

$$\vec{AB} = \begin{pmatrix} 3 \\ 8 \\ 1 \end{pmatrix} - \begin{pmatrix} 1 \\ 3 \\ 3 \end{pmatrix} = \begin{pmatrix} 2 \\ 5 \\ -2 \end{pmatrix} B_1$$

$$\vec{BC} = \begin{pmatrix} 7 \\ 20 \\ 3 \end{pmatrix} - \begin{pmatrix} 3 \\ 8 \\ 1 \end{pmatrix} = \begin{pmatrix} 4 \\ 12 \\ 2 \end{pmatrix} B_1$$

direction ratios of $\vec{AB} = 2:-6:-2 = 1:-3:-1 B_1$

direction ratios of $\vec{BC} = 4:-12:-4 = 1:-3:-1 B_1$

Since \vec{AB} and \vec{BC} have the same direction ratios and contain a common point B,

A, B and C are collinear. B_1

$$2. \textcircled{2} \vec{OZ} = \lambda \vec{OY}$$

$$\begin{aligned} \vec{OY} &= \vec{OA} + \frac{1}{2} \vec{AB} \\ &= \vec{a} + \frac{1}{2}(\vec{b} - \vec{a}) \\ &= \frac{1}{2}(\vec{a} + \vec{b}) \end{aligned}$$

$$\vec{OZ} = \frac{\lambda}{2}(\vec{a} + \vec{b}) \text{ --- (1) } B_1$$

$$\vec{OZ} = \vec{OX} + \mu \vec{XB}$$

$$= \frac{1}{2}\vec{a} + \mu(\vec{b} - \frac{1}{2}\vec{a})$$

$$\vec{OZ} = \frac{1}{2}(\vec{a} + 2\mu\vec{b} - \mu\vec{a}) \text{ --- (2) } B_1$$

Equating components:

$$q: \lambda = 1 - \mu$$

$$k: -\lambda = 2\mu$$

$$1 - 3\mu = 0 \Rightarrow \mu = \frac{1}{3} \Rightarrow \lambda = \frac{2}{3} A_1$$

$$\therefore \vec{OZ} = \frac{1}{3}(\vec{a} + \vec{b}) B_1$$

$$\textcircled{3} \underline{d_1} = \begin{pmatrix} 4 \\ 6 \\ -2 \end{pmatrix}, \underline{d_2} = \begin{pmatrix} 0 \\ 1 \\ 0 \end{pmatrix} B_1$$

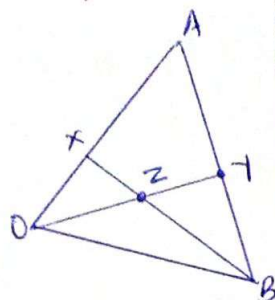
$$\underline{d_1} \cdot \underline{d_2} = |\underline{d_1}| |\underline{d_2}| \cos \theta$$

$$\begin{pmatrix} 4 \\ 6 \\ -2 \end{pmatrix} \cdot \begin{pmatrix} 0 \\ 1 \\ 0 \end{pmatrix} = \sqrt{(4)^2 + (6)^2 + (-2)^2} \sqrt{0^2 + 1^2 + 0^2} \cos \theta$$

$$6 = \sqrt{56} \cos \theta$$

$$\theta = \cos^{-1}(\frac{6}{\sqrt{56}}) = 36.7^\circ A_1$$

$$\begin{aligned} \text{direction ratios} &= 4:6:-2 \\ &= 2:3:-1 B_1 \end{aligned}$$



④ Suppose the lines intersect

$$\vec{r} = \vec{r}_2$$

$$\begin{pmatrix} 17+2\alpha \\ 2-3\alpha \\ -6+9\alpha \end{pmatrix} = \begin{pmatrix} 2+6\beta \\ -3+7\beta \\ 4-\beta \end{pmatrix}$$

$$6\beta - 2\alpha = 15$$

$$7\beta + 3\alpha = 5 M_1 \Rightarrow$$

$$\beta + 9\alpha = 10$$

$$\begin{aligned} 21\beta + 9\alpha &= 15 \\ -\beta + 9\alpha &= 10 \end{aligned}$$

$$20\beta = 5 \Rightarrow \beta = \frac{1}{4} A_1$$

$$9\alpha = 10 - \frac{1}{4} \Rightarrow 9\alpha = \frac{39}{4} \Rightarrow \alpha = \frac{12}{13} A_1$$

$$6\beta - 2\alpha = \frac{3}{2} - 2\left(\frac{12}{13}\right) \neq 15$$

Since α and β are inconsistent, the lines don't intersect hence are skew. B_1

$$\textcircled{5} \vec{PQ} = \begin{pmatrix} 1 \\ 2 \\ -1 \end{pmatrix} - \begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix} = \begin{pmatrix} 0 \\ 1 \\ -2 \end{pmatrix} B_1$$

$$\vec{PR} = \begin{pmatrix} 3 \\ 2 \\ -1 \end{pmatrix} - \begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix} = \begin{pmatrix} 2 \\ 1 \\ -2 \end{pmatrix}$$

$$\underline{n} = \vec{PQ} \wedge \vec{PR} = \begin{vmatrix} \underline{i} & \underline{j} & \underline{k} \\ 0 & 1 & -2 \\ 2 & 1 & -2 \end{vmatrix} M_1$$

$$\underline{n} = -7\underline{i} - 4\underline{j} + 6\underline{k} A_1$$

$$\underline{r} \cdot \underline{n} = \underline{a} \cdot \underline{n}$$

$$\underline{r} \cdot \begin{pmatrix} -7 \\ -4 \\ 6 \end{pmatrix} = \begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix} \cdot \begin{pmatrix} -7 \\ -4 \\ 6 \end{pmatrix} M_1$$

$$\underline{r} \cdot \begin{pmatrix} -7 \\ -4 \\ 6 \end{pmatrix} = -7 - 4 + 6$$

$\therefore \underline{r} \cdot \begin{pmatrix} -7 \\ -4 \\ 6 \end{pmatrix} = -5$ is the vector product equation of the plane.

$$\textcircled{6} \vec{AP} = \lambda \underline{n} \Rightarrow \begin{pmatrix} x \\ y \\ z \end{pmatrix} - \begin{pmatrix} 25 \\ 5 \\ 7 \end{pmatrix} = \lambda \begin{pmatrix} 12 \\ 4 \\ 3 \end{pmatrix}$$

$$\begin{pmatrix} x \\ y \\ z \end{pmatrix} = \begin{pmatrix} 12\lambda + 25 \\ 4\lambda + 5 \\ 3\lambda + 7 \end{pmatrix} B_1$$

$$12x + 4y + 3z = 3$$

$$12(12\lambda + 25) + 4(4\lambda + 5) + 3(3\lambda + 7) = 3 M_1$$

$$144\lambda + 300 + 16\lambda + 20 + 9\lambda + 21 = 3$$

$$169\lambda = -338 \Rightarrow \lambda = -2 A_1$$

$$\begin{pmatrix} x \\ y \\ z \end{pmatrix} = \begin{pmatrix} 12(-2) + 25 \\ 4(-2) + 5 \\ 3(-2) + 7 \end{pmatrix} = \begin{pmatrix} 1 \\ -3 \\ 1 \end{pmatrix} B_1$$

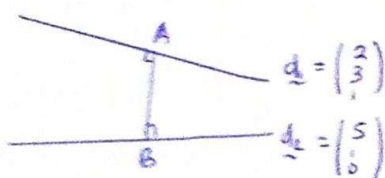
The foot of the perpendicular is $(1, -3, 1) B_1$

$$d_1 = \frac{2(2) - 3(2) + 1 - 1}{\sqrt{(2)^2 + (-3)^2 + (1)^2}} = \frac{-2}{\sqrt{14}} \quad \text{M}$$

$$d_2 = \frac{2(1) - 3(-2) + 1 - 1}{\sqrt{(2)^2 + (-2)^2 + (1)^2}} = \frac{8}{\sqrt{14}} \quad \text{M} \quad (05)$$

Since $d_1 d_2 < 0$, the points M and N lie on the opposite sides of the plane. B

(8)



$$H = \frac{1}{2}$$

$$A(1+2m, -1+3m, m)$$

$$B(-1+5m, 1m, 1)$$

$$\vec{AB} = \vec{OB} - \vec{OA} = \begin{pmatrix} -1+5m \\ 1m \\ 1 \end{pmatrix} - \begin{pmatrix} 1+2m \\ -1+3m \\ m \end{pmatrix} = \begin{pmatrix} 5m-2m-2 \\ n-3m+2 \\ 1-m \end{pmatrix}$$

$$d_1 \cdot \vec{AB} = 0 \quad \text{and} \quad d_2 \cdot \vec{AB} = 0$$

$$\begin{pmatrix} 5m-2m-2 \\ n-3m+2 \\ 1-m \end{pmatrix} \cdot \begin{pmatrix} 2 \\ 3 \\ 1 \end{pmatrix} = 0 \Rightarrow 13n - 14m + 3 = 0 \quad \text{--- (1)}$$

$$\begin{pmatrix} 5m-2m+2 \\ n-3m+2 \\ 1-m \end{pmatrix} \cdot \begin{pmatrix} 5 \\ 0 \\ 0 \end{pmatrix} = 0 \Rightarrow 26n - 13m - 8 = 0 \quad \text{--- (2)}$$

$$26n - 28m = -6 \quad \text{M}$$

$$-26n - 13m = 8$$

$$-15m = -4 \Rightarrow m = \frac{14}{15} \quad \text{A}$$

$$13n - \left(\frac{14 \times 14}{15}\right) = -3 \Rightarrow n = \frac{151}{195}$$

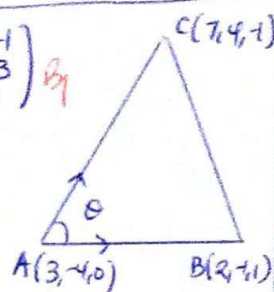
$$\vec{AB} = \begin{pmatrix} 5\left(\frac{151}{195}\right) - 2\left(\frac{14}{15}\right) - 2 \\ \frac{151}{195} - 3\left(\frac{14}{15}\right) + 2 \\ 1 - \frac{14}{15} \end{pmatrix} = \begin{pmatrix} \frac{1}{195} \\ -\frac{1}{39} \\ \frac{1}{15} \end{pmatrix} \quad \text{B}$$

$$|\vec{AB}| = \sqrt{\left(\frac{1}{195}\right)^2 + \left(-\frac{1}{39}\right)^2 + \left(\frac{1}{15}\right)^2}$$

$$= 0.07161 \text{ units} \quad \text{B}$$

$$(9a) \quad \vec{AB} = \begin{pmatrix} 2 \\ 1 \\ 1 \end{pmatrix} - \begin{pmatrix} 3 \\ 4 \\ 0 \end{pmatrix} = \begin{pmatrix} -1 \\ 3 \\ 1 \end{pmatrix} \quad \text{B}$$

$$\vec{AC} = \begin{pmatrix} 7 \\ 4 \\ 1 \end{pmatrix} - \begin{pmatrix} 3 \\ 4 \\ 0 \end{pmatrix} = \begin{pmatrix} 4 \\ 0 \\ 1 \end{pmatrix} \quad \text{B}$$



$$\vec{AC} \cdot \vec{AB} = |\vec{AB}| |\vec{AC}| \cos \theta$$

$$\begin{pmatrix} -1 \\ 3 \\ 1 \end{pmatrix} \cdot \begin{pmatrix} 4 \\ 0 \\ 1 \end{pmatrix} = \sqrt{(-1)^2 + (3)^2 + (1)^2} \sqrt{(4)^2 + (0)^2 + (1)^2} \cos \theta$$

$$-4 + 24 + 1 = \sqrt{11 \times 17} \cos \theta \quad \text{M}$$

$$\cos \theta = \frac{19}{9\sqrt{17}}$$

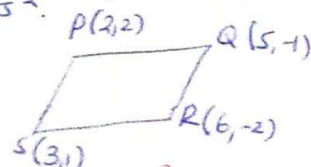
$$\theta = \cos^{-1}\left(\frac{19}{9\sqrt{17}}\right) = 50.47^\circ \quad \text{A}$$

Since the angle is not 0° or 180° , A, B and C are vertices of a triangle. B

$$A = \frac{1}{2} |\vec{AB}| |\vec{AC}| \sin \theta$$

$$= \frac{1}{2} \times 9\sqrt{11} \sin 50.47^\circ \quad \text{M}$$

$$= 11.5114 \text{ units}^2 \quad \text{A}$$



(b)

$$\vec{PS} = \begin{pmatrix} 1 \\ -1 \\ 1 \end{pmatrix} \quad \vec{QR} = \begin{pmatrix} 1 \\ -1 \\ 1 \end{pmatrix} \quad \text{B}$$

$$\vec{PQ} = \begin{pmatrix} 3 \\ -3 \\ 1 \end{pmatrix} = 3\begin{pmatrix} 1 \\ -1 \\ 1 \end{pmatrix} \quad \vec{SR} = \begin{pmatrix} 3 \\ -3 \\ 1 \end{pmatrix} = 3\begin{pmatrix} 1 \\ -1 \\ 1 \end{pmatrix} \quad \text{B}$$

The points P, Q, R and S lie on a straight line and can not form a quadrilateral. B

$$(10a) \quad \begin{pmatrix} x \\ y \\ z \end{pmatrix} = \begin{pmatrix} 1+3\lambda \\ -2+2\lambda \\ 1+5\lambda \end{pmatrix} \quad \text{B}$$

$$2x - y + 4z = 6$$

$$2(1+3\lambda) - (-2+2\lambda) + 4(1+5\lambda) = 32 \quad \text{M}$$

$$24\lambda = 24$$

$$\lambda = 1 \quad \text{A}$$

$$\begin{pmatrix} x \\ y \\ z \end{pmatrix} = \begin{pmatrix} 1+3(1) \\ -2+2(1) \\ 1+5(1) \end{pmatrix} = \begin{pmatrix} 4 \\ 0 \\ 6 \end{pmatrix} \quad \text{M}$$

The point of intersection is (4, 0, 6) A

(08)

(05)

(04)

$$\vec{a} = \begin{pmatrix} 2 \\ -1 \\ 4 \end{pmatrix}, \vec{d} = \begin{pmatrix} 3 \\ 2 \\ 5 \end{pmatrix}$$

$$\vec{a} \cdot \vec{d} = |\vec{a}| |\vec{d}| \sin \theta$$

$$\begin{pmatrix} 2 \\ -1 \\ 4 \end{pmatrix} \cdot \begin{pmatrix} 3 \\ 2 \\ 5 \end{pmatrix} = \sqrt{(2)^2 + (-1)^2 + (4)^2} \sqrt{(3)^2 + (2)^2 + (5)^2} \sin \theta$$

$$6 - 2 + 20 = \sqrt{21 \times 38} \sin \theta$$

$$\theta = \sin^{-1} \left(\frac{24}{\sqrt{21 \times 38}} \right) = 58.17^\circ$$

10b) $2x - y + 4z = 32$ M1
 $2(2) - (-2) + 4(5) = 26 \neq 32$ M1

$$2(1) - 2 + 4(-1) = -4 \neq 32$$

Both points don't lie on the line M1

11 (a) $\frac{x-2}{1} = \lambda \Rightarrow \frac{3-2}{1} = \lambda \Rightarrow \lambda = 1$ M1

$$\frac{2-y}{-2} = 1 \Rightarrow y = 4$$
 M1

$$\frac{z-3}{3} = 1 \Rightarrow z = 6$$
 M1

$$\therefore P \text{ is } (3, 4, 6)$$

$$\vec{PN} = \lambda \vec{d}$$

$$\begin{pmatrix} x \\ y \\ z \end{pmatrix} - \begin{pmatrix} 3 \\ 4 \\ 6 \end{pmatrix} = \lambda \begin{pmatrix} 2 \\ 1 \\ 4 \end{pmatrix}$$

$$\begin{pmatrix} x \\ y \\ z \end{pmatrix} = \begin{pmatrix} 3+2\lambda \\ 4+\lambda \\ 6+4\lambda \end{pmatrix}$$
 M1

$$2x + y + 4z = 13$$

$$2(3+2\lambda) + 4 + \lambda + 4(6+4\lambda) = 13$$
 M1

$$21\lambda + 34 = 13$$

$$21\lambda = -21$$
 M1

$$\lambda = -1$$

$$\begin{pmatrix} x \\ y \\ z \end{pmatrix} = \begin{pmatrix} 3+2(-1) \\ 4+(-1) \\ 6+4(-1) \end{pmatrix} = \begin{pmatrix} 1 \\ 3 \\ 2 \end{pmatrix}$$
 M1

$$\therefore N \text{ is } (1, 3, 2)$$
 M1

11 (b) $\vec{NP} = \lambda \begin{pmatrix} 2 \\ 1 \\ 4 \end{pmatrix}$

$$\vec{p} = \begin{pmatrix} 2 \\ 1 \\ 4 \end{pmatrix}$$
 M1

$$\vec{r} \cdot \vec{p} = \vec{q} \cdot \vec{p}$$

$$\begin{pmatrix} x \\ y \\ z \end{pmatrix} \cdot \begin{pmatrix} 2 \\ 1 \\ 4 \end{pmatrix} = \begin{pmatrix} 1 \\ 3 \\ 2 \end{pmatrix} \cdot \begin{pmatrix} 2 \\ 1 \\ 4 \end{pmatrix}$$
 M1

$$2x + y + 4z = 2 + 2 + 4$$
 M1

$2x + y + 4z = 0$ is the equation of plane M1

12 (a) $\vec{r} = \vec{a}$

$$\begin{pmatrix} 2+\lambda \\ 1+\lambda \\ 2\lambda \end{pmatrix} = \begin{pmatrix} 2+\mu \\ 2+2\mu \\ \mu \end{pmatrix}$$
 M1

$$2+\lambda = 2+\mu$$

$$-1+\lambda = 2+2\mu$$

$$1 = \mu \Rightarrow \mu = -1$$
 M1

$$\lambda = \mu \Rightarrow \lambda = -1$$
 M1

$$2+\lambda = 2+(-1)$$

$$2(-1) = -2 = \mu$$
 M1

$$\mu = -1$$

$$\begin{pmatrix} x \\ y \\ z \end{pmatrix} = \begin{pmatrix} 2-1 \\ 1-1 \\ 2(-1) \end{pmatrix} = \begin{pmatrix} 1 \\ 0 \\ -2 \end{pmatrix}$$
 M1

$\therefore \mu = -1$ and C is $(1, 0, -2)$

1b) $\vec{d}_1 = \begin{pmatrix} 1 \\ 1 \\ 2 \end{pmatrix}, \vec{d}_2 = \begin{pmatrix} 1 \\ 2 \\ 1 \end{pmatrix}$

$$\vec{n} = \vec{d}_1 \wedge \vec{d}_2 = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 1 & 1 & 2 \\ 1 & 2 & 1 \end{vmatrix}$$
 M1

$$= 3\hat{i} - \hat{j} - \hat{k}$$
 M1

$$\vec{n} = \begin{pmatrix} 3 \\ -1 \\ -1 \end{pmatrix}$$

$$\begin{pmatrix} x \\ y \\ z \end{pmatrix} \cdot \begin{pmatrix} 3 \\ -1 \\ -1 \end{pmatrix} = \begin{pmatrix} 2 \\ 1 \\ 0 \end{pmatrix} \cdot \begin{pmatrix} 3 \\ -1 \\ -1 \end{pmatrix}$$
 M1

$$3x - y - z = 6 - 1 + 0$$
 M1

$3x - y - z = 5$ is the equation of the plane. M1

13 (a)

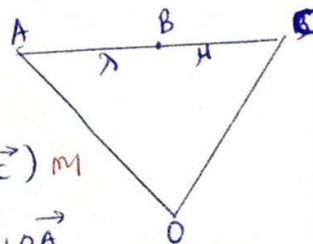
$$\frac{\vec{AC}}{\vec{CB}} = -\frac{\lambda}{\mu}$$
 M1

$$\mu(\vec{OC} - \vec{OA}) = -\lambda(\vec{OB} - \vec{OC})$$
 M1

$$\lambda \vec{OC} - \mu \vec{OC} = \lambda \vec{OB} - \mu \vec{OA}$$

$$(\lambda - \mu) \vec{OC} = \lambda \vec{b} - \mu \vec{a}$$
 M1

$$\vec{OC} = \frac{\lambda \vec{b} - \mu \vec{a}}{\lambda - \mu}$$
 M1



11 (b) $\vec{NP} = \lambda \begin{pmatrix} 2 \\ 1 \\ 4 \end{pmatrix}$

$$\vec{p} = \begin{pmatrix} 2 \\ 1 \\ 4 \end{pmatrix}$$
 M1

$$\vec{r} \cdot \vec{p} = \vec{q} \cdot \vec{p}$$

$$\begin{pmatrix} x \\ y \\ z \end{pmatrix} \cdot \begin{pmatrix} 2 \\ 1 \\ 4 \end{pmatrix} = \begin{pmatrix} 1 \\ 3 \\ 2 \end{pmatrix} \cdot \begin{pmatrix} 2 \\ 1 \\ 4 \end{pmatrix}$$
 M1

$$2x + y + 4z = 2 + 2 + 4$$
 M1

$2x + y + 4z = 0$ is the equation of plane M1

$$\vec{OP} = 3 \begin{pmatrix} -3 \\ -1 \\ -2 \end{pmatrix} - 2 \begin{pmatrix} 5 \\ 3 \\ 6 \end{pmatrix} = \begin{pmatrix} -9 \\ -3 \\ -4 \end{pmatrix} - \begin{pmatrix} 10 \\ 6 \\ 12 \end{pmatrix}$$

$$\vec{OP} = \begin{pmatrix} -19 \\ -9 \\ -16 \end{pmatrix} \quad A_1$$

$$\vec{OQ} = -1 \begin{pmatrix} -3 \\ -1 \\ -2 \end{pmatrix} + 5 \begin{pmatrix} 5 \\ 3 \\ 6 \end{pmatrix} = \frac{1}{4} \begin{pmatrix} 28 \\ 16 \\ 32 \end{pmatrix} = \begin{pmatrix} 7 \\ 4 \\ 8 \end{pmatrix} \quad A_1$$

$$R = \left(-\frac{19+7}{2}, -\frac{9+4}{2}, -\frac{16+8}{2} \right) \quad B_1$$

$$R \text{ is } (-6, -5/2, -5)$$

$$c) \quad d = \begin{pmatrix} 2 \\ 3 \\ 1 \end{pmatrix} \quad B_1$$

$$\begin{pmatrix} x \\ y \\ z \end{pmatrix} = \begin{pmatrix} -6 \\ -5/2 \\ -5 \end{pmatrix} + \lambda \begin{pmatrix} 2 \\ 3 \\ 1 \end{pmatrix} \quad m_1$$

$$\frac{x+6}{2} = \frac{y+5/2}{3} = \frac{z+5}{1} \text{ is the equation of the line.} \quad A_1$$

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$$\vec{OK} = \vec{OP} + \lambda \vec{PS}$$

$$\vec{PS} = \vec{OS} - \vec{OP}$$

$$\vec{OS} = 2\vec{r} - \vec{p}$$

$$\vec{OK} = \vec{OP} + \lambda \vec{PS}$$

$$\vec{RK} = \vec{OK} - \vec{OR}$$

$$= \frac{3}{2}\vec{r} - \vec{s}$$

$$= \frac{3\vec{r} - 2\vec{s}}{2}$$

$$\vec{OK} = \vec{r} + \frac{\mu}{2}(3\vec{r} - 2\vec{s}) \quad \text{--- (2) } B_1$$

comparing (1) and (2)

$$s: 2\lambda = 1 - \mu$$

$$r: 1 - \lambda = \frac{3}{2}\mu$$

$$2 - 2\lambda = 3\mu$$

$$+ 2\lambda = 1 - \mu$$

$$2 = 1 + 2\mu \quad m_1$$

$$2\mu = 1 \Rightarrow \mu = \frac{1}{2} \quad A_1$$

$$2\lambda = 1 - \mu \Rightarrow 2\lambda = \frac{1}{2}$$

$$\lambda = \frac{1}{4} \quad m_1$$

$$\vec{OK} = \vec{r} + \frac{1}{4}(2\vec{s} - \vec{r}) = \frac{4\vec{r} + 2\vec{s} - \vec{r}}{4}$$

$$\vec{OK} = \frac{1}{4}(3\vec{r} + 2\vec{s}) \quad B_1$$

$$\vec{PK} = -\vec{OP} + \vec{OK} = -\vec{r} + \frac{1}{4}(3\vec{r} + 2\vec{s})$$

$$\vec{PK} = \frac{1}{4}(2\vec{s} - \vec{r}) \quad B_1$$

$$\vec{PS} = 2\vec{s} - \vec{r} \Rightarrow \vec{KS} = \vec{PS} - \vec{PK} = (1 - \frac{1}{4})(2\vec{s} - \vec{r})$$

$$= \frac{3}{4}(2\vec{s} - \vec{r})$$

$$\frac{\vec{PK}}{\vec{KS}} = \frac{\frac{1}{4}(2\vec{s} - \vec{r})}{\frac{3}{4}(2\vec{s} - \vec{r})} = \frac{1}{3} \quad A_1$$

$\therefore K$ divides PS in the ratio $1:3$ B_1

$$15) a) \quad d_1 = \begin{pmatrix} 1 \\ 2 \\ 3 \end{pmatrix}, \quad d_2 = \begin{pmatrix} 1 \\ -3 \\ 1 \end{pmatrix} \quad B_1$$

$$n = d_1 \wedge d_2 = \begin{vmatrix} i & j & k \\ 1 & 2 & 3 \\ 1 & -3 & 1 \end{vmatrix} = 7i + 4j - 5k$$

$$r \cdot n = 0 \Rightarrow \begin{pmatrix} x \\ y \\ z \end{pmatrix} \cdot \begin{pmatrix} 7 \\ 4 \\ -5 \end{pmatrix} = 0 \Rightarrow \begin{pmatrix} 7 \\ 4 \\ -5 \end{pmatrix} \cdot \begin{pmatrix} 7 \\ 4 \\ -5 \end{pmatrix} = 0 \quad m_1$$

$7x + 4y - 5z = 0$ is the equation of plane A_1

$$b) \quad n = \begin{pmatrix} 2 \\ 1 \\ 3 \end{pmatrix} - \begin{pmatrix} 1 \\ -1 \\ 2 \end{pmatrix} = \begin{pmatrix} 1 \\ 2 \\ 1 \end{pmatrix} \quad m_1$$

$$r \cdot n = 0 \Rightarrow \begin{pmatrix} x \\ y \\ z \end{pmatrix} \cdot \begin{pmatrix} 1 \\ 2 \\ 1 \end{pmatrix} = 0 \Rightarrow \begin{pmatrix} 1 \\ 2 \\ 1 \end{pmatrix} \cdot \begin{pmatrix} 1 \\ 2 \\ 1 \end{pmatrix} = 0 \quad m_1$$

$x + 2y + z = 0$ is equation of the base A_1

$$r = \begin{pmatrix} 2+t \\ 1-t \\ 3-t \end{pmatrix}$$

$$x + 2y + z = 0$$

$$2t + 2(1-t) + 3-t = 0 \Rightarrow 2t = 6 \Rightarrow t = 3 \quad A_1$$

$$A = (2+3, 1-3, 3-3) \Rightarrow A \text{ is } (5, -2, 0) \quad B_1$$

$$\vec{AB} = \begin{pmatrix} 5 \\ 2 \\ 0 \end{pmatrix} - \begin{pmatrix} 1 \\ -1 \\ 2 \end{pmatrix} = \begin{pmatrix} 4 \\ 3 \\ -2 \end{pmatrix} \quad B_1$$

$$|\vec{AB}| = \sqrt{(4)^2 + (3)^2 + (-2)^2} = \sqrt{29} \text{ units} \quad B_1$$

16) a

$$\vec{PN} = \begin{pmatrix} x-p \\ y-q \\ z-r \end{pmatrix} = \lambda \begin{pmatrix} a \\ b \\ c \end{pmatrix}$$

$$\begin{pmatrix} x \\ y \\ z \end{pmatrix} = \begin{pmatrix} p + \lambda a \\ q + \lambda b \\ r + \lambda c \end{pmatrix}$$

$$ax + by + cz = d$$

$$a(p + \lambda a) + b(q + \lambda b) + c(r + \lambda c) = d \quad m_1$$

$$ap + bq + cr + \lambda(a^2 + b^2 + c^2) = d$$

$$1 - \lambda(a^2 + b^2 + c^2) = |ap + bq + cr - d|$$

$$\lambda = \frac{|ap + bq + cr - d|}{a^2 + b^2 + c^2} \quad B_1$$

$$|\vec{PN}| = \lambda \left| \begin{pmatrix} a \\ b \\ c \end{pmatrix} \right| = \lambda \sqrt{a^2 + b^2 + c^2} = \frac{|ap + bq + cr - d|}{\sqrt{a^2 + b^2 + c^2}} \quad m_1$$

$$\text{Shortest length} = \frac{|ap + bq + cr - d|}{\sqrt{a^2 + b^2 + c^2}} \quad A_1$$

$$b) \quad l = \frac{14}{\sqrt{(2)^2 + (-4)^2 + (3)^2}} = \frac{14}{7} = 2 \text{ units} \quad A_1$$

$$c) \quad d = \frac{|28 - 21|}{\sqrt{(4)^2 + (-2)^2 + (6)^2}} = \frac{7}{\sqrt{36}} = \frac{7}{6} = 1.166 \text{ units} \quad A_1$$