

MARKING GUIDE  
PHYSICS PAPER ONE  
P51011 (A-LEVEL)

1 a) (i) Rate of change of Velocity time.

(iii) Let  $V$  be velocity gained after time  $t$ .

$$\text{Acceleration} = \frac{\text{Change in Velocity}}{\text{Time taken}}$$

$$a = \frac{V-U}{t}, u=0 \checkmark$$

$$v = at \quad (\text{ii}) \checkmark$$

$$\text{Distance Covered} = \frac{\text{Average Velocity} \times \text{Time}}{2}$$

$$S = \frac{(U+V)t}{2}$$

$$S = \frac{1}{2}vt \quad (\text{iii}) \checkmark$$

Substituting (ii) in (iii)

$$S = \frac{1}{2} \times at \times t$$

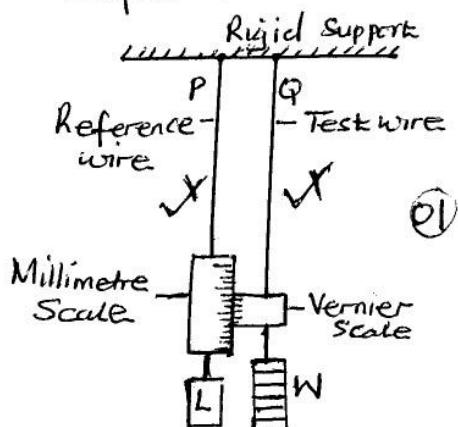
$$S = \frac{1}{2}at^2. \quad (\text{iv}) \checkmark$$

(b) (i) Gradual increase in strain when a material is subjected to a stress for a long time.

Q: When a stretching force is applied to a material for a long time.  
 Give in case if this

(ii) Ability (property) of a material to be pressed / hammered / rolled and forged into useful shapes.

(c)



- Two identical wires p and q suspended from the same rigid support.
- Wire p carries a millimetre scale and a load L is suspended on it to make it taut. (straight and free of kinks) while wire q carries a vernier scale.
- Length l of the test wire q is measured from the rigid support to the vernier and recorded.
- Diameter of the test wire is measured at different points using a micrometer screw gauge, average value d obtained and cross-section area calculated from  $A = \frac{\pi d^2}{4}$  and recorded.
- With no weight suspended on wire q, initial reading  $x_0$  of vernier and scale is read and recorded. (C5)
- A small weight w is then suspended on wire q and new reading x read and recorded and extension e calculated from  $e = x - x_0$  and recorded in metres.
- Weight is removed and the reading taken again to ensure that elastic limit is not exceeded.
- Experiment is repeated for increasing weights W and readings taken both when the wire is loaded and when the weight is removed and values of e recorded.
- A graph of values of W against values of e is plotted.

- Slope  $S$  of the graph is obtained and the ratio of tensile stress to tensile strain (Young's modulus) of the wire is calculated from

$$Y = \frac{SL}{A} \quad | \quad E = \frac{SL}{A}$$

(d) i) - Length of the wire ✓ o1

- Diameter of the wire ✓ o1 (Any two)
- Extension (Any two)
- Weights.

ii) - Two identical wires suspended from same rigid support ✓  
 - Wire must be thin ✓ o1 (Any two)  
 - Wire must be long enough  
 - Wire must be free of kinks

(e)  $d = 0.4\text{cm} = 0.004\text{m}$

$$l = 20\text{cm} = 0.20\text{m}$$

$$\alpha = 4.0 \times 10^{-3}\text{K}^{-1}$$

$$\Delta\theta = 35^\circ\text{C} - 20^\circ\text{C} = 15^\circ\text{C} \equiv (15\text{K})$$

i)  $e = \alpha l \Delta\theta \checkmark$

$$= 4.0 \times 10^{-3} \times 0.20 \times 15 \checkmark \\ = 0.012\text{m.} \checkmark$$

ii) Energy developed in the steel wire =  $\frac{EAE^2}{2L} \checkmark$

$$\text{Volume of the wire} = Al \checkmark$$

$$\text{Energy density} = \frac{\text{Energy developed}}{\text{Volume}}$$

$$= \frac{EAE^2}{2L}/Al$$

$$= \frac{1}{2} E \left(\frac{e}{L}\right)^2 \checkmark$$

$$= \frac{1}{2} \times 1.9 \times 10^{11} \times \left(\frac{0.012}{0.2}\right)^2 \checkmark$$

$$= \frac{1}{2} \times 1.9 \times 10^{11} \times (0.06)^2 \checkmark$$

$$= 3.42 \times 10^8 \text{ J m}^{-3} \checkmark$$

Total = 20marks

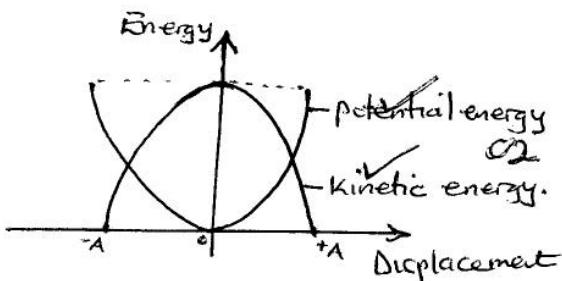
2. a) ii) Periodic motion whose acceleration is directly proportional to the displacement from a fixed point and is directed towards the same point. ✓ o1

(ii) - motion of car engine piston ✓  
 - Car shock absorbers ✓ o1 (Any two)  
 - Operation of pendulum clock ✓  
 - Strings of musical instruments guitars  
 - Diving boards. ✓

b) i) - motion is periodic ✓

- Acceleration is directly proportional to displacement from a fixed point ✓
- Acceleration is directed towards the fixed point. ✓ o2
- Mechanical energy is conserved. ✓

iii)



c) ii) Let  $K_1 = K$ ,  $K_2 = 2K$ .

- If  $K_o$  is the combined force constant, then:

$$\frac{1}{K_o} = \frac{1}{K_1} + \frac{1}{K_2} \checkmark$$

$$\frac{1}{K_o} = \frac{K_1 + K_2}{K_1 K_2}$$

$$K_o = \frac{K_1 K_2}{K_1 + K_2} \checkmark$$

$$= \frac{K \times 2K}{K + 2K}$$

$$= \frac{2K^2}{3K} \checkmark$$

$$K_o = \frac{2K}{3} \checkmark$$

- If applied horizontal force  $F$  on the mass produces a total extension  $x_F$  in both springs, then

$$F \propto x$$

$$F = K_o x$$

$$F = \frac{2K_o}{3} x \checkmark$$

- When the force is removed, (mass released), it executes S.h.m of acceleration  $\text{m s}^{-2}$

$$-F = ma$$

$$-\frac{2K_o}{3} x = ma$$

$$a = -\frac{2K_o}{3M} x \checkmark$$

- Comparing with  $a = -\omega^2 x$

$$\omega^2 = \frac{2K_o}{3M}$$

$$(2\pi f)^2 = \frac{2K_o}{3M} \checkmark$$

$$f^2 = \frac{2K_o}{4\pi^2 \times 3M}$$

$$f = \frac{1}{2\pi} \sqrt{\frac{2K_o}{3M}} \checkmark$$

$$\text{Energy developed} = \frac{1}{2} \times 4 \times 0.09$$

$$= 0.18 \text{ J.} \checkmark$$

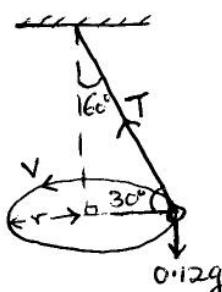
- (d) (i) - centripetal force (Friction force)

produces a moment of force on the boda boda cyclist about the centre of gravity away from the centre of the level circular track then the boda boda cyclist leans through an angle from the vertical towards the centre of the circular track so that the normal reaction provides a moment of force to the cyclist about the centre of gravity towards the centre of the circular track to counterbalance the moment of the centripetal force to keep the cyclist safe during motion and negotiate the circular track safely.

03

$$(ii) T = \frac{\pi}{2} \text{ seconds}$$

angle  $30^\circ$  (to horizontal),  $\theta = 60^\circ$  to the vertical  
 $m = 120g = 0.12 \text{ kg}$



- If  $v$  is speed round the circle, then

$$v^2 = rg \tan \theta$$

$$(rw)^2 = rg \tan \theta$$

$$\left(\frac{rx2\pi}{T}\right)^2 = rg \tan \theta$$

$$\frac{4\pi^2 r^2}{T^2} = g \tan \theta$$

$$\text{Energy developed} = \frac{1}{2} F x c$$

$$F = K_o x$$

$$x = \frac{F}{K_o} = \frac{4v}{400} \checkmark$$

$$= \frac{4 \times 9}{400} \checkmark$$

$$x = 0.09 \text{ m}$$

$$\frac{4\pi^2 r}{T^2} = g \tan \theta$$

$$r = \frac{T^2 g \tan \theta}{4\pi^2}$$

$$= \frac{\left(\frac{\pi}{2}\right)^2 \times 9.81 \times \tan 60^\circ}{4\pi^2}$$

$$= \frac{9.81 \times \tan 60^\circ}{16}$$

$$r = \underline{\underline{1.062 \text{ m.}}} \quad \checkmark \quad \text{c3}$$

Total = 20mks

3(a) (i) Friction force acting per unit cross-section area of a pipe on a liquid when flowing in a region of unit velocity gradient.

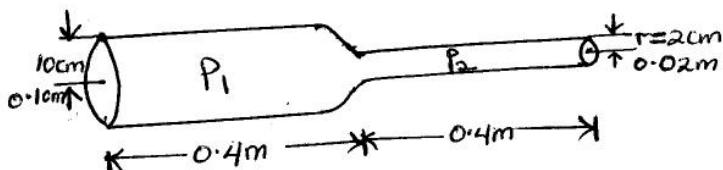
- (i) - radius of the pipe  $\checkmark$  c1
- Coefficient of viscosity of the fluid  $\checkmark$  (Ansatz)
- pressure gradient

b) (i)

<u>steady flow</u>	<u>turbulent flow</u>
<ul style="list-style-type: none"> <li>- All particles of the flowing fluid <u>equidistant</u> from the axis of flow have the same <u>velocity</u> and flow parallel to each other. (same direction)</li> </ul>	<ul style="list-style-type: none"> <li>- All particles of the flowing fluid <u>equidistant</u> from the axis of flow have <u>different velocities</u> and flow in <u>different directions</u>. <math>\checkmark</math> c3</li> </ul>

(ii) Let  $P_1$  = Pressure difference across the wide pipe  $\checkmark$

$P_2$  = pressure difference across the narrow pipe.  $\checkmark$



$$P_1 + P_2 = 5.2 \times 10^3$$

$$P_1 + P_2 = 5200 \quad \checkmark \quad \text{c1}$$

$$\text{Volume flow per second } \frac{V}{t} = \frac{\pi r^4 P}{8 \eta L} \cdot \checkmark$$

But volume flow per second is the same through both pipes.

$$\frac{\pi \times (0.10)^4 \times P_1}{8 \times 9.0 \times 10^{-3} \times 0.4} = \frac{\pi (0.02)^4 \times P_2}{8 \times 9.0 \times 10^{-3} \times 0.4} \quad \checkmark$$

$$(0.10)^4 \times P_1 = (0.02)^4 \times P_2$$

$$0.0001 P_1 = 1.6 \times 10^{-7} P_2$$

$$P_2 = 625 P_1 \quad \checkmark \quad \text{ii}$$

Substituting (ii) in (i)

$$P_1 + 625 P_1 = 5200$$

$$626 P_1 = 5200$$

$$P_1 = 8.307 \text{ Pa.} \quad \checkmark$$

$$P_2 = 625 \times 8.307 \quad \checkmark$$

$$= 5191.875 \text{ Pa.}$$

$$\frac{V}{t} = \frac{\pi \times (0.15)^4 \times 8.307}{8 \times 9.0 \times 10^{-3} \times 0.4} \quad \checkmark$$

$$\frac{V}{t} = 0.091 \text{ m}^3 \text{s}^{-1} \quad \checkmark$$

Density =  $\frac{\text{mass}}{\text{Volume}}$

$$\rho = \frac{m}{V}$$

$$m = \rho V \quad \checkmark$$

$$\frac{m}{t} = \rho \times \frac{V}{t} \quad \checkmark$$

$$= 1000 \times 0.091$$

$$= 91 \text{ kg s}^{-1} \quad \checkmark$$

OF

c) (i) - For streamline flow /  
steady flow / Uniform flow /  
orderly flow of a non-viscous  
incompressible liquid (fluid),  
the sum of pressure at any  
part plus K.E per unit volume  
plus P.E per unit volume is  
always a constant. ✓

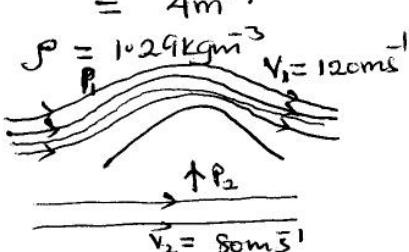
OR For streamline flow,  
 $P + \frac{1}{2} \rho v^2 + \rho gh = \text{constant}$   
 Give in case if a liquid is non-viscous and  
 this is incompressible.

where  $P$  = pressure at any part  
in the pipe of flow  
 $\frac{1}{2} \rho v^2$  = K.E per unit volume  
 $\rho gh$  = P.E per unit volume.

(ii) - Narrow section (part) of a pipe  
where velocity of flow is high. ✓

(iii) - Velocity of flow is inversely proportional to radius of the pipe (Cross-section area of the pipe).  
This closing off part of the tap reduces cross-section area leading to high velocity of flow and low pressure. ✓

$$\begin{aligned} d) A &= 4.0 \times 10^{-4} \text{ cm}^2 \\ &= 4.0 \times 10^{-4} \times 10^{-4} \\ &= 4 \text{ m}^2. \end{aligned}$$



$$P + \frac{1}{2} \rho v^2 = \text{constant} \quad \checkmark$$

$$P_1 + \frac{1}{2} \rho v_1^2 = P_2 + \frac{1}{2} \rho v_2^2$$

$$P_2 - P_1 = \frac{1}{2} \rho (v_1^2 - v_2^2)$$

$$P_2 - P_1 = P \text{ (resultant pressure)}$$

$$\begin{aligned} P &= \frac{1}{2} \times 1.029 (120^2 - 80^2) \\ P &= 5160 \text{ Pa} \quad \checkmark \end{aligned}$$

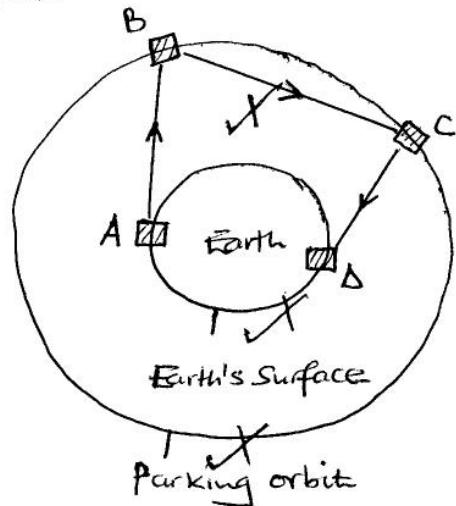
$$\begin{aligned} \text{Force } F &= P \times A \\ &= 5160 \times 4 \quad \text{cm}^2 \\ &= 20640 \text{ N.} \quad \text{Total = 2 units} \end{aligned}$$

4. a) (i) - Space body of small mass moving round a space body of big mass. ✓

(ii) - An orbit where a satellite is observed to be stationary (at rest) from one point on the Earth's surface if its period of rotation round the Earth is equal to that of the Earth round its axis which is 24 hrs.

- (b) - Planets describe ellipses round the Sun as a single focus. ✓  
 - The imaginary line joining the planet to the Sun sweeps out equal areas in equal time intervals. ✓  
 - The squares of the periods of revolution of planets round the Sun are directly proportional to the cubes of their mean separation distance from the Sun. ✓

c) (i)



- Satellite A on the Earth's Surface sends Communication Signals to Satellite B in the parking orbit. Satellite B then sends the signals to satellite C also in the parking orbit and finally C sends the signals to satellite D on the Earth's Surface and Communication is Completed.

$$\text{(ii)} \quad h = 42227 \text{ km} \\ = 42227000 \text{ m.}$$

$$r_e = 6.4 \times 10^6 \text{ m}$$

$$r = r_{\text{Earth}} \\ = 6.4 \times 10^6 + 42227000 \\ = 48627000 \quad \checkmark \\ = 4.8627 \times 10^7 \text{ m.}$$

$$T^2 = \frac{4\pi^2 r^3}{GM} \quad \checkmark$$

$$T^2 = \frac{4\pi^2 \times (4.8627 \times 10^7)^3}{6.67 \times 10^{-11} \times 5.97 \times 10^{24}} \quad \checkmark$$

$$T^2 = 1.14 \times 10^{10} \quad \checkmark$$

$$T = 106769.202863 \text{ seconds}$$

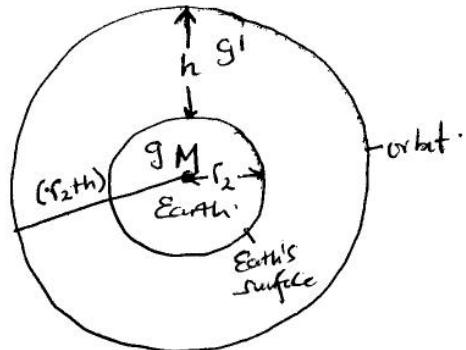
$$= \frac{106769.202863}{3600}$$

$$T = 30 \text{ hours (approx)} \quad \checkmark$$

Comment

- The satellite is not in a parking orbit.

(d)



- On the Earth's Surface, acceleration due to gravity is g

$$GM = gr_e^2 \quad \checkmark \text{ (i)}$$

where M is Mass of the Earth.

- At a height h above the Earth's Surface,  $g' = \frac{1}{9} \times g = \frac{g}{9} \checkmark$

$$GM = g'(r_2 + h)^2$$

$$GM = \frac{g(r_2 + h)^2}{9} \quad \checkmark \text{ (ii)}$$

$$(i) = (ii)$$

$$gr_e^2 = \frac{g(r+h)^2}{9} \quad \checkmark$$

$$gr_e^2 = (r_2 + h)^2$$

$$\sqrt{gr_e^2} = \sqrt{(r_2 + h)^2}$$

$$r_2 = r_2 + h \quad \checkmark$$

$$h = 2r_2 \cdot \checkmark$$

d) - Friction between the surface of the satellite and air molecules forces the satellite to reduce radius of orbit.

Mechanical energy and potential energy of the satellite reduce while its kinetic energy increases. The satellite speeds up leading to heat generation all over its surface and it can eventually burn out if no precautions are taken.

$$\text{Total} = 20 \text{ m/s}$$

5 a) i) A fraction  $\frac{1}{273.16}$  of the triple point of water

(ii) - The value of  $X$  is determined at triple point ( $T_r$ ) and recorded as  $X_{T_r}$

- The value of  $X$  is then determined at unknown but required temperature ( $T$ ) and recorded as  $X_T$

- Kelvin scale is given by

$$T = \frac{X_T}{X_{T_r}} \times 273.16 \text{ K}$$

b) ii) Should vary linearly and continuously with change in temperature

- Should give one reading at particular temperature (Any two)

- Should remain constant at constant temperature.

- Should be accurately measurable for a wide range of temperatures using simple apparatus.

(iii) - The thermometric property is length  $L$  of liquid column in a glass capillary tube

- The thermometer bulb is inserted in an ice-water mixture ( $0^\circ\text{C}$ ) and length of liquid column measured and recorded as  $L_0$ .
- The bulb is then inserted in steam from boiling water ( $100^\circ\text{C}$ ) and length of liquid column measured and recorded as  $L_{100}$ .
- Finally the thermometer bulb is inserted in a substance of unknown but required temperature ( $\theta^\circ\text{C}$ ) and length of liquid column measured and recorded as  $L_\theta$ .
- Since length varies linearly and continuously with change in temperature, then

$$\theta = \frac{L_\theta - L_0}{L_{100} - L_0} \times 100^\circ\text{C} \cdot \text{Ans}$$

$$c) R = R_0 (4 + \beta t^2)$$

$$\text{At } t = 10^\circ\text{C}, R = 40 \Omega$$

$$40 = R_0 (4 + \beta \times 10^2)$$

$$40 = R_0 (4 + 100\beta) \text{ Ans} \quad (i)$$

$$\text{At } t = 25^\circ\text{C}, R = 60 \Omega$$

$$60 = R_0 (4 + \beta \times 25^2)$$

$$60 = R_0 (4 + 625\beta) \text{ Ans} \quad (ii)$$

$$(i) \div (ii)$$

$$\frac{40}{60} = \frac{R_0 (4 + 100\beta)}{R_0 (4 + 625\beta)} \text{ Ans}$$

$$\frac{2}{3} = \frac{4+100\beta}{4+625\beta}$$

$$2(4+625\beta) = 3(4+100\beta)$$

$$8 + 1250\beta = 12 + 300\beta$$

$$1250\beta - 300 = 12 - 8$$

$$950\beta = 4$$

$$\beta = \frac{4}{950} = 4.21 \times 10^{-3} \text{ K}^{-1} (\text{°C})$$

Substituting  $\beta$  in (i)

$$40 = R_0 (4 + 100 \times 4.21 \times 10^{-3})$$

$$40 = 4.421 R_0$$

$$R_0 = 9.05 \Omega$$

$$R = 9.05 (4 + 4.21 \times 10^{-3} t^2)$$

$$\text{At } t = 40^\circ\text{C}$$

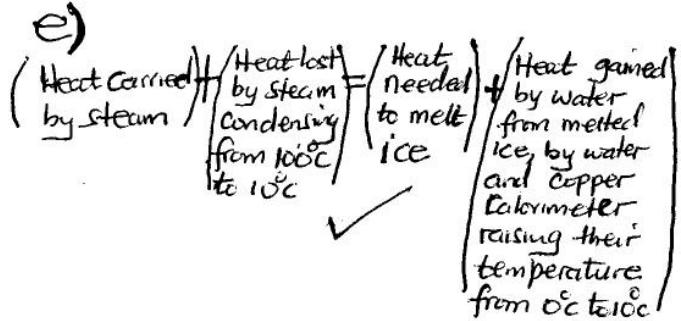
$$R = 9.05 (4 + 4.21 \times 10^{-3} \times 40^2)$$

$$= 97.1608$$

$$= 97.161 \Omega$$

- d) i) - placing a copper calorimeter in an insulator jacket  $\checkmark$   
 - polishing / silvering surface walls of the calorimeter  $\checkmark$  (any two)  
 - placing the copper calorimeter on a wooden block / cotton threads / insulator ring.  
 - Surrounding the calorimeter by a vacuum.

(ii) - According to  $-\frac{dQ}{dt} \propto \frac{A}{V}$ ,  
 the rate of heat loss of a body is inversely proportional to volume of the body. Since mass of the body is directly proportional to volume, rate of heat loss is inversely proportional to mass of the body, hence the smaller the mass the higher the rate of heat loss (rate of cooling) of a body.



$$m_s L_v + m_s C_w (100-10) = m_i L_f + (m_i C_{wt} + m_i C_{cal} + C)(10-0)$$

$$m_s \times 2.3 \times 10^6 + m_s \times 4200 \times 90 = 0.15 \times 3.34 \times 10^5$$

$$(0.15 \times 4200 \times 10.25 \times 4200 + 40)(10)$$

$$2678000 m_s = 50100 + 17200$$

$$2678000 m_s = 67300 \checkmark$$

$$m_s = \frac{67300}{2678000} \checkmark$$

$$= 0.025 \text{ kg.}$$

Total mass of water in the Calorimeter =  $m_s + m_i + m_w$

$$= (0.025 + 0.15 + 0.25) \text{ kg}$$

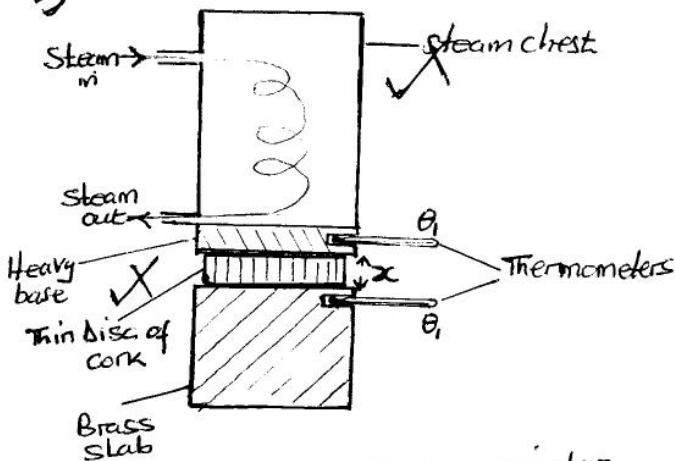
$$= 0.425 \text{ kg} \checkmark$$

$$\text{Total mass} = 20$$

6 a) i) Process of heat transfer through a material solid without movement of a solid as a whole/ or

ii) A solid is made up of molecules which are closely packed together. When heat is supplied to one end of the solid, molecules gain heat energy and vibrate at their mean position with increased amplitudes. During vibration, molecules collide with their adjacent neighbours and lose some of the heat energy setting them also into vibration and also collide with other molecules. The process continues causing heat transfer from the hot end of  $\Theta_2$  the solid to the other.

b)



- Cork is designed into a circular disc of thickness  $\propto$  and area  $A = \frac{\pi d^2}{4}$ ,  $d$  is its diameter.
- The disc is placed on a brass slab of mass  $m$  and specific heat capacity  $c$ .
- The disc is then heated from above using steam passed into the steam chest.

- The apparatus is left to run until the thermometers indicate steady temperatures  $\Theta_2$  and  $\Theta_1$  noted and recorded. ✓
- At steady state, heat flows through the disc at a uniform rate.

$$\frac{dQ}{dt} = KA \left( \frac{\Theta_2 - \Theta_1}{\propto} \right) \quad \text{X (i)}$$

Where,  $K$  is the required thermal conductivity

- The disc is then removed and the brass slab is directly heated by the steam chest until its temperature is slightly above  $\Theta_1$  by about  $10^\circ\text{C}$ .
- The steam chest is removed and the disc is placed back on the brass slab.
- Temperature of the brass slab is recorded in equal time intervals as it loses heat through the disc.
- A graph of values of temperature is plotted against time and the rate of temperature fall  $\frac{\Delta\theta}{\Delta t} = S$  is determined by drawing a tangent on the curve at a temperature  $\Theta_1$ . ✓

- Rate of heat flow through the disc from the brass slab is

$$\frac{dQ}{dt} = mcS \quad \text{ii} \quad \text{X}$$

- Using equations (i) and (ii), thermal conductivity of cork is calculated from

$$K = \frac{mcS}{A(\frac{\Theta_2 - \Theta_1}{\propto})} \quad \text{X} \quad \text{iii}$$

$$c) P = \frac{dQ}{dt} = 100W$$

$$d = 10.0cm = 0.10m$$

$$A = \pi d^2 = \frac{\pi (0.10)^2}{4} \checkmark$$

$$= 7.854 \times 10^{-3} m^2$$

$$x = 2.5cm = 0.025m$$

$$K = 110 \text{ W m}^{-1} \text{ K}^{-1}$$

Let temperature be  $\theta$

$$\frac{dQ}{dt} = KA(\theta - 55) \checkmark$$

$$100 = 110 \times 7.854 \times 10^{-3} \frac{(\theta - 55)}{0.025} \checkmark$$

$$2.5 = 0.86394(\theta - 55)$$

$$2.5 = 0.86394\theta - 47.5 \checkmark$$

$$0.86394\theta = 50.0167$$

$$\theta = \frac{50.0167}{0.86394}$$

$$\theta = 57.89^\circ C \checkmark$$

d) (i) A body which absorbs all heat radiations of different wavelengths incident on it reflects and transmits none.

- (ii) - Sun / stars  
 - Coil of a cooker / Electric heaters  
 - Stoves  
 - Burglar alarms  
 - filament of a lamp /

Incandescent light bulbs

$$e) l = 4cm = 0.04m$$

$$d = 2mm = 0.002m$$

$$r = \frac{d}{2} = \frac{0.002}{2} = 0.001m$$

$$A = 2\pi rl = 2\pi \times 0.001 \times 0.04$$

$$\text{Surface area} = 2.5133 \times 10^{-4} m^2.$$

$$P = 400W$$

Power radiated by a black body

$$= \frac{75}{100} \times 400$$

$$= 300W \checkmark$$

$$300 = A\sigma T^4 \checkmark$$

$$T^4 = \frac{300}{A\sigma}$$

$$T^4 = \frac{300}{2.5133 \times 10^{-4} \times 5.67 \times 10^{-8}}$$

$$T^4 = 2.10520244 \times 10^{13}$$

$$T = 2142.02K \checkmark$$

$$T\lambda_{max} = 2.9 \times 10^{-3}$$

$$\lambda_{max} = \frac{2.9 \times 10^{-3}}{2142.02}$$

$$= 1.354 \times 10^{-6} \checkmark$$

$$= 1.35 \times 10^{-6} m \checkmark$$

$$\text{Total} = 20 \text{ m}$$

7 a) (i) Process of change of state of a gas at constant heat / without heat entering or leaving the system.

- (ii) - Rapid expansion of the gas ✓  
 - Gas in a thick-walled poorly conductive vessel ✓  
 - No exchange of heat between the system and surrounding.  
 - Gas vessel fitted with a heavy piston.

b) State 1

Pressure = $P_0$	<u>Adiabatic Expansion</u>	Pressure = $P$
Volume = $V$		Volume = $2V$
Temperature = $T_1$		Temperature = $T_2$

$$(i) TV^{\gamma-1} = \text{constant} \quad \checkmark$$

$$T_1 V^{\gamma-1} = T_2 (2V)^{\gamma-1} \quad \checkmark$$

$$T_1 V^{\gamma-1} = T_2 \times 2^{\gamma-1} \times V^{\gamma-1}$$

$$\frac{T_1}{T_2} = T_2 \times 2^{\gamma-1} \quad \checkmark$$

$$\frac{T_1}{T_2} = 2^{\gamma-1} \quad \checkmark$$

(iii) Work done during adiabatic expansion from state 1 to

$$\text{state 2} = \frac{1}{\gamma-1} (P_1 V_1 - P_2 V_2) \quad \checkmark$$

$$= \frac{1}{\gamma-1} (P_0 V - P \times 2V)$$

$$= \frac{1}{\gamma-1} (P_0 - 2P) V \quad \checkmark$$

Using  $PV^\gamma = \text{constant}$ ,

$$P_1 V_1^\gamma = P_2 V_2^\gamma \quad \checkmark$$

$$P_0 V^\gamma = P \times (2V)^\gamma$$

$$P_0 V^\gamma = P \times 2^\gamma V^\gamma \quad \checkmark$$

$$P_0 = 2^\gamma P$$

$$P = \frac{P_0}{2^\gamma} \quad \checkmark$$

Substituting for  $P$ :

$$\text{Work done} = \frac{1}{\gamma-1} \left( P_0 - 2 \times \frac{P_0}{2^\gamma} \right) V \quad \checkmark$$

$$\text{Work done} = \frac{P_0 V}{\gamma-1} \left( 1 - \frac{2}{2^\gamma} \right)$$

$$\text{Work done} = \frac{P_0 V}{\gamma-1} \left( 1 - 2^{1-\gamma} \right) \quad \checkmark$$

c) (ii) A gas has molecules at large separation distances and always in continuous random motion. When temperature of the gas is increased (gas heated), molecules gain thermal energy and their random speeds increase. Increase in molecular speed causes increase in their kinetic energies hence a total increase in kinetic energy of the whole gas. 03

- (ii) - Negligible intermolecular forces
- Volume of gas molecules is negligible compared to volume of gas container ✓
- Molecules make perfectly elastic collisions. ✓
- Duration of collision is negligible compared to time between collision of gas molecules. ✓ ~~✓~~

d) i)  $P = \frac{1}{3} S \bar{c}^2$

$$\rho = \frac{M}{V} = \frac{\text{Mass of the gas}}{\text{Volume of the gas}}$$

$$\rho = \frac{Nm}{V}, N = \text{Number of Molecules.}$$

m = mass of a molecule.

$$P = \frac{Nm\bar{c}}{3V}$$

$$3PV = Nm\bar{c}^2$$

$$\frac{1}{2} \times 3PV = \frac{1}{2} \times Nm\bar{c}^2$$

$$\frac{3}{2} PV = N \left( \frac{1}{2} m\bar{c}^2 \right)$$

$$K.E_{\text{molecule}} = \frac{1}{2} m\bar{c}^2 = \frac{3}{2} K_B T \quad \checkmark$$

$K_B = \frac{R}{N_A}$  is Boltzmann Constant

$$\frac{3}{2} PV = N \times \frac{3}{2} K_B T$$

$$PV = N K_B T \quad \checkmark$$

- For a gas of pressure  $P_1$ , Volume  $V_1$  having  $N_1$  molecules at a temperature  $T_1$ ,

$$P_1 V_1 = N_1 K_B T_1 \quad \checkmark$$

- For another gas of pressure  $P_2$ , Volume  $V_2$  having  $N_2$  molecules at a temperature  $T_2$ ,

$$P_2 V_2 = N_2 K_B T_2 \quad \checkmark$$

- But according to Avogadro's hypothesis,

$$P_1 = P_2 = P, V_1 = V_2 = V \text{ and } T_1 = T_2 = T$$

$$PV = N_1 K_B T \quad \checkmark^{(i)}$$

$$PV = N_2 K_B T \quad \checkmark^{(ii)}$$

$$(i) = (ii)$$

$$N_1 K_B T = N_2 K_B T$$

$$\underline{N_1 = N_2. \quad \checkmark} \quad \checkmark$$

(ii)  $m = 40g = 4.0 \times 10^{-2} kg$

$$V = 2 \times 10^{-3} m^3$$

$$\rho = \frac{m}{V} = \frac{4.0 \times 10^{-2}}{2 \times 10^{-3}} \quad \checkmark$$

$$= 20 \text{ kg m}^{-3}$$

$$T = 0^\circ C = 273K$$

$$PV = RT$$

$$P = \frac{RT}{V} = \frac{8.31 \times 273}{2 \times 10^{-3}} \quad \checkmark$$

$$= 1134315 Pa$$

$$P = \frac{1}{3} S \bar{c}^2 \quad \checkmark$$

$$\bar{c} = \frac{3P}{S} = \frac{3 \times 1134315}{20} = 170147.25 \quad \checkmark$$

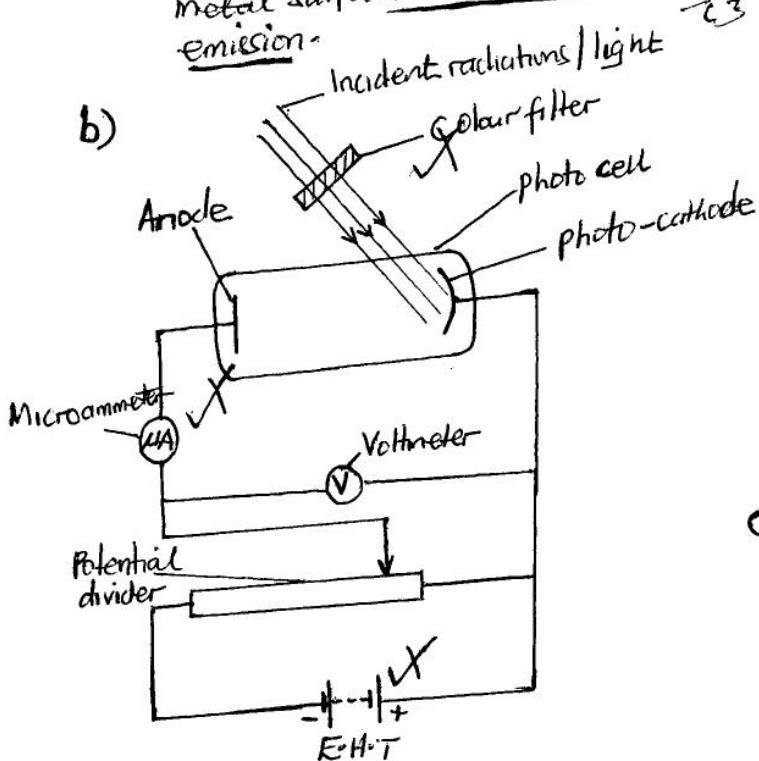
$$\text{Root mean square speed} = \sqrt{\bar{c}} = \sqrt{170147.25} \quad \checkmark$$

$$= 412.49 \text{ ms}^{-1} \quad \checkmark$$

$$\overline{T_{\text{eff}}} = 20 \text{ m/s} \quad \checkmark$$

8 a) (i) Process by which electrons are emitted from a metal plate when light/radiation of high/ enough energy is incident on it/ falls on it.

(ii) Electrons exist in the metal surface together with positive ions under attraction. When light (radiation) of high enough energy falls on the metal surface, electrons break away from the attraction of positive ions, become free and mobile. Kinetic energy of the electrons in the metal surface increases and those with maximum kinetic energy escape from the metal surface hence photo electric emission.



- The anode is made negative with respect to the cathode.

- Incident radiations are passed through a colour filter so that radiations of known frequency  $f$  fall on the photo-cathode.
- The cathode emits photo electrons which are received by the anode and the microammeter gives a deflection.
- The potential divider is varied until the microammeter shows zero deflection and the Voltmeter reading  $V_s$  is read and recorded.
- The experiment is repeated using different colour filters so that radiations of different frequencies  $f$  are directed to fall on the photo-cathode and corresponding values of  $V_s$  recorded at zero microammeter deflection.
- A graph of values of  $V_s$  is plotted against values of  $f$  and the intercept  $f_0$  on the horizontal axis ( $f$ -axis) read and recorded as the threshold frequency of the photo cathode.

$$c) \lambda = 4.5 \times 10^{-5} \text{ cm} = 4.5 \times 10^{-7} \text{ m}$$

$$P = 20 \text{ mW} = 0.02 \text{ W}$$

$$P = nE = \frac{nhc}{\lambda}$$

$$n = \frac{P\lambda}{hc}$$

$$n = \frac{0.02 \times 4.5 \times 10^7}{6.6 \times 10^{-34} \times 3.0 \times 10^8} \times$$

$$n = 4.55 \times 10^{16} \text{ emitted photo-electrons.}$$

Number of photo-electrons causing current ( $n'$ )

$$= \frac{60}{100} \times 4.55 \times 10^{16}$$

$$n' = 2.73 \times 10^{16} \text{ photo-electrons.}$$

$$n'e = It$$

$$I = \frac{n'e}{t} = \frac{2.73 \times 10^{16} \times 1.6 \times 10^{-19}}{1}$$

$$\underline{I = 4.37 \times 10^{-3} A}$$

d) Accelerating potential energy / work done by the accelerating potential, = Kinetic energy of the electron.

$$eV = \frac{1}{2}mv^2 \quad \text{(i)}$$

where  $V$  is velocity of the electron.

- In the magnetic field, the magnetic force on the electron gives the electron a centripetal force.

$$Bev = \frac{mv^2}{r}$$

$$v = \frac{Ber}{m} \quad \text{(ii)}$$

- Substituting (ii) in (i)

$$eV = \frac{1}{2}m \left( \frac{Ber}{m} \right)^2$$

$$2eV = \frac{B^2 e^2 r^2}{m^2}$$

$$2V = \frac{B^2 e r^2}{m}$$

$$\underline{\frac{e}{m} = \frac{2V}{B^2 r^2}}$$

e)  $\rho = 900 \text{ kg m}^{-3}$

$$r = 1.2 \times 10^{-6} \text{ m}$$

$$V = 150 \text{ V}$$

$$d = 1.5 \text{ cm} = 0.015 \text{ m.}$$

Electric force on the oil drop = Weight of the oil drop.

$$F_Q = mg \quad \checkmark$$

$$\frac{VQ}{d} = \frac{4\pi r^3 \rho g}{3}$$

$$\frac{Vne}{d} = \frac{4\pi r^3 \rho g}{3}$$

$$\underline{n = \frac{4\pi r^3 \rho g d}{3Ve}}$$

$$\underline{n = \frac{4\pi (1.2 \times 10^{-6})^3 \times 900 \times 4.8 \times 10^{-15}}{3 \times 150 \times 1.6 \times 10^{-19}}}$$

$$\underline{n = 40 \text{ electrons.}}$$

$$\text{Total = 20 mks}$$

Q a) (ii) Energy carried by an electron on an orbit round the nucleus of an atom. ✓ 01

(iii) When a radiation is passed through a gas, atoms of the gas gain energy from the radiation. Electrons in the lower energy levels of the atom gain energy and move from lower energy levels to higher energy levels making the atom excited and unstable.

Other electrons on higher energy levels then make a transition to occupy the vacant spaces left in the lower energy levels. During transition, electrons emit radiation which form an emission spectra. ✓ 03

b) (ii)  $E_n = \frac{-K}{n^2} = \frac{-me^4}{8\varepsilon_0^2 n^2 h^2}$

$$\bar{E}_{n_2} = \frac{-me^4}{8\varepsilon_0^2 n_2^2 h^2} \quad \checkmark$$

$$\bar{E}_{n_1} = \frac{-me^4}{8\varepsilon_0^2 n_1^2 h^2} \quad \checkmark$$

- A transition from  $n_2$  to  $n_1$  cause emission of radiations of energy given by:

$$\bar{E}_{n_2} - \bar{E}_{n_1} = hf \quad \checkmark$$

$$\frac{-me^4}{8\varepsilon_0^2 n_2^2 h^2} - \frac{-me^4}{8\varepsilon_0^2 n_1^2 h^2} = hf$$

$$hf = \frac{me^4}{8\varepsilon_0^2 n_1^2 h^2} - \frac{me^4}{8\varepsilon_0^2 n_2^2 h^2} \quad \times$$

$$hf = \frac{me^4}{8\varepsilon_0^2 h^2} \left( \frac{1}{n_1^2} - \frac{1}{n_2^2} \right) \quad \times$$

$$f = \frac{me^4 (n_2^2 - n_1^2)}{8\varepsilon_0^2 n_1^2 n_2^2 h^3} \quad \checkmark \quad 03$$

(iii)  $E_n = \frac{-20}{n^2} \text{ eV}$

$$E_5 = \frac{-20 \text{ eV}}{5^2} = -0.8 \text{ eV} \\ = -1.28 \times 10^{-19} \text{ J} \quad \times$$

$$E_2 = \frac{-20 \text{ eV}}{2^2} = -5.0 \text{ eV} \\ = -8.0 \times 10^{-19} \text{ J} \quad \times$$

$$E_5 - E_2 = \frac{hc}{\lambda} \quad \checkmark$$

$$-1.28 \times 10^{-19} - 8.0 \times 10^{-19} = \frac{6.6 \times 10^{-34} \times 3 \times 10^8}{\lambda} \quad \times$$

$$\lambda = \frac{1.98 \times 10^{-25}}{6.72 \times 10^{-19}} \quad \checkmark$$

$$\lambda = 2.95 \times 10^{-7} \text{ m.} \quad \checkmark$$

i) Ultra-violet radiations. ✓ 04

c) i) - Most alpha particles pass through the atom undeviated. This is because the biggest percentage of the atom is free space.

- Few alpha particles are deviated through small angles less than 90° (acute angles). This is due to force of repulsion between the nucleus and the positively charged alpha particles.
- Very few alpha particles are deviated through angles greater than 90° (obtuse angles). These tend to move so as to have a head-on collision with the tiny nucleus at the centre of the atom.

#### Conclusion:

An atom consists of a central nucleus where the positive charge and almost all the mass of the atom is concentrated.

- ii) Alpha particles have a short range in air so a vacuum is required to enable them move close to the nucleus of the atom with less of interference from air molecules.

d)

$$\text{Energy of alpha particle} = \text{Kinetic energy} = 4.2 \times 10^6 \times 1.6 \times 10^{-19}$$

$$\frac{1}{2}mv^2 = 4.2 \times 1.6 \times 10^{-13} \quad \checkmark$$

$$mv^2 = 2 \times 4.2 \times 1.6 \times 10^{-13}$$

$$mv^2 = 1.344 \times 10^{-13} \quad \checkmark$$

$$b_0 = 5.4 \times 10^{-12} \text{ cm} \\ = 5.4 \times 10^{-14} \text{ m.}$$

$$\frac{1}{4\pi\epsilon_0} = 9.0 \times 10^9$$

$$\frac{1}{\pi\epsilon_0} = 3.6 \times 10^9$$

$$\frac{1}{\pi\epsilon_0} = \frac{1}{3.6 \times 10^{10}} = 2.778 \times 10^{-11} \quad \checkmark$$

$$b_0 = \frac{Ze^2}{\pi\epsilon_0 mv^2}$$

$$Z = \frac{\pi\epsilon_0 mv^2 b_0}{e^2} \quad \checkmark$$

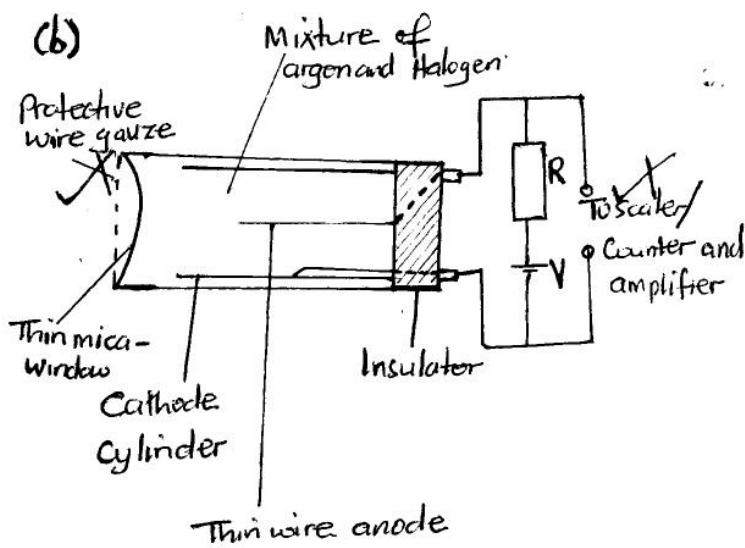
$$Z = \frac{2.778 \times 10^{-11} \times 1.344 \times 10^{-13} \times 5.4 \times 10^{-14}}{(1.6 \times 10^{-19})^2} \quad \checkmark$$

$$Z = 78.756 \quad \checkmark$$

$$Z = 79 \quad \checkmark \text{ (Approx.)} \quad \checkmark$$

$$\text{Total} = 20 \text{ m.s.}$$

- 10(a) i) Number of protons in the nucleus of an atom. ✓  
 ii) Fraction of the number of radioactive atoms of a material disintegrating per second. ✓  
 01



the thin wire anode, collide with air (gas) molecules, ionise them leading to formation of more ion pairs inside the tube.

← The concentration of ions (charges) on their respective electrodes ~~results into a pulse~~ ionisation current which flows through a high resistor R and sets up a p.d across it.

← The p.d set up across R is amplified and sent to a Scaler/Counter which registers the passage of ionising radiations inside the GM-tube. → 05

c) Total energy of  $\alpha$ -plex = 5 MeV

$$= 5 \times 10^6 \text{ eV}$$

$$= 5.0 \times 10^6 \text{ eV}$$

Energy required to form one ion-pair = 50 eV

Number of ion pairs formed  
 $= \frac{5.0 \times 10^6 \text{ eV}}{50 \text{ eV}}$

$$= 1.0 \times 10^5 \text{ ion pairs/ionisations}$$

Number of ionisations per mm in a range of 20mm

$$= \frac{1.0 \times 10^5 \text{ ionisations}}{20 \text{ mm}}$$

$$= 5.0 \times 10^3 \text{ ionisations per mm.}$$

d) (i) Original mass  $M_0 = 1g$ .

- At time  $t = T_{\frac{1}{2}}$  (Half life),

$$\text{Mass present } M = \frac{M_0}{2} \\ = \frac{1g}{2} \checkmark$$

- Using the decay law equation:

$$M = M_0 e^{-\lambda t} \checkmark$$

$$\frac{1}{2} g = 1g e^{-\lambda T_{\frac{1}{2}}} \checkmark$$

$$\frac{1}{2} = e^{-\lambda T_{\frac{1}{2}}}$$

$$\ln 2^{-1} = \ln e^{-\lambda T_{\frac{1}{2}}} \checkmark$$

$$-\ln 2 = -\lambda T_{\frac{1}{2}}, \ln e = 1$$

$$\ln 2 = \lambda T_{\frac{1}{2}}$$

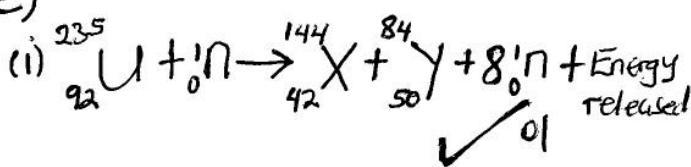
$$T_{\frac{1}{2}} = \frac{\ln 2}{\lambda} \checkmark \quad 03$$

$$\underline{T_{\frac{1}{2}} = \frac{0.693}{\lambda}}$$

(ii) - Nature of the radioactive sample.  $\checkmark$

- Number of radioactive atoms present in the sample.

e)



(ii) Total mass on left hand side

$$= 233.132\text{u} + 1.009\text{u}$$

$$= 234.141\text{u.} \checkmark$$

Total mass on the right hand side

$$= 144.212\text{u} + 81.413\text{u} + 8(1.009\text{u})$$

$$= 233.697\text{u} \checkmark$$

Mass defect ( $\Delta m$ ):

$$\Delta m = 234.141\text{u} - 233.697\text{u}$$

$$= 0.444\text{u} \checkmark$$

Energy of a photon released

$$= 0.444 \times 931 \text{ Mev}$$

$$= 413.364 \text{ Mev} \checkmark$$

$235\text{g} \xrightarrow{\text{Release}} 6.02 \times 10^{23}$  photons of energy

$1\text{g} \xrightarrow{\text{Release}} \frac{6.02 \times 10^{23}}{235}$  photons

$50\text{g} \xrightarrow{\text{Release}} \frac{6.02 \times 10^{23} \times 50}{235}$  photons

$$= 1.28 \times 10^{23} \text{ photons} \checkmark$$

Total energy released by  $50\text{g}$  of U-235

$$= 1.28 \times 10^{23} \times 413.364 \text{ Mev} \checkmark$$

$$= 5.291 \times 10^{25} \text{ Mev} \checkmark$$

-END-