

WAKISSHA JOINT MOCK EXAMINATIONS

MARKING GUIDE

Uganda Advanced Certificate of Education

UACE August

Mathematics P425/2

July/August 2023



$\frac{4}{7} + 2 \cdot \frac{4}{7} \left(\frac{3}{2} - x \right)$

$\frac{4}{7} + 21 - \frac{8}{7}$
 $\frac{7}{7} \frac{7}{7}$

1.

$$P(B) = \frac{1}{6}, \quad P(A \cap B) = \frac{1}{12}, \quad P(B/A) = \frac{1}{3}$$

$$\text{From } P(B/A) = \frac{P(B \cap A)}{P(A)}$$

$$\begin{aligned} \text{(a) (i)} \quad P(A) &= \frac{P(B \cap A)}{P(B/A)} \\ &= \frac{1}{12} \div \frac{1}{3} \\ &= \frac{1}{4} \end{aligned}$$

M₁

A₁

$$\begin{aligned} \text{(ii)} \quad P(A/B^c) &= \frac{P(A \cap B^c)}{P(B^c)} \\ &= P(A) = \frac{P(A \cap B)}{P(B)} \\ &= \frac{\frac{1}{4}}{\frac{5}{6}} \\ &= \frac{6}{20} \\ &= \frac{3}{10} \end{aligned}$$

M₁

A₁

$$\text{(iii) For independence } \frac{1}{12} = \frac{1}{4} \cdot \frac{1}{3}$$

$$\frac{1}{12} \neq \frac{1}{24}$$

A and B are not independent.

B₁

2. (i)

T(s)	240	300	360
$\theta^0 C$	75	θ_1	69

05 marks

B₁

$$\frac{69 - 75}{360 - 240} = \frac{\theta_1 - 75}{300 - 240}$$

$$\frac{-6}{120} = \frac{\theta_1 - 75}{60}$$

$$\theta_1 = 75 + \left(\frac{-6 \times 60}{120} \right)$$

$$= 70^\circ \rightarrow \theta_1 = 72^\circ C.$$

M₁

A₁

(ii)

T(s)	450	600	T ₁
θ°C	54	46	42

$$\frac{42-54}{T_1-450} = \frac{46-54}{600-450}$$

$$\frac{-14}{T_1-450} = \frac{-8}{120}$$

$$T_1 = 450 + \frac{14 \times 120}{8}$$

$$= 690 \text{ s}$$

$$T = 675 \text{ s.}$$

M₁A₁

5 marks

3.

$$u = 72 \times \frac{1000 \text{ ms}^{-1}}{3600}$$

$$= 20 \text{ ms}^{-1}$$

$$v = 36 \times \frac{1000}{3600}$$

$$= 10 \text{ ms}^{-1}$$

$$\text{From } v^2 = u^2 + 2as$$

$$10^2 = 20^2 + 2a \times 800$$

$$100 = 400 + 1600a$$

$$a = \frac{-3}{16} \text{ ms}^{-2} \text{ or } -0.1875 \text{ ms}^{-2}$$

B₁for both 20ms⁻¹
and 10ms⁻¹M₁A₁with correct
units.

$$\text{From } v^2 = u^2 + at$$

$$10 = 20 - \frac{3}{16}t$$

$$t = \frac{160}{3} \text{ second or } 53.3 \text{ seconds}$$

M₁A₁

≥10

5 marks

4.

$$\frac{P_{2021}}{P_{2000}} = \frac{90}{100}, \frac{P_{2022}}{P_{2021}} = \frac{120}{100}$$

B₁

$$\frac{P_{2022}}{P_{2000}} = \frac{P_{2022}}{P_{2021}} \times \frac{P_{2021}}{P_{2000}}$$

M₁

$$= \frac{120}{100} \times \frac{90}{100}$$

A₁

$$= \frac{27}{25}$$

M₁

$$\therefore P_{2022} = \frac{27}{25} \times 200,000$$

$$= 216000/-$$

A₁

5 marks

5.

$$d = \frac{2-1}{5} = 0.2 \text{ or } \frac{1}{5}$$

x	$y = x \sin x$	$\sin x$
1.0	0.8415	
1.2		1.1184
1.4		1.3796
1.6		1.5993
1.8		1.7529
2.0	1.8186	
sum	2.6601	5.8502

B₁B₁ - All values of xB₁ all values y

Using the trapezium rule for 6 ordinates.

$$= \frac{1}{2} \times 0.2 \times [2.6601 + 2 \times 5.8502]$$

$$= 0.1 \times 13.8205 \quad 14.3605$$

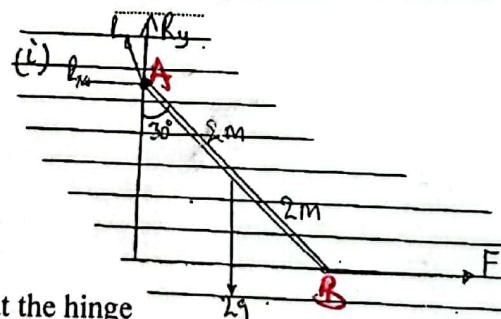
$$= 1.38205 \quad \approx 1.43605$$

$$I \approx 1.382 \quad \approx 1.436 \quad (3 \text{ d.p.})$$

M₁A₁

5 marks

6. (i)



Taking moments about the hinge

$$4F \cos 30^\circ = 2 \sin 30^\circ \times 2g$$

$$F = \frac{2 \times \sin 30^\circ \times 2 \times 9.8}{4 \times \cos 30^\circ}$$

$$= 5.6580N$$

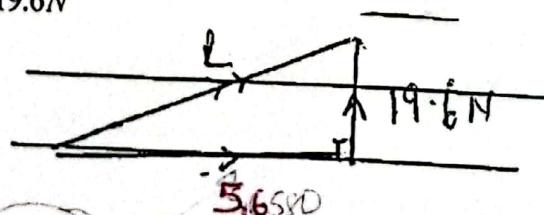
B₁M₁A₁

(ii) Resolving forces

$$R_y = 2g \quad R_x = F$$

$$= 2 \times 9.8 \quad R_x = 5.6580N$$

$$= 19.6N$$

M₁A₁

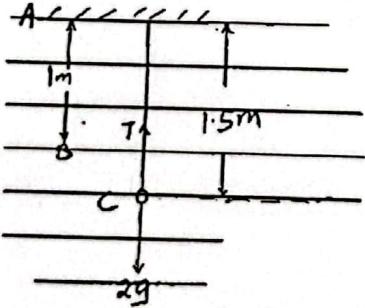
$$R = \sqrt{5.6580^2 + 19.6^2}$$

$$\therefore |R| = 20.4003N$$

5 marks

7.	(a) Let J: Jane, M: Mary, A: Alice $P(J) = P(J^1 \cap M^1 \cap A) = P(J^1) \cdot P(M^1) \cdot P(A)$ $= \frac{5}{6} \times \frac{5}{6} \times \frac{1}{6}$ $= \frac{25}{216}$ $\text{or } 0.1157$ (4dp)	M ₁	A ₁
----	--	----------------	----------------

	(b) 1 st time P(A) = $\frac{1}{6}$ 2 nd time P(A) = $\frac{1}{6} \times \left(\frac{5}{6}\right)^3$ 3 rd time P(A) = $\frac{1}{6} \times \left(\frac{5}{6}\right)^6$ $P(\text{winning}) = \frac{1}{6} + \frac{1}{6} \left(\frac{5}{6}\right)^3 + \frac{1}{6} \left(\frac{5}{6}\right)^6 + \dots$ $a = \frac{1}{6}, r = \left(\frac{5}{6}\right)^3$ $S_{\infty} = \frac{a}{1-r}$ $= \frac{\frac{1}{6}}{1 - \left(\frac{5}{6}\right)^3}$ $= \frac{36}{91} \text{ or } 0.3956$ (4dp)	M ₁	A ₁
--	---	----------------	----------------

8.		5 marks	
	From point A to B Loss in P.E = gain in K. E $= 2 \times 9.8 \times 1$ $= 19.6 \text{ J}$	B ₁	
	From B to C Loss in P.E and K.E = elastic P.E stored $19.6 + 2 \times 9.8 \times x = \frac{\lambda x^2}{2l_0}$	A ₁	
	$19.6 + 2 \times 9.8 \times (1.5 - 1) = \frac{\lambda (1.5 - 1)^2}{2 \times 1}$	M ₁	
	$\therefore \lambda = 235.2 \text{ N}$	A ₁	5 marks

9.	<table border="1" style="width: 100%; border-collapse: collapse;"> <thead> <tr> <th style="text-align: left;">Height</th><th style="text-align: left;">Freq</th><th style="text-align: center;">x</th><th style="text-align: center;">fx</th><th style="text-align: center;">fx^2</th><th style="text-align: center;">C.f</th></tr> </thead> <tbody> <tr> <td>120 - 124</td><td>5</td><td style="text-align: center;">122</td><td style="text-align: center;">610</td><td style="text-align: center;">74420</td><td style="text-align: center;">5</td></tr> <tr> <td>125 - 129</td><td>17</td><td style="text-align: center;">127</td><td style="text-align: center;">2159</td><td style="text-align: center;">274193</td><td style="text-align: center;">22</td></tr> <tr> <td>130 - 134</td><td>20</td><td style="text-align: center;">132</td><td style="text-align: center;">2640</td><td style="text-align: center;">348480</td><td style="text-align: center;">42</td></tr> <tr> <td>135 - 139</td><td>25</td><td style="text-align: center;">137</td><td style="text-align: center;">3425</td><td style="text-align: center;">469225</td><td style="text-align: center;">67</td></tr> <tr> <td>140 - 144</td><td>15</td><td style="text-align: center;">142</td><td style="text-align: center;">2130</td><td style="text-align: center;">302460</td><td style="text-align: center;">82</td></tr> <tr> <td>145 - 149</td><td>6</td><td style="text-align: center;">147</td><td style="text-align: center;">882</td><td style="text-align: center;">129654</td><td style="text-align: center;">88</td></tr> <tr> <td>150 - 154</td><td>2</td><td style="text-align: center;">152</td><td style="text-align: center;">304</td><td style="text-align: center;">46208</td><td style="text-align: center;">90</td></tr> <tr> <td></td><td style="text-align: center;">$\Sigma f = 90$</td><td></td><td style="text-align: center;">$\Sigma fx = 12150$ B_1</td><td style="text-align: center;">$\Sigma fx^2 = 1644640$ B_1</td><td></td></tr> </tbody> </table>	Height	Freq	x	fx	fx^2	C.f	120 - 124	5	122	610	74420	5	125 - 129	17	127	2159	274193	22	130 - 134	20	132	2640	348480	42	135 - 139	25	137	3425	469225	67	140 - 144	15	142	2130	302460	82	145 - 149	6	147	882	129654	88	150 - 154	2	152	304	46208	90		$\Sigma f = 90$		$\Sigma fx = 12150$ B_1	$\Sigma fx^2 = 1644640$ B_1		cb
Height	Freq	x	fx	fx^2	C.f																																																			
120 - 124	5	122	610	74420	5																																																			
125 - 129	17	127	2159	274193	22																																																			
130 - 134	20	132	2640	348480	42																																																			
135 - 139	25	137	3425	469225	67																																																			
140 - 144	15	142	2130	302460	82																																																			
145 - 149	6	147	882	129654	88																																																			
150 - 154	2	152	304	46208	90																																																			
	$\Sigma f = 90$		$\Sigma fx = 12150$ B_1	$\Sigma fx^2 = 1644640$ B_1																																																				
	<p>(a) Mean = $\frac{\Sigma fx}{\Sigma f}$ $SD = \sqrt{\frac{1644640 - (135)^2}{90}}$</p> $= \frac{12150}{90} \quad M_1 \quad = 6.9841$ $= 135cm \quad A_1$	M_1																																																						
	<p>(b) On graph paper at the back.</p>	A_1																																																						
	<p>(c) (i) Median = $\frac{50}{100} \times 90$ $= 45$ $= 135cm \quad \pm 0.5$</p>	B_1																																																						
	<p>(ii) 20^{th} percentile = $\frac{20}{100} \times 90$ $= 18$ $= 128.5\text{cm (graph)}$</p>	B_1																																																						
	<p>80^{th} percentile = $\frac{80}{100} \times 90$ $= 72$ $= 141\text{ cm (graph)}$</p>	B_1																																																						
	<p>Range = $141 - 128.5$ $= 12.5\text{cm}$</p>	A_1																																																						
10	<p>(a) $x = \sqrt[4]{N}$ $x^4 - N = 0$ $f(x) = x^4 - N$ \leftarrow $f'(x) = 4x^3$ \leftarrow $f'(x_n) = 4x_n^3$</p>	B_1 B_1																																																						

$$f(x_n) = x_n^4 - N$$

$$x_{n+1} = x_n - \frac{f(x_n)}{f'(x_n)}$$

$$x_{n+1} = x_n - \frac{x_n^4 - N}{4x_n^3}$$

$$= \frac{4x_n^4 - x_n^4 + N}{4x_n^3}$$

$$= \frac{3x_n^4 + N}{4x_n^3}$$

$$= \frac{3x^4}{4x_n^3} + \frac{N}{4x_n^3}$$

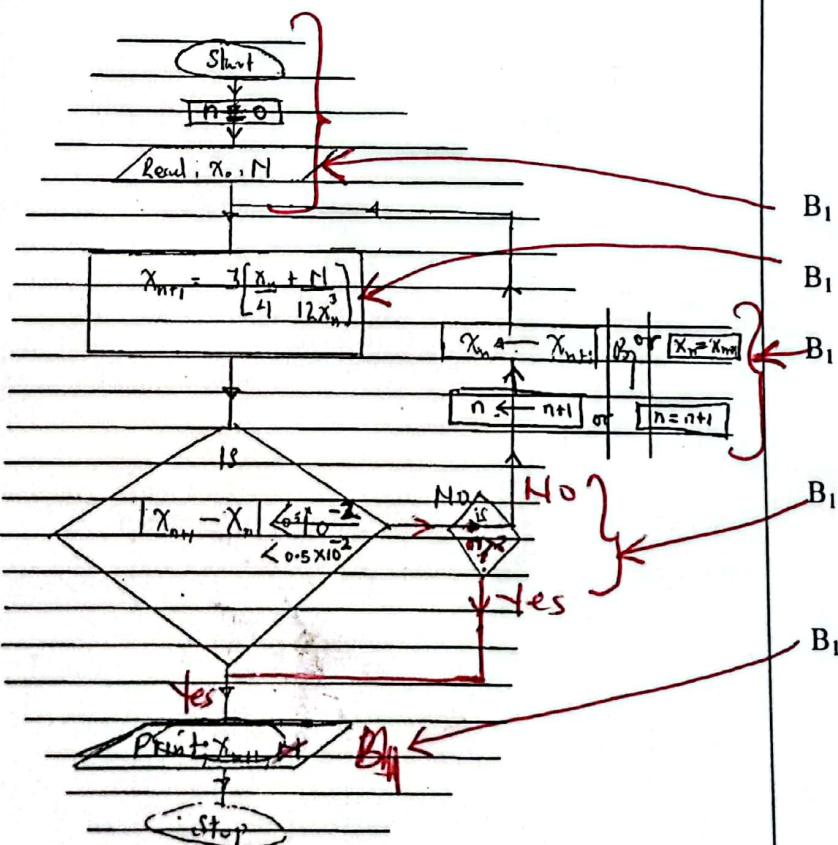
$$= 3 \left[\frac{x_n}{4} + \frac{N}{3.4x_n^3} \right]$$

$$= 3 \left[\frac{x_n}{4} + \frac{N}{12x_n^3} \right] \text{ as required}$$

M₁

B₁

(b) (i) & (ii)



$-2kx + 4k$

(c)

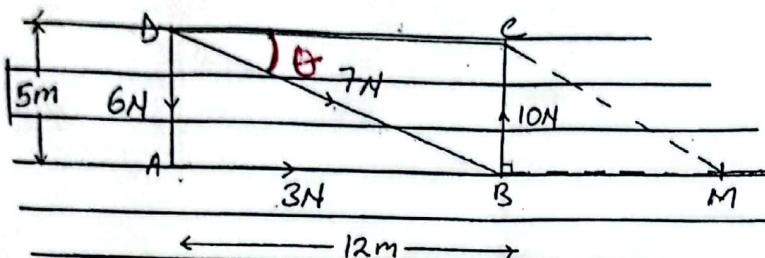
n	x_n	x_{n+1}	$ x_{n+1} - x_n $
0	3	3.1667	0.1667
1	3.1667	3.1544	0.0123
2	3.1544	3.1543	0.0001

$$x = 3.15, N = 99$$

- B₁ → Correct x_n .
- B₁ → Correct $|x_{n+1} - x_n|$
- B₁ → Correct output.

11

(a)



12 marks

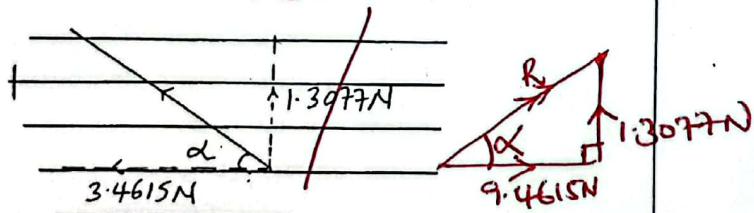
$$R = \begin{pmatrix} 3 \\ 0 \end{pmatrix} + \begin{pmatrix} 0 \\ 10 \end{pmatrix} + \begin{pmatrix} 0 \\ -6 \end{pmatrix} + \begin{pmatrix} 7 \times \frac{12}{13} \\ -7 \times \frac{5}{13} \end{pmatrix}$$

$$= \begin{pmatrix} 9.4615 \\ -3.4615 \end{pmatrix} N$$

$$R^2 = 9.4615^2 + 1.3077^2$$

$$|R| = \sqrt{(-3.4615)^2 + (1.3077)^2}$$

$$= 3.7002N \quad 9.551414$$



$$\alpha = \tan^{-1} \left(\frac{1.3077}{3.4615} \right)$$

$$= 20.6958^\circ$$

The resultant is 3.7002N in the direction N69.30°W

$$\alpha = \tan^{-1} \frac{1.3077}{9.4615}$$

$$\alpha = 7.87^\circ \text{ or } 82.13^\circ E$$

with AB or with the horizontal

Spring direction.

$$(b) A \quad G = 10 \times 12 - \left(7 \times 12 \times \frac{5}{13} \right)$$

$$= 87.6923 \text{ N.m.}$$

$$\begin{vmatrix} x & -3.4615 \\ y & 1.3077 \end{vmatrix} = 87.6923$$

$$\begin{vmatrix} x & 9.4615 \\ y & 1.3077 \end{vmatrix} = 87.6923$$

$$1.3077x - 9.4615y = 87.6923$$

$$\text{When } y = 0, x = \frac{87.6923}{1.3077}$$

$$= 67.0584 \text{ m}$$

B₁ {eqn 3}.

B₁ (Sub y = 0)

Correct value of G with units

$$\begin{aligned} \overline{BM} &= 67.0584 - 12 \\ &= 55.0584 \\ \overline{MC} &= \sqrt{5^2 + 55.0584^2} \\ &= 55.285m \end{aligned}$$

B_1

M₁

A₁

M₁

12

(i) Area, $\frac{1}{2}k\left(2 + \frac{3}{2}\right) = 1$

$$\frac{7}{4}k = 1$$

$$k = \frac{4}{7}$$

(ii) for $0 \leq x \leq \frac{3}{2}$, $f(x) = \frac{4}{7}$

$$\text{for } \frac{3}{2} \leq x \leq 2, \quad \frac{0 - \frac{4}{7}}{2 - \frac{3}{2}} = \frac{y - \frac{4}{7}}{x - \frac{3}{2}}$$

$$\frac{\frac{4}{7}}{\frac{1}{2}} = \frac{y - \frac{4}{7}}{x - \frac{3}{2}}$$

$$y - \frac{4}{7} = \frac{-8}{7}(x - \frac{3}{2})$$

$$y = \frac{-8x}{7} + \frac{16}{7}$$

$$f(x) = \frac{8}{7}(2-x)$$

$$f(x) = \begin{cases} \frac{4}{7}, & 0 \leq x \leq \frac{3}{2} \\ \frac{8}{7}(2-x), & \frac{3}{2} \leq x \leq 2 \\ 0, & \text{otherwise} \end{cases}$$

A₁

B₁

M₁

$\geq 4D$

$\cancel{2} \cancel{x}$

B₁

(iii) $P\left(\frac{1}{2} \leq x \leq \frac{7}{2}\right) = \int_{\frac{1}{2}}^{\frac{3}{2}} \frac{4}{7} dx + \int_{\frac{3}{2}}^{\frac{7}{2}} \frac{8}{7}(2-x) dx$

$$= \left[\frac{4x}{7} \right]_{\frac{1}{2}}^{\frac{3}{2}} + \frac{8}{7} \left[2x - \frac{1}{2}x^2 \right]_{\frac{3}{2}}^{\frac{7}{2}}$$

$$= \frac{4}{7} + \frac{8}{7} \left[\left(\frac{7}{2} - \frac{49}{32} \right) - \left(3 - \frac{9}{8} \right) \right]$$

$$= \frac{4}{7} + \frac{8}{7} \left(\frac{63}{32} - \frac{15}{8} \right)$$

$$= \frac{4}{7} + \frac{3}{28}$$

$$= \frac{19}{28}$$

Correct integral with limits see

M₁ Substn f l m b

A₁

$\geq 4D$

$$\frac{4(-2x+4)}{7} - \frac{8}{7}x + \frac{16}{7}$$

$$\begin{aligned}
 \text{(iv)} \quad E(X) &= \int_0^1 x \cdot \frac{4}{7} dx + \int_1^2 x \cdot \frac{8}{7} (2-x) dx \\
 &= \frac{4}{7} \left(\frac{1}{2} x^2 \right) \Big|_0^1 + \frac{8}{7} \left[x^2 - \frac{1}{3} x^3 \right] \Big|_1^2 \\
 &= \frac{2}{7} \cdot \frac{9}{4} + \frac{8}{7} \left(\frac{4}{3} - \frac{9}{8} \right) \\
 &= \frac{9}{14} + \frac{8}{7} \left(\frac{5}{24} \right) \\
 &= \frac{37}{42}
 \end{aligned}$$

M₁
M_{1'}

Integration
with limits
Substitution
limits

A₁

≥ 20

12 marks

13 (a) $y_1 = x_1 + e_1, y_2 = x_2 + e_2$

$$\begin{aligned}
 ey_1 y_2 &= y_1 y_2 - x_1 x_2 \\
 &= (x_1 + e_1)(x_2 + e_2) - x_1 x_2 \\
 &= x_1 x_2 + x_1 e_2 + x_2 e_1 + e_1 e_2 - x_1 x_2 \\
 &= x_1 e_2 + x_2 e_1 + e_1 e_2
 \end{aligned}$$

As $e_1 e_2$ becomes too small then $e_1 e_2 \approx 0$

$$ey_1 y_2 = x_1 e_2 + x_2 e_1$$

$$\left| \frac{ey_1 y_2}{y_1 y_2} \right| = \left| \frac{x_1 e_2 + x_2 e_1}{x_1 x_2} \right|$$

$$= \left| \frac{e_2}{x_2} + \frac{e_1}{x_1} \right|$$

$$\leq \left| \frac{e_2}{x_2} \right| + \left| \frac{e_1}{x_1} \right|$$

$$\left| \frac{ey_1 y_2}{y_1 y_2}_{\text{Max}} \right| = \left| \frac{e_1}{x_1} \right| + \left| \frac{e_2}{x_2} \right| \text{ as required.}$$

M₁

defn of error.

B₁

assumption

B_{1'}

M_{1'}

R.E

B₁

simplification

B₁'

triangular inequality

A₁

(b) Let $a = 2.675, b = 4.800, c = 15.2$

$$\begin{aligned}
 e_a &= 0.5 \times 10^{-3}, e_b = 0.5 \times 10^{-3}, e_c = 0.5 \times 10^{-1} \\
 d &= 0.92 \quad e_d = 0.5 \times 10^{-2}
 \end{aligned}$$

$$\text{Max} \left(2.675 \left(4.800 - \frac{15.2}{0.92} \right) \right)$$

$$= 2.675 \left[4.8005 - \frac{15.15}{0.925} \right]$$

$$= -30.9766 \quad -30.977$$

$$\text{Min} \left[2.675 \left(4.800 - \frac{15.2}{0.92} \right) \right]$$

$$= 2.6745 \left[4.7995 - \frac{15.25}{0.915} \right]$$

$$= -31.7508 \quad -31.739$$

$$\text{Range} [-31.7508, -30.9766] \quad [-31.739, -30.977]$$

M₁
A₁

M₁
A₁
B₁

4/7 X
2/7 X
C6/7 X

14

$$(a) r(t) = 4 \sin 3t \hat{i} + 8 \cos 3t \hat{j}$$

$$\text{at } t=0, r(0) = 4 \sin 0 \hat{i} + 8 \cos 0 \hat{j}$$

$$v = \frac{d(r(t))}{dt} = 12 \cos 3t \hat{i} - 24 \sin 3t \hat{j}$$

$$\text{at } t=0, v(0) = 12 \cos 0 \hat{i} + 8 \cos 0 \hat{j} - 24 \sin 0 \hat{j}$$

$$= 12 \hat{i} \text{ ms}^{-1}$$

$$a = \frac{dv}{dt} = -36 \sin 3t \hat{i} - 72 \cos 3t \hat{j}$$

but $F = ma$

$$\begin{aligned}\tilde{F} &= 3(-36 \sin 3t \hat{i} - 72 \cos 3t \hat{j}) \\ &= 3(-9)(4 \sin 3t \hat{i} - 8 \cos 3t \hat{j}) \\ &= -27(4 \sin 3t \hat{i} + 8 \cos 3t \hat{j}) \\ &= -27 \hat{x}\end{aligned}$$

B_IM_IM_IA_IB_IM_IM_IA_I

$$(b) \text{ Speed} = 10 \text{ ms}^{-1} \text{ cross section area} = 5 \text{ cm}^2$$

$$h = 4 \text{ m}$$

$$\text{Volume of water} = 10 \times \frac{5}{100^2} \text{ m}^3$$

$$= \frac{50}{100^2} \text{ m}^3$$

Mass of water raised and issued per second.

$$\begin{aligned}&= \frac{50}{100^2} \times 1000 \text{ kg (density)} \\ &= 5 \text{ kg}\end{aligned}$$

B_IB_I

$$\cancel{P}E = mgh$$

$$= 5(9.8)(4)T$$

$$= 196J$$

$$KE = \frac{1}{2}mv^2$$

$$= \frac{1}{2}(s)(10)^2$$

$$= 250J$$

Work done per second by the pump.

$$= PE + KE$$

$$= (96 + 250) J$$

$$= 446J$$

$$= 446W$$

M_IA_I

15

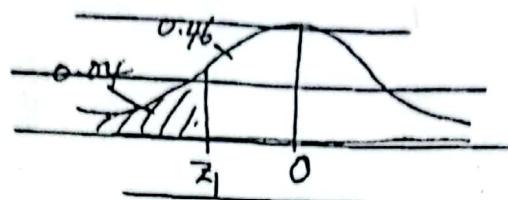
(a) Let x be a r.v for "the marks scored"

$$n = 350$$

$$P(X < 40) = \frac{14}{350}$$

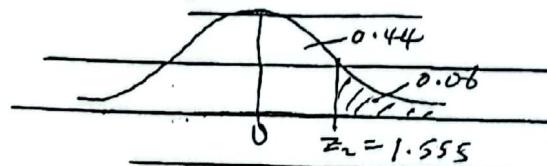
$$P(X > 60) = \frac{21}{350}$$

$$P(X < 40) = P\left(z < \frac{40 - \mu}{\sigma}\right)$$



$$\frac{40 - \mu}{\sigma} = -1.751$$

$$P(X > 60) = P(z <) \frac{60 - \mu}{\sigma}$$



$$\frac{60 - \mu}{\sigma} = 1.555$$

$$\mu - 1.751\sigma = 40$$

$$\begin{array}{l} \mu + 1.555\sigma = 60 \\ -3.30688 = -20 \end{array}$$

$$\sigma = 6.050 \text{ (3dp)}$$

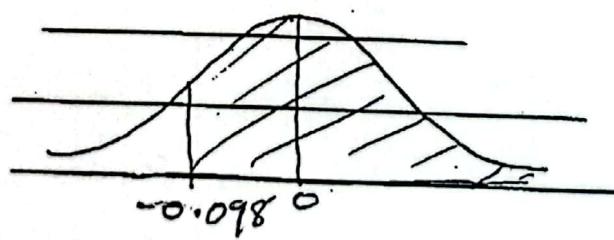
From $\mu = 40 + 1.751\sigma$

$$= 40 + 1.751 (6.050)$$

$$= 50.594 \quad (3dp)$$

$$(b) \quad P(X > 50) = P\left(Z > \frac{50 - 50.594}{6.050}\right)$$

$$= P(Z > -0.098)$$



$$= 0.5 + \phi(0.098)$$

$$= 0.5 + 0.0391 \cancel{+} \cancel{+} \cancel{+} \cancel{+}$$

$$= 0.5391$$

B1

B1

M₁

A₁

M

A₁

$\geq 3D$

≥ 3 D

7,3D

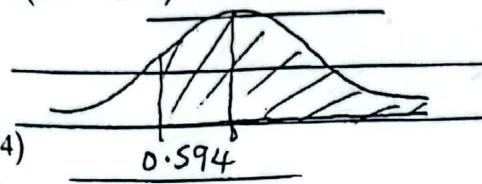
1

1

$$(c) p(X > 47) = P\left(Z > \frac{47 - 50.594}{6.050}\right)$$

$$= P(Z > -0.594)$$

$$\begin{aligned} &= 0.5 + \phi(0.594) \\ &= 0.5 + 0.2238 \\ &= 0.7238 \end{aligned}$$



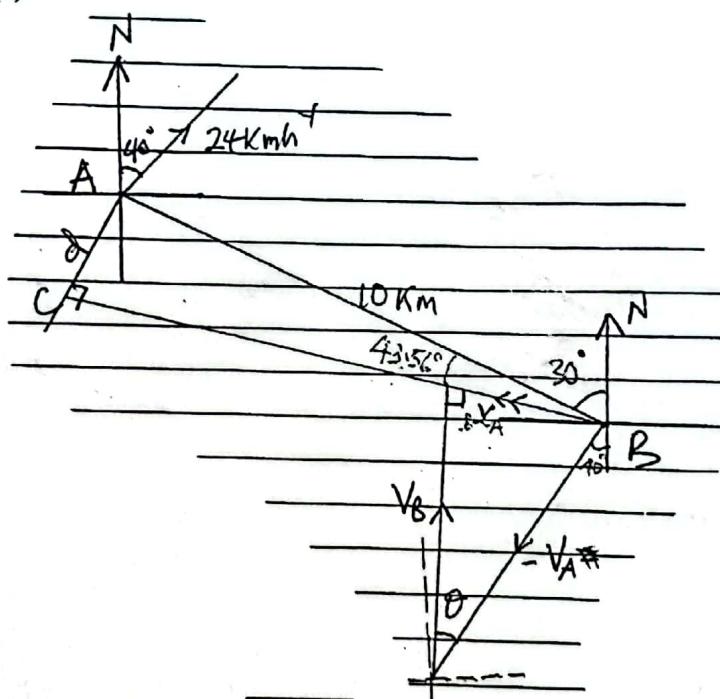
M₁

M₁

A₁

$$\begin{aligned} \text{Number of students} &= 350 (0.7238 - 0.5391) \\ &= 350 (0.1847) \\ &= 64.6 \\ &\approx 65 \text{ students} \end{aligned}$$

16 (a)



B₁

Location of position

B₁

correct vector diagrams

$$\begin{aligned} BVA &= \sqrt{24^2 - 22^2} \\ &= 9.5917 \text{ kmh}^{-1} \end{aligned}$$

$$\cos \theta = \frac{22}{24}, \theta = \cos^{-1}\left(\frac{22}{24}\right), \theta = 23.56^\circ$$

Course is N16.44°E or Bearing is 016.44°

M₁

B₁

M₁B₁

A₁

$$\begin{aligned} (b) d &= 10 \sin 43.56^\circ \\ &= 6.8911 \text{ km} \end{aligned}$$

M₁

A₁

$$\begin{aligned} (c) \text{ Time} &= \frac{BC}{|BVA|} = \frac{10 \cos 43.56^\circ}{9.5917} \\ &= 0.7555 \text{ hrs} \times 60 \\ &= 45 \text{ minutes.} \end{aligned}$$

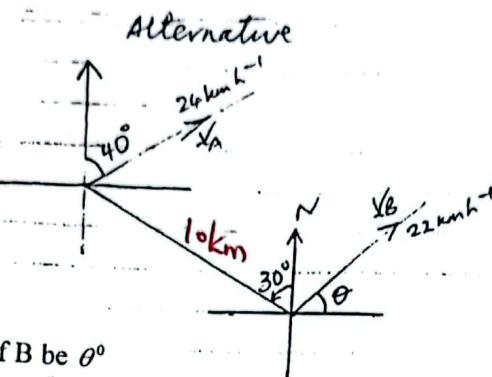
M₁

B₁

A₁

12 marks

(a)

Let the course of B be θ°

$$\underline{V}_B = \begin{pmatrix} 22\cos\theta \\ 22\sin\theta \end{pmatrix}, \underline{V}_A = \begin{pmatrix} 24\cos 50^{\circ} \\ 24\sin 50^{\circ} \end{pmatrix}$$

$$\underline{V}_B = \begin{pmatrix} 22\cos\theta \\ 22\sin\theta \end{pmatrix}, \underline{V}_A = \begin{pmatrix} 24\cos 50^{\circ} \\ 24\sin 50^{\circ} \end{pmatrix}$$

$$= \begin{pmatrix} 22\cos\theta - 15.4269 \\ 22\sin\theta - 18.3851 \end{pmatrix}$$

$$\underline{V}_B \cdot \underline{V}_A = 0 \quad ; \quad \begin{pmatrix} 22\cos\theta \\ 22\sin\theta \end{pmatrix} \cdot \begin{pmatrix} 22\cos\theta - 15.4269 \\ 24\cos\theta - 18.3851 \end{pmatrix} = 0$$

$$\begin{aligned} 339.3918\cos\theta + 404.4722\sin\theta &= 484 \\ 339.3918^2 + 404.4722^2 \cos(\theta - 50^{\circ}) &= 484 \end{aligned}$$

$$\cos(\theta - 50^{\circ}) = \frac{484}{528.0005}$$

$$\theta - 50^{\circ} = 23.56^{\circ}$$

$$\theta = 73.56^{\circ}$$

The course must be on bearing 016.44° or N 16.44° EB₁

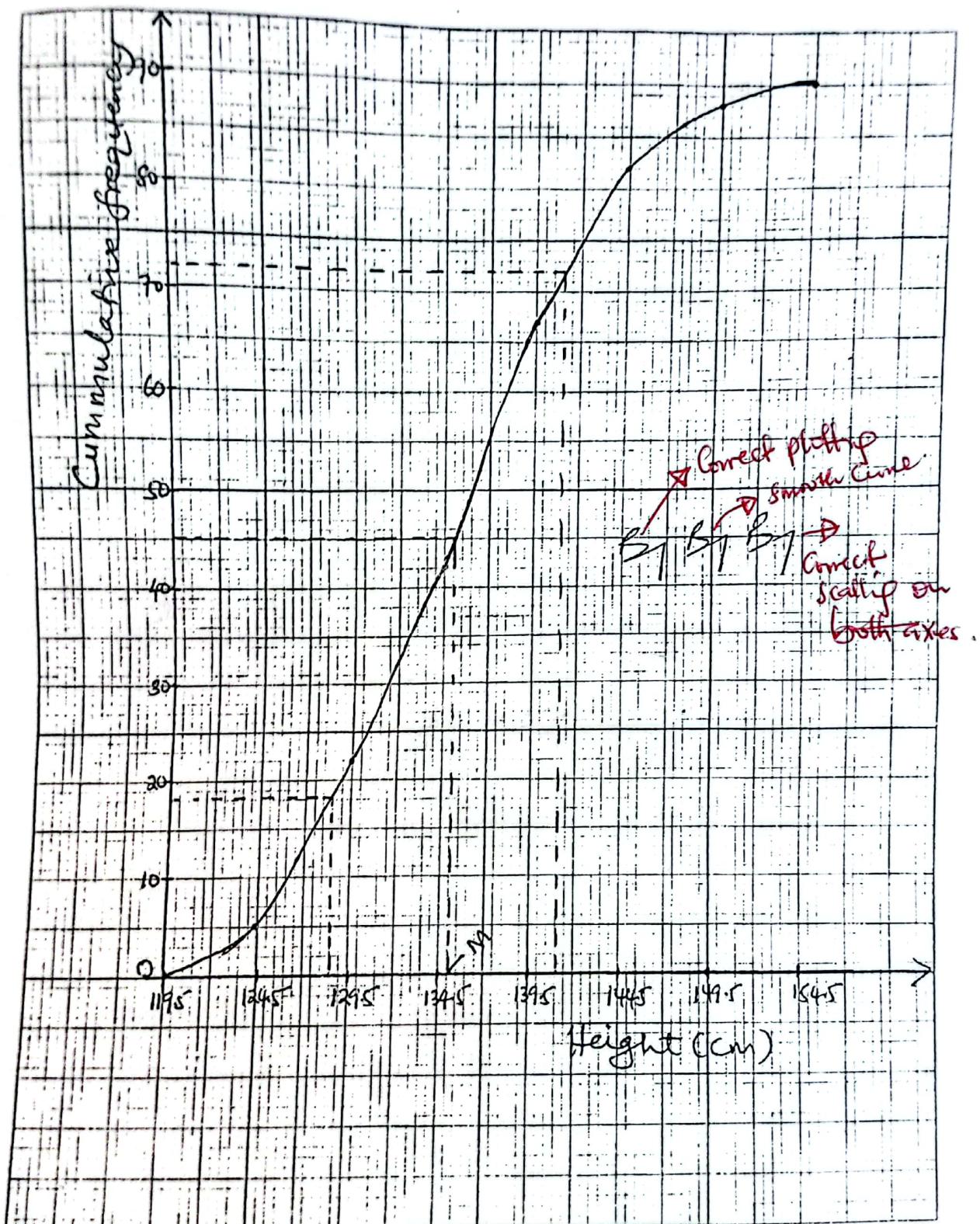
Correct vector diagrams

B₁

for both

B₁M₁M₁B₁A₁

9. (b)



END