

P.7 MATHEMATICS

TERM ONE

◆ THEME: SETS

❖ SET CONCEPTS.....8

- Finite and infinite sets
- Describing parts of a venn diagram
- Listing elements from a venn diagram
- Representing sets on venn diagrams
- Subsets
- Number of elements in a venn diagram
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- Application of sets
- Revision questions

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- Forming numerals from digits
- Place values and values of numbers up to hundred millions
- Writing in words
- Writing in figure
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- Roman numerals

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- Basic names of bases
- Place values and values of bases
- Converting from non decimal bases to decimal bases
- Converting from decimal bases to non decimal bases
- Converting from non decimal bases to non decimal bases
- Addition of bases
- Subtraction of bases
- Multiplication of bases
- Division of bases
- Solving for unknown bases

Mathematics is the key

❖ OPERATION ON WHOLE NUMBERS.....

- Addition of big numbers
- Subtraction of big numbers
- Multiplication of big numbers
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- Distributive property
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- Associative property
- Laws of indices
- Application of indices

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- Divisibility tests
- Types of numbers
- Finding sum of consecutive counting numbers using the formula
- Factors and multiples
- Prime factorisation
- LCM and HCF
- Application of LCM and HCF
- Consecutive numbers
- Squares and square roots
- Cube roots

TERM TWO

❖ FRACTIONS.....

- Addition and subtraction of fractions
- Multiplication of fractions
- Division of fractions
- Mixed operation on fractions (using BODMAS)
- Application of fractions
- Application of fractions involving "of the remainder"
- Application of fractions involving "taps"

• DECIMALS

- Changing vulgar fractions to decimals
- Changing non recurring decimals to vulgar fractions
- Changing recurring decimals to vulgar fractions
- Addition and subtraction of decimals
- Multiplication of decimals
- Division of decimals
- Mixed operations

Mathematics is the key

Mathematics IS the KEY

| | |
|--|----|
| ➤ Application of decimals | |
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| ➤ Expressing quantities as ratios | |
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| ➤ Finding percentage of increase and decrease | |
| ➤ Finding original numbers after increase | |
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| ➤ Percentage increase and decrease | |
| ➤ Percentage profit and loss | |
| ➤ Finding selling price(SP) when cost price (CP) percentage profit or loss are given | |
| ➤ Finding cost price(CP) when given selling price (SP) and percentage profit. | |
| ➤ Finding cost price(CP) when given selling price (SP) and percentage loss | |
| ➤ Mixed application of profit and loss | |
| ➤ Finding discount | |
| ➤ Percentage discount | |
| ➤ Finding marked price when given percentage discount and cash price | |
| ➤ Finding simple interest | |
| ➤ Finding rate | |
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| ❖ INTEGERS | 85 |
| ➤ Arranging and ordering integers using a number line | |
| ➤ Addition and subtraction of integers with and without a number line. | |
| ➤ Multiplication of integers with and without a number line. | |
| ➤ Division of integers with and without a number line. | |
| ➤ Writing mathematical statements / sentences | |

Mathematics is the Key

- **FINITE / MODULAR SYSTEM**
 - Writing numbers in finite system
 - Equivalences in finite system
 - Addition in finite system
 - Subtraction in finite system
 - Multiplication in finite system
 - Division in finite system
 - Application of finite system in days of the week.
 - Application of finite system in 12 and 24 hour time.
 - Application of finite system in months of the year.
 - Applying more than one finite in solving problems
 - Solving equations

◆ **THEME:INTERPRETATION OF GRAPHS AND DATA**

❖ **DATA HANDLING**.....95

- Revision about graphs
- Solving problems on pie charts
- Construction of pie charts
- Measures of central tendency and range (statistics)
- Complex mean / average
- Probability
- Plotting coordinates
- Plotting and joining coordinates
- Completing tables using equation of line
- Drawing lines for given ordered pairs

◆ **THEME:GEOMETRY**

❖ **LINES, ANGLES AND GEOMETRIC FIGURES**.....22

- Names of polygons
- Interior and exterior angles
- Finding number of sides of a polygon
- Finding number of triangles and right angles
- Finding number of sides when given right angles and triangles
- Finding interior angle sum
- Finding number of sides when given interior angle sum
- Angles of an isosceles triangle
- Interior and exterior angles of a triangle
- More about angles on triangles
- Interior angles of other polygons



- Exterior angles of polygons
- Angles on parallel lines
- More about angles on parallel lines
- Properties of quadrilaterals
- Complementary angles
- Supplementary angles
- **CONSTRUCTION**
- Constructing special angles
- Constructing other angles
- Constructing perpendicular bisectors
- Constructing perpendicular lines from a point
- Construction of parallel lines
- Construction of a pentagon when given side
- Construction of polygons using a centre angle
- Construction of a square when given a side
- Construction of a square in a circle
- Construction of a square using diagonals
- Construction of a rectangle when given sides
- Construction of a rectangle when given one side and diagonals
- Construction of a triangle when given sides(**SSS**)
- Construction of a triangle when given two sides and one angle(**SAS**)
- Construction of a triangle when given two angles and one side(**ASA**)
- Construction of a rhombus when given diagonals
- Construction of a rhombus when given side and angle
- Construction of a parallelogram when given side and angle
- Construction of a parallelogram when given diagonals and side
- Construction of a parallelogram when given sides and one diagonal
- Construction of a trapezium
- **BEARING AND SCALE DRAWING**
- Rotations and revolutions
- Angles on a compass and clock face
- Ordinary bearing (directions)
- True bearing
- More about true bearing
- Opposite bearing
- Expressing distance in a given scale
- Scale drawing

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◆ THEME: MEASUREMENTS

❖ TIME 162

- Converting from 12 hr clock to 24 hr clock
- Converting from 24 hr clock to 12 hr clock
- Duration
- Distance, speed and time
- Changing from km/hr to m/sec and viceversa
- Average speed
- Time tables
- Travel graphs
- Drawing travel graphs

TERM THREE

❖ LENGTH, MASS AND CAPACITY 181

- Conversion of length, mass and capacity. (review)
- Finding perimeter. (review)
- Finding area of simple shapes. (review)
- Finding area of square, rhombus and kite using diagonals.
- Finding perimeter and area of parallelogram
- Comparing sides of polygons
- Using apothem to find area
- More about area
- Circle properties
- Finding circumference of a circle and parts of a circle
- Finding perimeter of a circle and parts of a circle
- Finding radius or diameter when given circumference
- Finding radius or diameter when given perimeter
- More about perimeter (irregular figures)
- Finding area of a circle and parts of a circle
- Finding radius or diameter when given area
- Finding area of combined shapes
- Finding shaded area
- More about circumference (revolutions)
- More about perimeter. (no. of poles)
- VOLUME AND SURFACE AREA
- Converting from square metres (cm^2) to square centimetres (cm^2) and viceversa
- Converting from square kilometres (km^2) to square metres (m^2) and viceversa
- Converting from cubic metres (cm^3) to cubic centimetres (cm^3) and viceversa
- Volume and capacity of cylinders

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- Finding missing sides when given volume of a cylinder
- Volume and capacity of triangular prisms
- Finding missing sides when given volume of a triangular prism
- More about cylinders
- Volume and capacity of trapezoidal prisms
- TSA of cubes and cuboids
- Find missing sides when given TSA of cubes and cuboids
- TSA of a triangular prism
- TSA of a trapezoidal prism
- TSA of closed cylinders
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- Packing boxes in boxes
- Packing cylinders in boxes
- Comparing volume of different objects

◆ THEME: ALGEBRA

❖ ALGEBRA.....213

- Substitution
- Collecting like terms
- Addition and subtraction of fractional algebraic terms
- Multiplication and division of fractional algebraic terms
- Factorizing completely
- Removing brackets
- Removing brackets in fractional algebraic terms
- Solving simple equations
- Solving equations involving squares and square roots
- Solving equations involving brackets
- Solving equations involving fractions
- Forming and solving equations
- Application of algebra in ages
- Finding solution sets
- Solving and writing solution sets
- Finding solution sets with compound inequalities
- Solving and writing solution sets with compound inequalities

Mathematics is the key

TERM ONE: SET CONCEPTS

Key words: universal, complement, subsets, union, intersection, empty, finite, infinite, probability

SUBTOPIC: FINITE AND INFINITE SETS

A **finite** set is a set whose members can be listed down and has an end.

e.g set T = {even numbers between 4 and 12}

$$T = \{6, 8, 10\}$$

An **infinite** set is a set whose members are endless.

e.g. a set of odd numbers, a set of all stars in the sky, a set of all integers.

Set K= {all prime numbers}

$$K = \{2, 3, 5, 7, 11, 13, \dots\}$$

Activity

1. State whether the following sets are finite or infinite:

G = {girls in your class}

B = {boys in your class}

W= {days of the week}

K = {square numbers}

P= {pupils who like football}

T = {multiples of three}

H = {all alphabetical letters}

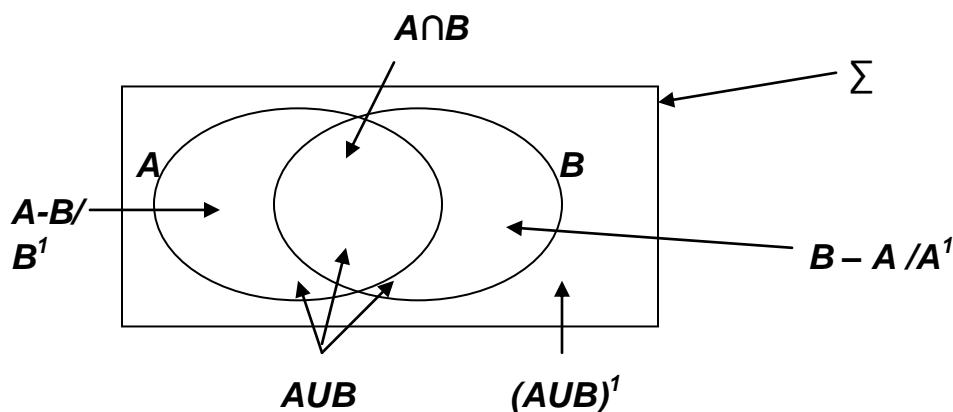
F = {months of the year}

REFERENCE

Fountain pri. maths book 7 pg 9

New MK pri. maths book 7 page 16-17

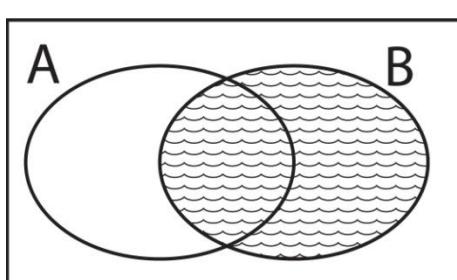
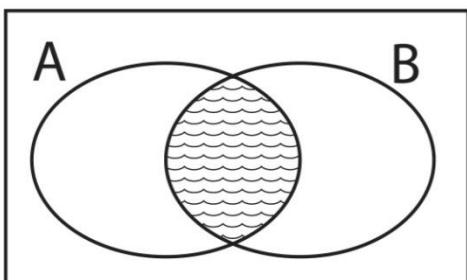
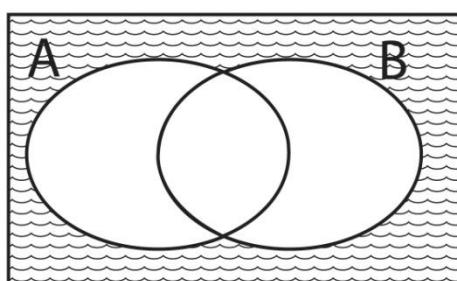
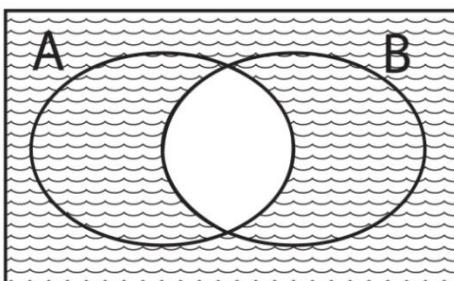
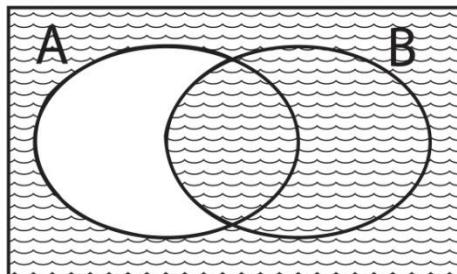
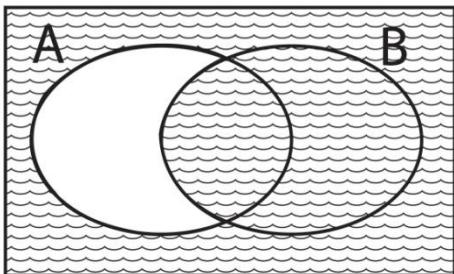
SUBTOPIC:Regions/describing points of venn diagram



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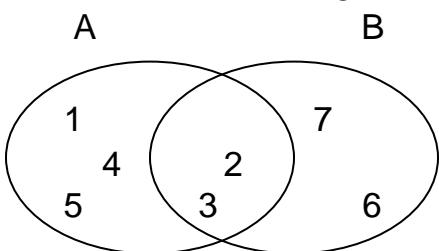
Activity

Describe the shaded regions



SUBTOPIC: LISTING ELEMENTS

1. Given the venn diagram below:



List members of the following using the above venn diagram:

- (i) Set B
- (ii) Set A¹
- (iii) (B ∩ A)
- (iv) (A ∪ B)
- (v) A - B

SUBTOPIC: REPRESENTING SETS ON VENN DIAGRAMS

Example:

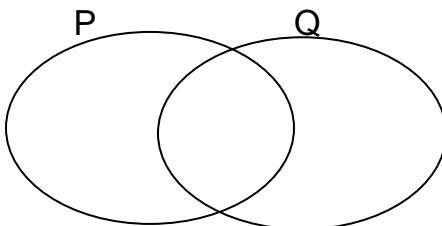
If $P = \{\text{Factors of } 24\}$

$Q = \{\text{Multiples of } 4 \text{ less than } 25\}$

(i) List elements of : $P = \{1, 2, 3, 4, 5, 6, 8, 12, 24, \}$

$Q = \{4, 8, 12, 16, 20, 24\}$

(ii) Represent the above sets on a venn diagram below:



(iii) What is: (a) $P \cap Q$ (b) $n(P \cup Q)$

Activity:

1. Given that set $A = \{\text{Even numbers less than } 15\}$
 $B = \{\text{Composite numbers less than } 15\}$

(a) List down the members of the above sets.

(b) Represent the above sets on a venn diagram

2. Given that $\mathcal{E} = \{\text{whole numbers less than } 15\}$

Set $P = \{4, 6, 14, 8, 0, 12, 3, 7\}$

Set $Q = \{1, 3, 5, 7, 9, 11, 13\}$

(a).Write down the numbers of $P \cap Q$

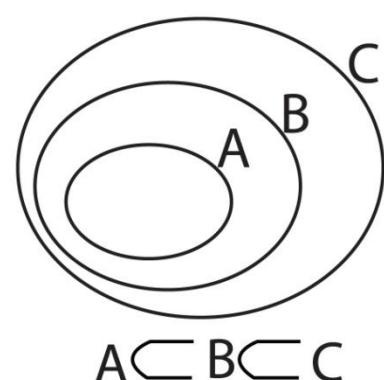
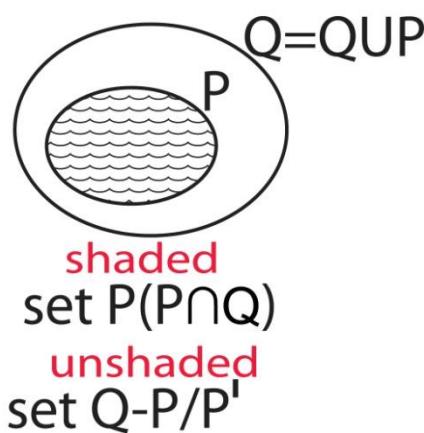
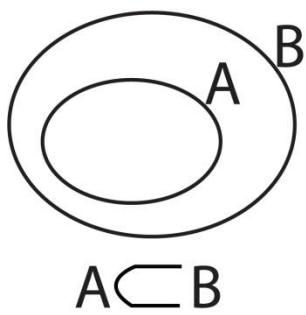
(b).Represent the above sets on a venn diagram

SUB TOPIC : SUBSETS

A subset is a set that can be got from another set.

The symbol for “is a subset of” is \subset

Subsets on venn diagram



Activity

1. Draw a venn diagram to show that;

 - (a). all dogs(D) are animals (A)
 - (b) all girls(G) are females(F)
 - (c) teachers(T) and pupils(P) are found in a school(S)

SUBTOPIC: FINDING THE NUMBER OF SUBSETS AND PROPER SUBSETS

1. Given that set A= { a, b }.
- a) Find the number of subsets in set A

By listing: { }, { a }, { b }, { a, b }
 No. of subsets in (A) = 4 subsets

Using: **No. of subsets = 2^n** (*Where 'n' = number of elements,*)
 $= 2^2$
 $= 2 \times 2$
= 4 subsets

- b) Find the number of proper subsets in set A

By listing: { }, { a }, { b }
 No. of proper subsets in set A = 3 subsets

Using : **No. of proper subsets = $(2^n) - 1$**
 $= 2^2$
 $= 2 \times 2 - 1$
 $= 4 - 1$
=3 proper subsets

2. Set A has 8 subsets. Find the number of elements in set A.

Using $2^n = \text{no. of subsets}$
 $2^n = 8 - \text{factorise}$
 $2^n = 2^3$
 $n = 3$
 $n(A) = 3$

| | |
|---|---|
| 2 | 8 |
| 2 | 4 |
| 2 | 2 |
| | 1 |

$8 = 2^3$

Activity

1. List the subsets for each of the following sets:
 - a) B = {p, q } b) C= {x, y, z} c) D= { t } d) E={ p, q, r, s}
2. How many subsets are in each of the sets above?
3. Find the number of elements in a set with 16 subsets
4. Set P has 15 proper subsets. How many elements are in set P?
5. Find the number of elements in a set with the following number of subsets
 - a) 4 subsets b) 32 subsets c) 64 subsets

REFERENCE

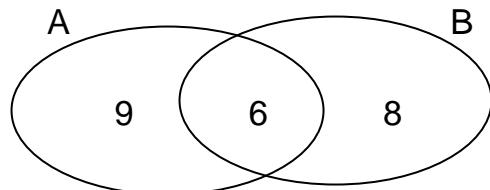
a New MK primary maths book 7 page 2 – 4

Fountain primary maths book 7 page 2

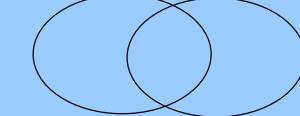
SUB TOPIC: NUMBER OF ELEMENTS ON VENN DIAGRAMS

Example

The diagram below shows the number of pupils who eat apples (A) and beans (B). Use it to answer the questions that follow:



A REMEMBER B



$$(A \cup B) = A^1 + A \cap B + B^1$$

$$A = A \text{ only} + A \cap B$$

$$B = B \text{ only} + A \cap B$$

$$\Sigma = A \text{ only} + A \cap B + B \text{ only} + (A \cup B)^1$$

- (i) How many pupils eat both apples and beans?

6 pupils

- (ii) How many pupils eat beans?

$$n(B) = 6 + 8 = 14$$

- (iii) How many pupils eat apples?

$$9 + 6 = 15 \text{ pupils}$$

- (iv) How many pupils eat only one type of food?

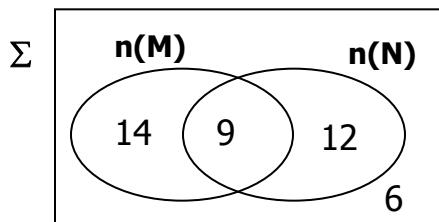
$$9 + 8 = 17 \text{ pupils}$$

- (v) Find the number of pupils in the whole class.

$$9 + 6 + 8 = 23 \text{ pupils}$$

Try these

1. Study the venn diagram below and use it to answer the questions that follow



Find

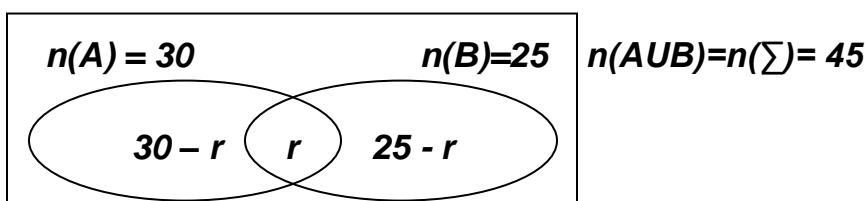
- (a) $n(M)$
- (b) $n(N)$
- (c) $n(M \cup N)$
- (d) $n(M \cap N)^1$
- (e) $n(\Sigma)$

REFERENCE

A New MK Maths Revised Edition Bk 7 Pg 9

SUB TOPIC: SOLVING PROBLEMS USING VENN DIAGRAMS

1. Given that $n(A) = 30$, $n(B) = 25$ and $n(A \cup B) = 45$.
 - (a) Draw a venn diagram to show the above information.



- (b) Find $n(A \cap B)$

Let the number in $(A \cap B)$ be r .

$$30 - r + r + 25 - r = 45$$

$$30 + 25 + r - r - r = 45$$

$$55 - r = 45$$

$$55 - 55 - r = 45 - 55$$

$$-r = -10$$

$$\underline{-r = -10}$$

$$\underline{-1} \quad \underline{-1}$$

$$\underline{\underline{r = 10}}$$

- (ii) $n(A \text{ only})$

$$n(A \text{ only}) = 30 - r$$

$$= 30 - 10$$

$$\underline{\underline{= 20}}$$

- (c). If a member is picked at random, find the probability of selecting a member in $(A \cap B)^I$

$$n(A \cap B)^I = (30 - r) + (25 - r)$$

$$= (30 - 10) + (25 - 10)$$

$$= 20 + 15$$

$$= 35$$

$$n(E) = 35$$

$$SS = 45$$

$$Probability = \frac{35}{45}$$

REFERENCE

A New MK Primary Maths ppls Bk 7 Pg 10 – 11

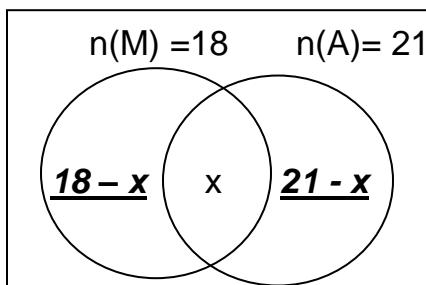
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SUB TOPIC: APPLICATION OF SETS

Examples

1. In a class of 30 pupils 18 like music (M), 21 like Art (A) and some like both.

a) Represent the above information on a Venn diagram.



$$n(\Sigma) = 30$$

b) How many pupils like both subjects?

$$18 - x + x + 21 - x = 30$$

$$18 + 21 - x = 30$$

$$39 - x = 30$$

$$39 - 39 - x = 30 - 39$$

$$-x = -9$$

$$\underline{-x} = \underline{-9}$$

$$-1 \quad -1$$

$$x = 9$$

∴ 9 Pupils like both subjects

(c).How many pupils like one subject?

$$18 - x + 21 - x$$

$$18 - 9 + 21 - 9$$

$$9 + 12$$

$$21 \text{pupils}$$

(d).What is the probability of selecting a pupil who likes one subject?

$$n(E) = 21$$

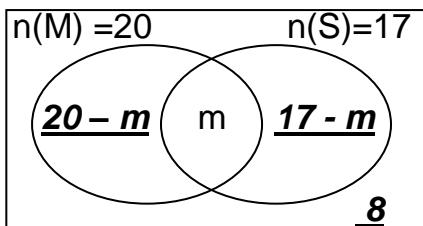
$$SS = 30$$

$$\text{Probability} = \frac{21}{30}$$

2. In a class of 40 pupils, 20 like mathematics (M), 17 like science (S), m like both subjects while 8 do not like any of the subjects.

a) Represent the above information on a Venn diagram.

$$n(\Sigma) = 40$$



b) How many pupils like both subjects?

$$8 + 20 - m + m + 17 - m = 40$$

$$28 + 17 - m = 40$$

$$45 - m = 40$$

$$45 - 45 - m = 40 - 45$$

$$-m = -5$$

$$\frac{-m}{-1} = \frac{-5}{-1}$$

$$m = 5$$

∴ 5 Pupils like both subjects

Mathematics is the key

c) What is the probability of selecting a pupil who likes only one subject?

$$(20-x) + (17-x)$$

$$(20 - 5) + (17 - 5) \quad \text{Prob (only one subject)} = \frac{27}{40}$$

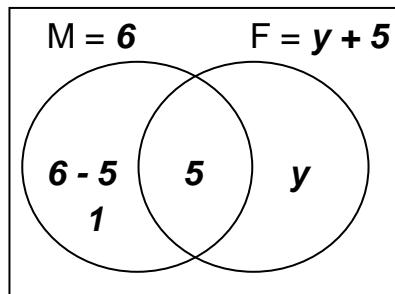
$$15 + 12$$

27 pupils

3. In a family of 10 members, 6 members eat meat (M), 5 members eat both meat and fish (F) while 'y' members eat only fish.

- i) Represent the above information on a Venn diagram

$$n(\Sigma) = 10$$



- ii) How many members eat only fish?

$$y + 5 + 1 = 10$$

$$y + 6 = 10$$

$$y + 6 - 6 = 10 - 6$$

$$y = 4$$

- iii) Find the number of pupils who eat fish.

(y + 5) Pupils

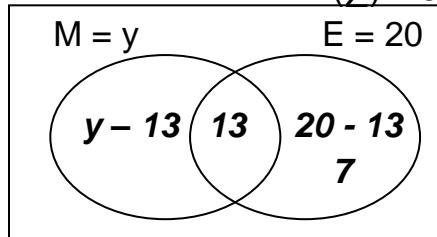
$$4 + 5$$

9 Pupils

4. In a class of 35 pupils, y like mathematics (M), 20 like English (E) while 13 like both subjects.

- a) Using a Venn diagram, show the above information

$$n(\Sigma) = 35$$



b) Find the number of pupils who like mathematics.

$$\begin{array}{l}
 y - 13 + 13 + 20 - 13 = 35 \\
 \quad\quad\quad\quad\quad OR \\
 \quad\quad\quad\quad\quad y + 7 = 35 \\
 \quad\quad\quad\quad\quad y + 7 - 7 = 35 - 7 \\
 \quad\quad\quad\quad\quad y = 28
 \end{array}
 \quad
 \begin{array}{l}
 y + 20 - 13 = 35 \\
 \quad\quad\quad\quad\quad y + 7 = 35 \\
 \quad\quad\quad\quad\quad y + 7 - 7 = 35 - 7 \\
 \quad\quad\quad\quad\quad y = 28
 \end{array}$$

OR

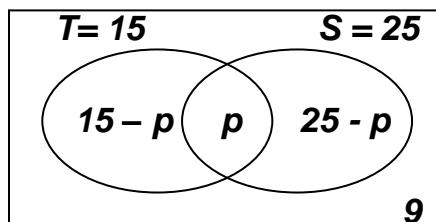
$$\begin{array}{l}
 y - 13 + 20 = 35 \\
 \quad\quad\quad\quad\quad y + 7 = 35 \\
 \quad\quad\quad\quad\quad y + 7 - 7 = 35 - 7 \\
 \quad\quad\quad\quad\quad y = 28
 \end{array}$$

∴ 28 Pupils like mathematics

5. In a group of 40 people, they all play football(F), 9 play football only, 15 play tennis(T) and football, 25 swim(S) and play football and some enjoy all the three games.

- a. Draw a Venn diagram to represent the above information

$$n(\mathcal{E}) = n(F) = 40$$



- b. How many people participate in all the three activities?

$$\begin{aligned}
 15 - p + p + 25 - p + 9 &= 40 \\
 15 + 25 - p + 9 &= 40 \\
 49 - p &= 40 \\
 49 - 49 - p &= 40 - 49 \\
 -p &= -9 \\
 \frac{-p}{-1} &= \frac{-9}{-1} \\
 p &= 9
 \end{aligned}$$

REFERENCES

- Fountain primary maths Book 7 pages 16 to 17
 MK Book 7 pages 10 to 11
 Understanding math Book 7 page 9
 Macmillan Book 7 page 9s
 Functional math Book 7 pages 12

TOPICAL QUESTIONS ON SET CONCEPTS

1. Given that:

$$\text{Set } P = \{1, 2, 3, 4, 5, 6, 7\}$$

$$K = \{0, 2, 4, 8, 9, 10\}$$

Find (i) $P \cap K$

$$(ii) n(P \cup K)$$

$$(iii) P - K$$

$$(iv) K^1$$

$$(v) (P \cap K)^1$$

2. Draw a venn diagram to show that all dogs (D) are animals (A)

3. Given that Set A = {all prime numbers less than 20} B = {all factors of 16}

4. Given that a set has 32 subsets. How many elements has it?

5. In a class of 30 pupils, 10 pupils like History (H) 14 like Geography (G) and 12 do not like either of the subjects.

(i) Draw a venn diagram to represent this information.

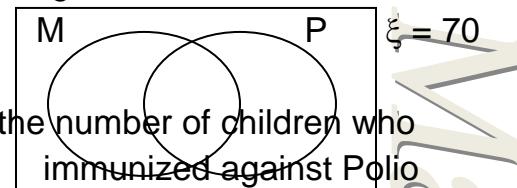
(ii) How many pupils like both subjects?

(iii) How many pupils like History?

(iv) How many pupils like one subject?

6. Seventy children were taken to a clinic for immunization, 45 children were immunized against Measles (M) X children were immunized against Polio (P) 6 children were immunized against measles and Polio. 1 child was not immunized at all.

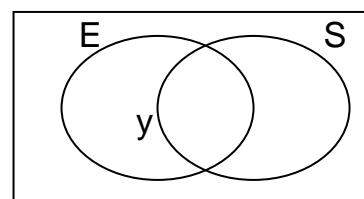
(a) Represent the information in the venn diagram



(b) Find the number of children who were immunized against Polio only.

7. In a class of 40 pupils, 25 like English (E), 15 like Science (S) Y pupils like both English and Science and 8 do not like any of the 2 subjects.

(a) Complete the venn diagram.



(b) Find the value of y.

(c) What is the probability of picking a pupil who likes only one subject?

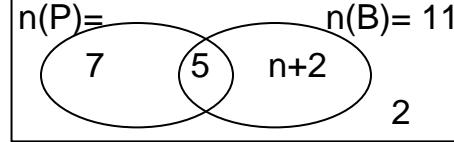
8. In a class of 20 pupils where two languages are spoken, 14 speak Luganda (L), 15 speak Kiswahili (K).

(a) Draw a venn diagram and show the information given.

(b) Find the number of pupils who speak both Luganda and Kiswahili.

(c) Find the number of pupils who speak only one language.

9. Use the venn diagram below.



(a) Find the value of

$$(i) n$$

(ii) Universal set

$$(iii) n(P \cap B)^1$$

10. In a class of 60 pupils, all enjoy eating beans, 33 enjoy eating meat (M), 35 enjoy eating fish (F), If P pupils enjoy all the three while 2 enjoy eating beans only.
- Represent the information on a venn diagram.
 - Find the value of P.
 - How many pupils enjoy only fish?

11. Given that Set X = {a, d, c, d} Find the number of:

- Sub sets
- Proper subsets

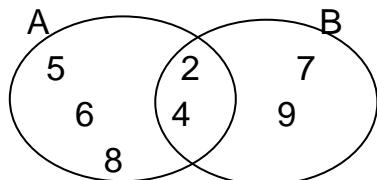
12. Write two examples of empty sets

13. Draw a symbol for equivalent set

14. Given that K= {a,b,c,d,e,f }

KUL={ a,b,c,d,e,f,g,h,i,j }. Find n(L)

15. In the figure below find A'B

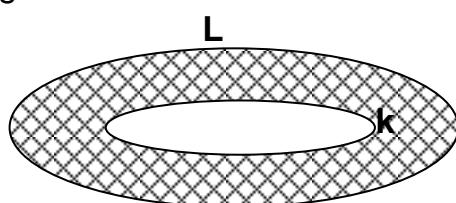


16. Set k = {a,b,c }. List all subsets of set k

17. Given that M = {all prime numbers less than 15 }.Find n(M)

18. Given that A= {1,2,3,4,5} and B = {1,3,5,7,9}. Find the number of subsets in A \cap B.

19. Describe the shaded part on the venn diagram



20. Draw a venn diagram to show that all cows are animals

21. Given that.

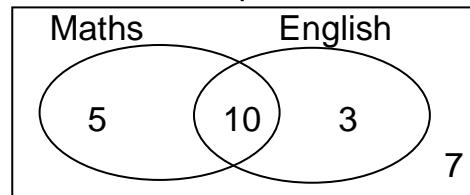
Set A={all counting numbers less than 10}

B = {all odd numbers from 1 to 10}.

Find n(A \cup B)

22. Set T has 16 subsets. How many elements has set T?

23. Study the venn diagram below and use it to answer the questions



(a).How many pupils study mathematics?

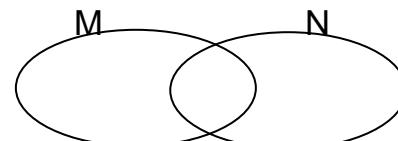
(b)How many pupils do not study mathematics?

(c).Find the probability of selecting a pupil who studies either Mathematics or English.

24. Express the number of pupils who study one subject as a percentage of the whole class

25. Set K has 31 proper subsets. How many elements are in set K?

17. Shade M'∩N



18. Given that

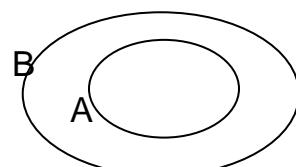
$$X=\{p, q, r, s, t\}$$

$$Y=\{o, p, a, q, u, e\}$$

Find n(X-Y)

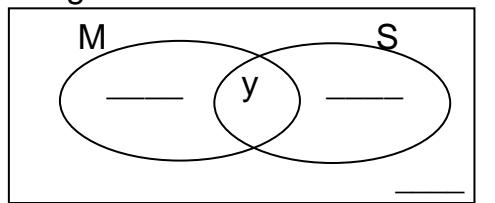
19. How many subsets are in a set with six elements?

20. What is the relationship between A and B as shown in the venn diagram below?



21. In a class of **50 boys**, **40** like mathematics (**M**) and **25** like science (**S**).some boys **y** like both subjects and **2** do not like any of the **two** subjects.

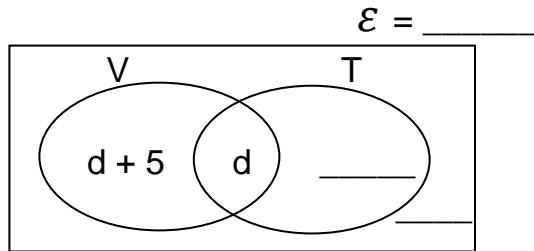
- (a) Show the information in the venn diagram below.



(b).How many boys like mathematics only?

22. In a class, **31**pupils play tennis (**T**) and (**d+5**) play volley ball (**V**) only. **d** pupils play both games while **3** play neither of the games.

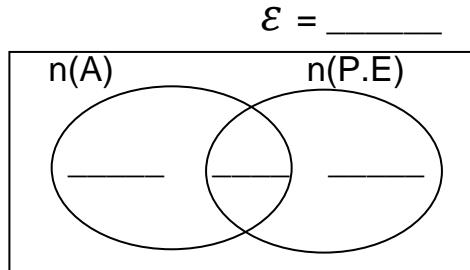
(a).Complete the venn diagram.



(b).If **27** pupils play volley ball altogether, find the value of d.

23.In a class of thirty five members, all of them like music (M),(3y-4)enjoy Art(A) and music only,(y+6) enjoy P.E and music and only (y+2) enjoy all the three activities, while (y+1)enjoy music only.

(a). Show the above information on a venn diagram below.



(b) How many members enjoy ;

(i).Music and P.E?

(ii).Music and art

(c).How many pupils are in the whole class?

d). What is the probability of selecting a member at random who likes only one subject?

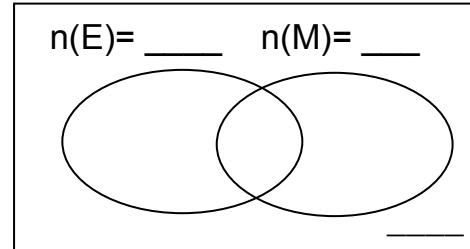
25.Given than $n(\Sigma) = 25$, $n(A) = 15$, $n(B) = 18$ and $n(A \cup B)' = 2$

(a) Draw a venn diagram to show the above information.

(b)Find $n(A \cap B)$

26.In a class of 65 children, $x + 31$ like Maths (M), 12 like English only, $11 + x$ like both Math and English while X like neither of the two subjects.

(a)Represent the above information on the venn diagram below.



(b)Find the value of X

(c)If a boy is picked at random, what is the probability of picking a boy who likes one subject?

WHOLE NUMBERS

SUBTOPIC: FORMING NUMERALS USING GIVEN DIGITS

CONTENT: Using digits to form smallest and largest numbers.

Finding the sum of/product/difference/quotient between the smallest and largest numbers formed from the given digits.

Examples:

- ❖ Write down all 3-digit numerals that can be formed using the digits; 4, 6, 7

476 467 647 674 746 764

- ❖ Find the difference between the smallest and highest numerals formed.

Smallest = 467

Biggest = 764

Difference = 764 - 467

$$\begin{array}{r} - 467 \\ 297 \end{array}$$

Activity:

- ✓ Using digits **3, 0, 6**, form all 3 - digit numerals that can be formed.
- ✓ Find the product of the smallest and the biggest numerals formed.

- ❖ Write down all three digit even numerals that can be formed from **8, 3, 4**.

- ❖ Find the sum of all 3-digit odd numbers that can be formed

SUBTOPIC: PLACE VALUES AND VALUES OF DIGITS UP TO HUNDRED MILLIONS

The place value chart

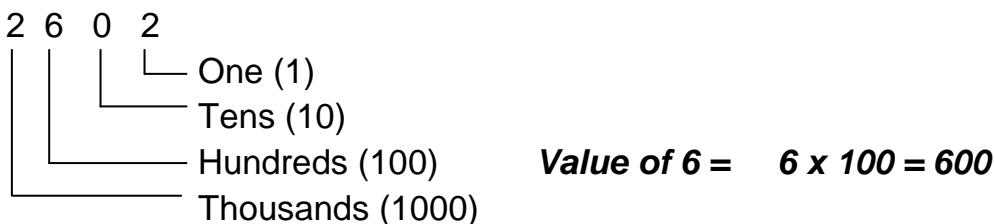
| Million | | | Thousands | | | Units | | |
|---------|---|---|-----------|---|---|-------|---|---|
| H | T | O | H | T | O | H | T | O |
| 2 | 8 | 7 | 6 | 5 | 4 | 3 | 2 | 9 |

The table below shows the place values and values of the numeral above

| Digit | Place value in words | Place value in figures | Value (digit × P.V) |
|-------|----------------------|------------------------|---------------------|
| 9 | Ones | 1 | $9 \times 1 = 9$ |
| 2 | Tens | 10 | $2 \times 10 = 20$ |
| 3 | Hundreds | | |

Mathematics is the key

Example: Find the value of 6 in the number 2602



Activity:

1. Write the place value and value of 9 in
 - (a). 345987
 - (b). 26490321
 - (c). 689458345
2. Find the sum of the value of seven and the place value of 9 in 23745893

SUB TOPIC: WRITING IN WORDS (UP TO HUNDRED MILLION)

Examples:

- (i) Write 20,480 in words.

| Thousand | Units |
|----------|-------|
| 20 | 480 |

Twenty thousand, four hundred eighty.

- (ii) 60,808,040

| Million | Thousand | Units |
|---------|----------|-------|
| 60 | 808 | 040 |

Sixty million, eight hundred eight thousand forty.

Activity:

Write the following in words.

- 34,567
- 9,999,999
- 30,230,203

SUB TOPIC: WRITING NUMERALS IN FIGURES

Examples:

Write in figures:

- (i) Fifty seven million four hundred twenty one thousand nine hundred five.

$$57 \text{ million} = 57,000,000$$

$$\begin{array}{r} 421 \text{ thousand} \\ + 421,000 \\ \hline 905 & 905 \\ \hline 57,421,905 \end{array}$$

- (ii) A quarter of a million

$$A \text{ million} = 1,000,000$$

$$\frac{1}{4} \text{ of } 1,000,000$$

$$\underline{1} \times 1,000,000$$

$$4$$

$$= 250,000$$

- (iii) Write “ sixty million, four hundred thirty nine thousand, seven” in figures

- (iv) Write “ six hundred thirty nine thousand, seven” in figures

- (v) Write “ three million, thirty nine thousand, eight” in figures

- (vi) Write “ nine million, four hundred thirty nine thousand, six” in figures

- (vii) Write “thirty nine thousand, fifty seven” in figures

SUB TOPIC: EXPANDED NOTATION

CONTENT: Expanding numerals using:

- Place values
- Values
- Powers of ten/exponents

Examples:

Expand: 5624 using:

Place values: $5624 = (5 \times 1000) + (6 \times 100) + (2 \times 10) + (4 \times 1)$

Values: $5624 = 5000 + 600 + 20 + 4$

| 10^3 | 10^2 | 10^1 | 10^0 |
|--------|--------|--------|--------|
| 5 | 6 | 2 | 4 |

Powers: $5624 = (5 \times 10^3) + (6 \times 10^2) + (2 \times 10^1) + (4 \times 10^0)$

Mathematics is the key

Activity:

Expand the following as instructed

- 2,354 (place values)
- 40,369 (place values)
- 45,689 (values)
- 29,542(values)
- 890765 (exponents)
- 2354 (powers)

SUB TOPIC: FINDING THE EXPANDED NUMBERS (SHORT FORM)

Examples:

Write as a single number.

$$\begin{aligned}
 \text{(i)} \quad & (6 \times 10,000 + (4 \times 10) + (5 \times 1)) \\
 & (6 \times 10000) + (4 \times 100) + (5 \times 1) \\
 = & 60,000 + 400 + 5 \\
 = & 60000 \\
 & \begin{array}{r} 400 \\ + \quad 5 \\ \hline 60405 \end{array}
 \end{aligned}$$

$$\begin{aligned}
 \text{(ii)} \quad & 9000000 + 700\ 00 + 50000 + 1000 + 30 + 8 \\
 = & 9\ 000\ 000 \\
 & \begin{array}{r} 700\ 000 \\ 50\ 000 \\ 1\ 000 \\ 30 \\ + \quad 8 \\ \hline 9\ 750\ 038 \end{array}
 \end{aligned}$$

$$\begin{aligned}
 \text{(iii)} \quad & (2 \times 10^5) + (4 \times 10^3) + (6 \times 10^0) + (7 \times 10^2) \\
 & (2 \times 10 \times 10 \times 10 \times 10 \times 10) + (4 \times 10 \times 10 \times 10) + (6 \times 1) + (7 \times 10 \times 10) \\
 & 200,000 + 4000 + 6 + 700 \\
 & \begin{array}{r} 200\ 000 \\ 4000 \\ 700 \\ + \quad 6 \\ \hline 204706 \end{array}
 \end{aligned}$$

Activity

What number has been expanded to give?

- $3000 + 200 + 3$
- $(5 \times 1000) + (9 \times 100) + (2 \times 10) + (8 \times 1)$
- $(9 \times 10^4) + (9 \times 10^2) + (2 \times 10^1) + (8 \times 10^0)$

SUB TOPIC: STANDARD FORM/SCIENTIFIC NOTATION

Writing whole numbers in Scientific notation

Examples:

- (i) Write 453 in standard form

$$4.53 \times 100$$

$$4.53 \times 10 \times 10$$

$$\underline{4.53 \times 10^2}$$

- (ii) Express 650000 in Scientific notation.

$$650,000 = 6.5 \times 100,000$$

$$= 6.5 \times 10 \times 10 \times 10 \times 10 \times 10 \times 10$$

$$\underline{= 6.5 \times 10^5}$$

Express the following decimals in standard notation/Scientific form.

- (i) 365.72

$$\underline{3.6572 \times 10^2}$$

- (ii) 0.67

$$\underline{6.7 \times 10^{-1}}$$

1. Write the following numbers in standard form

- 652
- 9709
- 0.00034
- 29

2. Find the decimal number expressed in standard form.

a. 2.34×10^{-2}

b. 6.1×10^{-2}

REFERENCE MTC Revision Hand Book P.6, 6, P.7 Pg 29

Mathematics is the key

SUB TOPIC: ROUNDING OFF WHOLE NUMBERS

Examples:

Round off the following as instructed.

- (i) 3864 to the nearest hundreds.

$$\begin{array}{r} TH \ H \ T \ O \\ 3 \ 8 \ 6 \ 4 \\ + \ 1 \\ \hline 3 \ 9 \ 0 \ 0 \end{array}$$

- (ii) 214 (nearest tens)

$$\begin{array}{r} H \ T \ O \\ 2 \ 1 \ 4 \\ + \ 0 \\ \hline 2 \ 1 \ 0 \end{array}$$

- (iii) 4.78516 to the nearest thousandths.

$$\begin{array}{r} 0 \ T^{\text{th}} \ H^{\text{th}} \ TH^{\text{th}} \ T/TH^{\text{th}} \\ 4 . \ 7 \ 8 \ 5 \ -1 \\ + 0 . \ 0 \ 0 \ 0 \\ \hline 4. \ 7 \ 8 \ 5 \end{array}$$

(iii) 75.634 to the nearest whole number nearest whole number

$$\begin{array}{r}
 \text{T} \quad \text{0} \quad \text{Tth} \quad \text{Hth} \quad \text{THth} \\
 7 \quad 5 \cdot 6 \quad 3 \quad 4 \\
 + \quad 1 \\
 \hline
 7 \quad 6 \cdot
 \end{array}$$

Activity:

1. Round off the following as instructed in brackets

- 45637 (nearest hundreds)
- 99999 (nearest thousands)
- 780937887 (nearest millions)
- 89.58(nearest tenths)
- 23.786(nearest hundredths)
- 7.239(nearest two d.p)

REFERENCE

Macmillan Primary Mathematics Pupils' Bk 7 Pg 24
Mathematics Revision Hand Book P5, 6 & 7 Pg 28

SUB TOPIC: ROMAN NUMERALS (converting Hindu Arabic numerals to roman numerals)

BASIC ROMAN NUMERALS

| | | |
|-------------|-----------|-------------------------------|
| 1 | =I | NOTE: |
| 5 | =V | <i>All other numerals are</i> |
| 10 | =X | <i>got from basic roman</i> |
| 50 | =L | <i>numerals by adding or</i> |
| 100 | =C | <i>subtracting .</i> |
| 500 | =D | |
| 1000 | =M | |

Example

1. What 124 in Roman numerals

$$\begin{array}{r}
 \text{H} \quad \text{T} \quad \text{O} \\
 1 \quad 2 \quad 4 \\
 100 \quad 20 \quad 4 \\
 100 \quad + \quad 20 \quad + \quad 4 \\
 100 = \text{C} \\
 20 = \text{XX} \\
 4 = \text{IV} \\
 \therefore 124 = \text{CXXIV}
 \end{array}$$

$$\begin{aligned}
 \text{ii)} \quad & 1962 \\
 & 1000 + 900 + 60 + 2 \\
 & 1000 = \text{M} \\
 & 900 = \text{CM} \\
 & 60 = \text{LX} \\
 & 2 = \text{II} \\
 \therefore & 1962 = \text{MCMLXII}
 \end{aligned}$$

Mathematics is the Key

Activity

Write the following in roman numerals

- a) 49
- b) 235
- c) 333
- d) 78
- e) 140
- f) 999
- g) 1449

REFERENCE

Macmillan Pri MTC pupils bk 7 pg 16

A New MK Primary Mathematic Bk 7 pg 23

SUBTOPIC:ROMAN NUMERALS (conversion of Roman numerals to Hindu Arabic)

Write the following numbers in Hindu Arabic numerals

| | |
|---------------|----------------|
| (i) MXLV | (II) CD XCIV |
| $M + XL + V$ | $CD + XC + IV$ |
| $M = 1000$ | $CD = 400$ |
| $XL = 40$ | $XC = 90$ |
| $V = 5$ | $IV = 4$ |
| $MXLV = 1045$ | $CDXCIV = 494$ |

Activity

(i) **Write the following in Hindu Arabic numerals**

- XLIV
- CVIII
- XCIX
- CDXCIV
- MXCIV

(ii) **A church was built in MDCCCLXIV. Which year is this in Hindu Arabic?**

REFERENCE

A New MK Primary Maths Pupils Bk 7 Pg 24

Macmillan Primary Maths Pupils' Bk 7 Pg 16

BASES

GENERAL NAMES OF BASES

NAMES OF BASES AND DIGITS USED

| BASE | NAME | DIGITS USED |
|-------|------------------|------------------------------|
| two | binary | 0, 1 |
| three | ternary | 0, 1, 2 |
| four | quaternary | 0, 1, 2, 3 |
| five | quinary | 0, 1, 2, 3, 4 |
| six | senary | 0, 1, 2, 3, 4, 5 |
| seven | septenary | 0, 1, 2, 3, 4, 5, 6 |
| eight | octal | 0, 1, 2, 3, 4, 5, 6, 7 |
| nine | nonary | 0, 1, 2, 3, 4, 5, 6, 7, 8 |
| ten | denary / decimal | 0, 1, 2, 3, 4, 5, 6, 7, 8, 9 |

SUBTOPIC: Changing from non decimal bases to decimal bases

Example:

- (i) Change 234_{six} to base ten

$$\begin{array}{r} 2 \ 3 \ 4 \\ \swarrow \quad \swarrow \\ \text{Ones } (6^0) \\ \text{Sixes } (6^1) \\ \text{Six sixes } (6^2) \\ (2 \times 6^2) + (3 \times 6^1) + (4 \times 6^0) \\ (2 \times 6 \times 6) + (3 \times 6) + (4 \times 1) \\ (12 \times 6) + 18 + 4 \\ 72 + 22 \\ \underline{\underline{94 \text{ ten}}} \end{array}$$

Activity:

Convert the following to base ten

- (a) 241_{five}
- (b) 10101_{two}
- (c) 234_{six}
- (d) 212_{four}

REFERENCE

A New MK Primary Maths Pupils' Bk 6 Pg 40

Mathematics is the Key

SUB TOPIC: Changing from decimal bases to non-decimal bases

Example:

Change 25 to base seven

| | | |
|---|----|-----|
| 7 | 25 | r 4 |
| 7 | 3 | r 3 |
| 0 | | |

$$25 = 34 \text{ seven}$$

Activity

- ✓ Express the following as instructed
- 83 to nonary base.
 - 45 to base five
 - 23 to base two
 - 33 to quinary

REFERENCE

A New MK Primary Maths Pupils' Bk 6 Pg 39

SUB TOPIC: Changing from non decimal bases to non decimal bases

Example:

(i) Change 123 five to base six

123_{five} to base ten

$$1^2 2^1 3^0$$

$$(1 \times 5^2) + (2 \times 5^1) + (3 \times 5^0)$$

$$(1 \times 5 \times 5) + (2 \times 5) + (3 \times 1)$$

$$(5 \times 5) + 10 + 3$$

$$25 + 10 + 3$$

$$35 + 3$$

$$\underline{38_{\text{ten}}}$$

38_{ten} to base six

$$\begin{array}{|l|l|l|} \hline 6 & 38 & \text{rem } 2 \\ \hline 6 & 6 & \text{rem } 0 \\ \hline 6 & 1 & \text{rem } 1 \\ \hline 0 & & \\ \end{array}$$

$$\underline{102_{\text{six}}}$$

$$\underline{123_{\text{five}} = 102_{\text{six}}}$$

Activity

- Change 12_{three} to base five
- Change 34_{five} to base six
- Change 212_{three} to base seven
- Change 10101_{two} to base five
- 2t_{eleven} to base nine

REFERENCE

A New MK Primary Maths Pupils' Bk 6 Pg 39

Mathematics is the key

SUB TOPIC: Operation on bases – ADDITION

Example:

$$\begin{array}{r}
 225_{\text{six}} \\
 + 434_{\text{six}} \\
 \hline
 1103_{\text{six}}
 \end{array}$$

Activity

Workout the following

- (a) $110_{\text{two}} + 101_{\text{two}}$
- (b) $121_{\text{three}} + 212_{\text{three}}$
- (c) $123_{\text{five}} + 342_{\text{five}}$
- (d) $143_{\text{five}} + 11_{\text{five}}$ (answer in base ten)
- (e) $23_{\text{seven}} + 12_{\text{six}}$ (answer in base five)

REFERENCE

A New MK Primary Maths Pupils' Bk 7 Pg 38

SUB TOPIC: Operation on bases - SUBTRACTION

Examples:

(I) $671_{\text{nine}} - 285_{\text{nine}}$

$$\begin{array}{r}
 6^{\textcolor{red}{5}} 7^{\textcolor{red}{6}} 1^{\textcolor{red}{10}}_{\text{nine}} \\
 - 2 8 5_{\text{nine}} \\
 \hline
 3 7 5_{\text{nine}}
 \end{array}
 \quad
 \begin{array}{l}
 9 + 1 = 10 \\
 9 + 6 = 15
 \end{array}$$

Activity

Workout the following

- (a) $110_{\text{two}} - 100_{\text{two}}$
- (b) $1111_{\text{two}} - 101_{\text{two}}$
- (c) $221_{\text{three}} - 12_{\text{three}}$
- (d) $423_{\text{five}} - 142_{\text{five}}$
- (e) $143_{\text{five}} - 11_{\text{five}}$ (answer in base ten)
- (f) $345_{\text{six}} - 234_{\text{six}}$

REFERENCE

A New MK Old Edition Pupils Bk 7 Pg 39

SUB TOPIC: Operation on bases – MULTIPLICATION

CONTENT: Example:

(i)
$$\begin{array}{r} 1^1 & 2 & 1 \\ \times & 2 \\ \hline 1 & 0 & 1 & 2 \end{array} \text{ three}$$

$$1 \times 2 = 2$$

$$2 \times 2 = 4$$

$$4 \div 3 = 1 \text{ rem } 1$$

$$1 \times 2 = 2 + 1$$

$$3 \div 3 = 1 \text{ rem } 0$$

(ii)
$$\begin{array}{r} 3^3 & 4^3 & 5 \\ \times & 1 & 4 \\ \hline 2 & 3 & 1 & 2 \\ 3 & 4 & 5 \\ \hline 1 & 0 & 2 & 0 & 2 \end{array} \text{ six}$$

$$4 \times 5 = 20$$

$$20 \div 6 = 3 \text{ rem } 2$$

$$4 \times 4 = 16 + 3 = 19$$

$$19 \div 6 = 3 \text{ rem } 1$$

$$3 \times 4 = 12 + 3 = 15$$

$$15 \div 6 = 2 \text{ rem } 3$$

$$6 \div 6 = 1 \text{ rem } 0$$

$$8 \div 6 = 1 \text{ rem } 2$$

Activity

Multiply the following

- (a) $11_{\text{two}} \times 10_{\text{two}}$
- (b) $110_{\text{two}} \times 100_{\text{two}}$
- (c) $121_{\text{three}} \times 11_{\text{three}}$
- (d) $132_{\text{five}} - 12_{\text{five}}$

REFERENCE

A New MK Primary Maths Pupils' Bk 7 Pg 40 exercise 3:4

SUB TOPIC: Operation on bases – DIVISION

Examples:

(i) $204_{\text{five}} \div 14_{\text{five}}$.

204_{five} to base ten

$$(2 \times 52) + (0 \times 51) + (4 \times 50)$$

$$(2 \times 5 \times 5) + (0 \times 5) + (4 \times 1) + (10$$

$$\times 5) + 0 + 4$$

$$50 + 4$$

$$\underline{54}_{\text{ten}}$$

14_{five} to base ten

$$(1 \times 51) + (4 \times 50)$$

$$(1 \times 5) + (4 \times 1)$$

$$5 + 4$$

$$\underline{9}_{\text{ten}}$$

$$54 \div 9_{\text{ten}}$$

$$\underline{6}_{\text{ten}}$$

6_{ten} to base five

| | | |
|---|---|-------|
| 5 | 6 | rem 1 |
| 5 | 1 | rem 1 |
| | 0 | |

$$\underline{204}_{\text{five}} \div \underline{14}_{\text{five}} = \underline{11}_{\text{five}}$$

Mathematics is the key

(ii) $448_{\text{nine}} - 17_{\text{nine}}$ (answer in Septenary base)

REFERENCE

A New MK Old Edition Pupils Bk 7 Pg 41 - 42 exercise 3:5

SUB TOPIC: FINDING THE UNKNOWN BASE (missing base)

Examples:

(i) If $44p = 35$ nine

$$(4 \times p^1) + (4 \times p^0) = (3 \times 9^1) + (5 \times 9^0)$$

$$(4 \times p) + (4 \times 1) = (3 \times 9) + (5 \times 1)$$

$$4p + 4 = 27 + 5$$

$$4p + 4 = 32$$

$$4p + 4 - 4 = 32 - 4$$

$$4p + 0 = 28$$

$$\frac{4p}{4} = \frac{28}{4}$$

$$P = 7$$

(ii) $X^2 = 71$ nine

(iii) 325 six = q^3

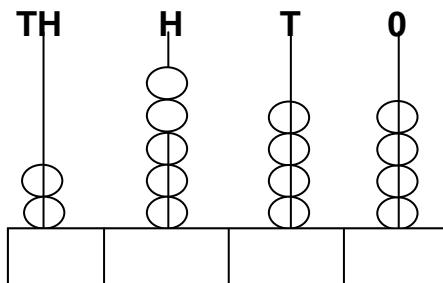
(iv) Solve for m. $44_m = 35_{\text{nine}}$

REFERENCE

A New MK Old Edition Pupils Bk 7 Pg 43

END OF TOPIC EXERCISE

1. Show 2843 on the abacus.
2. Write the number shown on the abacus in roman numerals.



3. Write the place value of each digit in 486349334.
4. Workout the sum of the value of 6, 8 and 7 in 4638047.

5. Workout the difference between that value of 7 and the place value of 9 in 49834734.

6. Write the product of the value of 6 and 3 in 8469 in roman numerals.
7. Write 4009009 in words.
8. Write "Two hundred thirty six thousand forty nine" in expanded form using exponents.
9. Expand 963.07 using values.
10. Which number was expanded to give $(6 \times 10^4) + (8 \times 10^2) + (3 \times 10^{-1}) + (7 \times 10^{-2})$
11. Round off 9999 to the nearest thousands.
12. Round off 67.987 to the nearest hundredths.

13. Round off 99.999 to the nearest hundredth.
14. Round off 16.873 to the nearest whole number.
15. Expand 635.057 using exponents.
16. St. Mary's college was constructed in MCMLXXXVII. In which year was it constructed?
17. Write 18.487 in words.
18. Find the sum of the value of 7 and the value of 3 in 3.467.
19. Write forty six and eighty seven thousandths in figures.
20. Change 16 to ternary.
21. Write all digits used in base six.
22. Write the value and place value of 3 in 432_{five} .
23. Workout. $110_{\text{two}} \times 11_{\text{two}}$
24. If $22_n = 18_{\text{ten}}$. Find the value of n
25. Add $22_{\text{five}} + 101_{\text{two}}$ (Answer in base six)
26. Solve for x. $x^2 + x^2 = 112_{\text{five}}$.
27. Solve for P. $44p = 35_{\text{nine}}$
28. Divide $31_{\text{five}} \div 22_{\text{three}}$ (Answer in base ten)

OPERATION ON NUMBERS

SUB TOPIC: ADDITION OF LARGE NUMBERS

Examples:

Add correctly:

$$\begin{array}{r}
 (i) \quad \begin{array}{r} 615 \ 146 \ 144 \\ + 320 \ 005 \ 614 \\ \hline 935 \ 151 \ 758 \end{array}
 \end{array}$$

- (ii) The population in four countries of a district shows that county A is 23,467, county B is 21 602, county C is 19 466 and county D is 25 102. What is the total population in the district?

$$\begin{array}{r}
 \begin{array}{rcl}
 \text{County A} & & 23 \ 467 \\
 \text{County B} & & 21 \ 602 \\
 \text{County C} & & 19 \ 466 \\
 \text{County D} & & +25 \ 012 \\
 \hline
 & & 89 \ 547
 \end{array}
 \end{array}$$

Emphasis on place value arrangement and re-grouping.

Activity

1. Add correctly
 - $23,456 + 89,045$
 - $668,433 + 998,765$
 - $4,677 + 78,890$
2. In a certain country, 467,883 patients contracted COVID-19 in March and 349,277 patients in April and 89,898 patients in May. How many patients contracted COVID-19 in the three months of the year 2020?

REFERENCE

A New MK Bk 7 Pg 45

Primary School Mathematics BK 7

SUB TOPIC: SUBTRACTION OF LARGE NUMBERS

CONTENT: Examples:

Subtract correctly:

(i)
$$\begin{array}{r} 596\ 148\ 320 \\ - 239\ 610\ 510 \\ \hline 356\ 537\ 810 \end{array}$$

- (ii) What is the difference between 3060 and 186?

$$\begin{array}{r} 3\ 060 \\ - 186 \\ \hline 2\ 874 \end{array}$$

Lattice method(Napier's rod method)

| | | | | | | |
|---|---|---|---|---|---|---|
| 2 | 1 | 4 | 0 | 3 | 2 | |
| 0 | 0 | 0 | 0 | 0 | 0 | 1 |
| 2 | 1 | 4 | 0 | 3 | 2 | |
| 2 | 0 | 0 | 0 | 0 | 0 | 3 |
| 6 | 3 | 2 | 0 | 9 | 6 | |
| 8 | 0 | 2 | 8 | 0 | 6 | 2 |
| 3 | 0 | 4 | 6 | 0 | 0 | 4 |
| 3 | 8 | 7 | 8 | 3 | 6 | 8 |

$$\therefore 214,032 \times 1,324 = 283\,378\,368$$

- (ii) A store can hold 1973 boxes each containing 34 pairs of shoes. How many pairs of shoes are in the store?

$$\begin{array}{r}
 1\,973 \\
 \times\, 34 \\
 \hline
 7\,892 \\
 +59\,190 \\
 \hline
 67\,082 \text{ pairs}
 \end{array}$$

Activity

- Multiply the following
 - 458×234
 - 24307×45
- 134 MPs contributed 9,570 kilograms of posho each on average during the time COVID-19. How many kilograms of posho did they contribute altogether?

REFERENCE

New MK Bk 7 exercise 3:2 Pg 46

SUB TOPIC: DIVISION OF LARGE NUMBERS

Examples:

- (i) Divide 3816648 by 132

$$\begin{array}{r} 28914 \\ \hline 132 \overline{)3816648} \\ -264 \\ \hline 1176 \\ -1056 \\ \hline 1206 \\ -1188 \\ \hline 184 \\ -132 \\ \hline 528 \\ -528 \\ \hline \end{array}$$

$$3816648 \div 132 = 28914$$

- (ii)

There are 6315 books to be packed in 15 boxes. How many books should be packed in each box?

$$\begin{array}{r} 421 \text{ books} \\ \hline 15 \overline{)6315} \\ -60 \\ \hline 31 \\ -30 \\ \hline 15 \\ -15 \\ \hline \end{array}$$

Activity

1. Divide the following

- $650075 \div 5$
- $5868 \div 12$

2. The RDC of a certain district shared sh.982,500 amongst 15 members on the COVID-19 task force in 2020. How much did each member get?

REFERENCE

A New MK Bk 7 Pg 46

SUB TOPIC: PROPERTIES OF NUMBERS

DISTRIBUTIVE PROPERTY

Examples:

Use the distributive property to work out:

(i) $(379 \times 27) + (27 \times 21)$

Re-arrange $(27 \times 379) + (27 \times 21)$

$= 27 \times (379 + 21)$

$= 27 \times 400$

$= 27 \times 400$

$= 10800$

(ii) $(137 \times 42) - (37 \times 42)$

$(137 \times 42) - (37 \times 42)$

$= (42 \times 137) - (42 \times 37)$

$= 42 \times (137 - 37)$

$= 42 \times 100$

$= 4200$

Mathematics is the key

Workout the following;

1. $(2 \times 17) + (2 \times 13)$
2. $(75 \times 29) - (75 \times 19)$
3. $(129 \times 37) - (129 \times 27)$
4. $(290 \div 70) - (10 \div 70)$
5. $(179 \div 13) - (10 \div 13)$

ASSOCIATIVE PROPERTY

Example

The alteration of the position of the brackets does not change the result.

Use the associative property to workout

$$(5+8)+2 = 5+(8+2) = (5+2)+8$$

$$\begin{array}{rcl} 13+2 & = & 5+10 \\ 15 & = & 15 \end{array} = \begin{array}{rcl} 7+8 \\ 15 \end{array}$$

The alteration of the position of the brackets does not change the result.

$$(5 \times 8) \times 2 = 5 \times (8 \times 2) = (5 \times 2) + 8$$

$$\begin{array}{rcl} 40 \times 2 & = & 5 \times 16 \\ 80 & = & 80 \end{array} = \begin{array}{rcl} 10 \times 8 \\ 80 \end{array}$$

Conclusion : the associative property holds for both addition and multiplication

COMMUTATIVE PROPERTY

Example

$$4+3 = 3+4 \quad (\text{What you start with does not affect the result})$$

$$\begin{array}{rcl} 7 & & 7 \end{array}$$

$$4 \times 3 = 3 \times 4 \quad (\text{What you start with does not affect the result})$$

$$12 = 12$$

Conclusion: The commutative property holds for both addition and multiplication

Given that $t^*y = ty + y$

Find;

- i) 2^*3
- ii) 5^*7

REFERENCE

A new MK pri MTC bk 7 pg 47 (new edition)

END OF TOPIC EXERCISE

1. A wire of length 161 metres was shared by some boys the average length of wire each boy got was 23 metres. Find the number of boys which shared the wire.
2. In a village there are 680 males, 328 females and 462 children. How many people are in that village altogether?
3. Workout $23 - 48 + 37$
4. In a league tournament, **3** points were awarded for a win, **1** point for a draw and **0** points for a loss. Five tournaments and the results were recorded as shown below.

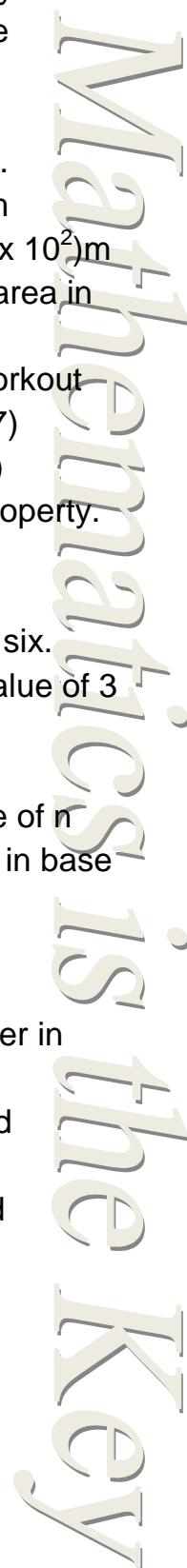
| Team | P | W | D | L | PTS |
|------------|---|---|---|---|-----|
| BURAMA FC | 6 | 3 | 2 | 1 | |
| BURUMA FC | 6 | 4 | 0 | 2 | |
| GADAMA FC | 6 | 5 | 1 | 0 | |
| ENDAKO FC | 6 | 2 | 2 | 2 | |
| PHILIPS FC | 6 | 4 | 2 | 0 | |

P = played **W**= win **D**= Draw
L= loss

Complete the table with the points for each team.

5. Musa's farm produces 1500 eggs everyday. If a tray of eggs is sold at sh.12000 and it holds 30 eggs.
- (a) How many trays does he get everyday?
- (b) How much money does he get every day?
- (c) A trader bought ten trays of eggs from the farm and sold each at sh. 450.

- (i) Calculate the profit made.
- (ii) A trader bought other ten trays and 75 eggs got broken. If he sold the remaining eggs at sh. 500 each. Calculate the loss he made.
6. Write 0.0867 in standard form.
7. Write 187000 in standard form
8. A parallelogram has base (8×10^2) m and height (6.5×10^{-2}) m. find its area in standard form
9. Use distributive property to workout the following. $(81 \times 17) + (19 \times 17)$
10. Workout. $(3.6 \times 5) + (6.4 \times 5)$
11. Workout using distributive property.
 $(65 \div 5) - (20 \div 5)$
12. Change 16 to ternary.
13. Write all digits used in base six.
14. Write the value and place value of 3 in 432_{five} .
15. Workout. $110_{\text{two}} \times 11_{\text{two}}$
16. If $22_n = 18_{\text{ten}}$. Find the value of n
17. Add $22_{\text{five}} + 101_{\text{two}}$ (Answer in base six)
18. Solve for x. $x^2 + x^2 = 112_{\text{five}}$.
19. Solve for P. $44p = 35_{\text{nine}}$
20. Divide $31_{\text{five}} \div 22_{\text{three}}$ (Answer in base ten)
21. Divide $32 \div 8$ using repeated subtraction.
22. Workout 4×6 using repeated addition
22. Workout $273900 \div 4565$



PATTERNS AND SEQUENCES

SUB TOPIC: DIVISIBILITY TESTS

Divisibility for 2.

A Number is divisible by 2 if the digit in the one's place is 0, 2, 4, 6, or 8 eg 1460

Test for 3:

A number is divisible by 3 if the sum of its digits is divisible by 3 eg $741 = 7 + 4 + 1 = 12$

Test for 4:

A number is divisible by 4 if the number formed by its last two digits is divisible by 4. eg 572. The last two digits are 7 and 2 therefore the number formed is 72 which is divisible by 4. Hence 572 is divisible by 4.

Test for five (5):

A number is divisible by 5 if the last digit in the ones place is either 0 or 5. eg 360 or 805.

Activity

1. Write any two numbers divisible by 2
2. Which of the numbers is divisible by 3

34

236

11190

2783

3. Which of the numbers is divisible by 4

4612

139

8500

7869

Test for 6:

A number is divisible by 6 if it is divisible by 2 and 3. In other words a number is divisible by 6 if it is even and the sum of its digits is divisible by 3.

Example:

618 is divisible by 6 since it is an even number and the sum of its digits $6 + 1 + 8 = 15$ is divisible by 3.

738 is divisible by 6 since it is an even number and the sum of its digits $7 + 3 + 8 = 18$ is divisible by 3. Therefore 738 is divisible by 6.

Test for 7:

When the last digit of a number is doubled and the result is subtracted from the number formed by the remaining digits, the outcome is divisible by 7.

Example: Take the number 861. the last digit is 1 and the number formed by the remaining digits is 86, double 1 to give $(1+1)=2$

Mathematics is the key

Subtract 2 from 86 to give $(86 - 2) = 84$
 84 is divisible by 7. Hence 861 is also divisible by 7.

Test for 8:

A number is divisible by 8 if the number formed by the last three digits is divisible by 8.

Example:

In the number 7960,760 the number formed by the last three digits. It is divisible by 8 therefore 7960 is divisible by 8.

Test for 9:

A number is divisible by 9 if the sum of its digits is divisible by 9.

Example: 198 the sum of 198 is $1+9+8 = 18$

18 is divisible by 9 therefore 198 is divisible by 9.

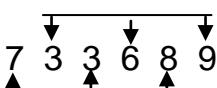
Test for 10:

A number is divisible by 10 if the digit in the ones place is 0 eg 70, 60, 120, 3010.

A number which is divisible by 10 is also divisible by 2 and 5.

Test for 11:

A number is divisible by 11 if the difference between the sum of the digits in even places and the sum of the digits in the odd place is zero (0) or divisible by 11.

eg Even position: 

Odd position

Sum of the numbers in odd positions = $7 + 3 + 8 = 18$

Sum of the numbers in even positions = $3 + 6 + 9 = 18$

Difference between sums = $18 - 18 = 0$

Since difference is divisible by 11

\therefore the number 676390 is divisible by 11.

Activity

- Which of the following numbers is divisible by 6
 456 1476 129
- Circle the numbers divisible by 10
 34 290 190 2789
- Which of the following numbers is divisible by 9
 1476 91099 189 4567

REFERENCE

A New Edition MK Primary Maths Pupils BK 7 Pg 60-63

SUB TOPIC: WHOLE, NATURAL, ODD, EVEN AND PRIME NUMBERS

(i) Whole numbers:

All positive numbers with zero (0) inclusive form a set of whole numbers
eg 0, 1, 2, 3, 4, 5, 6, 7, 8, 9,.....

(ii) Natural numbers:

Natural numbers are counting numbers. The first natural number is 1
eg 1, 2, 3, 4, 5, 6, 7, 8, 9,

(iii) Odd numbers:

Any number which is not exactly divisible by 2
eg 1, 3, 5, 7, 9,

(iv) Even numbers:

Any number which is exactly divisible by 2. The first even number is 0
eg 2, 4, 6, 8,

(v) Prime numbers:

Numbers with only two factors. One and itself. The first prime number is 2. 2 is the only even/prime number.

eg 2, 3, 5, 7,

Activity

1. Find the sum of the first five;
 - (a) Prime numbers
 - (b) Even numbers
 - (c) Odd numbers
2. Find the product of the fourth prime number and the third whole number.

REFERENCE

A New MK Primary Mathematics Bk 7

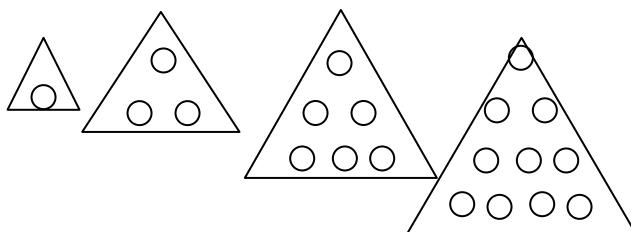
SUB TOPIC: COMPOSITE, TRIANGULAR, SQUARE, CUBE NUMBERS

(i) Composite numbers:

Numbers with more than two factors. Eg 4, 6, 8, 9 , 10, 12,.....

(ii) Triangular numbers:

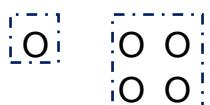
Numbers got by adding consecutive counting numbers eg 1, 3, 6, 10,



Mathematics is the key

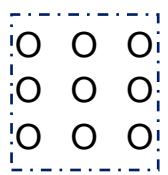
(iii) Square numbers:

Numbers got by adding consecutive odd numbers starting from 1.

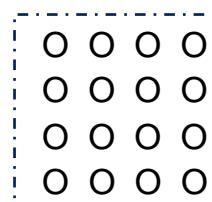


1

$$1 + 3$$



$$1 + 3 + 5$$



$$1 + 3 + 5 + 7$$

1

4

9

16

OR

Numbers got after squaring consecutive counting numbers

| | | | | |
|--------------|--------------|--------------|--------------|--------------|
| 1×1 | 2×2 | 3×3 | 4×4 | 5×5 |
| 1 | 4 | 9 | 16 | 25 |

(iv) Cube numbers:

Numbers got by multiplying a number by itself three times.

| | | | |
|----|-----------------------|-----|-------------|
| Eg | $1 \times 1 \times 1$ | $=$ | $1^3 = 1$ |
| | $2 \times 2 \times 2$ | $=$ | $2^3 = 8$ |
| | $3 \times 3 \times 3$ | $=$ | $3^3 = 27$ |
| | $4 \times 4 \times 4$ | $=$ | $4^3 = 64$ |
| | $5 \times 5 \times 5$ | $=$ | $5^3 = 125$ |

1. Find the sum of the first 8 composite numbers.
2. Find the sum of the third and the seventh triangular numbers.
3. Find the product of the fourth square number and the sixth cube number.

REFERENCE

A New MK Primary Mathematics Bk 7 exercise 4:3 Pg 65

SUB TOPIC: Finding sum of consecutive counting numbers using the formula

Sum of consecutive counting numbers

$$n\left(\frac{n+1}{2}\right)$$

Examples .

1. Find the sum of the first 20 counting numbers.

$$\begin{aligned} &n\left(\frac{n+1}{2}\right) \\ &20\left(\frac{20+1}{2}\right) \\ &20 \times \frac{21}{2} \\ &\underline{10 \times 21} \\ &\underline{\underline{210}} \end{aligned}$$

2. Find the sum of the first 15 counting numbers.
3. Find the sum of the first 40 counting numbers
4. What is the 100th triangular number?

SUB TOPIC: MULTIPLES AND FACTORS

- (i) Multiples:

These are numbers which are obtained by multiplying a number by consecutive counting numbers ie. $x 1 \quad x 2 \quad x 3$, etc

Examples:

(i) $M_6 = \{6 \times 1, 6 \times 2, 6 \times 3, 6 \times 4, 6 \times 5, 6 \times 6, 6 \times 7, \dots\}$

| | | | | | | |
|---|----|----|----|----|----|----|
| 6 | 12 | 18 | 24 | 30 | 36 | 42 |
|---|----|----|----|----|----|----|

(ii) $M_8 = \{8 \times 1, 8 \times 2, 8 \times 3, 8 \times 4, 8 \times 5, 8 \times 6, 8 \times 7, \dots\}$

| | | | | | | | |
|---|----|----|----|----|----|----|------|
| 8 | 16 | 24 | 32 | 40 | 48 | 56 | |
|---|----|----|----|----|----|----|------|

(ii) $M_9 = \{9 \times 1, 9 \times 2, 9 \times 3, 9 \times 4, 9 \times 5, 9 \times 6, 9 \times 7, \dots\}$

| | | | | | | | |
|---|----|----|----|----|----|----|------|
| 9 | 18 | 27 | 36 | 45 | 54 | 63 | |
|---|----|----|----|----|----|----|------|

- (ii) Factors:

Any one of a pair of numbers which when multiplied gives the same multiple is called a Factor.

List examples:

All factors of 6

$$6 \div 1 = 6$$

$$1 \times 6 = 6$$

$$6 \div 2 = 3$$

$$2 \times 3 = 6$$

$$6 \div 3 = 2$$

$$F_6 = \{1, 2, 3, 6\}$$

$$6 \div 6 = 1$$

$$F_6 = 1, 2, 3, 6$$

Note F_6 means factors of 6.

Find factors of 9.

$$1 \times 9 = 9$$

$$3 \times 3 = 9$$

$$F_9 = \{1, 3, 9\}$$

Activity

1. Find the first 10 multiples of;

- 5
- 6
- 12
- 9

2. Find the 20th multiple of 5

REFERENCE

A New MK Primary Mathematics Bk 7 Pg 81

3. Find all factors of;

- 12
- 15
- 24
- 29
- 36

SUB TOPIC: L.C.M AND H.C.F

- (i) **Find the LCM of 24, 36 and 40.**

| | | | |
|---|----|----|----|
| 2 | 24 | 36 | 40 |
| 2 | 12 | 18 | 20 |
| 2 | 6 | 9 | 10 |
| 3 | 3 | 9 | 5 |
| 3 | 1 | 3 | 5 |
| 5 | 1 | 1 | 5 |
| | 1 | 1 | 1 |

$$\begin{aligned}
 &= 2 \times 2 \times 2 \times 3 \times 3 \times 5 \\
 &= 4 \times 6 \times 15 \\
 &= 4 \times 90 \\
 &= 360
 \end{aligned}$$

- (ii) **Find the HCF of 6, 8 and 12.**

| | | | |
|---|---|---|----|
| 2 | 6 | 8 | 12 |
| | 3 | 4 | 6 |

$$= 2$$

Activity

1. Find the LCM of 4 and 12
2. Find the LCM of 12 and 16
3. Find the GCF of 15 and 18
4. Find the GCF of 24 and 36

REFERENCE

Mathematics Revision Hand Book for Primary 5 – 7 Pg 62

A New MK Primary Six Mathematics

SUB TOPIC: APPLICATION OF LCM AND GCF

REMEMBER

The least number that is divided by more than one numbers in called LCM.

The biggest number that divides more than one number at ago is called GCF.

The product of the LCM and GCF is equal to the product of the two numbers.

TRY THESE

- (i) Find the least number which is exactly divisible by 6, 8 and 12.
- (ii) What is the smallest number of sweets that can be shared by 3, 4 or 6 pupils leaving 5 sweets as a reminder?
- (iii) Two bells are used in Star p/s at intervals of 30 minutes and 40 minutes respectively. They are first rung together at 8:45 am, when will the two bells ring together again?
- (iv) The product of two numbers is 240. One of them is 60, workout their:
 - (a) LCM
 - (b) GCF
- (v) The LCM of x and y is 48 and HCF is 4. If $x=16$ find y .

REFERENCE

MK Primary Mathematics Bk 6 Pg 85 (Old Edition)

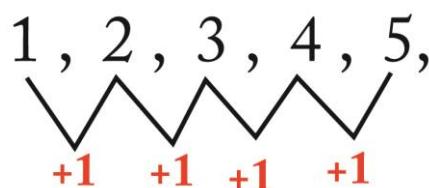
Oxford Primary Mathematics Bk 6 Pg 35

SUB TOPIC: CONSECUTIVE NUMBERS

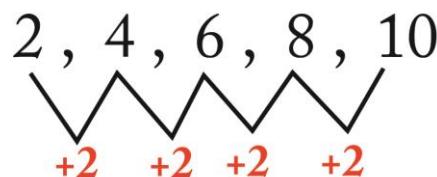
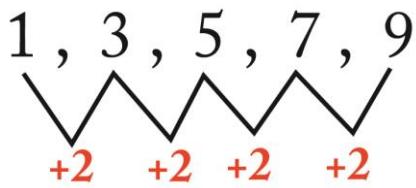
Consecutive numbers are numbers which follow each other using a defined pattern.

NOTE THE FOLLOWING

- * Counting number, integers and whole numbers have a range / a pattern of one.



- * Even numbers and odd numbers have a range of two.



Examples:

- (i). The sum of three consecutive counting numbers is 18. Find the numbers.

Let the first number be r .

| 1 st | 2 nd | 3 rd | Sum |
|-----------------|-----------------|-----------------|-----|
| R | $R + 1$ | $R + 2$ | 18 |

$$R + R + 1 + R + 2 = 18$$

$$R + R + R + 1 + 2 = 18$$

$$3R + 3 = 18$$

$$3R + 3 - 3 = 18 - 3$$

$$3R = 15$$

$$\frac{3R}{3} = \frac{15}{3}$$

$$R = 5$$

1ST NO.

$$R = 5$$

2ND NO.

$$R + 1 \text{ but } R = 5$$

$$5 + 1 = 6$$

3RD NO.

$$R + 2 \text{ where } R = 5$$

$$5 + 2 = 7$$

The numbers are

5, 6, AND 7

Example ii.

- (ii). The sum of 3 consecutive odd numbers is 15. Find the numbers

Let the first number be y .

| 1 st No. | 2 nd No. | 3 rd No. | Total |
|------------------------|------------------------|------------------------|-------|
| Y | $Y + 2$ | $Y + 4$ | 15 |

$$Y + Y + 2 + Y + 4 = 15$$

$$Y + Y + Y = 2 + 4 = 15$$

$$3Y + 6 = 15$$

$$3Y + 6 - 6 = 15 - 6$$

$$3Y = 9$$

$$\frac{3Y}{3} = \frac{9}{3}$$

$$Y = 3$$

1st No.

$$y = 3$$

2nd No.

$$y + 2 = y$$

$$\text{Where } y = 3$$

$$3 + 2 = 5$$

3rd No.

$$y + 4$$

$$\text{where } y = 3 \quad 3 + 4 = 7$$

The numbers are

3, 5, and 7

- (iii) The sum of 4 consecutive even numbers is 76. What are the numbers?
 (iv) The sum of three consecutive integers is 84. Find the numbers
 (v) The sum of 3 consecutive odd numbers is 39. Find the numbers

REFERENCE

A New MK Primary Bk 6 Pg 76 Old Edition)

SUB TOPIC: SQUARES AND SQUARE ROOTS

Examples:

- (i) Find the square root of 4.

$$\sqrt{4} = \begin{array}{|c|c|} \hline 2 & 4 \\ \hline 2 & 2 \\ \hline & 1 \\ \hline \end{array} = \sqrt{2 \times 2} = 2$$

- (ii) Find the square root of $7\frac{1}{9}$

$$\sqrt{7\frac{1}{9}} = \sqrt{\frac{64}{9}}$$

| | |
|---|----|
| 2 | 64 |
| 2 | 32 |
| 2 | 16 |
| 2 | 8 |
| 2 | 4 |
| 2 | 2 |
| | 1 |

| | |
|---|---|
| 3 | 9 |
| 3 | 3 |
| | 1 |

$$\sqrt{9} = 3$$

$$\sqrt{7\frac{1}{9}} = \sqrt{\frac{64}{9}} = \frac{8}{3} = 2\frac{2}{3}$$

$$\sqrt{64} = 2 \times 2 \times 2 = 8$$

- (iii) Find the square root of the following

- ❖ 81
- ❖ 196
- ❖ 400
- ❖ $20\frac{1}{4}$

- (iv) Find the square root of 0.36

REFERENCE

A New MK Pupils Bk 6 (Old Edition) Pg 90 – 92

SUB TOPIC: CUBE ROOTS

Example:

Find the cube root of 8.

$$\sqrt[3]{8} = \begin{array}{|c|c|} \hline 2 & 8 \\ \hline 2 & 4 \\ \hline 2 & 2 \\ \hline & 1 \\ \hline \end{array}$$

$$\sqrt[3]{8} = 2$$

Mathematics is the Key

Method 2:

$$\sqrt[3]{8} = (2^3)^{\frac{1}{3}}$$

$$2^{(3 \times \frac{1}{3})} = 2^1 = 2$$

Find the cube root of;

- (a) 27
- (b) 64
- (c) 125

REFERENCE

Teachers' collection

SUB TOPIC: FINDING MISSING NUMBERS WHEN GIVEN SEQUENCES

REMEMBER:

- Increasing sequences use addition patterns and multiplication patterns
- Reducing sequences use subtraction patterns and division patterns
- Some sequences fall under types of numbers
- Only prime numbers and composite numbers are the only types of numbers without defined patterns.

Examples

1. Find the next numbers in the sequences below.

a) 2, 3, 5, 8, 12, 17, 23

$$2 + 1 = 3$$

$$3 + 2 = 5$$

$$5 + 3 = 8$$

$$8 + 4 = 12$$

$$12 + 5 = 17$$

$$17 + 6 = 23$$

b) 18, 17, 14, 9, 2, -7

$$18 - 1 = 17$$

$$17 - 3 = 14$$

$$14 - 5 = 9$$

$$9 - 7 = 2$$

$$2 - 9 = -7$$

c) 2, 3, 5, 7, 11, **13, 17**

They are prime numbers

2. Find the next numbers in the following sequences.

- A) 2, 3, 6, 12, 22, _____, _____
- B) 64, 32, 16, 8, 4, _____, _____
- C) 1, 3, 6, 10, _____, _____
- D) 81, 64, 49, 36, _____, _____
- E) 3, 4, 12, 39, _____, _____

TOPICAL EXERCISE:

1. Add: $426 + 1519 + 3$
2. Subtract 105 from 200
3. Evaluate $3^x \div 3^2 = 27$
4. $5^3 \times 5^2 \div 5^1$
5. There were 32 apples in each box and 12 boxes in each carton. How many apples did Annet get if she bought 124 cartons?
6. What is the sum of 8456 litres of petrol and 45631 litres?
7. There were 38600 chicken on the teacher's farm. 12364 were sold on Idd day. How many remained?
8. At a party, 4848 people were served with sodas each. How many crates of soda were bought if each crate contains 24 bottles?
9. Work out (a) $2.5 \times 13 + 2.5 \times 7$
10. $4.5 \times 75 - 4.5 \times 25$
11. What number must be added to 54068 to give 60000?
12. Find the sum of even numbers between 13 and 31.
13. List down all the composite numbers between 2 and 15.
14. Find the G.C.F of 8 and 12.
15. What is the Lowest Common Multiple of 6, 8 and 16?
16. Workout the square root of 961.
17. The sum of 3 consecutive natural numbers is 63. Find the numbers.
18. Find the next number in the sequence: 4, 7, 6, 9, 8, 11, ...
19. What is the Smallest number which when divided by 9 and 11 leaves a remainder of 2?
20. Bulangiti buses leave for Kasese every 3 hours and Gateway buses leave for Soroti every four hours. Two buses set off from Kampala's bu park at 7:30am. When will the two buses leave together again?
21. The G.C.F of two numbers is 2 and their L.C.M is 24. If one of the numbers is 8, find the second number.
22. The sum of 3 consecutive even numbers is 36. Find their range.
23. Find the cube root of 64.
24. The area of a square garden is 169m². Find its perimeter.
25. Find the square root of 0.81

TERM TWO:FRACTIONS

SUB TOPIC: OPERATIONS OF FRACTIONS(Addition and subtraction)

Examples:

1. **workout** $\frac{1}{3} + \frac{1}{2}$

$$\begin{aligned}\frac{1}{3} + \frac{1}{2} &= \frac{2+3}{6} \\ &= \frac{5}{6}\end{aligned}$$

2. **Workout:** $1\frac{3}{4} + 1\frac{5}{6}$

$$1\frac{3}{4} + 1\frac{5}{6}$$

$$\frac{7}{4} + \frac{11}{6}$$

$$\frac{21 + 22}{12} = \frac{43}{12}$$

$$3\frac{7}{12}$$

3. **Workout:** $\frac{3}{4} - \frac{1}{3}$

$$\begin{array}{r} \frac{3}{4} - \frac{1}{3} \\ \hline 9 - 4 \\ \hline 5 \\ \hline 12 \end{array}$$

4. **Workout:** $3\frac{5}{6} - 1\frac{4}{5}$

$$\begin{array}{r} 3\frac{5}{6} - 1\frac{4}{5} \\ \hline \frac{23}{6} - \frac{9}{5} \\ \hline \left(\frac{23}{6} \times \frac{5}{5}\right) - \left(\frac{9}{5} \times \frac{6}{6}\right) \\ \hline 115 - 54 \\ \hline 30 \\ \hline \frac{61}{30} \end{array}$$

$$2\frac{1}{30}$$

Workout the following

(a) $\frac{1}{5} + \frac{2}{3}$

(b) $\frac{7}{8} - \frac{3}{5}$

(c) $2\frac{1}{2} + 3\frac{4}{7}$

(d) $5\frac{4}{5} - 3\frac{2}{7}$

REFERENCE

A New MK Primary Mathematics Bk 7 Pg 73/74

Mathematics is the Key

SUB TOPIC: OPERATION ON FRACTIONS(multiplication of fractions)

Examples:

1. **Workout:** $\frac{1}{5} \times 3$

$$\begin{array}{r} \frac{1}{5} \\ \times 3 \\ \hline 3 \\ 5 \\ \hline 5 \end{array}$$

2. **Workout:** $\frac{1}{3} \times \frac{3}{4}$

$$\begin{array}{r} \frac{1}{3} \\ \times \frac{3}{4} \\ \hline \end{array}$$

$$\begin{array}{r} 1 \\ \hline 4 \end{array}$$

3. **Workout:** $2 \frac{1}{4} \times 1 \frac{1}{5}$

$$\begin{array}{r} 9 \\ 4 \\ \times \frac{6}{5} \\ \hline 27 \\ 10 \\ \hline 2 \frac{7}{10} \end{array}$$

4. **Workout the following**

(a) $\frac{3}{7} \times 35$

(b) $\frac{2}{3} \times \frac{3}{10}$

(c) $\frac{5}{11} \times 1 \frac{1}{5}$

(d) $4 \frac{3}{7} \times 3 \frac{2}{3}$

REFERENCE

A New MK Primary Mathematics Pgs 75/76

SUB TOPIC: OPERATION ON FRACTIONS (Division of fractions)

Examples:

1. **Workout:** $\frac{2}{5} \div 2$

$$\begin{array}{r} 3 \\ \hline 2 \\ 1 \frac{1}{2} \end{array}$$

Try these:

$$\begin{array}{r} 2 \\ \hline 5 \\ \div 2 \end{array}$$

$$\begin{array}{r} 2 \\ \hline 5 \\ \times \frac{1}{2} \end{array}$$

$$\begin{array}{r} 1 \\ \hline 5 \end{array}$$

2. **Workout:** $\frac{3}{4} \div \frac{1}{2}$

$$\begin{array}{r} 3 \\ \hline 4 \\ \div \frac{1}{2} \\ 3 \\ \hline 4 \\ \times \frac{2}{1} \end{array}$$

1. **Workout the following.**

(a) $\frac{3}{4} \div \frac{1}{3}$

(b) $\frac{4}{5} \div \frac{1}{8}$

(c) $\frac{5}{11} \div \frac{7}{22}$

(d) $5 \frac{3}{4} \div 3 \frac{1}{2}$

REFERENCE

A New MK Primary Mathematics Bk 7 Pg 80

Mathematics is the key

Brackets

Of

Division

Multiplication

Addition

Subtraction

Examples:

1. Workout $\frac{2}{3}$ of $\frac{3}{4} - \frac{1}{3}$

$$\frac{2}{3} \text{ of } \frac{3}{4} - \frac{1}{3}$$

$$\left(\frac{2}{3} \times \frac{3}{4}\right) - \frac{1}{3}$$

$$\frac{1}{2} - \frac{1}{3}$$

$$\left(\frac{1}{2} \times \frac{3}{3}\right) - \left(\frac{1}{3} \times \frac{2}{2}\right)$$

$$\frac{3}{6} - \frac{2}{6}$$

$$\frac{3}{6} - \frac{2}{6}$$

$$\frac{1}{6}$$

$$\frac{1}{6}$$

2. : Workout $\frac{5}{6} - \frac{3}{4} \div \frac{3}{2}$

$$\frac{5}{6} - \frac{3}{4} \div \frac{3}{2}$$

$$\frac{5}{6} - \left(\frac{3}{4} \div \frac{3}{2}\right)$$

$$\frac{5}{6} - \frac{3}{4} \times \frac{2}{3}$$

$$\frac{5}{6} - \frac{1}{2}$$

$$\frac{\left(\frac{5}{6} \times 6\right) - \left(\frac{1}{2} \times 6\right)}{6}$$

$$\frac{5 - 3}{6}$$

$$\frac{2}{6}$$

$$\frac{1}{3}$$

Activity

1. Workout the following.

(a) $\frac{1}{2} - \frac{3}{4} + \frac{5}{6}$

(b) $\frac{2}{3} \times \frac{1}{3} \div \frac{3}{4}$

(c) $\frac{3}{7} \text{ of } \frac{5}{6} + 3\frac{1}{3}$

REFERENCE

A New MK Primary Mathematics Pg 127 (Old Edition)

SUB TOPIC: APPLICATION OF FRACTIONS IN REAL LIFE SITUATION

1. A boy had a jerry can full of water. He used $\frac{13}{20}$. What fraction remained?

$$1 - \frac{13}{20} = \frac{20}{20} - \frac{13}{20} = \frac{7}{20}$$

2. Mary bought a cake and she ate $\frac{1}{3}$ in the morning, $\frac{5}{12}$ in the afternoon and the rest in the evening. What fraction of the cake did she eat in the evening.

$$1 - \left(\frac{1}{3} + \frac{5}{12} \right)$$

$$1 - \left[\left(\frac{1}{3} \times \frac{4}{4} \right) + \frac{5}{12} \right]$$

$$1 - \left(\frac{4}{12} + \frac{5}{12} \right)$$

$$1 - \frac{9}{12}$$

$$\frac{12}{12} - \frac{9}{12}$$

$$\frac{3}{12}$$

$$\frac{1}{4}$$

3. If $\frac{2}{3}$ of a number is 40. What is the number?

Let the number be m

$$\frac{2}{3} \text{ of } m = 40$$

$$\frac{2}{3} \times m = 40$$

$$\frac{2m}{3} = 40$$

$$3 \times \frac{2m}{3} = 40 \times 3$$

$$2m = 120$$

$$\frac{2m}{2} = \frac{120}{2}$$

$$\underline{\underline{m = 40}}$$

4. $\frac{3}{4}$ of a number is 180. Find the number.

5. How many half litre cups of water can fill a 20 litre jerrycan?

6. In a class, $\frac{2}{5}$ are boys and the rest are girls.

(a) Find the fraction of girls.

(b) If there are 45 girls, how many pupils are in the class?

(c) If $\frac{1}{3}$ of the pupils have black shoes, how many pupils do not have black shoes?

Mathematics is the Key

7. The tank was $\frac{2}{3}$ full of water. One day , James used $\frac{1}{4}$ of the water for washing and 100 litres remained.
- What fraction of the tank was used for washing?
 - How many litres of water can it hold when full?
8. A, B and C contributed to start a Company. A paid $\frac{3}{10}$ of the cost and B contributed $\frac{5}{10}$ of the cost.
- What fraction did C contribute?
 - If C contributed shs 30,000 what was their total contribution?

REFERENCE A New MK Primary Mathematics Bk 7 Pgs 74 – 78

SUB TOPIC: APPLICATION OF FRACTIONS(of the remainder)

Examples:

1. Twaha spent $\frac{1}{3}$ of his money on books and $\frac{1}{6}$ of the remainder on transport.

- (i) What fraction of his money was left?

$$\text{Fraction spent on books} = \frac{1}{3}$$

$$\text{Remaining fraction: } 1 - \frac{1}{3} = \frac{3}{3} - \frac{1}{3} = \frac{2}{3}$$

$$\text{Fraction spent on transport: } \frac{1}{6} \text{ of } \frac{2}{3} = \frac{1}{6} \times \frac{2}{3} \\ = \frac{1}{9}$$

$$\text{transport and books: } \frac{1}{3} + \frac{1}{9}$$

$$\frac{1}{3} \times \frac{3}{3} + \frac{1}{9} = \frac{3}{9} + \frac{1}{9} = \frac{4}{9}$$

$$\text{Remained fraction} = 1 - \frac{4}{9} = \frac{9}{9} - \frac{4}{9} = \frac{5}{9}$$

- (ii) If he was left with shs 15,000= how much did he have at first?

Let the total be y.

$$\frac{5}{9} \text{ of } y = \text{sh. } 15,000$$

$$\frac{5}{9} \times y = \text{sh. } 15,000$$

$$\frac{5y}{9} = \text{sh. } 15,000$$

$$\frac{9}{5} \times \frac{5y}{9} = \text{sh. } 15000 \times \frac{9}{5}$$

$$y = \text{sh. } 3000 \times 9$$

$$y = \text{sh. } 27,000$$

He had sh. 27,000 at first

2. A father shared his land as follows, $\frac{1}{3}$ was given to the son, $\frac{1}{4}$ of the remaining land to the daughter and the rest was remained for the parents.

- (a).What fraction of the land remained for the parents

- (b).if the son got 12 hectares more than the daughter, calculate the total size of the land.

REFERENCE: A New MK Primary Mathematics Bk 7 Pg 78

SUB TOPIC: APPLICATION OF FRACTIONS(taps)

1. Tap A can fill the tank in 6 minutes and tap B can fill the same tank in 3 minutes. How long will both taps take to fill the tank if they are opened at the same time?
Method 1:

| | |
|---|-------------------------------|
| Tap A $\frac{1}{6}$ | Tap B $\frac{1}{3}$ |
| Tap A and B = $\frac{1}{6} + \frac{1}{3} = \frac{1+2}{6} = \frac{3}{6} = \frac{1}{2}$ | |
| In 1 minute the tank will be $1 \div \frac{1}{2} = 1 \times \frac{2}{1} = 2 \text{ minutes}$ | |

Note: $\frac{1}{2}$ (1 part is filled in 1 minute)
 $\frac{2}{2}$ (2 parts are filled in 2 minutes)

2. Tap A can fill the tank in 3 minutes while tap B can empty the same tank in 5 minutes. If they are opened at the same time, how long will they take to fill the tank?
3. Tap F can fill the tank in 6 hours, tap G can fill the tank in 8 hours and tap H can empty the tank in 12 hours. If they are opened at the same time, how long will they take to fill the tank?

REFERENCE

MK math Bk 7 Pg 79

SUB TOPIC: CHANGING VULGAR FRACTIONS TO DECIMALS

Examples

1. Convert $\frac{5}{8}$ to a decimal fraction

$$\begin{array}{r} 0.625 \\ 8 \overline{)50} \\ -48 \\ \hline 20 \\ -16 \\ \hline 40 \\ -40 \\ \hline 00 \end{array} \quad \frac{5}{8} = 0.625$$

Try these

1. Convert the following fractions to decimals

(a) $\frac{1}{2}$

(b) $\frac{1}{4}$

(c) $\frac{1}{8}$

Mathematics is the key

SUB TOPIC: CHANGING DECIMALS TO VULGAR FRACTIONS

Examples:

- Convert the following decimals to fractions

(a) **0.125**

$$0.125 = \frac{125}{1000}$$

$$0.125 = \frac{1}{8}$$

(b) **7.25**

$$7.25 = 7 + \frac{25}{100}$$

$$0.25 = \frac{1}{4}$$

$$0.25 = 7\frac{1}{4}$$

Activity

- Convert the following decimals to fractions

(a) 0.5

(b) 0.75

(c) 0.45

(d) 1.4

(e) 12.08

REFERENCE

A New MK Primary Mathematics Bk 7 Pg 88

SUB TOPIC: CHANGING VULGAR FRACTIONS TO RECURRING DECIMALS

Examples: Convert the following to decimal

(a) $\frac{3}{11}$

$$\begin{array}{r} 0.2727... \\ 11 \overline{)30} \\ -22 \\ \hline 80 \\ -77 \\ \hline 30 \\ -22 \\ \hline 80 \\ -77 \\ \hline 30 \end{array}$$

$$\frac{5}{8} = 0.2727...$$

(b) $\frac{1}{12}$

$$\begin{array}{r} 0.8333... \\ 12 \overline{)100} \\ -96 \\ \hline 40 \\ -36 \\ \hline 40 \\ -36 \\ \hline 4 \end{array}$$

$$\frac{5}{8} = 0.8333...$$

Convert the following to decimal



Mathematics is the Key

(a) $\frac{4}{11}$

(b) $\frac{1}{15}$

(c) $\frac{7}{9}$

(d) $\frac{9}{11}$

SUB TOPIC: CHANGING RECURRING DECIMALS TO VULGAR FRACTIONS

Examples:

- Changing recurring decimals to rational numbers:

1. $0.333\dots$

Let the No. be y

$$y = 0.333\dots$$

$$10 \times y = 0.333\dots \times 10$$

$$10y = 3.33\dots$$

$$10y = 3.33\dots$$

$$-y = 0.33\dots$$

$$\frac{9y}{9} = \frac{3}{9}$$

$$y = \frac{1}{3}$$

$$t = 0.4545\dots$$

$$100 \times t = 0.4545\dots \times 100$$

$$100t = 45.45\dots$$

$$\underline{-t - 0.45\dots}$$

$$99t = 45$$

$$\frac{99t}{99} = \frac{45}{99}$$

$$y = \frac{5}{11}$$

2. $0.4545\dots$

Let the No. be t

3. $0.1666\dots$

Let the No be a

$$a = 0.1666\dots$$

$$10 \times a = 0.1666\dots \times 10$$

$$10a = 1.666\dots$$

$$100 \times a = 0.166\dots \times 1000$$

$$100a = 16.666\dots$$

$$100a = 16.666\dots$$

$$\underline{-10a = -1.666\dots}$$

$$90a = 15$$

$$\frac{90a}{90} = \frac{15}{90}$$

$$a = \frac{1}{6}$$

Activity.

Convert the following recurring decimal fractions to vulgar fractions.

(a) $0.333\dots$

(b) $0.1212\dots$

Mathematics is the Key

(c) 0.6363...

(d) 0.01666...

REFERENCE

A New MK Primary Mathematics Bk 7 Pg 91

Mathematics is the Key

SUB TOPIC: DECIMALS (Addition and of decimals)

Examples:

Workout the following

1. $3.4 + 0.23$

$$\begin{array}{r} 3.4 \\ + 0.23 \\ \hline 3.63 \end{array}$$

2. $5 - 0.03$

$$\begin{array}{r} 5.00 \\ - 0.03 \\ \hline 4.97 \end{array}$$

Activity

Workout the following

(a) $4.57 + 4.94$

(b) $4.01 - 2.97$

(c) $5.47 + 23.98$

(d) $2 - 0.45$

Emphasis on:

- (i) arrangement of numbers according to place value.

REFERENCE

New MK Primary Mathematics Bk 7 Pg 94 (Old Edition)

SUB TOPIC: DECIMALS (Multiplication of decimals)

Examples:

Examples:

Workout the following

a. 27.36×6

$$\begin{array}{r} 27.36 \\ \times 6 \\ \hline 164.16 \end{array}$$

b. 11.9×0.3

$$\begin{array}{r} 119 \\ \hline 10 \\ 357 \\ \hline 100 \\ 3.57 \end{array}$$

Multiply the following.

- (a) 4.25×0.08
- (b) 12.45×3.6
- (c) 90.06×1.5

REFERENCE

New MK Primary Mathematics Bk 7 Pg 96 (Old Edition)

SUB TOPIC: DECIMALS (Division of decimals)

Examples:

$$1. \quad 0.72 \div 9$$

$$\frac{72}{100} \div \frac{9}{1}$$

$$\frac{72}{100} \times \frac{1}{9} = \frac{8}{100}$$

0.8

$$2. \quad 0.12 \div 0.3$$

$$\frac{12}{100} \div \frac{3}{10}$$

$$\frac{12}{100} \times \frac{10}{3} = \frac{4}{10}$$

0.4

Workout the following

- (a) $6.4 \div 0.08$
- (b) $1.25 \div 2.5$
- (c) $1.6 \div 1.2$

REFERENCE

New MK Primary Mathematics Bk 7 Pg 97 (Old Edition)

SUB TOPIC: DECIMALS (using BODMAS)

Examples

1. **Workout.** $8 - 5.16 + 3.07$
Re-arrange first $8 + 3.07 - 5.16$

| | |
|---------------------------------|--------------------------------|
| 8.00 | 11.07 |
| $+ 3.07$ | $- 5.16$ |
| <hr/> <u>11.07</u> | <hr/> <u>5.91</u> |

2. **Workout :** $0.2 \times 1.6 - 2.7$

$$(0.2 \times 1.6) - 1.7$$

$$3.2 - 1.7$$

1.5

3. **Workout:** $2.4 \div 1.2$ of 0.2
 $2.4 \div (1.2 \text{ of } 0.2)$

$$\begin{aligned}
 & 2.4 \div (1.2 \times 0.2) \\
 & \frac{24}{10} \div \left(\frac{12}{10} \times \frac{2}{10} \right) \\
 & \frac{24}{10} \div \left(\frac{24}{100} \right) \\
 & \frac{24}{10} \times \frac{100}{24} \\
 & \underline{\underline{10}}
 \end{aligned}$$

Activity

Workout the following

- (a) $5.6 - 7.8 + 6.12$
- (b) $1.6 + 0.6 \times 1.2$
- (c) $3.5 \times 0.12 \div 0.4$
- (d) $1.0 \text{ of } 6.4 \div 0.08$

SUB TOPIC: DECIMALS (mixed operation)

Examples:

Simplify the following

$$\begin{aligned}
 1. \quad & \frac{0.24 \times 0.3}{0.8} \\
 & \left(\frac{24}{100} \times \frac{3}{10} \right) \div \left(\frac{8}{10} \right) \\
 & \frac{24}{100} \times \frac{3}{10} \times \frac{10}{8} \\
 & \frac{3 \times 3}{100} = \frac{9}{100} \\
 & \underline{\underline{0.09}}
 \end{aligned}$$

$$\begin{aligned}
 2. \quad & \frac{0.06 \times 2.4}{1.2} \\
 3. \quad & \frac{0.24 \times 1.6}{3.6} \\
 4. \quad & \frac{2.7 \times 0.54}{1.63 + 0.17}
 \end{aligned}$$

REFERENCE

New MK Primary Mathematics Bk 7 Pg 135 (Old Edition)

SUBTOPIC: Word problems on decimals

1. A carpenter bought 3 pieces of timber each measuring 1.97m. Find the total length of the timber he bought.

$$1.97 \times 3m$$

$$\begin{array}{r} 197 \\ \times 3 \\ \hline 591 \\ \hline 100 \\ \hline 5.91 m \end{array}$$

2. How many 0.5 litre cups can be got from a 20 litre jerry can?

$$20 \div 0.5$$

$$20 \div \frac{5}{10}$$

$$20 \times \frac{10}{5}$$

$$4 \times 10$$

40 cups

3. How many 0.25 litre cups can fill a 15 litre jerrycan of water?

4. James cut 2.5 m pieces of cloth from a 40 metre piece of cloth. How many pieces did he get?

5. How many 0.5 litre cups can fill a 12 bucket of water?

RATIOS

A ratio is a comparison of objects

SUB TOPIC: Expressing quantities as ratios

Examples:

1. A class has 20 boys and 30 girls. What is the ratio of boys to girls?

The ratio of boys to girls.

Number of boys

Number of girls

$$\begin{array}{r} 20 \\ \hline 30 \\ 2 \\ \hline 3 \end{array}$$

The ratio of boys to girls is 2:3 and the ratio of girls to boys is 3:2

2. On Mr. Okello's farm, there are 40 cows, 25 goats, 60 hens and 15 pigs. Find the;
- Ratio of goats to cows
 - Ratio of hens to pigs

- (c) Ratio of pigs to cows
- (d) Ratio of cows to the total number
- (e) Cows to goats to pigs to hens

REFERENCE

New MK Primary Mathematics Bk 7 Pg 96 (Old Edition)

SUB TOPIC: Sharing quantities in ratios

Examples:

1. Bob, Bonny and Ben shared 60 oranges in the ratio of 2:3:5 respectively. How many oranges did each boy get?

Total ratio

$$2 + 3 + 5 = 10$$

Bob

$$\frac{2}{10} \times 60 = 2 \times 6 = 12 \text{ Oranges}$$

Bonny

$$\frac{3}{10} \times 60 = 3 \times 6 = 18 \text{ Oranges}$$

Ben

$$\frac{5}{10} \times 60 = 5 \times 6 = 30 \text{ Oranges}$$

2. Share 18 in the ratio 4:5

$$\textbf{Total ratio} = 4 + 5 = 9$$

$$\textbf{1st share} = \frac{4}{9} \times 18 = 4 \times 2 = 8$$

$$\textbf{2nd share} = \frac{5}{9} \times 18 = 5 \times 2 = 10$$

3. In a class of 80 pupils, the ratio of boys to girls is 3:5

(a) Find the number of girls

(b) Find the number of boys

(c) If $\frac{3}{4}$ of the girls have school uniform, how many girls don't have uniform?

4. James, Jack and Oscar shared sh.24,000 in the ratio of 3:7:2 respectively. How much money did each get?

REFERENCE

New MK Primary Mathematics Bk 7 Pg 99 (Old Edition)

SUB TOPIC: Finding the number shared in the given ratio

Examples:

- Mary, Jane and shared money in the ratio 2:3:1 respectively. If Mary got shs 12,000. How much money did they share?

$$\text{Total ratio} = 2 + 3 + 1 = 6$$

Mary had 2 parts rept sh. 12,00

$$1 \text{ part rept} \frac{\text{sh. } 12000}{2}$$

$$6 \text{ parts rept} \frac{\text{sh. } 12000}{2} \times 6$$

$$\text{sh. } 12000 \times 3$$

$$\text{sh. } 36,000$$

They shared sh 36,000

- The ratio of boys to girls in a class is 2:3. If there are 45 girls, how many pupils are in the class?
- The number of goats, cows and sheep on a certain farmare in the ratio of 4:3:5 respectively. There are 40 more sheep than goats on the farm. Find the number of each type of animal on the farm

REFERENCE

New MK Primary Mathematics Bk 7 Pg 112 (Old Edition)

SUB TOPIC: Increasing and decreasing quantities in a given ratio

Example1: Increase 80kg in the ratio of 5:4

$$\begin{aligned}\frac{5}{4} \times 80\text{kg} \\ 5 \times 20\text{kg} \\ \underline{100\text{kg}}\end{aligned}$$

Example 2: Decrease sh.2000 in the ratio of 3:5

$$\begin{aligned}\frac{3}{5} \times \text{sh. } 2,000 \\ 3 \times \text{sh. } 400 \\ \underline{\text{sh. } 1,600}\end{aligned}$$

Decrease the following as instructed

- 400g in the ratio of 1:4
- Sh.10,000 in the ration of 7:20

Increase the following as instructed

- 8,000g in the ratio of 1:4
- Sh.28,000 in the ration of 7:20

Mathematics is the key

REFERENCE

New MK Primary Mathematics Pg 97 (Old Edition)

SUB TOPIC: FINDING RATIO OF INCREASE OR DECREASE

Ratio of increase/decrease = $\frac{\text{New no.}}{\text{old no.}}$

Ratio of increase/decrease = *new number : old number*

Examples:

1. In what ratio must 30 be decreased to 24?

New: old

24: 30

$$\frac{24}{6} : \frac{30}{6}$$

4: 5

2. The number of pupils in a school increased from 480 by 60. In what ratio did it increase?

Old no. = 480

New no. = $480 + 60 = 540$

New: old

540: 480

$$\frac{540}{60} : \frac{480}{60}$$

9: 8

3. In what ratio must 90 be increased to 120
4. Allen's salary reduced from sh.90,000 to sh.85,000. In what ratio did Allen's salary reduce?
5. Dan's salary reduced from sh.90,000 to sh.85,000. In what ratio did Dan's salary reduce?
6. Jamada had 200 mangoes and later he sold 80 oranges. In what ratio did his oranges reduce?

REFERENCE

New MK Primary Mathematics Bk 7 Pg 97

SUB TOPIC: Finding numbers increased in ratios

1. What number becomes 54 when increased in the ratio of 9:8?

Let the number becomes k

$$\frac{9}{8} \times k = 54$$

$$\frac{9k}{8} = 54$$

$$8 \times \frac{9k}{8} = 54 \times 8$$

$$9k = 54 \times 8$$

$$\frac{9k}{9} = \frac{54 \times 8}{9}$$

$$k = 6 \times 8$$

$$\underline{k = 48}$$

Activity

1. The number of pupils in a class increased in the ratio of 3:4 to 120. How many pupils were in class before?
2. What number becomes 30 when increased in the ratio of 4:5?
3. Peters new salary is sh.300,000. Find his old salary if it was increased in the ratio of 15:13.

SUB TOPIC: Finding numbers decreased in ratios

1. What number becomes 64 when increased in the ratio of 8:11?

Let the number becomes k

$$\frac{8}{11} \times m = 64$$

$$\frac{8m}{11} = 64$$

$$11 \times \frac{8m}{11} = 64 \times 11$$

$$8m = 64 \times 11$$

$$\frac{8m}{8} = \frac{64 \times 11}{8}$$

$$m = 11 \times 8$$

$$\underline{m = 88}$$

Activity

1. The number of pupils in a class reduced in the ratio of 2:3 to 60. How many pupils were in class before?
2. What number becomes 63 when decreased in the ratio of 7:13?
3. After having an accident, Ann's eggs got broken and reduced in the ratio of 3:7.if she remained with 45 eggs, how many eggs did she have at first?

SUB TOPIC: Direct proportion

Examples:

- Two books cost shs 2000. Find the cost of 6 similar books.

$$\begin{aligned}
 & \text{2 books cost sh 2000} \\
 & \text{1 book costs } \frac{\text{sh 2000}}{2} \\
 & \text{6 books cost } \frac{\text{shs 2000}}{2} \times 6 \\
 & \quad 2000 \times 3 \\
 & \quad \underline{\text{Shs 6,000}}
 \end{aligned}$$

- The cost of 4 rulers is sh.2,800. find the cost of 13 similar rulers.
- A bicycle can cover a distance 20 km in just 40minutes. What distance can it cover in $2\frac{1}{2}$ hours moving at the same speed?
- $\frac{2}{3}$ of the books in the book shop are school text books. How many books are in the book shop altogether if the school textbooks are 240?

REFERENCE

New MK Primary Mathematics Bk 7 Pg 115 (Old Edition)

SUB TOPIC: Indirect/inverse proportion

Examples:

- 4 men take 9 days to complete a job. How long will 12 men take to finish the job at the same rate?

$$\begin{aligned}
 & \text{4 men take 9 days} \\
 & \text{1 man take } 9 \times 4 \text{ days} \\
 & \text{12 men take } \frac{9 \times 4}{12} \text{ days} \\
 & \quad \underline{\text{3 days}}
 \end{aligned}$$

- If 12 girls can sweep the compound in 90 minutes, how long will 15 girls take to sweep the same compound?
- A taxi can cover a distance in 4 hours at a speed of 60km/hour, at what speed can a taxi move in order to cover the same distance in 3hours

REFERENCE

New MK Primary Mathematics Bk 7 Pg 104 (New Edition)

Mathematics is the key

PERCENTAGES

SUB TOPIC: Expressing quantities as percentages

1. In a school, there are 150 boys and 100 girls. Express the number of;

(a) girls as a percentage

$$\frac{100}{100 + 150} \times 100\%$$

$$\frac{10}{25} \times 100\%$$

$$10 \times 4\%$$

$$40\%$$

(b) boys as a percentage

$$\underline{100\% - 40\% = 60\%}$$

2. On a farm, there are 20 goats and 15 sheep.

(a) Find the percentage of sheep on the farm

(b) Find the percentage of goats on the farm

3. James spent sh.5,000 and saved the rest of his sh.20,000 which he had.

(a) calculate the percentage of the money he spent.

(b) calculate the percentage of the money he saved.

4. Write 20 as a percentage of 80.

5. Amos got 12 out of 25 in a Maths test. Express his mark as a percent.

SUB TOPIC: Expressing one quantity as percentage of another

1. Express 15 minutes as percentage of an hour.

$$\frac{15}{60} \times 100\%$$

$$\frac{1}{4} \times 100\% = 25\%$$

2. Express 60cm as a percentage of 2m

3. Express 9 items as a percentage of $2\frac{1}{2}$ dozens.

4. What is 400m as a percentage of a kilometre?

5. Express 40 minutes as a percentage of 2 hours

SUB TOPIC: Finding quantities equivalent to a percentage

Examples

1. What is 20% of 60 mangoes?

20% of 60 mangoes

$$\frac{20}{100} \times 60 \text{ mangoes}$$

$$2 \times 6 \text{ mangoes}$$

$$12 \text{ mangoes}$$

2. What is $33\frac{1}{3}\%$ of 45 books?

$$33\frac{1}{3}\% \text{ of } 45 \text{ books}$$

$$33\frac{1}{3}\% \times 45 \text{ books}$$

$$\frac{33\frac{1}{3}}{100} \times 45 \text{ books}$$

$$\left(\frac{100}{3} \div 100\right) \times 45 \text{ books}$$

$$\left(\frac{100}{3} \times \frac{1}{100}\right) \times 45 \text{ books}$$

$$\frac{1}{3} \times 45 \text{ books}$$

$$\underline{\underline{15 \text{ books}}}$$

3. What is 78% of sh.40,000?

4. What is 34% of 250?

5. What is 60% of 50?

6. What is 12% of sh.69,000?

SUB TOPIC: Solving problems involving percentages

Examples:

1. If 20% of a number is 40, what is the number?

Let the number be m

$$20\% \text{ of } m = 40$$

$$\frac{20}{100} \times m = 40$$

$$\frac{m}{5} \times 5 = 40 \times 5$$

$$\underline{\underline{m = 200}}$$

2. If 80% of the children at the health centre were immunized against measles in the month of April,

(a) what percentage of the children were immunized in other months?

$$100\% - 80\% = 20\%$$

(b) How many children were immunized altogether given that 1600 children were immunized in April?

Let the total number of children be y

$$80\% \text{ of } y = 1600$$

$$\begin{aligned}
 \frac{80}{100} \times y &= 1600 \\
 \frac{8y}{10} &= 1600 \\
 10 \times \frac{8y}{10} &= 1600 \times 10 \\
 8y &= 1600 \times 10 \\
 \frac{8y}{8} &= \frac{16000}{8} \\
 y &= 2,000 \text{ children}
 \end{aligned}$$

(c) How many children were immunized in other months?

$$\begin{aligned}
 \frac{20}{100} \times 2000 &\text{ children} \\
 20 \times 20 & \\
 400 &\text{ children}
 \end{aligned}$$

Activity

1. If 30% of my salary is spent on food and I save sh. 21,000. What is my salary?
2. If 15% of a number is 90. Find the number.
3. If 40% of a class is absent;
 - a. What percentage is present?
 - b. How many pupils are in class if 24 pupils are absent in class?
4. 35% of the pupils in a school like rice while 10% like potatoes. If the rest like posho,
 - (a) What percentage of pupils like posho?
 - (b) How many pupils are in school if 63 pupils like posho?

SUB TOPIC: Solving problems involving percentages

Examples:

3. There are 20% more boys than girls in a class.
 - a) Find the percentage of girls.

Let the %ge of girls be m

| boys | girls | TL |
|------|-------|-----|
| m+20 | m | 100 |

$$\begin{aligned}
 m + m + 20 &= 100\% \\
 2m + 20 &= 100 \\
 2m + 20 - 20 &= 100 - 20 \\
 2m &= 80 \\
 \frac{2m}{2} &= \frac{80}{2} \\
 m &= 40\%
 \end{aligned}$$

b) Find the percentage of boys.

$$m + 20\%$$

$$40 + 20\%$$

$$60\%$$

c) If there are 90 boys in the class, how many pupils are in the class?

Let the total number of pupils be w

$$\frac{60}{100} \times w = 90$$

$$100 \times \frac{60w}{100} = 90 \times 100$$

$$60w = 90 \times 100$$

$$\frac{60w}{60} = \frac{90 \times 100}{60}$$

$$\underline{\underline{w = 150 \text{ pupils}}}$$

4. If 20% of a number is 40, what is the number?

Let the number be m

$$20\% \text{ of } m = 40$$

$$\frac{20}{100} \times m = 40$$

$$\frac{m}{5} \times 5 = 40 \times 5$$

$$\underline{\underline{m = 200}}$$

❖ Nanyonjo earns sh. 12,000. She spends 75% and saves the rest.

- How much does she spend?
- How much does she save?

❖ 4. If 30% of my salary is spent on food and I save sh. 21,000. What is my salary?

❖ If 40% of a class is absent, what percentage is present?

- What percentage is present?

❖ 35% of the pupils in a school like rice while 10% like potatoes. If the rest like posho, what percentage of pupils like posho?

REFERENCE

New MK Primary Mathematics Bk 7 Pg 111 and 112 (New Edition)

New MK Primary Mathematics Bk 7 Pg 113 - 114 (New Edition)

SUB TOPIC: Increasing quantities using percentages

Examples:

1. Increase 800 by 20%

New amount: = $100\% + 20\% \text{ of old amount}$

$$= 120\% \times 800$$

$$= \frac{120}{100} \times 800$$

$$\underline{\underline{= 960}}$$

2. Increase 800 pupils by $12\frac{1}{2}\%$:

New number = $100\% + 12\frac{1}{2}\% \text{ of old number}$

$$= 112\frac{1}{2}\% \text{ of } 800 \text{ pupils}$$

$$= \frac{225}{2} \times 800 \text{ pupils}$$

$$= \frac{225}{2} \div 100 \times 800$$

$$= \frac{225}{2} \times \frac{1}{100} \times 800$$

$$= (225 \times 4) \text{ pupils}$$

$$\underline{\underline{= 900 \text{ pupils}}}$$

3. Increase shs 4800 by 10% and then by 20%

Old amount = shs 4800

$$10\% \text{ increment} = 100\% + 10\% = 110\%$$

$$20\% \text{ increment} = 100\% + 20\% = 120\%$$

$$110\% \times 120\% \text{ of sh. } 4800$$

$$\frac{110}{100} \times \frac{120}{100} \times \text{sh. } 4800$$

$$11 \times 12 \times 48$$

$$\underline{\underline{\text{Sh. } 6336}}$$

❖ Increase the following as instructed

- 90 by 15%
- 400 by 60%
- Sh.20,000 by 20% by 30%

REFERENCE

New MK Primary Mathematics Bk 7 Pg 109 - 110 (New Edition)

Mathematics is the Key

SUB TOPIC: Decreasing quantities using percentages

1. Decrease sh. 1,500 by 10%

New amount as percentage

$$100\% - 10\% = 90\%$$

New amount: = 90% of sh. 1500 =

$$\frac{90}{100} \times \text{sh. } 1500$$

$$90 \times 15$$

$$\underline{\text{sh. } 1350}$$

2. Decrease 720 dollar a by $33\frac{1}{3}\%$

$$\text{New percentage} = 100\% - 33\frac{1}{3}\% = 66\frac{2}{3}\%$$

$$\text{New amount} = 66\frac{2}{3}\% \text{ of } 720 \text{ dollars}$$

$$\frac{200}{3}\% \text{ of } 720 \text{ dollars}$$

$$\frac{200}{3} \times \frac{1}{100} \times 720 \text{ dollars}$$

$$2 \times 240 \text{ dollars}$$

$$\underline{480 \text{ dollars}}$$

Decrease the following as instructed

(a) 800 by 15%

(b) 200 goats by 20%

(c) Sh.200,000 by 5% then 30%

REFERENCE

A New MK Primary Mathematics 2000 Bk 7 Pg 117

Mathematics Revision Handbook P5 – P7 Pg 101

SUB TOPIC: FINDING THE ORIGINAL NUMBER AFTER %age INCREASE

Examples:

1. What amount of money when increased by 20% becomes Sh.1440?

Let the amount be x.

New amount = (100% + 20) of x

$$120\% \times x = \text{sh. } 1440$$

$$\frac{120x}{100} = \text{sh. } 1440$$

$$10 \times \frac{12x}{10} = \text{sh. } 1440 \times 10$$

$$\underline{12x = \text{sh. } 14400}$$

Mathematics is the key

$$\begin{aligned}\frac{12x}{12} &= \frac{\text{sh. } 14400}{12} \\ x &= \underline{\text{sh. } 1,200}\end{aligned}$$

2. The number of pupils in a class increased by 10% to 44 pupils. Find the number of pupils before the increase.
3. What number becomes 10400 when increased by 30%?

REFERENCE

A New MK Primary Mathematics Bk 6 & 7 Pg 118

SUB TOPIC: FINDING THE ORIGINAL NUMBER AFTER THE DECREASE

Examples:

1. A worker's salary was decreased by 35% to sh.1560.

Let the old salary be x .

$$\text{New salary} = (100\% - 35\%) \text{ of } x$$

$$\begin{aligned}1560 &= \frac{65x}{100} \\ 1560 \times 100 &= \frac{65x}{100} \times 100 \\ \frac{65x}{65} &= \frac{1560 \times 100}{65} \\ x &= \underline{\text{shs. } 2400}\end{aligned}$$

2. What number when decreased by 25% becomes 30,000?
3. What amount of money becomes sh.sh.7,200 when decreased by 10%?

REFERENCE

A New MK Primary Mathematics Bk 7 Pg 119

SUB TOPIC: FINDING PERCENTAGE INCREASE AND DECREASE

$$\text{Percentage increase} = \frac{\text{increase}}{\text{old no.}} \times 100\%$$

$$\text{Percentage decrease} = \frac{\text{decrease}}{\text{old no.}} \times 100\%$$

Mathematics is the key

Examples:

- By what percentage will 480 be increased to become 540?

Old number = 480

New number = 540

Increase = $540 - 480$

$$= 60$$

Percentage increase:

$$\frac{60}{480} \times 100\%$$

8

$$\underline{\underline{12\frac{1}{2}\%}}$$

- When 240 is decreased, it becomes 192. Calculate the percentage decrease.

Old number = 240

New number = 192

Decrease = $240 - 192$

$$= 48$$

$$\text{Percentage decrease} = \frac{48}{240} \times 100\%$$

$$= \underline{\underline{20\%}}$$

- The number of pupils in a school increased from 500 to 650 in just one term. Calculate the percentage increase
- Mary's salary decreased from sh.4,000,000 by sh.500,000. Calculate her percentage decrease.

REFERENCE

A New MK Primary Mathematics Bk 6 & 7 Pg 121 - 122

SUB TOPIC: PERCENTAGE PROFIT

$$\text{Percentage profit} = \frac{\text{profit}}{\text{CP}} \times 100\%$$

$$\text{PROFIT} = \text{SP} - \text{CP}$$

Examples:

1. An article was bought at sh.100,000 and sold at sh.120,000. Calculate the percentage profit.

$$\text{Cost price} = \text{sh. } 100,000$$

$$\text{Selling price} = \text{sh. } 120,000$$

$$\text{Profit} = 120,000 - 100,000$$

$$= 20,000$$

$$\text{Percentage profit}$$

$$\frac{\text{sh. } 20,000}{\text{sh. } 100,000} \times 100\%$$

$$\frac{2}{10} \times 100\%$$

$$2 \times 10$$

$$\underline{20\%}$$

2. Alison bought a hankie at sh.1,600 and later sold it at sh.2,000. Find his percentage profit.
3. A man sold a goat at sh. 120,000 making a profit of sh.20,000. Calculate his percentage profit.
4. Moses bought a shirt for sh.6,000 and sold it making a profit of sh.2,000.
 - (a) Find his selling price.
 - (b) Find his percentage profit.

SUB TOPIC: PERCENTAGE LOSS

$$\text{Percentage loss} = \frac{\text{loss}}{\text{CP}} \times 100\%$$

$$\text{LOSS} = \text{CP} - \text{SP}$$

4. I bought a radio at sh.100,000 but I was forced to sell it at sh.80,000. Find my percentage loss.

$$\text{Buying price} = \text{sh. } 100,000$$

$$\text{Selling price} = \text{sh. } 80,000$$

$$\text{Loss} = \text{BP} - \text{SP}$$

$$\text{sh. } 100,000 - \text{sh. } 80,000$$

$$\underline{\text{sh. } 20,000}$$

$$\underline{\text{Percentage loss:}}$$

$$\frac{\text{loss}}{\text{CP}} \times 100\%$$

$$\frac{20,000}{100,000} \times 100\% \\ \frac{100\%}{5} = 20\%$$

5. Kakuru bought a book for sh.5,000 and sold it for sh.4,500. Calculate his percentage loss.
6. Mugisha sold a rabbit for sh.15,000 making a loss of sh.4,000. calculate his percentage loss.
7. Mercy bought a blouse for sh.15,000 and sold it at a loss of sh.3,000.
 - (a) At what price did he sell the blouse?
 - (b) Find her percentage loss

REFERENCE

A New MK Primary Mathematics Bk 7 Pg 123 – 124
 Mathematics Revision Hand book P.5 – P.7 Pg 104

SUB TOPIC: Finding SP when percentage profit/loss and CP are given

REMEMBER

- The cost price (CP) is the old number.
- The selling price(SP) is the new number.
- When given percentage increase, increase the old number(CP) to get the new number(SP).

If the %ge profit is k%

$$\frac{100\% + k\%}{100} \times CP = SP$$

- When given percentage decrease, decrease the old number(CP) to get the new number(SP).

If the %ge loss is m%

$$\frac{100\% - m\%}{100} \times CP = SP$$

Examples

1. After selling a shirt which he bought at sh.8,000, the shopkeeper made a profit of 20%. How much money did he sell the shirt?

$$SP = \frac{100 + 20}{100} \times sh. 8,000$$

$$\frac{120}{100} \times sh. 8,000$$

$$120 \times sh. 80$$

$$\underline{sh. 9,600}$$

Mathematics is the Key

2. James bought a goat at sh.120,000 and later sold it at a loss of 10%, how much did he get after selling the goat?

$$SP = \frac{100 - 10}{100} \times sh. 120,000$$

$$\frac{90}{100} \times sh. 120,000$$

$$90 \times sh. 1,200$$

$$\underline{\text{sh. } 108,000}$$

3. A skirt was bought at sh.10,000. How much was it sold if a profit of 20% was raised?
 4. After selling a tray of eggs, a farmer made a profit of 5%. At what price did he sell the tray of eggs if the cost price of the tray of eggs is sh.9,000.

SUB TOPIC: Finding CP when percentage profit and SP are given

Examples:

1. After selling a pair of shoes at sh. 21,000, a trader made a profit of 20%. Find the buying price of the pair of shoes.

$$Cost\ price\ as\ a\ percentage = 100\%$$

$$Selling\ price\ as\ a\ percentage = 100\% + 20\% = 120\%$$

$$120\% \ represents = sh. 21,000$$

$$1\% \ represents = \frac{shs. 21000}{120}$$

$$100\% \ represents = \frac{shs. 700}{4} \times 100 \\ = (25 \times 700) \\ \underline{\underline{= shs. 17,500}}$$

2. a) By selling a blanket at sh. 36000, a trader made a profit of 20%. Calculate the cost price of the blanket
 (b). At what price did he sell it in order to gain 15%?

SUB TOPIC: Finding CP when percentage loss and SP are given

1. By selling his cow at sh. 34,000, Obala made a loss of 15%. How much did the cow cost?

$$\text{Loss} = 15\%$$

$$CP = 100\%$$

$$SP = 100\% - 15\%$$

$$= 85\%$$

$$85\% \text{ of } CP = shs. 34,000$$

$$\frac{85}{100} CP = shs. 34,000$$

$$100 \times \frac{85cp}{100} = shs. 34,000 \times 100$$

$$85cp = shs. 3,400,000$$

$$\frac{85cp}{85} = \frac{shs. 3,400,000}{85}$$

$$\underline{\underline{CP = shs. 40,000}} \quad \underline{\underline{}}$$

2. A dealer sold a bicycle for sh. 45000 there by losing 10%

- (a) Calculate the original price of the bicycle.
(b) How much did he lose

REFERENCE

A New MK Primary Mathematics Bk 7 Pg 125

SUB TOPIC: Mixed application of profit and lossExample

1. Paul bought a bicycle at sh.300,000. He sold it to Tom at a profit of 10%. Tom sold it to Mary at a loss of 35%. What did Mary pay for the bicycle?

$$\begin{aligned} & \frac{\text{Tom paid}}{100\% - 10\%} \times sh. 300,000 \\ & \frac{100}{90} \times sh. 3,000 \\ & sh. 270,000 \\ & \frac{\text{Mary paid}}{100\% - 35\%} \times sh. 270,000 \\ & \frac{100}{65} \times sh. 2,700 \\ & sh. 175,500 \end{aligned}$$

2. Alex bought a cow and sold it to Mary at a loss of 20%. Mary sold to Peter at a gain of 10%. Peter paid sh.240, 000 for it. How much money did Alex pay for the cow?

Mathematics is the key

$$\text{discount} = MP - CP$$

MP = *Marked price*

CP = *Cash Price*

$$\% \text{ge discount} = \frac{\text{Discount}}{MP} \times 100\%$$

Example:

1. The market price of a shirt was sh.1500. After a discount, a customer paid sh.1200.

(a) How much was the discount?

$$\begin{aligned}\text{Discount} &= \text{Marked price} - \text{cash price} \\ &= \text{sh.1500} - \text{sh.1200} \\ &= \underline{\underline{\text{sh.300}}}\end{aligned}$$

(b). Express the discount as a percentage

$$\begin{aligned}\text{Percentage discount} &= \frac{\text{discount}}{\text{marked price}} \times 100\% \\ &= \frac{\text{shs.300}}{\text{shs.1500}} \times 100\% \\ &= \frac{1}{5} \times 100\% \\ &= \underline{\underline{20\%}}\end{aligned}$$

2. The marked price of a bicycle is shs 60,000. A customer is offered a discount of 15%. How much money does the customer pay?

$$100\% - 15\% = 85\%$$

$$\begin{aligned}\text{Amount paid} &= \frac{85}{100} \times \text{shs. } 60,000 \\ &= 85 \times \text{shs. } 600 \\ &= \underline{\underline{\text{shs. } 51,000}}\end{aligned}$$

3. The marked price of a book is sh.4000. If a customer is offered a 10% discount:

- (a) How much is the discount?
- (b) How much does the customer pay?

REFERENCE

A New MK Primary Mathematics Bk 7 Pg 129

Mathematics is the Key

SUB TOPIC: PERCENTAGE DISCOUNT

$$\text{Percentage Discount} = \frac{\text{profit}}{\text{CP}} \times 100\%$$

Examples:

1. Alex paid sh.2,000 for an article that is for sh.2,500. Calculate his percentage discount.

$$MP = \text{sh. } 2,500$$

$$CP = \text{sh. } 2,000$$

$$\begin{aligned} \text{Discount} &= \text{sh. } 2,500 - \text{sh. } 2,000 \\ &= \text{sh. } 5,00 \end{aligned}$$

Percentage discount

$$\frac{\text{sh. } 500}{\text{sh. } 2,500} \times 100\%$$

$$\frac{1}{5} \times 100\%$$

20%

2. Mercy paid sh.12,000 after being given a discount of sh.3,000. Calculate the percentage discount offered.
3. My mother paid sh.23,000 for items worth sh.25,000 in a super market. Calculate the percentage discount offered to the mother.

SUB TOPIC: Finding marked price when given %ge discount and cash price

Example:

1. Cissy paid sh.18,000 for a hand bag after being given a discount of 10%. Calculate the marked price.

Cost price as %age = 100%

Discount offered = 10%

$$\begin{aligned} \text{Cissy paid} &= 100\% - 10\% \\ &= \underline{90\%} \end{aligned}$$

Let the marked price be x

$$\frac{90}{100} \times x = \text{shs. } 18,000$$

$$100 \times \frac{90x}{100} = \text{shs. } 18,000 \times 100$$

$$90x = \text{shs. } 18,000 \times 100$$

$$\frac{90x}{90} = \frac{\text{shs. } 18,000 \times 100}{90}$$

$$x = \underline{\text{shs. } 20,000}$$

Mathematics is the Key

2. After being given a discount of 15%, a man paid sh.76,500 for a blanket.

Calculate the marked price of the blanket

REFERENCE

A New MK Primary Mathematics Bk 7 Pg 130-131

SUB TOPIC: Finding simple interest

Example:

7. A Man deposited sh.40,000 for 5 years at a simple interest rate of $2\frac{1}{2}\%$ per year.
Calculate his simple interest and the total amount after 5 years.

$$SI = PTR$$

$$\begin{aligned} &= 40,000 \times 5 \times 2\frac{1}{2}\% \\ &= 40,000 \times 5 \times \frac{2\frac{1}{2}}{100} \\ &= 400 \times 5 \times \frac{5}{2} \\ &= 200 \times 25 \\ &= \underline{\text{shs } 5,000} \end{aligned}$$

Amount = Principle + Interest

$$\text{shs } (40,000 + 5000)$$

$$\underline{\text{shs } (45,000)}$$

8. Calculate the simple interest on sh.8000 for 2yrs at 10% per annum
 9. Calculate the simple interest on sh.24000 for 8 months at simple interest rate of 15% per year.
 10. Calculate the simple interest on sh. 24000 for 8 months at a simple interest rate of 2% per month.

REFERENCE

A New MK Primary Mathematics Bk 7 Pg 132 - 133

SUB TOPIC: FINDING THE PERCENTAGE RATE

Example:

1. Calculate the rate of interest if shs 30,000 can yield a simple interest of shs 1,125 in 9 months.

$$PTR = SI$$

$$\frac{\text{shs.}30,000}{1} \times \frac{9}{12} \times \frac{R}{100} = \text{shs. } 1,125$$

$$\frac{\text{shs.}2700R}{12} = \text{Shs. } 1,125$$

$$12 \times \frac{\text{shs.}2700R}{12} = \text{shs. } 1,125 \times 12$$

$$\text{shs. } 2700R = \text{shs. } 1,125 \times 12$$

$$\frac{\text{shs.}2700R}{\text{shs.}2700} = \frac{\text{shs.}13,500}{\text{shs.}2700}$$

$$R = 5\%$$

2. Nabifo deposited sh.50000 on her saving s account. At the end of 3yrs the simple interest earned was sh.15000. Calculate the rate of interest.

REFERENCE

A New MK Primary Mathematics Bk 7 Pg 138 - 139

Mathematics is the key

SUB TOPIC: CALCULATING PRINCIPAL

Example:

1. What principal will yield shs 6,000 at 5% per year for 3 years?

$$SI = 6000$$

$$\frac{15P}{100} = 6000$$

$$R = 5\% \text{ per year}$$

$$100$$

$$T = 3 \text{ years}$$

$$100 \times \frac{15P}{100} = 6000 \times 100$$

$$P \times R \times T = \text{Simple interest}$$

$$100$$

$$P \times \frac{5}{100} \times 3 = 6000$$

$$\frac{15P}{15} = \frac{600,000}{15}$$

$$100$$

$$P = \text{shs.}40,000$$

$$\underline{\text{Principal}} = \text{shs.}40,000$$

2. A farmer borrowed money at $12 \frac{1}{2}\%$ per year. After 2 years, a simple interest of shs 8,000 was paid. Find the amount borrowed.

Solution:

$$SI = \text{shs.}8,000$$

$$P = \text{shs.}800,000 \div \frac{25}{2} \times 2$$

$$T = 2 \text{ years}$$

$$P = \text{shs.} \frac{800,000}{25}$$

$$R = 12 \frac{1}{2}\%$$

$$P = \text{shs.}32,000$$

$$P = SI \times 100$$

$$\underline{\text{Principal}} = \text{shs.}32,000$$

$$R \times T$$

$$P = \text{shs.} \frac{8,000 \times 100}{12 \frac{1}{2} \times 2}$$

3. Ali borrowed money from a bank that offers a 10% p.a rate for 4 years. If he paid sh.32,000 after 4 years. How much did he borrow?

4. What sum of money will yield sh.4,800 in 4 years at 3% p.a?

REFERENCE

A New MK Primary Mathematics Bk 7 Pg 140

SUB TOPIC: CALCULATING TIME**Example:**

1. In what time will shs 12,000 yield an interest of shs 1,800 at 5% per year.

$$\begin{array}{ll}
 P \times T \times R = SI & P \times R \times T = SI \\
 SI = 1800 = & 12,000 \times \frac{5}{100} \times T = \text{shs. } 1800 \\
 P = 12,000 & 100 \\
 R = 5\% & \frac{600}{600} T = \frac{1800^3}{600} \\
 & T = 3 \text{ years}
 \end{array}$$

2. How long will sh.48,000 take to yield sh.5400 at 15% per year?

$$\begin{array}{ll}
 P = \text{sh. } 48,000 & \text{shs. } 480 \times 15T = \text{shs. } 5400 \\
 R = 15\% \text{ per year} & \text{shs. } 7200T = \text{shs. } 5400 \\
 SI = \text{sh. } 5400 & \text{shs. } 7200 \quad \text{shs. } 7200 \\
 P \times R \times T = SI & T = \frac{3}{4} \text{ years} \\
 \text{Shs. } 48,000 \times \frac{15}{100} \times T = \text{sh. } 5400 & = (\frac{3}{4} \times 12) \\
 & = 9 \text{ months}
 \end{array}$$

3. How long will sh.48,000 take to yield sh.7,200 at a rate of 5% per year?

REFERENCE

A New MK Primary Mathematics Bk 7 Pg 142

SUB TOPIC: More about simple interest

1. A man borrowed money in a bank which offers a rate of 10% p.a for 3 years.
Calculate the sum of money he borrowed if he returned sh.26,000 after 3 years.

$$\begin{aligned}
 P + SI &= AMOUNT \\
 P + PRT &= AMOUNT \\
 P + P \times \frac{10}{100} \times 3 &= \text{sh. } 26,000 \\
 P + \frac{3P}{10} &= \text{sh. } 26,000 \\
 10 \times P + \frac{3P}{10} \times 10 &= \text{sh. } 26,000 \times 10 \\
 10P + 3P &= \text{sh. } 260,000 \\
 13P &= \text{sh. } 260,000 \\
 \frac{13P}{13} &= \frac{\text{sh. } 260,000}{13} \\
 P &= \text{sh. } 20,000
 \end{aligned}$$

Mathematics is the key

2. Sarah deposited sh. m in the bank which offers a 15% per annum for 9 month. If she got sh.534,000 after p months. Find the value of m.

TOPICAL EXERCISE ON FRACTIONS

1. Name the types of fractions and give an example on each.
2. Divide: $\frac{2}{3} \div \frac{1}{3}$
3. Simplify: $\frac{1}{2} - \frac{1}{4} - \frac{1}{3}$
4. Salim's bicycle got spoilt after he had covered a distance of 20km which was $\frac{1}{4}$ of his journey. How long was the journey?
5. In a class of 120 pupils, the ratio of girls to boys is 4:2. Find the number of boys.
6. Work out: $\frac{1}{4} + \frac{3}{5}$.
7. Simplify: $\frac{0.27 \times 0.06}{0.9 \times 0.3}$
8. Work out: $\frac{1}{4} - \frac{1}{8}$
9. Otim had 30km still to cover after traveling $\frac{3}{5}$ of the journey. How was the journey?
10. Simplify: $\frac{1}{2} \div \frac{1}{4}$
11. Subtract: $\frac{1}{2} - \frac{1}{4}$
12. In Star Schools, $\frac{3}{4}$ of the pupils who sat for the Primary Leaving Examination passed.
 - (a) If those who failed were 30, find the number of pupils who passed.
 - (b) What percentage of pupils failed the examination?
13. $\frac{2}{3} - \frac{1}{2}$
14. Add: $35.7 + 0.35$
15. A bus broke down after covering $\frac{5}{7}$ of the journey. The remaining distance to complete the journey was 140km. How long was the whole journey?
16. Divide: $4.2 \div 0.03$
17. Add: $4.05 + 11.4 + 2.36$
18. Usamah spent $\frac{1}{4}$ of his salary on food, $\frac{1}{3}$ of the remainder on debts and saved shs 3,600= .
 - (a) How much did he spend on paying debts?
 - (b) What are his earnings per month?
19. Arrange in ascending order: $\frac{1}{2}$, $\frac{3}{4}$, 0.03 and $\frac{2}{3}$.
20. Tap A takes 9 minutes to fill in the tank.
Tap B takes 12 minutes and Tap C takes 18 minutes. How long will A, B and C take to fill the tank if opened together?
21. The cost of 4 rules is shs 800. What is the cost of 6 similar rulers?
22. 5 handkerchiefs take 30 minutes to dry when exposed to the sunshine. How long will 12 handkerchiefs take to dry if exposed to the same sunshine?
23. 12 men can build a classroom in 5 days.
 - (a) How many men are needed to do the whole job in 1 day?
 - (b) How long will 10 men take to do the job?

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FRACTIONS (PERCENTAGES) TOPICAL QUESTIONS:

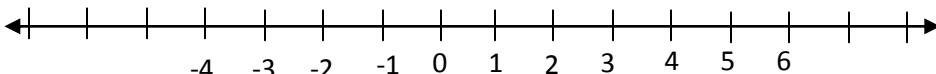
1. Express 2:5 as a percentage.
2. Change 0.8 as a percentage
3. Express 66.6% as a fraction to the lowest terms.
4. Express 40cm as a percentage of 2M.
5. What is 10% of 2200 pencils?
6. A bag of cement cost shs 5,600. How much will it cost after a 30% increase?
7. Asiimwe deposited shs 50,000 in Uganda Commercial Bank which offers an interest of 30% per year. How much money will Asiimwe have in the Bank after six months?
8. Okello bought a car at shs 2,500,000 and sold it to Otim at a profit of 20%. Otim then sold it to Tumwine at a loss of 15%. How much did Tumwine pay for the car?
9. If 280 is increased by x it becomes 392. Find the value of x .
10. Decrease 65kg by 5.
11. A farmer has the following animals:
Chicken = 30
Goats = 35
Sheep = 15
Rabbits = 10
What percentage of the total animals are rabbits.
12. Milk was mixed with water to make tea. If 14 litres of milk was used and this was 40% more than the amount of water in the tea, how was tea prepared?
13. Mugisha bought about at shs 200,000 and sold it as shs 180,000 what was his percentage loss?
14. (a) Okello's wage was increased by 10% to shs 77,000 per month. Find his salary?
(b) If his new wage of shs 77,000 was decreased by 5%, find his final wage.
15. A man spent 20% of his salary on food, 10% on transport, 40% on medical care and the rest on rent.
(i) Find the percentage of his salary spent on rent.
(ii) How much does he spend on medical care if he earns 800,000 as his salary?
(iii) How much more is spent on food than transport?
16. Fatuma had shs 5,000 if she used 10% of her money to buy soap what was her balance?
17. The cost price of a 50kg bag of sugar is shs 45,000. At what price must he sell each kilogram in order to make a profit of 20%.
18. Kakeeto bought three bags of soya beans at shs. 21,000 each. If each bag weighed 70kg and sold each kg at shs 250.
(a) Calculate his percentage gain or loss.
(b) At what price must he sell each kg in order to make a profit of 20%?

Mathematics is the key to success.

INTEGERS

SUB TOPIC: ORDERING AND ARRANGING INTEGERS ON A NUMBERLINE

The number line:



- i) All integers to the left of zero are -ve.
- ii) All integers to the right of zero are +ve
- iii) Any integer is less than that on its right.
- iv) Any integer is more than that on its left.
- v) Integers on a number line are arranged in ascending order from left to right.

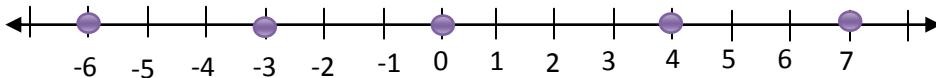
Examples

1. Use $>$, $<$ or $=$ to compare the pair of integers. Given:

- (i) $-6 < -3$
- (ii) $-3 < 0$
- (iii) $0 < +4$
- (iv) $0 > -6$
- (v) $-3 > -6$
- (vi) $+7 > +4$
- (vii) $+4 = +4$
- (viii) $-8 = -8$

2. Arrange in descending order/decreasing order the following integers:

$-6, 0, +7, -3, +4$



$+7, +4, 0, -3, -6$

3. Use $>$, $<$ or $=$ to compare the following pairs of integers.

- | | | |
|-------------------------------------|---------------------------------------|--|
| (i) $-2 \underline{\hspace{1cm}} 0$ | (ii) $-1 \underline{\hspace{1cm}} -3$ | (iii) $-6 \underline{\hspace{1cm}} -6$ |
| (iv) $8 \underline{\hspace{1cm}} 8$ | (v) $5 \underline{\hspace{1cm}} -5$ | (vi) $-7 \underline{\hspace{1cm}} 7$ |

4. Arrange the following integers in ascending order (increasing order)

$-8, 2, -1, 5, -3, +7$

5. Arrange the integers below in descending order.

$0, -7, +4, -6, +1$

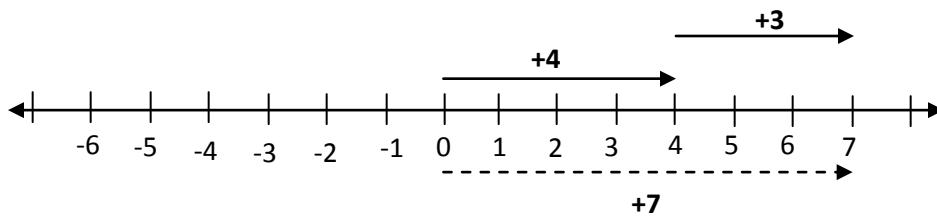
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REFERENCE

A New MK Primary Mathematics 2000 Bk 7 Pg 348 (New Edition)

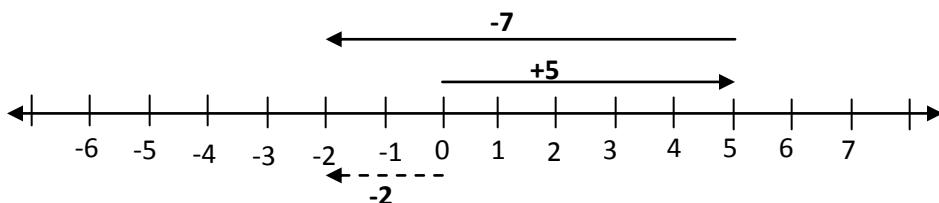
SUB TOPIC: ADDITION OF INTEGERS USING A NUMBER LINE

Example 1. Workout: $+4 + +3$



$$\underline{+4 + +3 = +7}$$

Example 2. Workout: $+5 + -7$



$$\underline{+5 + -7 = -2}$$

Add the following using a number line

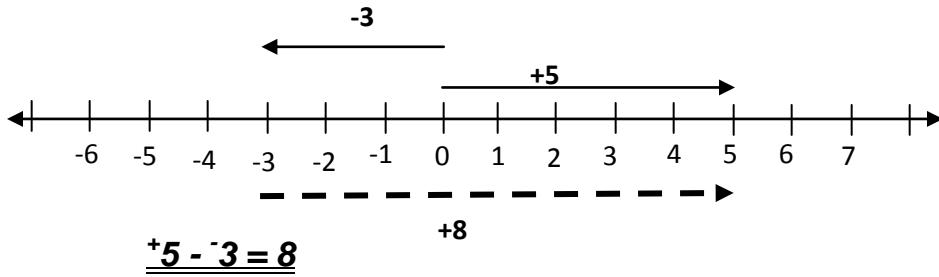
- (i) $-3 + +9$ (ii) $-4 + +5$

REFERENCE

A New MK Primary Mathematics 2000 Bk 7 Pg 346 (New Edition)

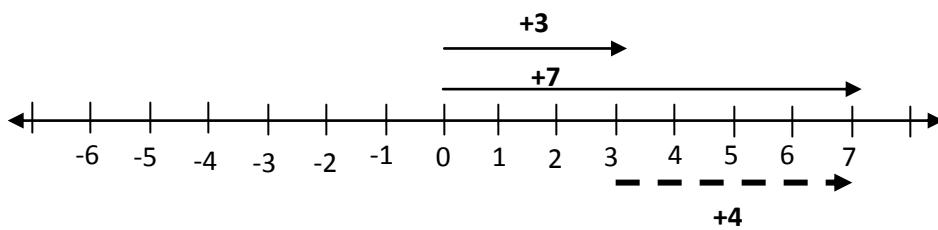
SUB TOPIC: SUBTRACTION OF INTEGERS USING A NUMBERLINE

Example 1. $+5 - 3$



$$\underline{+5 - 3 = 2}$$

Example 2. $+7 - +3$



$$\underline{+7 - 3 = 4}$$

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$$\underline{+7 - 3 = +4}$$

Workout the following using a number line

- (i) $-3 - -11$ (ii) $8 - +8$

REFERENCE

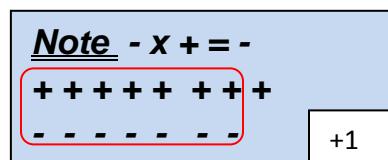
A New MK Primary Mathematics 2000 Bk 7 Pg 356 (New Edition)

SUB TOPIC: SUBTRACTING INTERGERS WITHOUT NUMBER LINES

Example 1.

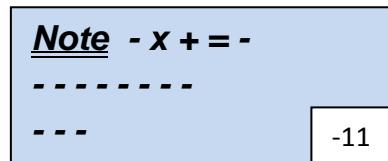
1. Workout: $+8 - +7$

$$\begin{array}{r} +8 - +7 \\ \hline +8 - 7 \\ \hline +1 \end{array}$$



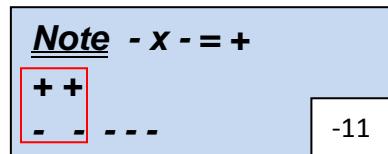
2. Workout: $-8 - +3$

$$\begin{array}{r} -8 - +3 \\ \hline -8 - 3 \\ \hline -11 \end{array}$$



3. workout: $-5 - -2$

$$\begin{array}{r} -5 + 2 \\ \hline +2 - 5 \\ \hline -3 \end{array}$$



8. Subtract the following integers.

- (i) $+4 - +2$ (ii) $+7 - -4$ (iii) $-3 - +7$

REFERENCE

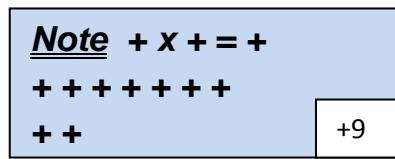
A New MK Primary Mathematics 2000 Bk 7 356 (New Edition)

SUB TOPIC: ADDING INTEGERS WITHOUT USING A NUMBERLINE

Example 1.

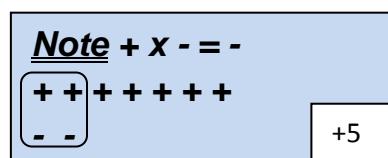
1. Workout $+7 + +2$

$$\begin{array}{r} +7 + 2 \\ \hline +7 + 2 \\ \hline +9 \end{array}$$



2. Workout $+7 + -2$

$$\begin{array}{r} +7 + -2 \\ \hline +7 - 2 \\ \hline +5 \end{array}$$



3. Workout :-7 + -2

$$\begin{array}{r}
 -7 + -2 \\
 -7 - 2 \\
 \hline
 -9
 \end{array}$$

Note $+x - = -$

- - - - -

- -

-11

Add the following integers.

- (i) $+1 + +7$ (ii) $+8 + -2$ (iii) $+18 + -18$

REFERENCE

A New MK Primary Mathematics 2000 Bk 7 Pg 352 (New Edition)

SUB TOPIC: MULTIPLICATION OF INTEGERS

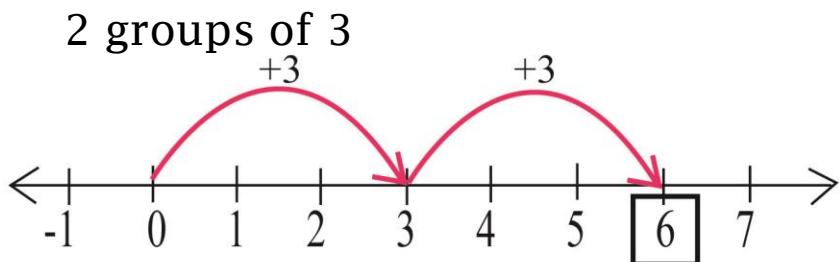
Examples:

1. $+2 \times +6 = +12$
2. $+2 \times -6 = -12$
3. $-2 \times -6 = +12$

Multiplication of integers on a number line:

Examples:

1. Workout $+2 \times +3$



NOTE:

- +ve x +ve = +ve
- +ve x -ve = -ve
- ve x -ve = +ve

2. Multiply:

- (i) $+4 \times -2$ (ii) -6×3

3. Workout -2×8 using a number line.

REFERENCE

A New MK Primary Mathematics 2000 Bk 7 Pg 352 (New Edition)

SUB TOPIC: DIVISION OF INTEGERS

NOTE:

- +ve \div +ve = +ve
- +ve \div -ve = -ve
- ve \div +ve = -ve
- ve \div -ve = +ve

Examples:

1. $+16 \div +2 = +8$
2. $+16 \div -2 = -8$
3. $-16 \div +2 = -8$
4. $-16 \div -2 = +8$

Divide:

$$(i) \quad -9 \div -3 \qquad (ii) \quad 27 \div -9$$

REFERENCE

A New MK Primary Mathematics 2000 Bk 7 Pg 361 (New Edition)

SUB TOPIC: APPLICATION OF INTEGERS

BC, LOSS, Time before, debts, below sea level are **negative**.

AD, profit, time after, above sea level are **positive**

Example 1:

A Scientist was born in 30BC and died immediately after his birthday in 76AD. How old was he when he died?

The man lived from -30 to +76

$$\begin{aligned} \text{The Scientist lived for } & +76 - (-30) \\ & = 76 + 30 \\ & = \underline{\underline{106 \text{ years}}} \end{aligned}$$

Example 2

The temperature of a drink dropped from 10°C to -4°C . By how many degrees did drop?

Old temp = 10°C

New temp = -4°C .

The temp. of the drink dropped by $10^{\circ}\text{C} - (-4^{\circ}\text{C})$

$$\begin{aligned} & = 10^{\circ}\text{C} + 4^{\circ}\text{C} \\ & = \underline{\underline{14^{\circ}\text{C}}} \end{aligned}$$

Example 3

A teacher awards 4 marks for every correct answer and deducts a mark for every wrong answer.

(a). If a pupils gets 12 correct answers in a test of 20 numbers, how many marks does he get ?

Correct answers = 12

Wrong answers = $20 - 12$

$$\underline{\underline{= 8}}$$

$$\begin{aligned} \text{Marks scored} & = (12 \times 4) - (8 \times 1) \\ & = 48 - 8 \\ & = \underline{\underline{40}} \end{aligned}$$

(b). If pupil gets 60 marks in a test of 30 questions, how wrong answers will he have got?

Let the wrong answers be m

Correct answers = $30 - m$

$$4(30 - m) - (mx1) = 60$$

$$120 - 4m - m = 60$$

$$120 - 5m = 60$$

$$120 - 120 - 5m = 60 - 120$$

$$-5m = -60$$

$$\frac{-5m}{-5} = \frac{-60}{-5}$$

$$\underline{m = 12 \text{ wrong answers}}$$

Try these

1. Flavia was born in 2BC and she died in 38AD after her birthday. How old was she when she died?

2. John left a balance of shs 1,000 with the milk vendor. He then bought 5 litres of milk from the milk vendor at shs.1000 each litre. How much did he pay to meet his bill?

3. Iganga FC arrived at Nakivubo Football stadium 15 minutes before the start of the football match. The team left the stadium 15 minutes after the end of a 45 minutes first half of the match. How long was the team in the stadium?

4. In an examination you are awarded 7 marks of every correct answer and 3 marks deducted for every wrong answer. A candidate had 9 questions correct and 5 questions wrong. What mark did the candidate score?

REFERENCE

A New MK Primary Mathematics 2000 Bk 7 Pg 362 - 363 (New Edition)

FINITE/MODULAR SYSTEM

Finite system/modular system is a system of writing remainders

SUB TOPIC: writing numbers in finite system

1. Write the following in finite system.

(a) 8 in finite 5

$$8 = 8 \div 5 \text{ (finite 5)}$$

$$8 = 1 \text{ rem } 3 \text{ (finite 5)}$$

$$\underline{8 = 3 \text{ (finite 5)}}$$

2. 40 in finite 12

$$40 = 40 \div 12 \text{ (finite 12)}$$

$$40 = 3 \text{ rem } 4 \text{ (finite 12)}$$

$$\underline{40 = 4 \text{ (finite 12)}}$$

Write;

- (a) 25 in finite 4
- (b) 16 in mod 7
- (c) 39 in finite 12
- (d) 100 in finite 6
- (e) 485 in mod 9

SUBTOPIC: Writing equivalences in finite system

1. Write equivalent numbers of $2(\text{mod } 5)$

$$\underline{\underline{2(\text{mod } 5)} = \{2, 7, 12, 17, 22, 27 \dots\}}$$

2. Write the first 5 equivalent numbers of $7(\text{finite } 9)$

$$\underline{\underline{7(\text{finite } 9)} = \{7, 16, 25, 34, 43\}}$$

3. Write the first eight equivalent numbers of;

- a) 3(finite 5)
- b) 2(finite 9)
- c) 11(finite 12)
- d) 6(finite 9)
- e) 1(finite 5)

SUBTOPIC: Addition of numbers in finite system

Examples:

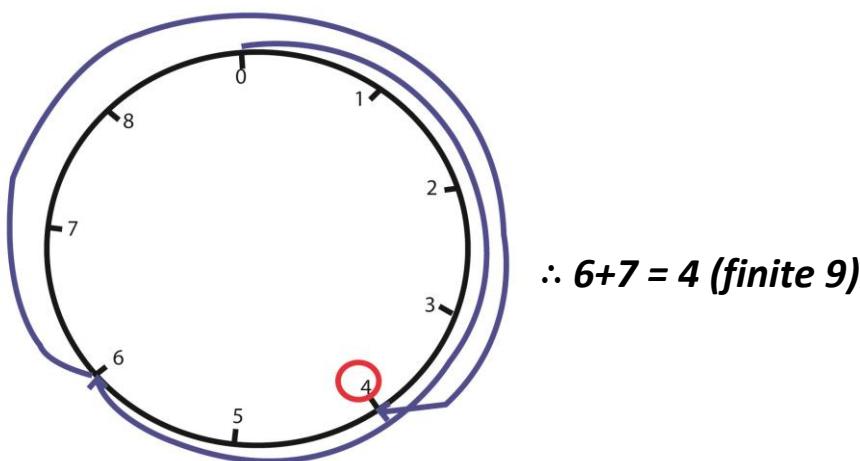
(i) Add: $6 + 7 = \underline{\underline{\quad}}$ (finite 9)

$$6 + 7 = \underline{\underline{\quad}} (\text{finite 9})$$

$$13 \div 9 = 1 \text{ rem } 4 \text{ (finite 9)}$$

$$\therefore \underline{\underline{6 + 7 = 4 \text{ (finite 9)}}}$$

Using a dial / clockface



(ii) Add: $8 + 6 + 3 = \underline{\underline{\quad}}$ (finite 13)

$$(8 + 6) + 3 = \underline{\quad} \text{ (finite 13)}$$

$$17 \div 13 = 1 \text{ rem } 4 \text{ (finite 13)}$$

$$\therefore 8 + 6 + 3 = 4 \text{ (finite 13)}$$

(iii) Workout : $3 + 4 + 5 = x$ (finite 7)

$$x = 3 + 4 + 5 \text{ (finite 7)}$$

$$x = 12 \div 7 \text{ (finite 7)}$$

$$x = 1 \text{ rem } 5 \text{ (finite 7)}$$

$$\underline{x = 5 \text{ (finite 7)}}$$

(iv) Workout the following

- $5 + 8 = \underline{\quad}$ (mod 9)

- $6 + 3 = \underline{\quad}$ (finite 7)

- $2 + 11 + 7 = k \text{ (mod 12)}$

REFERENCE

A New MK Old Edition Pupils Bk 6 Pg 47

SUB TOPIC: SUBTRACTION IN THE FINITE SYSTEM

Workout the following

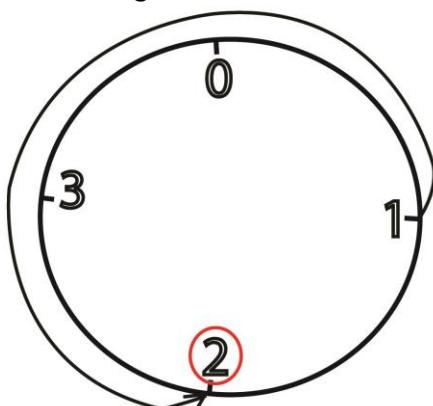
(i) $1 - 3 = \underline{\quad}$ (finite 4)

$$(1 + 4) - 3 = \underline{\quad} \text{ (finite 4)}$$

$$5 - 3 = \underline{2} \text{ (finite 4)}$$

$$\therefore 1 - 3 = 2 \text{ (finite 4)}$$

Using a dial / clock face



$$\therefore 1 - 3 = 2 \text{ (finite 4)}$$

(ii) $2^2 - 5 = \underline{\quad}$ (finite 7)

$$(2 \times 2) - 5 = \underline{\quad} \text{ (finite 7)}$$

$$4 - 5 = \underline{\quad} \text{ (finite 7)}$$

$$4 + 7 - 5 = \underline{\quad} \text{ (finite 7)}$$

$$11 - 5 = 6 \text{ (finite 7)}$$

$$\therefore 2^2 - 5 = 6 \text{ (finite 7)}$$

(iii) $2 - 6 - 4 - 8 = \underline{\quad}$ (finite 9)

- (iv) $10 - 6 = \underline{\hspace{2cm}}$ (mod 12)
 (v) $3 - 6 = \underline{\hspace{2cm}}$ (mod 7)
 (vi) $2 - 49 = \underline{\hspace{2cm}}$ (finite 9)

REFERENCE

A New MK Pupils Bk 7 Pg 48

SUB TOPIC: MULTIPLICATION USING THE FINITE SYSTEM

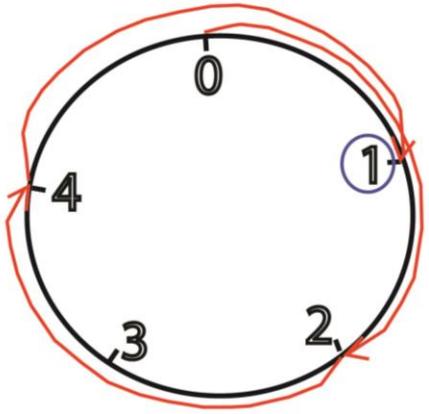
Examples:

Workout the following

(i) $5 \times 7 = \underline{\hspace{2cm}}$ (finite 9)
 $5 \times 7 = \underline{\hspace{2cm}}$ (finite 9)
 $35 \div 9 = 3 \text{ rem } 8$ (finite 9)
 $\therefore 5 \times 7 = 8$ (finite 9)

(ii) $2^3 = \underline{\hspace{2cm}}$ (finite 7)
 $2^3 = 2 \times 2 \times 2$
 $= 4 \times 2$
 $= 8$
 $2^3 = 8 \div 3 = 1 \text{ rem } 1$ (finite 7)
 $2^3 = 1 \text{ rem } 1$ (finite 7)
 $\therefore 2^3 = 1$ (finite 7)

(iii) $3 \times 2 = \underline{\hspace{2cm}}$ (mod 5) using a dial



$\therefore 3 \times 2 = 1$ (mod 5)

- (iv) $4 \times 6 = \underline{\hspace{2cm}}$ (mod 12)
 (v) $3 \times 5 = \underline{\hspace{2cm}}$ (mod 7)
 (vi) $8 \times 9 = \underline{\hspace{2cm}}$ (mod 4)
 (vii) $4 \times 6 = \underline{\hspace{2cm}}$ (mod 9)

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REFERENCE

A New MK Primary Maths Pupils Bk 7 Pg 50

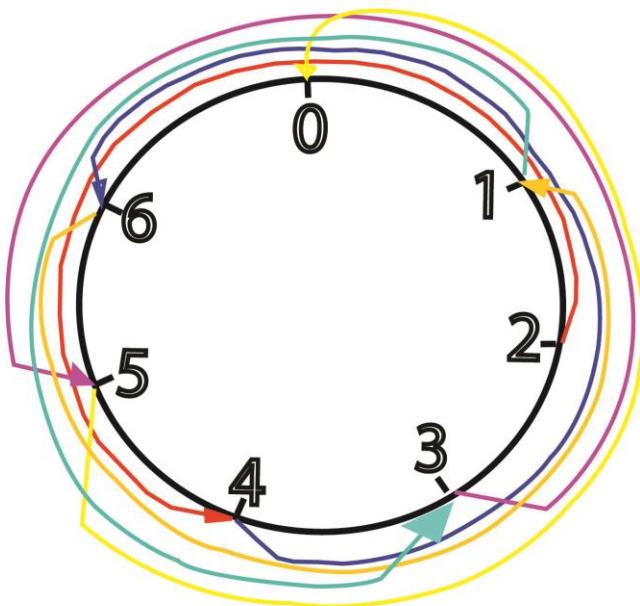
SUB TOPIC: DIVISION IN THE FINITE SYSTEM

Example:

1. Divide $2 \div 5 = \underline{\quad}$ (Mod 7)

$$\begin{aligned}2 \div 5 &= \underline{\quad} (\text{mod } 7) \\2(\text{mod } 7) &= \{2, 9, 16, 23, 30, \dots\} \\30 \div 5 &= 6 (\text{mod } 7) \\ \therefore 2 \div 5 &= 6 (\text{mod } 7)\end{aligned}$$

Using a dial / clock face



2. Work out the following

- (a) $2 \div 6 = \underline{\quad}$ (mod 7)
- (b) $4 \div 6 = \underline{\quad}$ (mod 5)
- (c) $8 \div 11 = \underline{\quad}$ (mod 12)

REFERENCE

A New MK Primary Maths Pupils Bk 7
Maths Revision Hand Book 5, 6 & 7 Pg 35

Mathematics is the KEY

SUB TOPIC: Application of finite 7 in days of the week.

- (i) Today is Thursday, what day of the week will it be 82 days from today?

Thursday stands for 4

$$4 + 82 = \underline{\quad} \text{ (finite 7)}$$

$$86 = \underline{\quad} \text{ (finite 7)}$$

$$86 \div 7 = 12 \text{ rem } 2 \text{ (finite 7)}$$

2 stands for Tuesday

It will be Tuesday

- (ii) Today is Tuesday what day of the week was it 85 days ago.

2 represents Tuesday

$$2 - 85 = \underline{\quad} \text{ (finite 7)}$$

$$85 \div 7 = 12 \text{ rem } 1 \text{ (finite 7)}$$

$$85 = 1 \text{ (finite 7)}$$

$$2 - 1 = 1 \text{ (finite 7)}$$

1 stands for Monday

The day was Monday.

- (iii) Today is Wednesday, what day of the week was it 30 days ago?

- (iv) Today is Saturday, what day of the week will it be after 58 days?

REFERENCE

A New MK Primary Maths Pupils Bk 7 Pg 53

SUB TOPIC: Application of finite 12 in months of the year

Digits representing specific months in the year.

| JAN | FEB | MAR | APRIL | MAY | JUN | JULY | AUG | SEPT | OCT | NOV | DEC |
|------------|------------|------------|--------------|------------|------------|-------------|------------|-------------|------------|------------|------------|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 0 |

Example:

- (i) It is July now, which month of the year will it be after 2132 months?

7 represents July

$$7 + 2132 = \underline{\quad} \text{ (finite 2)}$$

$$2139 = \underline{\quad} \text{ (finite 12)}$$

$$2139 \div 12 = 178 \text{ rem } 3 \text{ (finite 12)}$$

3 stands for March

The month will be March.

- (ii) It is April now, which month of the year was it 346 months ago?

4 stands for April

$$4 - 346 = \underline{\quad} \text{ (finite 12)}$$

$$346 \div 12 = 28 \text{ rem } 10 \text{ (finite 12)}$$

$$346 = 10 \text{ (finite 12)}$$

$$4 - 10 = \underline{\quad} \text{ (fin 12)}$$

$$(4 + 12) - 10 = \underline{\quad} \text{ (finite 12)}$$

$$16 - 10 = 6 \text{ (finite 12)}$$

6 stands for June

$$\begin{array}{r}
 & 28 \\
 12) & 346 \\
 -24 & \downarrow \\
 \hline
 106 \\
 -96 \\
 \hline
 10
 \end{array}$$

The month was June

- (iii) It is March now, which month of the year was it 206 months ago?
- (iv) It is July now, which month of the year will it be after 2890 months?

REFERENCE

A New MK Primary Maths Pupils Bk 7 Pg 54 – 55

SUB TOPIC: Applications of finite 12 in 12 hour clock

NOTE:

When the quotient is odd, the units will change (pm to am, am to pm)

When the quotient is even, the units will not change.

Example:

- (i) It is 7:00 am. What time will it be after nine hours from now?

$$7 + 9 = \underline{\quad} \text{ (finite 12)}$$

$$16 = \underline{\quad} \text{ (finite 12)}$$

$$16 \div 12 = 1 \text{ rem } 4 \text{ (finite 12)}$$

It will be 4:00pm

(It will change to pm if the quotient is an odd number)

- (ii) It is 11:00 pm what time will it be nineteen hours from now?

$$11 + 19 = \underline{\quad} \text{ (finite 12)}$$

$$30 = \underline{\quad} \text{ (finite 12)}$$

$$30 \div 12 = 2 \text{ rem } 6$$

$$11+19 = \underline{6} \text{ (finite 12)}$$

It will be 6:00pm

(it will remain in pm since the quotient is an even number.)

- (iii) Given that time now is 4:00am. What time of the day was it 95 hours ago?
- (iv) Anita travelled for 81 hour after leaving her home at 2:30pm. At what time did she arrive the final destination?
- (v) It is 7:00 am. What time will it be after 9 hours from now?

REFERENCE

A New MK Primary Maths Pupils Bk 7 Pg 55- 56

SUB TOPIC: Applying more than one finite at ago.

Example 1

Find the least number of oranges when divided by 6 or 8, there is always a remainder of 5.

$$4(\text{mod } 8) = \{4, 12, 20, 28, 36, \dots\}$$

$$4(\text{mod } 6) = \{4, 10, 16, 22, 28, 34, \dots\}$$

28 oranges

Example: 2

A Headmaster bought some pens. Teachers grouped them in groups of nines but seven pens were left and when they grouped them in groups of 8, 4 pens were left. When they grouped them in 3's only 1 pen was left. How many pens were bought by the headmaster?

$$7 (\text{finite } 9) = \{7, 16, 25, 34, 43, 52, 61, \dots\}$$

$$4 (\text{finite } 8) = \{4, 12, 20, 28, 36, 44, 52, 60, \dots\}$$

$$1 (\text{finite } 3) = \{1, 4, 7, 10, 13, 16, 19, 22, 25, 28, 31, 34, 37, 40, 43, 46, 49, 52, 55, \dots\}$$

The headmaster bought 52 pens.

Try these

- π A P.7 class teacher 2018 arranged his candidates in groups of 8, 6 remained when he grouped them in 11, only 2 remained and when he grouped them in 5, 1 pupil remained. How many candidates are in P.7 2018?
- π Find the least number of fruits when shared by 15 pupils or 18 pupils there is always a remainder of 3 fruits

REFERENCE

A New MK Primary Maths Pupils Bk 7 Pg 57

SUB TOPIC: SOLVING EQUATIONS USING THE FINITE SYSTEM

Examples:

$$\begin{aligned} \text{(i)} \quad x - 4 &= 3 \pmod{7} \\ x - 4 + 4 &= 3 + 4 \pmod{7} \\ x + 0 &= 7 \pmod{7} \\ x &= 7 \div 7 \pmod{7} \\ x &= 1 \text{ rem } 0 \pmod{7} \\ \underline{x = 0 \pmod{7}} \end{aligned}$$

$$\begin{aligned} \text{(ii)} \quad m + 4 &= 3 \pmod{5} \\ m + 4 - 4 &= 3 - 4 \pmod{5} \\ m + 0 &= (3 + 5) - 4 \pmod{5} \\ m &= 8 - 4 \pmod{5} \\ \underline{m = 4 \pmod{5}} \end{aligned}$$

(iii) $2x - 3 = 3$ (finite 4)
 ~~$2x - 3 + 3 = 3 + 3$ (finite 4)~~
 ~~$2x + 0 = 6$ (finite 4)~~
 ~~$\underline{2} \quad \underline{2}$~~
 ~~$x = 3$ (finite 4)~~

(iv) $2(2x - 1) = 4$ (finite 7)
 ~~$2 \times 2x - 1 \times 2 = 4$ (finite 7)~~
 ~~$4x - 2 = 4$ (finite 7)~~
 ~~$4x - 2 + 2 = 4 + 2$ (finite 7)~~
 ~~$4x = 6$ (finite 7)~~
 ~~$4x = 6 + 7$ (finite 7)~~
 ~~$4x = 13 + 7$ (fin 7)~~

$$\frac{4x}{4} = \frac{20^5}{4_1}$$

 ~~$X = 5$~~

Try these

Solve the following

- (a) $p + 2 = 4$ (finite 5)
- (b) $3(m - 2) = 1$ (finite 5)
- (c) $\frac{3y + 6}{5} = 2$ (finite 5)
- (d) $2(2k - 1) = 4$ (mod 7)
- (e) $3y = 4$ (finite 7)

REFERENCE

A New MK Primary Maths Pupils Bk 7 Pg 49 - 50

TOPICAL TEST

- ii. Find the additive inverse of the following
 - a) -5
 - b) 4
 - c) -12
- iii. Work out the following without a number line
 - a) $-6 + -2$
 - b) $+5 - 6$
 - c) -3×-5
- iv. Workout the following using a number line
 - a) $-4 + +5$
 - b) $6 - -3$
 - c) $+3 \times -4$

- v. Evaluate $33 = \underline{\hspace{2cm}}$ (mode 7)
- vi. Write the equivalent numbers of 3(finite 5)
- vii. Simplify: $2 - 4 = \underline{\hspace{2cm}}$ (finite 5)
- viii. Simplify : $5 \times 6 = \underline{\hspace{2cm}}$ (finite 7)
- ix. Solve (i) $y - 5 = 4$ (finite 5)
 (ii) $2(x - 2) = 3$ (finite 6)
- x. Divide $1 \div 5 = \underline{\hspace{2cm}}$ (finite 6)
- xi. Today is Tuesday. What day of the week will it be after 46 days?
- xii. Today is Friday. What day of the week was it 37 days ago?
- xiii. A Plane left Entebbe airport at 1100 hours and arrived at New Park after 27 hours. At what time did it arrive?. (Give your answer in 24 hour clock).
- xiv. Find the least number when divided by 12 or 15 leaves 6 as a remainder.

DATA HANDLING

SUB TOPIC: PICTO GRAPHS(review)

Definition:

A pictograph is where we use pictures to represent quantities of actual items.

Example:

The graph below shows the number of books that were given to different schools.

| | |
|-----------------|--|
| Kyengera P/s | |
| Nakasero P/S | |
| Mengo P/s | |
| Old Kampala P/s | |
| Winston P/s | |

Given that stands for 100 books and for 50 books.

- (a) How many more books did Mengo pupils get than Kyengera?
 4×100
400 books
- (b) Which school had the maximum number of books?
Winston p/s

- (c) Find the total number of books that were given out to the five schools.

$$15 \times 100$$

1500 books

- (d) Calculate the average number of books that were distributed to the five schools.

$$\begin{aligned}\text{Average} &= \frac{\text{sum of items}}{\text{number of items}} \\ &= \frac{1500}{5} \\ &= \underline{\underline{300 \text{ books}}}\end{aligned}$$

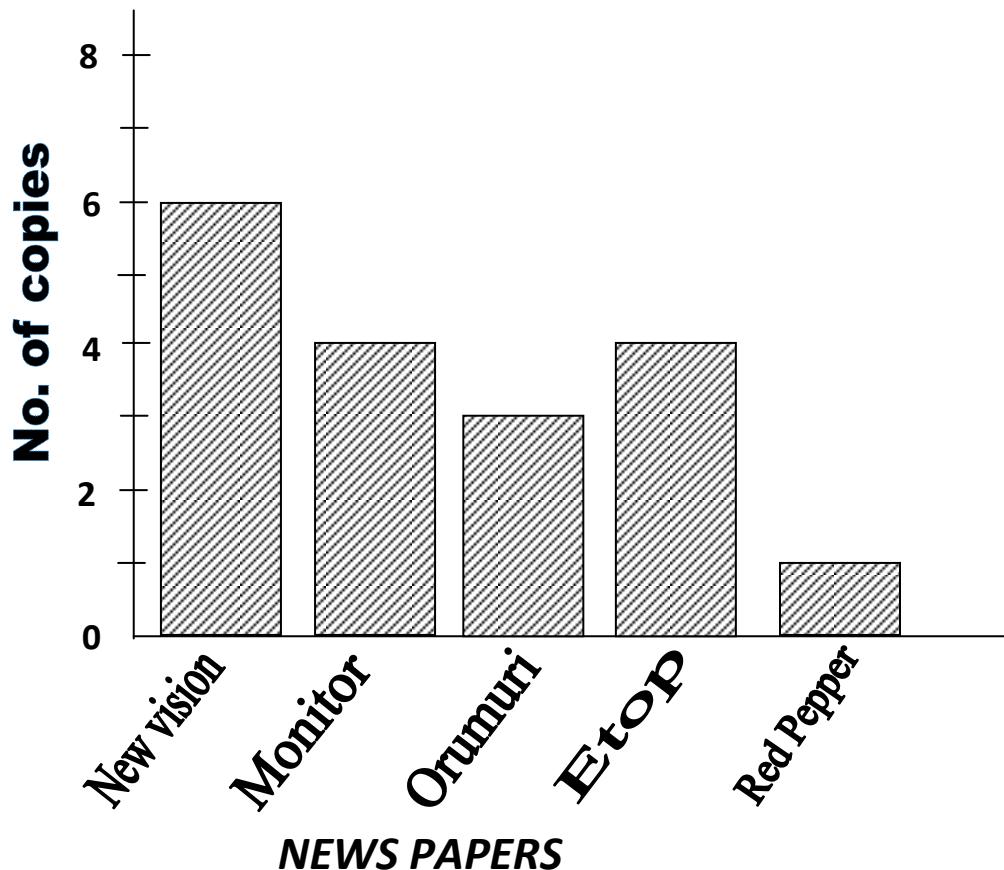
REFERENCE

A New MK Primary Mathematics Bk 7

SUB TOPIC: BAR GRAPHS(review)

Example:

The bar graph represents the copies of Newspapers which were sold to the Education Manager's office on a certain day. Use it to answer the questions that follow:



- (a) Which Newspaper was sold in the biggest number?

New vision

- (b) How many copies were sold altogether?

$$6 + 4 + 3 + 4 + 1$$

18 copies

Mathematics is the Key

(c) Which newspaper was sold in the least number ?

Red pepper

(d) How many more copies of New Vision were sold than the Red Pepper?

$$6 - 1 = 5 \text{ more copies}$$

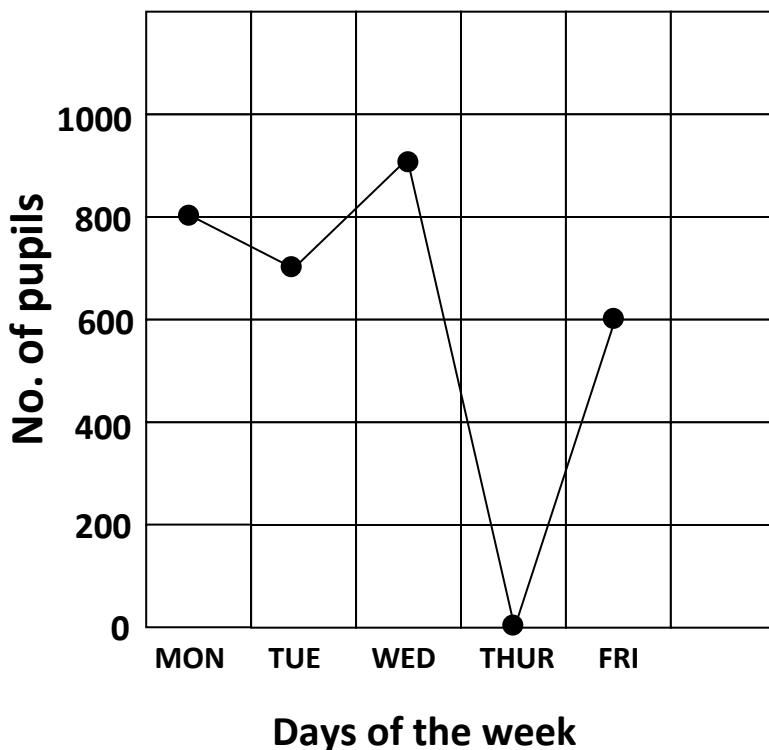
REFERENCE

A New MK Primary Mathematics Bk 7

SUB TOPIC: LINE GRAPHS(review)

Example 1:

The graph represents the schools' daily attendance for a week. Use the information on the graph to make a table showing the daily attendance.



Questions

(i) On which day was the attendance high?

On Wednesday

(ii) On which day was the attendance 600?

On Friday

(iii) How many pupils attended on Tuesday?

700 pupils

(iv) What was the average attendance that week?

$$\begin{aligned}\text{Average} &= \frac{\text{sum of items}}{\text{number of items}} \\ &= \frac{800+700+900+0+600}{5}\end{aligned}$$

Mathematics is the Key

$$\begin{array}{r}
 3000 \\
 - 5 \\
 \hline
 = 600 \text{ pupils}
 \end{array}$$

- (v) How many more pupils attended on Wednesday than Tuesday?
 $900 - 700 = 200 \text{ more pupils}$

REFERENCE

A New MK Primary Mathematics Bk 7 exercise 10:4 Pg 150

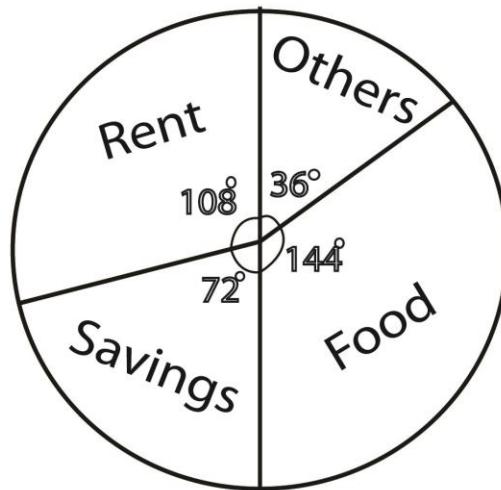
SUB TOPIC: PIE CHARTS INVOLVING DEGREES

REMEMBER:

Angles in all sectors of a pie chart add up to 360°

Example:

1. The pie chart below shows the monthly expenditure and savings of Mr. Mugisha who earns sh.72,000



- (a) How much does he spend on each item?

Savings

$$\frac{72^\circ}{360^\circ} \times \text{sh. } 72,000$$

$$72 \times \text{sh. } 200$$

$$\underline{\text{Sh. } 14,400}$$

Rent

$$\frac{108^\circ}{360^\circ} \times \text{sh. } 72,000$$

$$108 \times \text{sh. } 200$$

$$\underline{\text{Sh. } 21600}$$

Food

$$\frac{144^\circ}{360^\circ} \times \text{sh. } 72,000$$

$$144 \times \text{sh. } 200$$

$$\underline{\text{Sh. } 28,800}$$

Others

$$\frac{36^\circ}{360^\circ} \times \text{sh. } 72,000$$

$$\underline{\text{Sh. } 7,200}$$

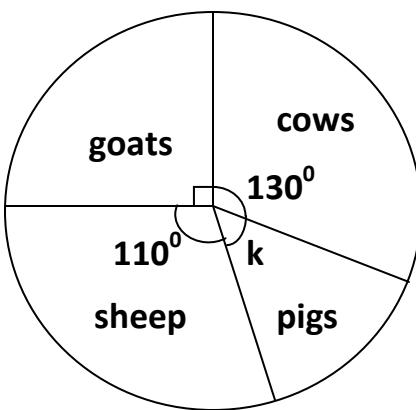
- (b) Change the sector angle for others and percentages.

$$\frac{36^\circ}{360^\circ} \times 100\%$$

$$\underline{10\%}$$

Mathematics is the key

2. The pie chart below shows how 72 animals are distributed on Mr. Kato's farm. Use it to answer the questions that follow.



- (a) Find the value of k

$$k + 110^\circ + 130^\circ + 90^\circ = 360^\circ$$

$$k + 330^\circ = 360^\circ$$

$$k + 330^\circ - 330^\circ = 360^\circ - 330^\circ$$

$$\underline{k = 30^\circ}$$

- (b) How many cows are on the farm?

$$\frac{130^\circ}{360^\circ} \times 72$$

$$\frac{13}{36} \times 72$$

$$13 \times 2$$

26 cows

- (c) How many more sheep than goats are on the farm?

$$110^\circ - 90^\circ = 20^\circ$$

$$\frac{20^\circ}{360^\circ} \times 72$$

$$\frac{2}{36} \times 72$$

$$2 \times 2$$

4 more sheep

- (d) Express the sector angle for goats as a percentage.

$$\frac{90^\circ}{360^\circ} \times 100\%$$

$$\frac{1}{4} \times 100\%$$

$$25\%$$

(e) What is the ratio of cows to pigs?

$$\frac{130^\circ}{30^\circ} = \frac{13}{3}$$

13:3

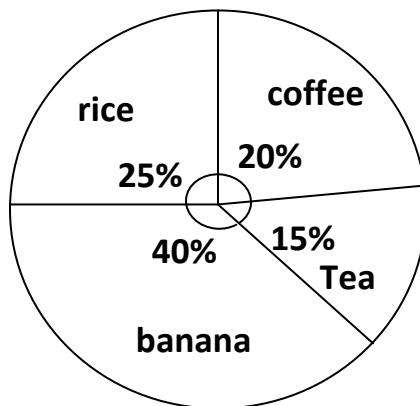
SUB TOPIC: PIE CHARTS INVOLVING PERCENTAGES

REMEMBER:

Percentages in all sectors of the pie chart add up to 100%

Examples

4. Study the pie chart below which shows how 60 acres of land were cultivated



- a. What area of the land was used for Tea planting?

$$\frac{15}{100} \times 60 \text{ acres}$$

$$\frac{3}{2} \times 6$$

$$3 \times 3$$

9 acres

- b. What area of the land was used for coffee planting?

$$\frac{20}{100} \times 60 \text{ acres}$$

$$2 \times 6$$

12 acres

- c. What area of the land was used for rice planting?

$$\frac{25}{100} \times 60 \text{ acres}$$

$$\frac{5}{2} \times 6$$

$$5 \times 3$$

15 acres

- d. Express the area of land for banana planting as a fraction

$$\frac{40}{100}$$

$$\frac{4}{10}$$

$$\frac{2}{5}$$

- e. How many more acres of land were used for banana planting than tea planting?

$$40\% - 15\% = 25\%$$

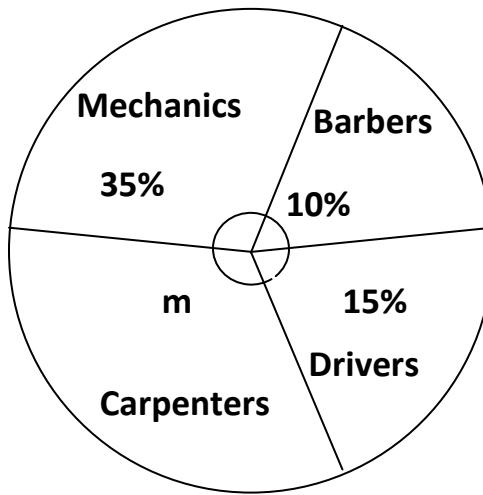
$$\frac{25}{100} \times 60 \text{ acres}$$

$$\frac{5}{2} \times 6$$

$$5 \times 3$$

15 more acres

5. The pie chart below shows how the COVID-19 task force of a certain district shared 40,000kg of posho flour to different groups of people who were stopped from working. Use it to answer the questions that follow.



- a. Find the value of m

$$m + 10\% + 35\% + 15\% = 100\%$$

$$m + 60\% = 100\%$$

$$m + 60\% - 60\% = 100\% - 60\%$$

$$m = 40\%$$

- b. How many kilograms of posho were given to drivers?

$$\frac{15}{100} \times 40,000\text{kg}$$

$$15 \times 400\text{kg}$$

$$60,000\text{kg}$$

c. How many more kilograms of posho were given to carpenters than barbers?

$$40\% - 10\% = 30\%$$

$$\frac{30}{100} \times 40,000\text{kg}$$

$$30 \times 400$$

$$12,000\text{kg}$$

d. What is the ratio of the mechanics' share to the total share?

$$\frac{35}{100}$$

$$\frac{7}{20}$$

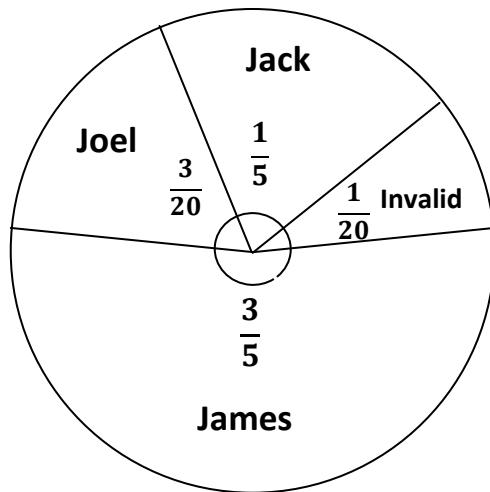
$$7:20$$

SUB TOPIC: PIE CHARTS INVOLVING FRACTIONS

REMEMBER:

Fractions in all the sectors add up to 1 whole.

- The pie chart below shows how three boys got their votes in Boona fm p/s given that 720 votes were cast altogether. Use it to answer the questions that follow.



- How many votes did James get?

$$\frac{3}{5} \times 720$$

$$3 \times 144$$

$$432 \text{ votes}$$

- How many votes did Jack get?

$$\frac{1}{5} \times 720$$

$$1 \times 144$$

$$144 \text{ votes}$$

- How many votes were invalid?

$$\frac{1}{20} \times 720$$

$$1 \times 36$$

36 votes

(d) How many more votes did James get than Joel?

Joel

$$\frac{3}{20} \times 720$$

$$3 \times 36$$

108 votes

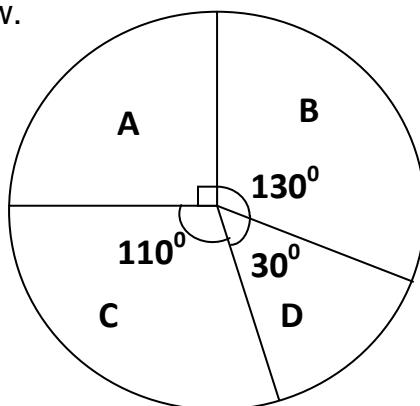
$$\underline{432 \text{ votes} - 108 \text{ votes} = 324 \text{ more votes}}$$

(e) Who won the election?

James

SUB TOPIC: SOLVING PROBLEMS INVOLVING PIE-CHARTS

- Study the pie-chart below which shows the number of COVID-19 testing kits that were distributed in different countries in 2020 and use it to answer the questions that follow.



- How many kits were distributed altogether if country D got 15 million kits?

let the total number of kits be P

$$\frac{30^\circ}{360^\circ} \times P = 15,000,000$$

$$\frac{36}{3} \times \frac{3P}{36} = 15,000,000 \times \frac{36}{3}$$

$$P = 15,000,000 \times 12$$

$$\underline{P = 180,000,000 \text{ kits}}$$

- How many kits were distributed to country B?

$$\frac{130^\circ}{360^\circ} \times 180,000,000 \text{ kits}$$

$$130 \times 500000$$

65,000,000 kits

(c) How many more kits were distributed to country C than country A?

$$110^\circ - 90^\circ = 20^\circ$$

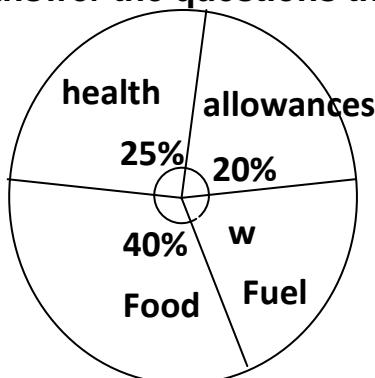
$$\frac{20^\circ}{360^\circ} \times 180,000,000 \text{ kits}$$

$$20 \times 500000$$

10,000,000 more kits

Your turn

The pie chart below shows how the District COVID-19 task force distributed money. Use it to answer the questions that follow.



- (a) Find the value of w.
- (b) Find the total amount of money distributed if sh.60m was given the health sector.
- (c) Find the amount of money for food?
- (d) How much money was paid to the workers as allowances?
- (e) Express the amount of money for fuel as a fraction.

SUB TOPIC: CONSTRUCTION OF PIE-CHARTS

The table below shows how Allen spent her money on the first day of the term

| Item | Money |
|--------------|-----------|
| Books | sh.8,000 |
| Pens | Sh.4,000 |
| Pads | Sh.6,000 |
| Pocket money | Sh.12,000 |

Construct a pie chart using a radius of 3.5cm showing the above information

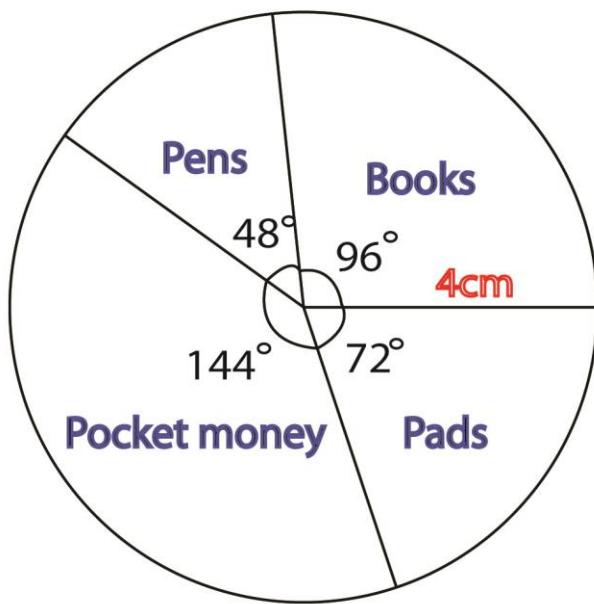
Total

$$\text{sh. } 8,000 + \text{sh. } 4,000 + \text{sh. } 6,000 + 12,000 = \text{sh. } 30,000$$

| Books | Pens | Pads | Pocket money |
|---|--|--|---|
| sh. 8,000 | sh. 4000 | sh. 6000 | sh. 12000 |
| $\frac{\text{sh. } 8,000}{\text{sh. } 30,000} \times 360^\circ$ | $\frac{\text{sh. } 4000}{\text{sh. } 30,000} \times 360^\circ$ | $\frac{\text{sh. } 6000}{\text{sh. } 30,000} \times 360^\circ$ | $\frac{\text{sh. } 12000}{\text{sh. } 30,000} \times 360^\circ$ |
| $8 \times 12^\circ$ | $4 \times 12^\circ$ | $6 \times 12^\circ$ | $12 \times 12^\circ$ |
| 96° | 48° | 72° | 144° |

check

$$96^\circ + 48^\circ + 72^\circ + 144^\circ = 360^\circ$$



2. Waswa spent $\frac{1}{3}$ of his money on books and $\frac{1}{6}$ of the remainder on transport and the rest as pocket money.

- (i) What fraction of his money was left for pocket money?

$$\text{Fraction spent on books} = \frac{1}{3}$$

$$\text{Remaining fraction: } 1 - \frac{1}{3} = \frac{3}{3} - \frac{1}{3} = \frac{2}{3}$$

$$\begin{aligned}\text{Fraction spent on transport: } &\frac{1}{6} \text{ of } \frac{2}{3} = \frac{1}{6} \times \frac{2}{3} \\ &= \frac{1}{9}\end{aligned}$$

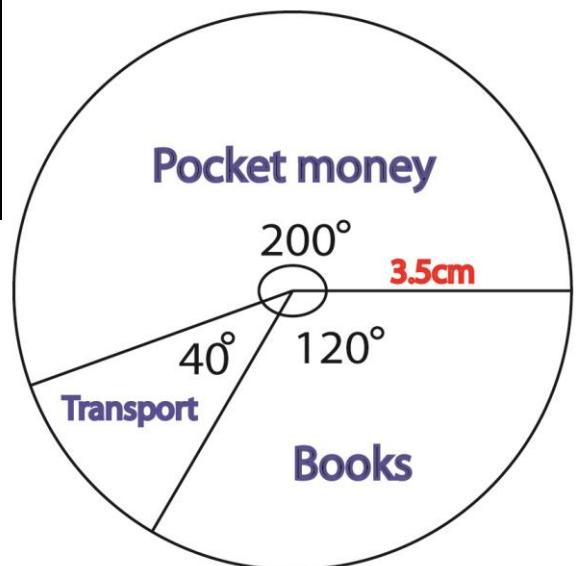
$$\text{transport and books: } \frac{1}{3} + \frac{1}{9}$$

$$\frac{1}{3} \times \frac{3}{3} + \frac{1}{9} = \frac{3}{9} + \frac{1}{9} = \frac{4}{9}$$

$$\text{Remained fraction} = 1 - \frac{4}{9} = \frac{9}{9} - \frac{4}{9} = \frac{5}{9}$$

- (ii) Using a radius of 4cm, construct a pie chart showing the information

| Books | Transport | Pocket money |
|--|---------------------------------------|---|
| $\frac{1}{3} \times 360^\circ$ 120° | $\frac{1}{9} \times 360^\circ$ 40° | $\frac{5}{9} \times 360^\circ$ $5 \times 40^\circ$ 200° |



1. In a certain town, 40% of the population are Baganda, 10% are Basoga, 30% are Bagisu and the rest are Acholi. Draw an accurate pie-chart for the above information.

2. Nambooze spends her monthly salary as follows ;

sh. 12,000 on school fees

sh. 6000 on transport and

sh. 18,000 on food

Draw an accurate pie chart for this information

3. On Adam's farm there are 9 goats, 6 cows, 3 pigs and 7 sheep. Using a radius of 4 cm, construct an accurate pie chart.

4. Father shared his land as follows

$\frac{1}{3}$ to the first born

$\frac{2}{9}$

$\frac{1}{9}$ to the second born

$\frac{1}{9}$

$\frac{1}{9}$ to the last born

$\frac{1}{9}$

The rest to the wife

Use the information to construct a pie chart

5. In a certain town, 40% of the population are Baganda, 10% are Basoga, 30% are Bagisu and the rest are Acholi. Draw an accurate pie-chart for the above information

6. Nambooze spends her monthly salary as follows ;

sh. 12,000 on school fees

sh. 6000 on transport and

sh. 18,000 on food

Draw an accurate pie chart for this information

REFERENCES

Fountain primary maths Book 7 pages 177 to 198

MK Book 7 pages 164 to 188

SUB TOPIC: Measures of central tendency and range (STATISTICS)

NOTE THESE:

❖ Mode

The most frequent value in an observation.

❖ Model frequency

The number of times the mode appear.

❖ Median

This is the middle number got after arranging in either ascending or descending order

❖ **Mean / Average**

The measure of central tendency of a set of values computed by dividing the sum of the values by their number.

❖ **Range**

The difference between the smallest and the largest observation in a sample

❖ **Frequency**

The number of times an event appears in an experiment.

Example:

- Amuza scored the following marks in MID term exams

SST – 60

MTC – 85

ENG – 82

SCI – 60

RE – 53

- Calculate his mode

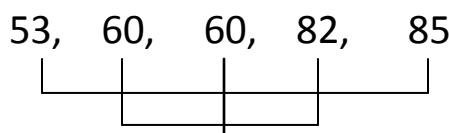
| Marks | Freq |
|-------|------|
| 85 | 1 |
| 82 | 1 |
| 60 | 2 |
| 53 | 1 |

$$\text{Mode} = 60$$

- Find his range

$$\begin{aligned}\text{Range} &= H - L \\ &= 85 - 53 \\ &= 32\end{aligned}$$

- What is his median mark?



$$\text{Median} = 60$$

- Find his mean mark

$$\begin{aligned}\text{Mean} &= \frac{\text{sum of items}}{\text{no. of items}} \\ &= \frac{53 + 60 + 60 + 82 + 85}{5} \\ &= \frac{340}{5} \\ &= 68\end{aligned}$$

2. The table below represents the goals scored by different teams.

| | | | | | |
|-----------------|---|---|---|---|----|
| Goals scored | 2 | 3 | 6 | 7 | 10 |
| Number of teams | 4 | 1 | 2 | 1 | 2 |

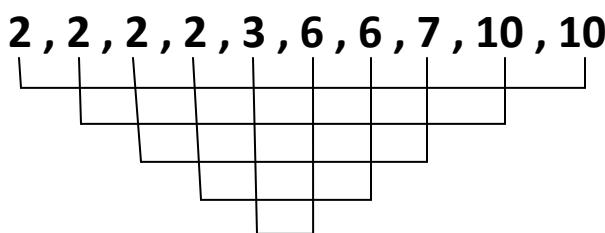
- (a) Find the mode.

2 goals

- (b) What was the modal frequency?

4

- (c) Calculate the median



$$\text{Median} = \frac{3 + 6}{2}$$

$$= \frac{9}{2}$$

$$\underline{\underline{= 4.5}}$$

- (d) Calculate the mean

$$\begin{aligned} \text{Mean} &= \frac{SI}{NI} \\ &= \frac{2 \times 4 + 3 + 6 \times 2 + 7 + 10 + 10}{4+1+2+1+2} \\ &= \frac{50}{10} \\ &= 5 \end{aligned}$$

3. Find the medium of the following scores 3, 1, 2, 0, 6, 1, 4

4. The table below shows the performance of pupils in a P.7 class in mathematics exam.

| | | | | | | | | |
|-------|-----|----|----|----|----|----|----|----|
| Marks | 100 | 90 | 80 | 70 | 60 | 50 | 40 | 30 |
| Freq | 0 | 2 | 1 | 1 | 6 | 4 | 4 | 2 |

- (a).How many pupils are in P.7 class?

- (b).What was the highest mark obtained in this exam?

- (c).Workout the range

- (d)Calculate the average mark.

SUB TOPIC:COMPLEX AVERAGE/INVERSE OF AVERAGE

Examples

1. The average of 4 boys in a group is 12 years. A young boy of 7 years joined the group. Find the average age of the 5 boys.

$$\text{Mean} = \frac{\text{Total}}{\text{Number of boys}}$$

$$\begin{aligned}\text{Total age} &= \text{Mean age} \times \text{number of boys} \\ &= 12 \times 4 \\ &= \underline{\underline{48 \text{ years}}}\end{aligned}$$

$$\begin{aligned}\text{Mean age of 5 boys} &= \frac{\text{Sum of ages}}{\text{Number of boys}} \\ &= \frac{48 + 7}{5} \\ &= 55 \\ &= \underline{\underline{11 \text{ years}}}\end{aligned}$$

2. The average weight of 6 pupils is 30kg. when the teacher joins them, their average becomes 36kg. Find the weight of the teacher.

$$\underline{\underline{\text{total weight of 6 pupils}}}$$

$$\begin{aligned}\text{Total weight} &= \text{Mean} \times \text{number} \\ &= 30 \times 6 \\ &= \underline{\underline{180 \text{ kg}}}\end{aligned}$$

$$\underline{\underline{\text{Total weight of 6 pupils and the teacher}}}$$

$$\begin{aligned}\text{Total weight} &= \text{Mean} \times \text{number} \\ &= 36 \times 7 \\ &= \underline{\underline{252 \text{ kg}}}\end{aligned}$$

$$\underline{\underline{\text{weight of the teacher}}}$$

$$252\text{kg} - 180\text{kg} = 72\text{kg}$$

Try these

1. The average mark of 36 pupils in a class is 5. Two pupils whose marks are 20 and 24 leave the group. Find the average mark of the remaining pupils.
2. The mean age of 5 children is 12years, if a sixth child joins them, the mean age becomes 11years, find the age of the 6th child.

Mathematics is the key

3. The average weight of 6 pupils is 40kg; the average weight of other 4 pupils is 30kg.

Find the average weight of all the pupils

SUB TOPIC: FINDING MISSING NUMBERS WHEN GIVEN AVERAGE

3. The table below shows the marks obtained by some pupils in a test. Use the information to answer the questions that follow.

| | | | | |
|------------------|----|---|----|----|
| Marks | 40 | m | 60 | 70 |
| Number of pupils | 2 | 6 | 3 | 3 |

If the mean mark is 55, find the value of m

$$\text{Mean} = \frac{\text{sum of items}}{\text{number of items}}$$
$$\frac{40 \times 2 + m \times 6 + 60 \times 3 + 70 \times 3}{2 + 6 + 3 + 3} = 55$$
$$\frac{80 + 6m + 180 + 210}{14} = 55$$
$$14 \times \frac{6m + 470}{14} = 55 \times 14$$
$$6m + 470 = 770$$
$$6m + 470 - 470 = 770 - 470$$
$$6m = 300$$
$$\frac{6m}{6} = \frac{300}{6}$$
$$\underline{\underline{m = 50}}$$

Example 3

The mean of $y + 1$, 5 and y is 6. Find the value of y .

$$\frac{(y + 1) + 5 + y}{3} = 6$$
$$\frac{y + y + 5}{3} = 6$$
$$3 \times \frac{2y + 6}{3} = 6 \times 3$$
$$2y + 6 = 6 \times 3$$
$$2y + 6 - 6 = 18 - 6$$
$$\frac{2y}{2} = \frac{12}{2}$$
$$\underline{\underline{y = 6}}$$

Try these

1. The table below represents the goals scored by different teams.

| | | | | | |
|--------------|---|---|---|---|----|
| Goals scored | 2 | 3 | k | 7 | 10 |
| No. of teams | 4 | 1 | 2 | 1 | 2 |

Mathematics is the Key

- (a) Find the value of k if the mean number of goals is 5
 - (b) Find the modal number of goals.
 - (c) What was the modal frequency?
 - (d) Calculate the median
2. The average of a, a-7, 3 and 2a is 8. Find the value of a.

EVALUATION ACTIVITY:

Macmillan Primary Maths Bk 7 Pg 148

SUB TOPIC: PROBABILITY

Probability is a measure of the likelihood of an event happening. Probability ranges from 0 to 1

REMEMBER

Probability of zero (0) means that there is no chance at all.

Probability that is less than a half means that it is a bad chance.

Probability that is a half means that the chances are 50 50.

Probability that is greater than a half means that it is a good chance.

Probability of one (1) means that you have all chances

$$\text{Probability} = \frac{\text{number of events}}{\text{sample space}}$$

Example: A basket has 2 ripe mangoes and 6 raw mangoes. What is the probability of Twaha picking a ripe mango at random?

: $\text{Probability} = \frac{\text{number of events}}{\text{sample space}}$

$$n(E) = 2$$

$$\text{Total chances (SS)} = 2 + 6 = 8$$

$$\text{Probability} = \frac{2}{8}$$

Try these

1. What is the probability that a baby will be produced by a pregnant mother?
2. The probability that Peter will pass his examinations is $\frac{2}{7}$. What is the probability that he will not pass his examinations?
3. In a tin there are 30 blue and red pens. If the probability of picking a red pen is $\frac{8}{5}$, how many red pens are in the tin?
4. In a football match a team will either win, draw or lose a game.
 - (a) What is the probability that a team wins the game?
 - (b) Find the probability that a team draws the match.
 - (c) What is the probability of a team losing a match?

SUB TOPIC: TOSSING A COIN OR A DICE

Example 1:

If a coin is tossed once, what is the probability of getting a head on the top?

Total chances = {H, T}

Number of possible outcomes (SS) = 2

Expected outcomes = {H}

$$n(E) = 1$$

$$\text{Probability} = \frac{n(E)}{SS}$$
$$= \underline{\underline{\frac{1}{2}}}$$

Example 2:

When a die is rolled once, what is the probability of getting an even number on top?

Probability space = {all expected outcomes}

$$\{1, 2, 3, 4, 5, 6\}$$

$$(s.s) = 6$$

Expected outcomes = {all desired chances}

$$(E) = \{2, 4, 6\}$$

$$n(E) = 3$$

$$\text{Probability} = \frac{n(E)}{SS} = \frac{3}{6}$$

Try these

1. A coin is tossed once. What is the probability of getting ;
 - (a) A head on top
 - (b) A tail on top
 - (c) A head or a tail on top
2. A dice is tossed once. What is the probability of getting;
 - (a). an even number on top.
 - (b). a prime number on top.
 - (c). a number less than five on top

REFERENCE

A New MK Primary Bk 7 Page 189

Mathematics is the key

SUB TOPIC: COORDINATE GRAPHS

1. Plot the following points on a grid

A (-1, 4) B(5, 4) C(5, 0) D(-1, 0)

Join the points name the figure formed and find its area.

Rectangle

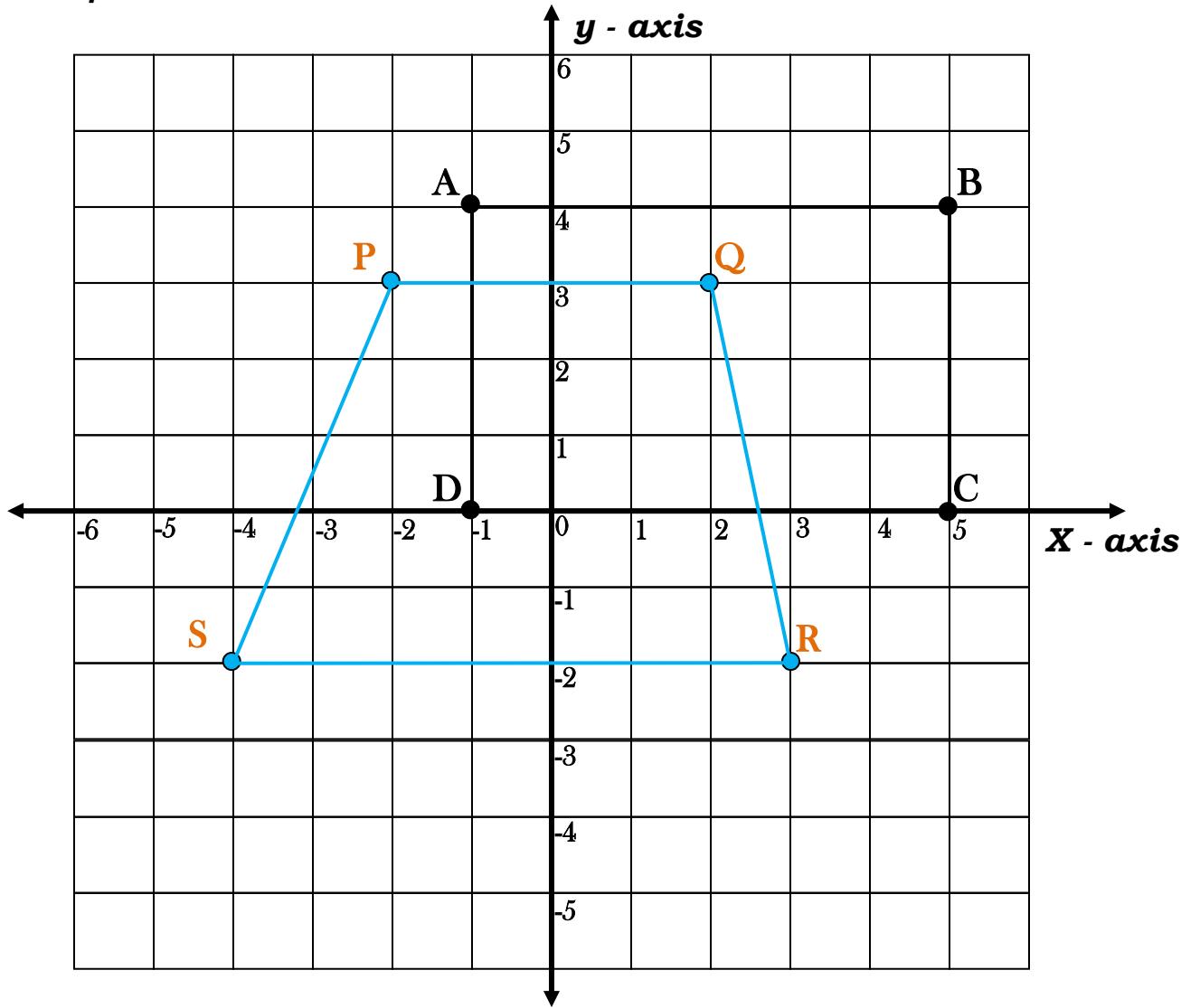
Area = 6×4

= 24 square units

2. Plot the following **P (-2, 3)** **Q(2, 3)** **R(3, -2)** **S(-4, -2)**

Join the points and name the figure formed.

Trapezium



REFERENCE

A New MK Primary Mathematics Bk 7

SUB TOPIC: GRAPHS OF EQUATIONS

Completing tables using equations of lines

Example:

- Given that $x = y$. Complete the table.

| | | | | | | | | |
|---|----|----|---|---|---|---|---|---|
| X | -2 | -1 | 0 | 1 | 2 | 3 | 4 | 5 |
| Y | -2 | -1 | 0 | 1 | 2 | 3 | 4 | 5 |

2. Given that $2x = y$. Complete the table below

| | | | | | |
|---|-----|-----|---|---|---|
| X | - 4 | - 2 | 0 | 2 | 4 |
| Y | - 2 | - 1 | 0 | 1 | 2 |

3. Given that $Y = 2x - 1$ Complete the table.

$$Y = 2x - 1$$

$$Y = 2x - 2 - 1$$

$$Y = -4 - 1$$

$$\underline{\underline{Y = -5}}$$

$$Y = 2x - 1$$

$$Y = 2x 0 - 1$$

$$Y = 0 - 1$$

$$\underline{\underline{Y = -1}}$$

$$Y = 2x - 1$$

$$Y = 2x 2 - 1$$

$$Y = 4 - 1$$

$$\underline{\underline{Y = 3}}$$

$$Y = 2x - 1$$

$$Y = 2x - 1 - 1$$

$$Y = -2 - 1$$

$$\underline{\underline{Y = -3}}$$

$$Y = 2x - 1$$

$$Y = 2x 1 - 1$$

$$Y = 2 - 1$$

$$\underline{\underline{Y = 1}}$$

$$Y = 2x - 1$$

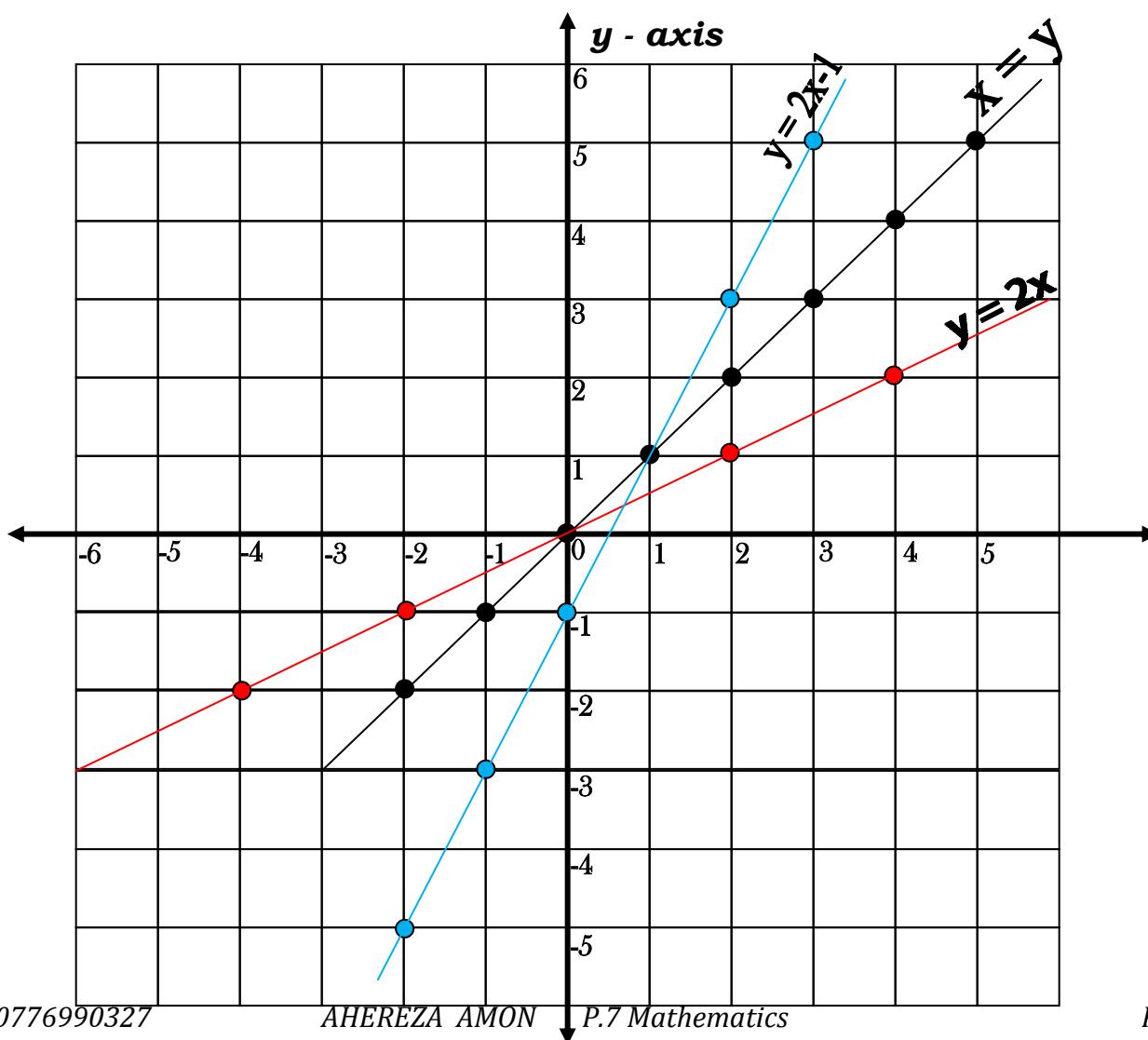
$$Y = 2x 3 - 1$$

$$Y = 6 - 1$$

$$\underline{\underline{Y = 5}}$$

| | | | | | | |
|---|-----|-----|-----|---|---|---|
| X | - 2 | - 1 | 0 | 1 | 2 | 3 |
| Y | - 5 | - 3 | - 1 | 1 | 3 | 5 |

- (a) Plot lines for the equation above .



4. Complete the table $y = 3x - 5$

| | | | | | |
|---|---|----|---------------|----|---|
| X | 4 | — | $\frac{1}{3}$ | — | 3 |
| Y | — | -2 | — | -8 | — |

5. $3x + y = 5$ Complete the table

| | | | | | | |
|---|---|---|---|---|---|---|
| X | 0 | 1 | 2 | — | 6 | — |
| Y | 5 | — | — | 7 | — | 3 |

REFERENCE

A New MK Primary Mathematics Bk 7

SUB TOPIC: FORMING EQUATIONS OF LINES FROM ORDERED PAIRS

Example:

1. Line A in the graph passes through (-3,-3), (-2, -2) (-1, -1), (0, 0), (1, 1), (2, 2), (3, 3)

The table shows the x and y coordinates from line A.

| | | | | | | | |
|---|----|----|----|---|---|---|---|
| X | -3 | -2 | -1 | 0 | 1 | 2 | 3 |
| Y | -3 | -2 | -1 | 0 | 1 | 2 | 3 |

In comparison x co - ordinates are equal to the y coordinates

$$y = x$$

The equation of line A is $y = x$

2. Line B passes through (-3, -2), (-2, -1), (-1, 0), (0, 1), (1, 2), (2, 3), (3, 4), etc

| | | | | | | | |
|---|----|----|----|---|---|---|---|
| X | -3 | -2 | -1 | 0 | 1 | 2 | 3 |
| Y | -2 | -1 | 0 | 1 | 2 | 3 | 4 |

$$Y = x + 1$$

$$-2 = -3 + 1$$

$$-1 = -2 + 1$$

$$0 = -1 + 1$$

$$1 = 0 + 1$$

$$2 = 1 + 1$$

$$3 = 2 + 1$$

The equation for line B is $y = x + 1$

REFERENCE

MK Bk 7 Pg 185

Mathematics is the Key

TOPICAL EXERCISE ON GRAPHS

1. Hamisa kept the following daily record of the number of people who visited their home in a week: 3, 5, 3, 2, 0, 3, 5. Find the mean.
2. A die is rolled once. What is the probability that a composite number will show on top?
3. The average height of Peter, James and John is 51cm. If the height of Peter is 53cm and that of James is 46cm Find the height of John.
4. Mary kept the following record of rainfall in centimeters 4, 3, 6, 5, 3, 0. Find the mode.
5. a FOOT BALL TEAM CAN WIN, DRAW OR LOSE A Match. What is the probability that it will win a Match?
6. The mean of the scores: 8, 7, 6, 5, $(a - 5)$ is 6
 - (a) Find the value of a .
 - (b) Find the range of the scores.
7. Sumaya scored the following marks in her homework exercises: 2, 5, 7, 3, 10, 4, 7, 11, 8, 3
 - (a) Find her median mark
 - (b) Find the mean mark
 - (c) Find the probability that Sumaya scored a mark above her mean mark
8. The equation of a line is $2x + 1 = y$. Make a table for the coordinates of x and y with the coordinates of x between -2 and +3. Show the line on a graph.
9. Given that $x = 2y + 1$ Complete the table below.

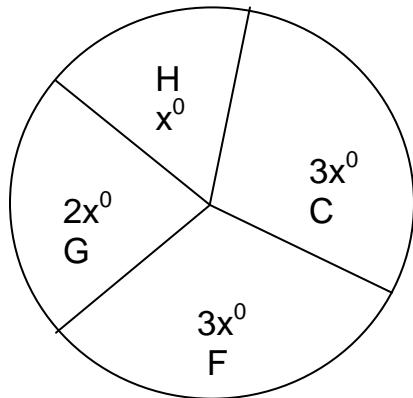
| | | | | | |
|---|---|---|---|---|---|
| X | 1 | — | 5 | — | 9 |
| Y | — | 1 | — | 3 | — |

10. (a) Draw a grid and plot the following points:
 - (i) A (-4, 3)
 - (ii) B (0, 3)
 - (iii) C (2, -3)
 - (iv) D (-4, -1)
 - (b) Join the points A to B, B to C, C to D, D to A
 - (c) Name the quadrilateral formed.
 - (d) Find the area of the quadrilateral formed above.
11. Find the mean of x , 4, $2x$, 6 and $2x$.
12. What number is mid way of $\frac{1}{2}$ and $\frac{1}{3}$?
13. A cyclist traveled from town P to R as follows. For 2 hours, he cycled from P to town Q a distance of 30km and then rested for 1 hour from Q. He continued for another 1 hour to town R at a speed of 40km/hr.
 - (a) Draw a travel graph to show his journey
14. Given that $Y = 2x - 1$
 - (a) Complete the table below.

| | | | | | | |
|---|----|---|---|---|---|---|
| X | 0 | 1 | 2 | 3 | 4 | 5 |
| Y | -1 | 1 | — | — | — | — |

- (b) Plot the points given in the table above on a graph.

15. The average of 3, 5, 4, 7, 9, 5 and y is 5. Find:
- the value of y
 - the median
 - the mode
16. The average speed of a car is 60km/hr for 30 minutes. What distance is covered?
17. The pie chart below shows how a farmer has divided his land. C is for cash crops, G is for grazing, F is for food crops and for other purposes . The land available is 720 hectares.



- (a) How many hectares are left for grazing?
 (b) If he pays rent of shs 200 per hectare per year, how much will he pay for land reserved for cash crops?
18. In a Mathematics test given to a class, the marks scored frequency and total marks scored are shown in the table below.

| Marks scored | Frequency | Total marks |
|--------------|-----------|-------------|
| 4 | 4 | 16 |
| _____ | 9 | 45 |
| 6 | _____ | 84 |
| 7 | 8 | _____ |
| 9 | 5 | 45 |

19. Study the frequency table and answer the questions that follow:

| | | | | |
|-----------------|----|----|----|----|
| Marks scored | 20 | 40 | 70 | 50 |
| No. of children | 2 | 3 | 1 | 1 |

- (a) How many pupils did the test?
 (b) Find their mean mark.
 (c) Calculate their median mark.
 (d) What was the modal mark.
 (e) Workout the range

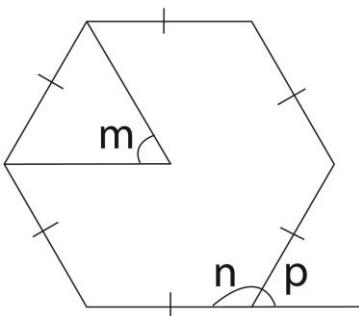
- (a) Complete the table
 (b) What was the mode?
 (c) How many pupils were in the class?
 (d) What was the average mark scored?

LINES, ANGLES AND GEOMETRICAL FIGURES

SUB TOPIC: Names of polygons

| NAME | SIDES |
|---------------|-------|
| triangles | 3 |
| quadrilateral | 4 |
| pentagon | 5 |
| hexagon | 6 |
| heptagon | 7 |
| octagon | 8 |
| nonagon | 9 |
| decagon | 10 |
| hendecagon | 11 |
| duo decagon | 12 |

SUBTOPIC: interior and exterior angles of a polygon



Examples

1. The exterior angle of a regular polygon is 36° . Find the size of the interior angle?

Let the interior angle be m

$$m + 36^\circ = 180^\circ$$

$$m + 36^\circ - 36^\circ = 180^\circ - 36^\circ$$

$$\underline{\underline{m = 144^\circ}}$$

2. The interior angle of a regular polygon is 115° . find the size of its exterior angle.

Let the exterior angle be m

$$m + 115^\circ = 180^\circ$$

$$m + 115^\circ - 115^\circ = 180^\circ - 115^\circ$$

$$\underline{\underline{m = 65^\circ}}$$

3. Find the size of the exterior angle of a polygon whose interior angle is;

(a) 120°

(b) 80°

4. Find the size of an interior angle of a polygon whose exterior angle is 45° .

SUB TOPIC: Calculating the number of sides of a polygon

Examples:

1. Calculate the number of sides of a regular polygon whose exterior angle is 30° .

$$\text{Number of sides} = \frac{360^\circ}{\text{each ext angle}}$$

$$= \frac{360^\circ}{30^\circ}$$

No of sides = 12 sides.

2. The interior angle of a regular polygon is 144° . Name the polygon.
Let the ext angle be x .

$$\text{No of side} = \frac{360^\circ}{36^\circ}$$

$= 10 \text{ sides}$

$X + 144^\circ = 180^\circ$

$X + 144^\circ - 144^\circ = 180^\circ - 144^\circ$

$X = 36^\circ$

Exterior angle = 36°

The polygon is a decagon

3. The interior angle of a regular polygon is 90° more than the exterior angle.

- (a) Calculate the exterior angle

Let the ext. angle be x

Int. angle = $x + 90^\circ$

Ext. angle x

$$x + 90^\circ + x = 180^\circ$$

$$2x + 90^\circ - 90^\circ = 180^\circ - 90^\circ$$

$$\underline{\underline{2x}} = \underline{\underline{90}}$$

$$\underline{2} \quad \underline{2}$$

$$x = 45^\circ$$

ext. angle = 45°

- (b) How many sides has the polygon?

No of sides = $\frac{360^\circ}{45^\circ}$

$$= 8$$

8 sides

Mathematics is the key

Calculate the number of sides of a polygon whose exterior angle is;

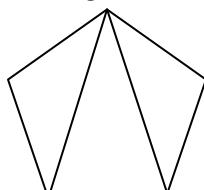
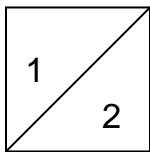
- (a) 36°
- (b) 45°
- (c) 60°

REFERENCE

A New MK Primary Mathematics 2000 Bk 7 Pg 246 - 249(New Edition)

SUB TOPIC: Triangulation

Triangulation is forming triangles in a polygon.



Quadrilateral

Pentagon

$$\text{Number of triangles} = n - 2$$

Each triangle contains two right angles.

$$\text{Number of right angles} = 2(n - 2)$$

$$= \underline{\underline{2n - 4}}$$

| Polygon | Number of sides | Number of triangles | Number of right angles |
|---------------|-----------------|-----------------------|--------------------------------|
| Quadrilateral | 4 | $4 - 2 = 2$ triangles | $2 \times 2 = 4$ right angles |
| Pentagon | 5 | $5 - 2 = 3$ triangles | $3 \times 2 = 6$ right angles |
| Hexagon | 6 | $6 - 2 = 4$ triangles | $4 \times 2 = 8$ right angles |
| Heptagon | 7 | $7 - 2 = 5$ triangles | $5 \times 2 = 10$ right angles |

Examples:

1. How many triangles and right angles can be formed in a polygon with 8 sides?

$$\begin{aligned}\text{No of triangles} &= n - 2 \\ &= 8 - 2 \\ &= \underline{\underline{6 \text{ triangles}}}\end{aligned}$$

$$\begin{aligned}\text{No. of right angles} &= 6 \times 2 \\ &= \underline{\underline{12 \text{ right angles}}}\end{aligned}$$

2. Calculate the number of triangles and the number right angles of;

- (a) A 6 six sided polygon
- (b) A duo decagon
- (c) A 20 sided polygon

Mathematics is the Key

REFERENCE

A New MK Primary Mathematics 2000 Bk 7 Pg 237-250 (New Edition)

SUB TOPIC: Finding number of sides of a polygon when given number of triangles or right angles

1. If 10 triangles can be formed in regular polygon, find the number of sides of the polygon.

$$\text{No. of triangles} = n - 2$$

$$n - 2 = 10$$

$$n - 2 + 2 = 10 + 2$$

$$\underline{\underline{n = 12 \text{ sides}}}$$

2. Find the number of sides of a polygon with 16 triangles

$$2(n - 2) = \text{no. of right angles}$$

$$2n - 4 = 16$$

$$2n - 4 + 4 = 16 + 4$$

$$2n = 20$$

$$\frac{2n}{2} = \frac{20}{2}$$

$$\underline{\underline{n = 10 \text{ sides}}}$$

3. Find the number of sides of a polygon with;

(a) 10 right triangles

(b) 4 triangles

4. Name the polygon with;

(a) 8 triangles

(b) 18 right angles

**SUB TOPIC: THE SUM OF INTERIOR ANGLES OF A REGULAR POLYGON
(interior angle sum)**

$$\text{Interior angle sum} = 180^\circ(n - 2) \text{ or } 90^\circ(2n - 4)$$

Examples:

1. The interior angle of a regular pentagon is 108° . Calculate the sum of all interior angles of the polygon.

A pentagon has 5 sides.

Each int. angle = 108°

$$\text{The sum of interior angles} = 108^\circ \times 5$$

$$\underline{\underline{= 540^\circ}}$$

Mathematics is the key

2. Calculate the interior angle sum of a regular polygon with 7 sides.

Int. angle sum = $180^\circ(n-2)$

$$180^\circ(7-2)$$

$$180^\circ \times 5$$

$$\underline{\underline{900^\circ}}$$

3. Each exterior angle of a polygon is 30° . Calculate the sum of the interior angles of a polygon.

No. of sides

$$\frac{360^\circ}{30^\circ}$$

12 sides

The sum of int. angles

$$180^\circ(n-2)$$

$$180^\circ(12-2)$$

$$180 \times 10$$

$$\underline{\underline{1800^\circ}}$$

4. Find the sum of interior angles of ;

- (a) A polygon with 8sides
- (b) A polygon with 18sides
- (c) A heptagon
- (d) A polygon with 15 sides

REFERENCE

A New MK Primary Mathematics 2000 Bk 7 Pg 252 - 257 (New Edition)

SUB TOPIC: Finding number of sides when given interior angle sum

1. The sum of interior angles of a regular polygon is 1440° .

- (a) How many sides has the polygon?

$$180^\circ(n-2) = \text{int. angle sum}$$

$$180^\circ(n-2) = 1440^\circ$$

$$\frac{180^\circ(n-2)}{180^\circ} = \frac{1440^\circ}{180^\circ}$$

$$n-2 = 8$$

$$n-2+2 = 8+2$$

$$\underline{\underline{n = 10 \text{ sides}}}$$

- (b) What is the size of each exterior angle of the polygon?

$$360^\circ \div 10 = 36^\circ$$

Mathematics is the Key

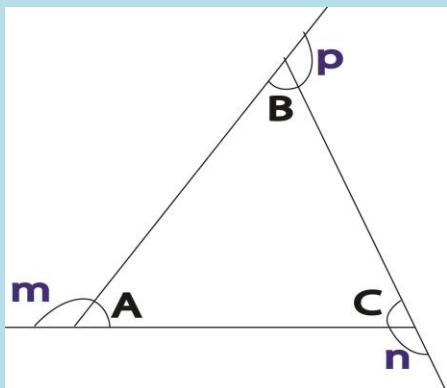
2. Calculate the number of sides of a polygon whose interior angle sum is;

- (a) 1800°
- (b) 540°
- (c) 720°

REFERENCE

A New MK Primary Mathematics 2000 Bk 7 Pg 252 - 257 (New Edition)

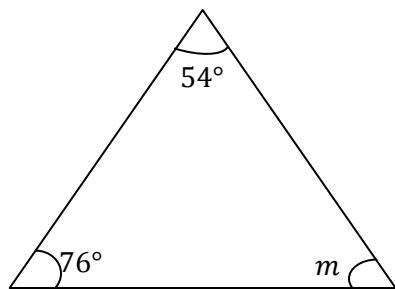
SUB TOPIC: ANGLES OF TRIANGLES



$$A + B + C = 180^\circ$$

Examples

1. Find the missing angle

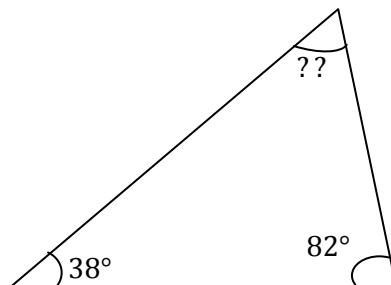
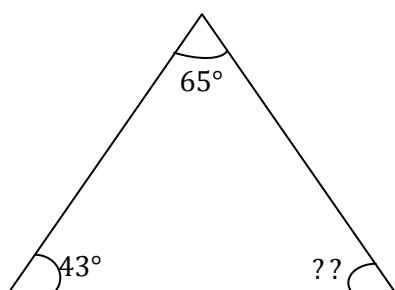


$$m + 76^\circ + 54^\circ = 180^\circ$$

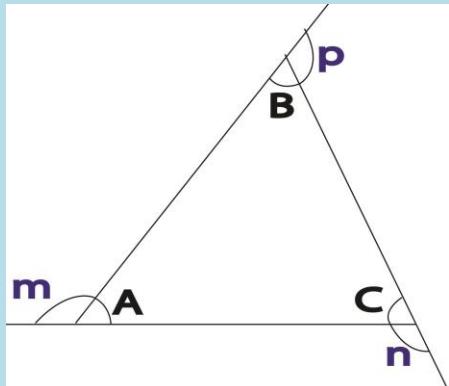
$$m + 130^\circ = 180^\circ$$

$$m + 130^\circ - 130^\circ = 180^\circ - 130^\circ$$

$$\underline{\underline{m = 50^\circ}}$$



Angle properties of triangles



Two interior angles of a triangle add up to one opposite exterior angle

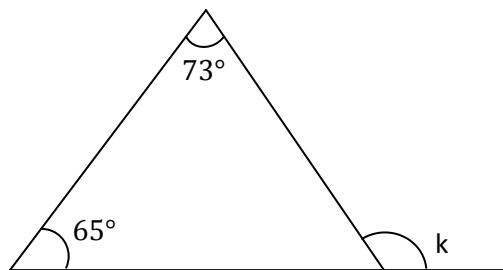
$$A + B = n$$

$$B + C = m$$

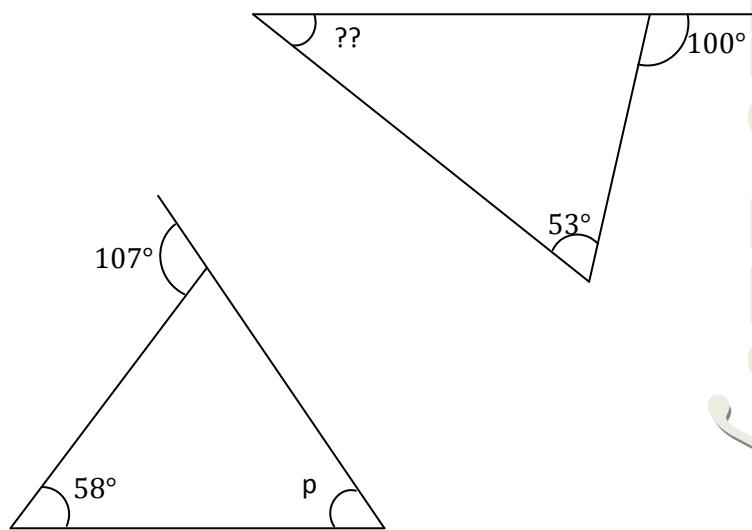
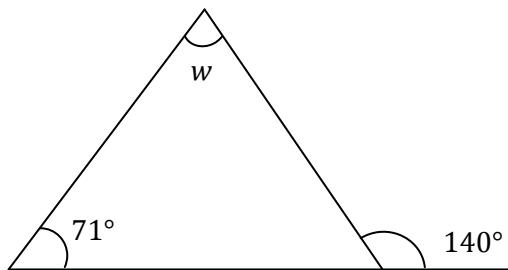
$$A + C = p$$

Examples

- Find the missing angle in the figures below

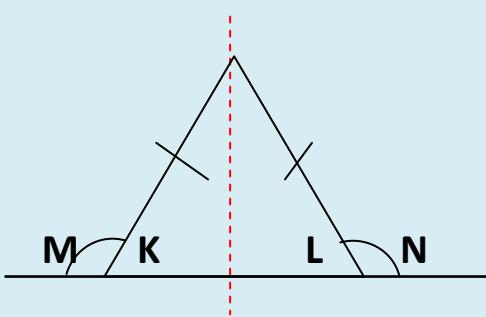


$$\begin{aligned} k &= 65^\circ + 73^\circ \\ k &= \underline{\underline{138^\circ}} \end{aligned}$$



Mathematics is the Key

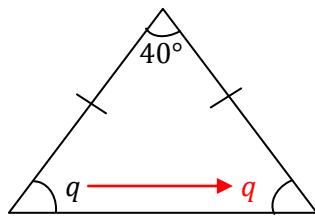
Angle properties of triangles



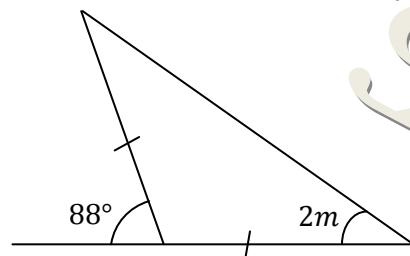
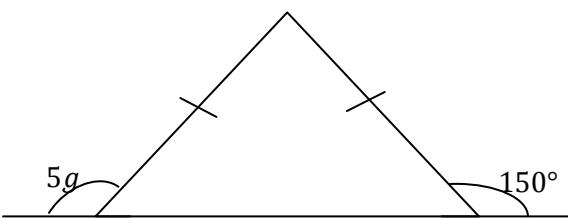
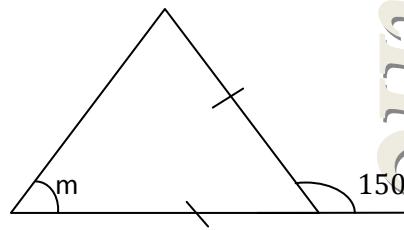
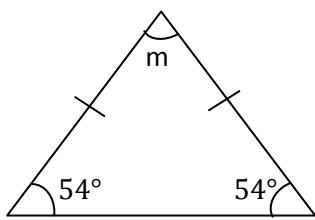
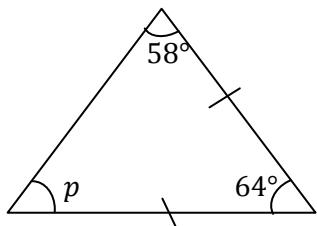
- ❖ Two sides are equal
 - ❖ It has one line of symmetry
 - ❖ Base angles are equal
- $$\angle K = \angle L$$
- $$\angle M = \angle N$$

Examples

- Find the value of the unknown in degrees.



$$\begin{aligned}
 q + q + 40^\circ &= 180^\circ \\
 2q + 40^\circ &= 180^\circ \\
 2q + 40^\circ - 40^\circ &= 180^\circ - 40^\circ \\
 2q &= 140^\circ \\
 \frac{2q}{2} &= \frac{140^\circ}{2} \\
 q &= 70^\circ
 \end{aligned}$$



Mathematics is the Key

REFERENCE

A New MK Primary Mathematics 2000 Bk 7 Pg 229-235 (New Edition)

SUB TOPIC: PROPERTIES OF REGULAR POLYGONS

- **The number of centre, exterior or interior angles is equal to the number of sides.**
- **The centre angle is equal to the exterior angle in a regular polygon.**
- **Interior angle plus exterior angle is equal to 180° .**
- **All exterior angles of a regular polygon add up to 360° .**

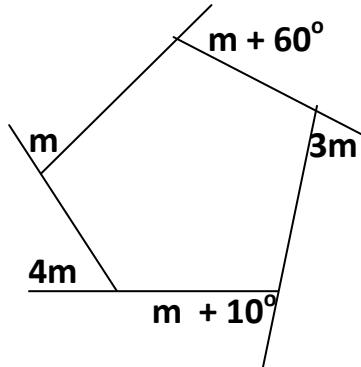
Exterior angles of polygons

Examples:

1. The exterior angles of a quadrilateral are $2x$, x , $3x$ and $x + 10^\circ$. find the value of x .

$$\begin{aligned}2x + x + 10^\circ + 3x + x &= 360^\circ \\7x + 10^\circ &= 360^\circ \\7x + 10^\circ - 10^\circ &= 360^\circ - 10^\circ \\7x &= \underline{\underline{350^\circ}} \\7 &\quad 7 \\x &= \underline{\underline{50^\circ}}\end{aligned}$$

2. Use the figure below to find the value of the unknown.



$$\begin{aligned}m + 4m + m + 10^\circ + m + 60^\circ + 3m &= 360^\circ \\10m + 70^\circ &= 360^\circ \\10m + 70^\circ - 70^\circ &= 360^\circ - 70^\circ \\10m &= \underline{\underline{290^\circ}} \\10 &\quad 10 \\m &= \underline{\underline{30^\circ}}\end{aligned}$$

REFERENCE

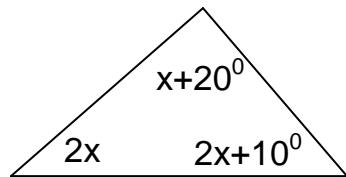
A New MK Primary Mathematics 2000 Bk 7 Pg 242 – 244 (New Edition)

Mathematics is the key

SUB TOPIC: MORE ABOUT INTERIOR ANGLE SUM OF POLYGONS

Examples

- Find the value of x in the figure.



$$\text{Sum of int. angles of triangle} = 180^\circ$$

$$x + 20^\circ + 2x + 2x + 10 = 180^\circ$$

$$5x + 30^\circ = 180^\circ$$

$$5x + 30^\circ - 30^\circ = 180^\circ - 30^\circ$$

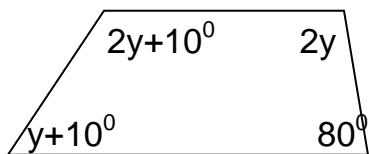
$$5x = 150^\circ$$

$$\underline{5x = 150^\circ}$$

$$\underline{\quad \quad \quad 5}$$

$$\underline{x = 30^\circ}$$

- Find the value of y .



$$\text{Int. angle sum} = 360^\circ$$

$$2y + y + 10 + 2y + 10 + 80 = 360^\circ$$

$$2y + y + 2y + 10 + 10 + 80 = 360^\circ$$

$$5y + 100^\circ = 360^\circ$$

$$5y + 100^\circ - 100^\circ = 360^\circ - 100^\circ$$

$$\underline{5y = 260^\circ}$$

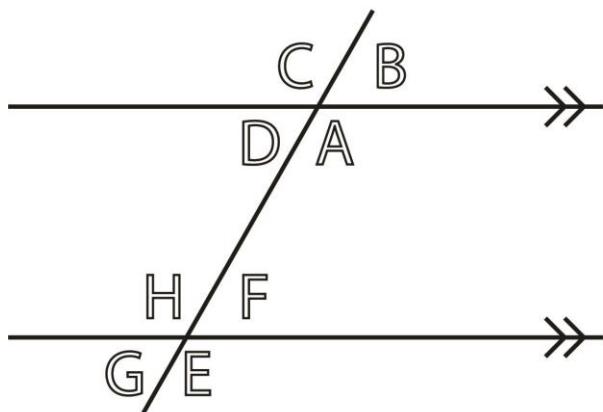
$$\underline{\quad \quad \quad 5}$$

$$\underline{y = 52^\circ}$$

- Interior angles of an octagon are $2x, x, 3x, 4x, x, 2x, 3x$ and x . find the value of x

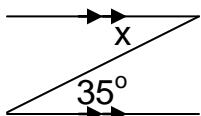
SUB TOPIC: ANGLES ON PARALLEL LINES

Properties of angles on parallel lines

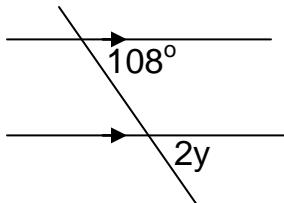


- $A + B = 180^\circ$ (supp. $\angle S$)
- $A = C$ (vertically opp $\angle S$)
- $A = E$ (corresp $\angle S$)
- $D = G$ (corresp $\angle S$)
- $B = F$ (corresp $\angle S$)
- $C = H$ (corresp $\angle S$)
- $A = H \& D = f$ (alt. Int $\angle S$)
- $G = B \& C = E$ (Alt. ext. $\angle S$)
- $A + F = 180^\circ$ (co.int. $\angle S$)
- $D + H = 180^\circ$ (co.int. $\angle S$)
- $C + G = 180^\circ$ (co.ext. $\angle S$)
- $B + E = 180^\circ$ (co.ext. $\angle S$)
- $H = E$ (vertically opp. $\angle S$)
- $A + B + C + D = 360^\circ$ ($\angle S$ at a point)

1. Solve for the unknowns



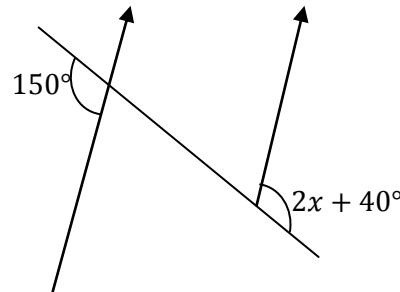
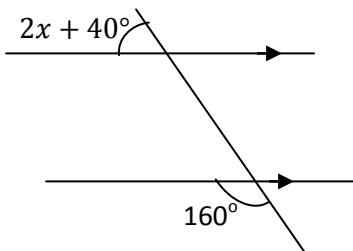
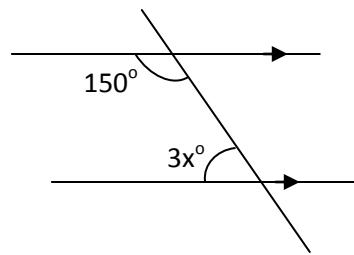
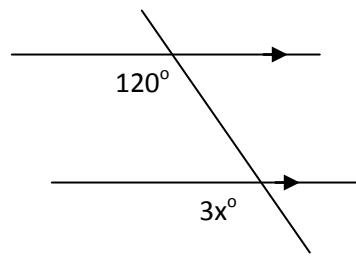
$$\underline{x = 350 \text{ (Alt. int } \angle\text{s)}}$$



$$2y = 108^\circ \text{ (corr. } \angle\text{s)}$$

$$\frac{2y}{2} = \frac{108^\circ}{2}$$

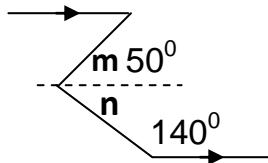
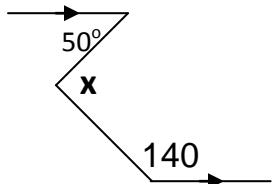
$$\underline{y = 54^\circ}$$



SUB TOPIC: More about angles on parallel lines

Examples:

1. Find the value of x.



Imaginary lines

Draw imaginary lines

$$\underline{m = 50^\circ \text{ (Alt. int } \angle\text{s)}}$$

$$n + 140^\circ = 180^\circ \text{ (Co. int. } \angle\text{s)}$$

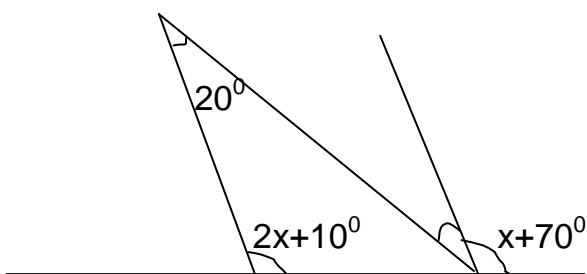
$$n + 140^\circ - 140^\circ = 180^\circ - 140^\circ$$

$$\underline{n = 40^\circ}$$

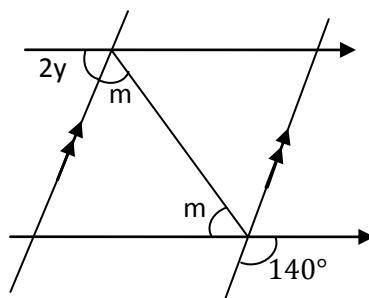
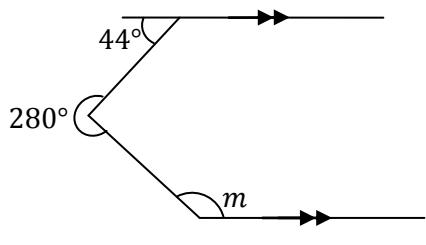
$$x = 40^\circ + 50^\circ$$

$$\underline{x = 90^\circ}$$

2. Find the value of x and k



3. Find the value of the unknowns in degrees



REFERENCE

A New MK Primary Mathematics 2000 Bk 7 Pg 213 (New Edition)

SUB TOPIC: Angle properties of quadrilaterals

A quadrilateral is a figure with 4 sides

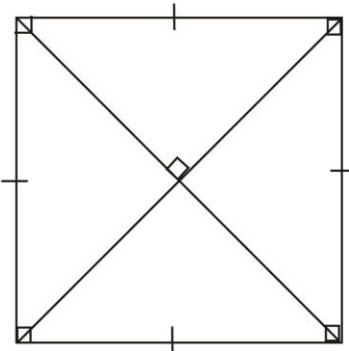
Examples of quadrilaterals

- **Square**
- **Kite**
- **Parallelogram**
- **Rectangle**
- **Rhombus**
- **Trapezium**

Remember:

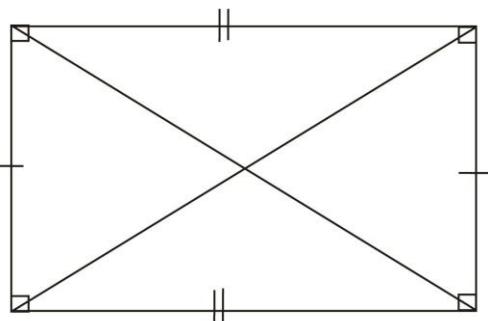
A square is a regular quadrilateral.

SQUARE



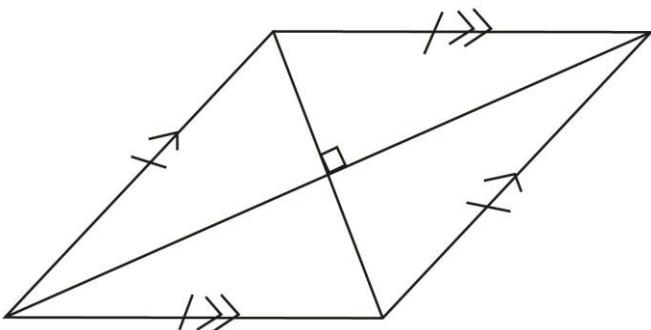
- All sides are equal.
- It has 4 right angles.
- Opposite sides are parallel.
- Diagonals are equal and they bisect each other at a right angle.
- It has 4 lines of folding symmetry.
- Diagonals bisect each angle at every vertex.
- Opposite angles are equal.

RECTANGLE



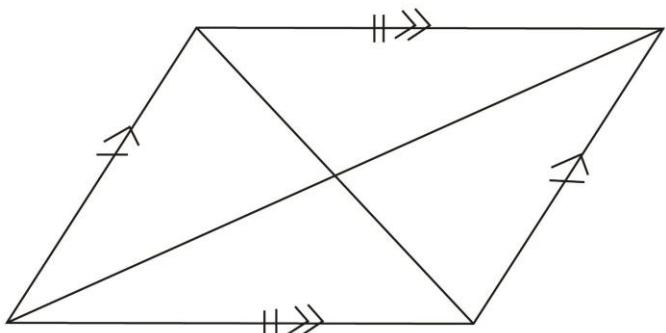
- Opposite sides are equal and parallel.
- It has 4 right angles.
- Diagonals are equal and they bisect each other.
- Diagonals do not meet at right angle.
- It has 2 lines of folding symmetry.
- Opposite angles are equal.

RHOMBUS



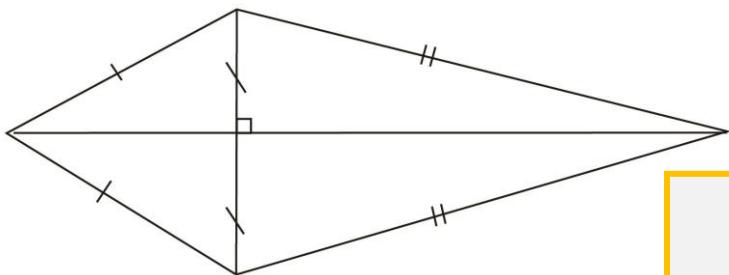
- All sides are equal
- Opposite sides are parallel.
- Diagonals are not equal and they bisect each other at a right angle.
- Diagonals bisect each angle at every vertex.
- It has 2 lines of folding symmetry.
- Opposite angles are equal.

PARALLELOGRAM

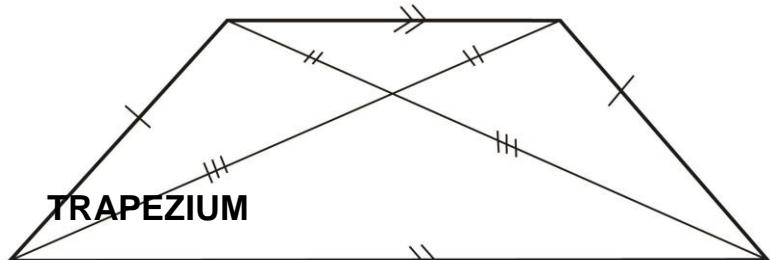


- Opposite sides are equal and parallel.
- Diagonals are not equal and they bisect each other.
- Diagonals do not bisect each angle at every vertex.
- It has no lines of folding symmetry
- Opposite angles are equal.

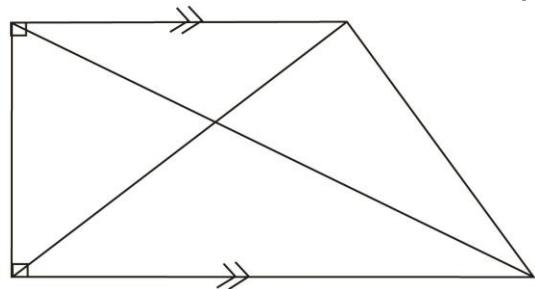
KITE



- Adjacent sides are equal.
- Diagonals are not equal and they meet each other at a right angle.
- The longer diagonal bisects the shorter diagonal and the angles at the vertices.
- It has 1 line of folding symmetry.
- Opposite angles are equal.



TRAPEZIUM



Right angled trapezium

Isosceles trapezium

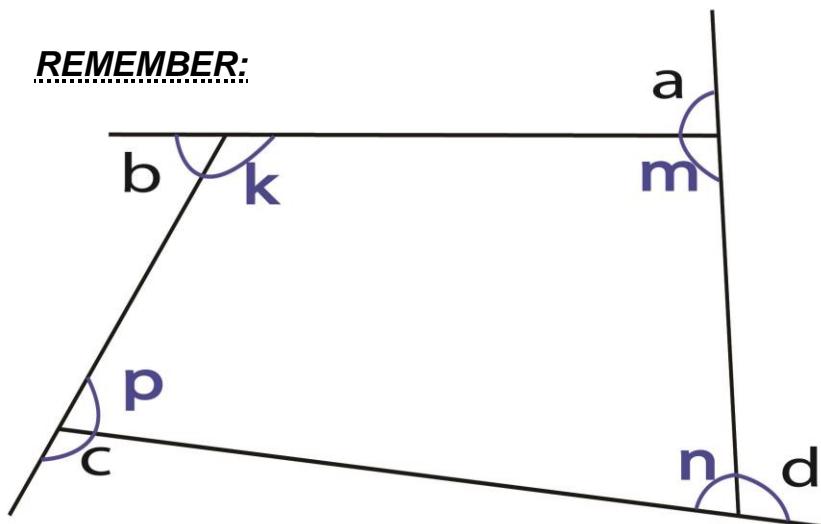
ISOSCELES TRAPEZIUM

- Two of the sides are parallel.
- Diagonals are equal but they do not bisect each other.
- Diagonals do not bisect angles in the vertices.
- Opposite angles are not equal.
- It has 1 line of folding symmetry.
- Opposite angles are not equal.

RIGHT ANGLED TRAPEZIUM

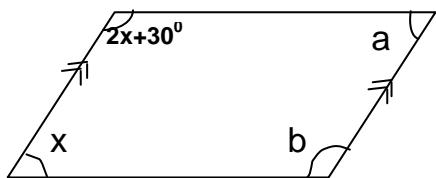
- Two of the sides are parallel.
- Diagonals are not equal and they do not bisect each other.
- Diagonals do not bisect angles in the vertices.
- Opposite angles are not equal.
- It has no lines of folding symmetry.
- Opposite angles are equal.

REMEMBER:



- Interior angle sum of a quadrilateral is 360°
 $k + m + n + p = 360^\circ$
- Exterior angle sum of every polygon is 360°
 $a + b + c + d = 360^\circ$

1. Calculate the size of angles x , b , a



REFERENCE

A New MK Primary Mathematics 2000 Bk 7 Pg 237-241 (New Edition)

SUB TOPIC: Complementary angles

An angle with 90° is called a right angle.

Any two angles that add up to 90° are complementary angles.

Examples:

- xv. What is the complement of 30° ?

Let the complement be x

$$X + 30^{\circ} = 90^{\circ}$$

$$X + 30 - 30 = 90 - 30$$

$$\underline{x = 60}$$

- xvi. Find the complement of $(x + 40)^{\circ}$

$$90^{\circ} - (x + 40)^{\circ}$$

$$90^{\circ} - x^{\circ} - 40^{\circ}$$

$$90^{\circ} - 40^{\circ} - x^{\circ}$$

$$\underline{(50 - x)^{\circ}}$$

- xvii. What angle is $\frac{1}{2}$ of its complement?

Let the angle be k

| ANGLE | COMPL. | TL |
|-------|--------|--------------|
| k | $2k$ | 90° |

$$2k + k = 90^{\circ}$$

$$3k = 90^{\circ}$$

$$\frac{3k}{3} = \frac{90^{\circ}}{3}$$

$$\underline{K = 30^{\circ}}$$

- xviii. Find the complement of ;

- (a) 30°
- (b) 63°
- (c) $m - 15^{\circ}$
- (d) p°

- xix. What angle is 5 times its complement

REFERENCE

A New MK Primary Mathematics 2000 Bk 7 Pg 202-203 (New Edition)

SUB TOPIC: Supplementary angles

Supplementary angles are two angles that add up to 180° .

Examples:

$$X + Y = 180^{\circ} \text{ (supp. angles)}$$

1. In the above figure, if $x = 48^{\circ}$, find y .

$$x + y = 180^{\circ}$$

$$y + 48^{\circ} = 180^{\circ}$$

$$y + 48^{\circ} - 48^{\circ} = 180^{\circ} - 48^{\circ}$$

$$\underline{y = 132^{\circ}}$$

2. What angle is $\frac{1}{4}$ of its supplement?

Let the angle be m

| ANGLE | SUPPL. | TL |
|-------|--------|---------------|
| K | $4k$ | 180° |

$$4k + k = 180^{\circ}$$

$$5k = 180^{\circ}$$

$$\frac{5k}{5} = \frac{180^{\circ}}{5}$$

$$\underline{\underline{K = 36^{\circ}}}$$

3. Find the supplement of;

a. 135°

b. $2k - 20^{\circ}$

4. What angle is 5 times its supplement?

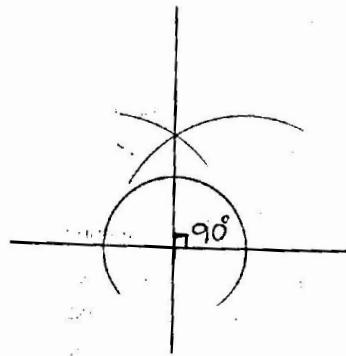
REFERENCE

A New MK Primary Mathematics 2000 Bk 7 exercise 11:56 Pg 204 (New Edition)

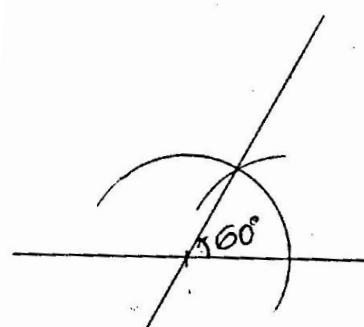
CONSTRUCTION

SUB TOPIC: Constructing special angles

1. Construct an angle of 90°

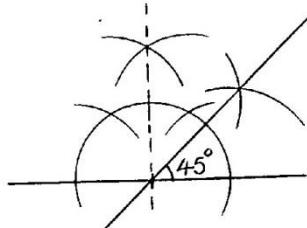


2. Construct an angle of 60°

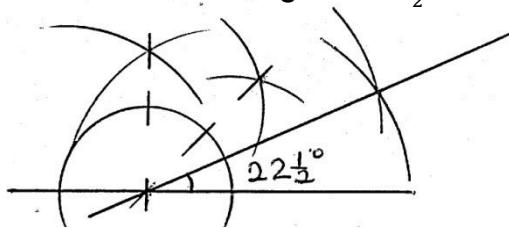


SUB TOPIC: Constructing other angles

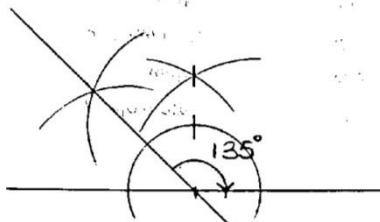
1. Construct an angle of 45°



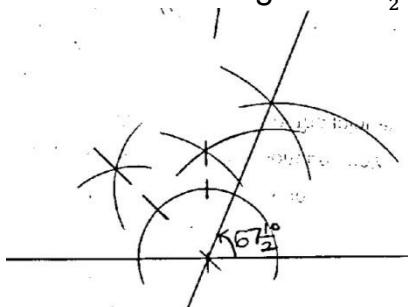
2. Construct an angle of $22\frac{1}{2}^{\circ}$



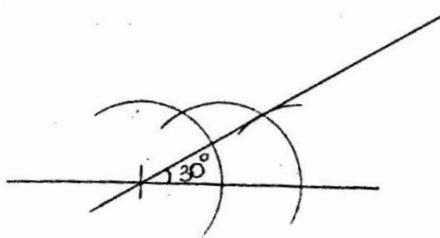
3. Construct an angle of 135°



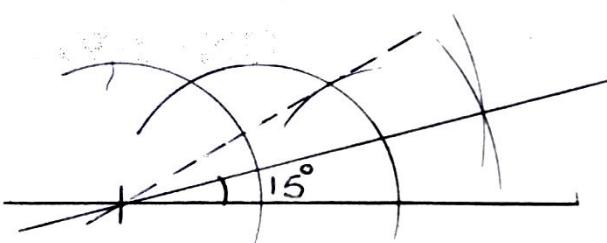
4. Construct an angle of $67\frac{1}{2}^{\circ}$



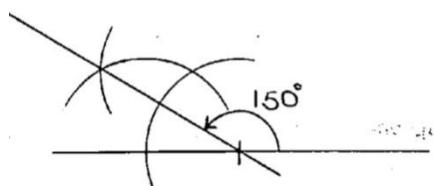
5. Construct an angle of 30°



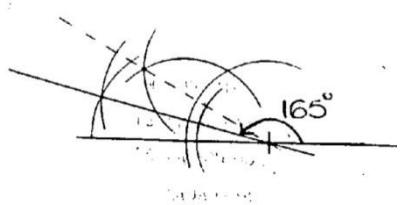
6. Construct an angle of 15°



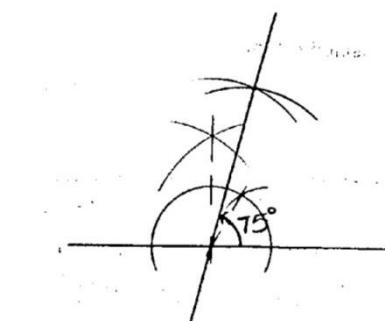
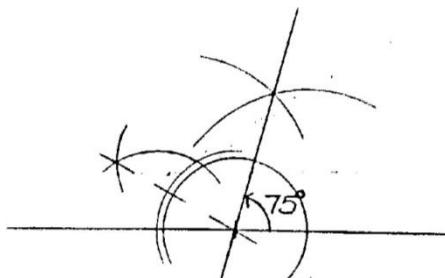
7. Construct an angle of 150°



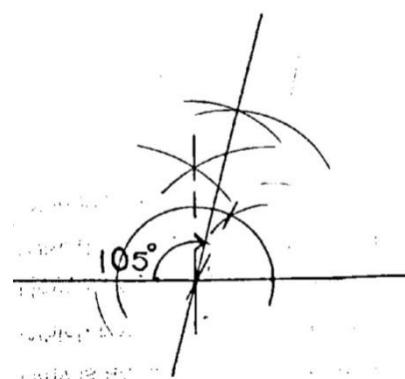
8. Construct an angle of 165°



9. Construct an angle of 75°



10. Construct an angle of 105°



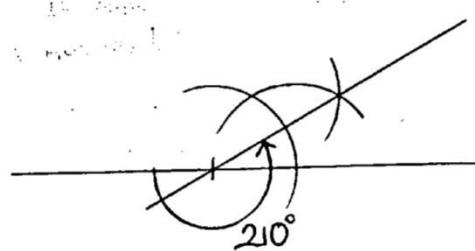
REFERENCE

A New MK Primary Mathematics 2000 Bk 7 Pg 277 - 279 (New Edition)

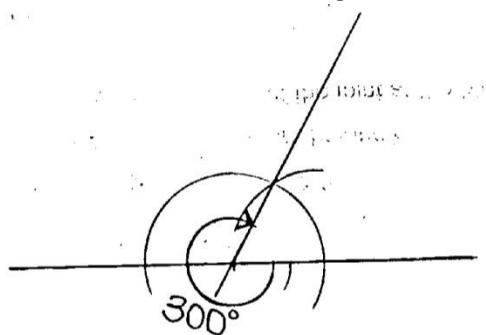
SUB TOPIC: Constructing reflex angles

A reflex angle is constructed by adding 180° to other angles

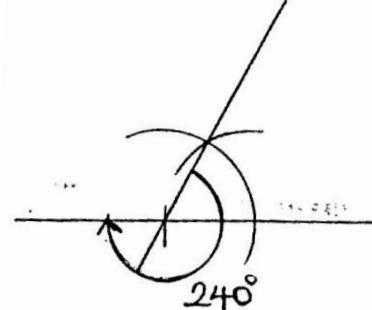
1. Construct an angle of 210°



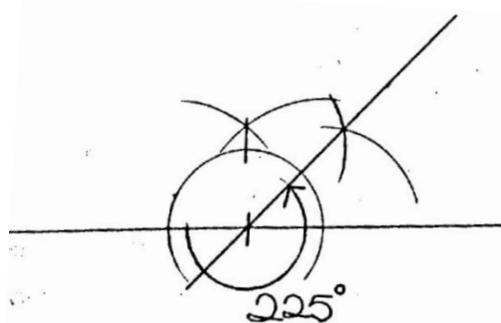
2. Construct an angle of 300°



3. Construct an angle of 240°

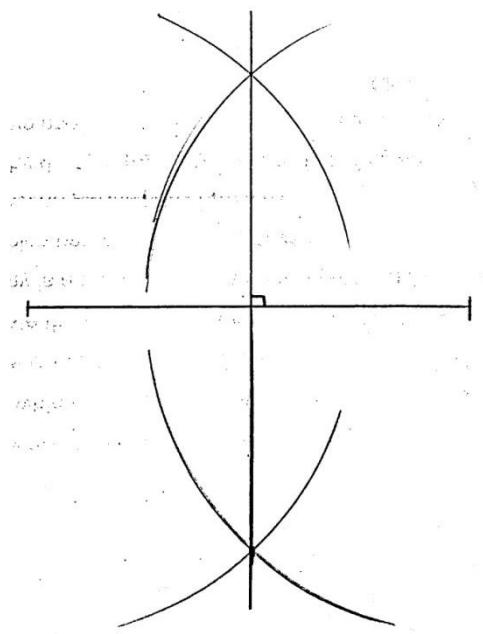


4. Construct an angle of 225°



SUB TOPIC: Constructing perpendicular bisectors

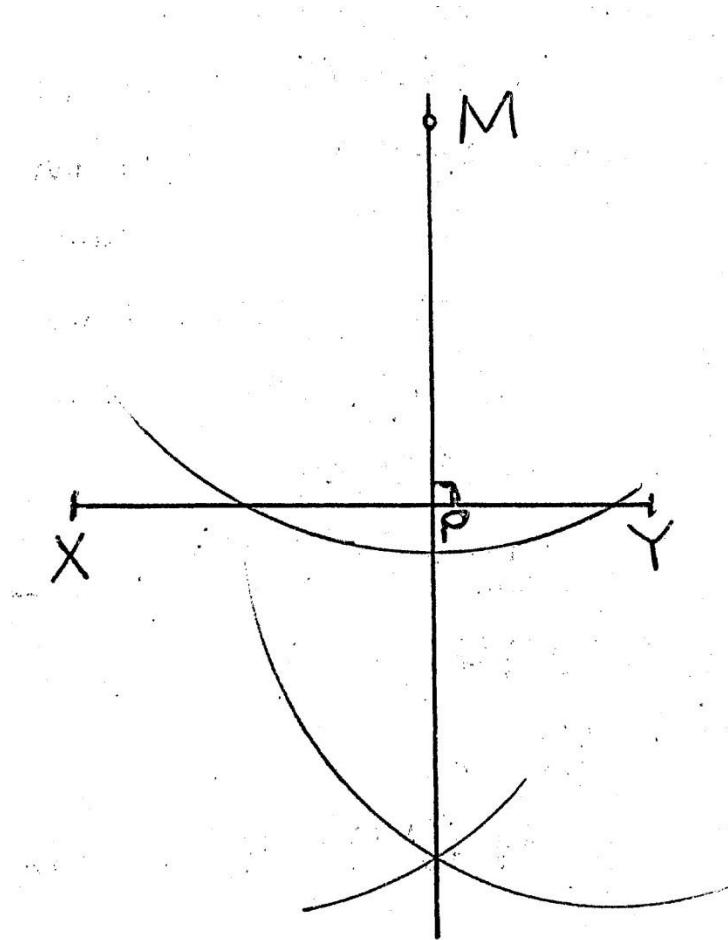
1. Bisect the line below



Mathematics is the Key

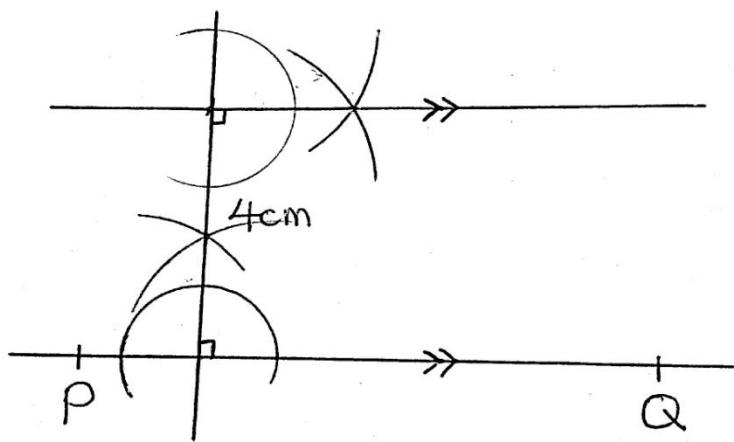
SUB TOPIC: Constructing perpendicular from a point

1. Using a ruler, a pencil and a pair of compasses, drop a perpendicular from M to meet line XY at p.



SUB TOPIC: Constructing parallel lines

1. Construct a line parallel to line PQ below such that the lines are 4 cm apart.

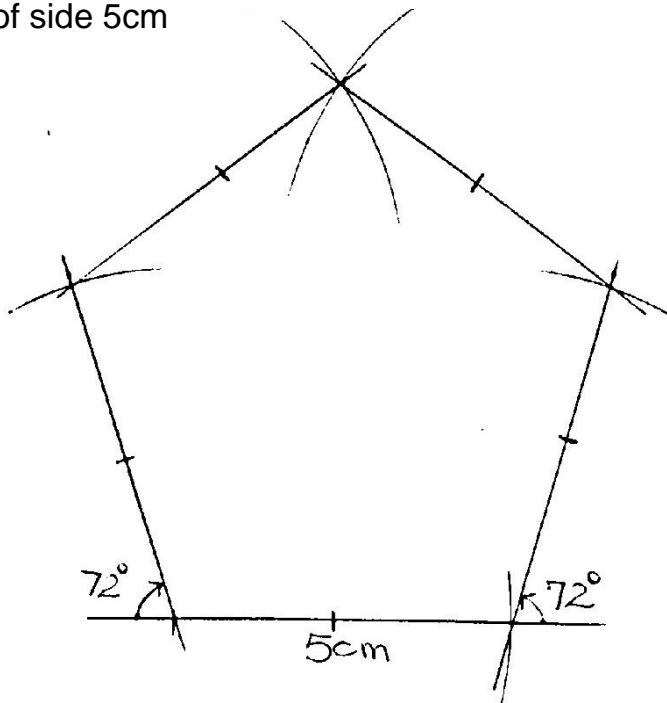
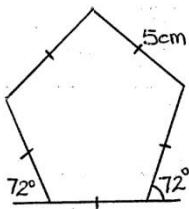


Mathematics is the Key

SUB TOPIC: Constructing a pentagon when given a side

1. Construct a pentagon of side 5cm

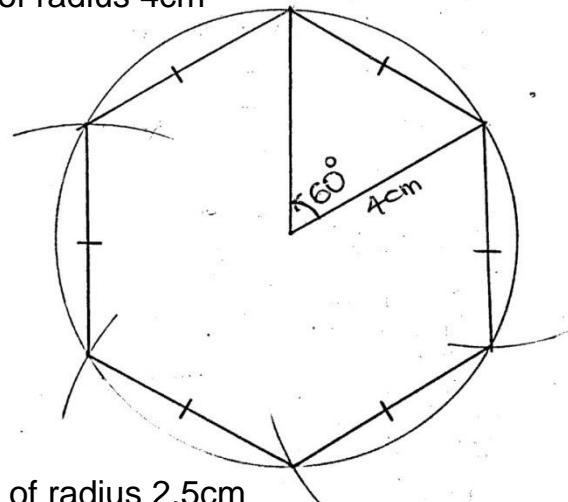
$$\text{Ext. angle} = \frac{360^\circ}{5} \\ \underline{\underline{= 72^\circ}}$$



SUB TOPIC: Constructing polygons using a centre angle

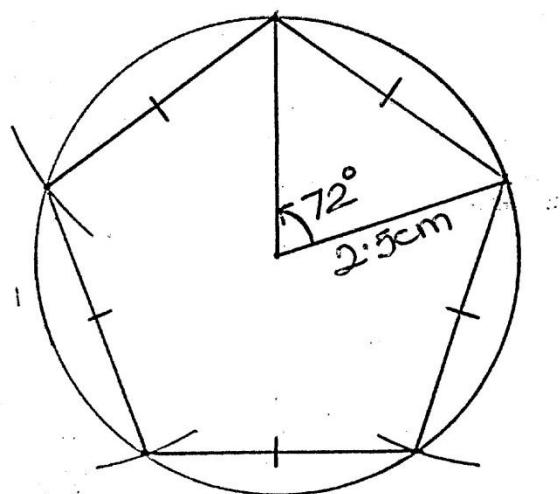
1. Construct a hexagon in a circle of radius 4cm

$$\text{Centre angle} = \frac{360^\circ}{6} \\ \underline{\underline{= 60^\circ}}$$



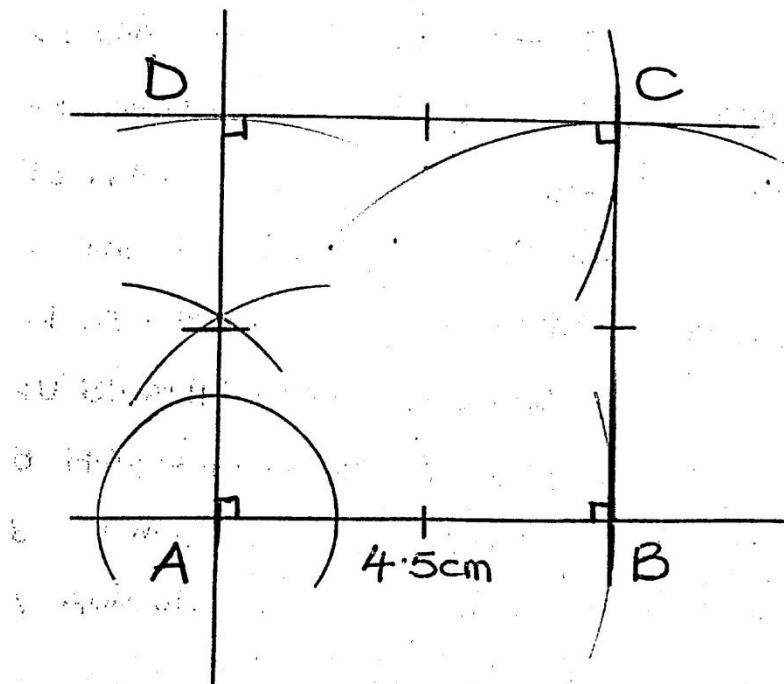
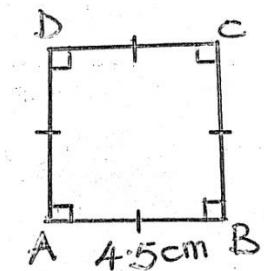
2. Construct a pentagon in a circle of radius 2.5cm

$$\text{Centre angle} = \frac{360^\circ}{5} \\ \underline{\underline{= 72^\circ}}$$



SUB TOPIC: Constructing a square when given side

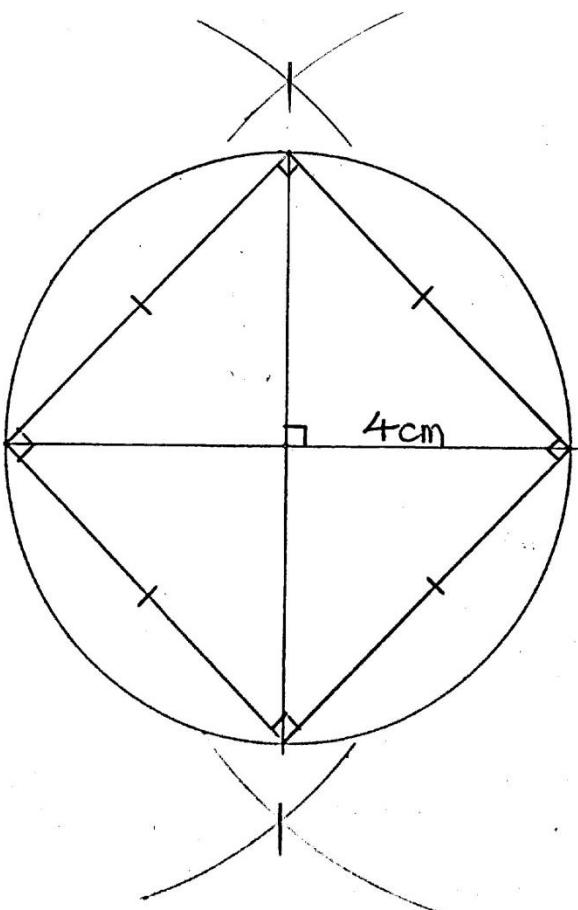
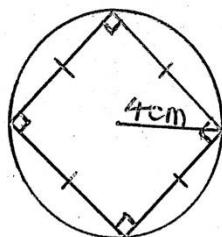
1. Construct square ABCD of side 4.5cm



2. Construct a square of side 5.3 cm
3. Construct square MNOP where $MN=4\text{cm}$

SUB TOPIC: Constructing a square in a circle

1. Construct a square in a circle of radius 4cm

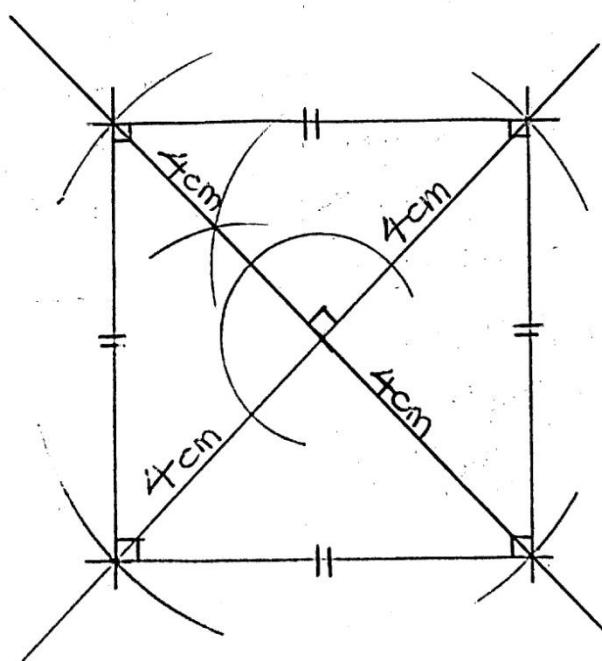
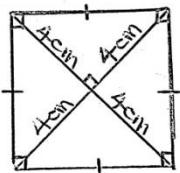


▲ Measure the length of one side

2. Construct a square in a circle of radius 6cm
3. Construct a square in a circle of radius 3.5cm

SUB TOPIC: Constructing a square using diagonals

1. Construct a square whose diagonal is 8cm

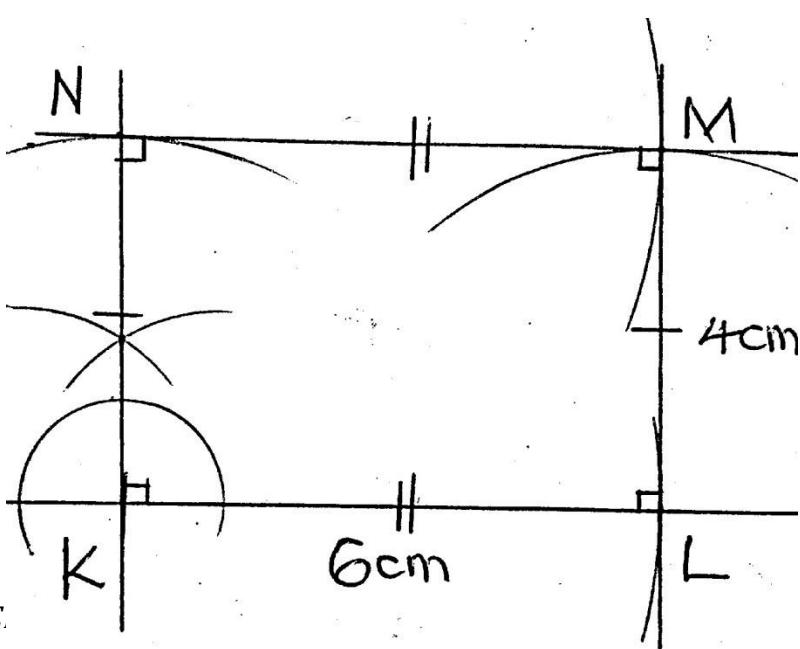
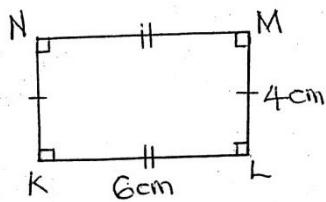


▲ Measure the length of one side

2. Construct a square whose diagonal is 9cm
3. Construct square PQRS whose diagonal is 8cm

SUB TOPIC: Constructing a rectangle when given sides

1. Construct rectangle KLMN where KL=6cm and LM = 4cm.



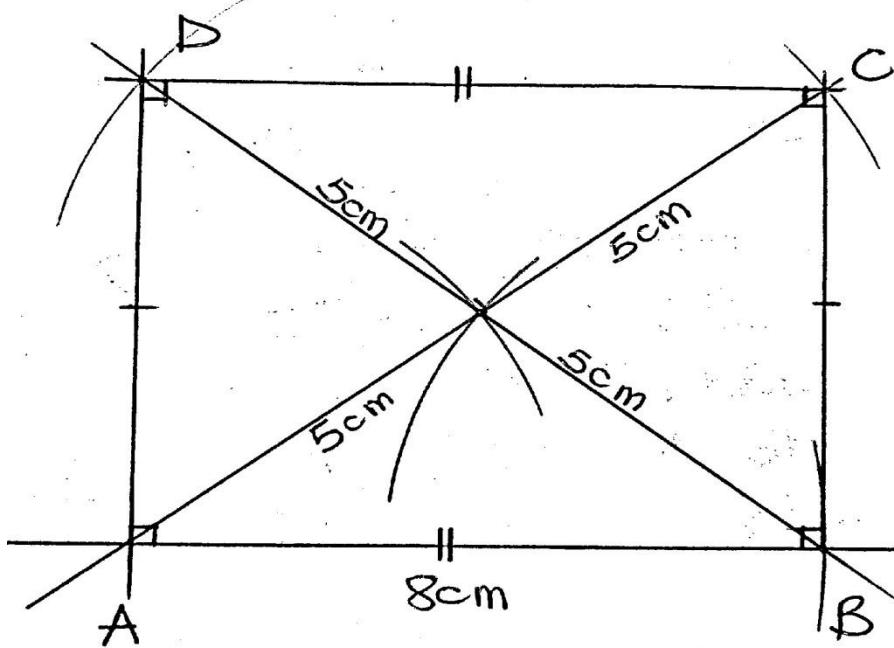
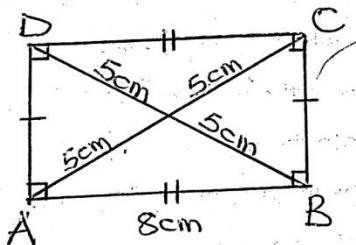
▲ Measure diagonal KM

▲ Measure angle MKL

2. Construct a rectangle whose length is 7cm and width is 4.3cm.

SUB TOPIC: Constructing a rectangle when one side and diagonals

1. Construct rectangle ABCD where AB= 8cm and AC=10cm

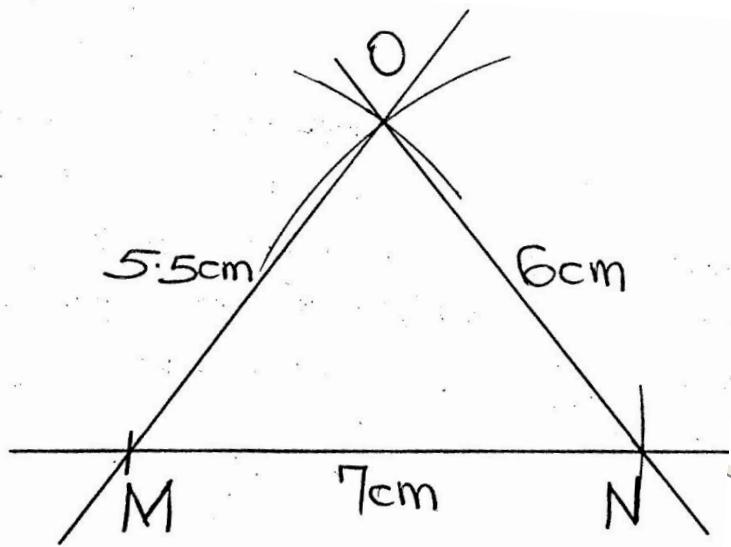
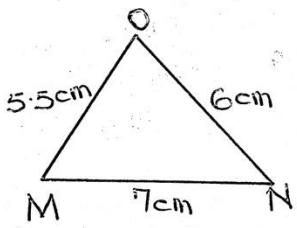


▲ Measure the width of the rectangle.

▲ Measure angle DBA

SUB TOPIC: Constructing a triangle when given sides(SSS)

1. Construct triangle MNO where MN= 7cm, NO=6cm and MO=5.5cm

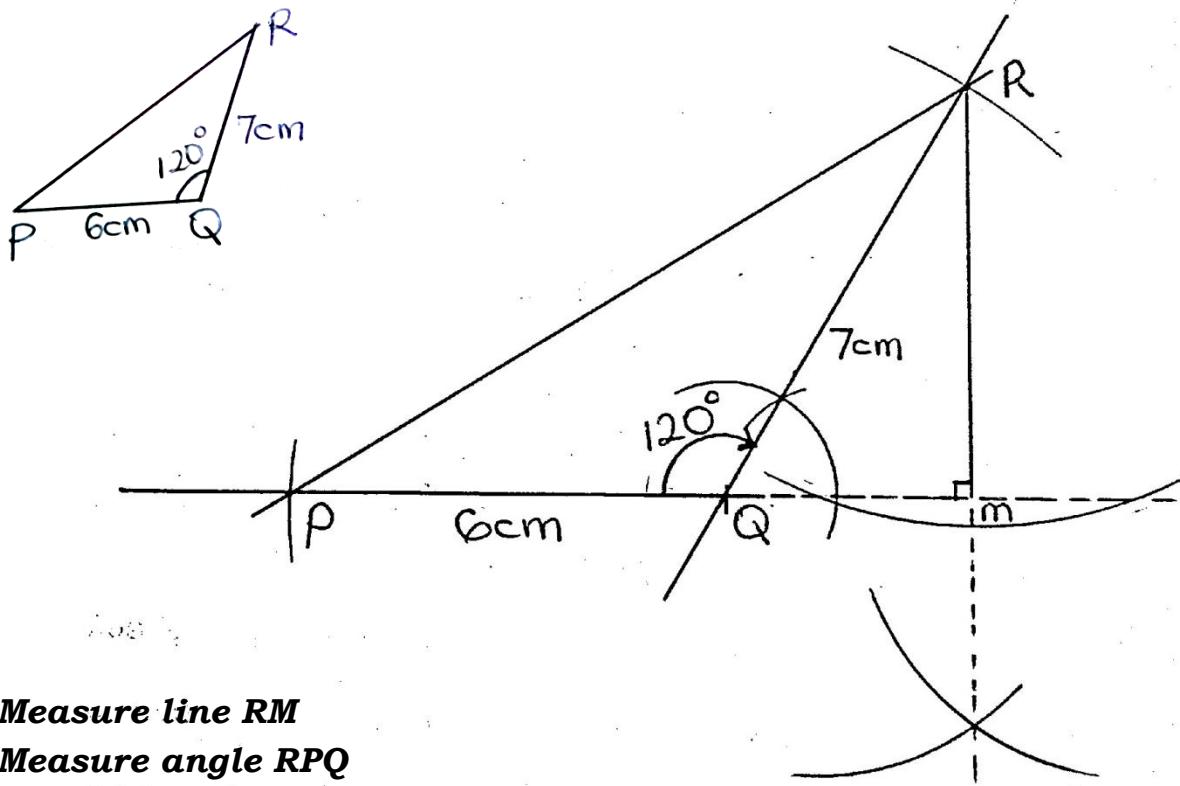


▲ Measure angle OMN.

2. Construct triangle KLM in which KL = 7.3cm KM = LM = 8cm

SUB TOPIC: Constructing a triangle when given two sides and one angle(SAS)

1. Construct triangle PQR where line PQ = 6cm, angle PQR = 120° and QR=7cm. Drop a perpendicular from R to meet PQ at m.

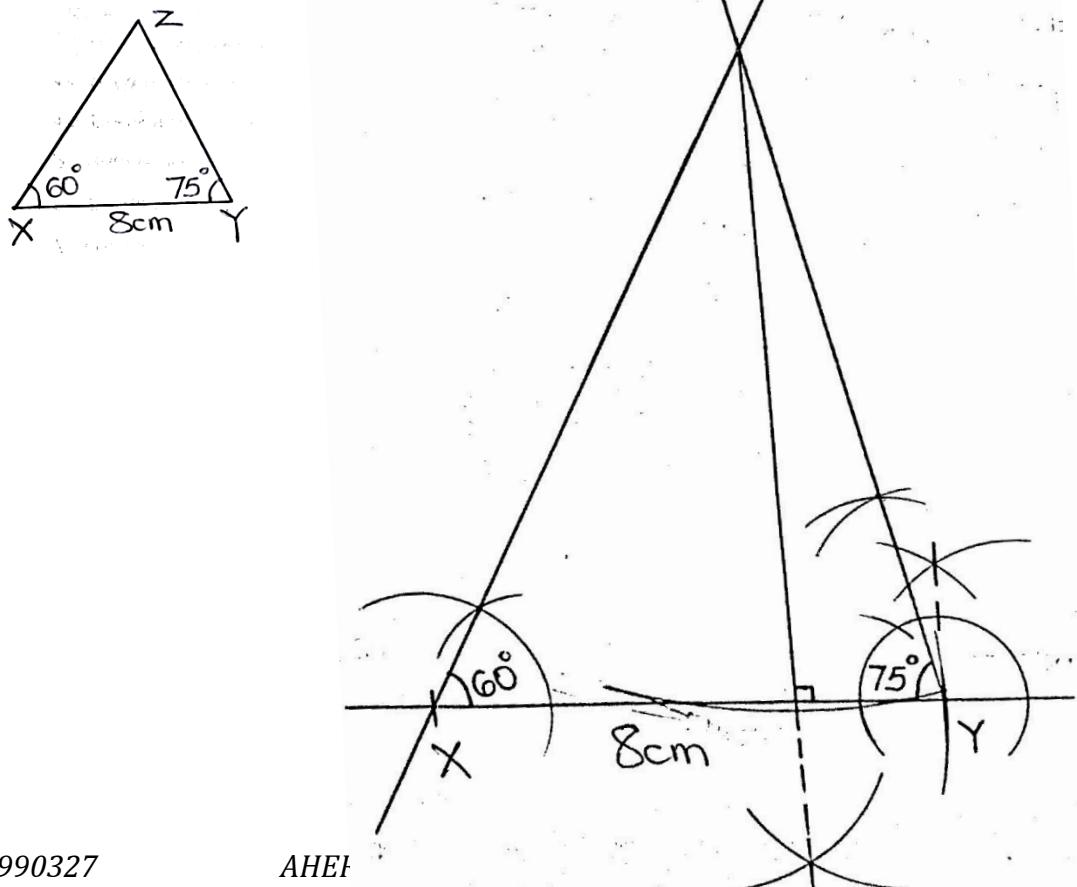


▲ Measure line RM

▲ Measure angle RPQ

SUB TOPIC: Constructing a triangle when given two angles and one side(ASA)

1. Construct triangle XYZ where XY=8cm, angle ZXY = 60° and angle XYZ= 75° . drop a perpendicular from Z to meet XY .



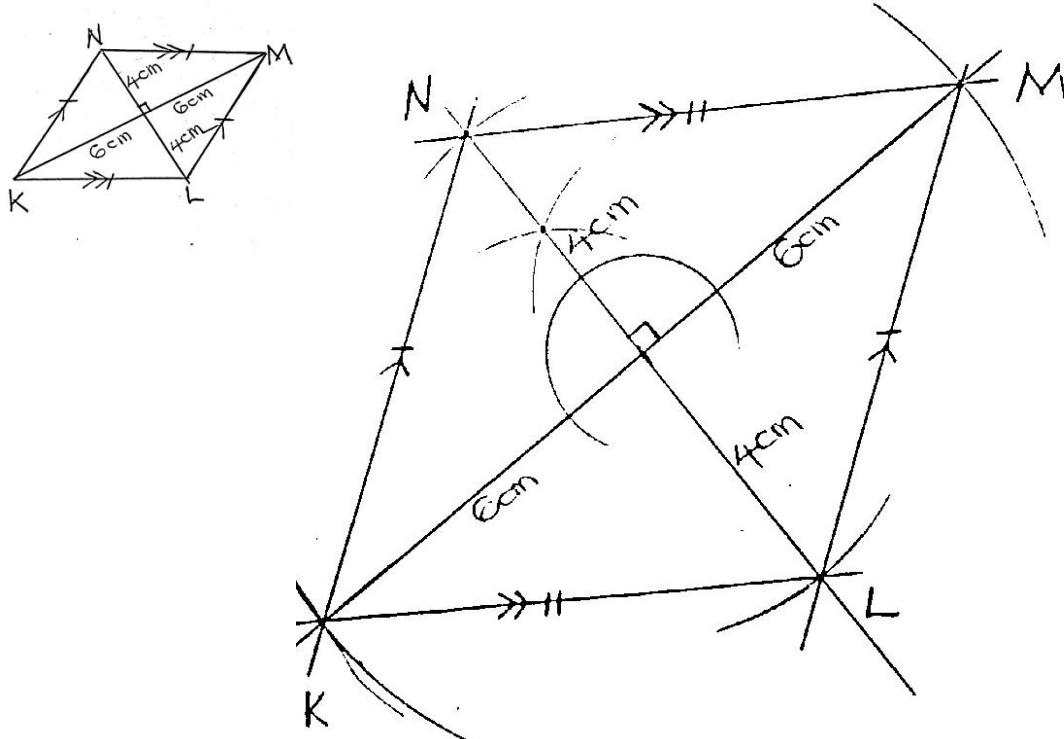
Mathematics is the Key

- ▲ **Measure line XZ**
- ▲ **Measure line YZ**
- ▲ **Measure the height of the triangle**
- ▲ **Find its area**

2. Construct a triangle RST where angle R = 60^0 angle S = 45^0 and RS = 5cm
Measure the length of ST and angle T.

SUB TOPIC: Constructing a rhombus when given diagonals

1. Construct rhombus KLMN where KM=12cm and LN=8cm.

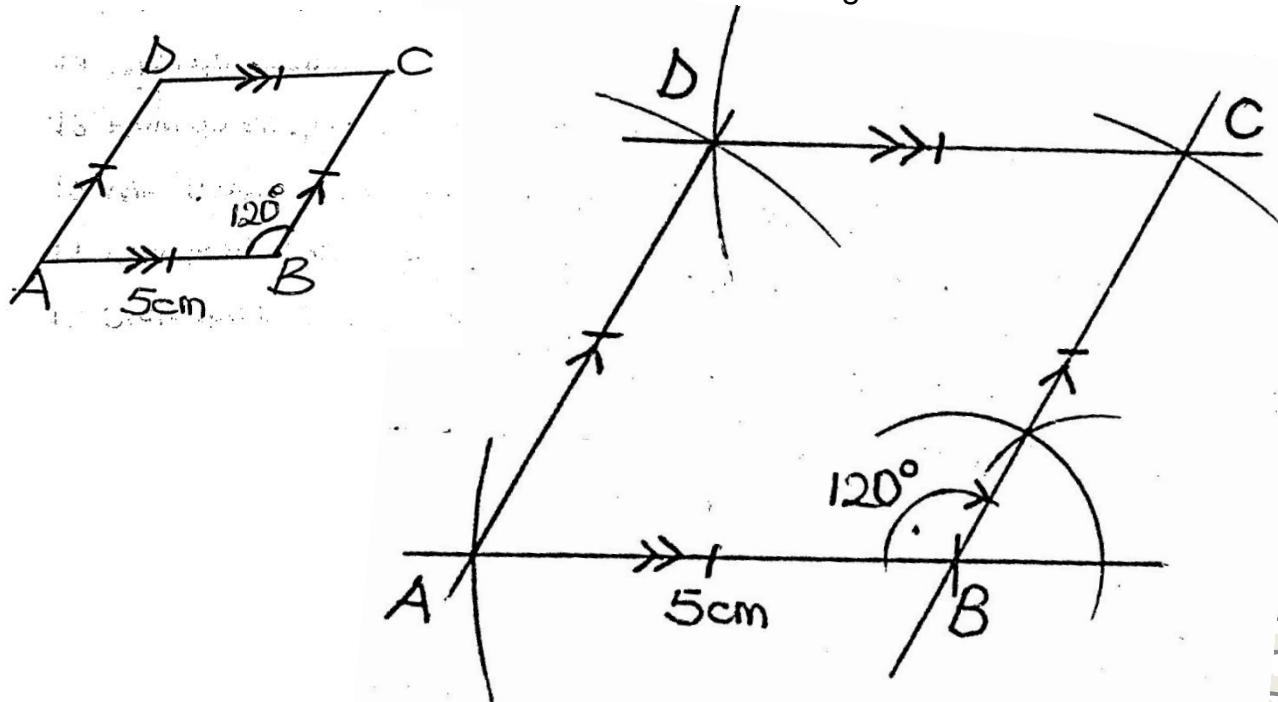


- ▲ **Measure line LM**
- ▲ **Measure angle NKL**
- ▲ **Measure angle MKN**
- ▲ **Measure angle KNL**

2. Construct a rhombus whose diagonals are 16cm and 12cm respectively.

SUB TOPIC: Constructing a rhombus when given an angle and a side

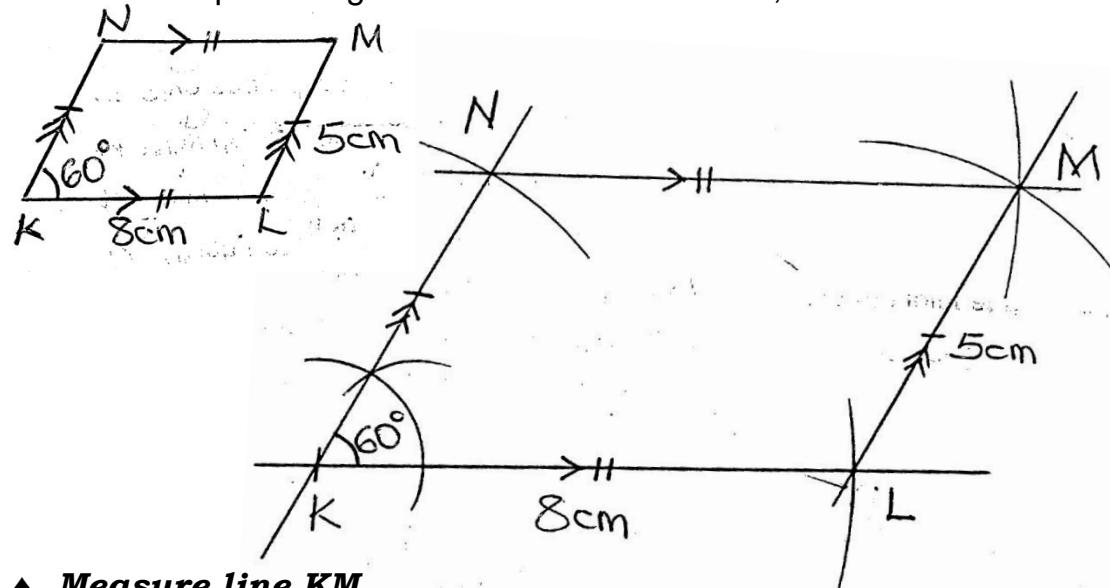
1. Construct rhombus ABCD where AB = 5cm and angle ABC=120°



- ▲ **Measure line AC**
- ▲ **Measure line BD**
- ▲ **Measure angle DAB**
- ▲ **Measure angle CAB**

SUB TOPIC: Constructing a parallelogram when given side and angle

1. Construct parallelogram KLMN where KL=8cm,LM=5cm and LKN=60°

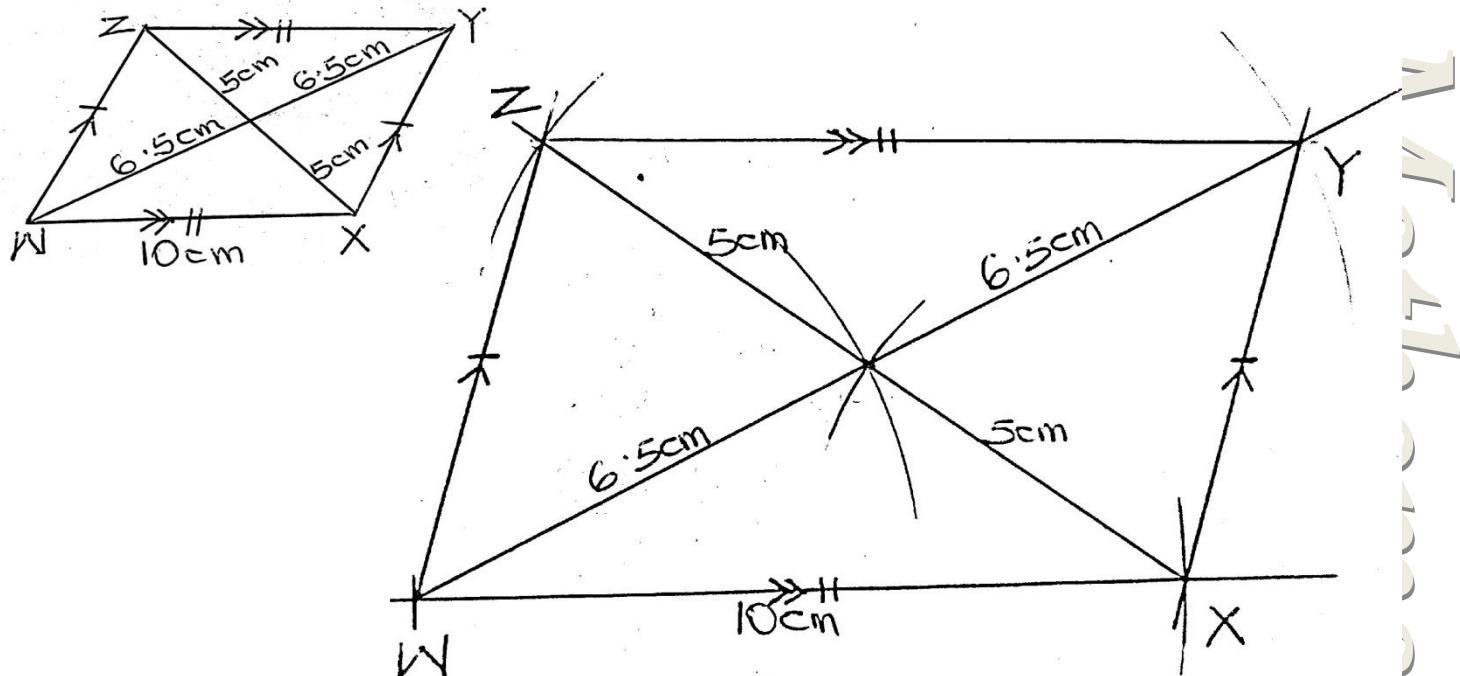


- ▲ **Measure line KM**
- ▲ **Measure line NL**
- ▲ **Measure angle MKL**
- ▲ **Measure angle KLM**

Mathematics is the key

SUB TOPIC: Constructing a parallelogram when given one side and diagonals

1. Construct parallelogram WXYZ where $WX = 10\text{cm}$, $WY = 13\text{cm}$ and $XZ = 10\text{cm}$.

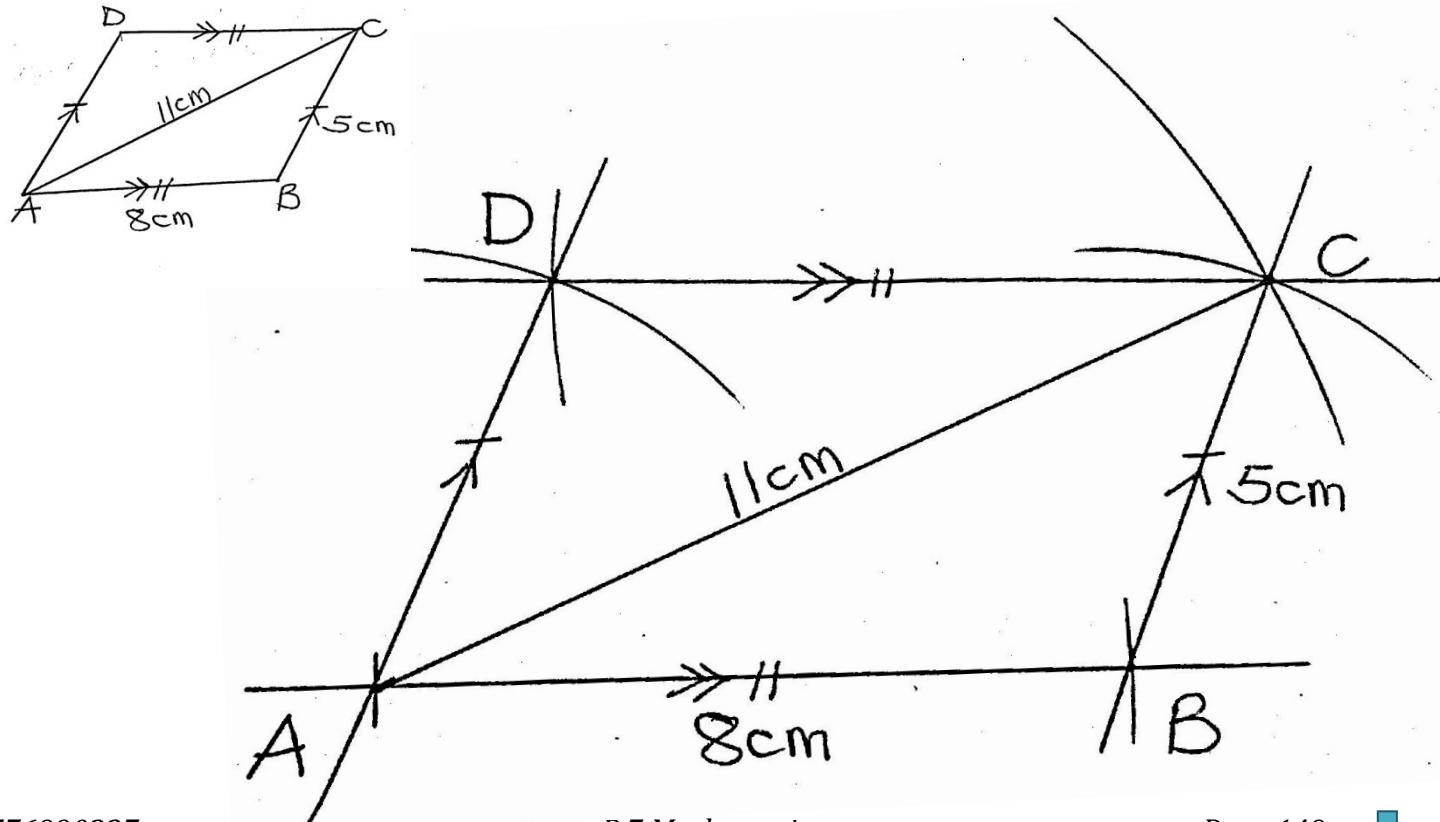


- ▲ **Measure line XY**
- ▲ **Measure angle YWX**
- ▲ **Measure angle WXY**
- ▲ **Measure angle WZX**

SOL

SUB TOPIC: Constructing a parallelogram when given sides and one diagonal

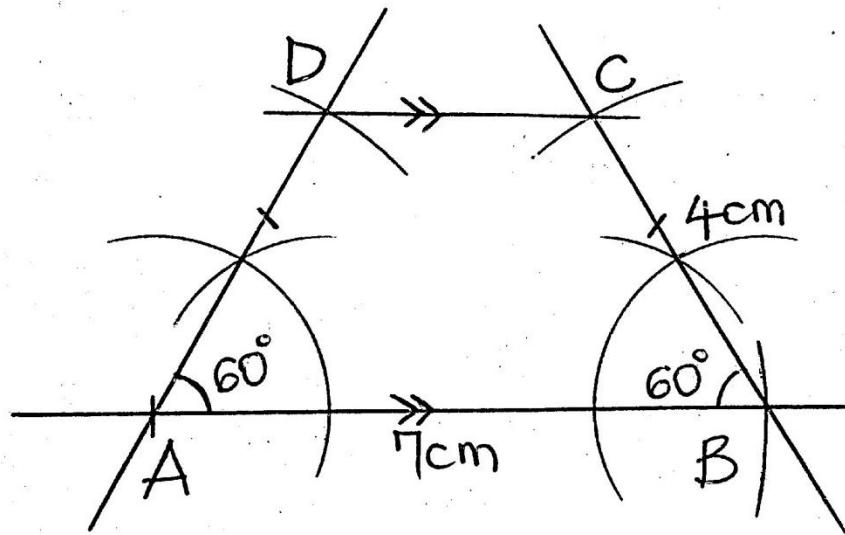
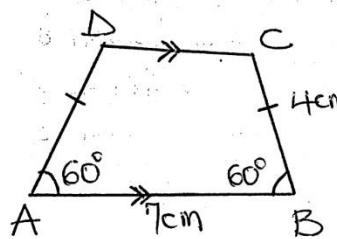
1. Construct parallelogram ABCD where $AB=8\text{cm}$, $BC=5\text{cm}$ and $AC=11\text{cm}$



- ▲ **Measure line BD**
- ▲ **Measure angle ABC**
- ▲ **Measure angle ABD**
- ▲ **Measure angle ACD**

SUB TOPIC: Constructing a trapezium

Construct quadrilateral ABCD where AB = 7cm, angle BAD =ABC=60°. Line AD=BC=4cm.



- ▲ **Measure line AC**
- ▲ **Measure line DC**
- ▲ **Measure angle ADC**
- ▲ **Measure angle BDA**

BEARING AND SCALE DRAWING

SUB TOPIC: Rotations/Revolutions/Complete turns

This is the act of turning around a centre or an axis

$$1 \text{ complete turn} / 1 \text{ rotation} / 1 \text{ revolution} = 360^\circ$$

Examples

- How many degrees are in two complete turns?

$$1 \text{ turn} = 360^\circ$$

$$\begin{aligned} 2 \text{ complete turns} &= 360^\circ \times 2 \\ &\equiv 720^\circ \end{aligned}$$

2. How many revolutions make up 1080° ?

$360^\circ = 1 \text{ revolution}$

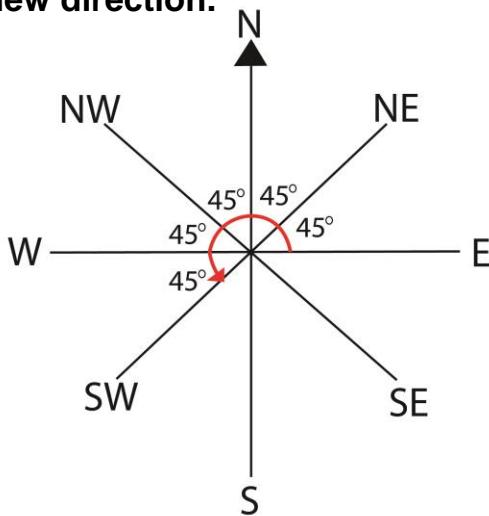
$$\begin{aligned} 1080^\circ &= \frac{1080^\circ}{360^\circ} \\ &= \frac{108}{36} \\ &\equiv 3 \text{ revolutions} \end{aligned}$$

3. How many degrees are in $\frac{1}{2}$ turn?

4. A boy made 4 complete turns. Through what angle did he turn?

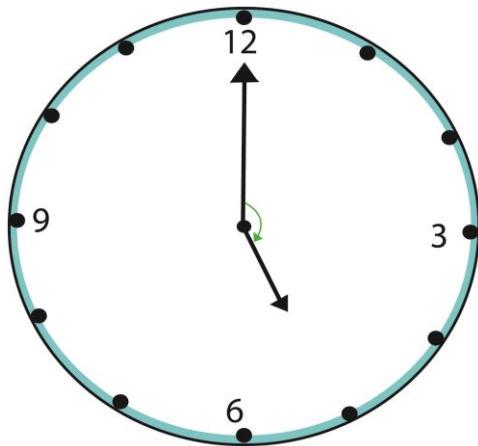
SUB TOPIC: Angles on a compass and a clock face

1. Kakuru was facing in East and turned anticlockwise through an angle of 225° . Find his new direction.



His new direction became South West

2. Calculate the smaller angle between the hands on the clock face below.



$$\frac{25}{60} \times 360^\circ$$

$$25 \times 6^\circ$$

$$\underline{150^\circ}$$

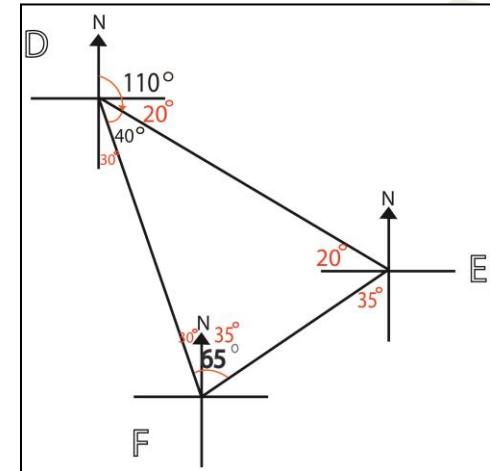
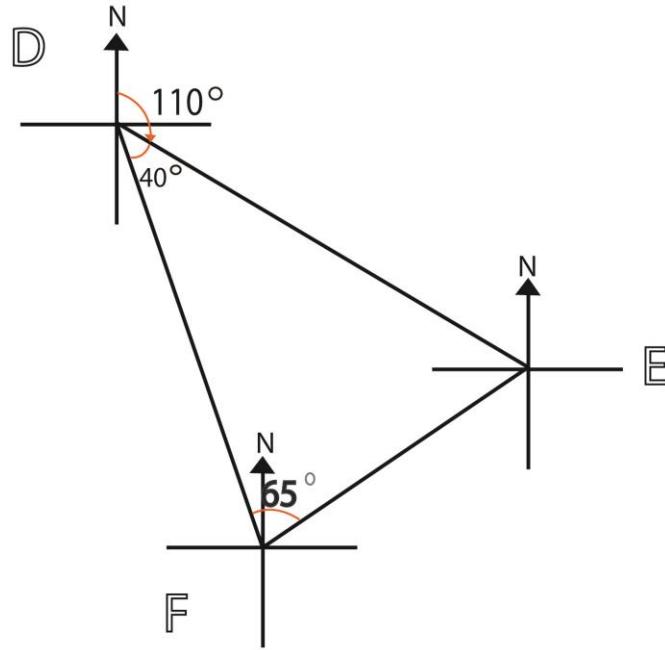
3. What angle can one turn after turning from South East to North in a clockwise direction?
4. What smaller angle is between West and North East?
5. Find the smaller angle between the North West and South West

SUB TOPIC: Ordinary bearing (directions)

NOTE

- ❖ Ordinary bearing (direction) is measured from either North or South but never from East or West
- ❖ The direction of P from Q is at point Q

1. Study the diagram below and use it to answer the questions that follow



What is the direction of;

a) F from E

$S35^{\circ}W$

b) E from D

$S70^{\circ}E$

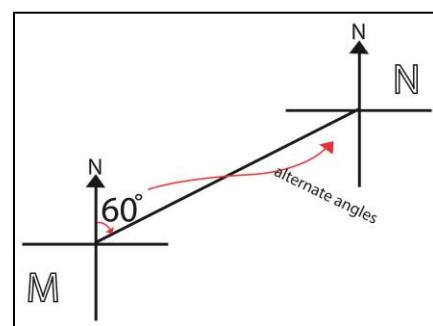
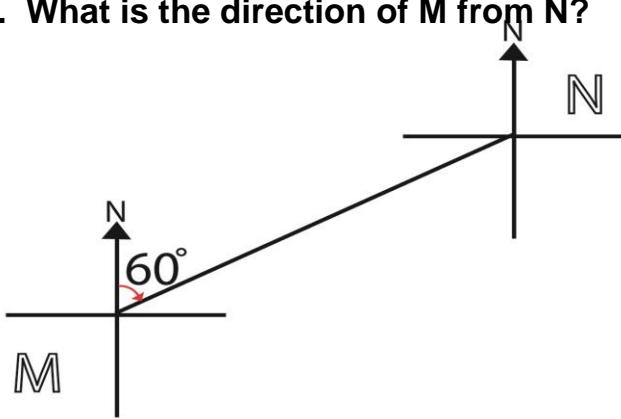
c) D from F

$N30^{\circ}W$

d) E from F

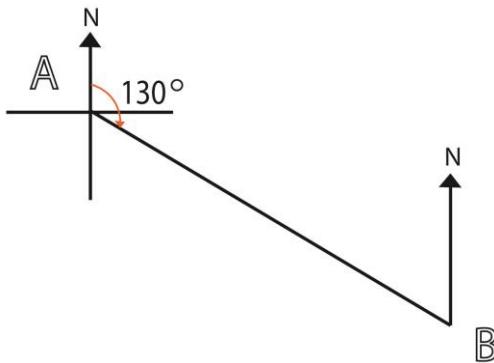
$N35^{\circ}E$

2. What is the direction of M from N?

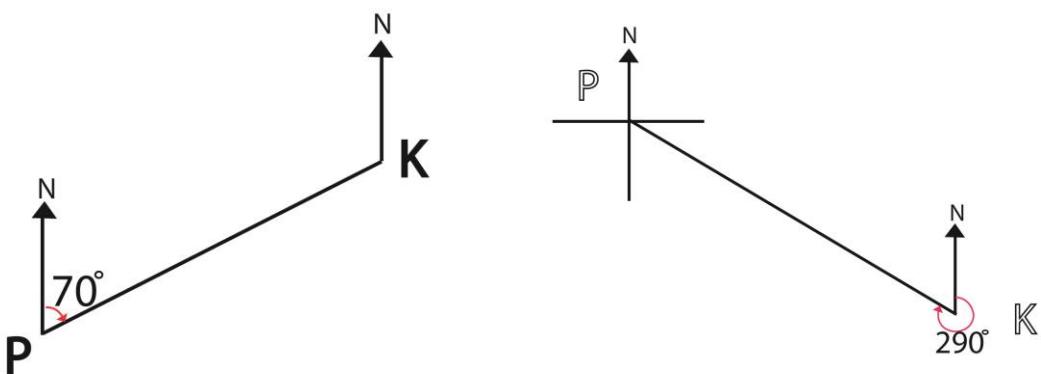


$S60^{\circ}W$

3. What is the direction of B from A?



4. What is the direction of K from P?

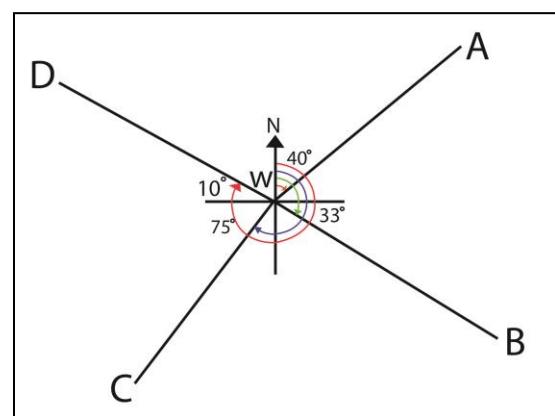
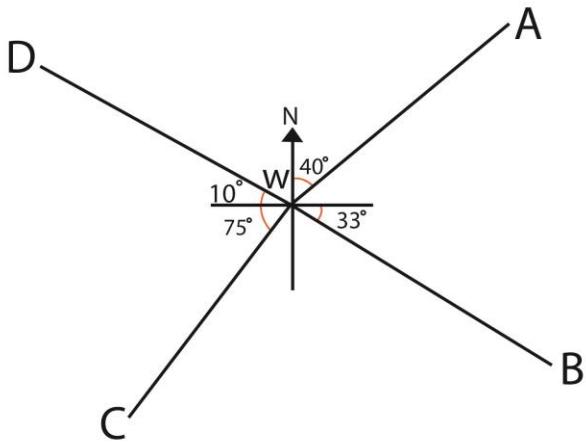


SUB TOPIC: True bearing

REMEMBER

- Bearing is measured from NORTH in a CLOCKWISE direction only.
- Bearing MUST be written in three digits i.e 030° , 000° , 126° etc
- The bearing of NORTH is 000° , 360°

1. Study the diagram below and use it to answer the questions that follow.



Find the bearing of;

a) A from W

$$040^\circ$$

The bearing of A from W is 040°

b) B from W

$$90^\circ + 33^\circ = 123^\circ$$

The bearing of B from W is 123°

c) C from W

$$90^\circ - 75^\circ = 25^\circ$$

$$180^\circ + 25^\circ = 205^\circ$$

The bearing of C from W is 205°

d) D from W

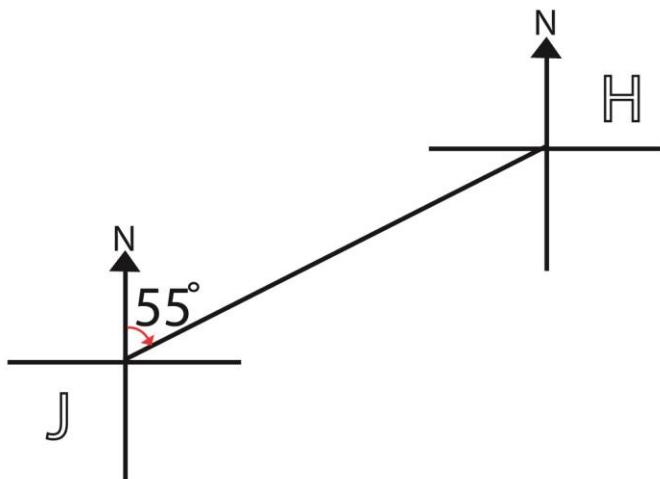
$$90^\circ + 90^\circ + 90^\circ + 10^\circ = 280^\circ$$

The bearing of D from W is 280°

SUB TOPIC: More about true bearing

Examples

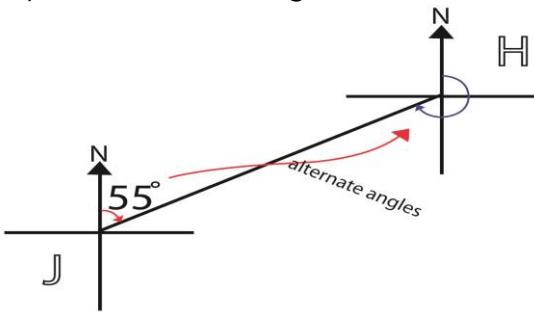
1. Study the diagram below



a) Find the bearing of H from J

The bearing of H from J is 055°

b) Find the bearing of J from H



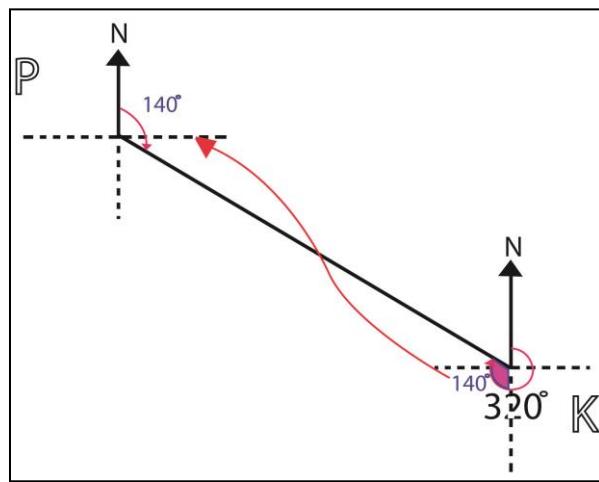
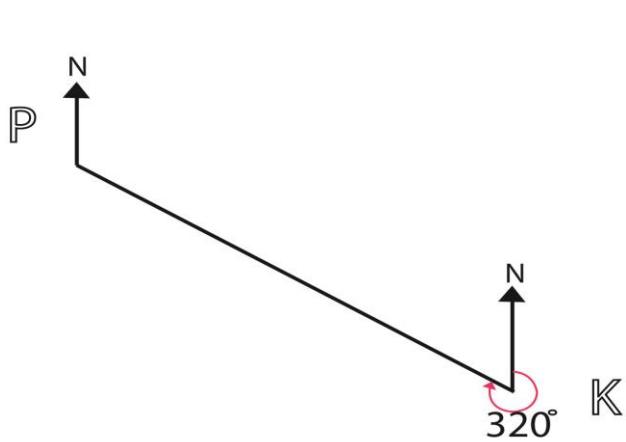
$$90^\circ + 90^\circ + 55^\circ$$

$$180^\circ + 55^\circ$$

$$135^\circ$$

The bearing of J from H is 235°

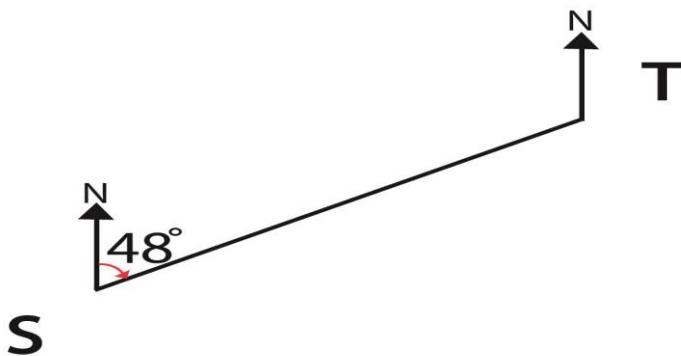
2. Use the diagram below to find the bearing of K from P



$$320^\circ - 180^\circ = 140^\circ$$

The bearing of K from P is 140°

3. Use the diagram below to find the bearing of S from T



SUB TOPIC: Opposite bearing

NOTE

- ❖ When the given bearing is less than 180° , to get its opposite bearing add 180° to it.
- ❖ When the bearing is greater than 180° , subtract 180° from it.

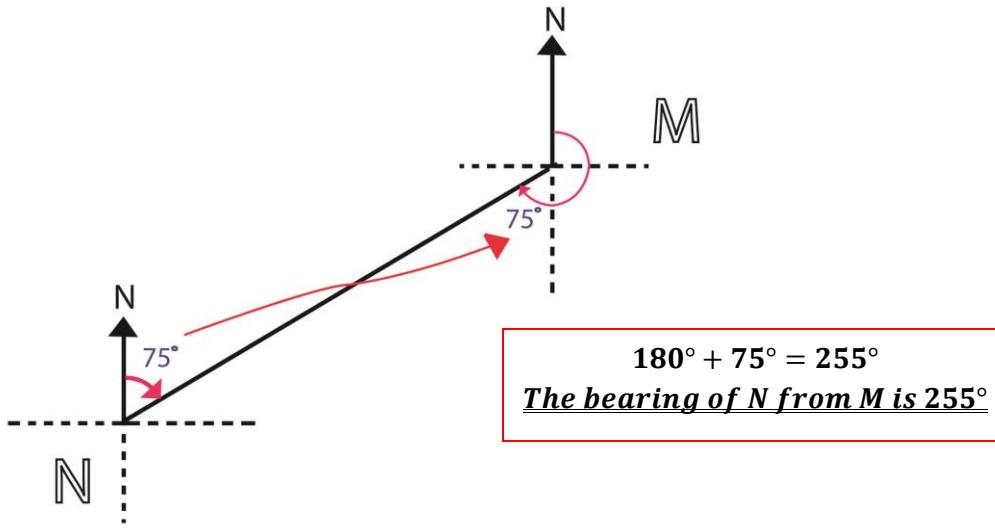
Try these

1. The bearing of A from B is 040° . Find the bearing of B from A.

$$180^\circ + 040^\circ = 220^\circ$$

The bearing of B from A is 220°

2. The bearing of M from N is 075° . Find the bearing of N from M.
(use a diagram)



3. The bearing of X from Y is 300° . Find the bearing of Y from X.

$$300^\circ - 180^\circ = 120^\circ$$

The bearing of Y from X is 120°

4. The bearing of K from P is 050° . Find the bearing of P from K.
5. The bearing of B from C is 250° . Find the bearing of C from B

Mathematics is the key

SUB TOPIC: Expressing distance in a given scale

Examples

1. The distance between two towns on a map is 3.5cm. Find the actual distance on the ground in km if the scale is 1:100,000.

1cm represents 100,000cm

3.5cm represent $3.5 \times 100,000\text{cm}$

$$\underline{\underline{350,000\text{cm}}}$$

cm to km

$$100,000\text{cm} = 1\text{km}$$

$$350,000\text{cm} = \frac{350,000}{100,000}\text{km}$$
$$= 3.5\text{km}$$

The actual distance is 3.5km

2. The actual distance between village A and B is 8.5 km. Find the distance between the two towns on a map if the scale is 1:1000,000.

km to cm

$$1\text{km} = 100,000\text{cm}$$

$$8.5\text{km} = 8.5 \times 100,000\text{cm}$$
$$= 850,000\text{cm}$$

1,000,000cm represent 1cm

$$850,000\text{cm represent } \frac{850,000}{1,000,000}$$
$$\underline{\underline{0.85\text{cm}}}$$

The distance on the map is 0.85cm

3. The distance between two ports on a map is 6cm. Calculate the scale used on that map if the actual distance is 120km on the ground.

km to cm

$$1\text{km} = 100,000\text{cm}$$

$$120\text{km} = 120 \times 100,000\text{cm}$$
$$= 12,000,000\text{cm}$$

$$6\text{cm}: 12,000,000\text{cm}$$

$$\frac{6\text{cm}}{6\text{cm}} : \frac{12,000,000\text{cm}}{6\text{cm}}$$

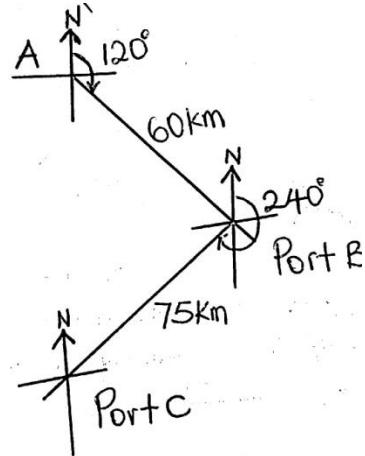
$$\underline{\underline{1:2,000,000}}$$

Mathematics is the Key

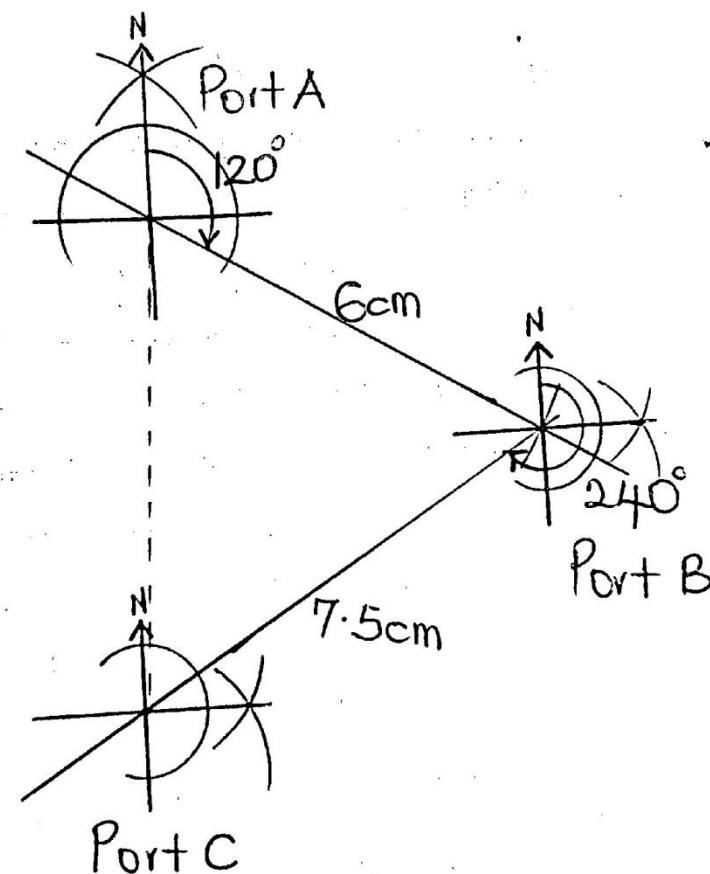
4. The distance between the church and the hospital on the map is 4.5cm. find the actual distance on the ground if 1cm represents 80m.

SUB TOPIC: Scale drawing

1. A ship left port A for port B on a bearing of 120° a distance of 60km. it then continued to port C on a bearing of 240° a distance of 75km. Using a scale of 1cm:10km. Draw an accurate diagram to show the three ports.



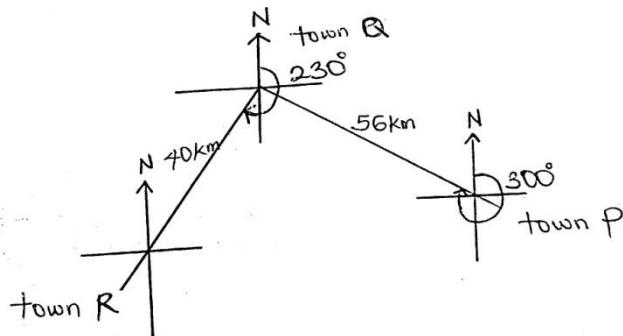
| | |
|---------------------|---|
| 1cm represents 10km | |
| 60km | $60\text{km} \div 10\text{km} = 6\text{cm}$ |
| 75km | $75\text{km} \div 10\text{km} = 7.5\text{cm}$ |



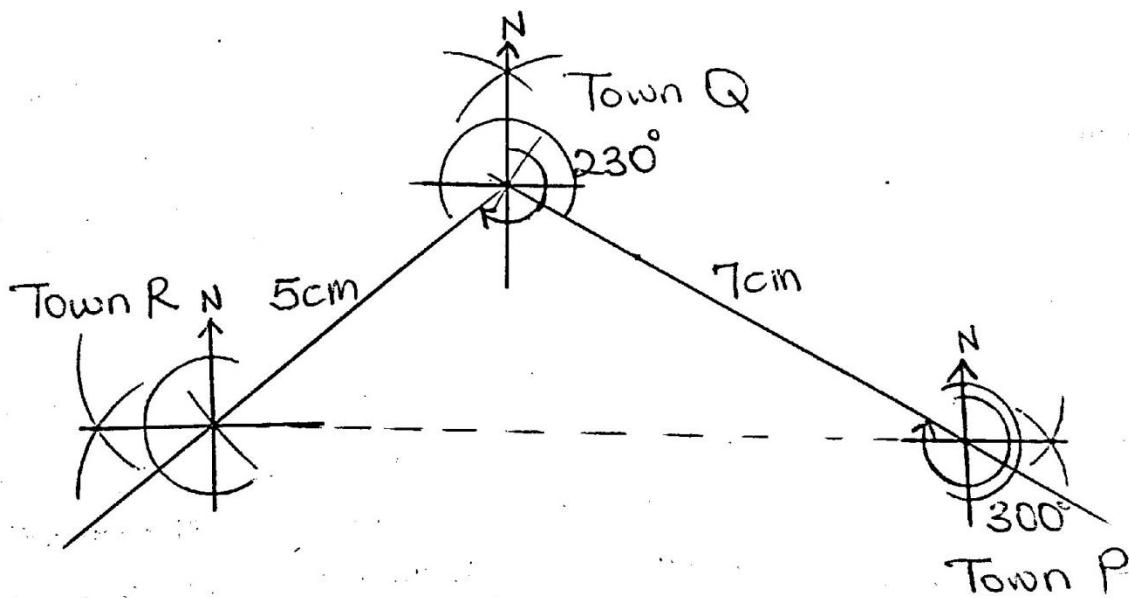
- ▲ Find the shortest distance from port A to port C.
- ▲ Find the bearing of port A from port C

2. A driver drove from town P on a bearing of 300° to town Q for a distance of 56km. the driver left town Q and drove on a bearing of 230° to town R for a distance of 40km.

Using a scale of 1cm to represent 8km, draw an accurate diagram to show the route of the driver.



| | |
|--------------------|--|
| 1cm represents 8km | |
| 56km | $56\text{km} \div 8\text{km} = 7\text{cm}$ |
| 40km | $40\text{km} \div 8\text{km} = 5\text{cm}$ |

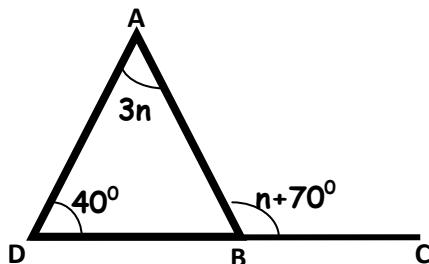


- ▲ Find the shortest distance from town P to town R.
- ▲ Find the bearing of Town R from Town P.

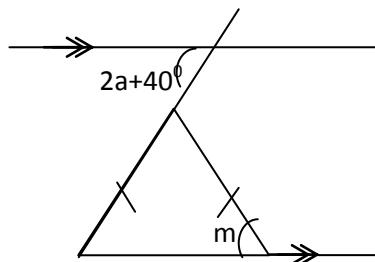
TOPICAL REVISION QUESTIONS:

Mathematics is the Key

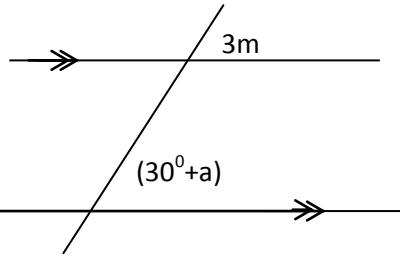
- With the help of a ruler and pair of compasses only, construct the following angles.
 - 30°
 - 45°
 - 75°
 - 120°
- Construct using a ruler and pair of compasses only the triangles with the following measurement.
 - Triangle ABC where $AB = 7\text{cm}$, $AC = 6\text{cm}$ and $BC = 5\text{cm}$
 - Triangle PQR where $PQ = 8\text{cm}$, $\angle Q = 120^\circ$ and $QR = 5\text{cm}$. Measure PR
- What is the smaller angle between West and South West.
- The bearing of a village P from town K is 049. What is the bearing of town K from village P.
- Construct a square WXYZ whose sides are 4.5cm.
- Each interior angle of a regular polygon is 120° .
 - Find the number of sides of the polygon.
 - Calculate its interior angle sum.
- How many degrees will Munduni turn through in $3 \frac{1}{4}$ revolutions?
- Town B is 60km South of town A and town C is 80km East of town B.
Draw an accurate diagram for the 3 towns and measure the shortest distance between A and C
- In the triangle ABC below, find the value of n



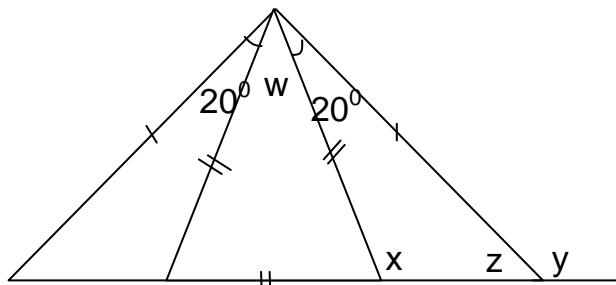
- The supplement of $(a+30)^\circ$ is 40° , find the value of a
- From the diagram below, angle $m = 3a$. Find the value of a



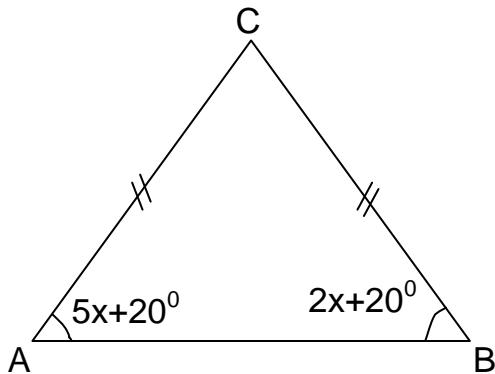
12. Given that $m = 2a$, find the value of a in degrees.



13. Calculate the size of angle w , x , y , z



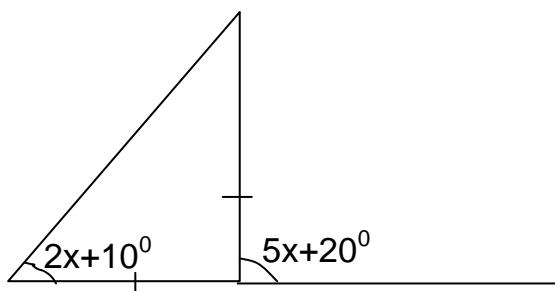
14. Use the figure below to answer the question the questions that follow.



(a) Find the value of x

(b) Find the size of angle ACB

15. find the value of x in degrees



TIME

SUB TOPIC: Conversion of 12 hour time to 24 hour time

Example

1. Change 2:00am to 24 hour clock

$$\begin{array}{r} 2:00\text{am} \\ +00:00 \\ \hline 02\ 00\ \text{hrs} \end{array}$$

2. Change 8:30pm to 24 hour lock

$$\begin{array}{r} 8:30\ \text{pm} \\ +12:00 \\ \hline 20\ 30\ \text{hrs} \end{array}$$

NOTE:

12 noon and 12 mid night is special time which means that we just state the answer as shown below.

12:30 am = 00:30 hrs

12:30 pm = 12:30hrs

3. Change the following time to 24hour clock.

- (a) 5:30am
(b) 4:18pm
(c) 12:12am

- (d) 12:19pm
(e) 11:11pm

REFERENCE

A New MK Primary Mathematics 2000 Bk 7 Pg 412 (New Edition)

SUB TOPIC: Changing 24 hour clock to 12 hour clock

Example

1. Write 0436 hrs in the 12-hour clock

$$\begin{array}{r} 04\ 36\ \text{hrs} \\ -00\ 00 \\ \hline 4:36\ \text{am} \end{array}$$

2. Write 2340 hrs in the 12-hour clock time

$$\begin{array}{r} 23\ 40\text{hrs} \\ -12\ 00 \\ \hline 11:40\ \text{pm} \end{array}$$

3. Write 1245hrs in 12 hour clock

1245hrs = 12:45 pm

4. Write 0045hrs in 12 hour clock

0045hrs = 12:45hrs

Mathematics is the Key

5. Write the following time in 12 hour clock.

- (a) **0319hrs**
- (b) **1529hrs**
- (c) **1256hrs**
- (d) **0013hrs**
- (e) **1943hrs**

REFERENCE

A New MK Primary Mathematics 2000 Bk 7 Pg 413 (New Edition)

SUB TOPIC: Finding duration

$$\text{Duration} = \text{Ending time} - \text{Starting time}$$

$$\text{Duration} = ET - ST$$

Example

1. A lesson started at 8:30 am and ended at 11:00 am. How long did the lesson take?

$$\begin{array}{r} 11:00 \text{ am} \\ - 8:30 \text{ am} \\ \hline 2:30 \end{array} \quad \begin{array}{l} 2\text{hours } 30\text{minutes} \\ 2\frac{30}{60}\text{hours} = 2\frac{1}{2}\text{hours} \end{array}$$

2. A bus left Nairobi at 1315 hours and arrived in Kampala at 1630 hrs. How long did the journey take?

$$\begin{array}{r} 1630 \text{ hrs} \\ - 1315 \text{ hrs} \\ \hline 3 \ 15 \end{array} \quad \begin{array}{l} 3\text{hours } 15\text{minutes} \\ 3\frac{15}{60}\text{ hours} = 3\frac{1}{4}\text{ hours} \end{array}$$

3. A party started at 2000hrs and ended at 11:30pm. How long did the party last? (Express 11:30pm in 24 hr-clock)

$$\begin{array}{r} 11:30\text{pm} \\ + 12:00\text{hrs} \\ \hline 2330\text{hrs} \end{array} \quad \begin{array}{r} 200\text{hrs} \\ - 200\text{hrs} \\ \hline 3:30 \end{array}$$

The party lasted for 3 hours and 30 minutes.

Mathematics is the Key

4. A baby slept at 10:00pm and woke up at 3:30 am. How long did the baby sleep?

10:00pm to 12:00 mid night

$$\begin{array}{r} 12:00 \\ +10:00 \\ \hline 2:00 \end{array}$$

Total time

$$\begin{array}{r} 2:00 \\ +3:30 \\ \hline 5:30 \end{array}$$

The baby slept for 5 hours 30 minutes

5. A man started his journey at 6:35am and reached the destination at 10:00am. how long did the journey take?
 6. A motorist left town A at 11:00am and reached town B at 3:00pm. How long did he take to move from tow A to town B?
 7. Jamil started digging at 6:50am and ended at 1000hrs. How long did he take digging?
 8. How many hours are their between 8:00pm to 3:00am?

SUB TOPIC: More problems on duration

REMEMBER

$$\text{Duration} = ET - ST$$

$$ET = ST + \text{Duration}$$

$$ST = ED - \text{Duration}$$

Examples

1. A 45 minute lesson ended at 5:20pm. At what time did the lesson start?

$$ST = ET - \text{Duration}$$

$$\begin{array}{r} 5:20pm \\ -00:45 \\ \hline 4:35pm \end{array}$$

2. Hope started the journey at 8:00am and took 1hr 30minutes. At what time did the journey end?

$$ED = ST + \text{Duration}$$

$$\begin{array}{r} 8:00am \\ +1:30 \\ \hline 9:30am \end{array}$$

3. A motorist moved for 3hours from town A to Town B. if he reached town B at 7:30 pm, at what time did he start the journey?
 4. Mercy started revising at 5:45am and took $2\frac{1}{2}$ hours. At what time did he end the revisions?

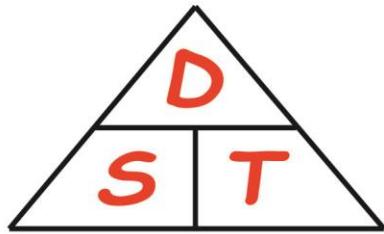
Mathematics is the key

5. A truck moved for 5 hours and reached the destination at 2:00am. At what time did he start the journey?

REFERENCE

A New MK Primary Mathematics 2000 Bk 7 Pg 414 (New Edition)

SUB TOPIC: Finding Distance



$$Distance = S \times T$$

$$Speed = \frac{D}{T}$$

$$Time = \frac{D}{S}$$

Distance is measured in km or m

Examples

1. Alex moved from town A to town B at a speed of 40km/hr for 2hours. How far is town A from town B?

$$\begin{aligned} D &= S \times T \\ &= \frac{40\text{km}}{\text{hr}} \times 2\text{hrs} \\ &= 40\text{km} \times 2 \\ &= \underline{\underline{80\text{km}}} \end{aligned}$$

2. A car travelled for $2\frac{1}{2}$ hours at a speed of 80km/hr. How far did he move?

$$\begin{aligned} D &= S \times T \\ &= \frac{80\text{km}}{\text{hr}} \times 2\frac{1}{2}\text{hrs} \\ &= 80\text{km} \times \frac{5}{2} \\ &= 40\text{km} \times 5 \\ &= \underline{\underline{200\text{km}}} \end{aligned}$$

3. A bus travelled from town Q to town R for 6 hours at a speed of 65km/hr. What is the distance between town Q and R?
4. Allen moved from town Y at 4:30pm and reached town X at 5:00pm. If she was moving at a speed of 120km,
- (a) How long did he take travelling?
- (b) How far is town X from town Y?

Mathematics is the key

SUB TOPIC: Finding Speed

The units for speed are km/hr or m/s

Examples

- Kagoma takes 45 minutes to drive from home to town a distance of 30km.
Calculate his speed in km/hr.

$$\begin{aligned} \text{Speed} &= \frac{\text{distance}}{\text{time}} \\ &= 30\text{km} \div \frac{45}{60} \text{ hrs} \\ &= 30\text{km} \times \frac{60}{45} \text{ hrs} \\ &= \underline{\underline{40\text{km/hr}}} \end{aligned}$$

- James covered a distance of 80km in just 2 hours. At what speed was he moving?
- A bus moved for $2\frac{1}{2}$ hours from town A to town B. If the distance from town a to town b is 100km, find the speed at which the bus was moving.
- Daniel covered 45km in only 45 minutes. Find his speed in km/hr.

SUB TOPIC: Finding Time

Examples

- A driver covered 60km at a speed of 15km/hrs. How long did he take travelling?

$$\text{Time} = \frac{D}{S}$$

$$\begin{aligned} \text{Time} &= \frac{60\text{km}}{15\text{km/hr}} \\ \text{Time} &= \underline{\underline{4 \text{ hours}}} \end{aligned}$$

- A boy moved a distance of 180m at a speed of 2m/s. How many seconds did he take to cover the distance?

$$\begin{aligned} \text{Time} &= \frac{D}{S} \\ \text{Time} &= \frac{180\text{m}}{2\text{m/s}} \\ \text{Time} &= \underline{\underline{90 \text{seconds}}} \end{aligned}$$

- Calculate the time taken to cover 80km at a speed of 20km/hr
- Amon travelled from home to school at a speed of 80km/hr which is a distance of 120km. How long did he take to reach school?
- A truck moving at 150km/hour covered a distance of 450km. how long did the journey take?

Mathematics is the key

SUB TOPIC: Changing km/hr to m/s and vice versa

Example

1. Change 10m/s to km /hr

$$10\text{m/s} = \frac{10\text{m}}{1\text{s}}$$

$$1 \text{ hour} = 3600 \text{hrs}$$

$$1 \text{ km} = 1000 \text{m}$$

$$\begin{aligned}10\text{m/s} &= \frac{10 \div 1000}{1 \div 3600} \\&= \frac{10}{1000} \div \frac{1}{3600} \\&= \frac{10}{1000} \times \frac{3600}{1} \\&= \underline{\underline{36 \text{ km/hr}}}\end{aligned}$$

2. Change 90km/hr to m/s

$$\begin{aligned}90\text{km/hr} &= \frac{90\text{km}}{1\text{hr}} \\&= \frac{90 \times 1000}{1 \times 3600} \\&= \underline{\underline{25 \text{ m/s}}}\end{aligned}$$

3. Change the following as instructed

(a) **15 m/s to km/hr**

(b) **72km/hr to m/s**

(c) **40m/s to km/hr**

(d) **108km/hr to m/s**

REFERENCE

A New MK Primary Mathematics Bk 7 pg 331 (old edition)

SUB TOPIC: Finding the average speed

1. Dungu travelled from town A to town B at a speed of 60km/hr for $3\frac{1}{2}$ hours. Then he went to town C from B at a speed of 80km/hr in $1\frac{1}{2}$ hrs . Calculate the average speed for the whole journey.

$$\text{Average speed} = \frac{TDC}{TTT}$$

Distance 1

$$D = S \times T$$

$$\begin{aligned}&= 60\text{km/hr} \times 3\frac{1}{2}\text{hrs} \\&= 60 \times \frac{7}{2} \text{km} \\&= 30 \times 7 \text{km} \\&= \underline{\underline{210\text{km}}}\end{aligned}$$

Distance 2

$$D = S \times T$$

$$\begin{aligned}&= 80\text{km/hr} \times 1\frac{1}{2}\text{hrs} \\&= 80 \times \frac{3}{2} \text{km} \\&= 40 \times 3 \text{km} \\&= \underline{\underline{120\text{km}}}\end{aligned}$$

$$TDC = 210\text{km} + 120\text{km} = 330\text{km}$$

$$TTT = 1\frac{1}{2}\text{hrs} + 3\frac{1}{2}\text{hrs} = 5\text{hrs}$$

$$\begin{aligned}\text{Average speed} &= \frac{330\text{km}}{5\text{hrs}} \\&= \underline{\underline{66 \text{ km/hr}}}\end{aligned}$$

Mathematics is the key

2. A bus driver left town **A** at 6:00am driving at an average speed of 30km/hr for 2 hours to town **B**. he stopped at **B** for 30minutes and then left for **C** driving at 60km/hr for $\frac{1}{2}$ hours. He stopped at C for $\frac{1}{2}$ an hour and then drove back at 140km/hr.
 - (a) Calculate his average speed.
 - (b) At what time did he reach town C.
3. A bus driver left town **A** at 7:30am driving at an average speed of 70km/hr for 2 hours to town **B**. he stopped at **B** for an hour and then left driving at 35 km/hr back to town **A**. Calculate his average speed.
4. A bus driver left town **R** at 6:40am driving at an average speed of 25km/hr for 2 hours to town **S**. He stopped at **S** for an hour and then left for **T** driving at 30km/hr for 3hours. Calculate his average speed for the whole journey.

SUB TOPIC: School Time Table

Example:

1. Study the time table below for a P.6 class in Kyebando Primary School and answer the questions that follow.

| | | | | | | | | | |
|-------------|------------|------------|----------|-------------|-------------|--------------|----------|-------------|-------------|
| From | 8:30 am | 9:10 am | 9:50 Am | 10:30 Am | 11:10 Am | 11:50 Am | 12:30 pm | 2:00 pm | 2:40 pm |
| To | 9:10 am | 9:50 am | 10:30 Am | 11:10 Am | 11:50 am | 12:30 pm | 2:00 pm | 2:40 pm | 3:20 pm |
| MON | MTC | ENG | | PAPE | PAPE | R.E | | PAPE | PAPE |
| TUE. | SCI | MTC | | R.E | R.E | ENG | | MDD | MDD |
| WED. | SST | ENG | | IPS | SCI | SCI | | SST | SST |
| THUR | ENG | SCI | | MTC | MTC | L.LAG | | ENG | ENG |
| FRI | MTC | MTC | | KISW | ENG | SCI | | R.E | MTC |
| | | | | | | | | IPS | IPS |

- (i) How long does each lesson last?

$$9:10^{70}\text{am} \quad (60 + 10) = 70 \text{ minutes}$$

$$\underline{-8:30 \text{ am}}$$

$$\underline{\underline{40}}$$

Each lesson lasts for 40 minutes

- (vi) At what time does break end?

$$\underline{10:30\text{am}}$$

- (iii) For how long do the pupils take studying Science the whole week?

$$\underline{5 \text{ lessons} \times 40 \text{ minutes} = 200 \text{ minutes}}$$

SUB TOPIC: Taxi and bus time tables

Example

- The table shows the departure and arrival time of a taxi at given stations.
Study it and answer the questions that follow:

| Station | Arrival | Departure |
|---------|---------|-----------|
| Tororo | | 6:00am |
| Iganga | 7:30am | 7:45am |
| Jinja | 8:35am | 8:50am |
| Kampala | 10:50am | |

- How long did the taxi take to move from Tororo to Iganga?
Time of arrival – Time of departure

$$\begin{array}{r}
 7:30\text{am} \\
 - 6:00\text{am} \\
 \hline
 1:30
 \end{array}$$

It took 1 hour 30 minutes

- How long was the taxis stopover in Jinja?

$$\begin{array}{r}
 8:50\text{am} \\
 - 8:35\text{am} \\
 \hline
 0:15
 \end{array}
 \quad \text{It was 15 minutes}$$

- How long did the taxi take to move from Iganga to Kampala?

$$\begin{array}{r}
 10 : 50 \text{ am} \\
 - 7 : 45 \text{ am} \\
 \hline
 3 : 15
 \end{array}$$

It took 3 hours and 15 minutes

SUB TOPIC: Train timetables

Example

- The tables below shows the departure, the arrival time and the fares for a train from Mityana to Tororo. Study the table carefully:

| Station | Arrival | Departure |
|---------|---------|-----------------|
| Mityana | | 11:00pm |
| Bujjuko | 11:45pm | 12:00 Mid night |
| Kampala | 12:30am | 12:45am |
| Jinja | 1:30am | 1:40am |
| Iganga | 2:10am | 2:30am |
| Tororo | 3:30am | |

Table II:

Mty

| | | | | | | |
|-------------|-------------|-------------|-------------|-------------|------------|--|
| 500 | BJK | | | | | |
| 1000 | 500 | Kla | | | | |
| 1600 | 1100 | 1000 | JNJ | | | |
| 2600 | 2100 | 2000 | 1000 | ING | | |
| 3600 | 3100 | 3000 | 2000 | 1000 | TRR | |

- (a) How long does the train take to move from Mityana to Kampala?

12:30am

- 11:00pm

1:30

1 hour and 30 minutes

- (e) Three tourists boarded the train from Kampala to Iganga. How much did they pay?

Solution: Kampala to Iganga costs shs 2,000

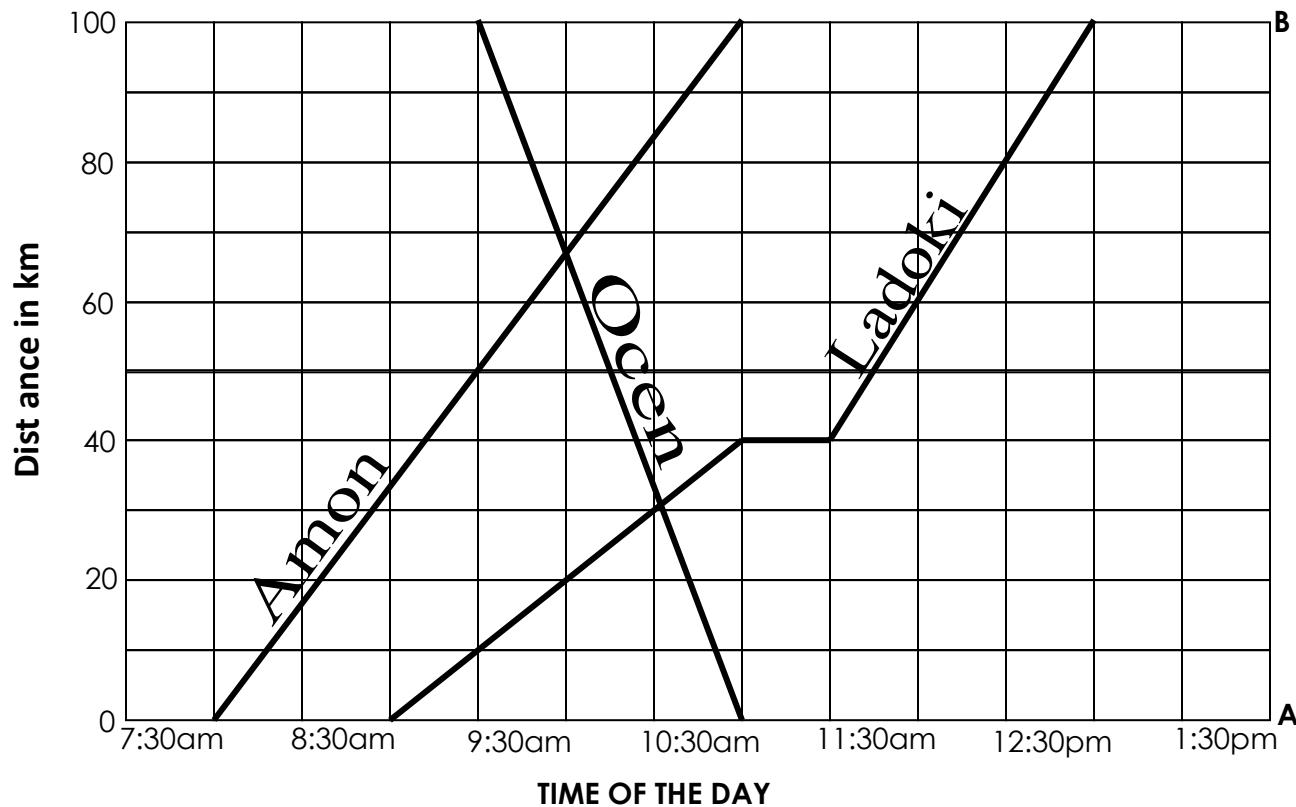
Sh.2000 X 3 = shs 6,000

SUB TOPIC: INTERPRETING TRAVEL GRAPHS (Distance Time graph)

A travel graph is one which shows the distance travelled in a period of time
Time is shown on the horizontal axis and distance is shown on the vertical axis.

Example1

The graph below shows 3 people who moved between town A and town B. Amon started from town A at 8:00 am to town B, Ladoki started the journey at 9:00am to town B and Ocen started the journey fom B at 9:30am to town A .



Questions

- ii. What is the scale on the horizontal axis.?

One small square represents 30 minutes

- iii. What is the scale on the vertical axis?

One small square represents 10 km

- iv. Find the average speed for Ladoki.

$$\text{Average speed} = \frac{TDC}{TTT}$$

$$TDC = 100 \text{ km}$$

$$TTT = 4 \text{ hours}$$

$$\begin{aligned} \text{Average speed} &= \frac{100 \text{ km}}{4 \text{ hrs}} \\ &\underline{\underline{= 25 \text{ km/hr}}} \end{aligned}$$

- v. How many hours did Amon take to complete her journey?

3hours

- vi. At what time did Amon meet Ocen?

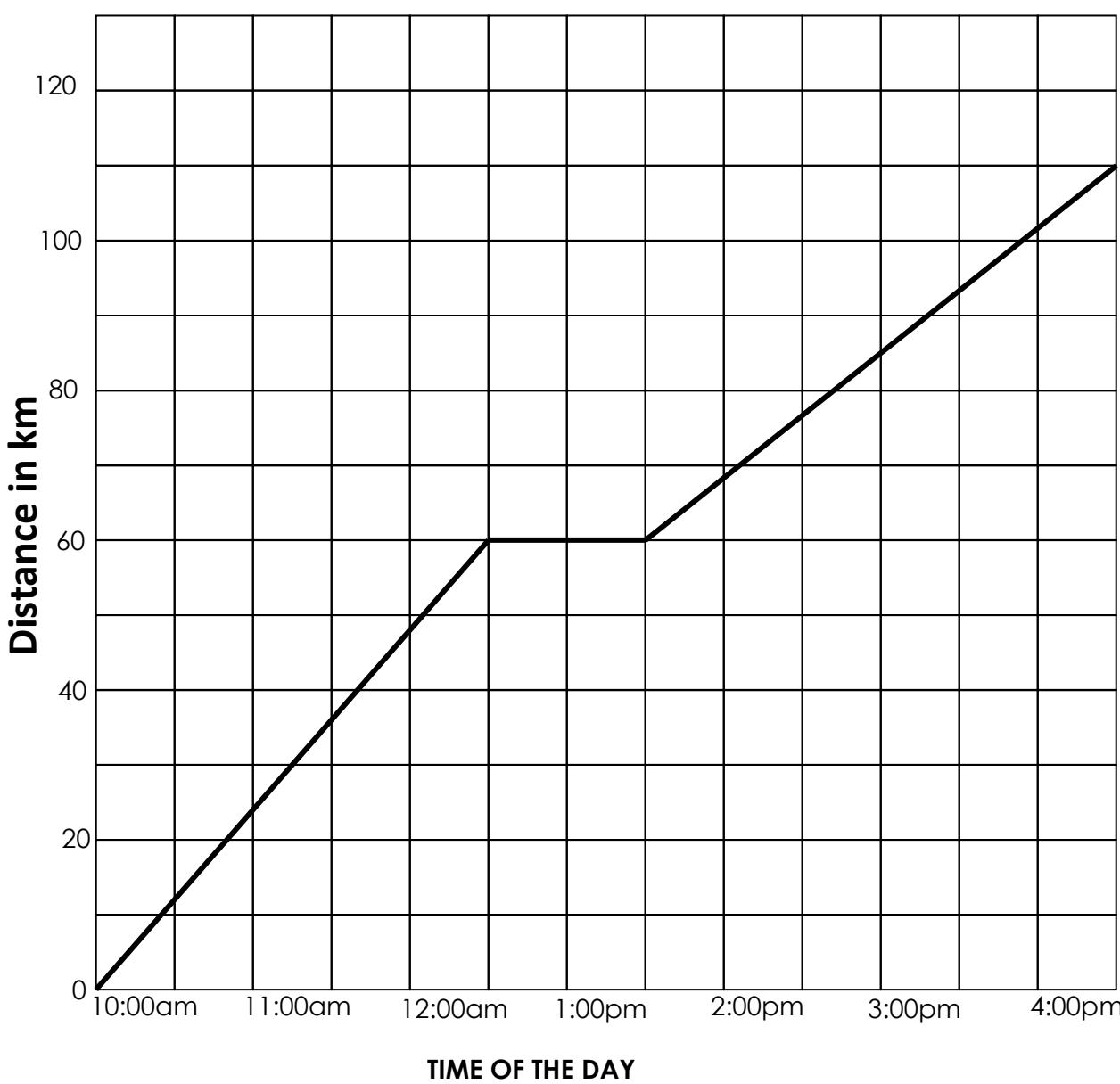
At 10:00am

- vii. How many hours earlier did Amon arrive at town B before Ladoki?

2 hours

Example 2

The graph below shows how the driver moved from ASA town to OMU town via EKO town. Use it to answer the questions that follow.



Questions

- What is the scale on the vertical axis?
1 small square represents 10km
- What is the scale on the horizontal axis?
1 small square represents 30 minutes
- At what time did he start the journey?
At 10:00am
- At what time did he reach OMU?
At 4:30pm
- How long did he take resting?
1 hour
- How far is ASA from OMU?

110km

g) How long did he take to move from ASA to EKO?

2hours 30minutes

h) What is the distance from EKO to OMU?

i) At what speed was he moving from ASA to OMU?

j) Find his average speed for the whole journey.

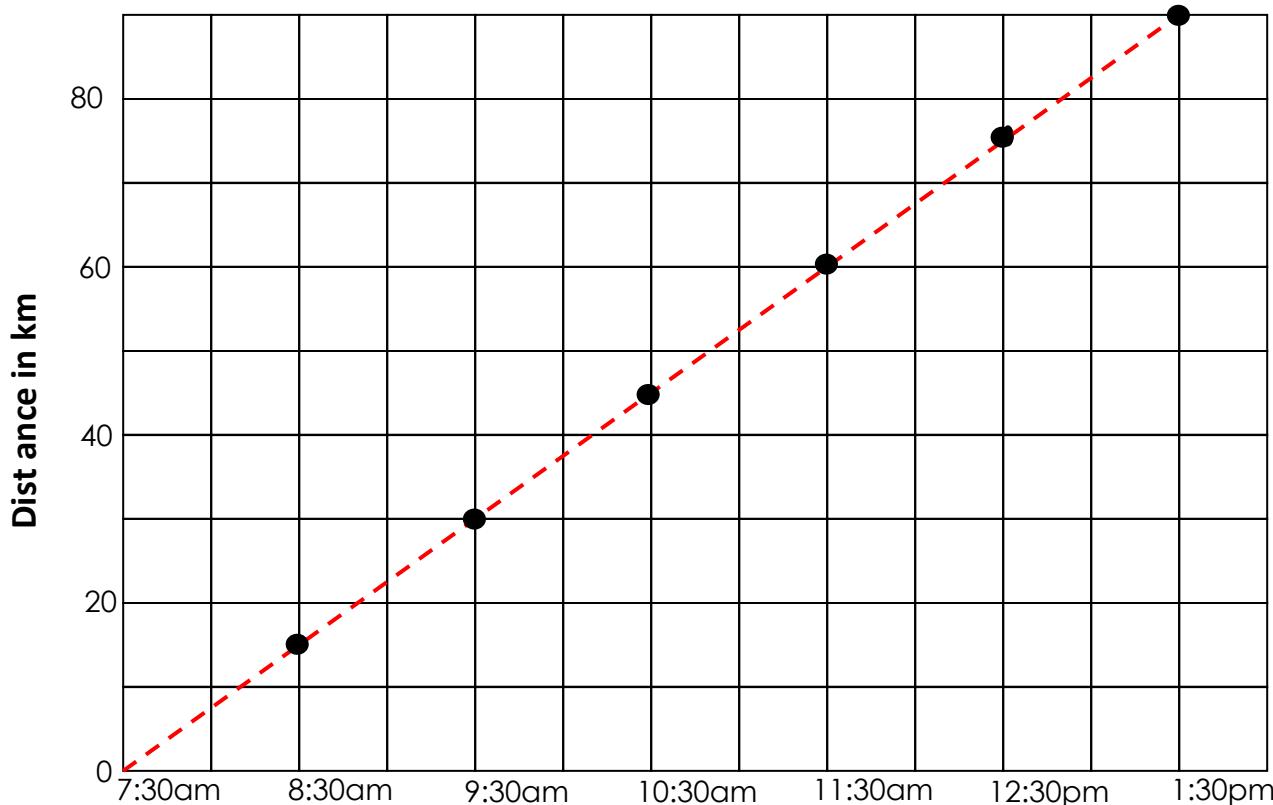
SUB TOPIC: DRAWING TRAVEL GRAPHS

Example 1:

Mukasa covered a journey in 6 hours traveling at 15 K.P.H. Show the journey on the grid if he started the journey at 7:30am.

| | | | | | | | |
|------|-----------|---------------------|---------------------|---------------------|---------------------|---------------------|---------------|
| KM | 0^{+15} | 15km^{+15} | 30km^{+15} | 45km^{+15} | 60km^{+15} | 75km^{+15} | 90km |
| Time | 0^{+1} | 1 hr^{+1} | 2hrs^{+1} | 3hrs^{+1} | 4 hrs^{+1} | 5hrs^{+1} | 6hrs |

A graph representing Mukasa's journey.



Example 2

TIME OF THE DAY

Town M is 150km from town G. A motorcyclist started the journey from town M at 10:30am .He was travelling at a speed of 25km/hr for 2 hours. he rested for 30 minutes and then continued at a speed of 50km/hr for the rest of the journey to town G.

Mathematics is the key to success

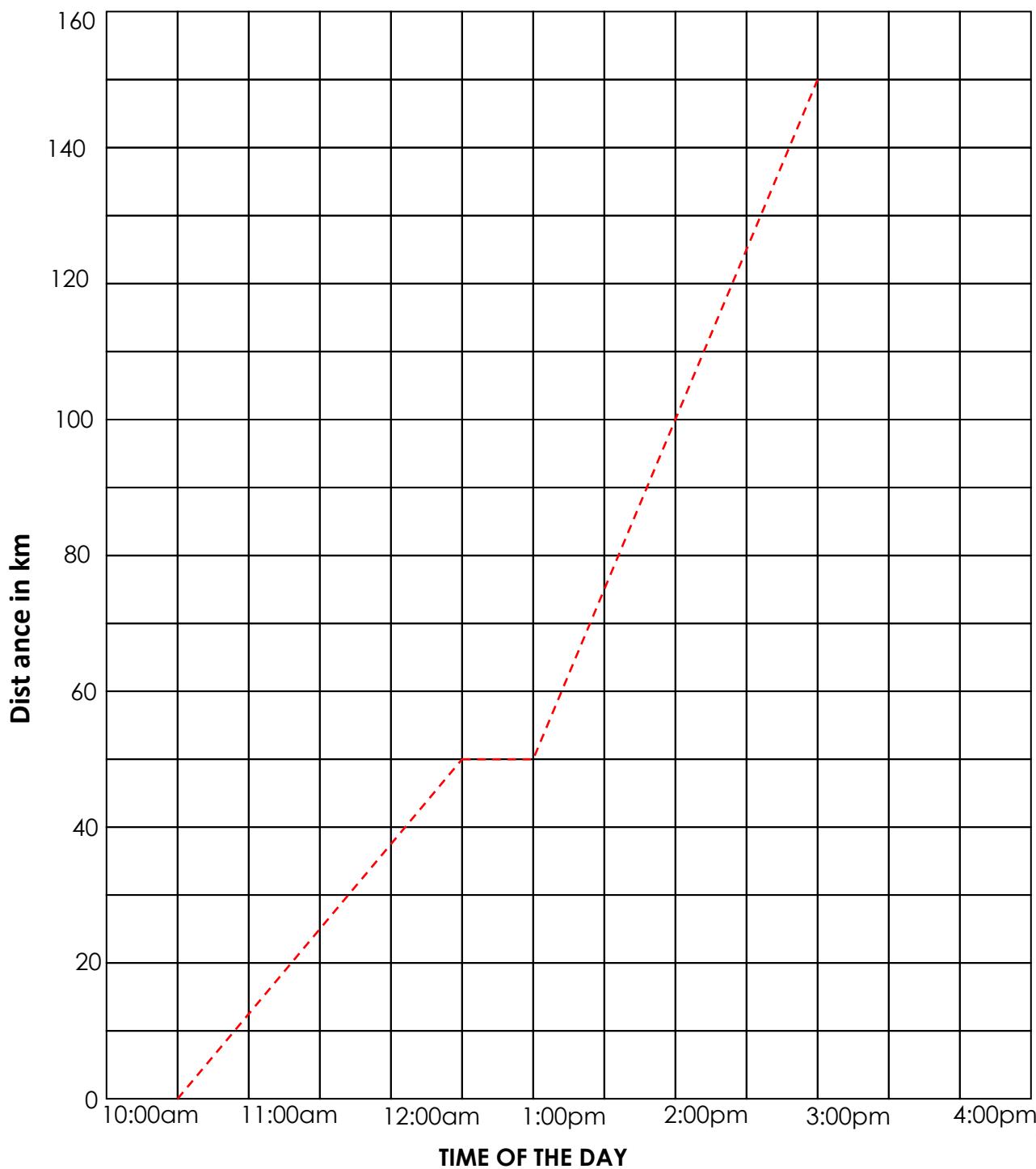
(a). Represent the motorcyclist's journey on the graph below.

Phase 1

$$\begin{aligned} \text{Distance} &= S \times T \\ &= 25\text{km/hr} \times 2\text{hrs} \\ &= 50\text{ km} \end{aligned}$$

Phase 2

$$\begin{aligned} D &= 150\text{ km} - 50\text{ km} = 100\text{ km} \\ \text{Time} &= 100\text{km} \div 50\text{km/hr} \\ &= 2\text{ hours} \end{aligned}$$



(b). At what time did he reach town G?

At 3:00 pm

REFERENCE

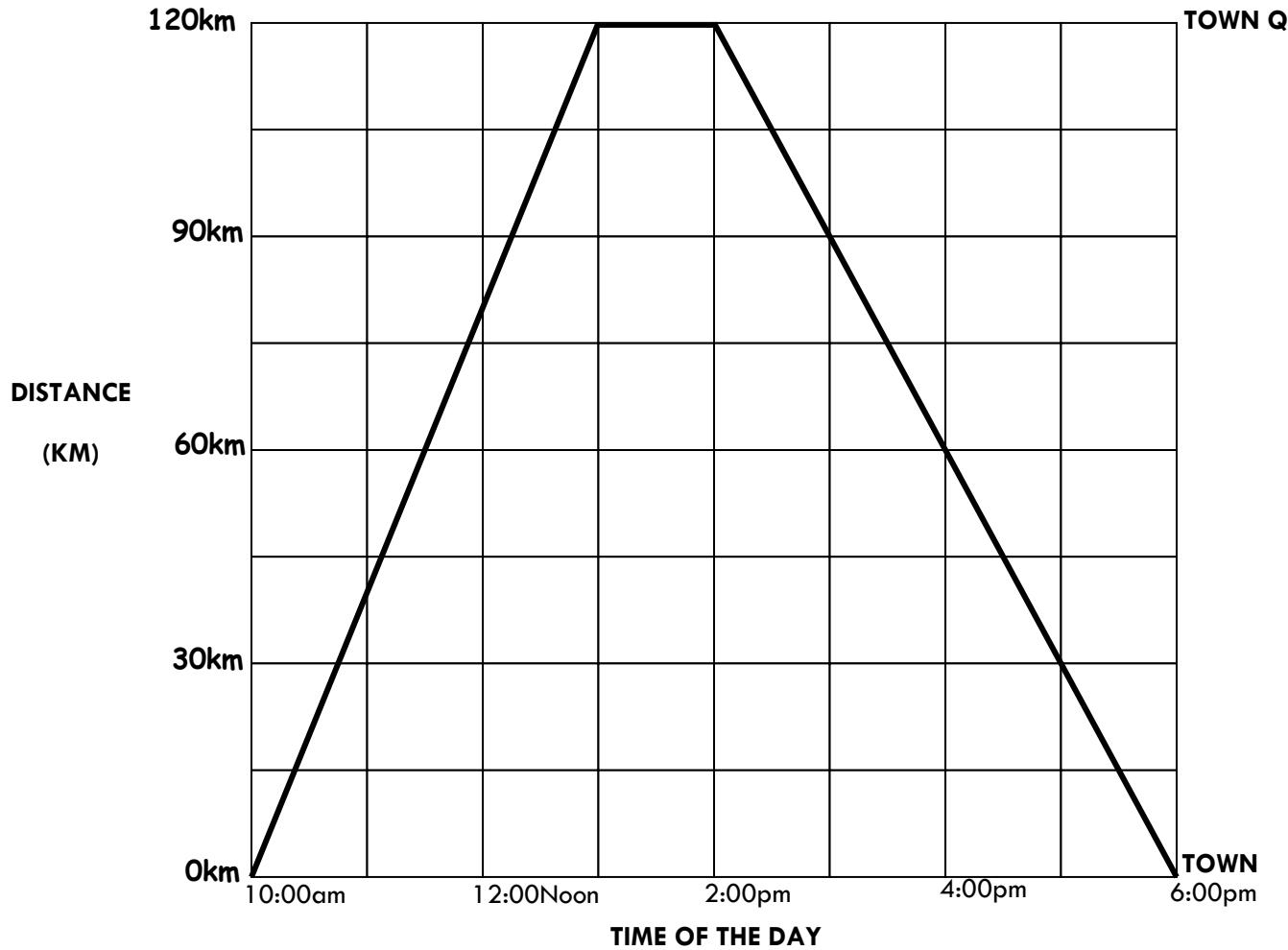
A New MK Primary Mathematics 2000 Bk 7 Pg 418 - 419 (New Edition)

TOPICAL QUESTIONS ON TIME

1. Namayanja arrives at Kampala at 11:20pm and leaves at 2:00am to travel to Nairobi. She is due into Nairobi at 6:00am the following day. Unfortunately she is delayed and arrives at 9:30am.
 - (a) How late is Namayanja in arriving at Nairobi?
 - (b) For how long does Namayanja have to wait in Kampala?
 - (c) At what time does Namayanja leave Kampala on the 24 – hour clock?
2. A lesson started at 10:30am and ended at 11:50 am. How long did the lesson last?
3. Convert 7200 seconds into hours.
4. Convert 1717 hours to a 12- hour clock.
5. Thieves escaped from the prisons at 12:15 am. Express this time in a 24-hour clock.
6. Convert $2 \frac{1}{2}$ hours to minutes.
7. It takes 4 hours for a bus traveling at 75 km/hr to move from town X to town y. Find the time taken by a bus traveling at 50km/hr to cover the same distance.
8. Express 90km/hr as m/sec.
9. Convert 10m/second to km/hour
10. A motorist covered 140km between 11:25 am and 2:55pm. Find his average speed.
11. It takes a car industry 1 hour 10 minutes 20 seconds to assemble a car. How long will it take to assemble 50 cars?
12. A bus driver left town **A** at 6:00am driving at an average speed of 50km/hr for 3 hours to town **B**. he stopped at **B** for 2hours and then left for **C** driving at 60km/hr for 1hour. Calculate the average speed for the whole journey

Mathematics
Is the Key

13. The travel graph below shows a motorists' journey from town P to town Q and back to P. Use it to answer the questions that follow



- At what time did the motorist arrive at town Q?
- How long did the return journey take?
- What was the total distance covered by the motorist?
- Find the total time taken by the motorist over the entire journey while travelling?
- Calculate the motorists' average speed over the whole journey while travelling

MONEY

SUB TOPIC: Shopping lists

Example

- A mother had a twenty thousand shilling note and bought the following items.
 - 1 $\frac{1}{2}$ kg of beans at shs.3,000 per kg.
 - 500g of salt at sh. 2,600 each kg.
 - 2 bars of soap at sh.8,000
 - 12 tomatoes at sh.800 for every 4 tomatoes
 - (a) How much did she spend altogether?

Mathematics is the key

| Beans | Salt | Soap | Total exp. |
|--|--|---------------------------------------|-----------------------------------|
| $1\frac{1}{2} \text{ kg} \times \text{sh. } 3,000$ | $1\text{kg} = 1000\text{g}$ $\frac{500}{1000} \times \text{sh. } 2,600$ | sh. 8,000 | sh. 4,500 sh. 1,300 |
| $\frac{3}{2} \times \text{sh. } 3,000$ | $50 \times \text{sh. } 26$ | Tomatoes | sh. 8,000 |
| $3 \times \text{sh. } 1,500$ | sh. 1,300 | $\frac{12}{4} \times \text{sh. } 800$ | $\underline{+ \text{sh. } 2,400}$ |
| sh. 4,500 | | $3 \times \text{sh. } 800$ | <u>sh. 16,200</u> |
| | | sh. 2,400 | |

(b) Find her change

$$\begin{aligned} \text{Change} &= \text{Money at hand} - \text{Total expenditure} \\ &= \text{sh. } 20,000 - \text{sh. } 16,200 \\ &= \text{sh. } 3,800 \end{aligned}$$

Activity

- During the COVID-19 pandemic, a lady bought the following items.

3 bottles of sanitizers at sh. 5,000@ bottle
 6 bars of soap at sh. 4,000@bar
 12 face masks at sh. 2,500 each
 A box of gloves at sh. 12,000

- How much money was spent altogether?
- If she went with 2-fifty shilling notes, calculate her change.

SUB TOPIC: Completing table bills



$$\text{Amount} = \text{Qty} \times \text{Un.C}$$

$$\text{Qty} = \frac{\text{Amount}}{\text{Un.C}}$$

$$\text{Un.C} = \frac{\text{Amount}}{\text{Qty}}$$

- Study the shopping table below which shows how Alvas bought items for the birthday party and use it to answer the questions

| Item | Quantity | Unit cost | Amount |
|--------------------------|-------------------------|-------------------|------------------|
| Sugar | 2kg | Sh. 3,600 | Sh. <u>7,200</u> |
| Rice | 4kg | Sh. <u>3,000</u> | Sh. 12,000 |
| Meat | $1\frac{1}{2}\text{kg}$ | Sh. <u>12,000</u> | Sh. 18,000 |
| Cooking oil | 500ml | Sh. 5,000@litre | Sh. <u>2,500</u> |
| Total expenditure | | | Sh. 49,700 |

(a) Complete the table

Sugar

$$2 \times sh. 3,600 = sh. 7,200$$

rice

$$sh. 12,000 \div 4 = sh. 3,000$$

meat

$$sh. 18,000 \div 1\frac{1}{2}$$

$$sh. 18,000 \div \frac{3}{2}$$

$$sh. 18,000 \times \frac{2}{3}$$

$$sh. 6,000 \times 2$$

sh. 12,000

Cooking oil

$$\frac{500}{1000} \times sh. sh. 5,000$$

$$sh. 500 \times 5$$

$$sh. 2,500$$

(b) Find the change given that he went with sh.50,000.

$$sh. 50,000 - sh. 49,700 = sh. 300$$

2. Complete the shopping table below

| Item | Quantity | Unit cost | Amount |
|--------------------------|------------|--------------|-----------|
| Books | 5 | Sh.2,000 | Sh._____ |
| Pens | _____ | Sh. 700 | Sh.6,300 |
| pencils | half dozen | Sh.4,500@doz | Sh._____ |
| Reams | 2 | Sh._____ | Sh.50,000 |
| <i>Total expenditure</i> | | | Sh._____ |

REFERENCE

A New MK Primary Mathematics 2000 Bk 7 Pg 214 - 216 (New Edition)

SUB TOPIC: CURRENCY (comparison of currencies)

Below are some of the countries with their currency

COUNTRY

Burundi

Zambia

Zimbabwe

German

Egypt

America

Britain

Kenya

Tanzania

Rwanda

CURRENCY

Burundi francs (BF)

Kwacha (Kch)

Zimbabwe Dollar (Z\$)

Deutsch mark (DM)

Egyptian pound

US Dollar(US\$)

GB pound(£)

Kenya shillings (Ksh)

Tanzania shilling (TZ sh)

Rwanda francs (RF)

Examples

1. Given that

$$1 \text{ US\$} = \text{Ugsh. } 3,700$$

$$1 \text{ TZ sh.} = \text{Ugsh. } 2.2$$

$$1 \text{ ksh} = \text{ugsh.}$$

- a) How much in Uganda shillings is equivalent to \$20 plus Tzsh. 30,00?

$$1 \text{ US\$} = \text{Ugsh. } 3,700$$

$$\text{Ugsh } 3,700 \times 20$$

$$\underline{\text{Ugsh } 74,000}$$

$$1 \text{ TZsh} = \text{Ugsh } 2.2$$

$$\begin{aligned} \text{TZ shs } 30,000 &= \text{Ush. } \frac{22}{10} \times 30,000 \\ &= \underline{\text{Ush. } 66,000} \end{aligned}$$

Total Uganda currency

$$\text{Ugsh } 74,000$$

$$+ \underline{\text{Ugsh } 66,000}$$

$$\underline{\text{Ush. } 140,000}$$

- b) Kizito works with the Tanzania high commission and his monthly salary is Ugsh.33,000. What is his salary in Tanzania currency?

$$\text{Ugsh. } 2.2 = \text{TZsh} 1$$

$$33,000 \div 2.2$$

$$33000 \div \frac{22}{10}$$

$$33000 \times \frac{10}{22}$$

$$3000 \times 5$$

$$\underline{\text{TZsh. } 15,000}$$

- c) A trader sold maize to Kenya for K sh. 150,000. How much money did he get in Uganda shillings given that 1 ksh. = Ugsh.20

Ksh 1 equivalent to U sh 20

$$\text{Ugsh. } 20 \times 150,000$$

$$\underline{\text{Ugshs } 3,000,000}$$

- d) Musiime exported coffee to USA and earned US\$ 25,000. He also exported maize to Kenya and earned K shs 500,000.Calculate his total earning in Uganda currency.
- e) Convert £ 37,000 to Uganda shillings.
- f) Mr Santu Daniel went to the Forex Bureau with Ugsh. 207200. How much in US\$ did he get in exchange.
- g) Convert GBP _____ to Kenya shillings.

SUB TOPIC: BUYING AND SELLING OF MONEY

4. The table below shows the rates at which different currencies are bought and sold.

| CURRENCY | BUYING(UGX) | SELLING(UGX) |
|--------------|-------------|--------------|
| 1 US dollar | 3600 | 3650 |
| 1 Euro | 4000 | 4020 |
| 1 Rwa. franc | 4.0 | 5.0 |

- (a) How many Euros did Musa get for ugsh.603,000?

$$1 \text{ Euro} = \text{Ugsh. } 4,020$$

$$\begin{array}{r} \text{Ugsh. } 603,000 \\ - \quad \quad \quad \text{Ugsh. } 4,020 \\ \hline 60300 \\ - \quad \quad \quad 402 \\ \hline 150 \end{array}$$

150 Euros

- (b) Amiina came from Rwanda with 111,000 Rwandese francs and exchanged them for us dollars. How many US dollars did she get from the bank?

Rwanda francs to Ugsh

$$1 \text{ Franc} = \text{Ugsh. } 4$$

$$111,000 \times 4$$

$$\underline{\text{Ugsh. } 444,000}$$

Ugsh to US dollars

$$\text{Ugsh. } 3700 = 1 \text{ US dollar}$$

$$\text{Ugsh. } 444,000$$

$$\begin{array}{r} \text{Ugsh. } 3700 \\ - \quad \quad \quad 4440 \\ \hline 37 \end{array}$$

$$\underline{120 \text{ US dollars}}$$

Mathematics is the Key

TERM III

LENGTH, MASS AND CAPACITY

SUB TOPIC: Comparing units/conversion of metric units(review)

Examples:

Comparing metric units

| | | | | | | |
|-----------|-----------|-----------|--------------|-----------|-----------|-----------|
| Km | Hm | Dm | Metre | dm | cm | mm |
| Kg | Hg | Dg | Gram | dg | cg | mg |
| lI | lI | lI | Litre | dl | cl | ml |

- (a) Change 7m to millimetres

$$1m = 1000mm$$

$$\begin{aligned} 7m &= (7 \times 1000m) \\ &= \underline{\underline{7000mm}} \end{aligned}$$

- (b). Change 800m to km

$$1000m = 1km$$

$$\begin{aligned} 800m &= \frac{800}{1000} \\ &= \frac{8}{10} \\ &= \underline{\underline{0.8km}} \end{aligned}$$

Convert the following as instructed

- (a) 4km to metres
- (b) 0.4 litres to milliliters
- (c) 2000g to kg
- (d) 50cm to m

REFERENCE

A New MK Primary Mathematics Bk 7 Pg 34

Mathematics is the Key

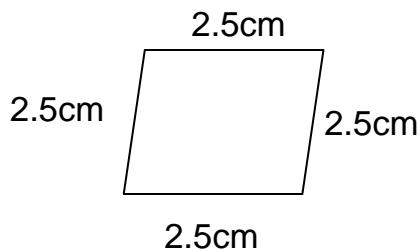
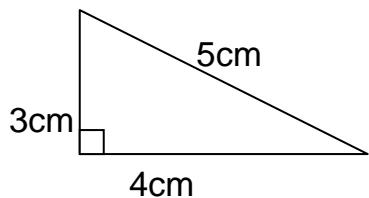
SUB TOPIC: Finding perimeter

Perimeter is the total distance around the figure

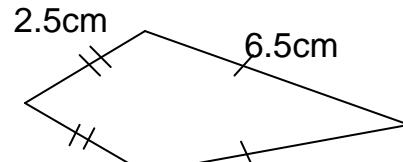
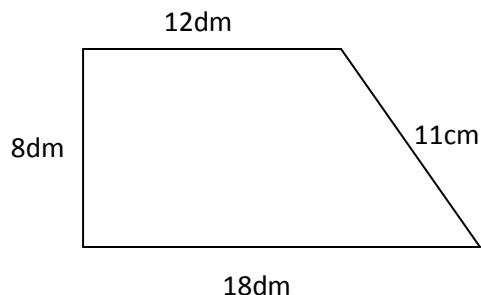
Examples:

Find the distance (Perimeter) around the shapes given below:

(i)



$$\begin{aligned} P &= 4\text{cm} + 3\text{cm} + 5\text{cm} \\ &= 7\text{cm} + 5\text{cm} \\ &= 12\text{cm} \end{aligned}$$



REFERENCE

A New MK Primary Mathematics Bk 7 Pg 347-350

SUB TOPIC: FINDING AREA OF SIMPLE SHAPES

BASIC FORMULAE

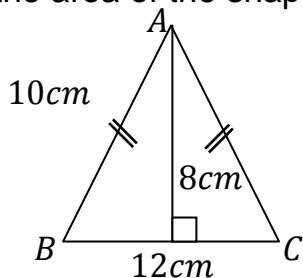
$$\text{SQUARE} = S \times S$$

$$\text{RECTANGLE} = L \times W$$

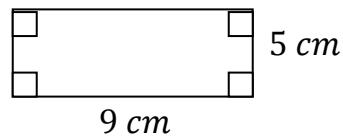
$$\text{TRIANGLE} = \frac{1}{2}bh$$

$$\text{TRAPEZIUM} = \frac{1}{2}h(a+b)$$

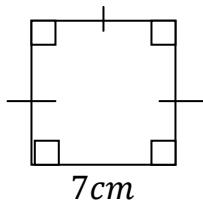
- Find the area of the shapes below



$$\begin{aligned} A &= \frac{1}{2} \times b \times h \\ &= \frac{1}{2} \times 12\text{cm} \times 8\text{cm} \\ &= 6\text{cm} \times 8\text{cm} \\ A &= 48\text{cm}^2 \end{aligned}$$



$$\begin{aligned} A &= L \times W \\ &= 9\text{cm} \times 5\text{cm} \\ &= 45\text{cm}^2 \end{aligned}$$

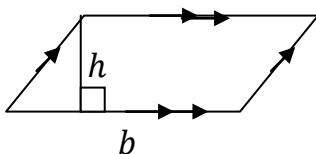


$$\begin{aligned}
 A &= S \times S \\
 &= 7\text{cm} \times 7\text{cm} \\
 &= \underline{\underline{49\text{cm}^2}}
 \end{aligned}$$

Try these

- Find the area of a square whose side is 13m*
- Calculate the area of a rectangle whose length is 14dm and width is 9dm.*
- Find the area of a triangle whose base is 25cm and height is 30cm.*

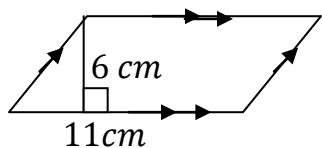
SUB TOPIC: Finding area of a parallelogram



$$\text{PARALLELOGRAM} = b \times h$$

Examples

1. Work out the area of the figure below.



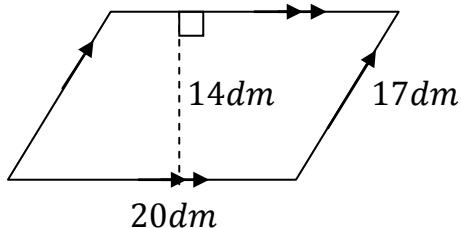
$$\begin{aligned}
 A &= b \times h \\
 &= 11\text{cm} \times 6\text{cm} \\
 &= \underline{\underline{66\text{cm}^2}}
 \end{aligned}$$

2. Find the area of a parallelogram whose base is 17cm and height is 10cm.

$$\begin{aligned}
 A &= b \times h \\
 A &= 17\text{cm} \times 10\text{cm} \\
 A &= \underline{\underline{170\text{cm}^2}}
 \end{aligned}$$

3. Find the area of a parallelogram whose base and height are 16cm and 11cm respectively.

4. Find the area and perimeter of the figure below



SUB TOPIC: Finding area of a Trapezium

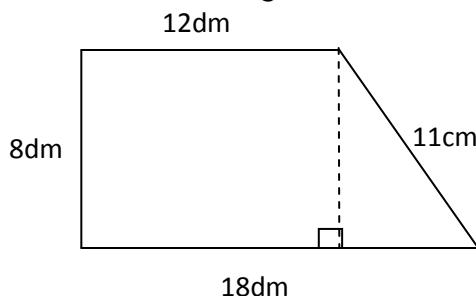
$$A = \frac{1}{2} b(a) \times h + \frac{1}{2} b(b) \times h$$

$$A = \frac{1}{2} a \times h + \frac{1}{2} b \times h$$

$$A = \frac{1}{2} h(a + b)$$

Examples

1. Find the area of the figure below.



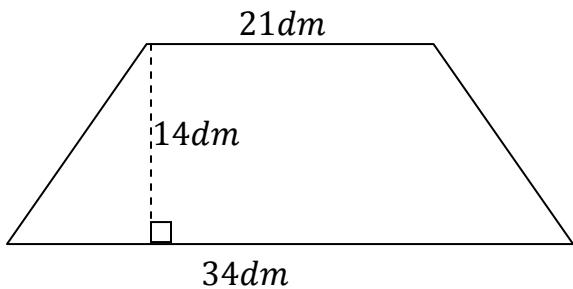
$$A = \frac{1}{2} h(a + b)$$

$$A = \frac{1}{2} \times 8\text{dm}(18\text{dm} + 12\text{dm})$$

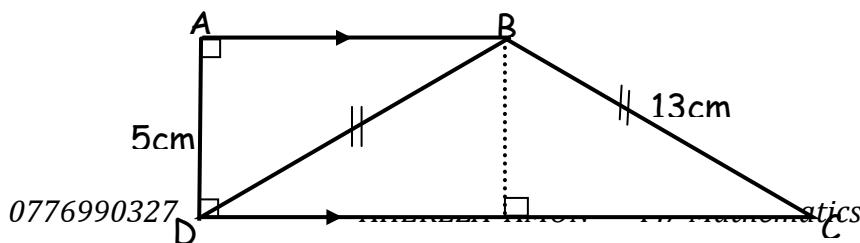
$$A = 4\text{dm} \times 30\text{dm}$$

$$\underline{\underline{A = 120\text{dm}^2}}$$

2. Find the area of the figure below.



3. The figure below is made up of two triangles ABD and BCD. Line BC=BD = 13cm
line AD = 5cm, line DC=24cm, AB= 12cm.



Calculate the area of the figure ABCD

REFERENCE

A New MK Primary Mathematics Bk 7 Pg 354

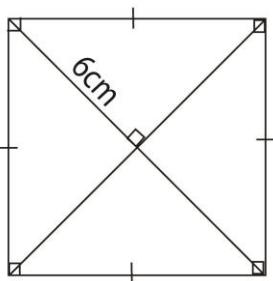
SUB TOPIC: QUADRILATERALS

CONTENT: finding area of a square, kite and rhombus using diagonals

NOTE: All shapes whose diagonals meet at a right angle use a similar formulae for area.

$$\text{AREA} = \frac{1}{2} \times d_1 \times d_2$$

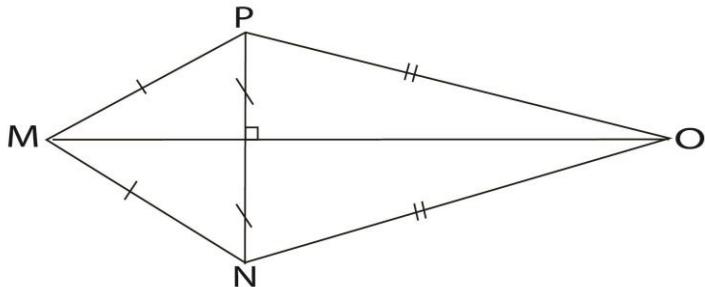
1. Calculate the area of the square below



$$\begin{aligned}\text{AREA} &= \frac{1}{2} \times d_1 \times d_2 \\ d_1 &= 6\text{cm} + 6\text{cm} \\ &= \underline{\underline{12\text{ cm}}}\end{aligned}$$

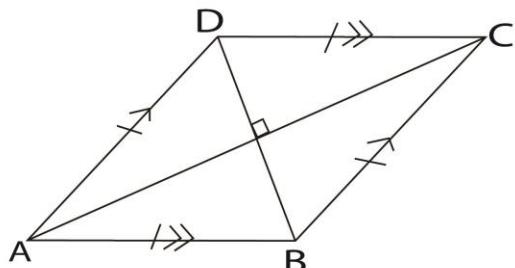
$$\begin{aligned}\text{Area} &= \frac{1}{2} \times 12\text{cm} \times 12\text{cm} \\ &= 6\text{cm} \times 12\text{cm} \\ &= \underline{\underline{72\text{ cm}^2}}\end{aligned}$$

2. In the figure below, line MO = 12cm and line PN = 5cm. Calculate its area.



$$\begin{aligned}\text{AREA} &= \frac{1}{2} \times d_1 \times d_2 \\ d_1 &= 12\text{ cm} \quad d_2 = 5\text{cm} \\ \text{Area} &= \frac{1}{2} \times 12\text{cm} \times 5\text{cm} \\ &= 6\text{cm} \times 5\text{cm} \\ &= \underline{\underline{30\text{ cm}^2}}\end{aligned}$$

3. Diagonals of rhombus ABCD measure 16m by 12m. Calculate its area.



$$\begin{aligned}\text{AREA} &= \frac{1}{2} \times d_1 \times d_2 \\ d_1 &= 16\text{m} \quad d_2 = 12\text{m} \\ \text{Area} &= \frac{1}{2} \times 16m \times 12m \\ &= 8m \times 12m \\ &= \underline{\underline{96\text{ m}^2}}\end{aligned}$$

REMEMBER:

Since these shapes have diagonals which meet at a right angle.

Divide the shape into right angled triangles and look for area of each triangle.

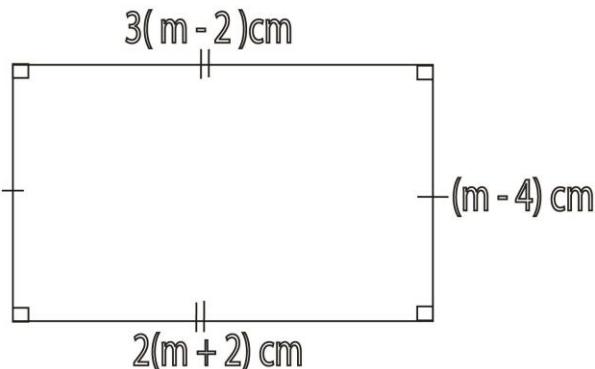
Later combine the areas.

Try these

- Find the area of a kite whose diagonals are 12cm and 4cm.
- Find the area of a square whose diagonal is 10cm.
- Calculate the area of a rhombus whose diagonals are 16cm and 10cm.

SUB TOPIC: Comparing sides of a polygon

- Study the figure below



- Find its area

(a) Find the value of m

$$2(m + 2)cm = 3(m - 2)cm$$

$$2(m + 2) = 3(m - 2)$$

$$2m + 4 = 3m - 6$$

$$2m - 3m = -6 - 4$$

$$-m = -10$$

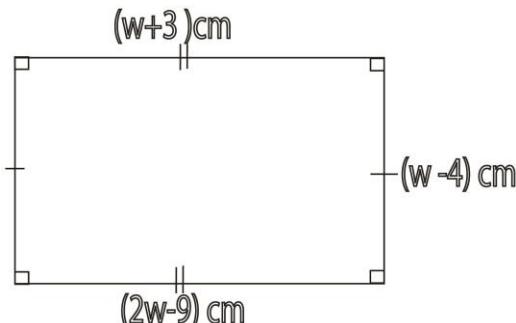
$$\frac{-m}{-1} = \frac{-10}{-1}$$

$$\underline{\underline{m = 10}}$$

$$\begin{aligned} \text{Length} &= 2(m + 2)cm & \text{width} &= (m + 4)cm \\ &= 2(10 + 2)cm & &= 10cm + 4cm \\ &= 2 \times 12cm & &= 14cm \\ &\underline{\underline{= 24cm}} \end{aligned}$$

$$\begin{aligned} \text{Area} &= L \times W \\ &= 24cm \times 14cm \\ &\underline{\underline{= 336cm^2}} \end{aligned}$$

Use the figure below to answer the questions



(a) Find the value of w

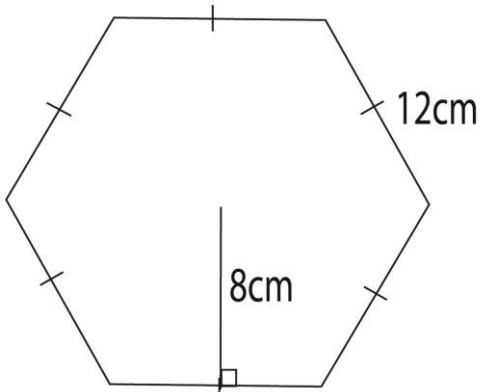
(b) Find the area and perimeter of the figure

SUB TOPIC: Using apothem to find area

An apothem is a line running from the centre perpendicular to any of the sides of a regular polygon.

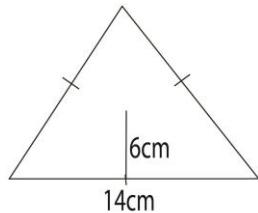
$$\text{Area} = \frac{1}{2} \times \text{apothem} \times \text{perimeter}$$

1. Study the figure below and find its area.



$$\begin{aligned}
 \text{Area} &= \frac{1}{2} \times \text{apothem} \times \text{perimeter} \\
 &= \frac{1}{2} \times 8\text{cm} \times (12\text{cm} \times 6) \\
 &= 4\text{cm} \times 72\text{cm} \\
 &= \underline{\underline{288\text{cm}^2}}
 \end{aligned}$$

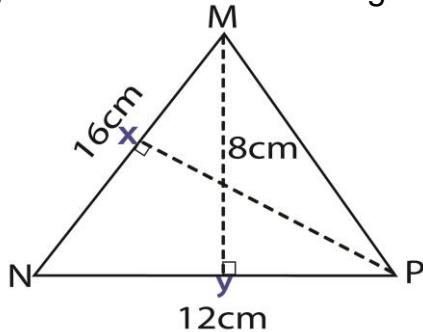
2. Find the area of the figure below



SUB TOPIC: Comparing areas

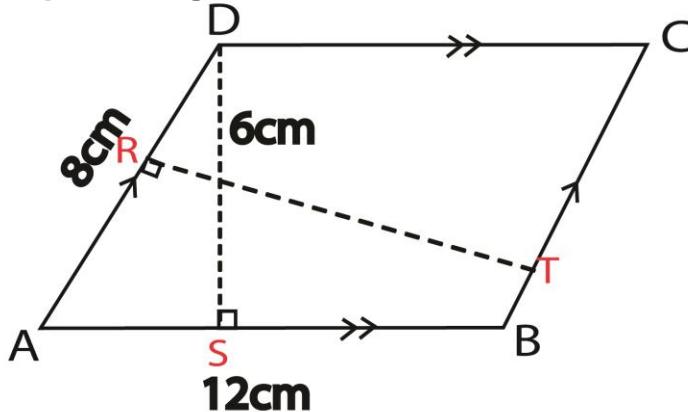
Example 1

1. The figure below shows a triangle with two heights. Find the length XP



$$\begin{aligned}\frac{1}{2}bh &= \frac{1}{2}bh \\ \frac{1}{2} \times 16\text{cm} \times h &= \frac{1}{2} \times 12\text{cm} \times 8\text{cm} \\ 8\text{cm}h &= 12\text{cm} \times 4\text{cm} \\ \frac{8\text{cm}h}{8\text{cm}} &= \frac{12\text{cm} \times 4\text{cm}}{8\text{cm}} \\ h &= 6\text{cm} \\ \underline{XP = 6\text{cm}}\end{aligned}$$

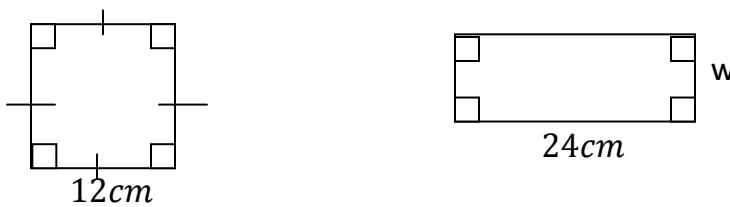
2. Study the parallelogram below and use it to answer the questions that follow



Find the length of line RT

$$\begin{aligned}bh &= bh \\ 8\text{cm} \times h &= 12\text{cm} \times 6\text{cm} \\ \frac{8\text{cm}h}{8\text{cm}} &= \frac{12\text{cm} \times 6\text{cm}}{8\text{cm}} \\ \underline{h = 9\text{cm}}\end{aligned}$$

3. The area of the rectangle is equal to the area of the square below.



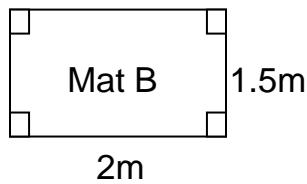
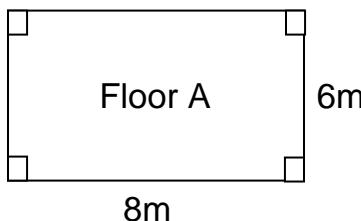
Find the value of w

$$\begin{aligned}L \times W &= S \times S \\ 24\text{cm} \times W &= 12\text{cm} \times 12\text{cm} \\ \frac{24\text{cm}W}{24\text{cm}} &= \frac{12\text{cm} \times 12\text{cm}}{24\text{cm}} \\ \underline{W = 6\text{cm}}\end{aligned}$$

SUBTOPIC: More about area

Examples:

- How many mats (B) can cover floor (A)?



NOTE: When carrying out division, the units must be similar

$$1m = 100cm$$

$$8m = 8 \times 100cm = 800cm$$

$$6m = 6 \times 100cm = 600cm$$

$$2m = 2 \times 100cm = 200cm$$

$$1.5m = 1.5 \times 100cm = 150cm$$

No. of mats

$$4 \times 4$$

16mats

Along length: 800

200

= 4 mats

Along width: 600

150

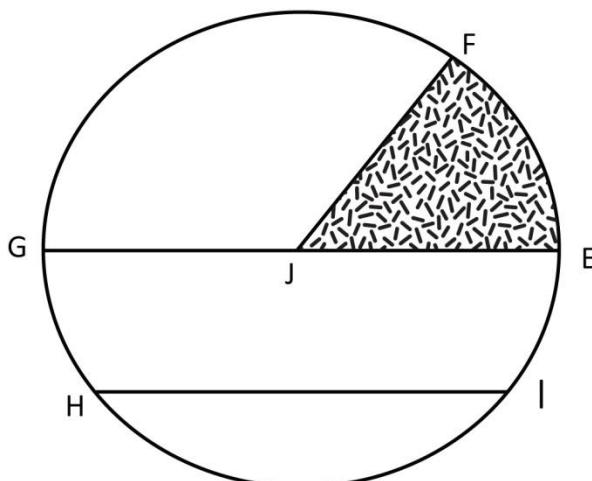
= 4 mats

- Circular cards of radius 14cm were cut from a rectangular manila paper of length 150cm and width 120 cm. How many cards were cut from the manila paper?

REFERENCE

A New MK Primary Mathematics Bk 7 Pg 356

CIRCLE PROPERTIES(review)



GE = diameter

JE = radius

HI = chord

FE = arc

JEF = sector

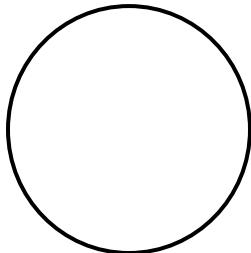
FEIHGF = circumference

JF = ???

NOTE: The diameter is the longest chord

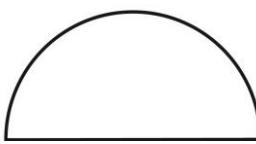
SUBTOPIC: Finding circumference of a circle and parts of a circle.

Circumference is the length of the arc.



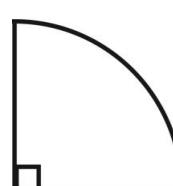
CIRCLE

$$C = \pi D$$



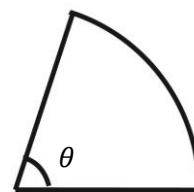
SEMI CIRCLE

$$C = \frac{1}{2}\pi D$$



QUADRANT

$$C = \frac{1}{4}\pi D$$



SECTOR

$$C = \frac{\theta}{360^\circ} \pi D$$

θ = sector angle

Mathematics is the key

1. Calculate the circumference of ; ($\pi = \frac{22}{7}$)

- (a) A circle whose diameter is 7m.

$$\begin{aligned} C &= \pi D \\ &= \frac{22}{7} \times 7m \\ &= \underline{\underline{22m}} \end{aligned}$$

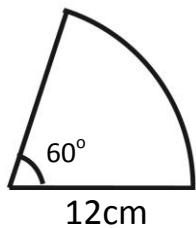
- (b) A semi circle whose radius is 7cm

$$\begin{aligned} C &= \frac{1}{2}\pi D \\ &= \frac{1}{2} \times \frac{22}{7} \times 7cm \times 2 \\ &= 11cm \times 2 \\ &= \underline{\underline{22m}} \end{aligned}$$

- (c) A quadrant whose radius is 14cm

$$\begin{aligned} C &= \frac{1}{4}\pi D \\ &= \frac{1}{4} \times \frac{22}{7} \times 14cm \times 2 \\ &= \frac{22}{4} \times 2cm \times 2 \\ &= \underline{\underline{22cm}} \end{aligned}$$

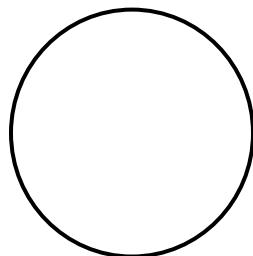
2. Calculate the circumference of the figure below. (Given that $\pi = 3.14$)



$$\begin{aligned} C &= \frac{\theta}{360^\circ} \pi D \\ &= \frac{60^\circ}{360^\circ} \times 3.14 \times 12cm \times 2 \\ &= \frac{1}{6} \times \frac{314}{100} \times 24cm \\ &= \frac{1256}{100} cm \\ &= \underline{\underline{12.56cm}} \end{aligned}$$

SUB TOPIC: Finding perimeter of a circle and parts of a circle

PERIMETER is the total distance around the city.

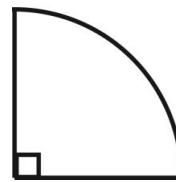
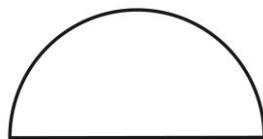


CIRCLE
Perim. = Circ
 $P = \pi D$

SEMI CIRCLE

$$P = C + D$$

$$P = \frac{1}{2}\pi D + D$$



QUADRANT

$$P = C + r + r$$

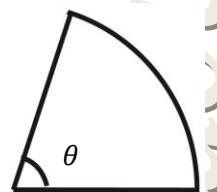
$$P = \frac{1}{4}\pi D + D$$

SECTOR

$$P = C + r + r$$

$$P = \frac{\theta}{360^\circ} \pi D + D$$

θ = sector angle



Examples

1. Calculate the perimeter of ;

(a) A semi circle whose radius is 14cm($\pi = \frac{22}{7}$)

$$\begin{aligned} P &= \frac{1}{2}\pi D + D \\ &= \frac{1}{2} \times \frac{22}{7} \times 14\text{cm} \times 2 + 14\text{cm} \times 2 \\ &= 44\text{cm} + 28\text{cm} \\ &\equiv 72\text{cm} \end{aligned}$$

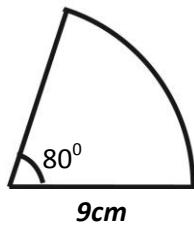
(b) A quadrant whose radius is 10cm($\pi = 3.14$)

$$P = \frac{1}{4}\pi D + D$$

$$D = 10\text{cm} \times 2 = 20\text{cm}$$

$$\begin{aligned} P &= \frac{1}{4} \times \frac{314}{100} \times 20\text{cm} + 20\text{cm} \\ &= \frac{314 \times 5}{100} + 20\text{cm} \\ &= \frac{1570}{100} + 20\text{cm} \\ &= 15.7 + 20\text{cm} \\ &\equiv 35.7\text{cm} \end{aligned}$$

2. Calculate the perimeter of the figure below.



$$P = \frac{\theta}{360^\circ} \pi D + D$$

$$D = 9\text{cm} \times 2 = 18\text{cm}$$

$$\begin{aligned} P &= \frac{80^\circ}{360^\circ} \times \frac{22}{7} \times 18\text{cm} + 18\text{cm} \\ &= \frac{2}{9} \times \frac{22}{7} \times 18\text{cm} + 18\text{cm} \\ &= \frac{88}{7}\text{cm} + 18\text{cm} \\ &= 12\frac{4}{7}\text{cm} + 18\text{cm} \\ &= 30\frac{4}{7}\text{cm} \end{aligned}$$

Mathematics is the key

SUB TOPIC: Finding the radius or diameter when given perimeter

Examples

1. The perimeter of a circle is 88m. Find its radius.

$$\pi D = P$$

$$\frac{22}{7}D = 88m$$

$$\frac{22D}{7} = 88m$$

$$7 \times \frac{22D}{7} = 88m \times 7$$

$$22D = 88 \times 7m$$

$$\frac{22D}{22} = \frac{88 \times 7m}{22}$$

$$D = 4 \times 7m$$

$$D = 28m$$

$$r = \frac{28m}{2}$$

$$r = 14m$$

$$\frac{1}{2}\pi D + D = P$$

$$\frac{1}{2} \times \frac{22}{7} \times D + D = 72cm$$

$$\frac{11D}{7} + D = 72cm$$

$$7 \times \frac{11D}{7} + \frac{D}{1} \times 7 = 72cm \times 7$$

$$11D + 7D = 72cm \times 7$$

$$18D = 72cm \times 7$$

$$\frac{18D}{18} = \frac{72cm \times 7}{18}$$

$$D = 4cm \times 7$$

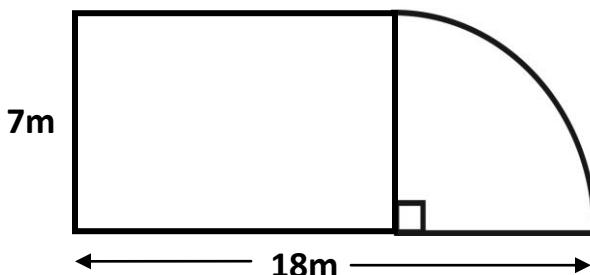
$$D = 28cm$$

2. The perimeter of a semicircle is 72 cm. Find its diameter.

SUB TOPIC: More about perimeter

Example

1. Study the figure below and find its perimeter



$$C = \frac{1}{4}\pi D$$

$$= \frac{1}{4} \times \frac{22}{7} \times 7m \times 2$$

$$= \frac{44m}{4}$$

$$= 11m$$

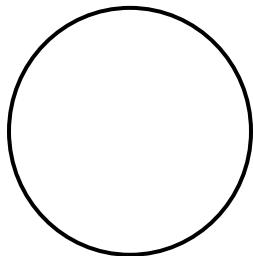
$$P = 18m + 11m + (18m - 7m) + 7m$$

$$= 29m + 11m + 7m$$

$$= 47m$$

Mathematics is the key

SUB TOPIC: Finding area of a circle and parts of a circle

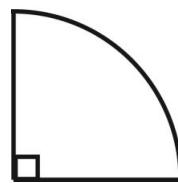
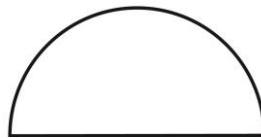


CIRCLE

$$A = \pi r^2$$

SEMI CIRCLE

$$A = \frac{1}{2} \pi r^2$$



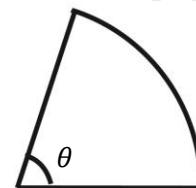
QUADRANT

$$A = \frac{1}{4} \pi r^2$$

SECTOR

$$A = \frac{\theta}{360^\circ} \pi r^2$$

θ = sector angle



1. Calculate the area of ; ($\pi = \frac{22}{7}$)

- (a) A circle whose diameter is 7m.

$$\begin{aligned} A &= \pi r^2 \\ &= \frac{22}{7} \times \frac{7m}{2} \times \frac{7m}{2} \\ &= \frac{11}{2} \times 7m \\ &= \frac{77}{2} m^2 \\ &= 38\frac{1}{2} m^2 \end{aligned}$$

- (b) A semi circle whose radius is 7cm

$$\begin{aligned} A &= \frac{1}{2} \pi r^2 \\ &= \frac{1}{2} \times \frac{22}{7} \times 7cm \times 7cm \\ &= 11cm \times 7cm \\ &\equiv 77cm^2 \end{aligned}$$

- (c) A quadrant whose radius is 14cm

$$\begin{aligned} A &= \frac{1}{4} \pi r^2 \\ &= \frac{1}{4} \times \frac{22}{7} \times 14cm \times 14cm \\ &= \frac{22}{4} \times 2cm \times 7cm \\ &= 11 \times 7cm^2 \\ &\equiv 77 cm^2 \end{aligned}$$

SUB TOPIC: Finding radius or diameter when given area

1. The area of a circle is 154cm^2 . Find its radius.

$$\begin{aligned} \pi r^2 &= A \\ \frac{22}{7} r^2 &= 154\text{m}^2 \\ \frac{22r^2}{7} &= 154\text{m}^2 \\ 7 \times \frac{22r^2}{7} &= 154\text{m}^2 \times 7 \\ 22r^2 &= 154 \times 7\text{m}^2 \\ \frac{22r^2}{22} &= \frac{154 \times 7\text{m}^2}{22} \\ r^2 &= 7 \times 7\text{m}^2 \\ r^2 &= \sqrt{49}\text{m}^2 \\ r &= 7\text{m} \end{aligned}$$

2. The area of a semicircle is 77cm^2 . Find its diameter.

$$\frac{1}{2}\pi r^2 = A$$

$$\frac{1}{2} \times \frac{22}{7} \times r^2 = 77 \text{ cm}^2$$

$$\frac{11r^2}{7} = 77 \text{ cm}^2$$

$$7 \times \frac{11r^2}{7} = 77 \text{ cm}^2 \times 7$$

$$11r^2 = 77\text{cm}^2 \times 7$$

$$\frac{11r^2}{11} = \frac{77\text{cm}^2 \times 7}{11}$$

$$r^2 = 7\text{cm}^2 \times 7)$$

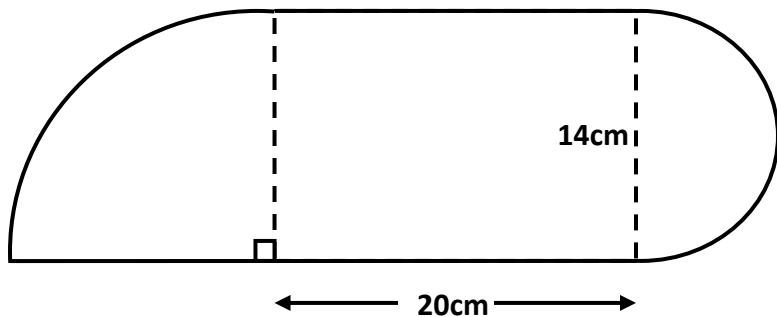
$$r^2 = \sqrt{49\text{cm}^2}$$

$$\underline{r = 7\text{cm}}$$

SUB TOPIC: Finding area of the combined shapes

Examples

1. Study the figure below and find its area.



Quadrant

$$\begin{aligned}
 A &= \frac{1}{4}\pi r^2 \\
 &= \frac{1}{4} \times \frac{22}{7} \times 14\text{cm} \times 14\text{cm} \\
 &= \frac{22}{4} \times 2\text{cm} \times 7\text{cm} \\
 &= 11 \times 7\text{cm}^2 \\
 &\equiv 77 \text{ cm}^2
 \end{aligned}$$

semicircle

$$r = 14\text{cm} \div 2 = 7\text{cm}$$

$$A = \frac{1}{2}\pi r^2$$

$$\begin{aligned}
 &= \frac{1}{2} \times \frac{22}{7} \times 7\text{cm} \times 7\text{cm} \\
 &= 11\text{cm} \times 7\text{cm} \\
 &\equiv 77\text{cm}^2
 \end{aligned}$$

Rectangle

$$\begin{aligned}
 A &= L \times W \\
 &= 20\text{cm} \times 14\text{cm} \\
 &\equiv 280\text{cm}^2
 \end{aligned}$$

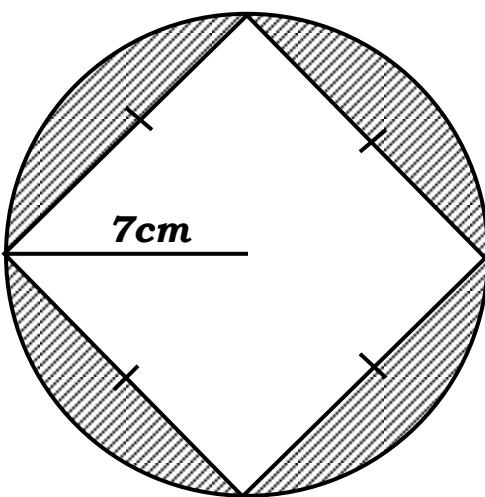
total area

$$\begin{aligned}
 &(280 + 77 + 77)\text{cm}^2 \\
 &\underline{\underline{434\text{cm}^2}}
 \end{aligned}$$

SUB TOPIC: Finding shaded area

Examples

1. Study the figure below and use it to answer the questions that follow.



Find the shaded area ($\pi = \frac{22}{7}$)

Square

$$\text{Diagonal} = 7\text{cm} + 7\text{cm} = 14\text{cm}$$

$$A = \frac{1}{2} \times d_I \times d_{II}$$

$$= \frac{1}{2} \times 14\text{cm} \times 14\text{cm}$$

$$= 7\text{cm} \times 14\text{cm}$$

$$= 98\text{cm}^2$$

circle

$$A = \pi r^2$$

$$= \frac{22}{7} \times 7\text{cm} \times 7\text{cm}$$

$$= 22\text{cm} \times 7\text{cm}$$

$$= 154\text{cm}^2$$

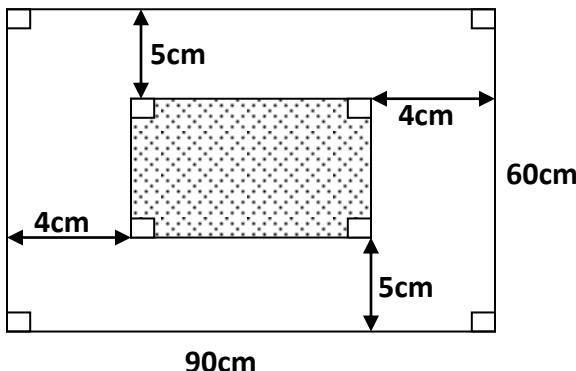
Shaded area

Outer area – Inner area

$$154\text{cm}^2 - 98\text{cm}^2$$

$$56\text{cm}^2$$

2. A table of size 90cm by 60cm was partly covered with a piece of cloth as shown in the figure below. What part of the table was uncovered?



SUB TOPIC: More about circumference(Revolutions)

$$\text{Revolutions} = \frac{\text{distance}}{\text{circumference}}$$

Examples

1. A bicycle tyre of radius 35cm covered a distance of 4.4km. How many revolutions did it make? (take pi as $\frac{22}{7}$)

$$C = \pi D \quad \underline{= 440,000\text{cm}}$$

$$= \frac{22}{7} \times 35\text{cm} \times 2$$

$$= 22 \times 10\text{cm}$$

$$\underline{= 220\text{cm}}$$

$$\text{Revolution} = \frac{\text{distance}}{\text{circumference}} \\ = \frac{440,000\text{cm}}{220\text{cm}} \\ \underline{= 2,000 \text{ revolutions}}$$

Km to cm

$$1\text{km} = 100,000\text{cm}$$

$$4.4\text{km} = 4.4 \times 100,000\text{cm}$$

2. A wire is wound round a cylindrical drum 1500 times. If the length of the wire is 6.6km. Find the radius of the tank.

Km to cm

$$1\text{km} = 100,000\text{cm}$$

$$6.6\text{km} = 6.6 \times 100,000\text{cm}$$

$$\underline{= 660,000\text{cm}}$$

$$\frac{\text{distance}}{\text{circumference}} = \text{revolutions}$$

$$\frac{660,000\text{cm}}{C} = 1500$$

$$C \times \frac{660,000\text{cm}}{C} = 1,500 \times C$$

$$1500C = 660,000\text{cm}$$

$$\frac{1500}{1500} = \frac{660,000\text{cm}}{1500}$$

$$C = \frac{6600\text{cm}}{15}$$

$$\underline{C = 440\text{cm}}$$

$$\pi D = C$$

$$\frac{22}{7}D = 440\text{cm}$$

$$\frac{22D}{7} = 440\text{cm}$$

$$7 \times \frac{22D}{7} = 440\text{cm} \times 7$$

$$22D = 440\text{cm} \times 7$$

$$\frac{22D}{22} = \frac{440 \times 7\text{cm}}{22}$$

$$D = 20 \times 7\text{cm}$$

$$\underline{D = 140\text{cm}}$$

$$r = \frac{140\text{cm}}{2}$$

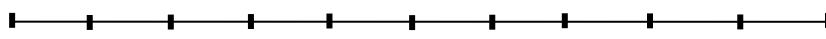
$$\underline{r = 70\text{cm}}$$

Mathematics is the key

SUB TOPIC: Application of perimeter

(a) Poles in a straight line (Open fences)

In open fences, the number of poles is one more than the number of spaces



There are 11 poles and 10 spaces in the figure above

$$\text{Number of poles} = \text{no. of spaces} + 1$$

$$\text{No. of spaces} = \frac{\text{distance}}{\text{interval}}$$

- Electric poles are planted 20m apart. Find the distance from the first pole to the 10th pole.

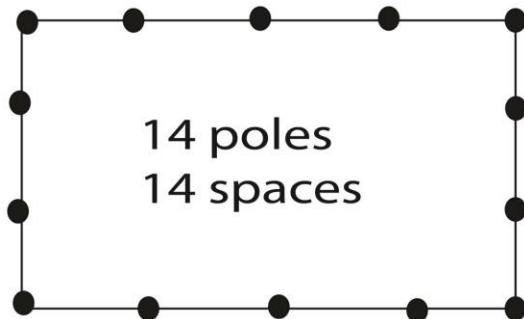
$$\text{No. of spaces} = \text{No of poles} - 1$$

$$\begin{aligned}\text{Distance} &= (10 - 1) \times 20\text{m} \\ &= 9 \times 20\text{m} \\ &= \underline{\underline{180\text{m}}}\end{aligned}$$

2. Closed fences:

In closed fences the number of poles corresponds with the number of spaces.

In the illustration below the number of poles is 14 and the number of spaces is also 14.



$$\text{No. of poles} = \frac{\text{perimeter}}{\text{interval}}$$

Example:

Mukasa's rectangular flower garden measures 10m by 8m. He fenced it, putting the poles 2m apart. How many poles did he need?

Perimeter of flower garden

$$\begin{aligned}P &= 2(l + w) \\ &= 2(10 + 8)\text{m} \\ &= 2(18) \\ &= \underline{\underline{36\text{m}}}\end{aligned}$$

No. of poles

$$\begin{aligned}&= \frac{\text{Perimeter}}{\text{interval}} \\ &= \frac{36\text{m}}{2\text{m}} \\ &= \underline{\underline{18 \text{ poles}}}\end{aligned}$$

Mathematics is the key

ACTIVITY:

1. When sprinting, Ivan athlete covers 180cm with every stride.
 - (a) How many strides does he take to finish 100m.
 - (b) How far does he run in 200 strides?
2. Telephone poles are 20m apart. What is the distance from the first pole to the 16th pole?
3. The distance around my farm is 400m. If I want posts for fencing spaced 4m, how many posts will I need?

REFERENCE

Macmillan Primary Mathematics Bk 7 Pg 81.

VOLUME AND SURFACE AREA

SUB TOPIC: Converting from square centimetres (cm^2) to square metres(m^2) and vice versa.

$$\begin{aligned}1\text{m} &= 100\text{cm} \\1\text{m}^2 &= 1\text{m} \times 1\text{m} \\&= 100\text{cm} \times 100\text{cm} \\&= 10,000\text{cm}^2\end{aligned}$$

Examples

1. Convert the following as instructed.
 - (a). 0.5 m^2 to square centimetres.

$$1\text{m}^2 = 10,000\text{cm}^2$$

$$\begin{aligned}0.5\text{m}^2 &= 0.5 \times 10,000\text{cm}^2 \\&\equiv 5,000\text{cm}^2\end{aligned}$$

- (b). 8000cm^2 to square metres

$$10,000\text{cm}^2 = 1\text{m}^2$$

$$5000\text{cm}^2 = \frac{5,000\text{cm}^2}{10,000\text{cm}^2} = \frac{1}{2} \text{ m}^2$$

- a. 2m^2
 - b. 45m^2
 - c. 0.03m^2

- a. $700,000\text{cm}^2$
 - b. $1,200\text{cm}^2$
 - c. $88,800\text{cm}^2$

SUB TOPIC: Converting from square kilometres (km^2) to square metres(m^2) and vice versa.

$$\begin{aligned}1\text{km} &= 1000\text{m} \\1\text{km}^2 &= 1\text{km} \times 1\text{km} \\&= 1000\text{m} \times 1000\text{m} \\&= 1,000,000\text{m}^2\end{aligned}$$

Examples

- Convert the following as instructed.

(a). 0.5 km^2 to square metres.

$$1\text{km}^2 = 1,000,000\text{m}^2$$

$$0.5\text{km}^2 = 0.5 \times 1,000,000\text{m}^2$$

$$\underline{\underline{= 500,000\text{m}^2}}$$

(b). $970,000\text{m}^2$ to square kilometres

$$1,000,000\text{m}^2 = 1\text{km}^2$$

$$970,000\text{m}^2 = \frac{970,000\text{m}^2}{1,000,000\text{m}^2}$$

$$\begin{aligned} &= \frac{97}{100} \text{ km}^2 \\ &= 0.97\text{km}^2 \end{aligned}$$

- Convert the following to square metres.

d. 2km^2

e. 45km^2

f. 0.03km^2

- Convert the following to square kilometres

d. $67,000,000\text{m}^2$

e. $1,200\text{m}^2$

f. $88,800\text{m}^2$

SUB TOPIC: Converting from cubic metres (m^3) to cubic centimetres(cm^3) and vice versa.

$$1\text{m} = 100\text{cm}$$

$$1\text{m}^3 = 1\text{m} \times 1\text{m} \times 1\text{m}$$

$$= 100\text{cm} \times 100\text{cm} \times 100\text{cm}$$

$$= 1,000,000\text{cm}^3$$

Examples

- Convert the following as instructed.

(a). 0.24 m^3 to cubic centimetres.

$$1\text{m}^3 = 1,000,000\text{cm}^3$$

$$0.24\text{m}^3 = 0.24 \times 1,000,000\text{cm}^3$$

$$\underline{\underline{= 240,000\text{cm}^3}}$$

(b). $8,600,000\text{cm}^3$ to cubic metres

$$1,000,000\text{cm}^3 = 1\text{m}^3$$

$$8,600,000\text{cm}^3 = \frac{8,600,000\text{cm}^3}{1,000,000\text{cm}^3}$$

$$= \frac{86}{10} \text{ m}^3 = 8.6\text{m}^3$$

- Convert the following to cubic centimetres.

g. $2\frac{1}{2}\text{m}^3$

h. 82m^3

i. 0.63m^3

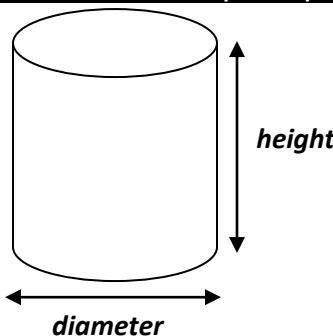
- Convert the following to square metres

g. $3,900,000\text{cm}^3$

h. $1,600\text{cm}^3$

i. $40,800\text{cm}^3$

SUB TOPIC: Volume and capacity of cylinders



NOTE

$1\text{litre} = 1,000\text{cm}^3$

$\text{Volume} = \text{base area} \times \text{height}$

$\text{volume} = \pi r^2 h$

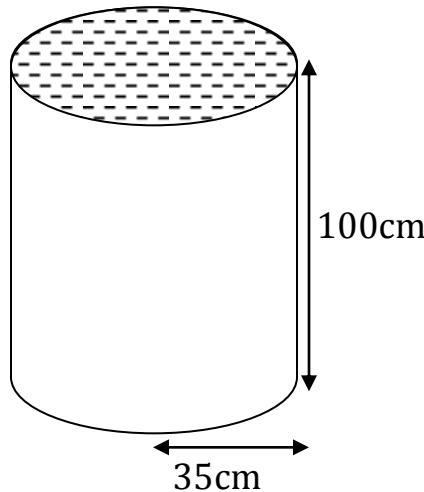
Examples

- Calculate the volume of a cylinder whose radius is 14cm and height is 30cm.

$$\text{Volume} = \pi r^2 h$$

$$\begin{aligned}
 &= \frac{22}{7} \times 14\text{cm} \times 14\text{cm} \times 30\text{cm} \\
 &= 22 \times 14\text{cm} \times 2\text{cm} \times 30\text{cm} \\
 &= 44 \times 420\text{cm}^3 \\
 &\underline{= 18480\text{cm}^3}
 \end{aligned}$$

- Below is a cylindrical tank. Study it and use it to answer the questions that follow.



- (a) Calculate the volume of the tank.

$$\text{Volume} = \pi r^2 h$$

$$\begin{aligned}
 &= \frac{22}{7} \times 35\text{cm} \times 35\text{cm} \times 100\text{cm} \\
 &= 22 \times 5\text{cm} \times 35\text{cm} \times 100\text{cm} \\
 &= 110 \times 3500\text{cm}^3 \\
 &\underline{= 385,000\text{cm}^3}
 \end{aligned}$$

(b). How many litres of water can it hold when full.

$$1000\text{cm}^3 = 1 \text{ litre}$$

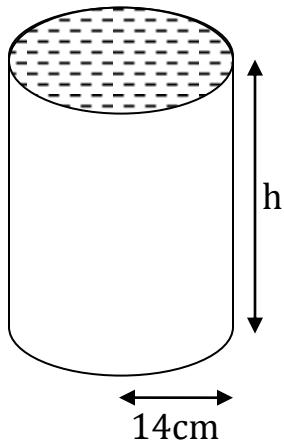
$$385,000\text{cm}^3 = \frac{385,000\text{cm}^3}{1,000\text{cm}^3}$$

$$= \underline{\underline{385 \text{ Litres}}}$$

SUB TOPIC: Finding missing sides volume and capacity of cylinders

Examples

1. The volume of the cylinder below is 18480cm^3 . Find the value of h.



$$\pi r^2 h = \text{Volume}$$

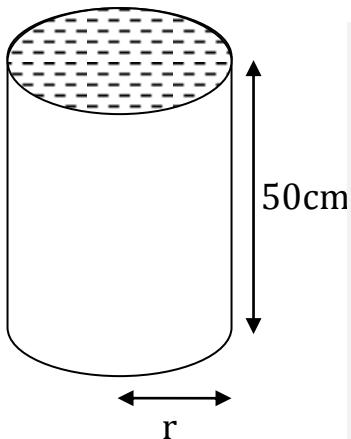
$$\frac{22}{7} \times 14\text{cm} \times 14\text{cm} \times h = 18480\text{cm}^3$$

$$44\text{cm} \times 14\text{cm} \times h = 18480\text{cm}^3$$

$$\frac{44\text{cm} \times 14\text{cm} \times h}{44\text{cm} \times 14\text{cm}} = \frac{18480\text{cm}^3}{44\text{cm} \times 14\text{cm}}$$

$$\underline{\underline{h = 30\text{cm}}}$$

2. The tank below holds 123.2 litres of water when full. Find its radius



$$\frac{\pi r^2 h}{1000\text{cm}^3} = \text{capacity}$$

$$\frac{\frac{22}{7} \times r \times r \times 50\text{cm}}{1000\text{cm}^3} = 123.2 \text{ l}$$

$$1000\text{cm}^3 \times \frac{\frac{22}{7} \times r \times r \times 50\text{cm}}{1000\text{cm}^3} = 123.2 \times 1000\text{cm}^3$$

$$7 \times \frac{1100\text{cm}r^2}{7} = 123200\text{cm}^3 \times 7$$

$$1100\text{cm}r^2 = 123200\text{cm}^3 \times 7$$

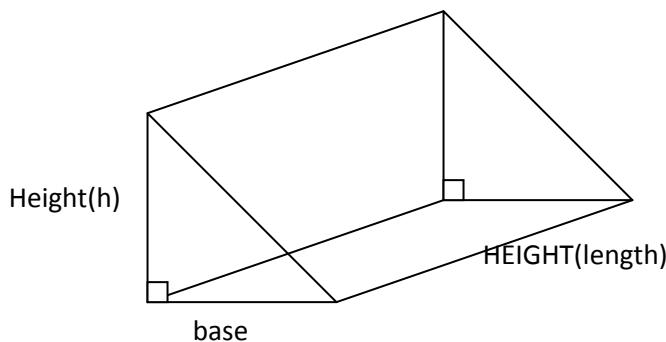
$$\frac{1100\text{cm}r^2}{1100\text{cm}} = \frac{123200\text{cm}^3 \times 7}{1100\text{cm}}$$

$$r^2 = 784\text{cm}^2$$

$$\sqrt{r^2} = \sqrt{784\text{cm}^2}$$

$$\underline{\underline{r = 28\text{cm}}}$$

SUB TOPIC: Volume and capacity of triangular prisms



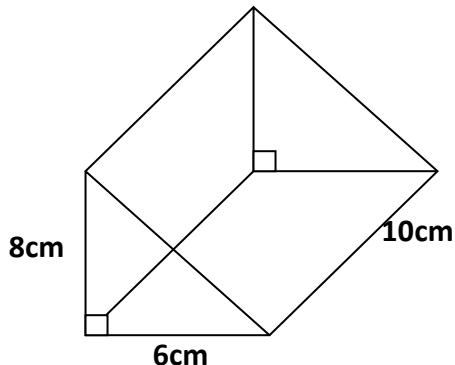
Volume = base area x height

$$\text{Volume} = \frac{1}{2}bh \times l$$

$$volume = \frac{1}{2}bhl$$

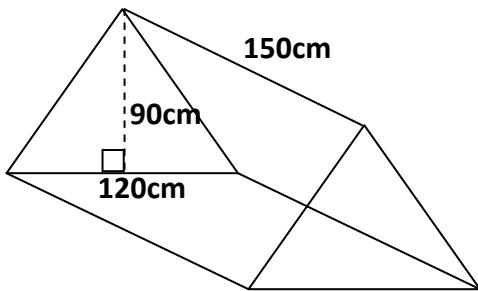
Examples

- Find the volume of the figure below



$$\begin{aligned} Volume &= \frac{1}{2}bhl \\ &= \frac{1}{2} \times 6\text{cm} \times 8\text{cm} \times 10\text{cm} \\ &= 3 \times 80\text{cm}^3 \\ &= 240\text{cm}^3 \end{aligned}$$

- Calculate the capacity of the figure below.



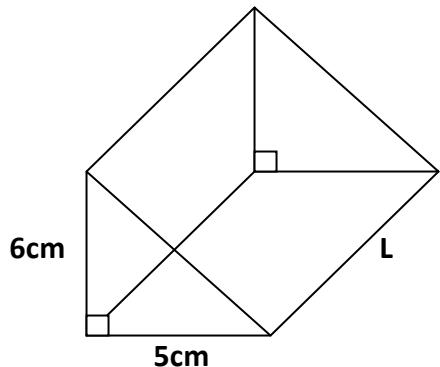
$$\begin{aligned} Volume &= \frac{1}{2}bhl \\ &= \frac{1}{2} \times 120\text{cm} \times 90\text{cm} \times 150\text{cm} \\ &= 60 \times 90 \times 150\text{cm}^3 \\ &= 5400 \times 150\text{cm}^3 \\ &= 810,000\text{cm}^3 \\ 1000\text{cm}^3 &= 1\text{litre} \\ \frac{810,000\text{cm}^3}{1,000\text{cm}^3} & \\ 810 &\text{ litres} \end{aligned}$$

Mathematics is the Key

SUB TOPIC: Finding missing sides of a triangular prism when given volume.

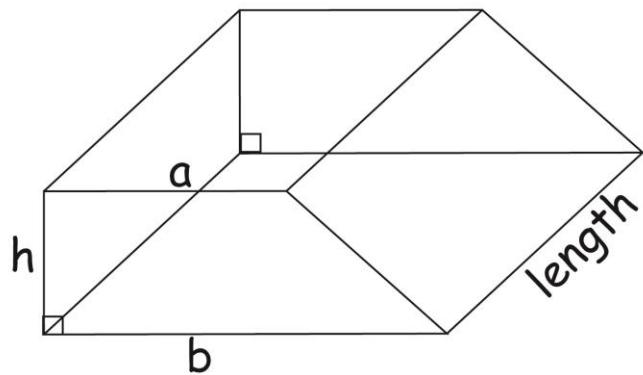
Examples

1. Find the missing side in the figure below given that its volume is 135cm^2



$$\begin{aligned}\frac{1}{2} bhl &= \text{Volume} \\ \frac{1}{2} \times 5\text{cm} \times 6\text{cm} \times L &= 135\text{cm}^3 \\ 3\text{cm} \times 5\text{cm} \times L &= 135\text{cm}^3 \\ \frac{3\text{cm} \times 5\text{cm} \times L}{3\text{cm} \times 5\text{cm}} &= \frac{135\text{cm}^3}{3\text{cm} \times 5\text{cm}} \\ L &= 9\text{cm}\end{aligned}$$

SUBTOPIC: Volume and capacity of trapezoidal prism



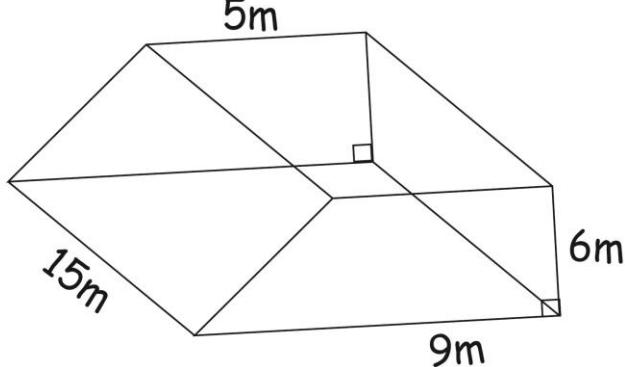
Volume = base area \times height

$$\text{Volume} = \frac{1}{2} h(a + b) \times L$$

$$\text{Volume} = \frac{1}{2} h(a + b)L$$

Examples

1. Calculate the volume of the figure below.



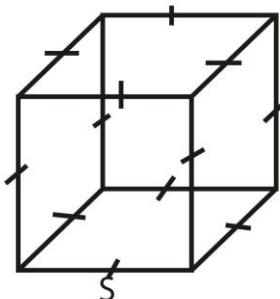
$$\begin{aligned}\text{Volume} &= \frac{1}{2} h(a + b)L \\ &= \frac{1}{2} \times 6\text{m} \times (5\text{m} + 9\text{m}) \times 15\text{m} \\ &= 3\text{m} \times 14\text{m} \times 15\text{m} \\ &= 42\text{m}^2 \times 15\text{m} \\ &= 630\text{m}^3\end{aligned}$$

Mathematics is the key

SUBTOPIC: Total surface area of cubes and cuboids

Total surface area is the area of all faces

CUBE



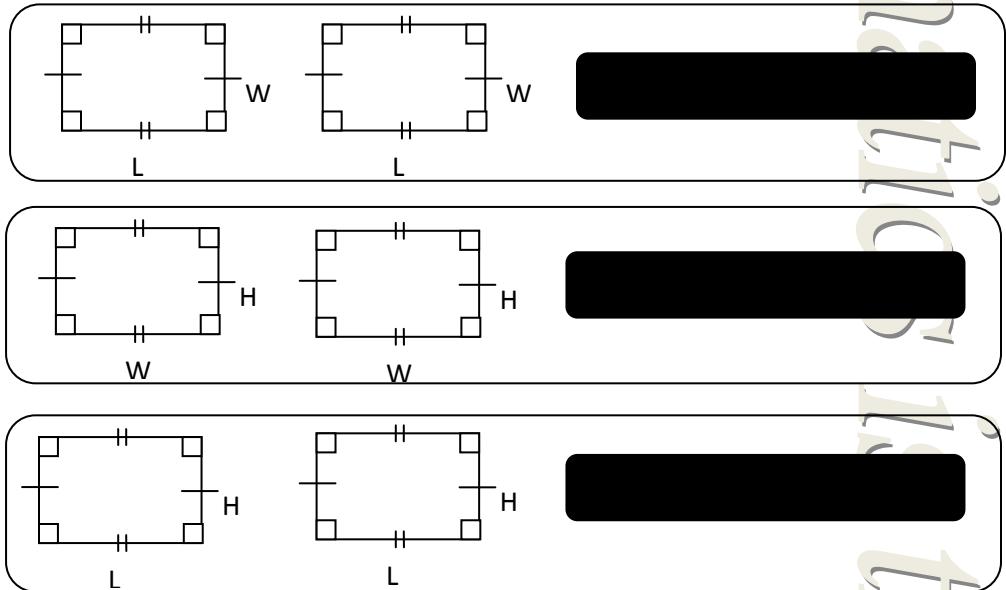
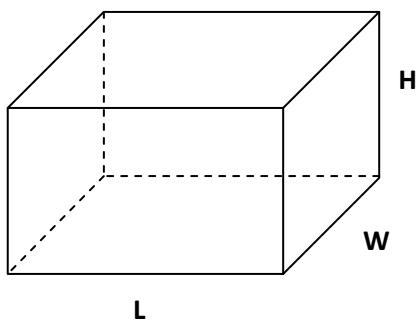
A cube has six equal faces of which they are all squares.

Area of a square is ($S \times S$)

$$TSA = 6 \times S \times S$$

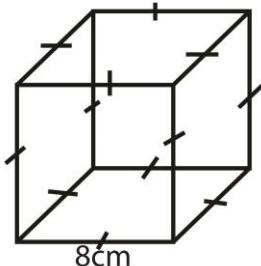
$$TSA = 6 \times S^2$$

$$TSA = 6S^2$$



$$\text{TOTAL SURFACE AREA} = 2(L \times W) + 2(W \times H) + 2(L \times H)$$

1. Find the total surface area of the figures below.

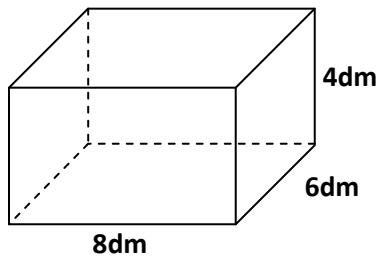


$$TSA = 6 \times S \times S$$

$$= 6 \times 8\text{cm} \times 8\text{cm}$$

$$= 6 \times 64\text{cm}^2$$

$$\underline{\underline{= 384\text{cm}^2}}$$



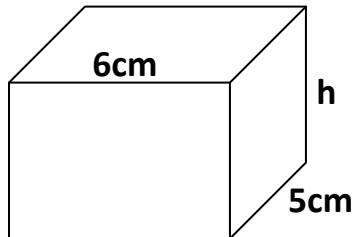
$$\begin{aligned}
 TSA &= 2(L \times W) + 2(W \times H) + 2(L \times H) \\
 &= 2(8dm \times 6dm) + 2(8dm \times 4dm) + 2(6dm \times 4dm) \\
 &= 2 \times 48dm^2 + 2 \times 32dm^2 + 2 \times 24dm^2 \\
 &= 96dm^2 + 64dm^2 + 48dm^2 \\
 &\equiv \underline{\underline{208dm^2}}
 \end{aligned}$$

2. Find the total surface area of the box measuring 10cm by 5cm by 4cm.
3. Find the total surface of the cube whose side is 10cm.

SUBTOPIC: Finding missing sides when given TSA of a cuboid.

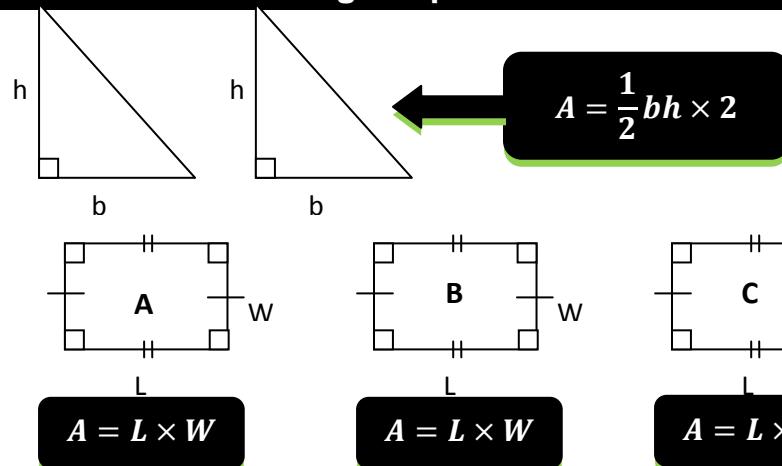
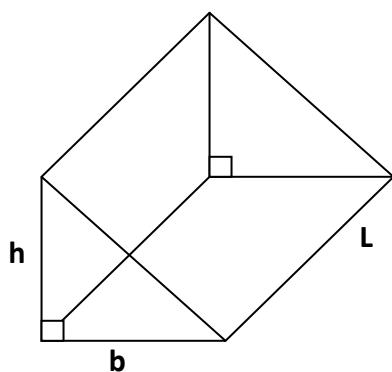
Examples

The total surface area of a cuboid is $148cm^2$. Find the value of h .



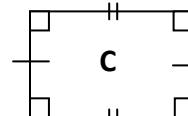
$$\begin{aligned}
 2(L \times W) + 2(W \times H) + 2(L \times H) &= TSA \\
 2(6cm \times 5cm) + 2(5cm \times h) + 2(6cm \times h) &= 148cm^2 \\
 2 \times 30cm^2 + 2 \times 5hcm + 2 \times 6hcm &= 148cm^2 \\
 60cm^2 + 10hcm + 12hcm &= 148cm^2 \\
 22hcm + 60cm^2 &= 148cm^2 \\
 22hcm + 60cm^2 - 60cm^2 &= 148cm^2 - 60cm^2 \\
 22hcm &= 88cm^2 \\
 \frac{22hcm}{22cm} &= \frac{88cm^2}{22cm} \\
 h &= 4cm
 \end{aligned}$$

SUBTOPIC: Finding total surface area of a triangular prism



$$A = L \times W$$

$$A = L \times W$$



$$A = L \times W$$

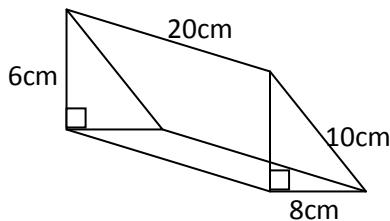


EXAMPLE

Find the total surface area of the triangular prism below.

Examples:

- Find the surface area of the figure below.



$$\frac{1}{2}bh \times 2$$

$$L \times W$$

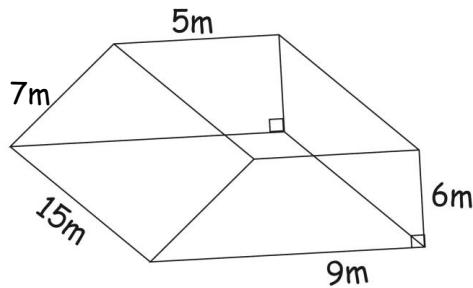
$$L \times W$$

$$L \times W$$

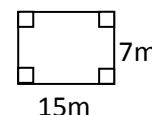
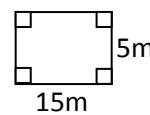
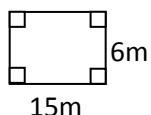
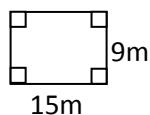
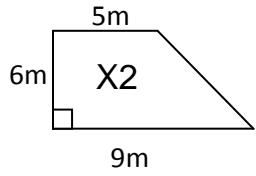
$$TSA = \frac{1}{2}bh \times 2 + L \times W + L \times W + L \times W$$

$$\left(\frac{1}{2} \times 8\text{cm} \times 6\text{cm} \times 2\right) + (8\text{cm} \times 20\text{cm}) + (10\text{cm} \times 20\text{cm}) + (6\text{cm} \times 20\text{cm}) \\ 48\text{cm}^2 + 160\text{cm}^2 + 200\text{cm}^2 + 120\text{cm}^2 \\ 208\text{cm}^2 + 320\text{cm}^2 \\ \underline{528\text{cm}^2}$$

SUB TOPIC: TSA of a trapezoidal prism



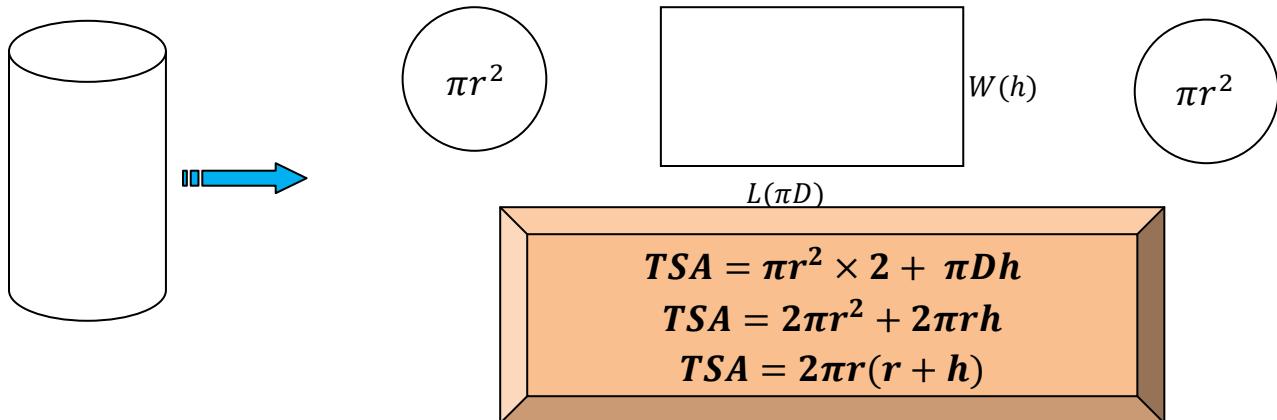
Main parts of the trapezoidal prism



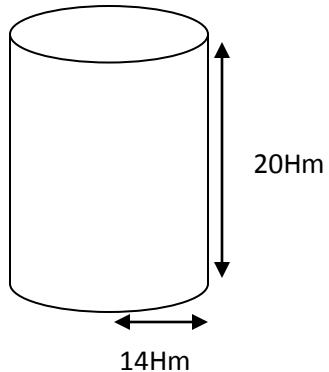
$$TSA = \frac{1}{2}h(a + b) \times 2 + L \times W + L \times W + L \times W + L \times W$$

$$6m(9m + 5m) + (15m \times 9m) + (15m \times 6m) + (15m \times 5m) + (15m \times 7m) \\ (6m \times 14m) + 135m^2 + 90m^2 + 75m^2 + 105m^2 \\ 84m^2 + 225m^2 + 180m^2 \\ \underline{489m^2}$$

SUB TOPIC: Total surface area of closed cylinders



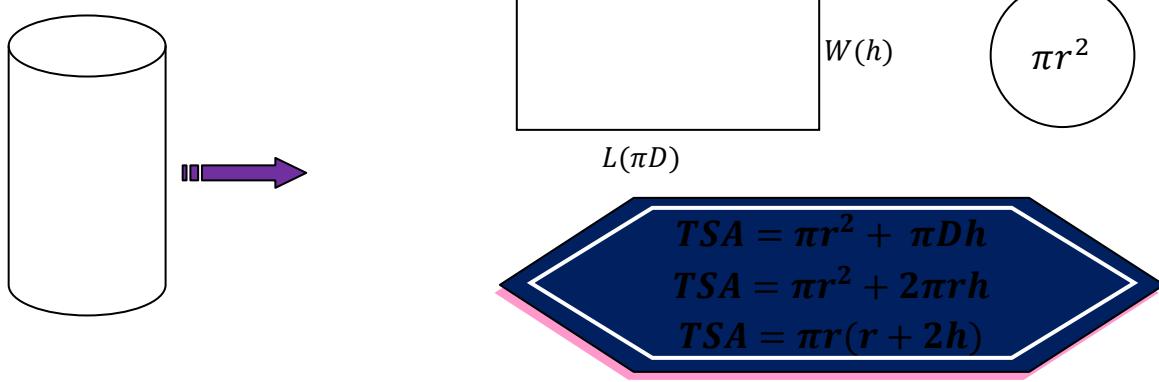
- Calculate the TSA of the cylinder below. (take pi as $\frac{22}{7}$)



$$\begin{aligned}
 & TSA = 2\pi r(r + h) \\
 & 2 \times \frac{22}{7} \times 14Hm(14Hm + 20Hm) \\
 & 44 \times 2Hm \times 34Hm \\
 & 88Hm \times 34Hm \\
 & \underline{\underline{TSA = 2992Hm^2}}
 \end{aligned}$$

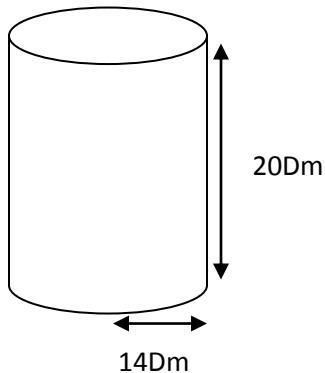
- Find the total surface area of a cylinder whose radius is 7cm and height 10cm

SUBTOPIC: Finding total surface of a cylinder open one end.



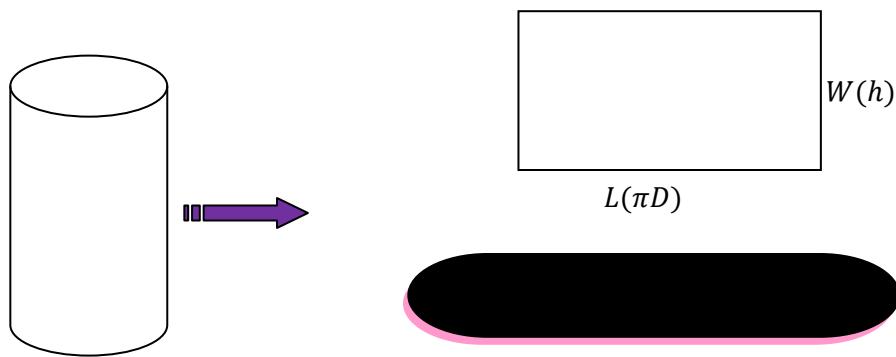
Mathematics is the key

Below is a metallic drum without a lid. Use it to answer the questions that follow.



$$\begin{aligned}TSA &= \pi r(r + 2h) \\ \frac{22}{7} \times 14Hm &(14Hm + 2 \times 20Hm) \\ 44Dm \times (14 + 40)Dm & \\ 44Dm \times 54Dm & \\ \underline{TSA = 2376Dm^2} &\end{aligned}$$

SUB TOPIC: Finding total surface area of hollow cylinders



A metallic drum of radius 21cm and height 75cm was cut properly to form a metallic door for the kitchen. Calculate the area of the door that was formed.

area of the door

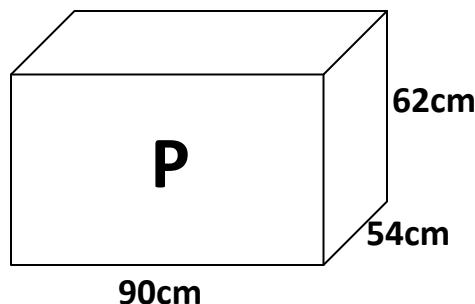
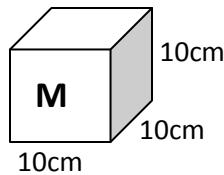
$$\begin{aligned}Area &= Circumference \times Height \\ &= \pi D \times h \\ &= \frac{22}{7} \times (21cm + 21cm) \times 75cm \\ &= \frac{22}{7} \times 42cm \times 75cm \\ &= 22 \times 6cm \times 75cm \\ &= 132cm \times 75cm \\ &= \underline{9900cm^2}\end{aligned}$$

Mathematics is the Key

SUBTOPIC: Packing boxes in boxes.

Examples.

1. Boxes of size M were packed in box P. Study them and answer the questions that follow.



- (a) How many boxes were packed in the first layer?

Along the length

$$\frac{90\text{cm}}{10\text{cm}} = 9 \text{ boxes}$$

Along the width

$$\frac{54\text{cm}}{10\text{cm}} = 5 \text{ boxes}$$

No. of boxes

$$9 \times 5 = 45 \text{ boxes}$$

- (b) How many layers of box M were formed in box P?

Along the height

$$\frac{62\text{cm}}{10\text{cm}} = 6 \text{ layers}$$

- (c).how many boxes were packed in the whole box

$$45 \times 6 = 270 \text{ boxes}$$

- (c) Calculate the volume of the space that remained.

Volume of the box P

$$\begin{aligned}V &= L \times W \times H \\&= 90\text{cm} \times 54\text{cm} \times 62\text{cm} \\&= 4860\text{cm}^2 \times 62\text{cm} \\&= 301320\text{cm}^3\end{aligned}$$

Volume of 270 small boxes

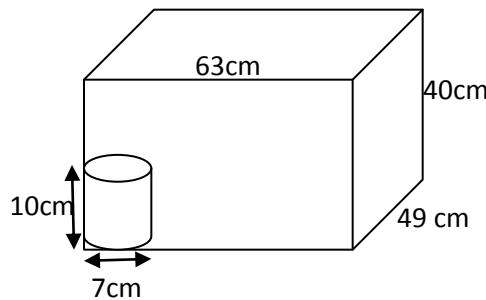
$$\begin{aligned}V &= S \times S \times S \times 270 \\&= 10\text{cm} \times 10\text{cm} \times 10\text{cm} \times 270 \\&= 1000\text{cm}^3 \times 270 \\&= 270,000\text{cm}^3\end{aligned}$$

Volume of the remaining space

$$\begin{aligned}&301,320\text{cm}^3 \\&- 270,000\text{cm}^3 \\&\hline 31,320\text{cm}^3\end{aligned}$$

SUBTOPIC: Packing cylinders in boxes

Tins of wood glue were packed in the box as shown below.



(a) How many tins were packed in the box altogether?

Along the length

$$\frac{63\text{cm}}{7\text{cm}} = 9 \text{ tins}$$

Along the width

$$\frac{49\text{cm}}{7\text{cm}} = 7 \text{ tins}$$

Along the height

$$\frac{40\text{cm}}{10\text{cm}} = 4 \text{ tins}$$

No. of tins

$$9 \times 7 \times 4 = 252 \text{ tins}$$

(b) Calculate the volume of the space that was left after packing.

Volume of the box

$$\begin{aligned} V &= L \times W \times H \\ &= 63\text{cm} \times 49\text{cm} \times 40\text{cm} \\ &= 3087\text{cm}^2 \times 40\text{cm} \\ &= 123,480\text{cm}^3 \end{aligned}$$

Volume of 252 tins

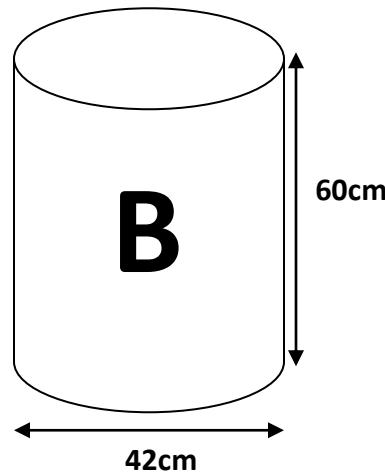
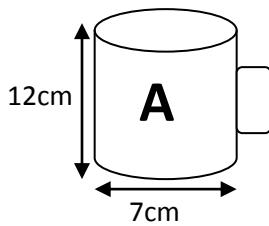
$$\begin{aligned} V &= \pi r^2 h \times 252 \\ &= \frac{22}{7} \times \frac{7\text{cm}}{2} \times \frac{7\text{cm}}{2} \times 10\text{cm} \times 252 \\ &= 77\text{cm}^2 \times 5\text{cm} \times 252 \\ &= 97,020\text{cm}^3 \end{aligned}$$

Volume of the remaining space

$$\begin{aligned} &123,480\text{cm}^3 \\ &- 97,020\text{cm}^3 \\ &\hline 26,460\text{cm}^3 \end{aligned}$$

SUB TOPIC: Comparing volume

At a party, milk was served using cups of size A from container B as shown below.



(a) How many full cups of milk were served to the visitors?

$$\frac{\text{volume of } B}{\text{volume of } A}$$

$$\frac{\pi r^2 h}{\pi r^2 h}$$

$$\begin{aligned} &\frac{22}{7} \times \frac{42\text{cm}}{2} \times \frac{42\text{cm}}{2} \times 60\text{cm} \\ &\frac{22}{7} \times \frac{7\text{cm}}{2} \times \frac{7\text{cm}}{2} \times 12\text{cm} \end{aligned}$$

$$\frac{11 \times 6\text{cm} \times 21\text{cm} \times 60\text{cm}}{11\text{cm} \times 7\text{cm} \times 6\text{cm}}$$

$$3 \times 60$$

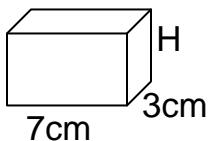
$$\underline{180 \text{ full cups}}$$

(b) If each visitor drank two cups, how many visitors attended the party?

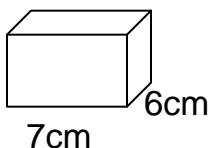
$$180 \div 2 = 90 \text{ visitors}$$

TOPICAL QUESTIONS

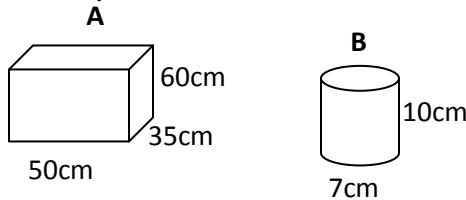
1. How many centimeters are in 0.75 metres?
2. The circumference of a circle is 17.584cm. Find the radius of the circle
(Use $\pi = 3.14$)
3. A cylindrical tank is 7m high. What is the capacity (in litres) of the tank if its radius is 7m?
4. The volume of the figure below is 105cm^3 . Find its height.



5. Find the base area of the figure below.



6. Given that the cylindrical tins B are to be packed into box A.



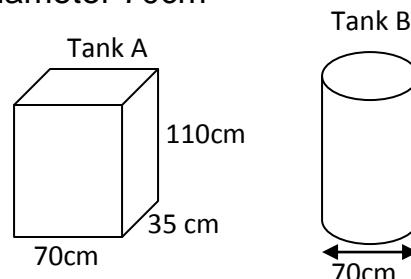
- (a) How many tins will be packed in the box?
- (b) If container A is a tank full of water, how many full cups of container B can you draw from the tank?

7. Abdul cut out circular plates of diameter 7cm from a rectangular sheet of metal of length 45cm and width 35cm as shown below.
 - (a) How many circular plates did he cut out from the rectangular sheet?
 - (b) Find the area of the unused sheet after cutting

out the circular plates.

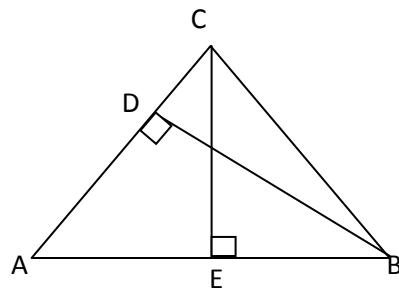
(take $\pi = \frac{22}{7}$)

8. A cuboid water tank (A) which is 70cm long by 35cm wide by 110cm high was filled with water. The water from tank A was all poured into the cylindrical tank B of diameter 70cm

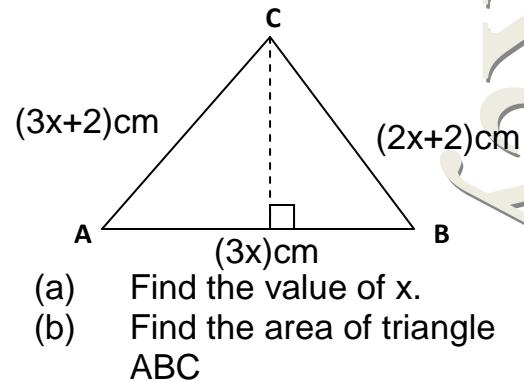


- (a) Find the volume of water in tank A when full.
- (b) Find the new height of water after it has been poured into tank B. (take $\pi = \frac{22}{7}$)

9. In the triangle below, $AB = 12\text{cm}$, $CE = 10\text{cm}$ and $AC = 16\text{cm}$. Find the length of BD in cm.

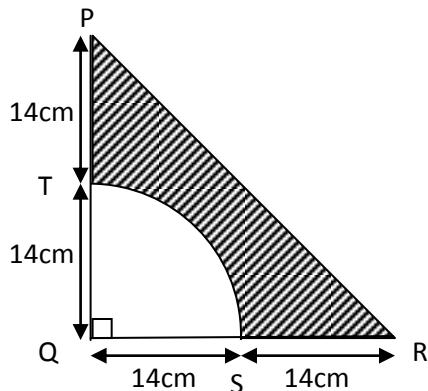


10. The figure ABC below is an isosceles triangle. Use it to answer the questions that follow.



- (a) Find the value of x .
- (b) Find the area of triangle ABC

- (c) Calculate the perimeter of the triangle.
- (d) Find the circumference of a circular compound whose radius is 14m. (take $\pi = \frac{22}{7}$)
11. In the figure below, $PQ = QR = 28\text{cm}$ use it to answer the questions that follow.



- (a) Find the area of triangle PQR.
(b) Find the area of the sector QST
(c) What is the area of the shaded part?

Mathematics is the Key

ALGEBRA

SUB TOPIC: SUBSTITUTION

CONTENT: Substituting or replacement of letters with numbers

$$1. \text{ If } a = 5, b = 4 \text{ and } c = 0$$

Find the value of $a + b + c$

$$5 + 4 + 0$$

$$9 + 0$$

$$9$$

$$2. \text{ Given that } x = 2 \text{ and } y = -2$$

Evaluate $x - y$

$$(x) - (y)$$

$$2 - (-2)$$

$$2 + 2$$

$$4$$

$$3. \text{ Given } a = \frac{3}{4}, b =$$

$\frac{1}{3}$. Find the value of $a + b$

$$(a) + (b)$$

$$\frac{3}{4} + \frac{1}{3}$$

$$9 + 4$$

$$\frac{12}{12}$$

$$\frac{13}{12}$$

$$\frac{1}{12}$$

$$4. \text{ If } y = 2,$$

(a). what is the value of $3y^2$?

$$3y^2 = 3 \times y \times y$$

$$= 3 \times 2 \times 2$$

$$= 3 \times 4$$

$$= 12$$

(b) what is the value of $(3y)^2$?

$$(3y)^2 = 3y \times 3y$$

$$= 3 \times 2 \times 3 \times 2$$

$$= 6 \times 6$$

$$= 36$$

5. Given that $a = 3, b = 4$ and $c = 5$

(a). What is $3a \times 3b$

(b) What is $c(b - a)$

6. If $m = 2$, what is the value of m^6 ?

7. If $a = \frac{1}{2}, c = \frac{2}{3}$ and $d =$

$\frac{1}{4}$. Evaluate $ac + d$

8. If $m = 4, n = 3$ and $p = 2$, what is $\frac{n^3 \times m^2}{mp}$

REFERENCE

A New MK Primary Mathematics 2000 Bk 7 Pg 434 (New Edition)

SUB TOPIC: Collecting and simplifying like terms

Examples:

$$1. \quad a + a + a = 3a$$

$$2. \quad 2p + 3p + p = 6p$$

$$3. \quad 2ab + ab + 5ab = 8ab$$

$$4. \quad \begin{aligned} x + y + x + y + x \\ x + x + x + y + y \\ \underline{3x + 2y} \end{aligned}$$

$$5. \quad \begin{aligned} 3p - 6f - p + 2f \\ 3p - p + 2f - 6f \\ \underline{2p - 4f} \end{aligned}$$

Simplify the following

$$(a) 2m + m + 4m$$

$$(b) 6k + 4p - 3k - 5p$$

$$(c) 2xy - y + 5xy - y$$

REFERENCE

A New MK Primary Mathematics 2000 Bk 7 Pg 430 & 431 (New Edition)

SUB TOPIC: Addition and subtraction

1. Simplify the following

(a) $\frac{2m}{3} + \frac{m}{2}$

$$\begin{aligned} &\frac{2m}{3} \times \frac{2}{2} + \frac{m}{2} \times \frac{3}{2} \\ &\frac{4m}{6} + \frac{3m}{6} \\ &\frac{4m + 3m}{6} \\ &\frac{7m}{6} \\ &1\frac{1}{6}m \end{aligned}$$

(b) $p - \frac{p}{3}$

$$\begin{aligned} &p - \frac{p}{3} \\ &\frac{1}{1} - \frac{1}{3} \\ &\frac{p}{1} \times 3 - \frac{p}{3} \times 3 \\ &\frac{3p - p}{3} \\ &\frac{2p}{3} \end{aligned}$$

2. Simplify the following

(a) $\frac{3d}{4} + d + \frac{d}{2}$

(b) $\frac{3r}{7} - \frac{2r}{6} + \frac{r}{4}$

REFERENCE

A New MK Primary Mathematics 2000 Bk 7 Pg 435 (New Edition)

SUB TOPIC: multiplication and division

1. Simplify the following.

(a) $\frac{3k}{7} \times \frac{1}{6}$

$$\frac{3k}{7} \times \frac{1}{6}$$

$$\frac{3k}{42}$$

$$\frac{k}{14}$$

(b) $\frac{\frac{4m}{11}}{\frac{m}{15}}$

$$\begin{aligned} &\frac{4m}{11} \div \frac{m}{15} \\ &\frac{4m}{11} \times \frac{15}{m} \\ &\frac{60}{11} \\ &\frac{5\frac{5}{11}}{11} \end{aligned}$$

(c) $\frac{6x}{9} \times \frac{1}{2} \div \frac{x}{4}$

(d) $\frac{3b}{13} \times \frac{3b}{5}$

SUB TOPIC: Factorising completely

Examples

1. Factorise $4xy - 12y$ completely

| | | |
|-----|-------|--------|
| 2 | $4xy$ | $-12y$ |
| 2 | $2xy$ | $-6y$ |
| y | xy | $-y$ |
| | x | -1 |

$$2 \times 2 \times y(x - 1)$$

$$4y(x - 1)$$

2. Factorise $2\pi r^2 + 2\pi rh$ completely

| | | |
|-------|------------|-----------|
| 2 | $2\pi r^2$ | $2\pi rh$ |
| π | πr^2 | πrh |
| r | r^2 | rh |
| | r | h |

$$2 \times \pi \times r(r + h)$$

$$2\pi r(r + h)$$

3. Factorise the following completely.

(a) $4mn - 18mn^2$

(b) $3a + 12ab - 18$

SUB TOPIC: Removing brackets

REMEMBER:

- When removing brackets, multiply the factor by every term inside brackets.
- A negative integer before brackets affects every sign inside brackets.
- A positive integer before brackets cannot affect the signs inside brackets.

Remove the brackets and simplify.

Example:

1. $3(x + y)$

$3(x + y)$

$3x + 3y$

2. $2(a - b)$

$2(a - b)$

$2a - 2b$

3. $4(2x - 6)$

4. $-9(m - 4)$

5. Add: $x + 4$ to $x + 1$

$(x + 4) + (x + 1)$

$X + 4 + x + 1$

$X + x + 4 + 1$

$2x + 5$

6. Subtract $y - 1$ from $2y + 3$

$(2y + 3) - (y - 1)$

$2y + 3 - y + 1$

$2y - y + 3 + 1$

$y + 4$

7. Add. $x - 4$ to $3x - 5$

8. Subtract $3p - 1$ from $5p - 3$

9. Find the supplement of $(x - 20)^\circ$

REFERENCE

A New MK Primary Mathematics 2000 Bk
7 Pg 432,433 & 434 (New Edition)

SUB TOPIC: Removing brackets involving fractions

Example:

Remove brackets and simplify

1. $\frac{1}{3}(3a + 9b)$

$\frac{1}{3}(3a + 9b)$

$(\frac{1}{3} \times 3a) + (\frac{1}{3} \times 9b)$

$a + 3b$

2. $\frac{3}{4}(8m - 12p)$

$\frac{3}{4} \times 8m - \frac{3}{4} \times 12p$

$3 \times 2m - 3 \times 3p$

$6m - 9p$

3. Half of $(2x + 4y)$ plus a third of $(6x + 9y)$

$\frac{1}{2}(2x + 4y) + \frac{1}{3}(6x + 9y)$

$\frac{1}{2} \times 2x + \frac{1}{2} \times 4y + \frac{1}{3} \times 6x + \frac{1}{3} \times 9y$

$x + 2y + 2x + 3y$

$x + 2x + 2y + 3y$

$3x + 5y$

4. Subtract $\frac{1}{2}(4x - 2y)$ from $\frac{1}{3}(6x - 9y)$

$$\begin{aligned}\frac{1}{3}(6x - 9y) - \frac{1}{2}(4x - 2y) \\ \frac{1}{3}x 6x - \frac{1}{3}x 9y - \frac{1}{2}x 4x + \frac{1}{2}x 2y \\ 2x - 3y - 2x + y \\ 2x - 2x - 3y + y \\ \underline{- 2y}\end{aligned}$$

5. Subtract $\frac{2}{3}(6x - 3y)$ from $\frac{1}{4}(8x - 12y)$

6. Remove brackets and
simplify. $\frac{2}{5}(5x + 15y) -$
 $\frac{1}{6}(12x - 24y)$

REFERENCE

A New MK Primary Mathematics 2000 Bk
7 Pg 436 (New Edition)

REFERENCE

A New MK Primary Mathematics 2000 Bk
7 Pg 441 (New Edition)

SUB TOPIC: POWERS or INDICES
(multiplication of powers with similar bases)

NOTE:

When multiplying powers with similar bases, write a single base and add the powers.

Example:

Simplify the following

a) $4^3 x 4^2$

$4 \times 4 \times 4 \times 4 \times 4$

4^5

OR

$4^3 x 4^2$

4^{3+2}

4^5

b) $x^3 \times x^2$

$x \times x \times x \times x \times x$

x^5

OR

$x^3 \times x^2$

x^{3+2}

x^5

Simplify the following

(a) $m^2 \times m \times m^4$

(b) $3^2 \times 3^5$

(c) $b^7 \times b^6$

Mathematics is the key

2. $p^2 + p^2$
 $p^2 + p^2$
 $2p^2$

3. $3m^3 + 4m^3$
 $3m^3 + 4m^3$
 $7m^3$

4. $3p^2 - 2p^3$
 $3p^2 - 2p^3$ (they are unlike terms)
5. $4m^2 - m^2$
6. $20k^4 + 17k^4$
7. $b^5 - b^3$

REFERENCE

A New MK Primary Mathematics 2000 Bk 7 Pg 442 (New Edition)

SUB TOPIC: POWERS or INDICES (Division of powers with similar bases)

NOTE:

When dividing powers with similar bases, write a single base and subtract the powers.

Example:

Simplify the following.

1. $3^4 \div 3^2$

$$\begin{array}{r} 3 \times 3 \times 3 \times 3 \\ \hline 3 \times 3 \\ 3^2 \end{array}$$

OR

$$\begin{array}{r} 3^4 \div 3^2 \\ 3^{4-2} \\ \underline{\underline{3^2}} \end{array}$$

2. $p^8 \div p^2$

$$\begin{array}{r} p \times p \\ \hline p \times p \\ p \times p \times p \times p \times p \times p \times p \\ \underline{\underline{p^6}} \end{array}$$

OR

$$\begin{array}{r} p^{8 \div 2} \\ p^{8-2} \\ \underline{\underline{p^6}} \end{array}$$

3. $n^7 \div n^9$

$$\frac{n \times n \times n \times n \times n \times n \times n \times n}{n \times n \times n}$$

$$\frac{1}{n \times n}$$

$$\frac{1}{n^2}$$

$$n^{-2}$$

OR

$$\begin{array}{r} n^7 \div n^9 \\ n^{7-9} \\ \underline{\underline{n^{-2}}} \end{array}$$

4. Simplify the following

(a). $m^2 \div m$

(b). $3^2 \div 3^5$

(c). $b^3 \div b^6$

REFERENCE

A New MK Primary Mathematics 2000 Bk 7 Pg 442 (New Edition)

SUB TOPIC: POWERS or INDICES (Multiplication and Division of powers with similar bases)

1. Simplify the following.

i. $\frac{k^4 \times k^3}{k^5}$

$$(k^4 \times k^3) \div k^5$$

$$(k^{4+3}) \div k^5$$

$$k^7 \div k^5$$

$$k^{7-5}$$

$$k^2$$

ii. $\frac{w^3 \times w^0 \times w^6}{w^{10}}$

iii. $\frac{p^5 \times p^3}{p^4}$

SUB TOPIC: POWERS or INDICES

(Solving for unknown powers)

1. Solve for the unknowns

(a) $2^x = 8$

$2^x = 8$

$2^x = 2^3$

$\underline{x = 3}$

| | |
|---|---|
| 2 | 8 |
| 2 | 4 |
| 2 | 2 |
| 1 | |

$8 = 2^3$

(b) $3^m \times 3^2 = 81$

$3^m \times 3^2 = 81$

$3^{m+2} = 3^4$

$m + 2 = 4$

$m + 2 - 2 = 4 - 2$

$\underline{m = 2}$

| | |
|---|----|
| 3 | 81 |
| 3 | 27 |
| 3 | 9 |
| 3 | 3 |
| 1 | |

$81 = 3^4$

(c) $4^{2x} \div 16 = 64$

$4^{2x} \div 16 = 64$

$4^{2x} \div 4^2 = 4^3$

$4^{2x-2} = 4^3$

$2x - 2 = 3$

$2x - 2 + 2 = 3 + 2$

$2x = 5$

$\frac{2x}{2} = \frac{5}{2}$

$x = 2\frac{1}{2}$

| | |
|---|----|
| 4 | 64 |
| 4 | 16 |
| 4 | 4 |
| 1 | |

$64 = 4^3$

| | |
|---|----|
| 4 | 16 |
| 4 | 4 |
| 1 | |

$16 = 4^2$

(d) $5^k = 125$

(e) $2^{m+4} \times 8 = 1$

SUB TOPIC: Solving simple equations.

Example: Solve the following equations

a) $x + 5 = 13$

$x + 5 - 5 = 13 - 5$

$\underline{x = 8}$

b) $2x + 6 = 18$

$2x + 6 - 6 = 18 - 6$

$2x = 12$

$\frac{2x}{2} = \frac{12}{2}$

$\underline{x = 6}$

c) $y - 3 = 5$

$y - 3 + 3 = 5 + 3$

$\underline{y = 8}$

d) $3a - 8 = 7$

$3a - 8 + 8 = 7 + 8$

$3a = 15$

$\frac{3a}{3} = \frac{15}{3}$

$\underline{a = 5}$

e) $6m = 24$

f) $5k - 3 = 37$

g) $4 - x = 7$

h) $16 = 9 + 2p$

REFERENCE

A New MK Primary Mathematics 2000 Bk 7 Pg 452 - 456 (New Edition)

SUB TOPIC: Solving equations involving brackets.

Solve the following equations

a) $2(m + 4) = 20$

$2(m + 4) = 20$

$2m + 8 = 20$

$2m + 8 + 8 = 20 + 8$

$2m = 28$

$\frac{2m}{2} = \frac{28}{2}$

$\underline{m = 14}$

b) $2(k - 2) - 3(k - 4) = -10$

$2(k - 2) - 3(k - 4) = -10$

$2k - 4 - 3k + 12 = -10$

$2k - 3k - 4 + 12 = -10$

$-k + 8 = -10$

$-k + 8 - 8 = -10 - 8$

$-k = -18$

$\frac{-k}{-1} = \frac{-18}{-1}$

$\underline{k = 18}$

Mathematics is the key

- c) $6(z - 4) = 0$
 d) $3x - (2 - x) = 14$
 e) $5(m - 2) + 6(m - 3) = 16$

3. $0.4P + 0.5 = 2.1$

$$\begin{aligned} \frac{4P}{10} + \frac{5}{10} &= \frac{21}{10} \\ 10 \times \frac{4P}{10} + \frac{5}{10} \times 10 &= \frac{21}{10} \times 10 \\ 4p + 5 &= 21 \\ 4p + 5 - 5 &= 21 - 5 \\ 4p &= 16 \\ \frac{4p}{4} &= \frac{16}{4} \\ p &= 4 \end{aligned}$$

SUB TOPIC: Solving equations involving fractions

When solving fractional equations, multiply the LCD (LCM of the denominators) on each algebraic term.

Solve the following equations

1. $\frac{1}{2}p = 6$

$\frac{1}{2}p = 6$

LCD = 2

$2 \times \frac{p}{2} = 6 \times 2$

$p = 12$

2. $\frac{13t}{3} + 2 = 15$

$\frac{13t}{3} + \frac{2}{1} = \frac{15}{1}$

LCD = 3

$3 \times \frac{13t}{3} + \frac{2}{1} \times 3 = \frac{15}{1} \times 3$

$13t + 6 = 45$

$13t + 6 - 6 = 45 - 6$

$13t = 39$

$\frac{13t}{13} = \frac{39}{13}$

$t = 3$

4. $3x + 7 - \frac{3x}{4} = 10$

$\frac{3x}{1} + \frac{7}{1} - \frac{3x}{4} = \frac{10}{1}$

LCD = 4

$4 \times \frac{3x}{1} + \frac{7}{1} \times 4 - \frac{3x}{4} \times 4 = \frac{10}{1} \times 4$

$12x + 28 - 3x = 40$

$12x - 3x + 28 = 40$

$9x + 28 = 40$

$9x + 28 - 28 = 40 - 28$

$\frac{9x}{9} = \frac{12}{9}$

$x = 1\frac{1}{3}$

5. $\frac{3m}{4} = 9$

6. $\frac{2p}{3} - p = 5$

7. $\frac{2k}{5} + k = 12$

8. $1.5y - 2.5 = 5.0$

9. $2p - 5 - \frac{3p}{5} = 10$

REFERENCE

A New MK Primary Mathematics 2000 Bk 7 Pg 457 (New Edition)

SUB TOPIC: Solving more equations involving fractions.

Examples:

Solve the following equations

$$1. \quad \frac{m+1}{3} + \frac{m}{4} = 2$$

$$\frac{m+1}{3} + \frac{m}{4} = 2$$

$$LCD = 12$$

$$12 \times \frac{m+1}{3} + \frac{m}{4} \times 12 = 2 \times 12$$

$$4(m+1) + m \times 3 = 2 \times 12$$

$$4m + 4 + 3m = 24$$

$$4m + 3m + 4 = 24$$

$$7m + 4 = 24$$

$$7m + 4 - 4 = 24 - 4$$

$$7m = 20$$

$$\frac{7m}{7} = \frac{20}{7}$$

$$m = 2\frac{6}{7}$$

$$2. \quad \frac{(3x+1)}{4} = \frac{(x+2)}{2}$$

$$\frac{(3x+1)}{4} = \frac{(x+2)}{2}$$

$$LCD = 4$$

$$4 \times \frac{(3x+1)}{4} = \frac{(x+2)}{2} \times 4$$

$$3x + 1 = 2(x + 2)$$

$$3x + 1 = 2x + 4$$

$$3x + 1 - 1 = 2x + 4 - 1$$

$$3x = 2x + 3$$

$$3x - 2x = 2x - 2x + 3$$

$$x = 3$$

$$3. \quad \frac{3x-1}{4} = \frac{7x+1}{6}$$

$$4. \quad \frac{w-5}{3} - w = \frac{2w+4}{5}$$

$$5. \quad \frac{3}{k+3} = \frac{2}{2k-5}$$

REFERENCE

A New MK Primary Mathematics 2000 Bk 7 Pg 461,462 (New Edition)

SUB TOPIC: Solving equations involving squares and square roots

Examples:

Solve the following equations

$$1. \quad m^2 - 4 = 21$$

$$m^2 - 4 = 21$$

$$m^2 - 4 + 4 = 21 + 4$$

$$m^2 = 25$$

$$\sqrt{m^2} = \sqrt{25}$$

$$m = 5$$

$$2. \quad \frac{1}{2} p^2 = 8$$

$$\frac{1}{2} p^2 = 8$$

$$2 \times \frac{p^2}{2} = 8 \times 2$$

$$p^2 = 16$$

$$\sqrt{p^2} = \sqrt{16}$$

$$p = 4$$

$$3. \quad \sqrt{2k} = 14$$

$$\sqrt{2k} = 14$$

$$\sqrt{2k}^2 = 14^2$$

$$2k = 196$$

$$\frac{2k}{2} = \frac{196}{2}$$

$$k = 98$$

$$4. \quad \frac{1}{4} x^2 = 16$$

$$\frac{1}{4} x^2 = 16$$

$$4 \times \frac{x^2}{4} = 16 \times 4$$

$$x^2 = 64$$

$$\sqrt[2]{x^2} = \sqrt[2]{64}$$

$$x = 8$$

Mathematics is the Key

5. $b^2 = 49$
6. $6m^2 = 54$
7. $2w^2 - 18 = 224$
8. $\frac{2p^2}{3} = 54$

A New MK Primary Mathematics 2000 Bk
7 Pg 461 & 460 (New Edition)

SUB TOPIC: Forming and solving equations

Example:

1. Baker bought 2kg of sugar at sh. 3p and 1kg of salt at sh. (p + 200). Find P if Baker paid sh 3700.

The cost of 2kg of sugar is

$$sh (2 \times 3p) = sh 6p$$

The cost of 1kg of salt is

$$sh (p + 200)$$

$$Sh 6p + sh. p + shs. 200 = shs. 3700$$

$$Sh 7p + sh. 200 = sh. 3700$$

$$Sh 7p + sh. 200 - shs. 200 = sh. 3700 - sh. 200$$

$$Sh. 7p = sh. 3500$$

$$\frac{Sh. 7p}{sh. 7} = \frac{sh. 3500}{sh. 7}$$

$$\underline{p = 500}$$

2. In a market, the cost of a pawpaw is sh. 800 more than the cost of a mango.

A mango costs two thirds the cost of a pine apple. The total cost of three fruits is sh 4300. Calculate the cost of a pineapple.

Let the cost of a pineapple be m

| pawpaw | pineapple | mango |
|--------------------------|-----------|----------------|
| $\frac{2}{3}m + sh. 800$ | m | $\frac{2}{3}m$ |

$$m + \frac{2}{3}m + \frac{2}{3}m + sh. 800 = sh. 4,300$$

$$\frac{1}{1} + \frac{2m}{3} + \frac{2m}{3} + \frac{1}{1} = \frac{1}{1}$$

$$\frac{m}{1} \times 3 + \frac{4m}{3} \times 3 + \frac{sh. 800}{1} \times 3 = \frac{sh. 4300}{1} \times 3$$

$$3m + 4m + sh. 2,400 = sh. 12,900$$

$$7m + sh. 2,400 = sh. 12,900$$

$$7m + sh. 2,400 - sh. 2,400 = sh. 12,900 - sh. 2,400$$

$$7m = sh. 10,500$$

Mathematics is the key

$$\frac{7m}{7} = \frac{sh. 10,500}{7}$$

$$\underline{\underline{m = sh. 1,500}} \quad \text{}$$

Let the cost of a mango be k

| pawpaw | pineapple | mango |
|---------------|----------------|-------|
| $k + sh. 800$ | $\frac{3}{2}k$ | k |

$$k + \frac{3}{2}k + k + sh. 800 = sh. 4,300$$

$$\frac{k}{1} + \frac{3k}{2} + \frac{k}{1} + \frac{sh. 800}{1} = \frac{sh. 4,300}{1}$$

$$\frac{k}{1} \times 2 + \frac{3k}{2} \times 2 + \frac{k}{1} \times 2 + \frac{sh. 800}{1} \times 2 = \frac{sh. 4300}{1} \times 2$$

$$2k + 3k + 2k + sh. 1,600 = sh. 8,600$$

$$7k + sh. 1,600 = sh. 8,600$$

$$7k + sh. 1,600 - sh. 1,600 = sh. 8,600 - sh. 1,600$$

$$7k = sh. 7,000$$

$$\frac{7k}{7} = \frac{sh. 7,000}{7}$$

$$\underline{\underline{k = sh. 1,000}}$$

pineapple

$$\frac{3}{2} \times sh. 1,000$$

$$3 \times sh. 500$$

$$\frac{1}{sh. 500}$$

Let the cost of a pawpaw be w

| pawpaw | pineapple | mango |
|--------|----------------------------|---------------|
| w | $\frac{3}{2}(w - sh. 800)$ | $w - sh. 800$ |

$$w + \frac{3}{2}(w - sh. 800) + w - sh. 800 = sh. 4,300$$

$$\frac{w}{1} + \frac{3(w - sh. 800)}{2} + \frac{w}{1} - \frac{sh. 800}{1} = \frac{sh. 4,300}{1}$$

$$\frac{w}{1} \times 2 + \frac{3(w - sh. 800)}{2} \times 2 + \frac{w}{1} \times 2 - \frac{sh. 800}{1} \times 2 = \frac{sh. 4300}{1} \times 2$$

$$2w + 3(w - sh. 800) + 2w - sh. 1,600 = sh. 8,600$$

$$2w + 3w - sh. 2,400 + 2w + sh. 1,600 = sh. 8,600$$

$$7w - sh. 1,600 - sh. 2,400 = sh. 8,600$$

$$7w - sh. 4,000 + sh. 4,000 = sh. 8,600 + sh. 4,000$$

$$7w = \text{sh. } 12,600$$

$$\frac{7w}{7} = \frac{\text{sh. } 12,600}{7}$$

$$w = \text{sh. } 1,800$$

pineapple

$$\frac{3}{2}(w - \text{sh. } 800)$$

$$\frac{3}{2}(\text{sh. } 1800 - \text{sh. } 800)$$

$$\frac{3}{2} \times \text{sh. } 1,000$$

$$3 \times \text{sh. } 5,00$$

$$\text{sh. } 1,500$$

3. A cup costs twice as much as a fork and a plate costs sh.600 more than a fork. If the total cost of all the three items is sh.3600, find the cost of each item.
4. James, Joan and Peter shared a certain amount of money. James got three times as much as Peter. Joan got sh.900 more than Peter. If Peter and James got sh.2,800, how much did Joan get?

REFERENCE

A New MK Primary Mathematics 2000 Bk 7 Pg 464 (New Edition)

SUBTOPIC: Application of algebra in ages

Examples.

1. Amon is twice as old as Bob. If their total age is 33 years. How old is each?

Let Bob's age be A

| Amon | Bob | TL |
|------|-----|---------|
| $2A$ | A | 33years |

$$2A + A = 33$$

$$3A = 33$$

$$\frac{3A}{3} = \frac{33}{3}$$

$$A = 11\text{years}$$

| Amon | Bob |
|------------------------------|---------|
| $2 \times 11 = 22\text{yrs}$ | 11years |

Mathematics is the Key

- 2. A father is 18 years older than his son. In 5 years ,their total age will be 48years. How old is each?**

Let the son's age be m

| | <i>father</i> | <i>son</i> | <i>TL</i> |
|-------------|---------------|------------|-----------|
| <i>now</i> | $m + 18$ | m | |
| <i>then</i> | $m + 18 + 5$ | $m + 5$ | 48years |

$$m + 18 + 5 + m + 5 = 48\text{years}$$

$$m + m + 18 + 10 = 48\text{years}$$

$$2m + 28 = 48\text{years}$$

$$2m + 28 - 28 = 48 - 28$$

$$2m = 20$$

$$\frac{2m}{2} = \frac{20}{2}$$

$$\underline{m = 10\text{years}}$$

| <i>father</i> | <i>son</i> |
|--------------------------|------------|
| $m + 18$ | |
| $10 + 18 = 28\text{yrs}$ | 10years |

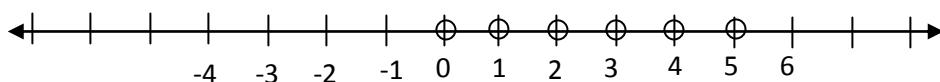
3. Jacob is 10 years younger than Jerome. Six years ago, Jerome was twice as old as Jacob. How old is Jacob?
4. A son is a half of his mother's age while the daughter is a third of his mothers age. If the total age of the son and the daughter is 30 years, how old is the mother?
5. The father is 25 years old and the son is 5 years old.
 - (a) In how many years time will the father be thrice as old as the son.?
 - (b) How old will the father be then?
6. January is a third as old as march. Four years ago the ratio of their age was 1:5.How old is each now?

SUB TOPIC: Writing solution sets

Examples:

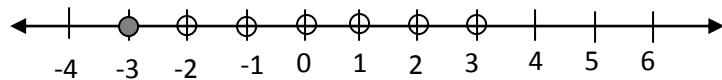
1. Write down the integers for the following inequalities.

(i) $x < 6$



$$\underline{x = \{5,4,3,2,1,0, -1, \dots\} \text{ (infinite set)}}$$

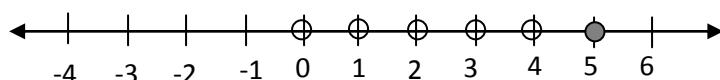
(ii) $m \geq -3$



$$\underline{m = \{-3, -2, -1, 0, 1, 2, \dots\} \text{ (infinite set)}}$$

Mathematics is the Key

(iii) $k \leq 5$ (where k is a whole number)



$$\underline{k = \{5, 4, 3, 2, 1, 0\}}$$

2. Write the solution sets for the following

$$h \geq 9$$

$$b < -4$$

$$y \leq -5$$

A New MK Primary Mathematics 2000 Bk 7 Exercise 6:1 Pg 71 (New Edition)

SUB TOPIC: Solving inequalities and writing their solution sets

*When dividing by a negative co-efficient,
the sign changes at the step of division.*

Examples:

Solve the following and write the solution set

1. $4X > 20$

$$4X > 20$$

$$\frac{4X}{4} > \frac{20}{4}$$

$$X > 5$$

$$\underline{X = \{6, 7, 8, 9, 10, \dots\}}$$

2. $-4m > 20$

$$-4m > 20$$

$$\frac{-4m}{-4} < \frac{20}{-4}$$

$$m < -5$$

$$\underline{m = \{-6, -7, -8, -9, \dots\}}$$

3. $3x + 6 < 9$

$$3x + 6 - 6 < 9 - 6$$

$$3x < 3$$

$$\frac{3x}{3} < \frac{3}{3}$$

$$X < 1$$

$$\underline{x = \{0, -1, -2, -3, \dots\}}$$

$$\begin{aligned}
 4. \quad & \frac{x}{7} - 5 > -4 \\
 & \frac{x}{7} - 5 > -4 \\
 & 7 \times \frac{x}{7} - 5 \times 7 > -4 \times 7 \\
 & x - 35 > -28 \\
 & x - 35 + 35 > -28 + 35 \\
 & x > 7 \\
 & \underline{x = \{8, 9, 10, 11, \dots\}}
 \end{aligned}$$

Solve the following and write the solution sets

- a) $5m < 20$
- b) $6p > -18$
- c) $2(x + 1) > 4$
- d) $3(2x + 3) < 18$
- e) $3y + 2 < 11$
- f) $4 - k \geq 9$
- g) $\frac{2w}{3} - 12 > 0$

REFERENCE

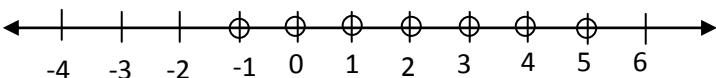
A New MK Primary Mathematics 2000 Bk 7 Exercise 6:3 and 6:4 Pg 74 (New Edition)

SUB TOPIC: Compound inequalities(writing solution sets)

Examples

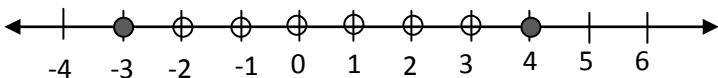
1. Write the solution set for

(a) $-2 < d < 6$



$d = \{-1, 0, 1, 2, 3, 4, 5\}$

(b) $4 \geq m \geq -3$



$m = \{-3, -2, -1, 0, 1, 2, 3, 4\}$

(c) $-6 < w < 2$

(d) $1 < p < 9$

(e) $7 > x - 4$

A New MK Primary Mathematics 2000 Bk 7 Pg 75 (New Edition)

SUB TOPIC: Solving and writing solution sets with compound inequalities.

Examples

Solve the following and write the solution sets

1. $8 > 2x > 2$

$$8 > 2x > 2$$

$$\frac{8}{2} > \frac{2x}{2} > \frac{2}{2}$$

$$4 > x > 1$$

$$\underline{x = \{2, 3\}}$$

2. $12 < -3x < 24$

$$12 < -3x < 24$$

$$\frac{12}{-3} > \frac{-3x}{-3} > \frac{24}{-3}$$

$$-4 > x > -8$$

$$\underline{x = \{-5, -6, -7\}}$$

3. $13 \geq 3x - 2 \geq 4$

$$13 \geq 3x - 2 \geq 4$$

$$13 + 2 \geq 3x - 2 + 2 \geq 4 + 2$$

$$15 \geq 3x \geq 6$$

$$\frac{15}{3} \geq \frac{3x}{3} \geq \frac{6}{3}$$

$$5 \geq x \geq 2$$

$$\underline{x = \{2, 3, 4, 5\}}$$

4. $12 > 3m > 3$

5. $15 \leq -5m \leq 40$

6. $-12 \geq 6b > 18$

TOPICAL WORK ON ALGEBRA

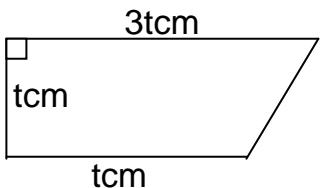
1. Solve: $x + 4x = 5$

2. Find the value of $\frac{5a - (m - a)}{a}$ when $a = 3$ and $m = 6$

3. Solve for b in $\frac{3}{5}(2b - 3) = 3$

4. If $\frac{1}{6}x = 1$. Find the value of x.

5. Solve $\frac{2x+2}{3} = \frac{x+3}{2}$
6. What is the value of $\frac{bc-d}{c^2}$ when $b = 8$, $c = 3$ and $d = 6$?
7. Solve: $x - 1 = 2x + 5$
8. Simplify: $(3x + 5) - (x + 1)$
9. Solve: $\frac{1}{2}(3y - 2) = \frac{2}{3}(2y + 3)$
10. Solve: $3(p - 4) - 2(3p - 1) = 2p - 15$
11. Simplify: $(4p - 3q) - (2q + p)$
12. Solve: $\frac{12}{x} + 2 = 6$
13. The area of the trapezium is 50cm^2 . Find the value of t.



14. Factorise completely: $2xy - 4x$.
 15. Given that $a = \frac{1}{2}$, $b = \frac{1}{3}$ and $c = \frac{1}{4}$. Find the value of $b + 2c + 3a$.
 16. Subtract $2x - 4$ from $5x - 4$
 17. Given that $x = 2y + 1$, complete the table.
- | | | | | | |
|---|-----|-------|-----|-----|-----|
| x | 1 | | 5 | ... | 9 |
| y | ... | 1 | ... | 3 | ... |
18. Zahara's mother bought 8 books at shs $(x - 150)$ each and 2 Mathematical sets at shs $(x + 100)$ each. She spent shs 5300 altogether. Find the amount of money spent on books.
 19. Tom has three daughters; Amanda, Brenda and Kate. Brenda is 2 years younger than Amanda, Kate's age is $\frac{1}{2}$ that of Brenda. The total age of the three girls is 27 years. How old is Kate?
 20. Find the solution set for the following inequalities:

| | | |
|--------------|---------------|---------------|
| (i) $x > 3$ | (ii) $x < -5$ | (iii) $x < 2$ |
| (iv) $x > 2$ | (v) $x < 4$ | |
 - (ii) Solve and give the solutions for x.

| | |
|---------------------|--------------------|
| (i) $-3x < -9$ | (ii) $-30 < 6x$ |
| (iii) $3x + 2 < 11$ | (iv) $4x - 5 < 19$ |
 - (iii) Solve and find the solution set for $y \cdot \frac{y}{3} + 4 < 6$
 - (iv) Solve the inequality below:

$$8 > 2x > -4$$