P425/2 APPLIED MATHEMATICS PAPER 2 JULY/AUGUST 2024 3 HOURS

# ASSHU BUSHENYI DISTRICT MOCK EXAMINATIONS 2024 UGANDA ADVANCED CERTIFICATE OF EDUCATION APPLIED MATHEMATICS PAPER 2 3 HOURS

### INSTRUCTIONS TO CANDIDATES

- Attempt all the eight questions in section A and only five questions from section B.
- Any additional question answered(s) answered will not be marked.
- All necessary working must be shown clearly.
- Any graphical number should fully be attempted on a graph paper.
- Silent non-programmable scientific calculator and mathematical tables with a list of formulae may be used.
- In numerical work take acceleration due to gravity(g) to be 9.8ms<sup>-2</sup>.

de Minter

#### SECTION A: (40 MARKS)

#### Answer all the questions in this section.

- 1. A particle P is observed to execute S.H.M with amplitude 2m and period 2 seconds. If P is initially moving at maximum speed, determine the;
  - (a) Distance moved by the particle until its half the maximum speed.
  - (b) Time taken by the particle to travel the distance in (i) above.

(5marks)

2. The table below is an extract from tables of X<sup>0</sup> and SinX<sup>0</sup>

| $X_0$             | 0.00   | 0.20   | 0.40   | 0.60   | 0.80   |
|-------------------|--------|--------|--------|--------|--------|
| SinX <sup>0</sup> | 0.1736 | 0.1771 | 0.1805 | 0.1840 | 0.1891 |

Use linear interpolation or extrapolation method to estimate.

- (a)  $Sin (10.27^0)$ ,
- (b) Sin<sup>-1</sup> (0.1899).

(5marks)

- 3. Independent events A and B are such that  $(P(A \cup B) = \frac{3}{5})$  and  $P(A) = \frac{2}{5}$ . Find;
  - (a) P(B)
  - (b)  $P(A \cap \overline{B})$

(5marks)

4. A uniform ladder AB of length 4m and mass 10kg rests with ends A on a rough horizontal ground and B on smooth vertical wall. If B is 2m above the ground and the co-efficient of friction between the ground and ladder is 0.27, find the maximum horizontal force that can be applied at A before motion occurs.

(5marks)

- 5. Given that x=12.7654 and y=13.80. State the maximum possible errors in x and y, determine the maximum value and minimum value and hence the absolute error in the expression  $\frac{(x+y)}{xy}$ . (5marks)
- 6. The table below shows the marks awarded to students A, B, C, D, E and F by two judges I and II during a certain competition.

| Students | Α  | В  | C  | D  | E  | F  |
|----------|----|----|----|----|----|----|
| Judge I  | 40 | 58 | 84 | 58 | 63 | 77 |
| Judge II | 58 | 71 | 83 | 65 | 71 | 53 |

Calculate the rank correlation co-efficient and give a comment at 5% level of significance.

(5marks)

- 7. A particle starts from rest moving with a constant acceleration of  $3 \text{ms}^{-2}$  for 12 seconds, for the next 48s the acceleration is  $\frac{1}{6} \text{ms}^{-2}$  and for the last 10s it decelerates uniformly to rest, by drawing the velocity-time graph. Find the,
  - (a) Velocities at different points,
  - (b) Total distance travelled.

(5marks)

- 8. A biased coin is tossed six times. The coin is such that the ratio of that tail to the head is 2:1. Find the probability of getting:
  - (a) At least 4 heads
  - (b) Between 3 and 5 tails.

(5marks)

## SECTION B (60 MARKS) Answer any five questions from this section. All questions carry equal marks

- 9. A lorry of mass 2,000kg travels around a circle of radius 500m at 48kmhr<sup>-1</sup>. The distance between the wheels is 2m and the centre of gravity of the lorry is 2.5m above the ground level, determine the;
  - (a) Horizontal and vertical pressure, if the wheels are at the same level.
  - (b) Height at which the outer tyre should be raised to avoid pressure on the wheels.

(12marks)

- 10. (a) Derive the simplest iterative formulae based on newton Raphson method for the equation  $10(1-\cos x)=2-3x$  and show that it's given by:  $x_{n+1} = \frac{10 x_n \sin x_n + 10\cos x_n 8}{10 \sin x_n + 3}$ : x=0,1,2,...
  - (b) Construct a flow chart that:
    - (i) Reads initial approximation  $(x_0)$ .
    - (ii) Computes and limits the error to a number corrected to 3 decimal places.
    - (iii) Prints the root  $(x_{n+1})$  and number of iterations (n).
  - (c) Using  $x_0 = 0.55$  and the flow chart in (b) above perform a dry run for the flow chart above.

(12marks)

- 11. (a) Box P contains 3 white and 4 blue beads while box Q contains 5 white and 3 blue beads. A bead is drawn at random from P and put into Q and then a bead is taken from Q and put into P. find the probability that the bead drawn from P is white. (5marks)
  - (b) Bag X contains 4 red and 3 blue pens, while bag Y contains 3 red and 2 blue pens. A bag is selected at random and two pens are drawn from it without replacement. Find the probability of picking:
    - (i) Pens of different colours.

(4marks)

(ii) Bag Y given that the pens drawn are of the same colour.

(3marks)

- 12. (a) Find the centre of gravity of a semicircular lamina of radius (r) from the base which is the diameter and show that it's given by  $\frac{4r}{3\pi}$ .
- (b) A semi-circular lamina of radius (r = OA) and base (OB) is cut from a large semi-circular lamina of radius (2r= OB), with diameter base (OC), determine the centre of gravity of the remainder from base (OC).

  (12 marks)

13. The table below shows the distribution of the height of students in a certain school.

| Height(cm) | Frequency |       |  |
|------------|-----------|-------|--|
| 120-<130   | 7         |       |  |
| 130-<135   | . 8       | the c |  |
| 135-<145   | 36        |       |  |
| 145-<155   | 39        |       |  |
| 155-<170   | 17        |       |  |
| 170-<175   | 3         |       |  |
| 175-<190   | 5         |       |  |

- (a) Calculate the;
  - (i) mean
  - (ii) Standard deviation
- (b) Draw a cumulative frequency curve and use it to estimate the
  - (i) Median
  - (ii) Number less than height 150cm.

(12marks)