P425/1
PURE MATHEMATICS
Paper 1
3 hours

WAKISSHA

Uganda Advanced Certificate of Education PURE MATHEMATICS

Paper 1

3 hours

INSTRUCTIONS TO CANDIDATES:

- Answer all the eight questions in section A and any five questions from section B.
- Any additional question(s) answered will not be marked.
- Show all necessary working clearly.
- Begin each answer on a fresh page of paper.
- Silent, non programmable scientific calculators and mathematical tables with a list of formulae may be used.

SECTION A (40 MARKS)

Answer all questions in this section.

1. Solve the simultaneous equations. p + q + r = 0, p + 2q + 2r = 2 and 2p + 3r = 4. (05 marks)

- 2. Determine the Cartesian's equation of a line passing through points A (2,5,4) and B (5,3,7) (05marks)
- 3. A Circle with Centre C, cuts another circle $x^2 + y^2 4x + 6y 7 = 0$ at right angles and passes through the point (1, 3). Find the locus of Centre C. (05marks)
- 4. Solve the equation $tan^{-1}(2x+1) = tan^{-1}(2) tan^{-1}(2x-1)$ (05marks)

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- 5. Evaluate $\int_{0}^{\sqrt{\frac{\pi}{2}}} \frac{x}{1+\sin(x^2)} dx$ (06marks)
- 6. A committee of four pupils is to be selected from three boys and seven girls.

 How many committees are formed in order to have girls as the majority in committee? (04marks)
- 7. Use Maclaurin's theorem to expand $In\sqrt{\left(\frac{1+2x}{1+x}\right)}$ up to x^2 (05marks)
- 8. The inside of a glass is in the shape of an inverted cone of depth 8cm and radius 4cm full of wine. The wine is leaking from small hole at vertex at rate 0.06cm³s⁻¹ into somebody mouth. Find the rate at which surface area of wine in contact with glass in decreasing when depth is 6cm. (05marks)

SECTION B (60 marks)

Answer any five questions from this section.

- 9. (a) Solve inequality; $\frac{x-2}{x+1} \ge \frac{x+1}{x+3}$ (06marks)
 - (b) John deposits Shs. 3,000,000 at beginning of every year in a micro-finance bank starting 2015, how much would he collect at the end of 2020 if the bank offers compound interest of 12.5% per annum and no withdrawal is made within the period.

 (06marks)
- 10. (a) Find the vector equation of the line passing through the point (3.1, 2) and perpendicular to the plane r.(2i-j+k)=4 hence find point of intersection of line and the plane.

- (b) The position vectors of the points A, B and C are 2i j + 5k, i 2j + k and 3i + j 2k respectively. Given that L and M are mid-points of AC and CB respectively.

 Show that BA = 2ML (06marks)
- 11. (a) Solve $\cos 3\theta + \cos 2\theta + \cos \theta = 0$, $0^0 \le \theta \le 180^0$ (05 marks)
 - (b) Show that $\sin 3\theta = 3\sin \theta 4\sin^3 \theta$, hence find all solutions of the equation $8x^3 6x + 1 = 0$. Correct to 3 decimal places. (07marks)
- 12. Given curve $y = \frac{(x-3)^2}{(x-9)(x-1)}$. Find equations of asymptoles and sketch the curve. (12marks)
- 13. Express $f(x) = \frac{x^3 + 4x^2 5x 4}{(x 2)^2(1 + x^2)}$ into partial fractions, hence evaluate $\int_3^5 f(x) dx$. (12marks)
 - 14. (a) Solve $x \frac{dy}{dx} + 2y = x^2$ when y (1) = 1. (05marks)
 - (b) A liquid cools in the environment of a constant temperature of 21°C at the rate proportional to the excess temperature. Initially the temperature of liquid is 100°C and after 10 minutes the temperature dropped by 16°C. Find how long it takes for the temperature of liquid to be 70°C. (07marks)
 - 15. (a) Given that the root of $z^4 4z^3 + 3z^2 + 3z^2 2z 6 = 0$ is 1-i, find other roots. (06marks)
 - (b) Evaluate $\left(1+i\sqrt{3}\right)^{\frac{2}{3}}$ (06marks)
 - 16. (a) Find the equation of a circle which is a tangent to the lines 3y = 4x, y = 8 and 4x + 3y = 0 (05marks)
 - (b) If the line y = mx + c is a tangent to the ellipse $a^2y^2 + b^2x^2 = a^2b^2$, prove that $C^2 = b^2 + a^2m^2$. Hence determine the equations of the common tangents to ellipse $4x^2 + 14y = 56$ and $3x^2 + 23y^2 = 69$ (07marks)