



# THE PEARL EDUCATIONAL CONSULT KAMPALA SCHOOLS

## UPPER PRIMARY PUPIL'S BOOK

NEW EDITION 2023

### ***BASIC AND APPLIED MATHEMATICAL FORMULA WITH EXAMPLES***

1) Subsets =  $2^n$

For example;

Given that set A = {a, b, c}, find the number of subsets set A has.

Subsets =  $2^n$

$$\begin{aligned} n &= 3 \\ &= 2^3 \\ &= (2 \times 2) \times 2 \\ &= 4 \times 2 \\ &= \underline{\underline{8 \text{ subsets.}}} \end{aligned}$$

2) Proper Subsets =  $2^n - 1$

For example;

Given that set P = {a, b, c, d}, how many proper subsets does set P has?

Proper subsets =  $2^n - 1$

$$\begin{aligned} n &= 4 \\ &= 2^4 - 1 \\ &= (2 \times 2) \times (2 \times 2) - 1 \\ &= (4 \times 4) - 1 \\ &= 16 - 1 \\ &= \underline{\underline{15 \text{ proper subsets.}}} \end{aligned}$$

3) Triangular number =  $n \frac{(n+1)}{2}$

n means number.

For example;

What is the 6<sup>th</sup> triangular number?

Triangular number =  $n \frac{(n+1)}{2}$

$$\begin{aligned} &= \frac{6(6+1)}{2} \\ &= \frac{6 \times 7}{2} \\ &= \frac{42}{2} \\ &= \underline{\underline{21.}} \end{aligned}$$

4) Square number =  $n^2$

Where n stands for number.

For example; Find the square of 4.

$$= 4^2$$

$$= 4 \times 4 =$$

$$\underline{16.}$$

Cube  
number  
 $= n^3$

Where n stands for number

For example;

What is the cube of 5?

$$= 5^3$$

$$= 5 \times 5 \times 5$$

$$= \underline{125.}$$

6) Increase = New - Old.

For example;

The number of pupils in P.6 class increased from 100 to 150 this year.

Calculate the increased number.

$$\text{Increase} = \text{New} - \text{old}$$

$$= 150 - 100 =$$

$$\underline{50.}$$

$$\text{➤ \% Increase} = \frac{\text{increase}}{\text{Original no.}} \times 100\%$$

For example;

The number of pupils increased from 400 to 420 in a school this year.

Calculate the percentage increase.

$$\% \text{ increase} = \frac{\text{increase}}{\text{Original no.}} \times 100\%$$

$$= \frac{420 - 400}{400} \times 100\%$$

$$= \frac{20}{400} \times 100\%$$

$$= \frac{20}{400} \times 100\%$$

$$= \frac{20}{400} \times 100\%$$

$$= \frac{20}{400} \times 100\%$$

$$= 5 \times 1\%$$

$$= \underline{5\%}$$

7) Decrease = Old - New

For example;

When 480 was decreased, it became 420. Calculate the decrease.

$$\text{Decrease} = \text{Old} - \text{New}$$

$$= 480 - 420$$

$$= \underline{60.}$$

$$\text{➤ \% decrease} = \frac{\text{decrease}}{\text{Original no.}} \times 100\%$$

For example;

By what percentage will 100 be decreased to become 80?

$$\% \text{ decrease} = \frac{\text{decrease}}{\text{Original no.}} \times 100\%$$

$$= \frac{100 - 80}{100} \times 100\%$$

$$= \frac{20}{100} \times 100\%$$

$$= \frac{20}{100} \times 100\%$$

$$= \frac{20}{100} \times 100\%$$

$$= \frac{20}{100} \times 100\%$$

$$= \frac{20}{100} \times 100\%$$

$$= \underline{20\%}$$

8) Profit = Selling Price (S.P) - Buying Price (B.P)

For example;

Kevin bought a television set at sh. 800,000 and sold it later at sh. 900,000. Calculate his profit.

$$\text{Profit} = \text{S.P} - \text{B.P}$$

$$= \text{sh. } 900,000 - \text{sh. } 800,000$$

$$= \underline{\text{sh. } 100,000.}$$

$$\text{➤ \% Profit} = \frac{\text{Profit}}{\text{Cost price (C.P)}} \times 100\%$$

For example;

Find the percentage profit on a chair bought at sh. 10,000 and sold at sh. 12,000.

$$\% \text{ Profit} = \frac{\text{Profit}}{\text{C.P}} \times 100\%$$

$$= \frac{12,000 - 10,000}{10,000} \times 100\%$$

$$= \frac{2,000}{10,000} \times 100\%$$

$$= 2 \times 10\%$$

$$= \underline{20\%}$$

9) Loss = Buying Price (B.P) - Selling Price (S.P)

For example;

Isaac bought a radio at sh. 60,000 and sold it at sh. 40,000. Calculate his loss.

$$\text{Loss} = \text{B.P} - \text{S.P}$$

$$= \text{sh. } 60,000 - \text{sh. } 40,000$$

$$= \underline{\text{sh. } 20,000}$$

$$\text{➤ \% Loss} = \frac{\text{Loss}}{\text{C.P}} \times 100\%$$

For example;

Sophia bought a car at sh. 8,000,000 and sold it at sh. 6,000,000. Calculate her percentage loss.

$$\% \text{ Loss} = \frac{\text{Loss}}{\text{C.P}} \times 100\%$$

$$= \frac{\text{sh. } 8,000,000 - \text{sh. } 6,000,000}{\text{Sh. } 8,000,000} \times 100\%$$

$$= \frac{\text{sh. } 2,000,000}{\text{Sh. } 8,000,000} \times 100\%^{25}$$

$$= 1 \times 25\%$$

$$= \underline{25\%}$$

10) Discount = Marked Price (M.P) - Cash Price (C.P)

For example;

The marked price of a radio is sh. 40,000. After a discount Bashir paid sh. 35,000 cash. How much was the discount?

$$\text{Discount} = \text{M.P} - \text{C.P}$$

$$= \text{sh. } 40,000 - \text{sh. } 35,000$$

$$= \underline{\text{sh. } 5,000}$$

$$\text{➤ \% discount} = \frac{\text{Discount}}{\text{M.P}} \times 100\%$$

For example;

The marked price of a set is sh. 1,500. Milly paid sh. 1,200 after being given a discount. What was the percentage discount?

$$\% \text{ discount} = \frac{\text{Discount}}{\text{M.P}} \times 100\%$$

$$= \frac{1,500 - 1,200}{1,500} \times 100\%$$

$$= \frac{300}{1500} \times 100\%$$

$$= \underline{20\% \text{ discount}}$$

$$11) \text{ Simple Interest (S.I)} = \text{Principal (P)} \times \text{Rate (R)} \times \text{Time (T)}$$

For example;

Calculate the simple interest on sh. 40,000 kept for 3 years at a rate of 30% per year.

$$\text{Simple interest} = P \times R \times T$$

$$= \text{sh. } 40,000 \times \frac{30}{100} \times 3$$

$$= \text{sh. } 400 \times 30 \times 3$$

$$= \text{sh. } 12,000 \times 3$$

$$= \underline{\text{sh. } 36,000}$$

$$12) \text{ Amount} = \text{Principal (P)} + \text{Interest (I)}$$

For example;

Calculate the amount on sh. 40,000 borrowed for 2 years at 10% per year.

$$\text{Interest} = P \times R \times T$$

$$= \text{sh. } 40,000 \times \frac{10}{100} \times 2$$

$$= \text{sh. } 400 \times 10 \times 2$$

$$= \underline{\text{sh. } 8,000}$$

$$\text{Amount} = \text{Principal} + \text{Interest}$$

$$= \text{Sh. } 40,000 + \text{sh. } 8,000$$

$$= \underline{\text{sh. } 48,000}$$

$$13) \text{ Rate} = \frac{\text{S.I} \times 100}{P \times T}$$

For example;

Sarah deposited sh. 60,000 on her savings account. At the end of 2 years the simple interest earned was sh. 12,000. Calculate the rate of interest.

$$\text{Rate} = \frac{\text{S.I} \times 100}{P \times T}$$

$$\begin{aligned}
 &= \text{sh. } \frac{6 \times 12,000 \times 5 \times 100}{\cancel{\text{Sh. } 60,000} \times \cancel{2}} \\
 &= 6 \times 5 \\
 &= \underline{30\%}
 \end{aligned}$$

$$14) \text{ Principal} = \frac{S.I \times 100}{R \times T}$$

For example;

What sum of money will yield an interest of Sh. 5,000 at a rate of 2% for 4 years?

$$\begin{aligned}
 \text{Principal} &= \frac{S.I \times 100}{R \times T} \\
 &= \text{sh. } \frac{5,000 \times 100}{\cancel{2} \times \cancel{4}} \times \frac{100}{25} \\
 &= \text{sh. } 2500 \times 25 \\
 &= \underline{\text{sh. } 65,500}
 \end{aligned}$$

$$15) \text{ Time} = \frac{S.I \times 100}{P \times R}$$

For example;

In what time will sh. 15,000 yield an interest of sh. 1,200 at 4% per year?

$$\begin{aligned}
 \text{Time} &= \frac{S.I \times 100}{P \times R} \\
 &= \frac{1,200 \times 100}{15,000 \times \cancel{4}} \\
 &= \frac{30^2}{15} \\
 &= \underline{2 \text{ years}}
 \end{aligned}$$

$$16) \text{ Range} = \text{Highest (H)} - \text{Lowest (L)}$$

For example;

Given the following marks scored by Mark in Mathematics papers; 70, 65, 40, 60, 20. Find his range.

$$\begin{aligned}
 \text{Range} &= H - L \\
 &= 70 - 20 \\
 &= \underline{50.}
 \end{aligned}$$

$$17) \text{ Mean} = \frac{\text{Total items}}{\text{No. of items}}$$

For example;

Joyce scored the following marks in her test; 50, 40, 70, 60. Calculate her mean.

$$\begin{aligned}
 \text{Mean} &= \frac{\text{Total marks}}{\text{No. of tests}} \\
 &= \frac{50 + 40 + 70 + 60}{4}
 \end{aligned}$$

$$= \frac{220}{4}$$

$$= \underline{55}.$$

18) Probability =  $\frac{\text{All expected outcomes (E)}}{\text{All possible outcomes (T)}}$

For example;

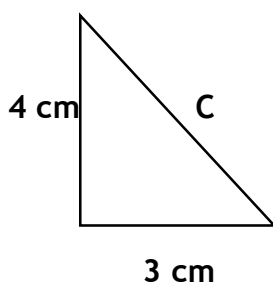
In a box, there are 7 red pens, 4 blue pens and 3 black ones. What would be the probability of choosing a blue pen? Probability =  $\frac{n(E)}{n(T)}$

$$= \frac{4}{7 + 4 + 3}$$

$$= \frac{4}{14}$$

19) Pythagoras Theorem:  $a^2 + b^2 = c^2$

For example;



$$a^2 + b^2 = c^2$$

$$9 + 16 = c^2$$

$$\sqrt{25} = \sqrt{c^2}$$

$$3^2 + 4^2 = c^2$$

$$c = \underline{5}$$

20) Number of sides of a polygon =  $\frac{\text{All exterior angles}}{\text{Each exterior angle}}$  which is;  
 $= \frac{360^\circ}{\text{Ext angle}}$

For example;

Calculate the number of sides of a regular polygon whose exterior angle is  $30^\circ$ .

$$\text{Number of sides} = \frac{360^\circ}{\text{Ext angle}}$$

$$= \frac{360^\circ}{30^\circ}$$

$$= \underline{12}$$

sides. 21) Number of

Triangles in a given polygon =  $(n - 2)$  n stands for number of sides a given polygon has.

For example;

How many triangles can be formed from a Hexagon?

$$\text{Number of triangles} = n - 2$$

$$= 6 - 2$$

$$= \underline{4 \text{ triangles.}}$$

22) Number of right angles of a polygon =  $2(n - 2)$  or  $2n - 4$ .

For example;

Calculate the number of right angles in a polygon with 7 sides.

$$\text{Number of right angles} = 2n - 4$$

$$= (2 \times 7) - 4$$

$$= 14 - 4$$

$$= \underline{10 \text{ right angles.}}$$

23) Interior angle sum of a polygon = Int. angle  $\times$  no. of triangle.  
 $= 180^\circ \times (n - 2) / 180^\circ (n - 2)$  or  
 $= 90^\circ (2n - 4).$

For example;

Calculate the interior angle sum of a polygon of 8 sides.

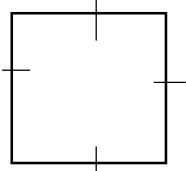
Angle sum =  $180^\circ (n-2)$   
 $= 180^\circ (8-2)$   
 $= 180^\circ \times 6$   
 $= \underline{1080^\circ}$

## 24) AREA OF;

i. Square =  $S \times S$  or  $(S^2)$  or  $L \times L$  or  $(L^2)$

For example;

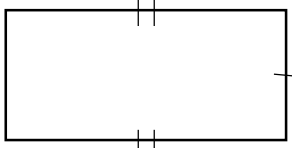
Find the area of the square whose side is 4 cm.

4  Area =  $S \times S$   
 $\text{cm} = 4 \text{ cm} \times 4 \text{ cm}$   
 $= \underline{16 \text{ cm}^2}$

ii. Rectangle =  $L \times W$  or  $(lw)$

For example;

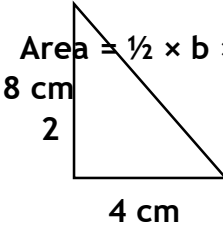
Find the area of the rectangle with length of 10 cm and 8 cm width.

 Area =  $L \times W$   
 $\text{cm} = 10 \text{ cm} \times 8 \text{ cm}$   
 $= \underline{80 \text{ cm}^2}$

iii. Triangle =  $\frac{1}{2} \times \text{base} \times \text{height}$  or  $\frac{(bh)}{2}$

For example;

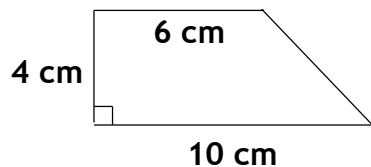
Find the area of triangle below.

 Area =  $\frac{1}{2} \times b \times h$   
 $= \underline{b \times h}$   
 $= \underline{\frac{4 \text{ cm} \times 8 \text{ cm}}{2}}$   
 $= 4 \times 4 \text{ cm}^2$   
 $= \underline{16 \text{ cm}^2}$

iv. Trapezium =  $\frac{1}{2} \times h \times (a+b)$

For example;

Find the area of the trapezium below.

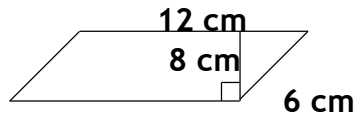


$$\begin{aligned}\text{Area} &= \frac{1}{2}h (a + b) \\ &= \frac{1}{2} \times 4 \text{ cm} \times (6 \text{ cm} + 10 \text{ cm}) \\ &= \frac{1}{2} \times 4 \text{ cm} \times 16 \text{ cm} \\ &= 4 \text{ cm} \times 4 \text{ cm} \\ &= \underline{16 \text{ cm}^2}\end{aligned}$$

- v. Parallelogram = Base (B)  $\times$  Height (H) (= b  $\times$  h)

For example;

Calculate the area of the parallelogram below.

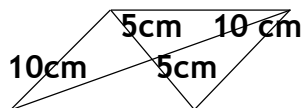


$$\begin{aligned}\text{Area} &= b \times h \\ &= 12 \text{ cm} \times 8 \text{ cm} \\ &= \underline{96 \text{ cm}^2}\end{aligned}$$

- vi. Rhombus and Kite =  $\frac{1}{2} \times d_1 \times d_2$

For example;

Find the area of the rhombus below.

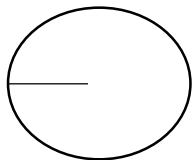


$$\begin{aligned}\text{Area} &= \frac{1}{2} \times d_1 \times d_2 \\ &= \frac{1}{2} \times 10 \text{ cm} \times 10 \text{ cm} \\ &= 10 \text{ cm} \times 10 \text{ cm} \\ &= \underline{100 \text{ cm}^2}\end{aligned}$$

- vii. Circle =  $\pi r^2$

For example;

Find the area of a circle whose radius is 14 cm.



$$\begin{aligned}\text{Area} &= \pi r^2 \\ &= \frac{22}{7} \times 14 \text{ cm} \times 14 \text{ cm} \\ &= 22 \times 7 \text{ cm} \times 14 \text{ cm} \\ &= \underline{616 \text{ cm}^2}\end{aligned}$$

- viii. Semi-Circle =  $\frac{1}{2} \pi r^2$

For example;

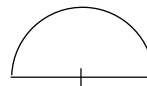
Calculate the area of a semi-circle of radius 7 cm.

$$\begin{aligned}\text{Area} &= \frac{1}{2} \pi r^2 \\ &= \frac{1}{2} \times \frac{22}{7} \times 7 \text{ cm} \times 7 \text{ cm}\end{aligned}$$

- ix.

7 cm

$$\begin{aligned}&= \frac{1}{4} \times \frac{22}{7} \times 7 \text{ cm} \times 7 \text{ cm} \\ &= \underline{77 \text{ cm}^2}\end{aligned}$$



Quadrant =  $\frac{1}{4} \pi r^2$

For example;

Find the area of a quadrant of a circle with radius 14 cm.

$$\text{Area} = \frac{1}{4} \pi r^2$$



14 cm

$$\begin{aligned}&= \frac{1}{4} \times \frac{22}{7} \times 14 \text{ cm} \times 14 \text{ cm} \\ &= 11 \times 2 \text{ cm} \times 7 \text{ cm} \\ &= \underline{154 \text{ cm}^2}\end{aligned}$$

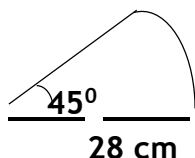
- x. Sector = given angle  $\times \pi r^2$



360°

**For example;**

Calculate the area of a sector of a circle of radius 28 cm and the center angle 45°



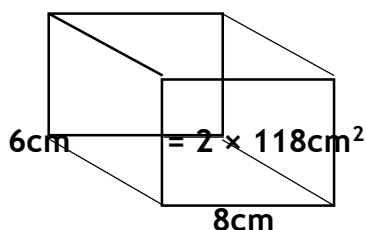
$$\begin{aligned}
 \text{Area} &= \frac{45^\circ}{360^\circ} \pi r^2 \\
 &= \frac{1}{8} \pi r^2 \\
 &= \frac{1}{8} \times \frac{22}{7} \times 28^2 \text{ cm} \times 28 \text{ cm} \\
 &= 11 \times 28 \text{ cm}^2 \\
 &= \underline{\underline{308 \text{ cm}^2}}
 \end{aligned}$$

## 25) TOTAL SURFACE AREA (T.S.A) OF;

a. Cuboid =  $(2lw) + (2lh) + (2wh)$  or  
 $2(LW + LH + WH)$

**For example;**

Find the total surface area of a cuboid whose sides measure 8cm by 5cm by 6cm.



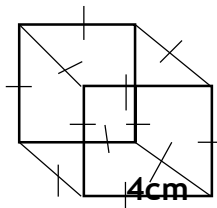
$$\begin{aligned}
 \text{T.S.A} &= 2((L \times W) + (L \times H) + (W \times H)) \\
 &= 2((8\text{cm} \times 5\text{cm}) + (8\text{cm} \times 6\text{cm}) + (5\text{cm} \times 6\text{cm})) \\
 &= 2((40\text{cm}^2) + (48\text{cm}^2) + (30\text{cm}^2)) \\
 &= \underline{\underline{236\text{cm}^2}}
 \end{aligned}$$

b. Cube =  $6(S \times S)$  or  $6 \times L^2$

**For example;**

Calculate the total surface area of a cube whose sides' measures 4cm.

$$\text{T.S.A} = 6 \times L^2$$

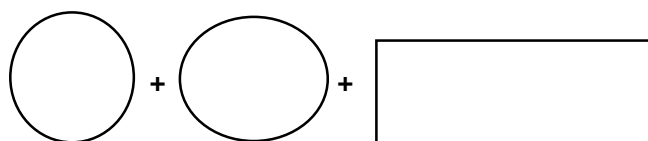


$$\begin{aligned}
 &= 6 \times 4\text{cm} \times 4\text{cm} \\
 &= 6 \times 16\text{cm}^2 \\
 &= \underline{\underline{96\text{cm}^2}}
 \end{aligned}$$

c. Cylinder =  $2\pi r^2 + 2\pi rh$  (when closed)

**For example;**

Calculate the total surface area of a cylinder whose radius is 7cm and height 10cm (Use  $\pi = \frac{22}{7}$ )



$$\begin{aligned}
 \text{T.S.A} &= 2\pi r^2 + 2\pi rh \\
 &= (2 \times \frac{22}{7} \times 7 \times 7) + (2 \times \frac{22}{7} \times 7 \times 10)
 \end{aligned}$$

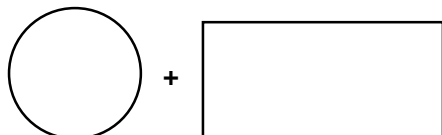
$$\begin{aligned}
 &= (44 \times 7) + (44 \times 10) \\
 &= 44(7+10) \\
 &= 44 \times 17 \\
 &= \underline{748\text{cm}^2}
 \end{aligned}$$

d. Cylinder =  $\pi r^2 + 2\pi rh$  (when one side is open)

For example;

Calculate the total surface area of an open cylinder whose radius is 7cm and height 8cm (Use  $\pi = 22/7$ )

Note: An open cylinder has one circular end.

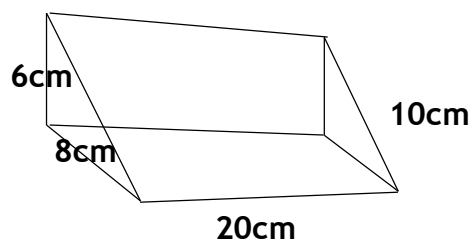


$$\begin{aligned}
 \text{T.S.A} &= \pi r^2 + 2\pi rh \\
 &= \left(\frac{22}{7} \times 7 \times 7\right) + \left(2 \times \frac{22}{7} \times 7 \times 8\right) \\
 &= (22 \times 7) + (44 \times 8) \\
 &= 154 + 352 \\
 &= \underline{506\text{cm}^2}
 \end{aligned}$$

e. Triangular prism =  $(b \times h) + (L \times W) + (L \times W) + (L \times W)$

For example;

Find the surface area of the triangular prism below.



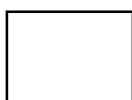
$$\begin{aligned}
 \text{T.S.A} &= (b \times h) + (L \times W) + (L \times W) + (L \times W) \\
 &= (8 \times 6) \text{ cm}^2 + (20 \times 8) \text{ cm}^2 + (20 \times 6) \text{ cm}^2 + (20 \times 10) \text{ cm}^2 \\
 &= 48 \text{ cm}^2 + 160 \text{ cm}^2 + 120 \text{ cm}^2 + 200 \text{ cm}^2 \\
 &= \underline{528 \text{ cm}^2}
 \end{aligned}$$

## 26) PERIMETER OF:

i. Square =  $S+S+S+S$  or  $4S$

For example;

Find the perimeter of the square whose sides are 4cm



$$\text{Perimeter} = 4 \times S$$

$$= 4 \times 4\text{cm}$$

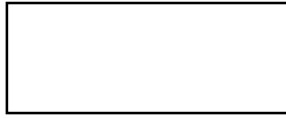
$$= \underline{16\text{cm}}$$

4cm

- ii. Rectangle =  $L+W+L+W$  or  $2(L+W)$  or  $2L+2W$

For example;

Find the perimeter of the rectangle below.



6 cm

$$\text{Perimeter} = 2(L + W)$$

$$= 2(10 + 6) \text{ cm}$$

$$= 2 \times 16 \text{ cm}$$

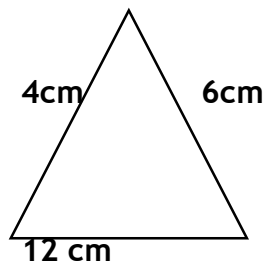
$$= \underline{32 \text{ cm}}$$

10 cm

- iii. Triangle =  $S_1+S_2+S_3$

For example;

Find the perimeter of triangle below.



$$\text{Perimeter} = S + S + s$$

$$= (12 \text{ cm} + 6 \text{ cm}) + 4 \text{ cm}$$

$$= 18 \text{ cm} + 6 \text{ cm}$$

$$= \underline{24 \text{ cm.}}$$

27)

## CIRCLES

- i. Diameter =  $2 \times \text{radius}$  ( $2r$ )

For example;

Find the diameter of a circle whose radius is 20cm.

$$\text{Diameter} = 2 \times \text{radius}$$

$$= 2 \times 20\text{cm} =$$

$$\underline{40\text{cm.}}$$

- ii. Radius =  $\frac{\text{Diameter}}{2}$  (D)

2

For example;

Find the radius of a circle whose diameter is 20cm

$$\text{Radius} = \frac{\text{Diameter}}{2}$$

2

$$= \frac{20\text{cm}}{2}$$

2

$$= \underline{10\text{cm.}}$$

28)

## CIRCUMFERENCE OF;

- i. Circle =  $\pi d$  (When diameter is given)

$$= 2\pi r \text{ (When radius is given)}$$

**For example;**

Calculate the circumference of a circle whose diameter is 21cm

(Use  $\pi = 22/7$ )

Circumference =  $\pi d$

$$= \frac{22}{7} \times 21 \text{ cm}$$

$$= 22 \times 3 \text{ cm}$$

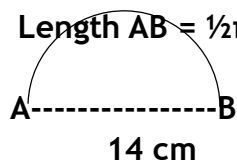
$$= \underline{66 \text{ cm.}}$$

ii. Length of Semi-circle (arc) =  $\frac{1}{2}\pi d$

**For example;**

Find the length of the semicircular arc AB

Length AB =  $\frac{1}{2}\pi d$



$$= \frac{1}{2} \times \frac{22}{7} \times 14$$

$$= 11 \times 2$$

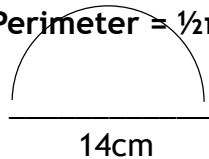
$$= 22 \text{ cm}$$

iii. Perimeter of Semi-circle =  $\frac{1}{2}\pi d + d$

**For example;**

Find the perimeter of the semicircular region AB.

Perimeter =  $\frac{1}{2}\pi d + d$



$$= \left( \frac{1}{2} \times \frac{22}{7} \times 14 \right) + 14$$

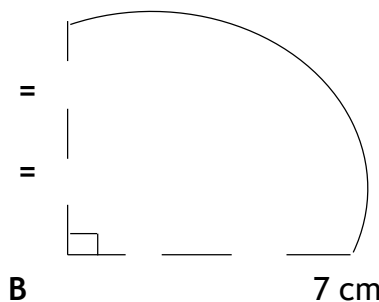
$$= (22 + 14) \text{ cm}$$

$$= \underline{36 \text{ cm}}$$

iv. Length of Quadrant =  $\frac{1}{4} 2\pi r$

**For example;**

Find the length of AC of the quadrant drawn below.



A The curved length =  $\frac{1}{4} (2\pi r)$

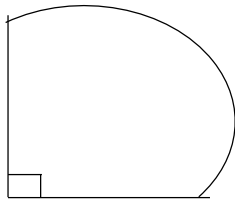
$$\frac{1}{4} \times 2 \times \frac{22}{7} \times 7$$

$$= \underline{11 \text{ cm.}}$$

4

**For example;**

Find the perimeter of the figure.



$$\begin{aligned}
 \text{A} \quad \text{Perimeter} &= \frac{1}{4}(2\pi r) + r + r \\
 &= \frac{1}{4} \times 2 \times \frac{22}{7} \times 7 + 7 + 7 \\
 &= 11 + 7 + 7 \\
 &= \underline{25 \text{ cm}}
 \end{aligned}$$

B

7 cm

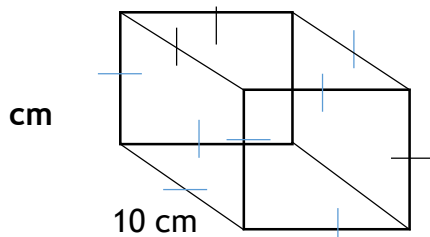
C

**29) VOLUME OF;**a. Cube = (Base area  $\times$  height)

$$= S \times S \times S$$

**For example;**

Find the volume of the cube below.



$$\text{Volume} = s \times s \times s$$

$$= (10 \text{ cm} \times 10 \text{ cm}) \times 10$$

$$= 100 \text{ cm}^2 \times 10 \text{ cm}$$

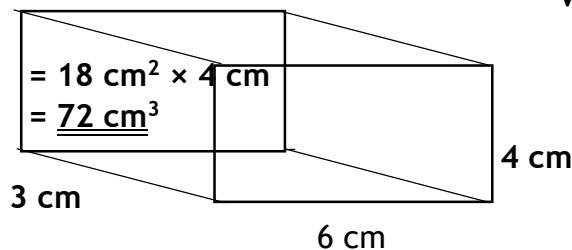
$$= \underline{1000 \text{ cm}^3}$$

b. Cuboid = Base area  $\times$  height

$$= L \times W \times H$$

**For example;**

Find the volume of the cuboid below



$$\text{Volume} = L \times W \times H$$

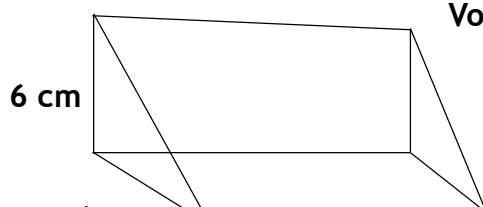
$$= (6 \text{ cm} \times 3 \text{ cm}) \times 4 \text{ cm}$$

c. Triangular Prism = (Area of triangle  $\times$  length)

$$= \frac{1}{2} b \times h \times l$$

**For example;**

Find the volume of the figure below.



$$\text{Volume} = \left(\frac{1}{2} \times b \times h\right) \times l$$

$$= \left(\frac{1}{2} \times 4^2 \text{ cm} \times 6 \text{ cm}\right) \times 10 \text{ cm}$$

$$= (2 \text{ cm} \times 6 \text{ cm}) \times 10 \text{ cm}$$

$$= 12 \text{ cm}^2 \times 10 \text{ cm}$$

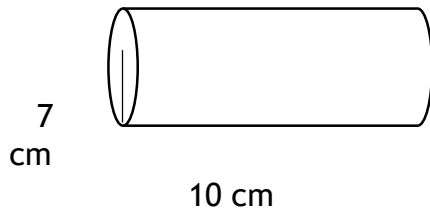
$$= \underline{120 \text{ cm}^3}$$

10 cm

$$\begin{aligned} \text{d. Cylinder} &= (\text{Area of circle} \times \text{height}) \\ &= (\pi r^2) h \end{aligned}$$

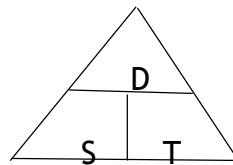
**For example;**

Find the volume of the cylinder below.



$$\begin{aligned} \text{Volume} &= (\pi r^2) \times h \\ &= \frac{22}{7} \times 7 \text{ cm} \times 7 \text{ cm} \times 10 \text{ cm} \\ &= (22 \text{ cm} \times 7 \text{ cm}) \times 10 \text{ cm} \\ &= 154 \text{ cm}^2 \times 10 \text{ cm} \\ &= \underline{\underline{1540 \text{ cm}^3}} \end{aligned}$$

$$\text{i) Distance (D) = Speed (S) \times \text{Time (T)}$$

**For example;**

James took 4 hours to cover a distance at a speed of 30 km hr. What distance did it cover?

$$\begin{aligned} \text{Distance} &= \text{speed} \times \text{time} \\ &= \underline{30\text{km}} \times \frac{4\text{hrs}}{1\text{hr}} \\ &= \underline{\underline{120\text{km}}} \end{aligned}$$

$$\text{ii) Speed (S) = } \frac{\text{Distance (D)}}{\text{Time (T)}}$$

**For example;**

Tom took 2 hours to cover a distance of 36 km on his bicycle. At what speed was she riding.

$$\begin{aligned} \text{Speed} &= \frac{\text{Distance}}{\text{Time}} \\ &= \frac{36\text{km}}{2\text{hrs}} \\ &= \underline{\underline{18\text{km/hr.}}} \end{aligned}$$

$$\text{Time (T) = Dist} \quad \text{iii} \quad \text{e (D)}$$

Speed (S)

For example;

How long will a car take to cover a distance of 120km at a speed of 40kmhr?

Time = Distance

Speed

$$= \frac{120\text{km}}{40\text{km}} \times 1\text{hr}$$

$$= \underline{3\text{hrs.}}$$

iv) Duration (D) = Ending Time (E.T) - Starting Time (S.T)

For example;

A plane left Entebbe at 1:00pm and arrived in Cairo at 5:30pm. How long did the flight take?

S/W

$$\begin{aligned} \text{Duration} &= \text{E.T} - \text{S.T} \\ &= 5:30\text{pm} - 1:00\text{pm} \\ &= \underline{4\text{hrs } 30\text{min or } 4\frac{1}{2}\text{hrs}} \end{aligned}$$

$$\begin{array}{r} \text{hrs. Min.} \\ 5 \quad 30 \\ - 1 \quad 00 \\ \hline 4 \text{ hrs. } 30\text{min} \end{array}$$

v) Ending Time (E.T) = Starting Time (S.T) + Duration (D)

For example;

A party started at 1:00pm and it lasted for 4hrs 30mins. At what time did it end?

Ending time = S.T + D

$$\begin{aligned} &= 1:00\text{pm} + 4\text{hrs } 30\text{mins} \\ &= \underline{5:30\text{pm}} \end{aligned}$$

P.O.W

1 00

$$\begin{array}{r} 4 \quad 30 \\ + 1 \quad 00 \\ \hline 5 \quad 30\text{pm} \end{array}$$

HJ

vi) Starting Time (S.T) = Ending Time (E.T) - Duration (D)

For example;

A party ended at 5:30pm and it lasted for 4hrs 30mins. At what time did it start?

$$\begin{aligned} \text{Starting time} &= \text{E.T} - \text{D} \\ &= 5:30\text{pm} - 4\text{hrs } 30\text{mins} \\ &= \underline{1:00\text{pm}} \end{aligned}$$

P.O.W

$$\begin{array}{r} 5 \quad 30 \\ - 4 \quad 30 \\ \hline 1 \quad 00\text{pm} \end{array}$$

## CONVERSION OF METRIC UNITS

King Henry's Daughter Mary Drank Cold Milk.

Kilometer (Km)	Hectometer (hm)	Decameter (Dm)	Meter (M)	Decimeter (dm)	Centimeter (cm)	Millimeter (mm)	Length (distance)
-------------------	--------------------	-------------------	--------------	-------------------	--------------------	--------------------	----------------------

Kilogram (Kg)	Hectogram (Hg)	Decagram (Dg)	Gram (G)	Decigram (dg)	Centigram (Cg)	Milligram (mg)	Mass (weighi
Kiloliter (Kl)	Hectoliter (Hl)	Decaliter (Dl)	Liter (L)	Deciliter (dl)	Centiliter (Cl)	Milliliter (ml)	Capacit

Where by >>> 1 km = 1000 m

1 kg = 1000 g

1 kl = 1000 l

1 l = 1000 ml

For example: Kl Hl Dl L dl cl ml

Change 5km to meter. 1 0 0

→

Km Hm Dm M dm cm mm 1liter

1 0 0 0 2l = (2 × 1000) ml

= 2000 ml

1km = 1000m

5km = (5 × 1000) m

= 5000m

Change 2liters to milliliter.

→

0

=1000ml

Express 24kg as grams

→

Kg Hg Dg G dg cg mg

1 0 0 0

1kg=1000g

34kg = (34×1000) g

= 34000grams

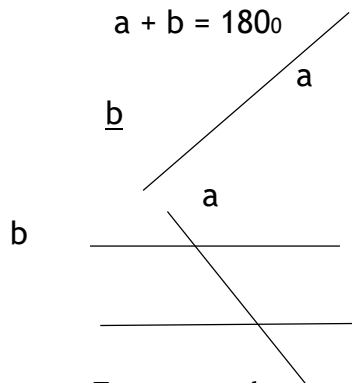
## ANGLES ON PARALLEL LINES.

### Co-interior Angles and Co-exterior Angles.

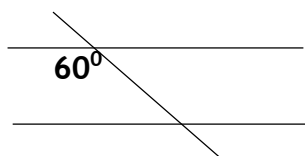
**Note:** The sum of Co-interior angles and Co-exterior angles is equal to 180°



Co-interior angles  
exterior angles  
 $a + b = 180^\circ$



For example;  
Find the value of angle



marked p

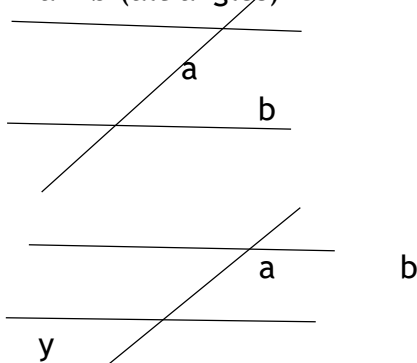
y

$$\begin{aligned}
 y + 60^\circ &= 180^\circ \text{ P.O.W} \\
 y + 60^\circ - 60^\circ &= 180^\circ - 60^\circ \\
 180^\circ y + 0 &= 120^\circ \div \\
 0 & \quad 0 - 130^\circ y \\
 \underline{120^\circ} & \quad 0 \quad \underline{50^\circ} \\
 & \quad \quad \quad p \\
 & \quad \quad \quad = 50^\circ
 \end{aligned}$$

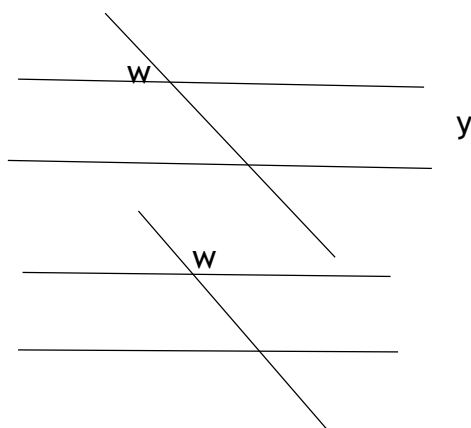
Alternate Interior  
and Alternate Exterior

**Note:** All alternate angles are equal.

Alternate Interior angles  
 $a = b$  (alt angles)

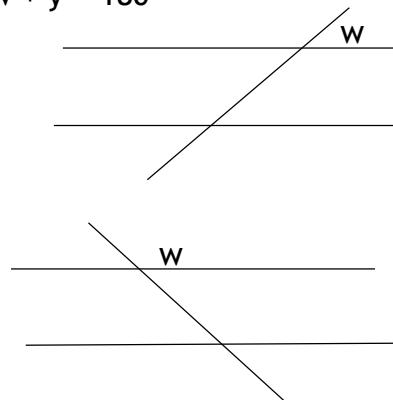


Alternate Exterior angles  
 $w = y$  (alt angles)

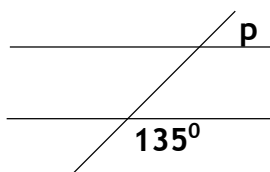


For example;

$$w + y = 180^\circ$$



For example;



$$\begin{aligned}
 p + 130^\circ &= 180^\circ \\
 p + 130^\circ - 135^\circ &= 180^\circ - 130^\circ \\
 p + 0 &= 50^\circ
 \end{aligned}$$

Co-

y

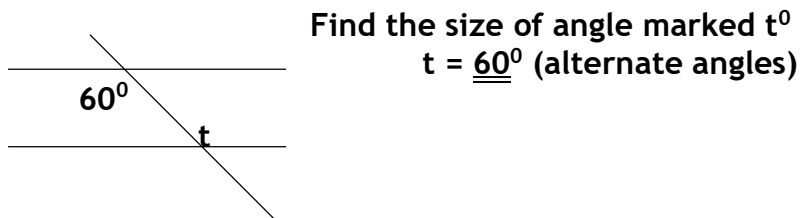
y

marked y  
Find the  
size of  
the angle

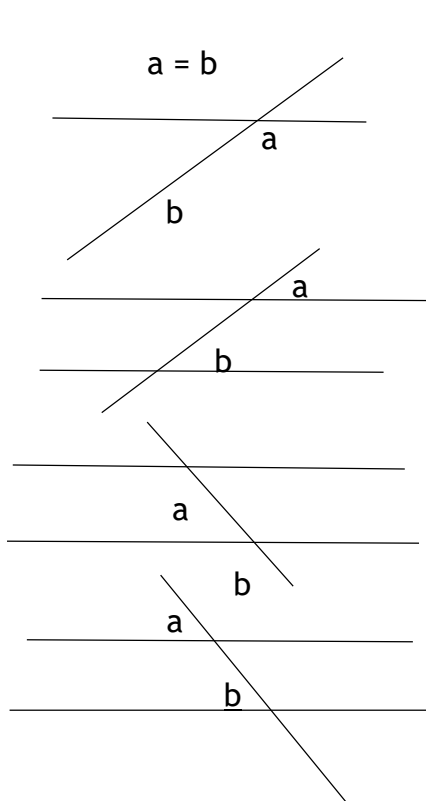
P.O.W  
 $180^\circ$

$$\begin{aligned}
 60^\circ \\
 = 120^\circ
 \end{aligned}$$

Angles  
Angles



## CORRESPONDING ANGLES.

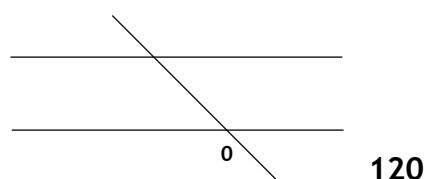


**Note:** All  
Corresponding  
angles are equal.

For  
Find the

f

example:  
size of angle marked f.



$f = 120^\circ$  (corresponding angles)

## INTEGERS

Positive (+)  $\times$  Negative (-) = Negative (-)

Negative (-)  $\times$  Positive (+) = Negative (-)

Positive (+)  $\times$  Positive (+) = Positive (+)

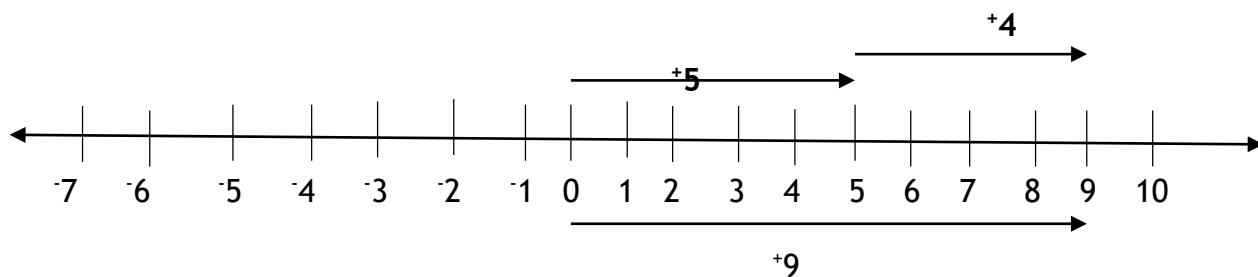
Negative (-)  $\times$  Negative (-) = Positive (+)

**NOTE:** Same/similar signs give positive results.  
Different signs give negative results.

**BUT:** When positives are greater than negatives, the result is positive.  
E.g.  $+5 + -3 = +2$ .

When negative is greater than positive, the result is a negative. E.g.  
 $+2 + -5 = -3$ .

For example:



So,  $+5 + +4 = +\underline{\underline{9}}$

For example;

Workout:  $-3 + -2$  (Using mind map)


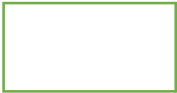


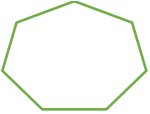
$-3 + (-2)$

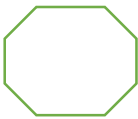

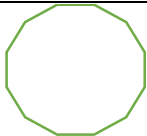
$-3-2$

-ve	- - - - -	-5
+ve		

So,  $-3 + -2 = -\underline{\underline{5}}$

### POLYGONS.

SHAPE	NUMBER OF SIDES
Triangle 	3
Quadrilateral Like: Rectangle, Square, Parallelogram, Kite, Trapezium and Rhombus. 	4
Pentagon 	5
Hexagon 	6
Septagon 	7

Octagon		8
Nonagon		9
Decagon		10
Hendagon/Nuodecagon		11
Duodecagon		12

Aid to memory

- ❖ A polygon is a simple closed figure joined by line segments at its end points (vertices). The prefix “POLY” means many. “GONS” means corners.

**BASES**

<u><b>BASES</b></u>	<u><b>BASE NAME</b></u>
Base one (1)	Unary base
Base two (2)	Binary base
Base three (3)	Trinary base/ternary base
Base four (4)	Quaternary base
Base five (5)	Quinary base
Base six (6)	Senary base/Seximal base
Base seven (7)	Septenary base/Septimal base
Base eight (8)	Octal base/Octonary base
Base nine (9)	Nonary base
Base ten (10)	Decimal base
Base eleven (11)	Undecimal base/undenary base
Base twelve (12)	Duodecimal base/dozenal

**EXAMPLES:**

1. Change  $100_{\text{two}}$  to base ten.

$$\begin{aligned}
 100_{\text{two}} &= (1 \times \text{two twos}) + (0 \times \text{twos}) + (0 \times \text{ones}) \\
 &= (1 \times 2 \times 2) + (0 \times 2) + (0 \times 1) \\
 &= 4 + 0 + 0 \\
 &= 4_{\text{ten}}
 \end{aligned}$$

Aid to memory:

To change non-decimal bases to decimal base, we multiple each digit in the numeral by its place value and then find the sum of the values.

2. Change  $12_{\text{ten}}$  to base two.

Base	No.	Rem
2	12	0
2	6	0
2	3	1
2	1	1
	0	

$$12_{\text{ten}} = 1100_{\text{two}}$$

Note: To change from decimal base to non-decimal base, we divide the given base ten number by given non-decimal base and record the remainders. We then read the remainders starting from the bottom.

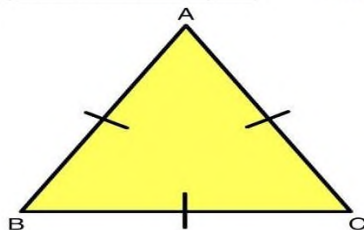
## TYPES AND PROPERTIES OF TRIANGLES.

### 1. Equilateral Triangle.

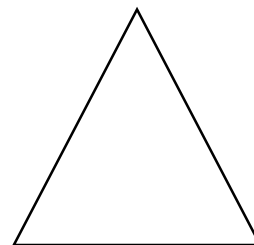
Has all the 3 sides equal  
All angles are equal  
Has 3 lines of symmetry

Equilateral Triangle

MATH  
MONKS



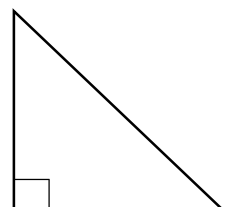
2. Isosceles triangle Two of its 3 sides are  
Two opposite angles are equal  
Has 1 line of symmetry Its interior angles  
add up to  $180^\circ$   
Its exterior angles add up to  $360^\circ$



equal

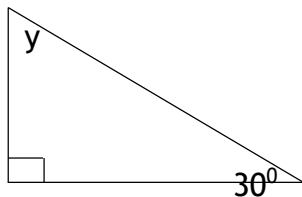
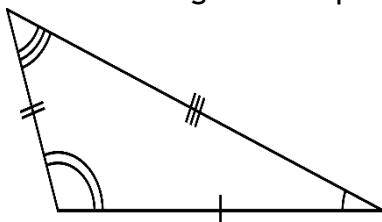
### 3. Right- angled scalene triangle

All sides are different  
All angles are different but one of them is  $90^\circ$   
Has no line of symmetry  
Its interior angles add up to  $180^\circ$



4. Scalene Triangle All Its 3 sides are not equal

Its interior angles add up to  $180^\circ$



$\Delta$

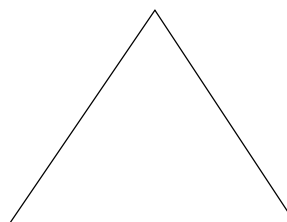
### EXAMPLES:

1. Find the size of angle y.
2. Find the size of r.

$50^\circ$

r

$60^\circ$



$y + 30^\circ + 90^\circ = 180^\circ$   
(angle sum of  $\Delta$ )

$$+ 50^\circ + 60^\circ = 180^\circ \text{ (sum of )}$$

$$110^\circ = 180^\circ$$

$$y + 120^\circ - 120^\circ = 180^\circ - 120^\circ$$

$$y = \underline{60^\circ}$$

$$180^\circ$$

$$r + 110^\circ - 110^\circ = 180^\circ - 110^\circ$$

$$= \underline{70^\circ}$$

$$\text{s/w}$$

$$\underline{70^\circ}$$

## ROMAN NUMERALS

Basic/Key Roman numerals.

Hindu-Arabic	1	5	10	50	100	500	1000
Roman numeral	I	V	X	L	C	D	M

**NOTE:** Other Roman numerals are got by either repeating or adding or subtracting.

Numerals beginning with the digits 2 and 3 are got by repeating.

Hindu-Arabic	2 = (1+1)	20 = (10+10)	200=(100+100)
Roman numeral	II	XX	CC

Hindu-Arabic	$3=(1+1+1)$	$30=(10+10+10)$	$300=(100+100+100)$
Roman numeral	III	XXX	CCC

**Numerals beginning with the digits 6, 7 and 8 are got by adding.**

Hindu-Arabic	$6=(5+1)$	$60=(50+10)$	$600=(500+100)$
Roman numeral	VI	LX	DC
Hindu-Arabic	$7=(5+2)$	$70=(50+20)$	$700=(500+200)$
Roman numeral	VII	LXX	DCC
Hindu-Arabic	$8=(5+3)$	$80=(50+30)$	$800=(500+300)$
Roman numeral	VIII	LXXX	DCCC

**Numerals beginning with the digits 4 and 9 are by subtracting.**

Hindu-Arabic	$4=(1 \text{ from } 5)$	$40=(10 \text{ from } 50)$	$400=(100 \text{ from } 500)$
Roman numeral	IV	XL	CD
Hindu-Arabic	$9=(1 \text{ from } 10)$	$90=(10 \text{ from } 100)$	$900=(100 \text{ from } 1000)$
Roman numeral	IX	XC	CM

**NOTE:** When Roman numerals, a letter is never repeated more than three times.

#### EXAMPLES:

1. Express **CMLXXV** as a Hindu Arabic numeral.

$$\begin{array}{rcl}
 \text{CMLXXV} & = & \text{CM} \quad \text{LXX} \quad \text{V} \\
 & & \downarrow \quad \downarrow \quad \downarrow \\
 & = & 900 + 70 + 5 \\
 & = & \underline{\underline{975}}
 \end{array}$$

2. Write **555** in Roman numerals.

$$\begin{array}{rcl}
 555 & = & 500 + 50 + 5 \\
 & = & \text{D} \quad \text{L} \quad \text{V} \\
 & = & \underline{\underline{DLV}}
 \end{array}$$

### DIVISIBILITY TEST.

**Divisibility test of 2:** The numbers ending with even digits like 0, 2, 4, 6 and 8 are divisible by 2. **E.g.** 682, 794, 370, 968, etc.

**Divisibility test of 3:** A number is exactly divisible by 3 if the sum of its digits is divisible by 3 or if the sum is a multiple of 3. **E.g.**  $255 = 2+5+5 = 12$  (12 is a multiple of 3 so, 255 can be divisible of 3).

**Divisibility test of 4:** A number is divisible by 4 if the number formed by its last two digits is divisible by 4 or multiple of 4. **E.g.** 572. The last two digits are 7 and 2, the number formed is 72 and 72 is a multiple of 4 so 572 can be divisible by 4.

**Divisibility test of 5:** A number is divisible by 5 if it ends with 5 or with 0. **E.g.** 20, 35, 470, 5675.

**Divisibility test for 6:** A number is divisible by 6 if it is divisible by 2 and 3. In other words a number is divisible by 6 if it is even and the sum of its digits is divisible by 3. **E.g.** 612 is divisible by 6 since it is an even number and the sum of its digits  $6+1+2 = 9$  is divisible by 3.

**Divisibility test for 7:** A number is divisible by 7 if the last digit of a number is doubled and the result is subtracted from the number formed by the remaining digits. The outcome is divisible by 7. **E.g.** take 315, the last digit is 5 and the remaining number is 31, double 5 to get  $(5 \times 2) = 10$ . Subtract 10 from 31 to give  $(31 - 10) = 21$ . 21 is divisible/multiple of 7, hence 315 is also divisible by 7.

**Divisibility test for 8:** A number is divisible by 8 if the number formed by the last three digits is divisible by 8. **E.g.** The number 4376, 376 is the number formed by the last three digits which is divisible by 8 therefore, 4376 is divisible by 8.

**Divisibility test for 9:** A number is divisible by 9 if the sum of its digits is divisible or a multiple of 9. **E.g.** 135 the sum is  $(1+3+5) = 9$ .

**Divisibility test for 10:** A number is divisible by 10 if the digit in the ones place (at end) is 0. Or a number which is divisible by 10 is also divisible by 2 and 5. **E.g.** 70, 800, 180, 3050.

**Divisibility test for 11:** A number is divisible by 11 if the difference between the sum of the digits in **even places** and the sum of the digits in the **odd places** is zero (0). **E.g.**

**Even position.**

489379

**Odd position.**

Sum of the number in odd position =  $4 + 9 + 7 = 20$ .

Sum of the number in even position =  $8 + 3 + 9 = 20$ .

The difference between sum of the numbers in even positions and sum of numbers in odd positions is  $20 - 20 = 0$ . So **489379** is divisible by 11.

## TYPES OF NUMBERS.

**Square numbers:** When a number is multiplied by itself once, you get a



**Cube numbers:** When a number is multiplied by itself three times, a cube number is formed. **E.g.**  $3 \times 3 \times 3 = 27$

**Triangle number:** When you add consecutive counting numbers from 1, the sum is always a triangle number.

$$1 = 1$$

$$1 + 2 = 3$$

$$1 + 2 + 3 = 6$$

$$1 + 2 + 3 + 4 = 10$$

**Prime numbers:** A prime number has only 2 factors (one and itself). **E.g.** 2, 3, 5, 7, 11, 13.

**Composite numbers:** A composite number has more than 2 factors. **E.g.** 4, 6, 8, 9, 10, 12.

**Even numbers:** Are numbers which are divisible by 2.

**E.g.** 0, 2, 4, 6, 8, 10, \_ \_ \_

**Odd numbers:** Are numbers which are not divisible by 2 or When divided by two it gives 1 as a reminder. **E.g.** 1, 3, 5, 7, 9, 11, 13, \_ \_ \_

### POINTS TO NOTE IN ANSWERING OR MAKING

1. All the working to the answers must be clearly shown.
2. Accuracy in the figures and diagrams is very important.
3. Ensure correct units are included on the answers.
4. All the work (steps) should be shown.
5. Omission of units leads to loss of marks.
6. Change of parameters for example using "X" instead of "y" given in the question leads to loss of marks.
7. Omission of labels on diagrams leads to loss marks.
8. Sketches are awarded marks.