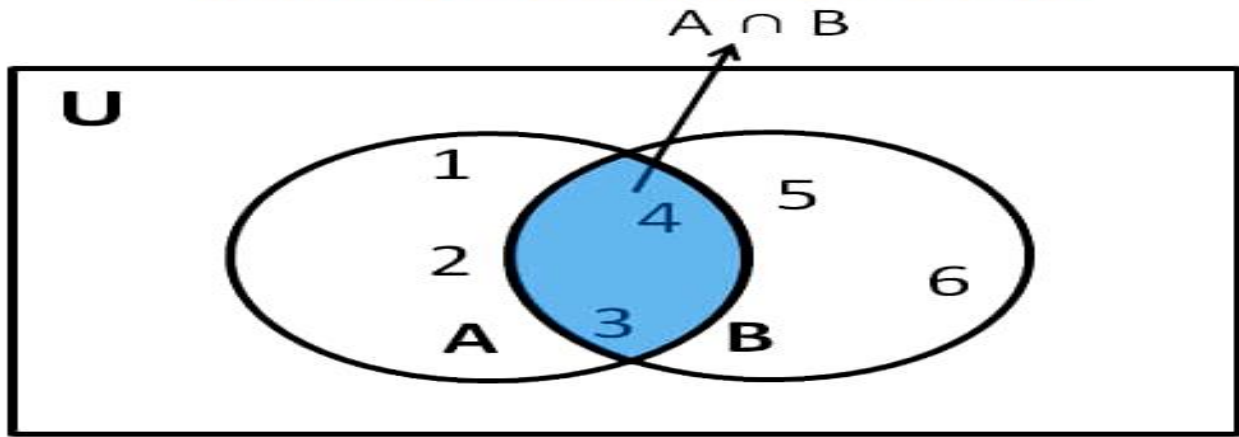


MTC

Teachers' Handbook

P.5 LESSON NOTES

Intersection of Sets



TERM 1 2024

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Name:

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STANDARD CURRICULUM



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QUALITY WORK

TERM 1 TOPICS

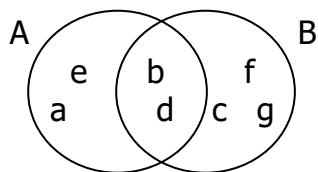
- SET CONCEPTS
- WHOLE NUMBERS
- OPERATIONS ON WHOLE NUMBERS
- PATTERNS AND SEQUENCES

WK. 1: Holiday work marking and corrections

TOPIC ONE. SETS

Review of P.4 work on sets (lesson 1,2 and 3)

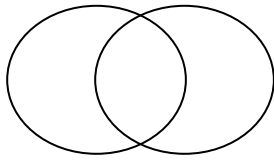
1. Draw set symbols for:
 - a) Subset of
 - b) Union set
 - c) Intersection set
 - d) Null set
 - e) Equal set
 - f) Non equivalent set
 - g) Equivalent set
 - h) Non equivalent set.
2. Given that Set $A = \{1, 2, 3, 4\}$
 $B = \{5, 6, 7, 8\}$
 $C = \{1, 3, 4, 2\}$ and
 $D = \{a, e, I, o, u\}$
 - a) Describe set A
 - b) Using symbols show the relationship between sets
 - (i) A and C
 - (ii) B and C
 - (iii) A and D.
3. Draw a Venn diagram and shade the regions below.
 - (i) $A \cap B$
 - (ii) $P \cup Q$
 - (iii) $F - G$
 - (iv) $G - F$
4. Study the Venn diagram below and answer the questions that follow.



- iv) Find $n(A \cup B)$

5. Given that $X = \{0, 1, 2, 3, 4\}$ and $Y = \{1, 3, 6, 9, 12\}$

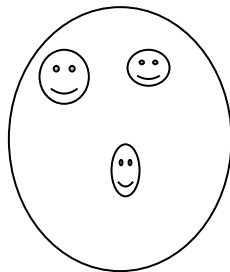
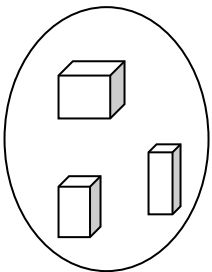
- a) Represent the two sets on the Venn diagram.



- b) From the Venn diagram, find

- (iii) $n(Y - X)$

Forming sets



Let the learners pick two sets and compare to find out whether they are equal or equivalent sets.

Activity

Forming sets from a big set with emphasis on the numbers.

Using symbols of $=$ or \leftrightarrow to describe the sets formed.

Ref; The winner mathematics book 5 page 1

Week 2 lesson 1 and 2

Complement of sets

Complement of a set means a set of members not in the givenset.

OR

Complement of the universal set are elements in the universal set but not in the given set.

EXAMPLE

Given that; $p = \{4, 3, 6, 7, 9\}$ and

$Q = \{1, 2, 3, 6, 7\}$

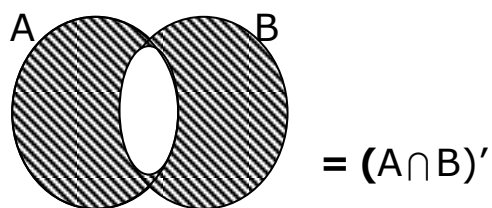
Write down members in p' [complement of set p]

$p' = \{1, 2, 3, 5, 7\}$

a. Find $n[p \cap q]$

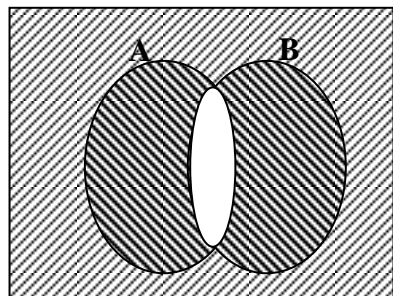
Note: The symbol for complement of a set

Shading regions for complement of a set

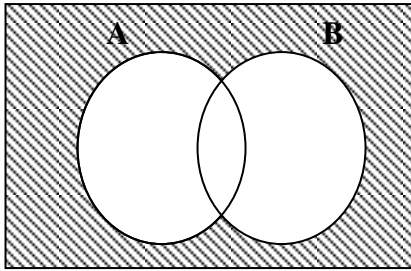


$A \cap B$ the complement

=



Draw and shade $(A \cup B)'$



ACTIVITY

Mk Book 6 page 8 - 15.

WK. 2: Lesson 3

SUBSETS

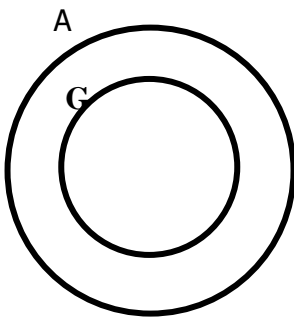
A subset is a small set got from a big set.

The bigger set from which a subset is got is called a Universal set or Super set.

The symbol for a subset is \subset

The symbol for not a subset is $\not\subset$ The symbol for Universal set is ξ .

1. Draw a Venn diagram to show that all goats (G) are Animals (A)



2. Given that set $Q = \{a, b, c\}$ List down all the subsets in set Q }.

$\{a\}, \{b\}, \{c\}$

$\{a,b\}, \{a,c\}, \{b,c\}$

$\{\}, \{a, b, c\} \implies$ Subsets \implies 8 in number.

N.B The empty set and the set itself (universal) are subsets of every set.

3. By calculating, find the number of subsets in set K if $K = \{7, 5, 3\}$

No. of subsets = 2^n where n represents the number of elements in the given set.

∴ Set K has 3 elements

$$\therefore n(c) = 2^n$$

$$= 2^3$$

$$= 2 \times 2 \times 2$$

$$= 4 \times 2$$

= 8 subsets

Ref: Mk. Bk 7 Pg 2

WK2: Lesson 4 & 5

APPLICATION OF SETS

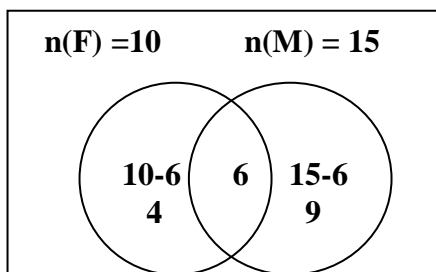
In a class of pupils, 15 eat fish (F) 10 eat meat (m) and 6 eat both fish and meat

$$n(F) = 15$$

$$n(m) = 10$$

$$n(F \cap m) = 6$$

a) Represent the above information on a Venn diagram.



b) How many pupils eat only fish?

$$10 - 6$$

4 pupils

c) How many pupils eat only meat?

$$15 - 6$$

9 pupils

d) How many pupils are in that class?

$$(10 + 6) + 6 + (15 - 6)$$

$$4 + 6 + 9$$

$$10 + 9$$

= 19 pupils

e) How many pupils like only one type of food?

Fish only + meat only

$$(10 - 6) + 15 - 6$$

$$4 + 9$$

= 13 pupils

2. Given that $n(A) = 15$ $n(B) = 25$ $n(A \cap B) = 5$

a) Represent the above information on a Venn diagram

REF: Mk book 6 pg 23-25

WK. 3: Lesson 1

Tossing a coin

A coin has 2 faces ahead and a tail. When it is tossed, the probability of a head or a tail showing up is a half. (Mk bk. 5 & functional Bk. 5)

Tossing a dice

A dice has 6 faces. The probability of getting one of the faces showing up is a sixth.

More about probability

Example.

- 1) What is the probability of picking a ripe mango, if there are 4 ripe mangoes and 6 rotten mangoes in a basket?
- 2) Probability about days of the week and months of the year.

TOPIC: WHOLE NUMBERS

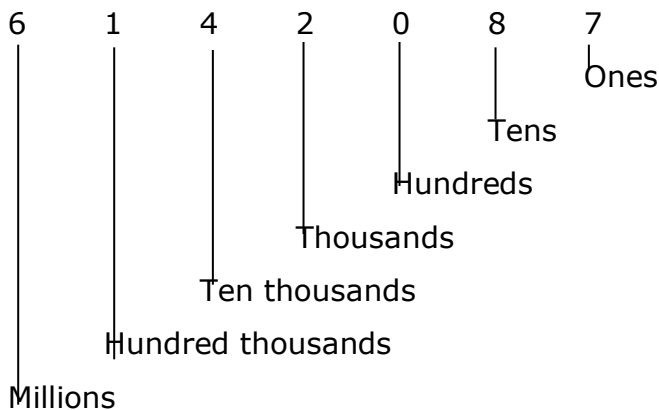
Review:

- Forming numerals from digits

WK. 3: Lesson 2

PLACE VALUES AND VALUES OF WHOLES

Reviewing place values up to millions.



Give the value of each digit in 4123456.

NUMBER	DIGIT	PLACE VALUE	VALUE
6,142,572	6	MILLIONS	$6 \times 1,000,000 = 6,000,000$
	1	HUNDRED THOUSANDS	$1 \times 100,000 = 100,000$
	4	TEN THOUSANDS	$4 \times 10,000 = 40,000$
	2	THOUSANDS	$2 \times 1000 = 2000$
	5	HUNDREDS	$5 \times 100 = 500$
	7	TENS	$7 \times 10 = 70$
	2	ONES	$2 \times 1 = 2$

REF: MK Bk 5 page 26 – 27

Functional MTC Bk. 5 pg. 17

WK. 3: Lesson 3

Writing figures in words

When writing in words, we group the number into it's major groups:

Example

4,156036

Millions	Thousands	Units
H T O	H T O	H T O
	1 5 6	0 3 6
4		

4 156 036 → **Four millions one hundred fifty six thousands thirty six.**

REF: Understanding MTC bk 5 pg 13, bk 6 pg 23

Prim MTC, Macmillan bk 5 pg 18 – 19

WK. 3: Lesson 4

Writing words in figures

Write six hundred two thousand, four hundred sixty four in figures.

Solution: breakdown the number in its groups.

Six hundred two thousand = 602,000

Four hundred sixty four = + 464

602,464

Example II

Write two million, seven hundred sixty five thousand four hundred thirty two in figures.

Two million \longrightarrow 2,000,000
Seven hundred sixty five thousand \longrightarrow 765,000
Four hundred thirty two \longrightarrow $\begin{array}{r} + \\ 432 \end{array}$
2,765,432

REF: Mk bk 6 pg 38 -39.

MK. BK 5 PAGE 28-29

Wk.3 lesson 5

EXPANTION OF WHOLE NUMBERS USING VALUES AND POWERS OF BASE TEN.

1. Expand 349 using values.

$$349 = (3 \times 100) + (4 \times 10) + (9 \times 1) \\ 300 + 40 + 9$$

2. Expand 48914 using values

3. Expand 148 using powers/ exponents.

4. Expand 7962 using,

i. Place values

ii. Values

iii. Powers of ten/ exponents

5. Writing expanded numbers as single numbers/ short form

a. $(2 \times 10^3) + (4 \times 10^2) + (3 \times 10^1) + (7 \times 10^0)$

b. $(50000) + (6000) + (400) + (60) + (7)$

c. $(6 \times 10^2) + (4 \times 10^1) + (3 \times 10^0)$

d. $(5 \times 10000) + (2 \times 1000) + (7 \times 100) + (6 \times 10) + (9 \times 1)$

WK. 4 Lesson 1

ROMAN NUMERALS

HINDU	1	5	10	50	100	500	1000
ROMAN	I	V	X	L	C	D	M

A) **Repeated Roman numerals**

Numbers with 2 and 3.

$$2 = I + I = \underline{II}$$

$$20 = 10 + 10 = \underline{XX}$$

$$3 = I + I + I = \underline{III}$$

$$30 = 10 + 10 + 10 = \underline{XXX}$$

$$2000 = 1000 + 1000 = \underline{MM}$$

$$3000 = 1000 + 1000 + 1000 = \underline{MMM}$$

$$200 = 100 + 100 = \underline{CC}$$

$$300 = 100 + 100 + 100 = \underline{CCC}$$

B) **Subtraction Roman Numerals**

(Number with 4 and 9)

$$4 = (5 - 1) = \underline{IV}$$

$$40 = (50 - 10) = \underline{XL}$$

$$9 = (10 - 1) = \underline{IX}$$

$$90 = (100 - 10) = \underline{XC}$$

$$400 = (500 - 100) = \underline{CD}$$

$$900 = (1000 - 100) = \underline{CM}$$

WK.4 Lesson 2

C) **Addition Roman numerals**

Numbers with (6, 7 and 8)

$$6 = (5+1) = \underline{VI}$$

$$60 = 50 + 10 = \underline{LX}$$

$$600 = 500 + 100 = \underline{DC}$$

$$7 = (5+2) = \underline{VII}$$

$$70 = (50+20) = \underline{LXX}$$

$$700 = 500 + 200 = \underline{DCC}$$

$$8 = (5+3) = \underline{VIII}$$

$$80 = (50 + 30) = \underline{LXXX}$$

$$800 = 500 + 300 = \underline{DCCC}$$

Examples

Write the following as Roman numerals.

i) $75 = 70 + 5$

$$= LXX + V$$

$$= \underline{LXXV}$$

$$445 = 400 + 40 + 5$$

$$= CD + XL + V$$

$$= \underline{CDXLV}$$

Changing roman numerals to Hindu – Arabic

Express LXXVI in Hindu – Arabic numerals

$$= LXX + VI$$

$$= 70 + 6$$

$$= \underline{76}$$

Mzee Yokana was born in the year MCMXLII. Express this year in Hindu – Arabic.

$$MCMXLII = M + CM + XL + II$$

$$1000 + 900 + 40 + 2$$

$$\underline{1942}$$

REFERENCE: Mk bk 5 pg 37 – 38

Fountain MTC Bk 5 pg 42 – 46

WK.4: Lesson 3 & 4

ROUNDING OFF WHOLE NUMBERS

Rounding off means expressing a given number as an estimate (rounded) rather than an exact number.

When rounding off, we consider that, if the digit on the right of the required place value is less than 5 we add to it 0 and replace all digits on it's right with 0's.

If the figure on the right of the place value is 5 or more add one to it.

Example

Round off 214 to the nearest tens.

H	T	O
2	1	4
	0	
<hr/>		
2	1	0

Example II

Round off 7591 to the nearest thousands.

Th	H	T	O
7	5	9	1
1	↓	↓	↓
<hr/>			
8	0	0	0
<hr/>			
∴ 7591 ≈ <u>8000</u>			

WK. 4: Lesson 5

OPERATION ON WHOLE NUMBERS

Review of work done in P.4 on addition and subtraction.

Ref: MK. MTC BK. 5 pg 48 – 51

Addition and its application

45038+24826

45038

+24826

69864

Mutoto has 1637 cows and Musaja has 374 more cows than Mutoto. How many cows do they have altogether?

No of cows for Musaja = No of cows for Mutoto + 374

$$1637 + 374 = 2011$$

$$\text{Total number of cows altogether } 2011 + 1637 = 3648$$

Subtraction and its application

A bus carries 172 passengers while an Omni bus carries 68. How many more people does a bus carry than an Omni bus?

$$45945 - 3243$$

$$45945$$

$$\underline{-3243}$$

$$\underline{42702}$$

Reference: St Bernard Mathematics book 5 page 32-33

WEEK 5 Lesson 1

MULTIPLICATION

Terms used: product

Example

- 1) Find the product of 28 and 23.

28	23 = 20 + 3
X 23	
28 x 20 = 560	
28 x 3 = + 84	
<u>644</u>	

- 2) In Moses' house there are 13 rooms and each room has 24 chairs. How many chairs are there altogether?

13	24 = 20 + 4
X 24	
13 x 4 = 52	
13 x 20 = + 260	
<u>312</u> chairs	

REFERENCE:

Understanding MTC bk 5 pg 42 – 45, MK BK. 6 pg 58 – 60
Macmillan MTC

WK. 5 : Lesson2

DIVISION

Terms used: **share.**

Quotient

Share 288 book s equally among 12 classes.

$$\begin{array}{r} 024 \\ 12 \overline{)288} \\ 0 \times 2 = 0 \underline{} \\ 28 \\ 2 \times 12 = 24 \underline{} \\ 48 \\ 4 \times 12 = 48 \underline{} \end{array}$$

1	12
2	24
3	36
4	48
5	60
6	72
7	84
8	96
9	108

Each class gets 24 books

REFERENCE: Understanding MTC bk 5 pg 50 – 56
Mk MTC bk. 5 pg. 58 – 62

WK. 5: Lesson 3

MIXED OPERATION (BODMAS)

Brackets

Of

Division

Multiplication

Addition

Subtraction

1) Workout: $240 \div (5 \times 8)$

$$240 \div 40$$

$$\frac{240}{40} = \underline{\underline{6}}$$

40

2) Simplify: $8 - 12 + 4$

$$8 + 4 - 12$$

$$12 - 12$$

0

REFERENCE: Understanding MTC bk 5 pg 56 - 62 MK. MTC BK. 5 PG. 63

WK. 5: Lesson 4

BASES

- Introduction
- Names of bas
 - The digit used in each base.
 - Place values

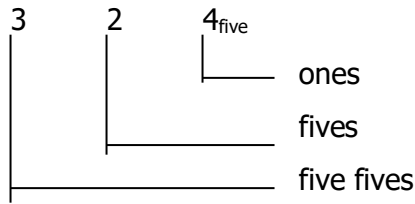
Bases: are systems of counting or grouping numbers.

Below are some of the systems their names and digits used in each.

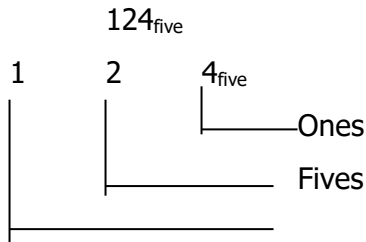
Base	Name of base	Digits used
Base Two	Binary	0, 1
Base Three	Ternary	0, 1, 2
Base Four	Quaternary	0, 1, 2, 3
Base Five	Quinary	0, 1, 2, 3, 4
Base Six	Senary	0, 1, 2, 3, 4, 5
Base Seven	Septenary	0, 1, 2, 3, 4, 5, 6
Base Eight	Octal	0, 1, 2, 3, 4, 5, 6, 7
Base nine	Nonary	0, 1, 2, 3, 4, 5, 6, 7, 8
Base Ten	Decimal (denary)	0, 1, 2, 3, 4, 5, 6, 7, 8, 9

Place values in base five

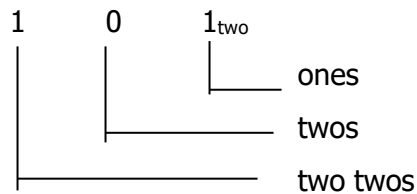
Give the place value of each of the digits in 324_{five}



Example II



In base two the place values are:



Writing bases in words

A part from base ten (decimal base), when writing other bases in words we name their individual digits.

Example

- i) 43_{five} in words is written as
Four, three, base five.
- ii) 213_{five} = Two, one, three, base five.

REFERENCE: MK Bk 5, pg 70 – 71

WK. 5: Lesson 5

EXPANDING BASES

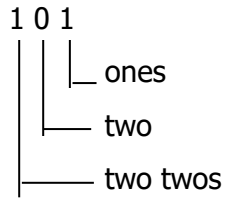
Example

Expand 13_{five}

13	=	(1 group of fives) (3ones)
$\begin{array}{ l} 1 \\ 3 \end{array}$	=	(1 x fives) + (3xones)
$\begin{array}{ l} 1 \\ 3 \end{array}$	=	<u>(1 x 5) + (3 x 1)</u>

Example III

Expand $1\ 0\ 1_{\text{two}}$



$$(1 \times 2 \times 2) + (0 \times 2) + (1 \times 1)$$

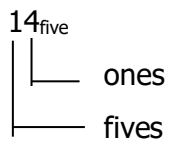
(REF: MK. BK. 5, PG. 71)

Wk6. Lesson 1

CHANGING FROM BASE FIVE TO BASE TEN

Example I

Change 14_{five} to base ten



$$= (1 \times 5) + (4 \times 1)$$

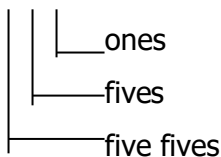
$$5 + 4$$

$$= \mathbf{9_{ten}}$$

Example II

Change 213_{five} to base ten

Place values 2 1 3



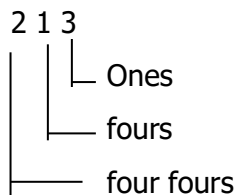
$$= (2 \times 5 \times 5) + (1 \times 5) + (3 \times 1)$$

$$50 + 5 + 3$$

$$= \mathbf{58_{ten}}$$

Example III

Change $2\ 1\ 3_{\text{four}}$ to base five.



$$(2 \times 4 \times 4) + (1 \times 4) + (3 \times 1)$$

$$(8 \times 4) + 4 + 3$$

$$= \mathbf{39_{ten}}$$

WK.6: Lesson 2

CHANGING FROM BASE TEN TO OTHER BASES

Change 9_{ten} to base five

	No.	Rem
5	9	4
	1	

$= 14_{\text{five}}$

Change 58_{ten} to base five.

	No.	Rem
5	58	3
5	11	1
	2	

$\therefore 58_{\text{ten}} = 213_{\text{five}}$

Express 33_{ten} to base three

	No.	Rem
3	33	0
3	11	2
3	3	0
	1	

$33_{\text{ten}} = 1020_{\text{three}}$

REFERENCE: MK BK 5 pg 72 // Mk. MTC Bk.7, Pg. 43 (Old edition)

WK. 6: Lesson 1

& Lesson 2

ADDITION OF BASES

Workout: $24_{\text{five}} + 33_{\text{five}}$

$$\begin{array}{r} 24_{\text{five}} \\ + 33_{\text{five}} \\ \hline 112_{\text{five}} \end{array}$$

$$\begin{aligned} 4 + 3 &= 7 \div 5 = 1^{\text{r}2} \\ 1 + 2 + 3 &= 6 \div 5 = 1^{\text{r}2} \end{aligned}$$

In addition if the answer is bigger than the base we divide, write the remainder and regroup the answer.

Example I

$$\begin{array}{r} 10011_{\text{two}} + 1100_{\text{two}} \\ 10011_{\text{two}} \\ \underline{1100_{\text{two}}} \\ \mathbf{11111_{\text{two}}} \end{array}$$

ACTIVITY: Understanding MTC bk 6 pg 46 – 47 // MTC bk 7 pg 40

WK. 6: Lesson 4

SUBTRACTION OF BASES

Example: $101_{\text{two}} - 11_{\text{two}}$

$$\begin{array}{r} 101_{\text{two}} \\ - 11_{\text{two}} \\ \hline 010 \end{array} \Rightarrow \mathbf{10_{\text{two}}}$$

Subtract: $40_{\text{five}} - 22_{\text{five}}$

$$\begin{array}{r} 40_{\text{five}} \\ - 22_{\text{five}} \\ \hline 13_{\text{five}} \end{array}$$

REFERENCE: Fountain MTC Bk. 5 pg 80 – 81

WK. 6: Lesson 5

MULTIPLICATION OF BASES

$$\begin{array}{r} 2_{\text{five}} \times 3 \\ \underline{11_{\text{five}}} \\ 6 \div 5 = 1^1 \end{array}$$

$$421_{\text{five}}$$

$$\times 3$$

$$\underline{2313_{\text{five}}}$$

REFERENCE: Mk bk 5 pg 74

Fountain MTC Bk. 5 pg 34

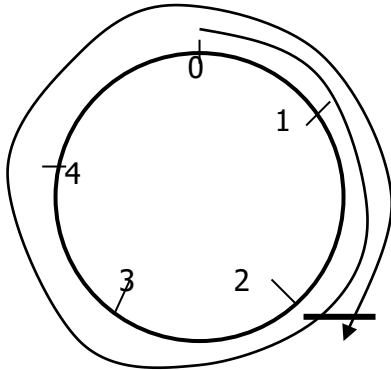
WK 7: Lesson 1

FINITE SYSTEMS

This is a system of grouping where we consider only the remainders.
It can also be called modular (mod) or clock Arithmetic.

Grouping in finite systems

Finite 5.



$$7 = 2 \text{ (finite 5)}$$

By calculation

$$\begin{aligned} 7 &= 7 \div 5 \\ &= 1r2 \end{aligned}$$

$$7 = 2 \text{ (finite 5)}$$

Express 10 in finites

$$\begin{aligned} 9 &= 10 \div 5 \\ &= 2r0 \end{aligned}$$

$$10 \equiv 0 \text{ (finite 5)}$$

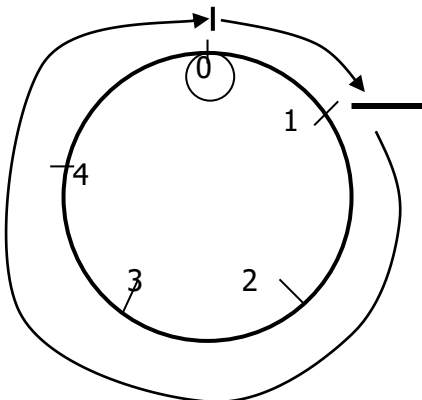
REFERENCE: MK MTC bk 5 pg 204 – 208, MK MTC 2000 Bk.5 PG. 89 – 92

WK 7: Lesson2

ADDITION IN FINITE SYSTEMS

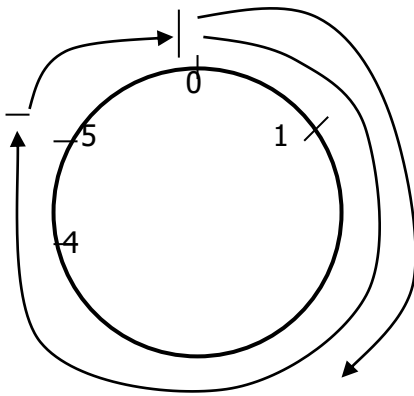
Using a dial

Add: $1 + 4$ (finite 5)



$$1 + 4 = 0 \text{ (finite 5)}$$

ii) $4 + 2 + 3$ (finite 7)



$4 + 2 + 3 + 2$ (finite 7)

$1 + 4 +$ (finite 5)

Reference: MK MTC Bk. 5 pg 212, MK MTC 2000 Bk. 5, pg 92 – 94

WK 7: Lesson 3

SUBTRACTION IN FINITE

1. $3 - 4 = \underline{\hspace{1cm}}$ (finite 5)

$(5 + 3) - 4$

$8 - 4 = 4$

2. $6 - 5 = \underline{\hspace{1cm}}$ (mod 7)

$6 - 5 = 1(\text{mod } 7)$

APPLICATION OF FINITE 7

If today is Tuesday, what day of the week will it be after 17 days from now?

Ref: MK Bk 7, pg 330

WK. 7: Lesson 4

PATTERNS AND SEQUENCES

Review of P.4 Work on G.C.F and L.C.M from listed factors and multiples

Mk MTC Bk. 5 pg 80 – 82

TYPES OF NUMBERS.

1) Whole numbers $\Rightarrow 0, 1, 2, 3, 4, 5, \dots$

2) Counting numbers/ Natural numbers $\Rightarrow 1, 2, 3, 4, 5, \dots$

3) Odd numbers: These are numbers that give a remainder when divided by 2

$\Rightarrow \{1, 3, 5, 7, \dots\}$

4) Even numbers: These are ones that are exactly divisible by two

$\Rightarrow \{0, 2, 4, 6, 8, 10, \dots\}$

- 5) Prime numbers: These are numbers with only two factors.
 $\Rightarrow \{2, 3, 5, 7, 11, 13, \dots\}$
- 6) Composite numbers: These are numbers with more than 2 factors
 $\Rightarrow \{4, 6, 8, 9, 10, 12, \dots\}$
- 7) Square numbers: These are numbers got by multiplying a number by its self.
 $\Rightarrow \{1, 4, 9, 16, 25, \dots\}$
- 8) Cubic numbers: These are got by multiplying the same number three times.
 $\{1, 8, 27, 64, \dots\}$ Triangular numbers: These are got by adding consecutive counting numbers.
- $$\{1, 3, 6, 10, 15, 21, \dots\}$$
- $$\begin{array}{cccccc} & \underbrace{1} & \underbrace{2} & \underbrace{3} & \underbrace{4} & \underbrace{5} & \underbrace{6} \\ & +2 & +3 & +4 & +5 & +6 & \end{array}$$

REFERENCE: Understanding MTC bk 6 pg 81 – 84
Mk Bk 5 Pg 80 – 89

WK 8: Lesson 1&2

DIVISIBILITY TESTS

These show which number is exactly divisible by another given number.

Divisibility test for 2.

A number is divisible by 2 if the last digit is an even number

i.e 0, 2, 4, 6, 8,

Divisibility test for 3.

A number is divisible by 3 if the sum of its digits is divisible by 3.

Example

State whether 144 is divisible by 3.

$$\begin{array}{l} \text{Sum of the digits} \qquad 1 + 4 + 4 \\ \qquad \qquad \qquad = 9 \end{array}$$

9 is divisible by 3

\therefore 144 is divisible by 3.

Divisibility test for 4

A number is divisible by 4 if its last two digits are zero or divisible by 4.

Divisibility test for 5

A number is divisible by 5 if its last digit is either 0 or 5.

Divisibility test for 6

A number is divisible by 6 if it is even and the sum of its digits is divisible by 3.

Example:

Is 612 divisible by 6 ?

612 is divisible by 6 since it is an even number and the sum of its digits ($6+1+2=9$) as shown is divisible by 3.

Divisibility test for 7

When the last digit of a number is doubled and the result is subtracted from the number formed by the remaining digits, the result must be divisible by 7.

Example:

Is 861 divisible by 7?

The last digit is 1 and the number formed by the remaining digits is 86.

When 1 is doubled it gives $(1+1) = 2$. Subtract 2 from 86 $(86-2) = 84$.

84 is divisible by 7 \therefore 861 is also divisible by 7.

Note: For big numbers that cannot easily be detected as numbers divisible by 7, repeat the same procedure on the last result obtained after subtracting.

Divisibility test for 9

A number is divisible by 9 if the sum of its digits is divisible by 9.

Example:

198: The sum of 198 is $1 + 9 + 8 = 18$

18 is divisible by 9 therefore 198 is divisible by 9.

Divisibility test for 10

A number is divisible by 10 if its last digit is 0.

REFERENCE: MK BK 6 pg 65 – 67.

WK.8: Lesson 3**PRIME FACTORIZATION OF NUMBERS**

Prime factorizing means dividing a number by its prime factors.

We use prime factors when prime factorizing e.g. $= \{2, 3, 5, 7, 11, 13 \dots\}$

Example I

Prime factorize 18.

We can either use a ladder or a factor tree. i.e.

2	18
3	9
3	3

We can represent the prime factors as follows.

- Set notation / subscript form

$$18 = \{2_1, 3_1, 3_2\}$$

- **Multiplication form**

$$18 = 2 \times 3 \times 3$$

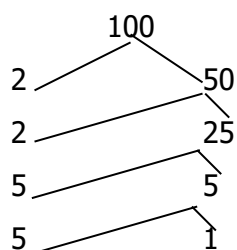
power form (expanded form)

$$18 = 2^1 \times 3^2$$

Example II

Prime factorize 100.

* Take note of factors of 100 that are prime numbers.



Subscript form ÷

$$100 = \{2_1, 2_2, 5_1, 5_2\}$$

Multiplication form

$$100 = 2 \times 2 \times 5 \times 5$$

Power form

$$100 = 2^2 \times 5^2$$

Ref: MK MTC BK. 5 pg 84 – 85, Fountain MTC BK. 5 pg 106 – 108

Understanding MTC Bk. 5 Pg. 79 – 81

WK. 8: Lesson 4

FINDING L.C.M BY PRIME FACTORIZING

Example

Find the L.C.M of 4 and 12 by prime factorization.

2	4	12
2	2	6
2	1	3
3	1	1

$$\text{L.C.M} = 2 \times 2 \times 3$$

$$= 4 \times 3$$

$$= \underline{\underline{12}}$$

Example II

Find the L.C.M of 12 and 20.

2	12	20
2	6	10
3	3	5
5	1	5
	1	1

$$\begin{aligned}\text{L.C.M} &= 2 \times 2 \times 3 \times 5 \\ &= 4 \times 15 \\ &= \underline{\underline{60}}\end{aligned}$$

REFERENCE: MK MTC Bk 5 pg 86.

WK. 8: Lesson 5**FINDING G.C.F BY PRIME FACTORIZING****Example:**

Find the G.C.F of 6 and 8

2	6	8
	3	4

$$\underline{\underline{\text{G.C.F} = 2}}$$

Example II

Find the G.C.F of 24 and 36.

2	24	36
2	12	18
3	6	9
	2	3

$$\text{G.C.F} = 2 \times 2 \times 3$$

$$\text{Reference:} \quad = 4 \times 3 = \underline{\underline{12}}$$

NEW MK. BK 5 PAGE 87**WK. 9 : Lesson 1****REPRESENTING PRIME FACTORS ON VENN DIAGRAMS****Example I**

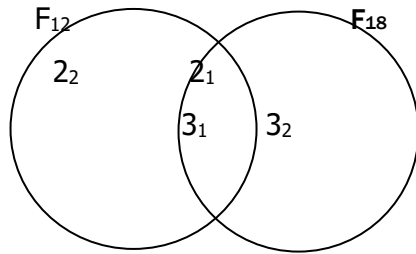
Represent the prime factors of 12 and 18 on a Venn diagram.

2	12
2	6
3	3
	1

2	18
3	9
3	3
	1

$$F_{12} = \{ 2_1, 2_2, 3_1 \}$$

$$F_{18} = \{ 2_1, 3_1, 3_2 \}$$



a) Find the G.C.F of 12 and 18.

G.C.F product of the intersection

$$F_{12} \cap F_{18} = \{2_1, 3_1\}$$

$$\therefore \text{G.C.F} = 2 \times 3$$

6

L.C.M = product of the union.

$$F_{12} \cup F_{18} = \{2_1, 2_2, 3_1, 3_2\}$$

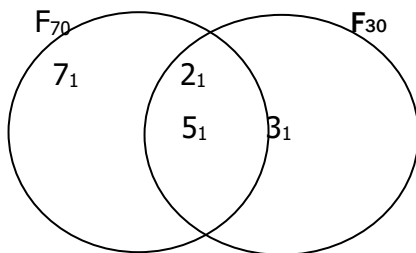
$$= 2 \times 2 \times 3 \times 3$$

$$= 4 \times 9$$

$$= \textbf{36}$$

Example 2

Below is a Venn diagram showing factors.



a) Find the G.C.f of 70 and 30.

G.C.F = product of the intersection

$$F_{70} \cap F_{30} = \{2_1, 5_1\}$$

$$\text{G.C.F} = 2 \times 5$$

$$= \textbf{10}$$

b) Find the L.C.M of 20 and 70.

L.C.M = product of the union

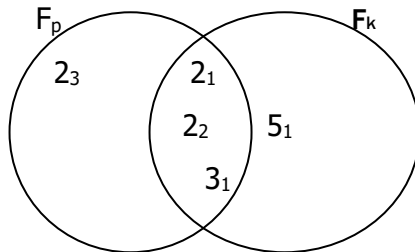
$$\text{L.C.m} = 2_1 \times 3_1 \times 5_1 \times 7_1$$

$$= 6 \times 35$$

$$\textbf{L.C.M} = \textbf{210.}$$

WK. 9 : Lesson 2

FINDING THE UNKNOWN NUMBER GIVEN PRIME FACTORS ON A VENN DIAGRAM



a) Find the value of p.

$$F_p = \{2_1, p, 2_2, 3_1\}$$

$$p = 4 \times 6$$

$$p = \underline{24}$$

b) Find the value of k.

$$F_k = \{2_1, 2_2, 3_1, 5_1\}$$

$$p = 2_1 \times 2_2 \times 3_1 \times 5_1$$

$$p = 2 \times 2 \times 3 \times 5$$

$$p = 4 \times 15$$

$$p = \underline{60}$$

REFERENCE: MK BK 6 Pg 88 – 89

WK.9 : Lesson 3,4 and 5

SQUARE ROOTS OF NUMBERS

Review of square numbers.

i.e. $\{1, 4, 9, 16, 25, 36, 49, 64, 81, \dots\}$

A square number is got by multiplying a number by itself.

A square root is a number that is multiplied by its self to give a square number.

The symbol for square root is $\sqrt{\quad}$

Example

Find the square root of 36.

2	36	$\sqrt{36} = \sqrt{(2 \times 2) \times (3 \times 3)}$
2	18	$\sqrt{36} = 2 \times 3$
3	9	$= \underline{6}$
3	3	

Example:

Find the square root of 100.

2	100
2	50
5	25
5	5
	1

$$\begin{aligned}
 \sqrt{100} &= \sqrt{(2 \times 2) \times (5 \times 5)} \\
 &= 2 \times 5 \\
 &= \mathbf{10}
 \end{aligned}$$

Ref: MK MTC BK. 5 pg. 89, MK MTC BK. 6 pg. 95