to head straight for the island to intercept the ship

Using a scale 0f 1 cm to represent 10 km, make a scale drawing showing the relative positions of A, B, D, P.

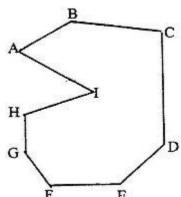
Hence find

- (i) The distance from A to D
- (ii) The bearing of the submarine from the ship was setting off from B
- (iii) The bearing of the island P from D
- (iv) The distance the submarine had to cover to reach the island P
- 2. Four towns R, T, K and G are such that T is 84 km directly to the north R, and K is on a bearing of 295⁰ from R at a distance of 60 km. G is on a bearing of 340⁰ from K and a distance of 30 km. Using a scale of 1 cm to represent 10 km, make an accurate scale drawing to show the relative positions of the town.

Find

(a) The distance and the bearing of T from K

- (b) The distance and the bearing G from T
- (c) The bearing of R from G
- 3. Two aeroplanes, S and T leave airports A at the same time. S flies on a bearing of 060 at 750 km/h while T flies on a bearing of 210^o at 900km/h.
 - (a) Using a suitable scale, draw a diagram to show the positions of the aeroplane after two hours.
 - (b) Use your diagram to determine
 - (i) The actual distance between the two aeroplanes
 - (ii) The bearing of T from S
 - (iii) The bearing of S from T
- 4. A point A is directly below a window. Another point B is 15 m from A and at the same horizontal level. From B angle of elevation of the top of the bottom of the window is 300 and the angle of elevation of the top of the window is 350. Calculate the vertical distance.
 - (a) From A to the bottom of the window
 - (b) From the bottom to top of the window
 - 4. Find by calculation the sum of all the interior angles in the figure ABCDEFGHI below

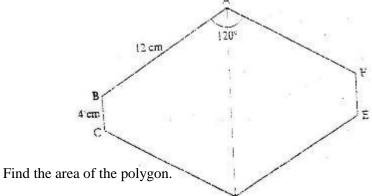


- 6. Shopping centers X, Y and Z are such that Y is 12 km south of X and Z is 15 km from X. Z is on a bearing of 330° from Y. Find the bearing of Z from X.
- 7. An electric pylon is 30m high. A point S on the top of the pylon is vertically above another point R on the ground. Points A and B are on the same horizontal ground as R. Point A due south of the pylon and the angle of elevation of S from A is 26°. Point B is due west of the pylon and the angle of elevation of S from B is 32°

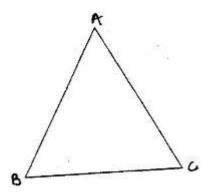
Find the

- (a) Distance from A and B
- (b) Bearing of B from A

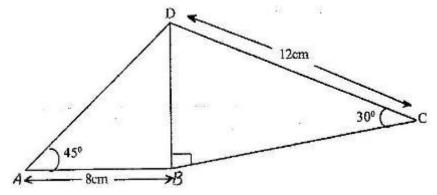
8. The figure below is a polygon in which AB = CD = FA = 12cm BC = EF = 4cm and $BAF = CDE = 120^{\circ}$. AD is a line of symmetry.



- 9. The figure below shows a triangle ABG
 - a) Using a ruler and a pair of compasses, determine a point D on the line BC such that BD:DC = 1:2.
- b) Find the area of triangle ABD, given that AB = AC.

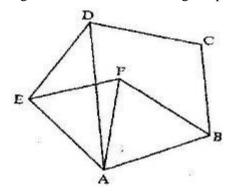


- 10. A boat at point x is 200 m to the south of point Y. The boat sails X to another point Z. Point Z is 200m on a bearing of 310⁰ from X, Y and Z are on the same horizontal plane.
 - (a) Calculate the bearing and the distance of Z from Y
 - (b) W is the point on the path of the boat nearest to Y. Calculate the distance WY
 - (c) A vertical tower stands at point Y. The angle of point X from the top of the tower is 6^0 calculate the angle of elevation of the top of the tower from W.
- 11. The figure below shows a quadrilateral ABCD in which AB = 8 cm, DC = 12 cm, \angle BAD = 45°, \angle CBD = 90° and BCD = 30°.



Find:

- (a) The length of BD
- (b) The size of the angle A D B
- 12. In the figure below, ABCDE is a regular pentagon and ABF is an equilateral triangle



Find the size of

- a) ∠ ADE
- b) ∠ AEF
- c) ∠DAF
- 13. In this question use a pair of compasses and a ruler only
 - (a) construct triangle ABC such that AB = 6 cm, BC = 8cm and $\angle ABC 135^0$ (2 marks)
 - (b) Construct the height of triangle ABC in a) above taking BC as the base (1 mark)
- 14. The size of an interior angle of a regular polygon is $3x^0$ while its exterior angle is $(x-20)^0$. Find the number of sides of the polygon
- 15. Points L and M are equidistant from another point K. The bearing of L from K is 330°. The bearing of M from K is 220°.

Calculate the bearing of M from L

- 16. Four points B,C,Q and D lie on the same plane point B is the 42 km due south- west of town Q. Point C is 50 km on a bearing of 560⁰ from Q. Point D is equidistant from B, Q and C.
 - (a) Using the scale 1 cm represents 10 km, construct a diagram showing the position of B, C, Q and D
 - (b) Determine the
 - (i) Distance between B and C
 - (ii) Bearing D from B
- 17. Two aeroplanes P and Q, leave an airport at the same time flies on a bearing of 240° at 900km/hr while Q flies due East at 750 km/hr
 - (a) Using a scale of 1v cm drawing to show the positions of the aeroplanes after 40 minutes.
 - (b) Use the scale drawing to find the distance between the two aeroplane after 40 minutes
 - (c) Determine the bearing of
 - (i) P from Q ans 254°
 - (ii) Q from P ans 74°
- 18. A port B is no a bearing of 080 from a port A and at a distance of 95 km. A submarine is stationed port D which is on a bearing of 200^o from A, and a distance of 124 km from B.

A ship leaves B and moves directly southwards to an island P, which is on a bearing of 140⁰ from A. The submarine at D on realizing that the ship was heading for the island P decides to head straight for the island to intercept the ship.

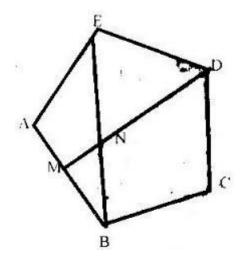
Using a scale of 1 cm to represent 10 km, make a scale drawing showing the relative position of A, B D and P.

Hence find:

- (i) The distance from A and D
- (ii) The bearing of the submarine from the ship when the ship was setting off from B
- (iii) The baring of the island P from D
- (iv) The distance the submarine had to cover to reach the island
- 19. Four towns R, T, K and G are such that T is 84 km directly to the north R and K is on a bearing of 295^o from R at a distance of 60 km. G is on a bearing of 340^o from K and a distance of 30 km. Using a scale of 1 cm to represent 10 km, make an acute scale drawing to show the relative positions of the towns.

Find

- (a) The distance and bearing of T from K
- (b) The bearing of R from G
- 20. In the figure below, ABCDE is a regular pentagon and M is the midpoint of AB. DM intersects EB at N. (T7)



Find the size of

- (a) \angle BAE
- (b) ∠ BED

- (c) \angle BNM
- 21. Use a ruler and compasses in this question. Draw a parallelogram ABCD in which AB = 8cm, BC = 6 cm and BAD = 75. By construction, determine the perpendicular distance between AB and CD.
- 22. The interior angles of the hexagon are $2x^0$, $\frac{1}{2}x^0$, $x + 40^0$, 110^0 , 130^0 and 160^0 . Find the value of the smallest angle.
- 23. The size of an interior angle of a regular polygon is 156⁰. Find the number of sides of the polygon.



Specific Objectives

By the end of the topic the learner should be able to:

- a.) Identify and sketch common solids
- b.) Identify vertices, edges and faces of common solids
- c.) State the geometric properties of common solids
- d.) Draw nets of solids accurately
- e.) Make models of solids from nets
- f.) Calculate surface area of solids from nets

Content

- a.) Common solids (cubes, cuboids, pyramids, prisms, cones, spheres, cylinders etc)
- b.) Vertices, edges and faces of common solids.
- c.) Geometric properties of common solids.
- d.) Nets of solids.
- e.) Models of solids from nets.
- f.) Surface area of solids from nets (include cubes, cuboids, cones, pyramids prisms)

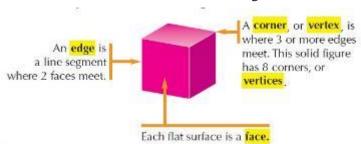
Introduction

A solid is an object which occupies space and has a definite or fixed shape. Solids are either regular or irregular.

Shape	Characteristics	Real Life Examples	
Sphere	no faces, edges or corners; completely round		
Cylinder	2 circular bases connected by a curved surface		
Cube	6 square faces, 12 edges and 8 corners; all sides equal		
Cone 1	round base with a curved surface that forms a point	A A	
Rectangular Prism	6 faces with opposite faces being equal, 12 edges and 8 corners		
Pyramid ©	square base and 4 triangular faces, 8 edges and 5 corners		

Note:

✓ Intersections of faces are called edges.



The point where three or more edges meet is called a vertex.

Sketching solids

To draw a reasonable sketch of a solid on

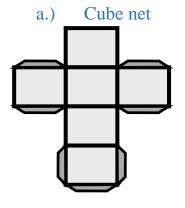
a plan paper, the following ideas are hepful:

Use of isometric projections

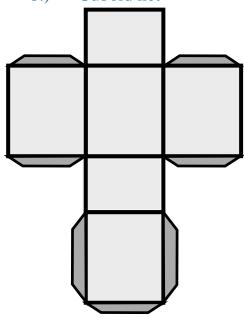
In this method the following points should be obtained:

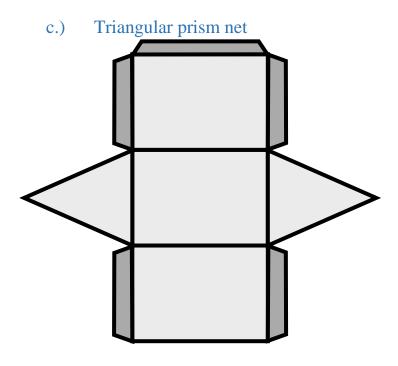
- ✓ Each edge should be drawn to the correct length.
- ✓ All rectangular faces must be drawn as parallelograms.
- ✓ Horizontal and vertical edges must be drawn accurately to scale.
- ✓ The base edges are drawn at an angle 30^{0} with the horizontal lines.
- ✓ Parallel lines are drawn parallel.

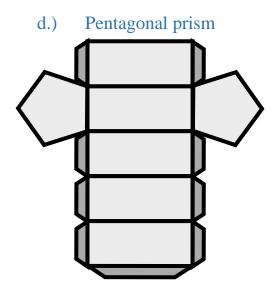
Examples

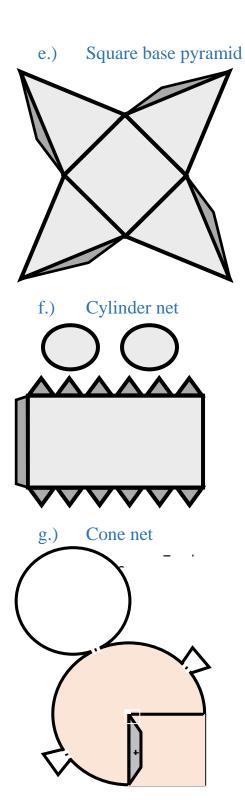


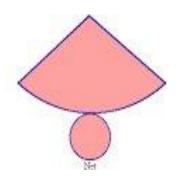






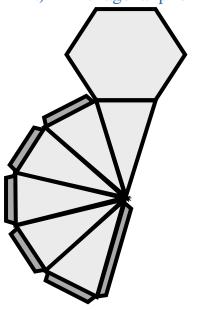




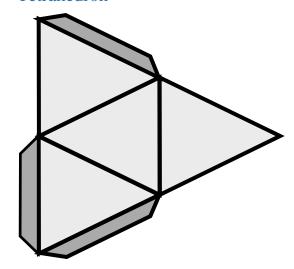


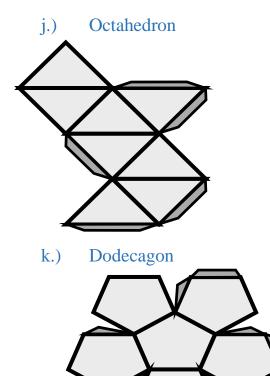
Cone net

h.) Hexagonal prism



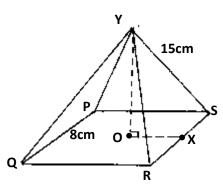
i.) Tetrahedron







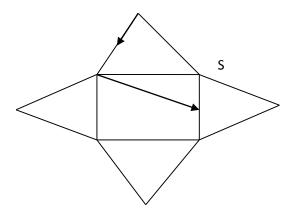
An ant moved from Y to X the midpoint of RS through P in the right pyramid below



Draw the net of the pyramid showing

path of the ann hence find the distance it moved.

Solution

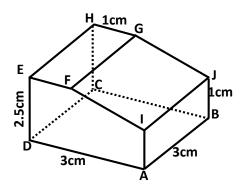


Distance=
$$15 + \sqrt{(144 + 16)}$$

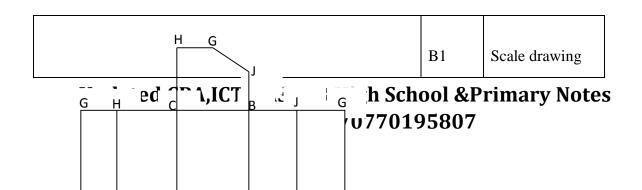
=27.649cm

Example

Draw the net of the solid below.



Solution



B1	Correct labeling
B1	Correct measurement of GJ and FI

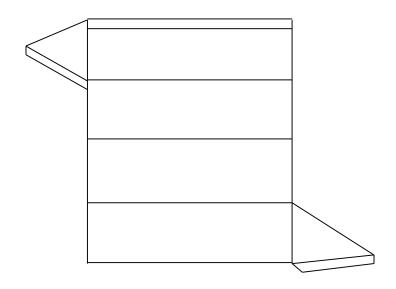
End of topic

Did you understand everything?

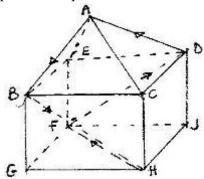
If not ask a teacher, friends or anybody and make sure you understand before going to sleep!

Past KCSE Questions on the topic

1. The figure below shows a net of a prism whose cross – section is an equilateral triangle.

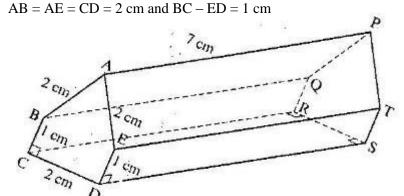


- a) Sketch the prism
 - b) State the number of planes of symmetry of the prism.
- 2. The figure below represents a square based solid with a path marked on it.



Sketch and label the net of the solid.

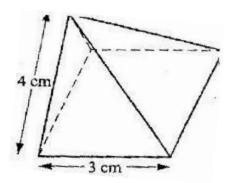
3. The figure below represents below represents a prism of length $7\ \mathrm{cm}$



Draw the net of the prism

(3 marks)

4. The diagram below represents a right pyramid on a square base of side 3 cm. The slant of the pyramid is 4 cm.



(a) Draw a net of the pyramid

(2 marks)

(b) On the net drawn, measure the height of a triangular face from the top of

the Pyramid

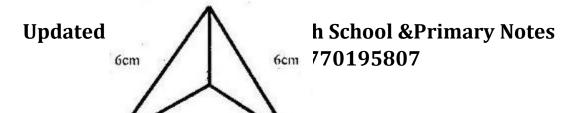
(1 mark)

5. (a) Draw a regular pentagon of side 4 cm

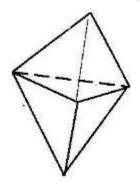
(1 mark)

(b) On the diagram drawn, construct a circle which touches all the sides of the pentagon (2 marks)

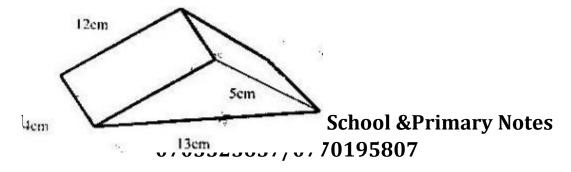
6. The figure below shows a solid regular tetrapack of sides 6 cm



- (a) Draw a net of the solid
 - (b) Find the surface area of the solid
- 7. The figure below shows a solid made by pasting two equal regular tetrahedral



- (a) Draw a net of the solid
- (b) If each face is an equilateral triangle of side 5cm, find the surface area of the solid.
- 8(a) Sketch the net of the prism shown below



(c) Find the surface area of the solid(d)
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0705525657 (Mr Isaboke)
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