## **SECTION A (40 MARKS)**

## Answer ALL questions in this section

- 1. Solve the equation  $Sin3\theta = Cos\theta$  for  $0^o \le \theta \le 180^o$ . (05 marks)
- 2. Given that  $x^3 = (y 3x)^2$  show that;  $2x \frac{dy}{dx} = 3y 3x$ .

  (05 marks)
- 3. A(3,5) and B(-5,-1) are points on a line. Find the coordinates of point C that divides  $\overrightarrow{AB}$  in the ratio 3:1.
  - (a) Internally
  - (b) Externally

(05 marks)

- Find the equation of the tangent to the curve y = 1 + 2sinx at  $x = \frac{\pi}{4}$ .

  (05 marks)
- 5. Given that z = 1 + 3i find the real numbers, x and y such that  $xZ + y\bar{Z} = 7 + 3i$ . (05 marks)
- 6. O(0,0) and Q(4,0) are fixed points. P(x,y) is a variable point. Given that  $\langle OPQ = 45^{\circ}$ , find the locus of P(x,y). (05 marks)
- 7. When a polynomial P(x) is divided by  $x^2 4$ , the remainder is 3x + 7. find the remainder when P(x) is divided by;
  - (a) x-2
  - (b) x + 2

(05 marks)

8. Evaluate;  $\int_0^{\sqrt{3}} \frac{dx}{\sqrt{3-x^2}}$  without using tables.

(05 marks)

## SECTION B (60 MARKS)

- 9.  $\sqrt{a}$  Express  $\sqrt{3} Sin\theta + Cos\theta$  in the form  $Rsin(\theta + \alpha)$ . (03 marks) Hence solve the equation  $\sqrt{3}Sin\theta + Cos\theta = \sqrt{2}$ , for  $0^o \le \theta \le 360^o$ . (03 marks)
  - (b) Prove the Cosine rule  $a^2 = b^2 + c^2 2bc \, Cos A$  for any triangle ABC. Hence solve the triangle in which b = 5cm, c = 8cm and  $A = 60^\circ$ .
  - 10.  $\vee$  (a) Use the mathematics of small changes to evaluate Sin 29.5° to 4 dpls. (05 marks)
    - (b) A right circular cone has a slant length of 9√3cm. Calculate the maximum volume of the cone; and state the corresponding values of the height and the radius in this case. (07 marks)
    - 11. (a) Find the term in  $x^{-3}$  in the expansion of;  $\left(x^2 + \frac{1}{2x}\right)^9$  (04 marks)
      - (b) Expand  $\sqrt{1 \frac{1}{4}x}$  up to the term in  $x^3$ ; and use the expansion to evaluate;
        - (i)  $\sqrt{15}$  to 3dps
        - (ii)  $\sqrt{7}$  to 4dps (08 marks)
  - 12. Express  $\frac{x^6 + 64}{x^4 16}$  in partial fractions; hence evaluate;

$$\int_{3}^{4} \frac{x^{6} + 64}{x^{4} - 16} dx \quad to \quad 4dps$$

(12 marks)

13.  $\sqrt{a}$  Find the coordinates of the point of intersection of the lines;  $\sqrt{2}$   $\sqrt{2}$   $\sqrt{2}$   $\sqrt{3}$ 

$$r_1 = \begin{pmatrix} 2 \\ -4 \\ 4 \end{pmatrix} + \lambda \begin{pmatrix} 2 \\ 3 \\ -1 \end{pmatrix}$$
 and  $r_2 = \begin{pmatrix} 10 \\ 1 \\ 7 \end{pmatrix} + \mu \begin{pmatrix} 3 \\ 1 \\ 2 \end{pmatrix}$ ;

and compute the acute angle between the lines.

(09 marks)

- (b) Write down the vector equation of the plane containing the two lines in (a) above.

  (03 marks)
- 14. Given the curve  $y = \frac{2x-5}{x^2-4}$ 
  - (a) Find its stationary points; hence state the region within which the curve does not lie.

    (b) Charles and the curve does not lie.
  - Sketch the curve, and deduce the solution to the inequality  $\frac{2x-5}{x^2-4} \ge 0$ (06 marks)
- Prove that the equations of the tangent to the parabola  $y^2 = 4ax$ At the variable point  $(at^2, 2at)$  is  $x - ty + at^2 = 0$ . (03 marks)
  - (b) Deduce the equations of the tangents to the parabola  $y^2 = 4ax$  from the external point A(-6a, a); (04 marks)

    Hence (i) find the coordinates of the points of section a
    - find the coordinates of the points of contact of the tangents with the parabola.

      (02 marks)
    - (ii) show that the tangents make 45° with each other.

(03 marks)

- 16. The temperature,  $\theta^o C$ , at a height h metres risen above the foot of a 1000 m high mountain, decreases at a rate which is directly proportional to
  - (a) A tourist notices that the temperature of water drops from 16°C, at the foot of the mountain, to -9°C at the peak of the mountain. Set up a differential equation for this problem and solve it. (06 marks)
  - (b) Calculate the;
    - (i) height at which water starts to freeze. (03 marks)
    - (ii) temperature the water should have at the foot of the mountain if it just freezes at the top of the mountain.

END