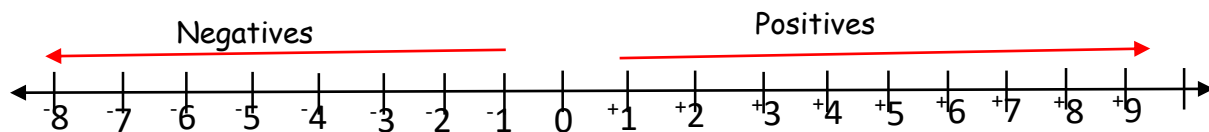


## TOPIC: INTEGERS

### CONTENT: Introduction and ordering integers

- An integer is a positive (+) or negative (-) number and zero.
- Examples of integers are {...-4,-3,-2,-1,0,+1,+2,+3,+4.....}
- Zero (0) is neither a negative (-) nor a positive integer.
- Integers can be represented on a number line.
- On a number line, positive (+) integers are put on the right hand side while negative (-) integers are put on the left as shown below



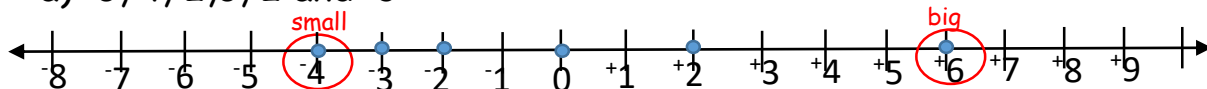
### Ordering integers

Integers can be ordered in either ascending or descending order

#### Examples

1. Arrange the following integers in ascending order

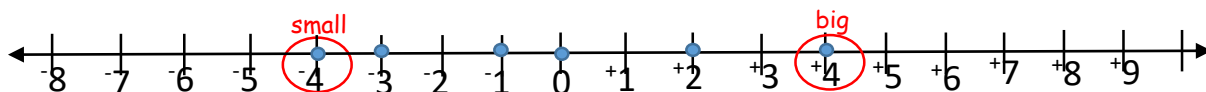
a) +6, -4, +2, 0, -2 and -3



Ascending order = {-4, -3, -2, 0, +2, +6}

2. Arrange the following integers in descending order

a) +4, -4, +2, 0, -1 and -3



Descending order = {+4, +2, 0, -2, -3, -4}

## Activity

1. Arrange the following integers in ascending order

a)  $+5, -3, +3, 0, -1$  and  $-4$

b)  $-5, -2, +4, 0, +1$  and  $-6$

c)  $+6, -7, +5, 0, -4$  and  $+3$

d)  $+4, -4, +2, 0, -1$  and  $-3$

2. Arrange the following integers in descending order

a)  $-5, -3, +3, 0, -1$  and  $+4$

b)  $+7, -3, +3, 0, -1$  and  $-4$

c)  $+4, -2, +3, 0, +1$  and  $-1$

d)  $+6, -3, +3, 0, -1$  and  $+4$

---

## Comparing integers using $<$ or $>$ or $=$

Examples

1. Compare the following integers using  $<$  or  $>$  or  $=$

a)  $-100 < 0$

b)  $+67 > -67$

c)  $-10 > -50$

## Activity

1. Compare the following integers using  $<$  or  $>$  or  $=$

a)  $-10 \dots \dots \dots 0$

b)  $+60 \dots \dots \dots -60$

c)  $-1 \dots \dots \dots -5$

d)  $-24 \dots \dots \dots +24$

e)  $+6 \dots \dots \dots -30$

c)  $-15 \dots \dots \dots -5$

---

## Additive inverse

### Points to note

- An additive inverse is an integer which when added to another integer gives zero.
- The inverse property states that "any number added to its inverse or opposite, gives zero".
- For example; a)  $+4 + -4 = 0$                       b)  $-9 + +9 = 0$

## Finding additive integers

### EXAMPLES

1. Find the additive inverse of +7

Let the inverse be k

$$k + +7 = 0$$

$$k + 7 - 7 = 0 - 7$$

$$k = -7$$

b) Find the additive inverse of -10

Let the inverse be r

$$r + -10 = 0$$

$$r - 10 + 10 = 0 + 10$$

$$r = +10$$

### Activity

a) Find the additive inverse of +6

b) Find the additive inverse of -4

c) Find the additive inverse of +9

d) Find the additive inverse of -5

e) Find the additive inverse of -12

f) Find the additive inverse of +8

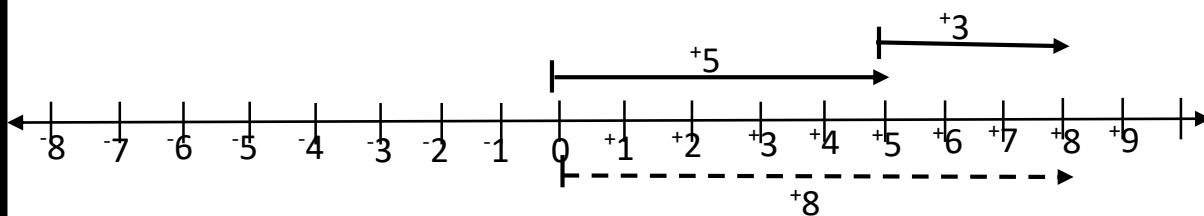
g) Find the additive inverse of -1

h) Find the additive inverse of +11

## Addition of integers using a number line

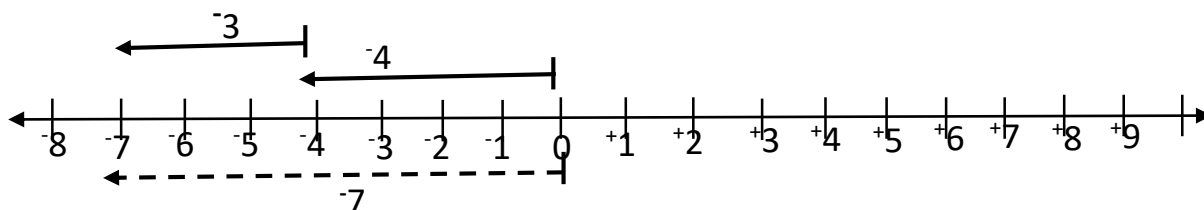
### Examples

1. Add +5 + +3 using a number line



$$+5 + +3 = +8$$

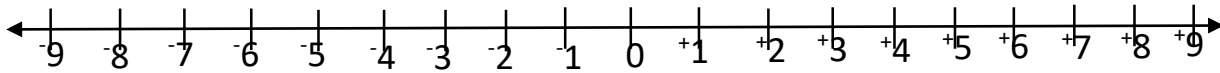
2. Add -4 + -3 using a number line



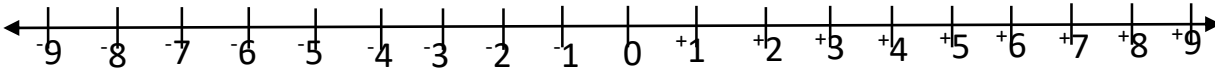
$$-4 + -3 = -7$$

## Activity

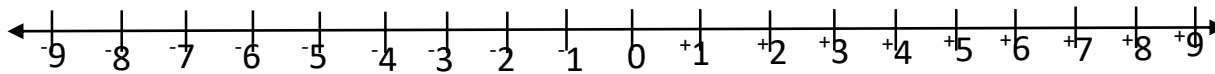
1. Add  $-5 + -4$  using a number line



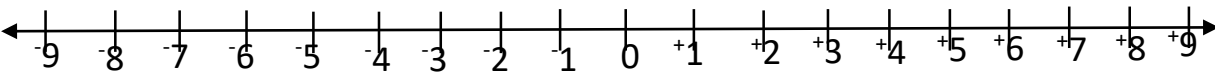
2. Add  $+6 + +3$  using a number line



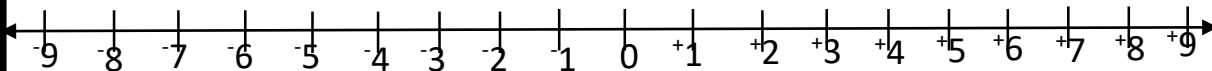
3. Add  $-6 + -2$  using a number line



4. Add  $-3 + -5$  using a number line



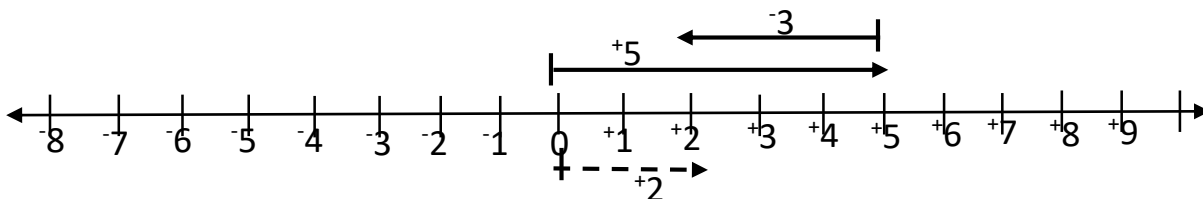
5. Add  $+4 + +2$  using a number line



## Addition of negative and positive integers using a number line

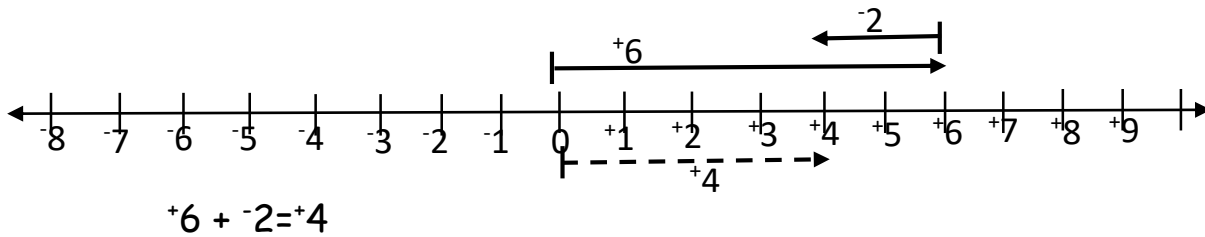
### Examples

1. Add  $+5 + -3$  using a number line

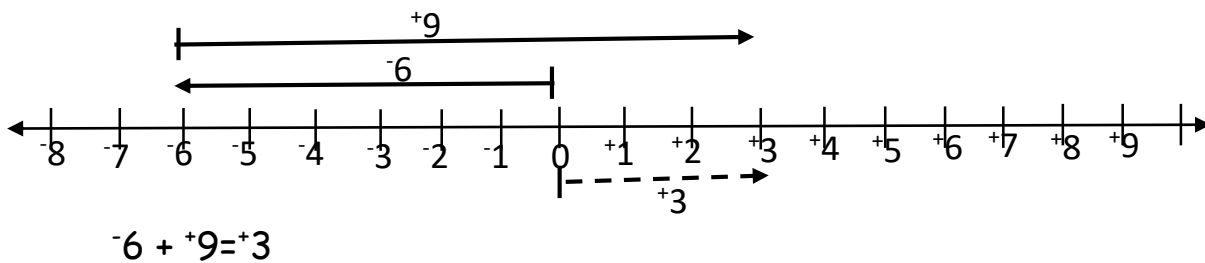


$$+5 + -3 = +2$$

2. Add  $+6 + -2$  using a number line

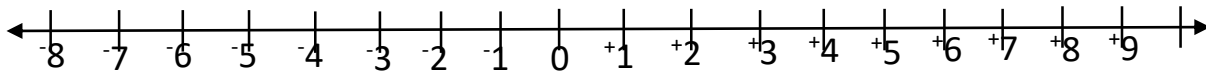


3. Add  $-6 + +9$  using a number line

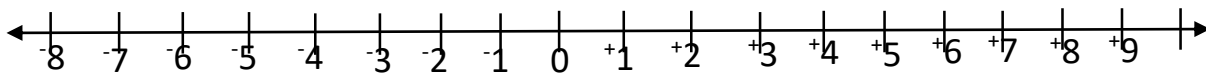


### Activity

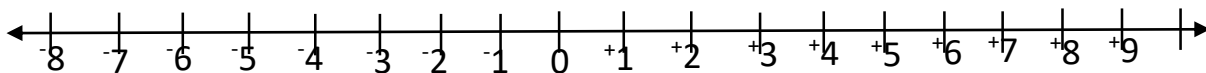
1. Add  $+7 + -3$  using a number line



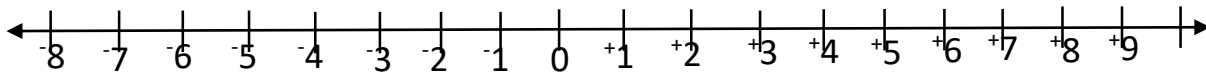
2. Add  $+9 + -5$  using a number line



3. Add  $-8 + +3$  using a number line



4. Add  $-4 + +9$  using a number line



## Addition of integers without using a number line

### Points to note

➤  $+(+) = +$

➤  $+(-) = -$

➤  $-(-) = +$

➤  $-(+) = -$

---

### Examples

1.Simplify:  $+6 + -2$

$$+6 + (-2)$$

$$+6 - 2$$

$$+4$$

2.Simplify:  $-7 + +2$

$$-7 + (+2)$$

$$-7 + 2$$

$$= -5$$

3.Simplify:  $-7 + -2$

$$-7 + (-2)$$

$$-7 - 2$$

$$-9$$

---

### Activity

1.Simplify:  $+9 + -5$

2.Simplify:  $+7 + -4$

3.Simplify:  $+5 + -2$

4.Simplify:  $-6 + -2$

5.Simplify:  $-9 + -6$

6.Simplify:  $+11 + -4$

7.Simplify:  $+8 + -5$

8.Simplify:  $-7 + -5$

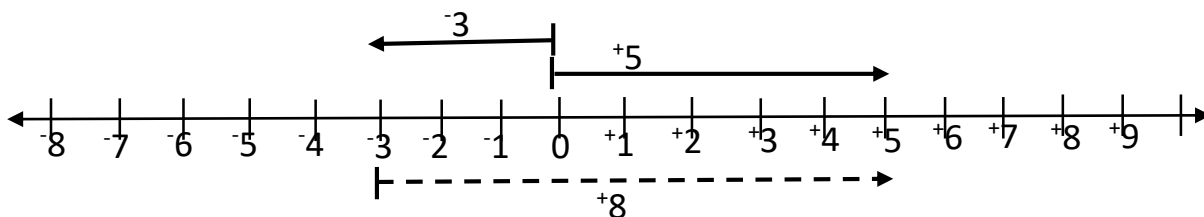
9.Simplify:  $+5 + -3$

---

## Subtraction of integers using a number line

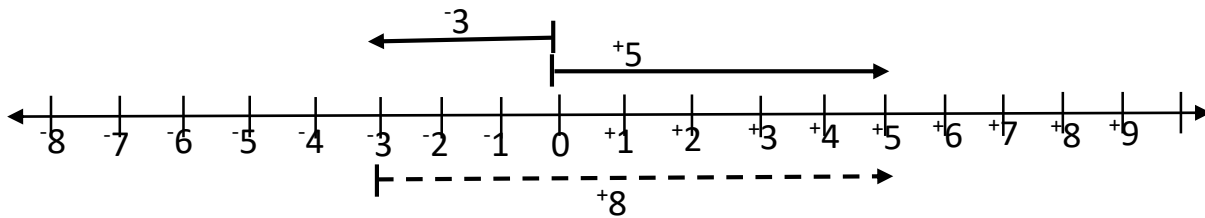
### Examples

1.Subtract  $+5 - -3$  using a number line



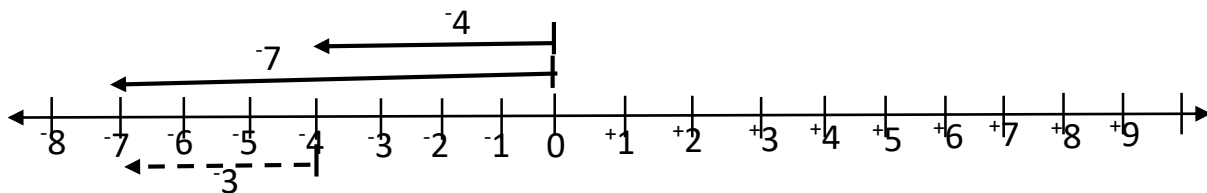
$$+5 - -3 = +8$$

2. Subtract  $+8 - -4$  using a number line



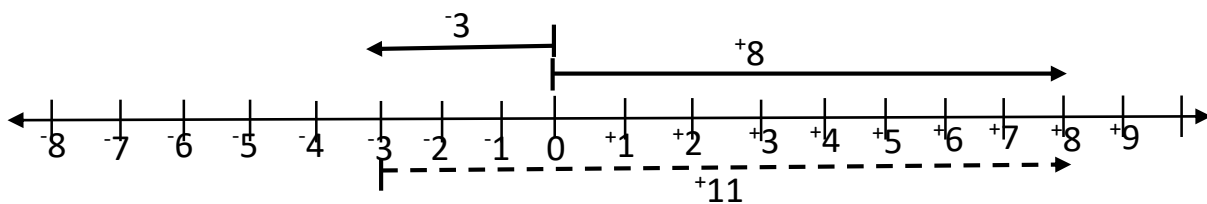
$$+5 - -3 = +8$$

3. Subtract  $-7 - -4$  using a number line



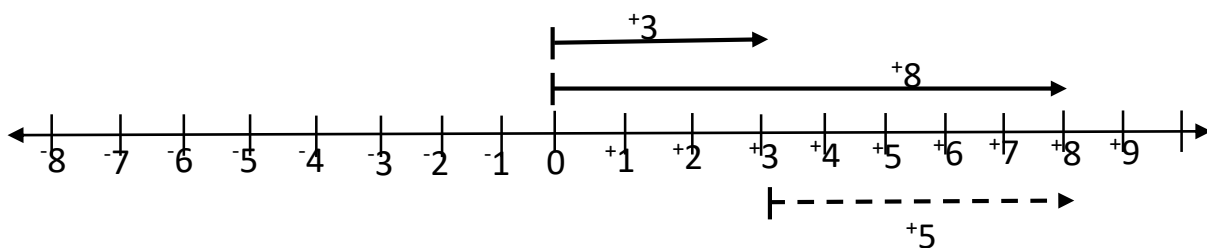
$$-7 - -4 = -3$$

4. Subtract  $+8 - -3$  using a number line



$$+8 - -3 = +11$$

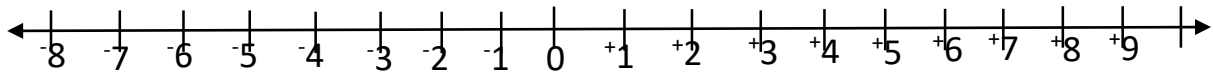
5. Subtract  $+8 - +3$  using a number line



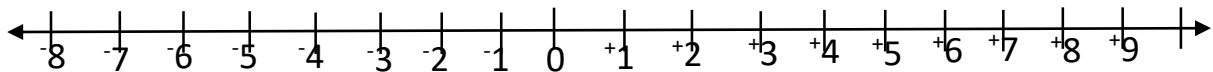
$$+8 - +3 = +5$$

## Activity

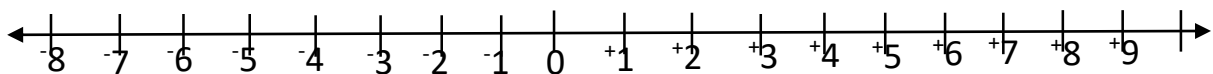
1.Subtract  $+5 - -2$  using a number line



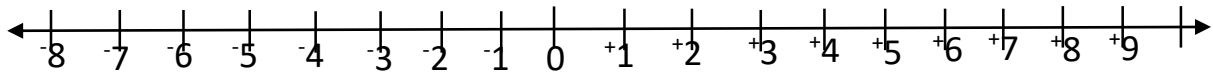
2.Subtract  $+7 - -4$  using a number line



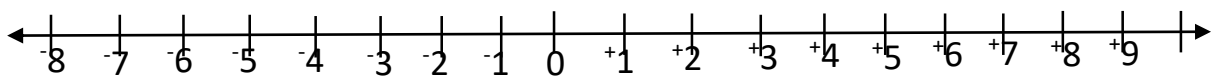
3.Subtract  $+5 - +2$  using a number line



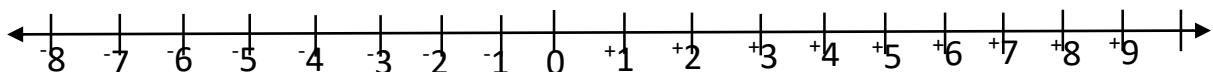
4.Subtract  $+7 - +5$  using a number line



5.Subtract  $-6 - -2$  using a number line



6.Subtract  $-8 - -5$  using a number line





## Subtraction of integers without using a number line

### Points to note

➤  $+(+) = +$

➤  $+(-) = -$

➤  $-(-) = +$

➤  $-(+) = -$

---

### Examples

1.Simplify:  $+6 - -2$

$$+6 - (-2)$$

$$+6 + 2$$

$$+8$$

2.Simplify:  $-7 - +2$

$$-7 - (+2)$$

$$-7 - 2$$

$$= -9$$

3.Simplify:  $-6 - -2$

$$-6 - (-2)$$

$$-6 + 2$$

$$-4$$

---

### Activity

1.Simplify:  $+9 - -5$

2.Simplify:  $+7 - +4$

3.Simplify:  $+5 - -2$

4.Simplify:  $-6 - +2$

5.Simplify:  $-9 - -6$

6.Simplify:  $+11 - +4$

7.Simplify:  $+8 - -5$

8.Simplify:  $-7 - +5$

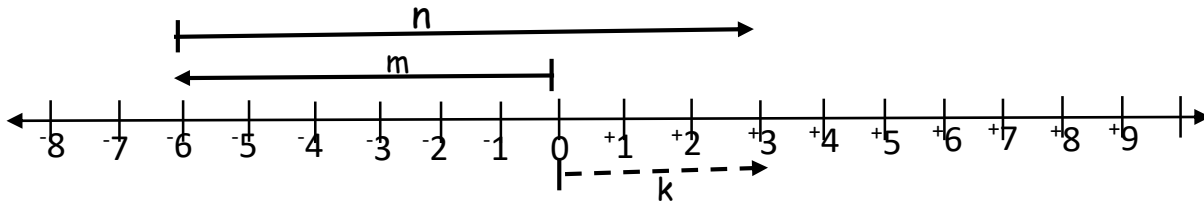
9.Simplify:  $+5 - -3$

---

## Forming addition mathematical statements from a number

### EXAMPLES

Use the number line below to answer the questions that follow



a) Write down the integer represented by the arrows  $m, n$  and  $k$

$$m = -6$$

$$n = +9$$

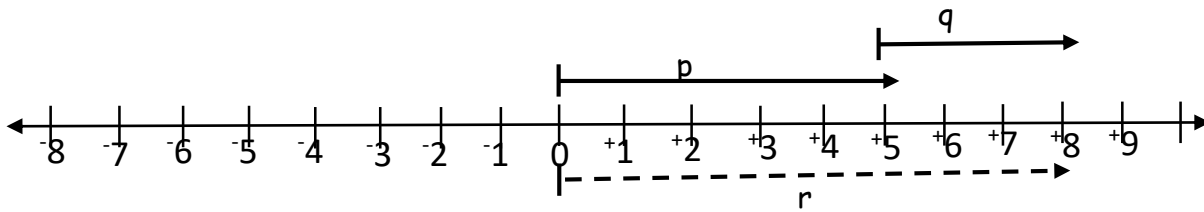
$$k = +3$$

b) Write down the addition mathematical statement shown on the above number line

$$m + n = k$$

$$-6 + +9 = +3$$

Use the number line below to answer the questions that follow



a) Write down the integer represented by the arrows  $p, q$  and  $r$

$$p = +5$$

$$q = +3$$

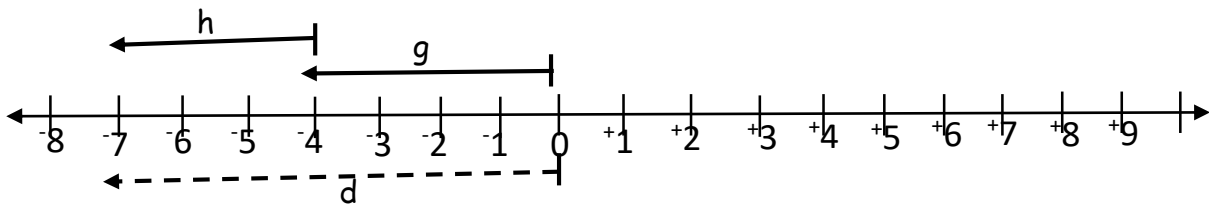
$$r = +8$$

b) Write down the addition mathematical statement shown on the above number line

$$p + q = r$$

$$+5 + +3 = +8$$

3. Use the number line below to answer the questions that follow



a) Write down the integer represented by the arrows g, h and d

$$g = -4$$

$$h = -3$$

$$d = -7$$

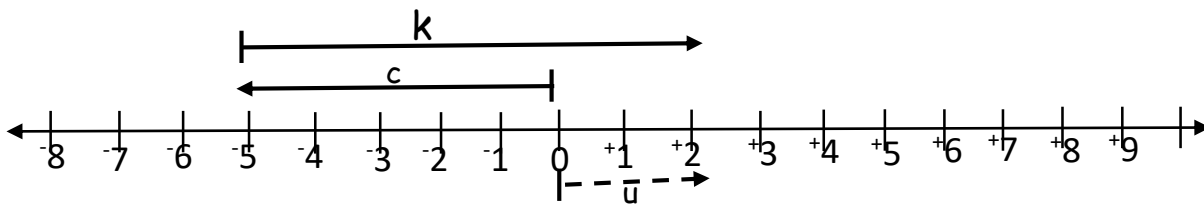
b) Write down the addition mathematical statement shown on the above number line

$$g + h = d$$

$$-4 + -3 = -7$$

### Activity

1. Use the number line below to answer the questions that follow



a) Write down the integer represented by the arrows c, k and u

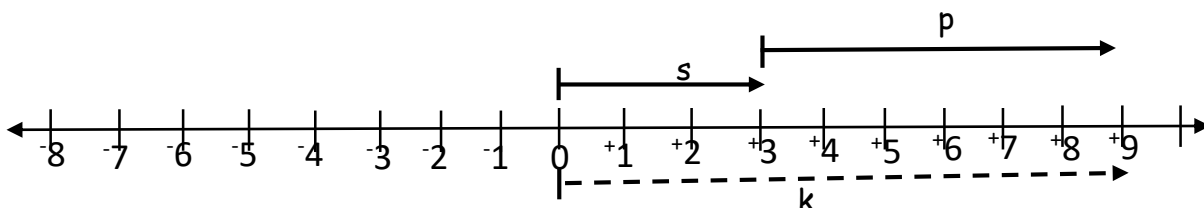
$$c = \dots\dots\dots$$

$$k = \dots\dots\dots$$

$$u = \dots\dots\dots$$

b) Write down the addition mathematical statement shown on the above number line

Use the number line below to answer the questions that follow



a) Write down the integer represented by the arrows p, q and r

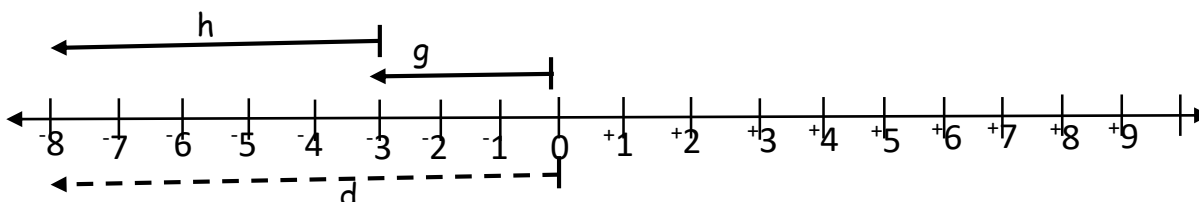
s=.....

p=.....

K=.....

b) Write down the addition mathematical statement shown on the above number line

3. Use the number line below to answer the questions that follow



a) Write down the integer represented by the arrows g, h and d

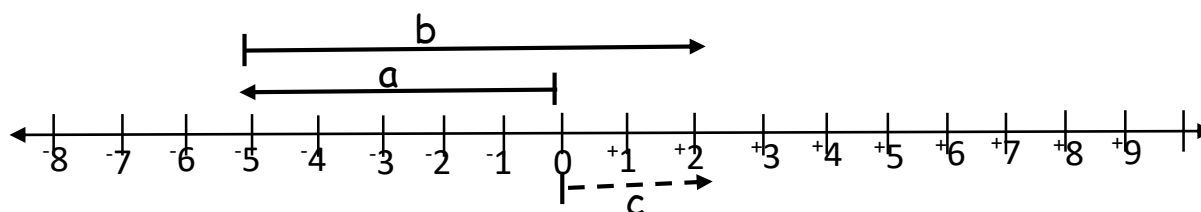
g=.....

h=.....

D=.....

b) Write down the addition mathematical statement shown on the above number line.

4. Use the number line below to answer the questions that follow



a) Write down the integer represented by the arrows a, b and c

a=.....

b=.....

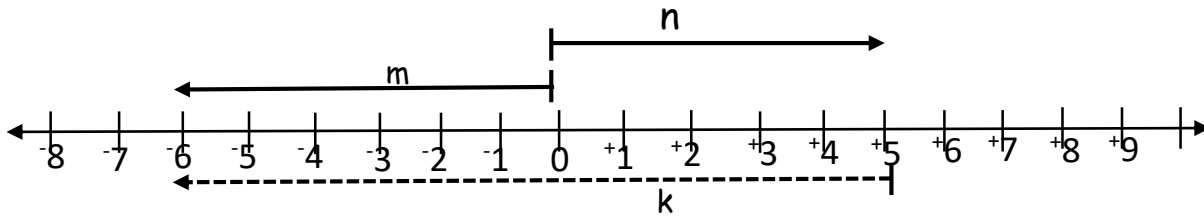
c=.....

b) Write down the addition mathematical statement shown on the above number line

## Forming subtraction mathematical statements from a number

### EXAMPLES

Use the number line below to answer the questions that follow



b) Write down the integer represented by the arrows m, n and k

$$m = -6$$

$$n = +5$$

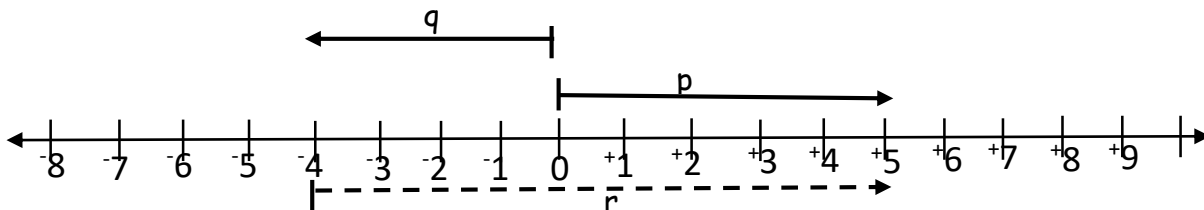
$$k = -11$$

b) Write down the subtraction mathematical statement shown on the above number line

$$m - n = k$$

$$-6 - +5 = -11$$

Use the number line below to answer the questions that follow



c) Write down the integer represented by the arrows p, q and r

$$p = +5$$

$$q = -4$$

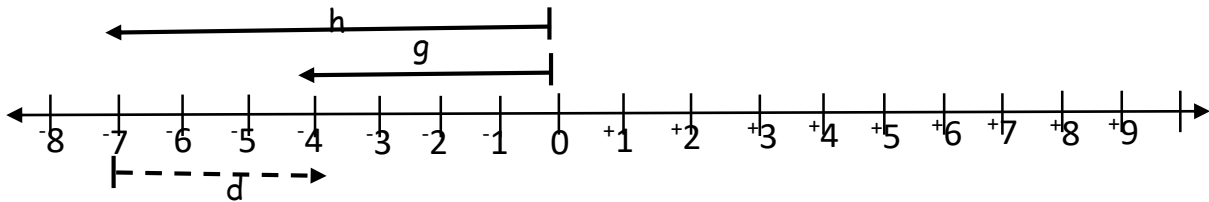
$$r = -9$$

d) Write down the subtraction mathematical statement shown on the above number line

$$p - q = r$$

$$+5 - -4 = +9$$

3. Use the number line below to answer the questions that follow



c) Write down the integer represented by the arrows  $g$ ,  $h$  and  $d$

$$g = -4$$

$$h = -7$$

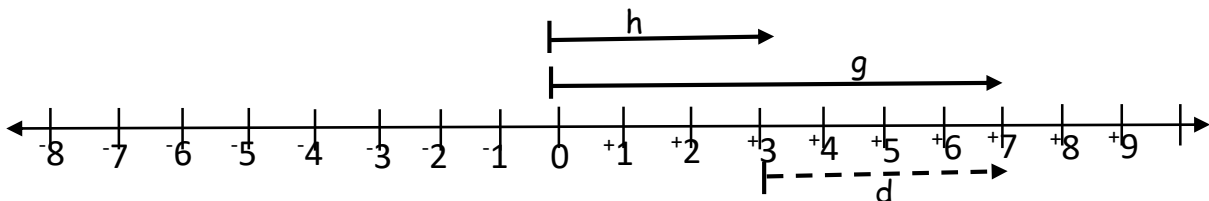
$$d = +3$$

b) Write down the subtraction mathematical statement shown on the above number line

$$g - h = d$$

$$-4 - -7 = +3$$

3. Use the number line below to answer the questions that follow



d) Write down the integer represented by the arrows  $g$ ,  $h$  and  $d$

$$g = +7$$

$$h = +3$$

$$d = +4$$

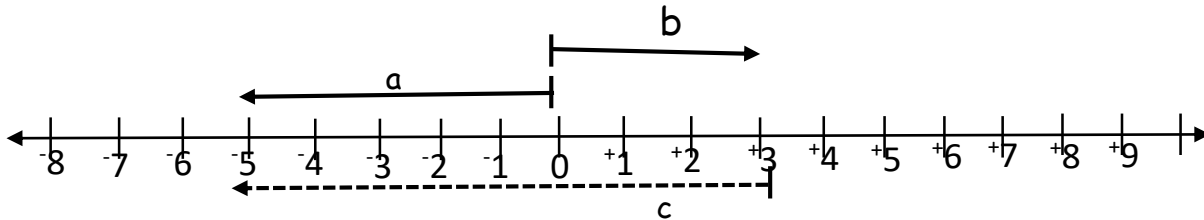
b) Write down the subtraction mathematical statement shown on the above number line

$$g - h = d$$

$$+7 - +3 = +4$$

## Activity

1. Use the number line below to answer the questions that follow



c) Write down the integer represented by the arrows a, b and c

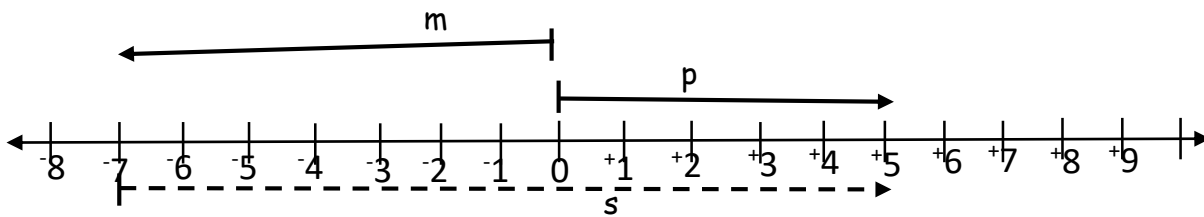
a=-----

b=-----

c=-----

b) Write down the subtraction mathematical statement shown on the above number line

Use the number line below to answer the questions that follow



e) Write down the integer represented by the arrows m, p and s

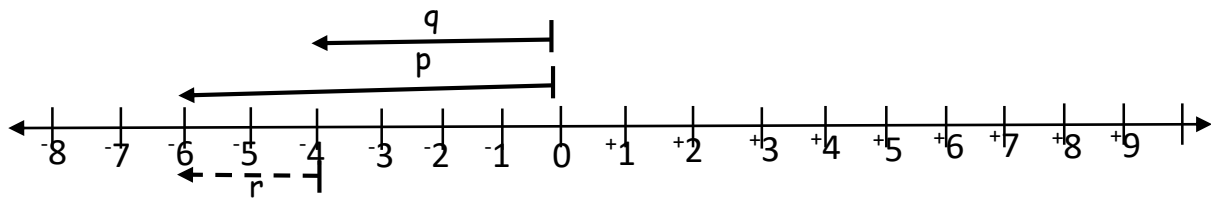
m=-----

p=-----

s=-----

f) Write down the subtraction mathematical statement shown on the above number line

3. Use the number line below to answer the questions that follow



e) Write down the integer represented by the arrows p, q and r

p=-----

q=-----

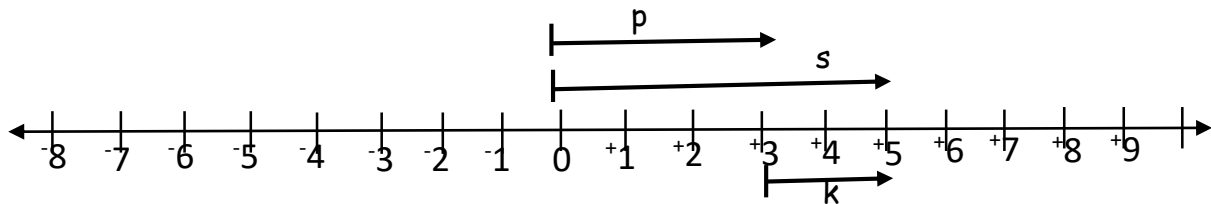
r=-----

---

b) Write down the subtraction mathematical statement shown on the above number line

---

3. Use the number line below to answer the questions that follow



f) Write down the integer represented by the arrows p, s and k

p=-----

s=-----

k=-----

---

b) Write down the subtraction mathematical statement shown on the above number line

---



## Multiplication of integers without using a number line

### Points to note

- $+ \times +$  or  $+(+)= +$
- $+ \times -$  or  $+(-)= -$
- $- \times -$  or  $-(-)= +$
- $- \times +$  or  $-(+)= -$

---

### Examples

- |                            |                            |                            |
|----------------------------|----------------------------|----------------------------|
| 1.Simplify: $+6 \times -2$ | 2.Simplify: $-7 \times +2$ | 3.Simplify: $-6 \times -2$ |
| $+6 \times -2$             | $-7 \times +2$             | $-6 \times -2$             |
| $-12$                      | $-14$                      | $+12$                      |
- 

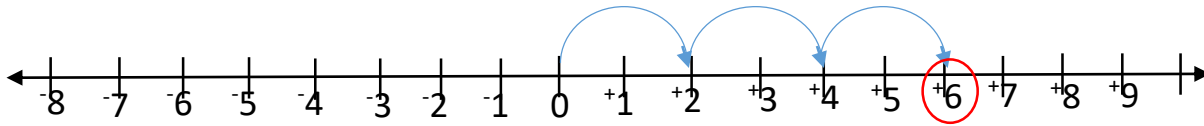
### Activity

- |                            |                            |                             |
|----------------------------|----------------------------|-----------------------------|
| 1.Simplify: $+9 \times -5$ | 2.Simplify: $+7 \times +4$ | 3.Simplify: $+5 \times -2$  |
| 4.Simplify: $-6 \times +2$ | 5.Simplify: $-9 \times -6$ | 6.Simplify: $+11 \times +4$ |
| 7.Simplify: $+8 \times -5$ | 8.Simplify: $-7 \times +5$ | 9.Simplify: $-5 \times -3$  |
-

## Multiplication of integers using a number line

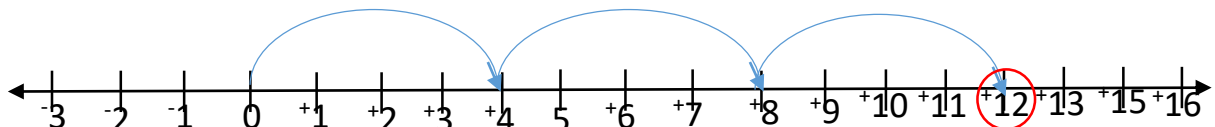
### Examples

1. Workout:  $3 \times +2$  using a number line  
( $+3 \times +2$  means three groups of twos)



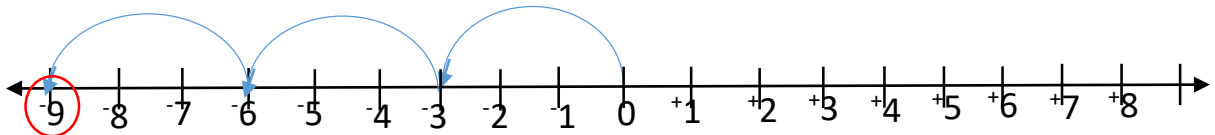
$$3 \times +2 = +6$$

2. Workout:  $3 \times +4$  using a number line



$$3 \times +4 = +12$$

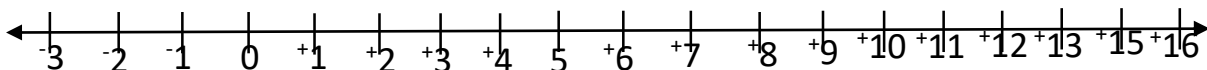
3. Workout:  $3 \times -3$  using a number line



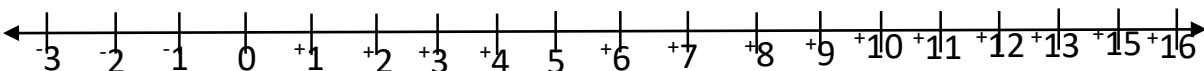
$$3 \times -3 = -9$$

### Activity

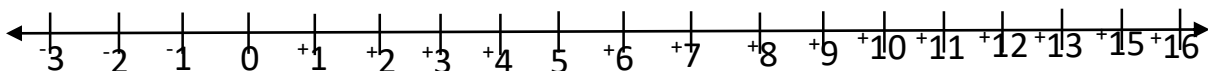
1. Workout:  $2 \times +3$  using a number line



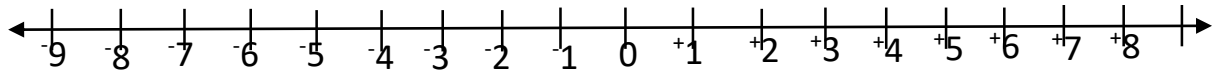
2. Workout:  $3 \times +3$  using a number line



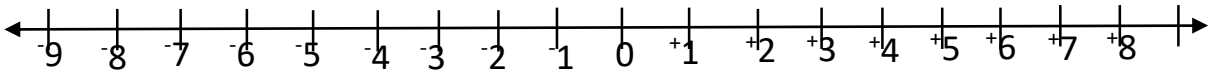
3. Workout:  $4 \times +2$  using a number line



4.Workout:  $3 \times -2$  using a number line



5.Workout:  $4 \times -2$  using a number line



## Division of integers without using a number line

Points to note

➤  $+\div+=+$

➤  $+\div=-$

➤  $-\div=-$

➤  $-\div+=-$

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Examples

1.Simplify: $+6 \div -2$	2.Simplify: $-32 \div +8$	3.Simplify: $-16 \div -4$
$+6 \div -2$	$-32 \div +8$	$-16 \div -4$
$-3$	$-4$	$+12$

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Activity

1.Simplify: $+9 \div -3$	2.Simplify: $+36 \div +4$	3.Simplify: $+24 \div -4$
4.Simplify: $-6 \div +2$	5.Simplify: $-42 \div -6$	6.Simplify: $+18 \div +2$
7.Simplify: $-28 \div -4$	8.Simplify: $-35 \div +5$	9.Simplify: $-15 \div -3$

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