P425/1
PURE MATHEMATICS
Paper 1
July/August 2024
3 hours



### WAKISSHA JOINT MOCK EXAMINATIONS

# Uganda Advanced Certificate of Education PURE MATHEMATICS

Paper 1

3 hours

#### INSTRUCTIONS TO CANDIDATES:

- Answer all the eight questions in section A and any five questions from section B.
- Any additional question(s) answered will not be marked.
- Show all necessary working clearly.
- Begin each answer on a fresh page of paper.
- Silent, non programmable scientific calculators and mathematical tables with a list of formulae may be used.

## **SECTION A (40 MARKS)**

Answer all questions in this section.

- 1. Calculate the coordinates of the point of intersection of the curve  $\frac{x}{y} + \frac{6y}{x} = 5 \text{ and line } x 2y 2 = 0$  (05 marks)
- 2. By using suitable substitution evaluate  $\int_0^1 \frac{x}{\sqrt{(1+x)}} dx$  (05 marks)
- 3. Given that  $\sin x + \sin y = \beta_1$  and  $\cos x + \cos y = \beta_2$ Show that

(i) 
$$\tan \frac{x+y}{2} = \frac{\beta_1}{\beta_2}$$
 (02 marks)

(ii) 
$$\cos(x+y) = \frac{\beta_2^2 - \beta_2^2}{\beta_2^2 + \beta_1^2}$$
 (03 marks)

- 4. Use small changes to estimate cube root of 27.15 (05 marks)
- Variable point P(x, y) moves such that its distance from point A (3,0) is equal to its distance from the line x + 3 = 0.
   Describe the locus of point P (05 marks)
- 6. Prove that points A( $^{-2}$ ,0,6) and B(3, $^{-4}$ , 5) lie on opposite sides of the plane 2x y + 3Z = 21. (05 marks)
- The second and third terms of a geometrical progression are 24 and 12(b + 1) respectively. Find b if the sum of the first three terms of the progression is 76.
- 8. Determine the area of the largest rectangular piece of land that can be enclosed by 200 meters of wire when fencing it, if one side has existing wall. (05 marks)

## SECTION B (60 marks)

Answer any five questions from his section.

9. (a) In a triangle ABC, prove that

$$\frac{\cos(\beta + C)}{\csc \beta \csc C} = \frac{bc}{ab + ac}$$
 (06 marks)

- (b) Find the solution of  $3 \cot \theta + \text{Cosec}\theta = 2 \text{ for } 0^{\circ} \le \theta \le 360^{\circ}$  (06 marks)
- 10. · (a) Use Demoivre's theorem to simplify  $\frac{\left[\sqrt{3}\left(\cos\theta+i\sin\theta\right]^{8}\right]}{\left[3\cos2\theta+3i\sin2\theta\right]^{3}}$ (04 marks)
  - (b) If  $(1+3i)Z_1 = 5(1+i)$ , show that locus of  $|Z-Z_1| = |Z_1|$ , where z is a complex number, is a circle and find its center and radius (08marks)
- 11. (a) The first term of an A.P is equal to the first term of a G.P whose common ratio is \(\frac{1}{3}\) and sum to infinity is 9. If the common difference of the A.P is 2. Find the sum of the sum first ten terms of the A.P (06 marks)
  - (b) If the letters or a word DEFEATED are arranged, find number of ways for which the 3Es will be separated. (06 marks)
- 12. (a) Find the equation of a plane containing points A(1,1,1) B(1,0,1) and C(3,2,1) (05 marks)
  - (b) Find the perpendicular distance of point A (2, 1, 4) from the line  $\underline{r} = \begin{pmatrix} 1 \\ 0 \\ 2 \end{pmatrix} + \lambda \begin{pmatrix} 2 \\ 1 \\ 2 \end{pmatrix}$  (07 marks)
- 13. (a) The normal at the point P(5 cos  $\theta$ , 4 sin  $\theta$ ) on an ellipse  $\frac{x^2}{25} + \frac{y^2}{16} = 1$  meets the x and y- axes at A and B respectively. Find the mid-point of line AB. (06 marks)
  - (b) Show that the circles  $x^2 + y^2 2ax + c^2 = 0$  and  $x^2 + y^2 2by c^2 = 0$  are orthogonal. (06 marks)

Turn Over

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14. (a) Evaluate 
$$\int_{1}^{3} \frac{x^2+1}{x^3+4x^2+3x} dx$$
 (07 marks)

(b) Find 
$$\int \frac{1}{3x^2 + 5x + 4} dx$$
 (05 marks)

- 15. The population of a certain village was noted that every year, 5 people die due to a deadly genetic disease and rate of population increase is proportional to the people present at that time. Given that initially population of that village was 120 and after a year increased to 210.
  - (a) Find the number of people after five years. (10 marks)
  - (b) What time will it take for the number of people in that village to be 37,275? (02 marks)
- 16. Given that  $y = x \frac{-8}{x^2}$ (a) Determine the;
  - (i) Intercept (02 marks)
  - (ii) Turning point (03 marks)
  - (iii) Equation of the a asymptotes (02 marks)
  - (b) Sketch the curve. (05 marks)

**END**