

This document is sponsored by

The Science Foundation College Kiwanga- Namanve
Uganda East Africa
Senior one to senior six

+256 778 633 682, 753 802709 Based on, best for sciences

UCE MATHEMATICS PAPER 2 2013 guide

#### SECTION A (40 marks)

## Answer all questions in this section

- 1. Without using mathematical tables or a calculator, simplify  $\frac{(0.25)^2 x \left(\frac{1}{64}\right)^2}{(128)^{-2}}$ . (04 marks)
- 2. Given that M = {the five multiples of 3) and S = {the first five square numbers}, find
  - (a) M∩S
  - (b) nM∩S)
- 3. The position vector of P and Q are  $\binom{-6}{15}$  and  $\binom{4}{5}$  respectively.

Find the magnitude of PQ. (04marks)

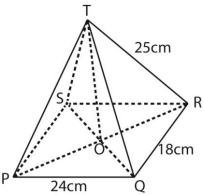
- 4. A line whose gradient is 3, passes through the point (2, 1). Find the
  - (a) equation of the line
  - (b) y-intercept (04marks)
- 5. Simplify  $\frac{2.4 \times 10^2}{6.0 \times 10^{-3}}$
- 6. Given the f(x) = 3x + 5 and  $g(x) = \frac{2}{x-5}$ ; find
  - (a) gf(x)
  - (b)  $gf(\frac{1}{2})$  (04marks)
- 7. Find the distance between the points (5, 9) and (-7, 2). Give your answer to one decimal place (04marks)
- A traveller had £800. She exchanged into Uganda shillings (Ug. Shs.) at a rate of £1 for Ug. Shs.
   3,200. She used Ug. Shs. 720, 000 in a hotel. How much money in Ug. Shs. Did she remain with?
   (04marks)
- 9. Two similar plastic containers have capacities of 2 litres and 54 litres. If the height of the big container is 87 cm, find the height of the small container. (04 marks)
- 10. A scale on a map is 1; 500,000. What distance in kilometres does 2 centimetre on the map represent?

## **SECTION B (60MARKS)**

Answer any five questions from this section. All questions carry equal marks.

- 11. If h(x) = px + 3 and that h(4) = 23.
  - (a) Find the value of
    - (i) p
    - (ii) h(0)
    - (iii) h(-5) (07marks)

- (b) determine
  - (i)  $h^{-1}(x)$
  - (ii)  $h^{-1}(13)$  (05 marks)
- 12. A quantity p is partly constant and partly varies as the square of q. when q = 2, p = 40; when q = 3, p = 65.
  - (a) Form an equation relating p and q. (08 marks)
  - (b) Determine the values of q when p = 100. (04 marks)
- 13. (a) Peter deposited shs. 2,500,000 in a bank which offers a compound interest of 15% per annum. How much money did he have in the bank at the end of two years? (05 marks)
  - (b) The cash price of a radio is shs. 720,000. It can be bought on a hire purchase terms by marking a deposit of 30% of the cash price and then paying 8 monthly instalments of shs. 85, 000 each.
    - (i) Find the cost of the radio on hire purchase term
    - (ii) How much more does one pay on hire purchase rather than on cash term? (07 marks)
- 14. In a class of 40 students, 18 play Hockey (H), 15 play Tennis (T) and 22 play Football. 7 play hockey and tennis. 9 play tennis and football. 8 play hockey and football. 4 play all the three games.
  - (a) Represent the given information on a Venn diagram. (06marks)
  - (b) Find the number of students who do not play any of the three games. (02 marks)
  - (c) Find the probability that a student chosen at random plays only
    - (i) one game
    - (ii) two games (04marks)
- 15. A cyclist sets off from town A at 4.00am at a speed of 20kmh<sup>-1</sup> to go to town B, 100km away. A motorist also sets off from town a at 7;30am at a speed of 100kmh<sup>-1</sup> to go to town B. Find
  - (a) distance from town A when the motorist overtakes the cyclist. (06 marks)
  - (b) time when the motorist overtakes the cyclist (03marks)
  - (c) time the cyclist reached town B (03marks)
- 16. A quadrilateral OABC has points P, Q and R on OA, OB and OC respectively. OA = 3OP, OB = 5OQ and OC = 2OR, OP = p, OQ = q and OR = r.
  - (a) Express the following vectors in terms of p, q, and r.
    - (i) PQ
    - (ii) AB
    - (iii) BC
    - (iv) CA (09marks)
  - (b) Given that OABC is a parallelogram, show that 3p 5q + 2r = 0 (03 marks)
- 17. In the figure below, PQRST is a right pyramid with a rectangular base. PQ = 24cm, QR = 18cm. the slanting edges are 25cm each.



Calculate the:

- (a) Height of the pyramid, (06marks)
- (b) Angle between the slanting face QRT and the base (03 marks)
- (c) Volume of the pyramid. (03marks)

## **Solutions**

## SECTION A (40 marks)

Answer all questions in this section

1. Without using mathematical tables or a calculator, simplify  $\frac{(0.25)^2 x \left(\frac{1}{64}\right)^2}{(128)^{-2}}$ . (04 marks)

$$\frac{(0.25)^2 x \left(\frac{1}{64}\right)^2}{(128)^{-2}} = (0.25)^2 x \left(\frac{1}{64}\right)^2 x (128)^2$$

$$= \left(\frac{25}{100}\right)^2 x \left(\frac{1}{64}\right)^2 x (2^7)^2$$

$$= \left(\frac{1}{4}\right)^2 x \left(\frac{1}{64}\right)^2 x (2^7)^2$$

$$= \left(\frac{1}{2^2}\right)^2 x \left(\frac{1}{2^6}\right)^2 x (2^7)^2$$

$$= 2^{-4} x 2^{-12} x 2^{14}$$

$$= 2^{-2} = \frac{1}{2^2} = \frac{1}{4}$$

2. Given that  $M = \{\text{the five multiples of 3}\}$  and  $S = \{\text{the first five square numbers}\}$ , find

No.	Multiple of 3 (M)	square No. (S
1	1 x 3 = 3	$1^2 = 1$
2	2 x 3 = 6	$2^2 = 4$
3	3 x 3 = 9	$3^2 = 9$
4	3 x 3 = 12	$4^2 = 16$
5	5 x 3 = 15	$5^2 = 25$
$M = \{3,$	6, 9, 12, 15}	

$$M = \{3, 6, 9, 12, 15\}$$

$$S = \{1, 4, 9, 16, 25\}$$

- (a)  $M \cap S = \{9\}$
- (b)  $nM \cap S$ ) = 1
- 3. The position vector of P and Q are  $\binom{-6}{15}$  and  $\binom{4}{5}$  respectively.

Find the magnitude of PQ. (04marks)

$$PQ = OQ - OP$$

$$= {4 \choose 5} - {-6 \choose 15} = {10 \choose -10}$$

$$|PQ| = \sqrt{10^2 + (-10)^2} = \sqrt{100 + 100} = \sqrt{200} = 14.142 = 14.14 (2D)$$

- 4. A line whose gradient is 3, passes through the point (2, 1). Find the
  - (a) equation of the line

Let a point with coordinates (x, y) line on the line

(2,1) 
$$(x, y)$$
  
Gradient =  $\frac{y-1}{x-2}$  = 3  
 $y-1 = 3(x-2)$   
 $y-1 = 3x-6$ 

$$y = 3x - 5$$

(b) y-intercept (04marks)

the line cuts y-axis when x =

$$y = 0 - 5 = -5$$

hence y- intercept = (0, -5)

5. Simplify 
$$\frac{2.4 \times 10^2}{6.0 \times 10^{-3}}$$
  $\frac{2.4 \times 10^2}{6.0 \times 10^{-3}} = \frac{24}{10} \times 10^2 \times \frac{1}{6} \times 10^3 = 4 \times 10^4$ 

- 6. Given the f(x) = 3x + 5 and  $g(x) = \frac{2}{x-5}$ ; find
  - (a) gf(x)

gf(x) = g(3x + 5) = 
$$\frac{2}{(3x+5)-5} = \frac{2}{3x}$$

$$\therefore gf(x) = \frac{2}{3x}$$

(b)  $gf(\frac{1}{2})$  (04marks)

$$gf(\frac{1}{2}) = \frac{2}{3\frac{1}{2}} = \frac{4}{3} = 1\frac{1}{3}$$

7. Find the distance between the points (5, 9) and (-7, 2). Give your answer to one decimal place (04marks)

Let points be P(5, 9) and Q(-7, 2).

Distance between two points =  $\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$ 

$$PQ = \sqrt{(-7-5)^2 + (2-9)^2}$$

$$=\sqrt{(-12)^2+(-7)^2}$$

$$=\sqrt{144 + 81}$$

$$=\sqrt{193}=13.9$$
 (1D)

- 8. A traveller had £800. She exchanged into Uganda shillings (Ug. Shs.) at a rate of £1 for Ug. Shs. 3,200. She used Ug. Shs. 720, 000 in a hotel. How much money in Ug. Shs. Did she remain with? (04marks)
- 9. Two similar plastic containers have capacities of 2 litres and 54 litres. If the height of the big container is 87 cm, find the height of the small container. (04 marks) V.S.F =  $\frac{volume\ of\ big\ cntainer}{volume\ of\ small\ container} = \frac{54}{2} = 27$

V.S.F = 
$$\frac{volume\ of\ big\ cntainer}{volume\ of\ small\ container} = \frac{54}{2} = 27$$

L.S. 
$$F = \sqrt[3]{27} = 3$$

But L.S.F = 
$$\frac{height\ of\ big\ container}{height\ of\ small\ container} = \frac{87}{h} = 3$$

$$h = \frac{87}{3} = 29cm$$

hence height of the small container is 29cm

h(4) = 4p + 3 = 23

10. A scale on a map is 1: 500,000. What distance in kilometres does 1 centimetre on the map represent?

$$1cm = 500,000cm$$

$$1 \text{cm} = \frac{500,000}{100,000} = 5km$$

# **SECTION B (60MARKS)**

Answer any five questions from this section. All questions carry equal marks.

- 11. If h(x) = px + 3 and that h(4) = 23.
  - (a) Find the value of

- (b) determine
  - $h^{-1}(x)$ (i) let y = 5x + 35x = y - 3 $x = \frac{y-3}{5}$   $h^{-1}(x) = \frac{x-3}{5}$
  - h<sup>-1</sup>(13) (05 marks) (ii)  $h^{-1}(13) = \frac{13-3}{5} = 2$
- 12. A quantity p is partly constant and partly varies as the square of q. when q = 2, p = 40; when q =3, p = 65.
  - (a) Form an equation relating p and q. (08 marks)

Form an equation relating p and 
$$p = a + kq^2$$
  
Substituting  $q = 2$  and  $p = 0$   
 $a + k(2)^2 = 40$   
 $a + 4k = 40$  ..............(i)  
Substituting  $q = 3$  and  $p = 65$   
 $a + k(3)^2 = 65$   
 $a + 9k = 65$  ............(ii)  
Subtracting (i) from (ii)  
 $5k = 25$   
 $k = 5$   
Substituting for  $k = 13$  in eqn. (i)

$$a = 20$$

Hence the equation

$$p = 20 + 5q^2$$

(b) Determine the values of q when p = 100. (04 marks)

$$100 = 20 + 5q^{2}$$

$$5q^{2} = 80$$

$$q = \sqrt{16} = \pm 4$$

Hence q = 4 and q = -4

13. (a) Peter deposited shs. 2,500,000 in a bank which offers a compound interest of 15% per annum. How much money did he have in the bank at the end of two years? (05 marks) With compound interest

$$A = p \left( 1 + \frac{r}{100} \right)^n$$
= 2, 500,000  $\left( 1 + \frac{15}{100} \right)^2$ 
= shs. 3,306,250

- (b) The cash price of a radio is shs. 720,000. It can be bought on a hire purchase terms by marking a deposit of 30% of the cash price and then paying 8 monthly instalments of shs. 85, 000 each.
  - (i) Find the cost of the radio on hire purchase term

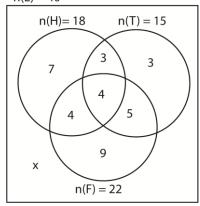
Cost = 
$$\frac{30}{100}$$
 x 720,000 + 8 x 85,000  
= 216,000 + 680,000  
= shs. 896,000

(ii) How much more does one pay on hire purchase rather than on cash term? (07 marks)

Extra money paid = 896,000 - 720,000 =shs. 176,000

- 14. In a class of 40 students, 18 play Hockey (H), 15 play Tennis (T) and 22 play Football. 7 play hockey and tennis. 9 play tennis and football. 8 play hockey and football. 4 play all the three games.
  - (a) Represent the given information on a Venn diagram. (06marks)

$$n(E) = 40$$
,  $n(H) = 18$ ,  $n(T) = 15$ ,  $n(F) = 22$ ,  $n(H \cap T) = 7$ ,  $n(T \cap F) = 9$ ,  $n(H \cap F) = 8$ ,  $n(H \cap T \cap F) = 4$   $n(E) = 40$ 



T only = 
$$15 - (3 + 5 + 4) = 3$$
  
H only =  $18 - (3 + 4 + 4) = 7$   
P only =  $22 - (4 + 4 + 5) = 9$ 

(b) Find the number of students who do not play any of the three games. (02 marks)

$$18 + 3 + 5 + 9 + x = 40$$

$$35 + x = 40$$

$$x = 5$$

hence the number of students that do not play any of the three is 5

- (c) Find the probability that a student chosen at random plays only
  - (i) one game
  - Students that play one game = n(H) only + n(T) only + n(F) only (ii) = 7 + 3 + 9 = 19

Probability for the student chosen =  $\frac{19}{40}$ 

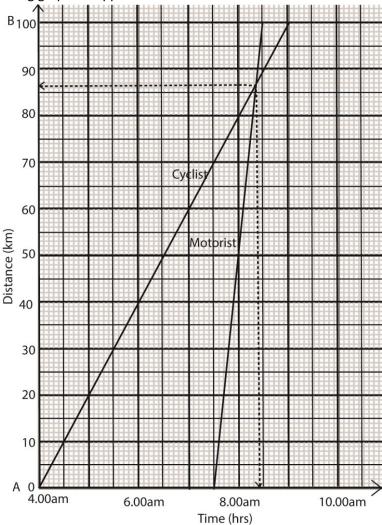
(iii) two games (04marks)

Students that play two games =  $n(H \cap T)$ ,  $n(T \cap F) = 9$ ,  $n(H \cap F) = 8$ 

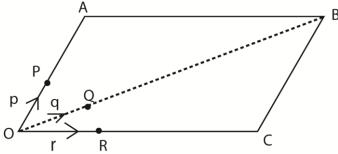
$$= 3 + 4 + 5 = 12$$

Probability that a student plays two games =  $\frac{12}{40} = \frac{3}{10} = 0.3$ 

15. A cyclist sets off from town A at 4.00am at a speed of 20kmh<sup>-1</sup> to go to town B, 100km away. A motorist also sets off from town a at 7;30am at a speed of 100kmh<sup>-1</sup> to go to town B. Find Using graphical approach.



- (a) distance from town A when the motorist overtakes the cyclist. (06 marks) 88km
- (b) time when the motorist overtakes the cyclist (03marks) 8:30 +  $\frac{4}{5}$  x 30 8:54am
- (c) time the cyclist reached town B (03marks) 9:00am
- 16. A quadrilateral OABC has points P, Q and R on OA, OB and OC respectively. OA = 3OP, OB = 5OQ and OC = 2OR, OP = p, OQ = q and OR = r.



(a) Express the following vectors in terms of p, q, and r.

(i) 
$$PQ = PO + OQ = -p + q$$

(ii) 
$$AB = AO + B = -3OP + 5OQ = -3p + 5q$$

(iii) BC = BO + OC  
= 
$$-(-3p + 5q) + 2OR$$
  
=  $3p - 5q + 2r$ 

$$CA = CO + OA$$

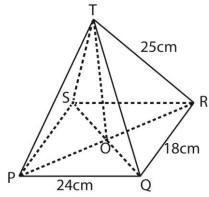
(b) Given that OABC is a parallelogram, show that 3p - 5q + 2r = 0 (03 marks)

$$OB = OA + AB$$

$$5q = 3p + 2r$$

$$\Rightarrow$$
 3p + 2r -5q = 0

17. In the figure below, PQRST is a right pyramid with a rectangular base. PQ = 24cm, QR = 18cm. the slanting edges are 25cm each.

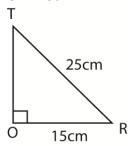


Calculate the:

(a) Height of the pyramid, (06marks)

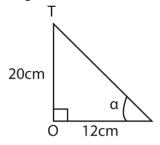
$$PR^2 = 24^2 + 18^2 = 576 + 324 = 900$$

$$PR = \sqrt{900} = 30cm$$



Height OT = 
$$\sqrt{25^2 - 15^2} = \sqrt{625 - 225} = \sqrt{400} = 20$$
cm

(b) Angle between the slanting face QRT and the base (03 marks)



$$\tan\alpha = \frac{20}{12}$$
 
$$\alpha = \tan^{-1}\left(\frac{20}{12}\right) = 59^{0}$$
 (c) Volume of the pyramid. (03marks)

Volume = 
$$\frac{1}{3}Lwh = \frac{1}{3} x 24 x 18 x 20 = 2,880 \text{ cm}^3$$

Thank you

Dr. Bbosa Science