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Magnetism (A-level) notes

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Magnetism

It refers to physical phenomena arising from the force caused by magnets, objects that produce fields that attract or repel other objects.

Magnetism is used by Electrical and Electronic Engineers to make components such as relays, solenoids, inductors, chokes, coils, loudspeakers, motors, generators, transformers, and electricity meters etc.

Magnetic field

This is a region of space around a magnet or a moving electric charge within which a force of magnetism acts.

In a magnetic field:

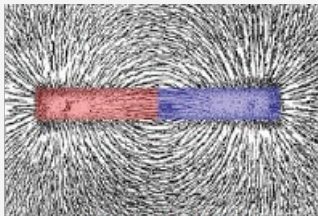
A magnetic force can be experienced

A moving charge experiences a magnetic force

A current-carrying conductor experiences a force

An e.m.f is induced in a moving conductor.

The figure below shows Iron filings attracted to a bar magnet to show the magnetic field.



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- **Magnetic Flux**

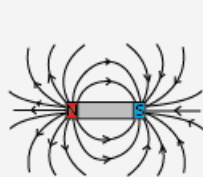
All magnets, no matter what their shape, have two regions called magnetic poles; North and South.

- The north of a compass magnet is the end that points towards the Earth's north.
- Like poles repel, unlike poles attract
- Magnetic fields are lines of force drawn from the North to the South of a magnet. The closer the field lines, the stronger the magnetic fields.
- The direction of magnetic field B , at any location is given by the direction of North Pole of the compass needle
- Magnetic field B is measured in N/Am or Tesla, T

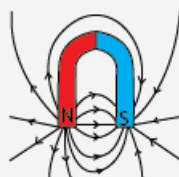
Drawings of magnetic field patterns are shown below

Magnetic field lines for a bar and horse shoe magnet

Magnetic field patterns around a bar and horse shoe magnets



Bar magnet

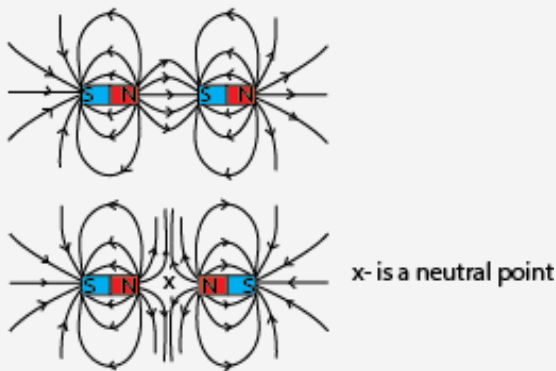


Horse shoe magnet

- Lines of force leave the North-Pole and enter the South Pole.
- An arrow should be drawn to show the direction of field lines

- Lines of force do not cross each other
- Magnetic field is strongest at the poles

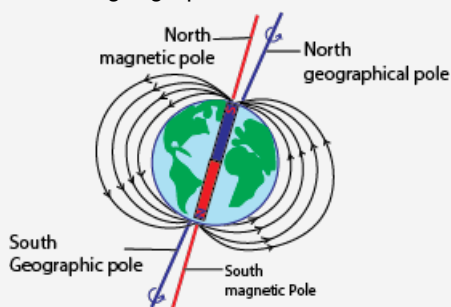
Magnetic field lines for two nearby magnets



Note that a line of the field will pass in opposite directions if like poles are nearby. A neutral point will be between them. A neutral point is a place around a magnet where a magnetic needle experiences zero magnetic force.

Earth's magnetic field

The earth's magnetic field lines are made up of parallel lines running from geographical south to geographical north.



The study of the earth's magnetic field involves:

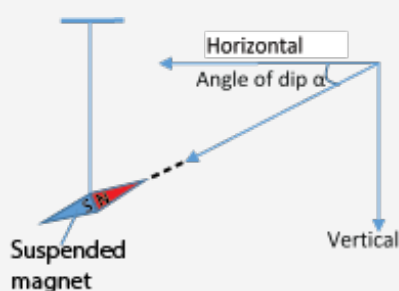
- Two imaginary lines called **magnetic meridian** and **geographical meridian**
- Two angles called angles of **dip** and **angle of declination**

Definitions

Magnetic meridian: This is the vertical plane containing the magnetic axis.

Geographic meridian: this is the vertical plane passing through the axis of rotation of the earth.

Angle of dip (inclination) α , is the angle that the axis of a freely suspended bar magnet makes with the horizontal when the magnet settles.



Angle of declination (magnetic variance)

This is the angle between the earth's magnetic and geographical meridians.

Or

the angle between magnetic north and true north.

Magnetic axis: This is the imaginary line passing through the earth's magnetic North and South Pole.

Geographical axis: This is the imaginary line through the center of the earth and passing through the geographic North and south.

Variation of Angle of dip, α , as one moves from the magnetic equator up to the North Pole

Generally the angle of dip varies from 0° at the magnetic equator to 90° at the North Pole.

Definitions

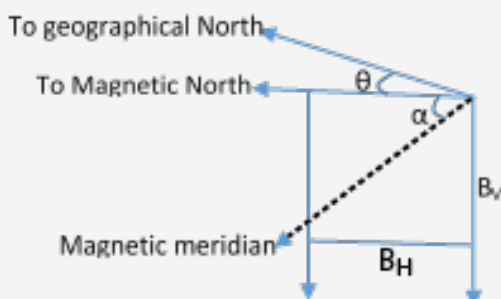
Magnetic Equator: This is the greatest circle in a horizontal plane perpendicular to the magnetic meridian where a freely suspended bar magnet experiences zero magnetic dip.

Explanation

At the magnetic equator, the earth's magnetic field lines are parallel to the horizontal. Therefore the angle of dip at the equator is zero, ($\alpha = 0$)

At the North Pole, the magnetic field lines are normal to the earth's surface, thus they are perpendicular to the horizontal. Therefore the angle of dip at the North Pole = 90° or $\alpha = 90^\circ$.

Illustration of the relationship of geographical north, magnetic north, angle of dip and angle of declination



α = angle of dip

θ = angle of declination

B_H = horizontal component of the earth's magnetic field

B_V = vertical component of magnetic field

B = resultant magnetic flux density

$$B_H = B \cos \alpha \dots\dots\dots (i)$$

$$B_V = B \sin \alpha \dots\dots\dots (ii)$$

$$\begin{aligned} B_H^2 + B_V^2 &= B^2 \cos^2 \alpha + B^2 \sin^2 \alpha \\ &= B^2 (\cos^2 \alpha + \sin^2 \alpha) \\ &= B^2 \end{aligned}$$

$$\therefore \text{The resultant magnetic field } B = \sqrt{(B_H^2 + B_V^2)}$$

Eqn. (i) and eqn. (ii)

$$\frac{B_V}{B_H} = \frac{B \sin \alpha}{B \cos \alpha}$$

$$\tan \alpha = \frac{B_V}{B_H}$$

$$\therefore \text{Angle of dip, } \alpha = \tan^{-1} \left[\frac{B_V}{B_H} \right]$$

Magnetic field patterns due to current carrying conductors

When a straight wire or conductor is carrying a steady or direct current, a magnetic field is created or generated around it.

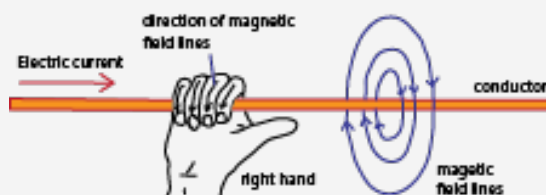
For a straight conductor, the magnetic field pattern is uniform with concentric circles around it.

The direction of magnetic field is determined by Right hand grip rule

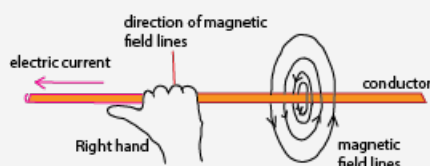
Right hand grip rule

Imagine gripping the conductor with the thumb straight in the direction of flow of current, with the finger curled around it, the direction in which the fingers gives the direction of magnetic field around the conductor, i.e.,

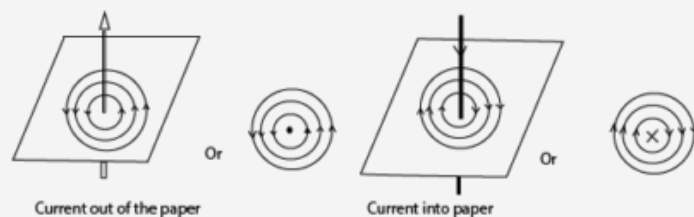
(i) Using right hand rule the magnetic field pattern for a conductor carrying current from left to the right can be predicted as follows



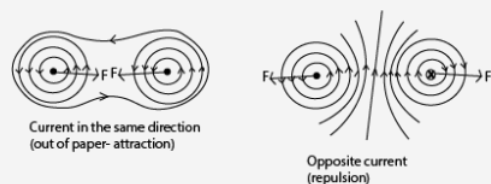
(ii) Using right hand rule the magnetic field pattern for a conductor carrying current from right to the left can be predicted as follows



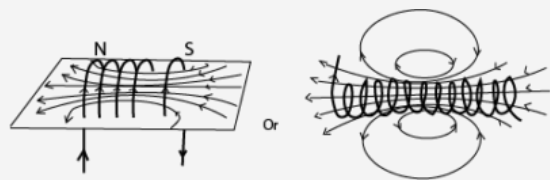
Magnetic field patterns for straight wires carrying a current perpendicularly out of or into the plane of paper as shown in fig (a) and (b) respectively below



Magnetic field pattern due to two nearby current carrying conductors having current flowing in same and opposite direction are shown below



Magnetic field pattern due solenoid carrying a current

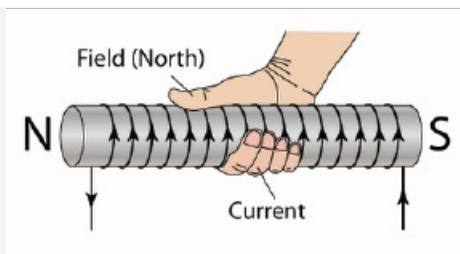


- Solenoid consists of a length of insulated wire coiled into a cylinder shape.
- Current in solenoid produces a stronger magnetic field inside the solenoid than outside. The field lines in this region are parallel and closely spaced showing the field is highly uniform in strength and direction.
- Field lines outside the solenoid are similar to that of a bar magnet, and it behaves in a similar way – as if it had a north pole at one end and South Pole at the other end.
- Strength of the field diminishes with distance from the solenoid.
- Reversing the direction of the current reverses the direction of the magnetic field.

Strength of the magnetic field can be increased by:

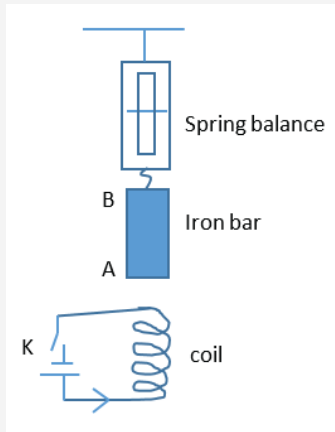
- increasing the current in the coil
- increasing the number of coils in the solenoid; and
- using a soft iron core within the solenoid.

Right-hand rule can be used to find the direction of the magnetic field. In this case, point the wrapped fingers (along the coil) in the direction of the conventional current. Then, the thumb will point to the direction of magnetic field within the solenoid.



Example 1

The diagram shows a piece of soft iron bar suspended freely on a spring balance. One end of the bar is close to the end of the coil connected to a source of e.m.f via switch K.



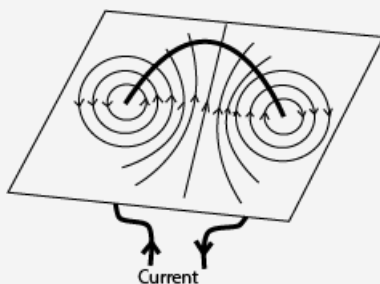
When switch K is closed, the spring balance reads 50B. State the polarity of AB and explain your observation

Solution

The upper end of the coil is a North Pole when K is closed.

Increase in spring balance reading shows that the iron bar is attracted. Thus A is a south pole while B is the North Pole.

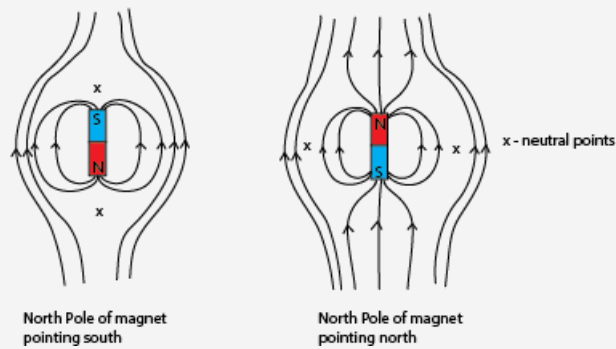
Magnetic field pattern due to coil



Magnetic field due to a bar magnet placed in the earth's local magnetic field

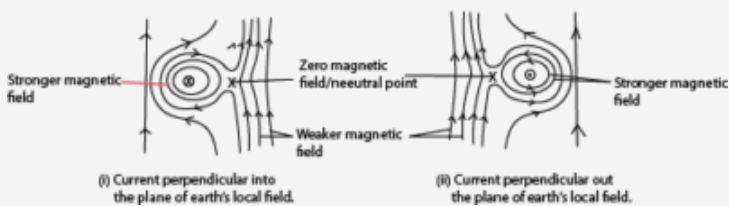
- (i) North Pole of the magnet facing down (geographical south)
- (ii) North of the magnet facing Up (geographical North)

Magnets in earth's magnetic field



Magnetic field pattern of a straight wire carrying a current perpendicular (across) the earth's local magnetic field

A straight wire carrying a current perpendicular (across) the earth's local magnetic field



Neutral point

This is a region of space where two magnetic fields of equal magnitude and opposite direction cancel out. A magnetic dipole (compass needle) experiences zero magnetic force at this point.

Magnetic flux density, **B** (magnetic induction)

This is the force acting perpendicularly on a conductor of length one meter carrying a current of one ampere in a direction normal to the field.

The S.I unit of B is tesla (T)

A tesla is the magnetic flux density in which a straight conductor of length 1m placed across the field and carrying a current of one ampere experiences a magnetic force of one Newton (1N)

$$1\text{T} = \frac{1\text{N}}{1\text{A} \times 1\text{m}}$$

Magnetic flux, Φ (phi)

Magnetic flux is defined as the number of magnetic field lines passing through a given closed surface.

It provides the measurement of the total magnetic field that passes through a given surface area.

The strength of the field around a magnet depends on how close you get.

Magnetic flux is a product of magnitude of magnetic flux density and area of projection normal to magnetic field lines

$$\text{i.e. } \phi = B \times A = BA$$

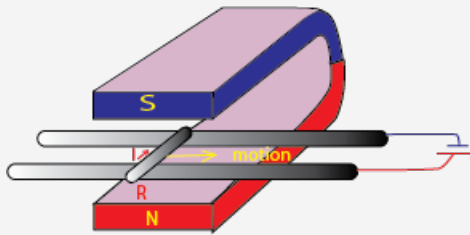
S.I unit of magnetic flux ϕ is Weber (Wb)

If a magnetic field is at an angle, θ , to the area, A , then

$$\phi = BA \cos \theta$$

Force on a conductor or Fleming's Rule

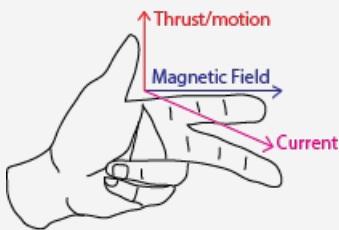
When a conductor carrying a current is placed in a magnetic field due to some source other than itself, it experiences a mechanical force.



To demonstrate this, a short brass rod R is connected across a pair of brass rails, as shown in above. A horseshoe magnet is placed so that the rod lies in the field between its poles. When current I passes through the rod, from an accumulator, the rod rolls along the rails. The direction of rolling is predicted by Fleming's Left Hand rule.

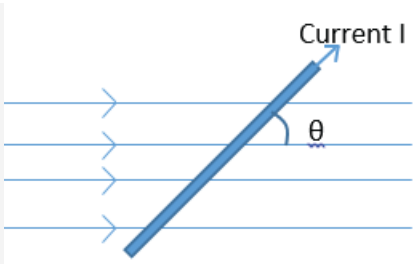
Fleming's Left Hand rule

States that when a straight conductor is placed across a magnetic field and a current is passed through it, the direction of magnetic force is predicted by the thumb when the first two fingers are placed perpendicular to each other. The first finger pointing in magnetic field direction and the second finger in the direction of current



Factors affecting the magnitude of force experienced by a current carrying conductor placed across a magnetic field

- Magnetic field strength or flux density, B ; magnetic force increases with magnetic field density.
- Size of current, I , flowing through the conductor; the force is directly proportional to the current.
- Length L of the conductor; the force is directly proportional to the length of the conductor.
i.e. $F \propto L$
- Angle of inclination of conductor across a magnetic field



$$F = BIL\sin\theta$$

When $\theta = 90^\circ$; $F = BIL$

When $\theta = 0$; $F = 0$

It follows that F is zero when the conductor is parallel to the field direction

Magnetic Permeability

Magnetic Permeability

Magnetic permeability is defined as the ratio of the magnetic induction to the magnetic intensity. It is a scalar quantity and denoted by the symbol, μ .

Magnetic permeability helps us measure a material's resistance to the magnetic field or measure of the degree to which magnetic field can penetrate through a material.

The magnetic permeability of a material indicates the ease with which an external magnetic field can create a higher magnetic force of attraction in the material.

The SI unit of magnetic permeability is Henry per meter.

Factors Affecting Magnetic Permeability

It depends on the nature of the material, humidity, position in the medium, temperature, and frequency of the applied force.

Magnetic Permeability Formula

Magnetic permeability formula is given as;

$$\text{Magnetic permeability } (\mu) = B/H$$

Where B = magnetic intensity and H = magnetizing field.

The SI unit of magnetic permeability is henneries per meter (H/m) or Newton per ampere squared ($\text{N}\cdot\text{A}^{-2}$).

Types of Permeability

The different types of permeability include;

Permeability of Free Space, air or vacuum.

It is represented by $\mu_0 = B_0/H$

The ratio of magnetic intensity in a vacuum and magnetizing field.

Permeability of Medium

The ratio of magnetic intensity in the medium and magnetizing field.

It is expressed as;

$$\mu = B/H$$

Relative Permeability

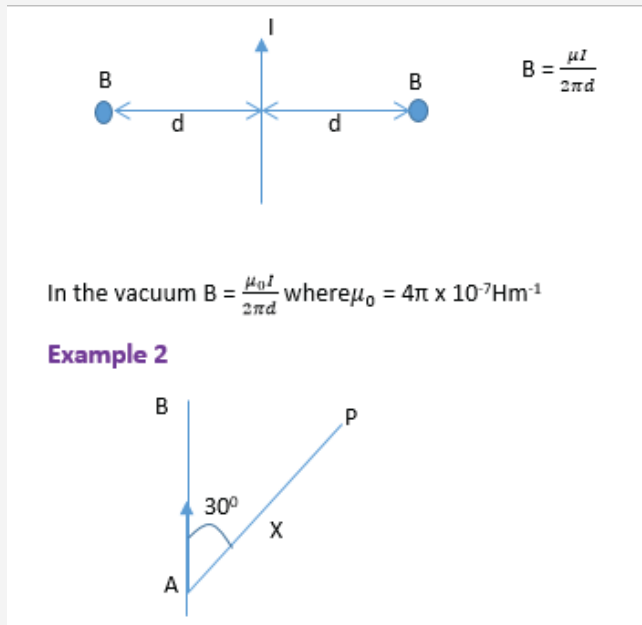
$$\mu_r = \frac{\mu}{\mu_0}$$

Relative permeability = $\frac{\text{number of lines of magnetic induction per unit area in a material}}{\text{number of lines per unit area in a vacuum}}$

Magnetic flux produced by a current

A straight wire carrying a current I in a medium of permeability, μ

At perpendicular distance, d from the wire



Write down the expression for magnetic flux density at P due to AB placed in a vacuum

Solution

The perpendicular distance, d , of P from AB = $x \sin 30^\circ$.

Thus at P, $B = \frac{\mu_0 I}{2\pi x (x \sin 30^\circ)}$

- (b) At the center of a plane circular coil of radius, r , and having N -turns of wire each carrying current I in the vacuum.



At the center of the coil, magnetic flux density, $B = \frac{\mu_0 NI}{2r}$ in the vacuum/air

Example 3

Determine the expression for magnetic flux density at the center of plane circular coil of 10 turns each radius r and carrying a current I in a vacuum.

Solution

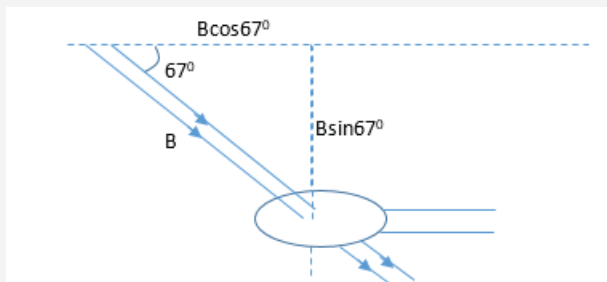
$$\text{From } B = \frac{\mu_0 NI}{2r}$$

$$B = \frac{\mu_0 N \cdot 10 \cdot I}{2r} = \frac{5\mu_0 NI}{r}$$

Example 4

A plane circular coil of 20 turns is placed with its surface flat on a horizontal table. If the

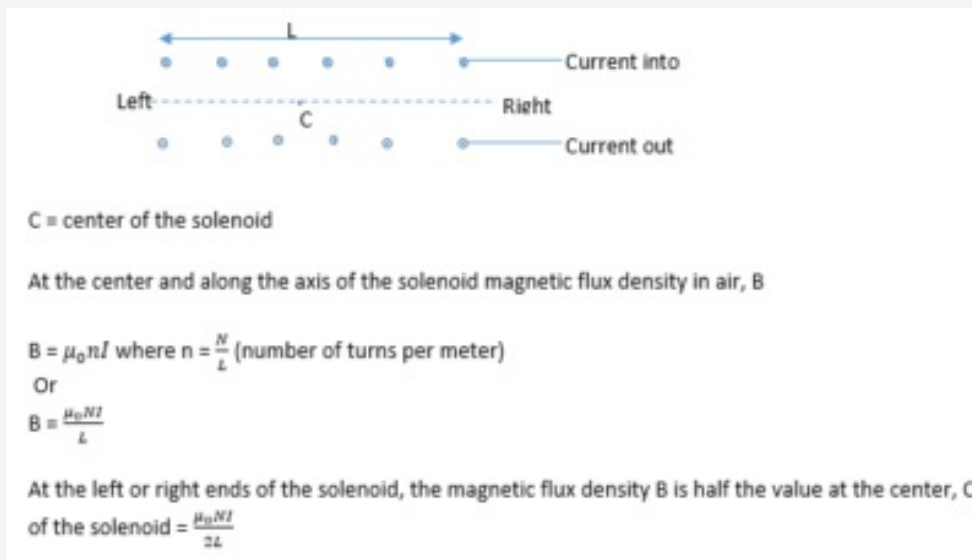
plane of the coil is threaded by magnetic field of flux density $3.6 \times 10^{-5} \text{T}$ at an angle 67° , find magnetic flux threading the coil of radius 5cm



Magnetic flux threading the plane of the coil normally

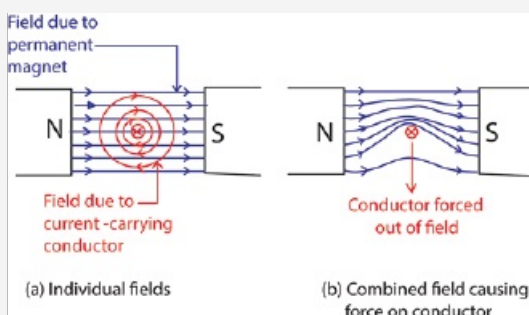
$$\begin{aligned}\phi &= B' A \quad \text{where } B' = B \sin 67^\circ \\ &= B A \sin 67^\circ \\ &= 2\pi r^2 \sin 67^\circ \\ &= 3.6 \times 10^{-5} \times 2\pi \times (0.05)^2 \times \sin 67^\circ \\ &= 2.6 \times 10^{-7} \text{Wb}\end{aligned}$$

Magnetic flux density due to a solenoid (long coil) carrying a current I



Magnetic force due to current carrying conductor

Whenever a straight conductor or wire carrying current I in the direction normal to an external magnetic field is placed across the field, the wire experiences magnetic force $F = BIL$ in the direction provided by Fleming's Left hand rule.



Explanation

The current carrying conductor produces a magnetic field around itself. This magnetic field interacts with the external magnetic field B where the wire is placed creating a

region of stronger magnetic field on one side of the wire and weaker magnetic field on another of the wire (opposite side)

The net force acts on the wire from the direction of stronger field to that of weaker field and is given by

$$F = BIL.$$

Derivation of $F = BIL$

Consider a conductor of length L , cross section area A with N free electrons

When a p.d is applied across its ends, the electrons begin to drift with velocity, $V = \frac{I}{n e A}$; where $n = \frac{N}{AL}$ (number of electrons per unit volume.)

When the conductor is placed across an external magnetic field of density B , each electron experiences a force

$$F_1 = BeV$$

$$= Be \cdot \frac{I}{n e A}$$

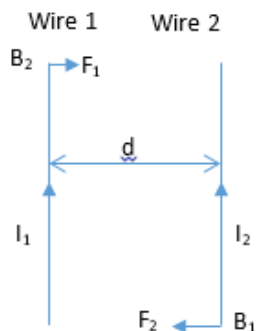
$$= \frac{BI}{nA}$$

$$\text{Total force on } N \text{ electrons, } F = NF_1 = \frac{NB I}{nA}$$

$$\text{But } N = nAL$$

$$\text{Thus } F = \frac{(nAL)BI}{nA} = BIL$$

Magnetic force on parallel straight wires/conductors carrying current I_1 and I_2 in the same direction



$$\text{Magnetic field due to wire 1 at a distance } d \text{ away} = B_1 = \frac{\mu_0 I_1}{2\pi d}$$

$$\text{Magnetic field due to wire 2, at a distance } d \text{ away} = B_2 = \frac{\mu_0 I_2}{2\pi d}$$

$$\text{Magnetic force acting on wire 1, } F_1 = B_2 I_1 L_1$$

$$\text{Substituting for } B_2; F_1 = \left(\frac{\mu_0 I_2}{2\pi d} \right) I_1 L_1 = \frac{\mu_0 I_2 I_1 L_1}{2\pi d} \text{ towards wire 2}$$

$$\text{Force per unit length, } F = \frac{F_1}{L_1} = \frac{\mu_0 I_2 I_1}{2\pi d}$$

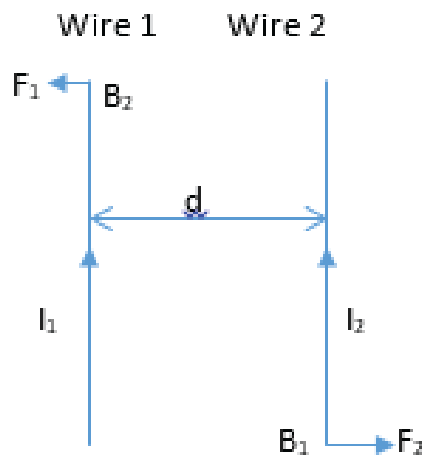
$$\text{Magnetic force on wire 2, } F_2 = B_1 I_2 L_2$$

$$\text{Substituting for } B_1, F_2 = \left(\frac{\mu_0 I_1}{2\pi d} \right) I_2 L_2 = \frac{\mu_0 I_2 I_1 L_2}{2\pi d} \text{ toward wire 1}$$

$$\text{Force per unit length } F = \frac{F_2}{L_2} = \frac{\mu_0 I_2 I_1}{2\pi d}$$

Magnetic force on parallel straight wires/conductors carrying current I_1 and I_2 in the opposite direction

Two straight and parallel conductors (wires) carrying current I_1 and I_2 in opposite direction experience magnetic forces $F_1 = B_2 I_1 L$ and $F_2 = B_1 I_2 L$ acting perpendicularly away from the next wire. (Repulsive forces)



Magnetic field due to wire 1 a distance d away = $B_1 = \frac{\mu_0 I_1}{2\pi d}$

Magnetic field due to wire 2, a distance d away = $B_2 = \frac{\mu_0 I_2}{2\pi d}$

Magnetic force acting on wire 1, $F_1 = B_2 I_1 L_1$

Substituting for B_2 ; $F_1 = \left(\frac{\mu_0 I_2}{2\pi d}\right) I_1 L_1 = \frac{\mu_0 I_2 I_1 L_1}{2\pi d}$ towards wire 2

Force per unit length, $F = \frac{F_1}{L_1} = \frac{\mu_0 I_2 I_1}{2\pi d}$

Magnetic force on wire 2, $F_2 = B_1 I_2 L_2$

Substituting for B_1 , $F_2 = \left(\frac{\mu_0 I_1}{2\pi d}\right) I_2 L_2 = \frac{\mu_0 I_2 I_1 L_2}{2\pi d}$ toward wire 1

Force per unit length $F = \frac{F_2}{L_2} = \frac{\mu_0 I_2 I_1}{2\pi d}$

Generally $F_1 = F_2 = F$

When current is flowing in the same direction, the forces between the wires are attractive but in different directions, the forces are repulsive.

Ampere

It is a unit of current.

Definition

An ampere is a steady current which when flowing in each of two straight parallel wires of infinite length and negligible cross section area and placed a distance of 1m apart in a vacuum produce a force of $2 \times 10^{-7} \text{N}$ per meter on each other.

Derivation of an ampere

From expression $\frac{F}{L} = \frac{\mu_0 I_2 I_1}{2\pi d}$

Suppose $I_1 = I_2 = 1\text{A}$, $d = 1\text{m}$, $\mu_0 = 4\pi \times 10^{-7}\text{H/m}$

$$\frac{F}{L} = \frac{4\pi \times 10^{-7} \times 1 \times 1}{2\pi \times 1} = 2.0 \times 10^{-7}\text{N/m}$$

Example 5

Two straight wires A and B carry currents 4A and 6A respectively in a vacuum. Given that A and B are parallel to each other and are a distance of 2.0cm apart, calculate the resultant magnetic field mid-way between the wires carrying current in

Opposite direction

Solution

(a) Opposite direction

Solution



$$B_A = \frac{\mu_0 I_A}{2\pi d_A}; B_B = \frac{\mu_0 I_B}{2\pi d_B}$$

Resultant magnetic field midway, $B = B_A + B_B$; $d_A = d_B = 1\text{cm} = 0.01\text{m}$

$$B = \frac{\mu_0 \times 4}{2\pi \times 0.01} + \frac{\mu_0 \times 6}{2\pi \times 0.01} = \frac{4\pi \times 10^{-7}}{2\pi \times 0.01} (4 + 6) = 2 \times 10^{-5}\text{T perpendicular to the plane of paper}$$

(b) Same direction



Resultant magnetic field midway, $B = B_A + (-B_B)$; $d_A = d_B = 1\text{cm} = 0.01\text{m}$

$$B = \frac{\mu_0 \times 6}{2\pi \times 0.01} - \frac{\mu_0 \times 4}{2\pi \times 0.01} = \frac{4\pi \times 10^{-7}}{2\pi \times 0.01} (6 - 4) = 4 \times 10^{-5}\text{T perpendicular to the plane of paper}$$

Example 6

Find the force per unit length of the wires when $I_A = 8.0\text{A}$, $I_B = 11.0\text{A}$ and $r = 3.0\text{cm}$

(04marks)

The magnetic flux density which A produces at B is given by

$$\frac{\mu_0 I_A}{2\pi r} = \frac{4\pi \times 10^{-7} \times 8}{2\pi \times 3 \times 10^{-2}} = 5.30 \times 10^{-5} \text{T}$$

Force exerted by A on B, $F = BI_B L$

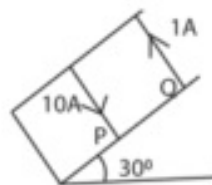
$$\frac{F}{L} = BI_B = 5.30 \times 10^{-5} \times 11 = 5.85 \times 10^{-4} \text{Nm}^{-1}.$$

Or

$$\frac{F}{L} = \frac{\mu_0 I_A I_B}{2\pi r} = \frac{4\pi \times 10^{-7} \times 8 \times 11}{2\pi \times 3 \times 10^{-2}} = 5.85 \times 10^{-4} \text{Nm}^{-1}$$

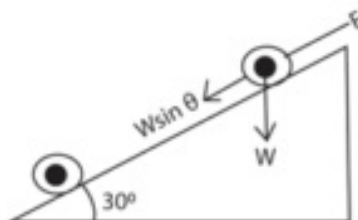
Example 7

Two parallel wires P and Q, each of length 0.2m carry currents of 10A and 1A respectively



The distance between the wires is 0.04m. If both wires remain stationary and the angle of the plane with the horizontal is 30° . Calculate weight of Q.

Solution



Force F between the two wires is given by

$$F = \frac{\mu_0 I_1 I_2 L}{2\pi a} = \frac{4\pi \times 10^{-7} \times 10 \times 1 \times 0.2}{2\pi \times 0.04} = 1.0 \times 10^{-3} \text{N}$$

But for equilibrium, the component of the weight along the slope is balanced by the magnetic force on the wire i.e. $F = W \sin \theta$

$$\Rightarrow W = \frac{F}{\sin \theta} = \frac{1.0 \times 10^{-3}}{\sin 30} = 2 \times 10^{-3} \text{N}$$

Example 8

Two parallel wire, P and Q of equal length 0.1m, each carrying a current of 10A are a distance 0.05m apart with P directly above Q. If P remains stationary, find the weight of P. (03marks)

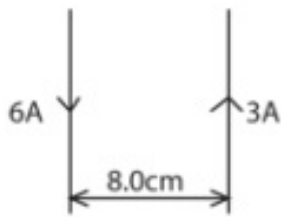
Solution

Force due to magnetic field on P = weight of P, W .

$$W = \frac{\mu_0 I_1 I_2 L}{2\pi a} = \frac{4\pi \times 10^{-7} \times 10 \times 10 \times 0.1}{2\pi \times 0.05} = 4.0 \times 10^{-5} \text{N}$$

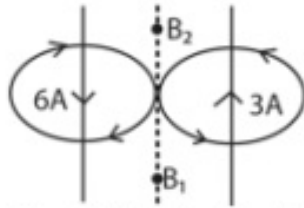
Example 9

Two straight long and straight wires of negligible cross-section area carry currents of 6.0A and 3.0A in opposite direction as shown below



If the wire are separated by a distance of 8.0cm, find the;

- (i) Magnetic flux density at a point mid-way between the wires (04marks)



Magnetic flux density midway between the wires.

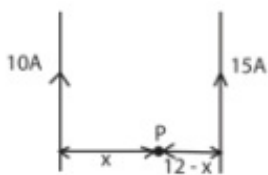
$$\begin{aligned} B &= B_1 + B_2 \\ &= \frac{\mu_0 I_1}{2\pi R} + \frac{\mu_0 I_2}{2\pi R} \\ &= \frac{6 \times 4\pi \times 10^{-7}}{2\pi \times 0.4} + \frac{3 \times 4\pi \times 10^{-7}}{2\pi \times 0.4} \\ &= 4.5 \times 10^{-5} \text{ T} \end{aligned}$$

- (ii) Force per meter between the wire (03marks)

$$\frac{F}{L} = \frac{\mu_0 I_1 I_2}{2\pi a} = \frac{4\pi \times 10^{-7} \times 6 \times 3}{2\pi \times 0.8} = 4.5 \times 10^{-5} \text{ Nm}^{-1}$$

Example 10

Two long parallel wires placed 12cm apart in air carry currents of 10A and 15A respectively in the same direction. Determine the position where the magnetic flux is zero. (04marks)



Let P be the point where the resultant magnetic flux is zero

$$\text{Then, } \frac{\mu_0 I_1}{2\pi x} = \frac{\mu_0 I_2}{2\pi (12-x)}$$

$$\frac{10}{x} = \frac{15}{12-x}$$

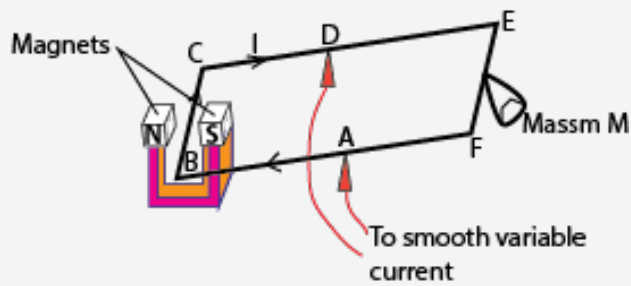
$$x = 4.8 \text{ cm}$$

P is 4.8cm from 10A current and 7.2 cm from the 15A current carrying conductor.

Measurements of current using a current balance

The ampere balance (also current balance or Kelvin balance) is an electromechanical apparatus used for the precise measurement of the SI unit of Electrical current, the ampere. It was invented by Williams Thomson 1st Baron Kelvin.

Set up



$AB = AF$, length $BC = L$ and the current through the wire is A

The magnets provide a uniform magnetic field, B , perpendicular to wire BC .

At equilibrium when the frame $BCEF$ is balanced

The force exerted on the wire = weight of the mass

$$BIL = Mg$$

$$I = \frac{Mg}{BL}$$

Sources of error

- Accuracy of length L
- Rigidity of the frame
- To avoid overheating, the current should be switched off as soon as measurements have been taken.
- Shield the set-up from the disturbance of wind.

Self-induction

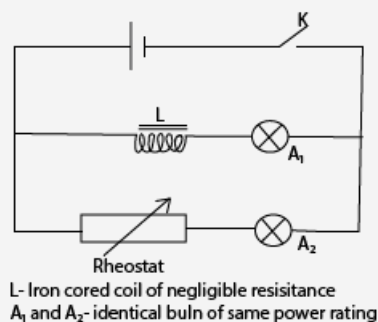
It is a process by which an e.m.f is induced in a coil or circuit when the magnetic flux linking it changes due to the current flowing in the same circuit/coil.

Mutual induction

It is a process by which an e.m.f is induced in a coil when the magnetic flux linking it changes as a result of a change in the current flowing in nearby coil.

Experiment to demonstrate self-induction.

The circuit is arranged as shown below.



Procedure

Switch K first closed and the rheostat adjusted until the two bulbs indicate the same brightness.

When the switch is opened and closed again, bulb A2 is observed to attain maximum brightness almost instantly while bulb A1 takes some time to attain maximum brightness.

Explanation

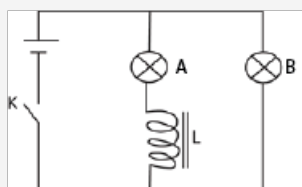
The current in A1 takes some time to attain a steady value due to back e.m.f induced in the coil as a result of change in the current flowing (due to self-induction) in the coil when the switch is closed.

The back e.m.f gradually decay to zero as current establishes a steady value and hence the current in the coil rises slowly to its maximum when the back e.m.f is zero.

Note that back e.m.f occurs only when charge/current is changing leading to change in magnetic flux linking it.

Example 11

In the figure below, A and B are identical bulbs and L is an iron cored coil.



Explain what will be observed when switch K is closed and when it is opened

When K is closed, bulb A lights dimly and slowly becomes brighter while B becomes bright almost instantly and later the two bulbs acquire the same brightness.

When K is closed, the current begins to flow around the closed circuit and gradually increases to its steady value or maximum. The sudden change or increase in the current creates an increase in the magnetic flux around the coil and large back e.m.f is induced into the coil due to self-induction.

Back e.m.f greatly opposes the flow of current in bulb A, causing most of the current to flow in bulb B, hence bulb A lights dimly and B brighter initially but later the back e.m.f decay to zero and bulbs A and B now light to the same brightness.

When the switch is opened, bulbs A and B dim out gradually before going off. The built up magnetic flux decay slowly to zero causing back e.m.f which tries to maintain the current in the circuit and hence the bulbs dim out gradually

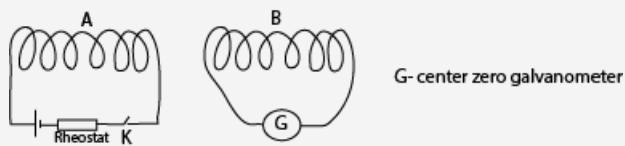
(ii) Explain what you would observe when a battery is replaced by a.c voltage source and K is closed.

Bulb A may not light while B lights brightly because a.c causes a higher constant rate of change in magnetic flux around the soft iron cored coil and hence back e.m.f is constantly induced in the coil which greatly opposes the flow of current in A. the current in A may not rise to a value enough to lit it.

Secondary observation

- The iron core become warm
The higher constant rate of changing magnetic flux caused by the a.c induces eddy currents in the core which generate heat by I^2R mechanism and hence the core become warm.
- The a.c also cause the direction of the magnetic domain in iron core to change according to the changing flux. This requires energy (hysteresis) which is later converted into heat energy in the core

Experiment to demonstrate mutual induction



- The setup is shown above, coil A is place close to coil B but not touching.
- When the switch K is closed, the galvanometer deflects indicating induction of e.m.f in the coil B, hence mutual induction.

Self-inductance

$$E = L \frac{di}{dt} \Rightarrow \frac{E}{\frac{di}{dt}}$$

It can be defined as the ratio of the magnitude of the back e.m.f induced in a coil or circuit to the rate of change of current flowing in the coil or circuit.

Or

$$E = L \frac{di}{dt}$$

$$\text{When } \frac{di}{dt} = 1 \text{ As}^{-1},$$

$$E = L$$

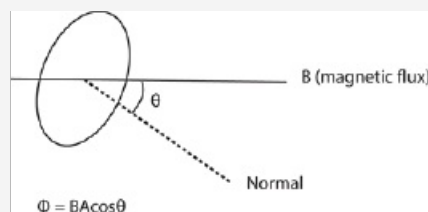
Thus self-inductance can also be defined as the magnitude of the back e.m.f induced in a coil or circuit when rate of change of current flowing in the coil is 1 As^{-1} .

Magnetic flux, Φ

Magnetic flux density is the force acting on a charge of 1 C moving with a velocity of 1 ms^{-1} at right angle to magnetic field.

Or

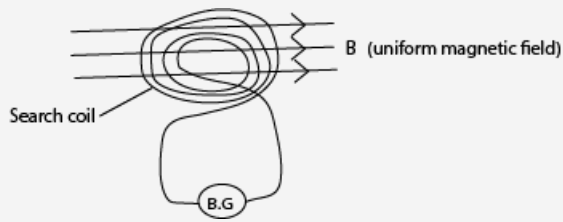
Magnetic flux is a vector whose magnitude is equal to the product of the area of the plane of the conductor or coil and the component of magnetic flux density normal to the plane of conductor or coil.



For a coil of N turns, magnetic flux linkage

$$\Phi = NBA \cos \theta$$

An experiment to determine the magnetic flux density of a uniform magnetic field using a search coil and ballistic galvanometer



A search coil of cross section area A and number of turn's N is connected in series with ballistic galvanometer.

The search coil is then placed in uniform magnetic field such that the plane of the coil is perpendicular to the magnetic field.

The coil is then pulled completely out of the field. The first deflection of the ballistic galvanometer noted θ_1 .

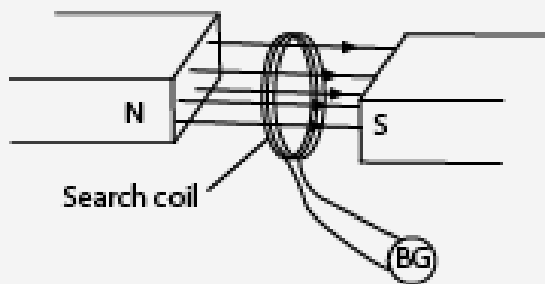
A capacitor of known capacitance C is then charged to a p.d. V and then charged through the ballistic galvanometer, θ_2 is noted

The magnetic flux density of uniform magnetic field is obtained from

$$B = \frac{CVR}{AN} \times \frac{\theta_1}{\theta_2}$$

Where R is the resistance of the whole circuit.

An experiment to measure the magnetic flux density between the poles pieces of a strong magnet.



A search coil is connected to a ballistic galvanometer. The coil is then placed with its plane normal to the magnetic field whose magnetic flux density, B is required.

The coil is then pulled completely out of the field and deflection θ_1 of ballistic galvanometer is noted

$$\frac{NAB}{R} = CQ, \text{ where } R = \text{resistance of the coil}$$

A capacitor of known capacitance Q is charged to a p.d. V and is then discharged through the ballistic galvanometer. The deflection θ_2 is noted

$$CV = C\theta_2$$

The magnetic flux density B is now calculated from

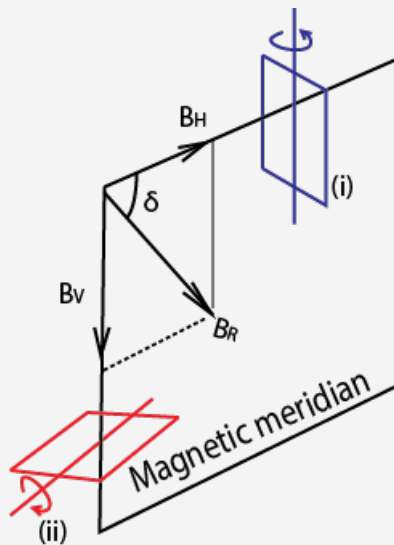
$$B = \frac{CVR\theta}{NA\theta_1}$$

where A is the area of the coil,

N is the number of turns in the coil and

R is the resistance of the coil circuit.

An experiment to determine the value of the earth's magnetic flux density at a place, using a search coil.



- A coil of known number of turns, N (about 100) and area A is connected to a calibrated ballistic galvanometer so that the total resistance in the circuit is R.
- The coil is placed in a vertical plane perpendicular to the magnetic meridian of the earth as shown in (i) in figure above. The coil is then rotated through 180° about the vertical axis. The maximum throw θ_1 is noted.
- The coil is then placed with its plane in horizontal plane perpendicular to the magnetic meridian of the earth as shown in (ii) in figure above. The coil is then rotated through 180° about the horizontal axis. The maximum throw θ_2 is noted.
- Treatment of results

$$B_H = \frac{k\theta_1 R}{2NA} \text{ and } B_V = \frac{k\theta_2 R}{2NA}$$

k is obtained by charging standard capacitor to a known p.d V and then discharging it through the ballistic galvanometer and the deflection α is noted.

$$k = \frac{CV}{\alpha}$$

Then B is calculated from $b = \sqrt{B_H^2 + B_V^2}$

Magnetic moment

Magnetic moment, also known as magnetic dipole moment, is the measure of the object's tendency to align with a magnetic field.

Magnetic Moment is defined as magnetic strength and orientation of a magnet or other object that produces a magnetic field.

The magnetic moment is a vector quantity. Magnetic moments of two magnets are compared using a deflected magnetometer

The structure and mode of action of the deflection magnetometer

The structure and mode of action of the deflection magnetometer

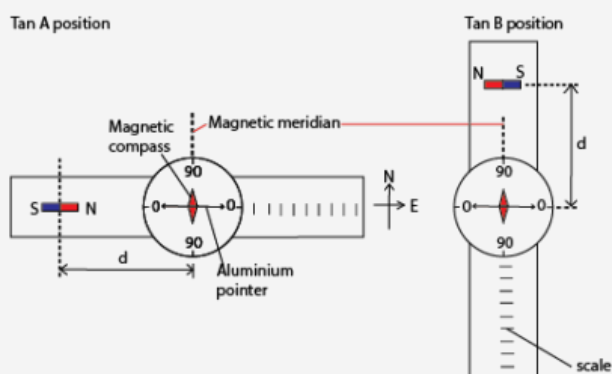
It consists of a small compass needle (small magnet) enclosed in a transparent box which is pivoted on a vertical axis and carries a light aluminium pointer. The pointer can rotate over a circular scale.

The box is fixed in the center of wooden box with two arms of linear scales of 0.5m each that coincide at the center of the magnetic compass.

Deflection magnetometer is used for

- Comparing magnetic moments of two magnets
- Verifying inverse law

The magnetometer can be used in two positions; i.e. Tan A position and Tan B position



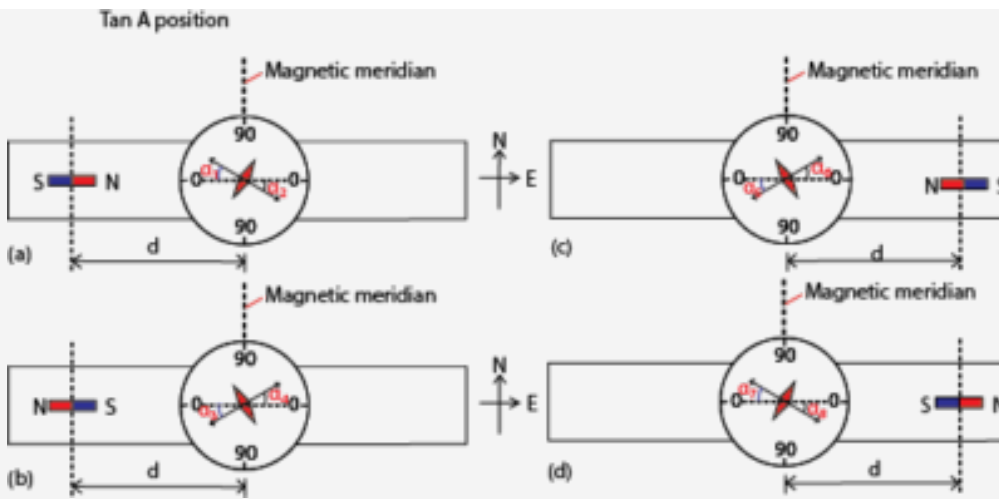
• Tan A position

The arms of magnetometer are adjusted to be parallel the aluminium pointer so that they lie in east-west direction and compass pointer adjusted to read zero degrees on the circular scale while the magnetic needle lies in the direction of magnetic meridian

• Tan B position

The arms of magnetometer are adjusted to be parallel the aluminium pointer so that they lie in north-south direction and compass pointer adjusted to read zero degrees on the circular scale while the magnetic needle lies in the direction of magnetic meridian

Comparing magnetic moments of two magnets using a magnetometer at equal distances in Tan A position



(a) The first bar magnet is placed a distance d from the magnetic compass as shown above and angles of deflection of aluminium pointer α_1 and α_2 are noted

(b) The polarity of the bar magnet in (a) is reversed and angles of deflections α_3 and α_4 are noted

(c) The first bar magnet is placed equal distance d from magnetic compass on the opposite arm and angles of deflection of aluminium pointer α_5 and α_6 are noted

(d) The polarity of the bar magnet in (c) is reversed and angles of deflections α_7 and α_8 are noted

(e) Average angle

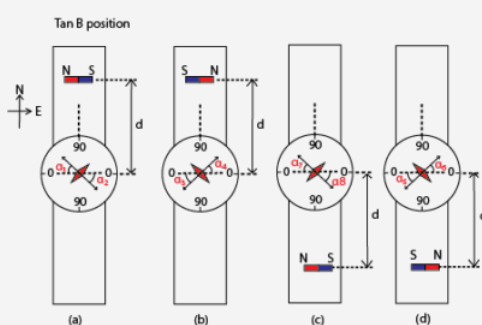
$$\theta_1 = \frac{\alpha_1 + \alpha_2 + \alpha_3 + \alpha_4 + \alpha_5 + \alpha_6 + \alpha_7 + \alpha_8}{8}$$

(f) Steps (a) to (e) are repeated for the second magnet to obtain average angle θ_2

(g) The ratio of magnetic moments is given by

$$\frac{M_1}{M_2} = \frac{\tan \theta_1}{\tan \theta_2}$$

Comparing magnetic moments of two magnets using a magnetometer at equal distances in Tan B position



(a) The first bar magnet is placed a distance d from the magnetic compass as shown

above and angles of deflection of aluminium pointer α_1 and α_2 are noted

(b) The polarity of the bar magnet in (a) is reversed and angles of deflections α_3 and α_4 are noted

(c) The first bar magnet is placed equal distance d from magnetic compass on the opposite arm and angles of deflection of aluminium pointer α_5 and α_6 are noted

(d) The polarity of the bar magnet in (c) is reversed and angles of deflections α_7 and α_8 are noted

(e) Average angle

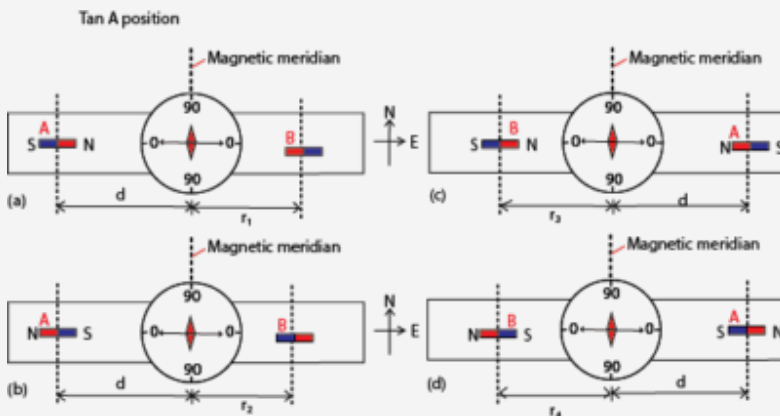
$$\theta_1 = \frac{\alpha_1 + \alpha_2 + \alpha_3 + \alpha_4 + \alpha_5 + \alpha_6 + \alpha_7 + \alpha_8}{8}$$

(f) Steps (a) to (e) are repeated for the second magnet to obtain average angle θ_2

(g) The ratio of magnetic moments is given by

$$\frac{M_1}{M_2} = \frac{\tan \theta_1}{\tan \theta_2}$$

Comparing magnetic moments of two magnets using a magnetometer and null method in tan A position



(a) Place one magnet a distance d from the magnetic compass and another on the opposite arm facing each other.

(b) Adjust the second magnet to a distance r_1 until the compass needle shows zero deflection

(c) Reverse the poles of the two magnets keeping the distance d of the first magnet and determine the distance r_2 of the second magnet leading to zero deflection.

(d) The magnets are interchanged keeping the distance d of first magnet unchanged, procedures (b) and (c) are repeated for distances r_3 and r_4 .

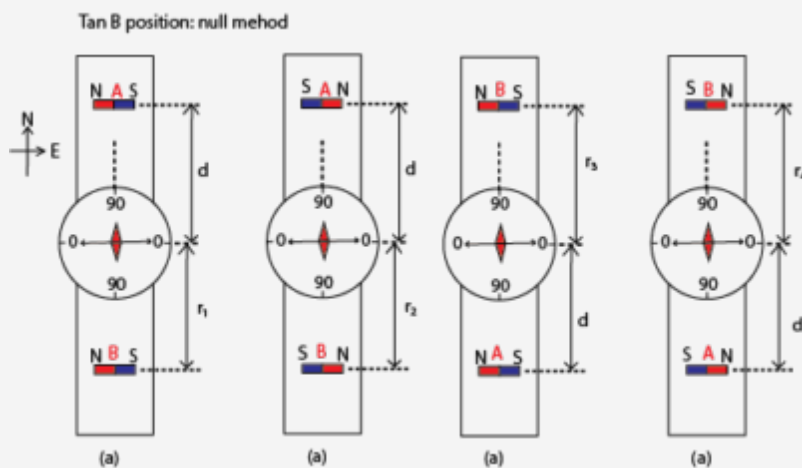
(e) Now

$$d_2 = \frac{r_1 + r_2 + r_3 + r_4}{4}$$

(f) The ratio of magnetic moments is given by

$$\frac{M_1}{M_2} = \frac{d_1^3}{d_2^3}$$

Comparing magnetic moments of two magnets using a magnetometer and null method in tan B position



(a) Place one magnet a distance d from the magnetic compass and another on the opposite arm facing each other.

(b) Adjust the second magnet to a distance r_1 until the compass needle shows zero deflection

(c) Reverse the poles of the two magnets keeping the distance d of the first magnet and determine the distance r_2 of the second magnet leading to zero to zero deflection.

(d) The magnets are interchanged keeping the distance d of first magnet unchanged, procedures (b) and (c) are repeated for distances r_3 and r_4 .

(e) Now

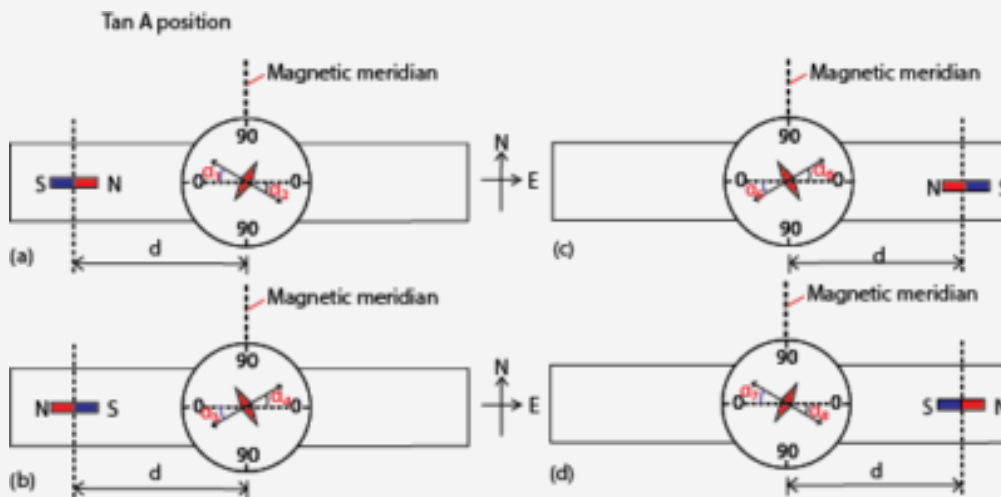
$$d_2 = \frac{r_1 + r_2 + r_3 + r_4}{4}$$

(f) The ratio of magnetic moments is given by

$$\frac{M_1}{M_2} = \frac{d_1^3}{d_2^3}$$

Verifying inverse square law with deflection magnetometer

A. Arrange the magnetometer in tan A position



(a) The first bar magnet is placed a distance d from the magnetic compass as shown above and angles of deflection of aluminium pointer α_1 and α_2 are noted

(b) The polarity of the bar magnet in (a) is reversed and angles of deflections α_3 and α_4 are noted

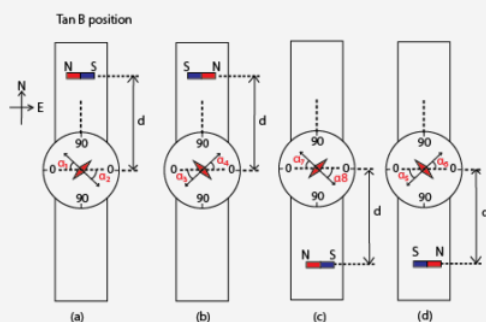
(c) The first bar magnet is placed equal distance d from magnetic compass on the opposite arm and angles of deflection of aluminium pointer α_5 and α_6 are noted

(d) The polarity of the bar magnet in (c) is reversed and angles of deflections α_7 and α_8 are noted

(e) Average angle

$$\theta_A = \frac{\alpha_1 + \alpha_2 + \alpha_3 + \alpha_4 + \alpha_5 + \alpha_6 + \alpha_7 + \alpha_8}{8}$$

B. Arrange the magnetometer in tan B position



(a) The first bar magnet is placed a distance d from the magnetic compass as shown above and angles of deflection of aluminium pointer α_1 and α_2 are noted

(b) The polarity of the bar magnet in (a) is reversed and angles of deflections α_3 and α_4 are noted

(c) The first bar magnet is placed equal distance d from magnetic compass on the opposite arm and angles of deflection of aluminium pointer α_5 and α_6 are noted

(d) The polarity of the bar magnet in (c) is reversed and angles of deflections α_7 and α_8 are noted

(e) Average angle

$$\theta_B = \frac{\alpha_1 + \alpha_2 + \alpha_3 + \alpha_4 + \alpha_5 + \alpha_6 + \alpha_7 + \alpha_8}{8}$$

(f) Inverse square law is verified if

$$\frac{\tan \theta_A}{\tan \theta_B} = 2$$

Electromagnetic induction

It is the induction of an e.m.f. in a conductor or in a coil by moving it relatively to a magnetic field

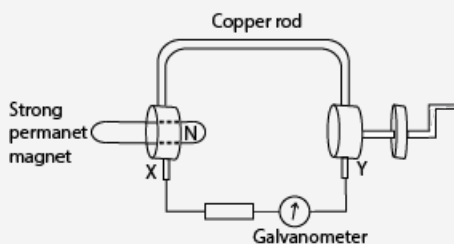
Laws of electromagnetic induction

Faraday's law of electromagnetic induction states that the magnitude of the e.m.f. induced in a circuit is directly proportional to the rate of change of magnetic flux linked with the circuit.

Lenz's Laws of electromagnetic induction states that induced current flows always in such a direction as to oppose the change which is giving rise to it.

An experiment to demonstrate Faraday's law of electromagnetic induction.

Verification setup



X and Y are brush contact.

A copper rod which can rotate round the north pole of permanent magnet is connected as shown above.

The wheel is turned steadily until the deflection of the galvanometer is constant.

The time, t , for N rotations is measured and the number of revolution (n) per second is determined from $n = N/t$. The deflection θ of the galvanometer is also noted.

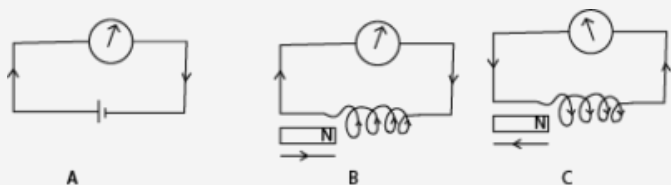
The experiment is repeated at different speed of rotation of the wheel and values of n and θ tabulated.

A graph of θ against n is plotted.

A straight line graph is obtained implying that $\theta \propto n$

Since $\theta \propto \text{e.m.f induced}$ and $n \propto \text{speed of rotation of the rod}$, then the induced e.m.f is proportional to the rate of change of flux linkage.

An experiment to illustrate Lenz's law of electromagnetic induction



- The galvanometer (A) is first connected in series with a battery and the direction for a given direction of current is determined.
- The battery is disconnected and is replaced by a coil of known winds.
- A strong permanent magnet (B) is brought towards the coil with N-pole facing the coil, the galvanometer deflects in a direction for which the side of the coil facing the magnet is N-pole.
- When the magnet (C) is move away from the coil, the galvanometer deflects in opposite direction, implying that the pole near the coil is a S-pole.

Interpretation of results

In the first case, the pole due to the induced current was repelling the approaching magnet, while in the second case, the pole was attracting the receding magnet. The induced current therefore is in such as to oppose the change causing it, which is Lenz's law.

Example 12

Explain why Lenz's law is referred to as an example of energy conservation or Why Lenz's law does not violet the principle of conservation of energy.

In order not to violet the principle of conservation of energy, the effects of induced current must oppose the motion of the magnet in such a way that work done by an external agent in moving the magnet is the one that is converted into electrical energy and hence there is just transformation of energy from one form to another (from mechanical energy to electrical energy) and hence Lenz's law is an example of energy conservation..

Magnetic moment of a coil.

Magnetic moment is torque experienced by the coil per tesla of magnetic field acting along the plane of the coil.

Or

Magnetic moment of a coil is a couple exerted on a coil when it is placed with its plane parallel to a magnetic field of 1T

Magnitude of e.m.f induced in a coil depends on

Number of turns N in the coil

Rate of change in magnetic flux

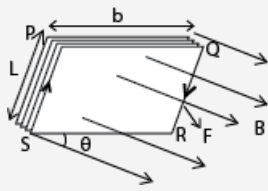
Strength of Magnetic flux

Area of the coil

Derivation of expression for torque on rectangular coil in a magnetic

field

Consider a rectangular coil of N turns each of dimensions $L \times b$ is inclined at an angle θ to uniform magnetic field of flux density, B .



- When current flows through the coil, the conductor experiences a magnetic force.
- Force on side $PQ = NBb\sin\theta$ (downwards) while Force on side $RS = NBb\sin\theta$ (upwards). The two forces cancel out due to rigidity of the coil.
- Side PS experiences force $NbL\cos\theta$ perpendicularly into the page while RQ experiences force $NbL\cos\theta$ perpendicularly out of page. The two forces constitute a couple whose moment of force
 $\tau = F \times b$
 $= NBbL\cos\theta$
 $= NBI A \cos\theta$ (where A is the area $= L \times b$)

Example 13

A small circular coil of 20 turns of wire lies in a uniform magnetic field of flux density $5.0 \times 10^{-2} \text{T}$. The normal to the coil makes an angle of 30° with the direction of the magnetic field. If the radius of the coil is 4cm and the coil carries a current of 2.0A, find the

(i) Magnetic moment of the coil (02marks)

$$M = NIA = 20\pi \times (4 \times 10^{-2})^2 \times 2 = 0.2 \text{Am}^2$$

(ii) Torque on the coil

$$T = MB\sin\theta = 0.2 \times 5 \times 10^{-2} \sin 30^\circ = 5.0 \times 10^{-3} \text{Nm}$$

Example 14

Show that when the magnetic flux linking a coil changes, the total charge which passes through is depends only on the resistance of the coil and total flux linking it (05marks).

Consider a coil of N turns each linked by magnetic flux of ϕ_1 .

Suppose the magnetic flux changes to ϕ_2 .

When the magnetic flux ϕ changes, an e.m.f ε is induced in the coil.

$$\varepsilon = \frac{-Nd\phi}{dt}$$

$$I = \frac{\varepsilon}{R}; R = \text{the resistance of the coil}$$

$$\varepsilon = IR$$

$$\text{Hence } IR = \frac{-Nd\phi}{dt}$$

But $I = \frac{dQ}{dt}$, where Q is the induced charge

$$\Rightarrow \frac{dQ}{dt} = \frac{-N}{R} \cdot \frac{d\phi}{dt}$$

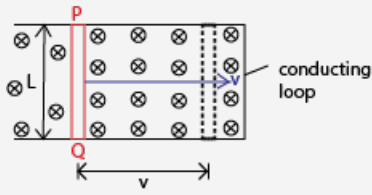
$$dQ = \frac{-N}{R} d\phi$$

The amount of the charge which passes through the coil when the magnetic flux changes from ϕ_1 to ϕ_2 is

$$Q = \frac{-N}{R} \int_{\phi_1}^{\phi_2} d\phi = \frac{-N}{R} (\phi_2 - \phi_1)$$

Derivation of e.m.f induced in a moving rod by applying the laws of electromagnetic induction

Considering a rod of length L meters moving at right angles to a uniform magnetic field of flux density B tesla moving with uniform speed v ms⁻¹ as shown in figure below:



The induced e.m.f, $E = \frac{\Delta\phi}{\Delta t}$ (i)

But $\phi = BA$ (ii)

$$\bullet \quad E = - \frac{d(BA)}{dt} \text{ (iii)}$$

$$= -B \frac{dA}{dt}$$

$$\text{But } \frac{dA}{dt} = -Lv \text{ (iv)}$$

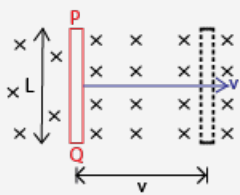
(Negative because the area is decreasing, rate of decrease in area)

$$\therefore E = -B \times -Lv$$

$$= BLv$$

Derivation of e.m.f induced in a moving rod by considering the force extended on the electrons

By virtue of motion of the rod in the magnetic field, the electrons inside the rod experiences a magnetic force.



Applying Fleming's right Hand Rule, the induced e.m.f for current is directly from Q to P.

The electrons flow or drift from P to Q thus acquires a positive charge and Q acquires a negative charge.

An electric field is thus setup which attracts electrons towards the positively charged end P.

Equilibrium is reached when upward electronic force is counterbalanced by the downward magnetic force.

At equilibrium, $Ee = Bev$

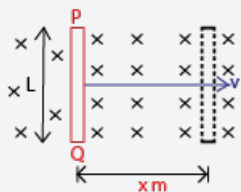
$E = BV$, where E is electric field intensity

But $E = \frac{E'}{L}$, where E' is the induced e.m.f.

$\therefore \frac{E'}{L} = Bv$ where v = speed of the rod, B = magnetic, L = length of the rod.

Derivation of e.m.f induced in a moving rod by applying the principle of conservation of energy

Consider a rod PQ placed at right angles to a uniform magnetic field of flux density B Tesla as shown.



Suppose the rod is moved through of x meters in time t seconds; from the principle of conservation of energy, work done by the external agent in moving the rod is what is conserved into electrical energy.

Therefore, electrical energy = work done in moving the rod.

If E is the induced e.m.f in the rod, then

$$E t = \text{Force} \times \text{distance}$$

But force = BIL , I is the induced current in the rod

$$E t = BILx$$

$$E = \frac{BLx}{t}$$

Since $\frac{x}{t} = v$ (speed of the body)

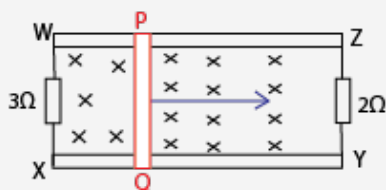
$$\therefore E = BLv$$

Example 15

A rod PQ, 1.2m long moves at right angles to a magnetic field of flux density 0.4T and at a speed of 4ms^{-1} . Find the e.m.f induced in the rod.

Induced e.m.f, $E = BLv = 0.4 \times 1.2 \times 4 = 1.92\text{V}$

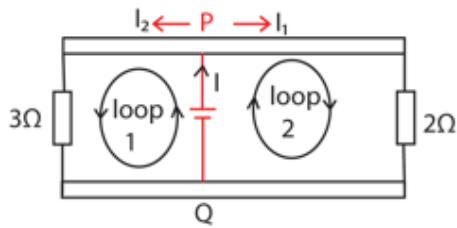
Example 16



In the figure above, a rod PQ 1.2m long is moved in a perpendicular magnetic field of flux density 0.4T at a speed of 4m/s along a frictionless rails XY and WZ. Find the power generated by the rod.

Solution

Applying Fleming's left hand rule, the induced current flows from Q to P, this gives the polarity of induced e.m.f with a positive terminal on the side P.



$$E = BLv = 0.4 \times 1.2 \times 4 = 1.92V$$

At the junction, $I = I_1 + I_2$

$$\text{From } I = \frac{V}{R}$$

Considering loop 1;

$$I_1 = \frac{1.92}{3} = 0.64A$$

Considering loop 2;

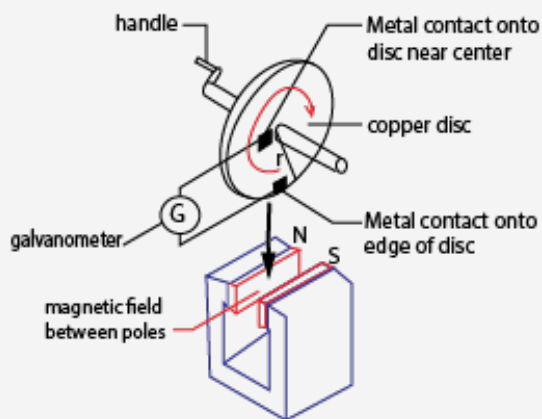
$$I_2 = \frac{1.92}{2} = 0.96A$$

$$I = I_1 + I_2 = 0.64 + 0.96 = 1.6A$$

$$\text{Power} = E = 1.92 \times 1.6 = 3.1W$$

E.m.f induced in a circular disc (disc dynamo)

A disc is an arrangement of obtaining electrical energy from mechanical energy by rotating a circular metal disc in a perpendicular magnetic field about an axle passing through its center.



The disc is rotated at uniform angular velocity, ω , and the e.m.f induced in the disc is tapped by connecting a wire between the center of the disc axle and the rim of the disc.

The induced e.m.f is due to the motion of linear conductor of length = radius r .

From the e.m.f induced in a moving rod

$$E = BLv \dots\dots\dots(i)$$

Where v is the average velocity,

$$v = (0+r\omega)/2 = r\omega/2 \dots\dots\dots(ii)$$

$$v = \frac{0+r\omega}{2} = \frac{r\omega}{2} \dots\dots\dots (ii)$$

(i) and (ii)

$$E = \frac{Br \times r\omega}{2} = \frac{Br^2\omega}{2}$$

But $\omega = 2\pi f$, where f is the frequency of rotation

$$E = \frac{B \times 2\pi r^2 f}{2} = B\pi r^2 f$$

$$E = B A f$$

Example 17

A circular metal disc of radius 8cm is rotated at right angle to a uniform magnetic field of flux density 0.4T at 80revolution per minute. Find the e.m.f induced in the disc.

Solution

Solution

$$\text{Induced e.m.f, } E = B A f, E = \pi r^2 = 3.14 \times 0.08^2, f = \frac{80}{60} \text{ rev/s}$$

$$E = 0.4 \times 3.14 \times 0.08^2 \times \frac{80}{60} = 0.011V$$

Example 18

A circular metal disc of radius 12cm is rotated in a perpendicular magnetic field of flux density 0.4T about an axle of radius 6cm at 52rev/min.

Solution

$$\text{Induced e.m.f, } E = B A f$$

$$= B (\pi (R^2 - r^2)) f$$

$$= 0.4 (\pi (0.12^2 - 0.06^2)) \times \frac{52}{60}$$

$$= 0.0117V$$

Example 19

A conducting disc of radius 0.05m with its plane perpendicular to uniform magnetic field of flux density 0.25T, rotates at 15 revolution per second about an axis through its center and perpendicular to its plane.

Calculate

(i) Magnetic flux threading the disc at any time (03marks)

Magnetic flux, $\phi = BA$ but $A = \pi r^2$

$$\phi = B\pi r^2$$

$$= 0.25 \times 3.14 \times (0.05)^2 = 1.96 \times 10^{-3} \text{Wb}$$

(ii) m.f generated between the center of the disc and any point on its rim.

$$\epsilon = B\pi r^2 f = 0.25 \times 3.14 \times (0.05)^2 \times 15 = 2.9 \times 10^{-2} V$$

$$\text{or } \epsilon = \phi f = 1.96 \times 10^{-3} \times 15 = 2.9 \times 10^{-2} V$$

Example 20

An aero plane of wing span 30m flies horizontally at a speed of 1000kmh⁻¹.

What is the p.d across the tips of its wings, if the horizontal component of the earth's magnetic field is $1.46 \times 10^{-4} \text{T}$? (Angle of dip at the place is 70°) (03marks)

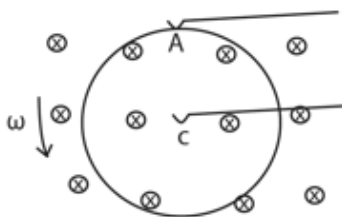
$$E = B_V L v; \text{ but } B_V = B_H \tan 70^\circ$$

$$E = B_H \tan 70^\circ L v$$

$$= 1.46 \times 10^{-4} \times \tan 70^\circ \times 30 \times \frac{1000 \times 1000}{1 \times 60 \times 60} = 3.34 \text{V}$$

Example 21

A circular metal disc of radius R, rotates in an anticlockwise direction at angular velocity, ω , in a uniform magnetic field of flux density, B, directed in to paper as shown in the figure below



A and C are contact points

Derive an expression for e.m.f induced between A and C.

Let r = radius of the disc

Thus AC cuts the magnetic flux continuously.

$$\text{The average velocity } V \text{ of AC} = \frac{0 + r\omega}{2} = \frac{r\omega}{2}$$

\therefore Induced e.m.f in AC = $E = BLV$

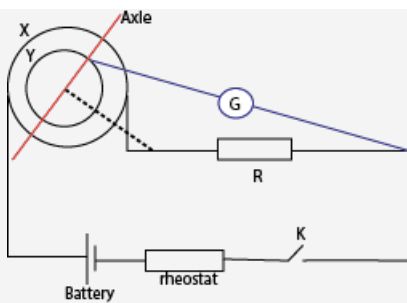
$$= \frac{B r \cdot r \omega}{2}$$

$$= \frac{1}{2} B r^2 \omega$$

Absolute method of measurement of resistance (Lorentz method)

The e.m.f induced in a moving rod is used in the absolute measurement.

A circular metal disc is placed inside a solenoid X of known number of turns, N and length, L meters in series with a battery, unknown resistance R, a rheostat and a switch K



Switch K is closed and the disc of diameter, r , is rotated about an axle passing through its center at such a speed until the e.m.f induced between the center and the rim is counter balanced by the potential difference across the resistor when the galvanometer shows no deflection

At this stage, the number of revolutions n in a given time t (s) are noted.

$$f = \frac{n}{t} \text{ revolution per second}$$

$$\text{Area } A \text{ of the disc} = \pi r^2$$

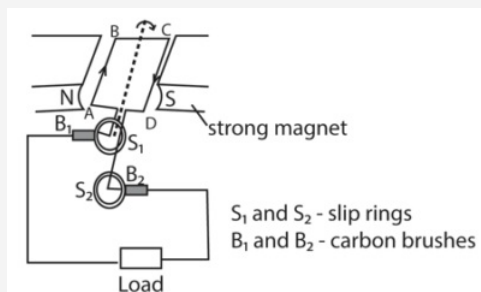
At no deflection the induced e.m.f in the disc, $BAf = IR$, where I is the current flowing through the coil

$$\text{But } B = \frac{\mu_0 NI}{L}$$

$$\therefore IR = \frac{\mu_0 NIAf}{L}$$

$$R = \frac{\mu_0 NIAf}{L}$$

The simple a.c generator



It consists of a rectangular coil of wire pivoted between opposite curve poles of a strong magnet and free to rotate about its axis with uniform angular velocity.

The ends of the coil are connected to two slip rings which press slightly against the carbon brushes connected to the load.

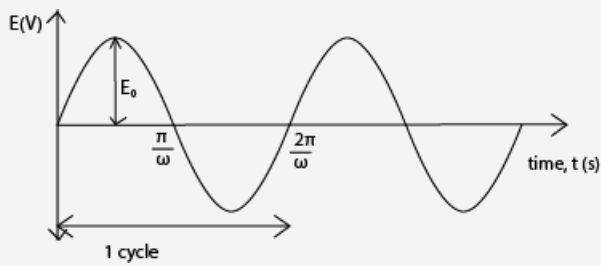
How it works

- The coil ABCD is rotated in a magnetic field, the magnetic field linked with it changes and hence e.m.f is induced away by means of slip rings which press slightly against the carbon brushes.
Applying Fleming's right hand rule, the induced current enters the coil AB and leaves the coil via CD.
- Starting with the coil in the vertical position, the magnetic flux linking it is maximum and hence no induced e.m.f.
- The induced e.m.f increases with the position of the coil in the magnetic field until it becomes maximum with the coil in horizontal position and then decreases to zero as the

coil rotates to the vertical position

- The force acting on the sides of the coil change as the coil passes over the position and hence the current flowing in the coil reverses. Hence an alternating e.m.f or current flows through the load.

A graph of induced e.m.f against time in an a.c generator



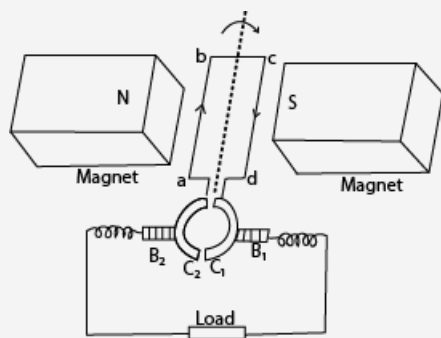
The main energy losses in a practical a.c. generator and how are they minimized?

Eddy current loss are minimized by laminating the armature

I^2R losses are minimized by use of low resistance winding wires

loss due to friction minimized by lubricating the rubbing parts

d.c. generator



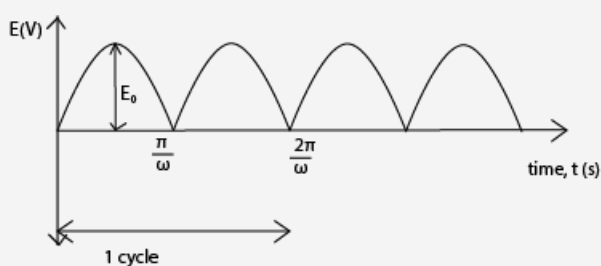
It consists of a rectangular coil $abcd$ of wire pivoted between curved poles of a strong magnet and free to rotate about its axis with a uniform velocity.

The ends of the coil are connected to two halves of split ring (commutators) which press lightly against the carbon brush.

Mode of action

When the coil rotates at uniform velocity in magnetic field, e.m.f is induced in it. When the coil is in vertical position, the commutators change brushes C_1 to B_2 and C_2 to B_1 . E.m.f reverses direction but the current does not change direction. Hence current flows in the same direction in a resistor.

A graph of induced e.m.f against time in a d.c generator



The peak value of induced e.m.f increases with increase in

The number of turns in the coil

The area of the coil

The strength of the magnetic field

The frequency of rotation of the coil

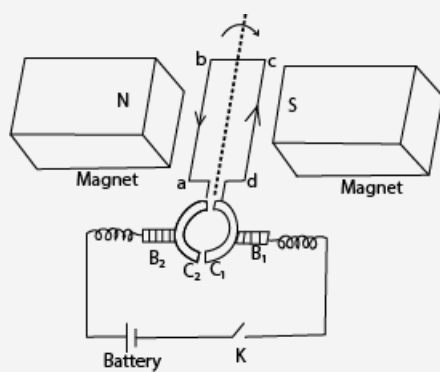
How to convert a d.c. generator be converted into an a.c. generator.

To convert a d.c. generator to an a.c. generator, the ends of the rectangular coil are connected to a pair of slip rings instead of the commutators.

How to convert an a.c. generator be converted into d.c. generator

To convert an a.c. generator to d.c. generator, the ends of the rectangular coil are connected to a pair of commutators instead of the slip rings.

A d.c motor



It consists of a rectangular coil abcd of wire pivoted between curved poles of a strong magnet and free to rotate about its axis with a uniform velocity.

The ends of the coil are connected to two halves of split ring (commutators) which press lightly against the carbon brush.

Mode of operation

The switch K is closed and current flows in the coil in the direction shown

Applying Fleming's left hand rule, ab experiences an upward force and side cd a downward force. The two forces constitute a couple which rotates the coil in a clockwise direction.

When the coil passes over the vertical position, the commutators change contact with the carbon brushes and current in the coil is immediately reversed. The force acting on the sides thus change and the coil continues to rotate in the same direction.

Because the conductor cuts the magnetic field, an e.m.f that oppose the supply voltage is induced in it called back e.m.f

If V is the supply voltage and E is the back e.m.f, then the current I_a is given by

$$I_a = \frac{V - E}{R_a} \text{ where } R_a \text{ is the armature resistance}$$

Back e.m.f and efficiency of the motor

When the armature coil of a motor rotates in magnetic field, an, e.m.f is induced in the coil. The induced e.m.f opposes the applied p.d. and is therefore a back e.m.f.

If V, E and r are applied p.d, induced e.m.f and resistance to the armature coil respectively, then the current flowing in the coil is given by

$$I = \frac{V-E}{r}$$

$$\Rightarrow V - E = Ir$$

Multiplying through by I

$$VI = EI + I^2r$$

Since I^2r is the power dissipated as heat in the armature, EI is the mechanical power output and VI is the power supplied.

$$\begin{aligned}\text{Efficiency of the motor, } \eta &= \frac{EI}{VI} \times 100\% \\ &= \frac{E}{V} \times 100\%\end{aligned}$$

Example 22

A motor whose armature resistance is 2Ω is operated on 240V mains supply. If the back e.m.f in the motor is 220V, calculate the armature current. (03marks)

$$I = \frac{V-E}{r} = \frac{240-220}{2} = 10A$$

Example 23

A transformer has 2000 turns in the primary coil. The primary coil is connected to a 240V mains. A 12 V, 36W lamp is connected to the secondary coil. If the efficiency of the transformer is 90%, determine the

(i) number of turns in the secondary coil (02marks)

$$N_s = \frac{V_s}{V_p} \times N_p = \frac{12}{240} \times 2000 = 100$$

(ii) current flowing in the primary coil (03marks)

$$I_s V_s = 0.9 I_p V_p$$

$$I_p = \frac{I_s V_s}{0.9 V_p} = \frac{36}{0.9 \times 240} = 0.167A$$

Example 24

Explain the significance of back e.m.f. in the operation of a d.c. motor (02marks)

The back e.m.f in a d.c. motor provides the useful power of the motor.

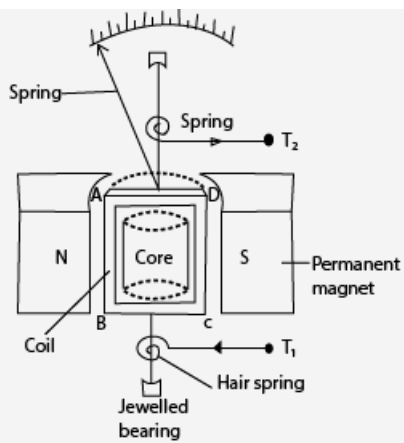
back e.m.f also reduces the heating effect in motor by reducing the current, since

$$I = \frac{V - E_b}{r} \text{ where } E_b = \text{back e.m.f}$$

Difference between a d.c generator and d.c motor

A d.c. generator converts mechanical energy into electrical energy while a d.c motor converts electrical energy into mechanical energy

Moving coil galvanometer.



Structure

It consists of a rectangular coil of fine insulated copper wire wound on an aluminium frame to provide electromagnetic damping.

The coil together with the frame of aluminium are mounted over a soft iron cylindrical core and freely pivoted on jeweled bearing to minimize friction at contact.

The suspension torsion wire suspending the coil is attached to a pair of control hair springs T1 and T2 for feeding current in and out of the coil and control rotation of the coil.

The coil is then suspended between concave pieces of a strong magnet to provide magnetic field.

Mode of action

Current I to be measured is passed into the coil via hair spring T1.

The current then causes the coil to experience a deflection torque, $\tau = NAB I$ due to a couple force causing rotation in a radial magnetic field.

The coil turns with the pointer through angle θ until stopped by restoring torque, $\tau = k\theta$ provided by a pair of hair springs T1 and T2.

At equilibrium, $NAB I = K\theta$

$$\therefore \text{current } I = \left(\frac{k}{NAB} \right) \theta$$

$I \propto \theta$, hence the instrument has a linear scale

Where B = magnetic field strength between the poles of the magnets

A = area of the plane of the coil

N = number of turns of the coil

k = torsion constant of suspension wire

The factors which affect the current sensitivity of a moving coil galvanometer

- Strength of magnet, current sensitivity is proportional to the strength of the magnets
- Number of turns, current sensitivity is proportional to the number of turns
- Nature of suspension torsion wire, current sensitivity is inversely proportional to the torsion constant of the suspension torsion wire.
- Area A of the plane of the coil; current sensitivity is proportional to the area of the plane of the coil
- Size of copper wire making the coil; current sensitivity is proportional to the size of copper wires making the coil since the bigger the wires the lower the resistance.

Example 25

Explain why a moving coil ammeter cannot be used to measure alternating current from the mains. (03marks)

The coil rotates about a vertical axis between the north and south concave poles of strong magnet. This provides a radial magnetic field. When an alternating current is passed through the coil, the torque on the coil reverses direction at the same frequency as current. The pointer vibrates with very small amplitude about the mean position hence a steady current reading cannot be taken

Example 26

Explain why a moving coil galvanometer should have a radial magnetic field, fine springs and many turns. (06marks)

Radial magnetic field ensures that the Force, F , remains normal to the plane of the coil when it turns through an angle i.e.

Torque on the coil $\tau = BANIsin\alpha$, where α is the angle between the normal to the coil and magnetic field this is balanced by restoring torque $= k\theta$ due to current, where θ is the angle turned through

$$\text{Thus, current sensitivity given by } \frac{\theta}{I} = \frac{BANIsin\alpha}{k}$$

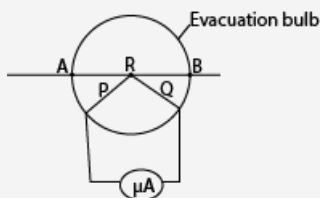
For a linear scale, $\sin \alpha = 1 \Rightarrow$ radial field

For current sensitivity, k must be small; i.e. the springs must be fine

For current sensitivity, N , must be large

Other a.c measuring instruments

Thermocouple ammeter



P and Q are dissimilar wires

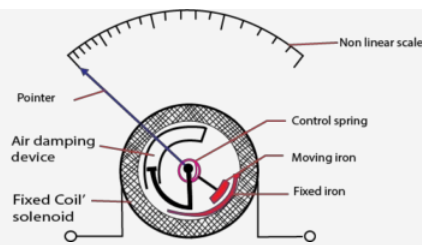
Current to be measured is passed through the wire AB and heats the junction R of the thermocouple. The thermoelectric effect generated at R causes a direct current to flow through the micrometer calibrated to measure the r.m.s value of current.

Example 27

Explain any precautionary measure taken in the design of thermocouple meter (02mark)

The fine wire is enclosed in an evacuated glass bulb to shield it from draughts. If the wire was in the open, some heat would be lost to the surrounding so that the temperature difference between the hot and cold junctions would not be proportional to the power dissipated in the wire.

The repulsion type moving iron meter.

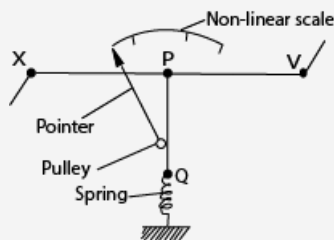


When a current is passed through the coil, the iron rods magnetize in the same poles adjacent to each other in whatever the direction of current. Hence they repel and the pointer move in the same direction until it is stopped by the restoring spring. Since the magnetic force is proportional to the square of the average current, hence, the deflection is proportional to the square of average current.

Advantage: it measured both direct and alternating current.

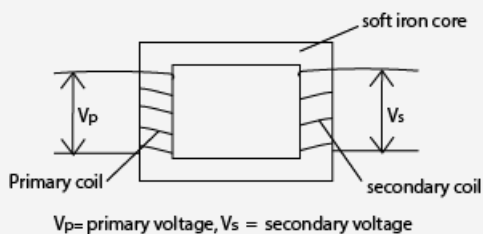
Disadvantage: it has nonlinear scale

A hot wire ammeter.



- The current flows through a fine resistance-wire XY, which it heats.
- The wire warms up to such a temperature that it loses heat-mainly by convection-at a rate equal to the average rate at which heat is developed in the wire.
- The rise in temperature of the wire makes it expand and sag; the sag is taken up by a second fine wire PQ, which is held taut by a spring.
- The wire PQ passes round a pulley attached to the pointer of the instrument, which rotates as the wire XY sags.
- The deflection of the pointer is roughly proportional to the average rate at which heat is developed in the wire XY; it is therefore roughly proportional to the average value of the square of the alternating current, and the scale is a square-law one.

The structure and action of a.c transformer.



Transformer consists of two coil of insulated wire, the primary and secondary wound on laminated soft iron core.

When alternating voltage, V_p is connected to primary coil, it drives alternating current in the primary coil.

The alternating current produces a varying magnetic flux ϕ_p that link the primary coils inducing a back e.m.f E_B in the primary.

The varying magnetic flux, ϕ_s links the secondary coil by mutual induction/inducing

alternating voltage, V_s in the secondary

$$V_p = N_p \frac{d\phi}{dt} \dots\dots\dots (i)$$
$$V_s = N_s \frac{d\phi}{dt} \dots\dots\dots (ii)$$

Eqn (i) \div Eqn (i)

$$\frac{V_p}{V_s} = \frac{N_p}{N_s}$$

When $N_s > N_p$ the transformer is a step up

$N_s < N_p$ the transformer is a step down

Example 28

Explain why the voltage at a generating power station must be stepped up to very high value for long distance transmission (03marks)

Transmission is at high voltage to reduce power loss

Note that

Power supplied, $P = IV$

$$I = \frac{P}{V}$$

Hence when V is high, I is small. From power loss, $P' = I^2R$, when I is small power loss is reduced.

Example 29

A transformer connected to a.c supply of peak voltage 240V is to supply a peak voltage of 9.0V to a mini-lighting system of resistance 5Ω . Calculate the

(i) r.m.s current supplied to the lighting system (02marks)

$$V_{r.m.s} = \frac{V_0}{\sqrt{2}}$$
$$I_{r.m.s} = \frac{V_{r.m.s}}{R} = \frac{V_0}{\sqrt{2}R}$$
$$= \frac{9.0}{5\sqrt{2}} = 1.27A$$

(ii) average power delivered to the lighting system. (02marks)

$$P = I^2R$$
$$= I_{r.m.s}^2 R$$
$$= (1.27)^2 \times 5$$
$$= 8.1W$$

Example 30

Explain why the current in the primary coil of a transformer increases when the secondary is connected to the load.

When load is connected to the secondary winding, a current flows in it. The current flows in such a direction as to reduce the back e.m.f in primary coil, hence the current increase

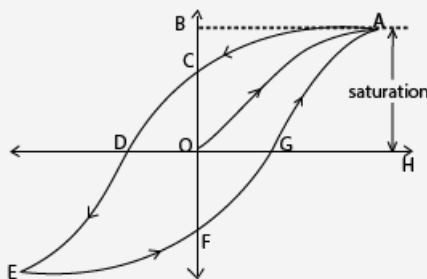
Energy losses in a transformer

- Heat dissipated in the windings by I^2R mechanism. This is minimized by use low resistance thick copper wires.

- Energy loss resulting from loss of flux or flux leakage. This is minimized by winding secondary coil on primary coil
- Eddy currents are minimized by laminating the core.
- loss due to friction minimized by lubricating the rubbing parts
- Hysteresis losses. When an alternating current is passes through the coil, wound on the core, the magnetic domain dipoles are forced to change directions according to changing magnetic flux created as a result of a.c. These changes of the domain dipoles require energy which is lost from the system. This energy loss is called hysteresis loss.

Hysteresis loss is minimized by using a core made of self-magnetic substance which requires very little energy to create magnetic reversal e.g. soft iron below the hysteresis curve of a ferromagnetic substance

A graph, explain the hysteresis curve for ferromagnetic material



- When a magnetic field is applied to a ferromagnetic material, the magnetic domains tend to align with the applied field. The magnetic flux density increases along OA until saturation.
- When the magnetizing field is reduced to zero, there is residue magnetization at C. This is due to failure of the dipoles to respond instantly. Energy is lost.
- To bring the dipoles to their original orientation, a magnetic field OD is applied in opposite direction. As the magnetic field is increased in this reversed direction, saturation is attained at E
- When reversed magnetic field is reduced to zero, state F is attained. Reversal of dipoles requires an increase of magnetic field in opposite direction to state EF. The cycle is then repeated on further increase of magnetic field
- The curve of B verses H is called a hysteresis curve

Uses of transformers

A transformer is used to step up or down voltage to suit the required appliance.

The appliances that may require a transformer include telephone, radios, loud speakers, x-ray machines. T.Vs and so on.

Eddy currents

If a block of metal is moved in a magnetic field or kept in changing magnetic field, free electrons in the conductor experience a force and begin to circulate.

This gives rise to induced currents in a closed circular path known as eddy currents.

These currents flow in such a direction so as to oppose the motion of a conductor in the field.

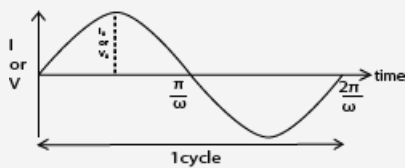
Eddy currents produce large amounts of heat in the soft iron core of transformers,

induction coils, electronics and thus reduce efficiency of electrical devices.

Uses of eddy currents

1. Damp oscillations in a moving coil galvanometer preventing oscillation of the pointer and leading to accurate reading
2. Eddy currents produce enough heat to melt metals in induction furnace.
3. Electric brakes: the axle of a train is surrounded by a coaxial cylindrical drum. When the train is to be stopped, a strong magnetic field is applied to the rotating drum. This generates large eddy currents that oppose motion of axle.
4. Speedometer, eddy current are used in speedometer

Sinusoidal a.c Currents



Terminologies

An alternating current or voltage

It is the voltage or current whose magnitude and direction varies periodically with time.

NB. Its variations with time can be represented by sine curve or wave and it is sometimes referred to as a sinusoidal current or voltage.

Example 31

What is meant by a sinusoidal voltage?

A sinusoidal voltage is a voltage whose variation with time can be represented by a sine curve.

Peak value/ amplitude

It is the maximum current or voltage of an alternating current.

NB: peak values are denoted by V_0 , V_m , I_0 or I_m .

Root mean squared value (r.m.s)

It is a steady current or voltage that would dissipate heat in a given resistor at the same rate as the alternative current or voltage.

$$I_{r.m.s} = \frac{I_0}{\sqrt{2}} \text{ and } V_{r.m.s} = \frac{V_0}{\sqrt{2}}$$

Period, T

It is the time taken to complete one cycle

Frequency, f

It is the number of cycles per second

$$f = \frac{1}{T}$$

a.c wave equation

The sinusoidal wave equation for a.c are represented by

$$V = V_0 \sin \omega t \text{ and,}$$

$$I = I_0 \sin \omega t$$

Where I_0 and V_0 are the peak alternating current or voltage

$$\text{But } \omega = \frac{2\pi}{T} \text{ and } T = \frac{1}{f}$$

$$\therefore \omega = 2\pi f$$

$$\therefore \omega = 2\pi f$$

Thus the wave equations can be written as

$$V = V_0 \sin 2\pi f t \text{ and,}$$

$$I = I_0 \sin 2\pi f t$$

From Ohm's law

$$V = IR$$

$$R = \frac{V_{r.m.s}}{I_{r.m.s}}$$

Example 32

Show that the r.m.s value of an alternating voltage is $V_{r.m.s} = \frac{V_0}{\sqrt{2}}$, where V_0 is the peak voltage (03marks)

$$\text{Instantaneous power} = \frac{V^2}{R}, \text{ where } V = V_0 \sin \omega t$$

$$P_{\text{inst}} = \frac{V_0^2 \sin^2 \omega t}{R}$$

$$\text{Average power, } P = \frac{V_0^2 \sin^2 \omega t}{R}$$

$$\text{But } \sin^2 \omega t = \frac{1}{2}$$

$$\text{For steady voltage, } P = \frac{V_{r.m.s}^2}{2R}$$

$$\Rightarrow \frac{V^2}{R} = \frac{V_{r.m.s}^2}{2R}$$

$$\text{Hence } V_{r.m.s} = \frac{V_0}{\sqrt{2}}$$

Example 33

A sinusoidal alternating voltage $V = 170 \sin 120\pi t$, voltage, is applied across a resistor of resistance 100Ω

Determine

(i) The r.m.s value of current which flows. (03marks)

$$I_{r.m.s} = \frac{V_{r.m.s}}{R} \text{ but } \frac{V_0}{\sqrt{2}}$$

$$\therefore I_{r.m.s} = \frac{V_0}{R\sqrt{2}} = \frac{170}{100\sqrt{2}} = 1.2 \text{ A}$$

(ii) The frequency of the current through the resistor. (02marks)

$$\omega = 2\pi f; \omega = 120\pi$$

$$\therefore f = \frac{\omega}{2\pi} = \frac{120\pi}{2\pi} = 60\text{Hz}$$

A capacitor in an a.c circuit

Consider a capacitor C farads in an a.c circuit as shown below

Assume a sinusoidal voltage

$$V = V_0 \sin \omega t \dots\dots\dots (i)$$

Across the capacitor plates from definition of capacitor.

The instantaneous charge Q on plates is

$$Q = CV \dots\dots\dots (ii)$$

Putting (i) into (ii)

$$Q = C V_0 \sin \omega t \dots\dots\dots (iii)$$

From definition of current

$$I = \frac{dQ}{dt} \text{ (rate of charge flow)}$$

$$I = \frac{d(CV_0 \sin \omega t)}{dt} \dots\dots\dots (iv)$$

$$I = \omega C V_0 \cos \omega t \dots\dots\dots (v)$$

Putting $\omega C V_0 = I_0$

$$I = I_0 \cos \omega t$$

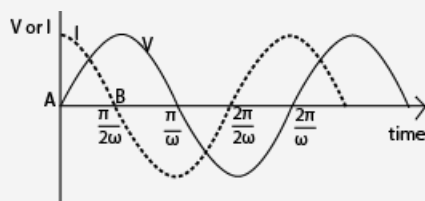
From trigonometry, $\cos \theta = \sin (\theta + \frac{\pi}{2})$

$$\therefore I = I_0 \sin (\omega t + \frac{\pi}{2})$$

$$= \omega C V_0 \sin (\omega t + \frac{\pi}{2})$$

Hence the current leads the voltage by a phase angle of $\frac{\pi}{2}$

Variation of V and I against time



Explanation of the curve

- The current I through (not across) a capacitor is $C \frac{dV}{dt}$. This is the slope of the voltage.
- When a capacitor is connected to an AC voltage (at the zero crossing) the maximum current flow will occur immediately, i.e. $t = 0$, $\frac{dV}{dt}$ will approach infinity instantly and then repeat as a sinusoidal waveform.
- There will be a peak current at every zero crossing of the voltage waveform. The current waveform will lead the voltage waveform 90 degrees.

Reactance

This is the non-resistive opposition to the flow of alternating current in either a capacitor or an inductor.

Greater reactance leads to smaller currents for the same applied voltage. Reactance is similar to electric resistance, although it differs in several respects

Reactance of a capacitor (capacitive reactance)

It's denoted by X_c .

$$\text{Definition, } X_c = \frac{V_0}{I_0} \text{ or } X_c = \frac{V_{r.m.s}}{I_{r.m.s}}$$

Derivation of an expression for reactance of a capacitor

Assume a sinusoidal voltage;

$$V = V_0 \sin \omega t \dots\dots\dots (i)$$

Across capacitor's plates; the instantaneous charge Q is

$$Q = CV \dots\dots\dots (ii)$$

$$Q = CV_0 \sin \omega t \dots\dots\dots (iii)$$

From definition of current,

$$I = \frac{dQ}{dt} \text{ (rate of charge flow) } \dots\dots\dots (iv)$$

$$I = \frac{d(CV_0 \sin \omega t)}{dt} \dots\dots\dots (v)$$

$$I = \omega CV_0 \cos \omega t \dots\dots\dots (vi)$$

$$\text{But } \omega CV_0 = I_0 \dots\dots\dots (vii)$$

From definition

$$\begin{aligned} \text{Capacitance reactance, } X_c &= \frac{V_0}{I_0} \\ &= \frac{V_0}{\omega CV_0} \\ &= \frac{1}{\omega C} \end{aligned}$$

$$\text{But } \omega = 2\pi f$$

$$\therefore X_c = \frac{1}{2\pi fC}$$

Example 34

A sinusoidal voltage of r.ms value 13.2V is connected across a 50 μ F capacitor.

(i) Find peak value of the charge on the capacitor (02marks)

$$Q_0 = CV_0 \text{ but } V_0 = V_{r.m.s} \times \sqrt{2}$$

$$\text{Hence } Q_0 = CV_{r.m.s} \times \sqrt{2}$$

$$= 50 \times 10^{-6} \times 13.2 \times \sqrt{2}$$

$$= 9.333 \times 10^{-6} \text{C}$$

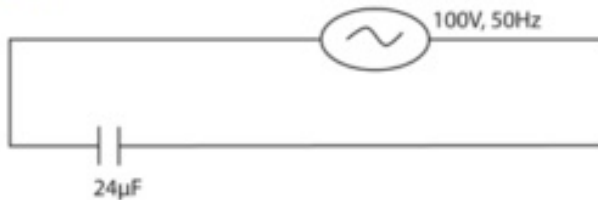
(iii) If the frequency of the alternating current is 49.6Hz, calculate the r.m.s value of current through the capacitor. (03marks)

$$\frac{V_{r.m.s}}{I_{r.m.s}} = \frac{1}{2\pi fC} = X_C$$

$$I_{r.m.s} = V_{r.m.s} \times 2\pi fC$$

$$= 13.2 \times 2\pi \times 49.6 \times 50 \times 10^{-6} = 0.206 \text{A}$$

Example 35



A 100V, 50Hz a.c. supply is connected across a capacitor of 24μF as shown in figure above. Calculate the reactance of the circuit (03marks)

$$\text{Capacitive reactance, } X_C = \frac{1}{2\pi fC} = \frac{1}{2\pi \times 50 \times 24 \times 10^{-6}} = 132.6\Omega$$

Example 36

A capacitor of capacitance 60μF is connected to an a.c. voltage supply of frequency 40Hz. An a.c. ammeter connected in series with the capacitor reads 2.2A. Find the p.d across the capacitor. (03marks).

$$X_C = \frac{I}{2\pi fC} = \frac{1}{2\pi \times 40 \times 60 \times 10^{-6}}$$

$$\text{Voltage, } V_{r.m.s} = I_{r.m.s} \times X_C$$

$$= \frac{2.2 \times 1}{2\pi \times 40 \times 60 \times 10^{-6}}$$

$$= 146 \text{V}$$

Example 37

A sinusoidal p.d of r.m.s value of 20V and frequency 50Hz is applied across a 100μF capacitor. Calculate the capacitive reactance of the circuit. (02 marks)

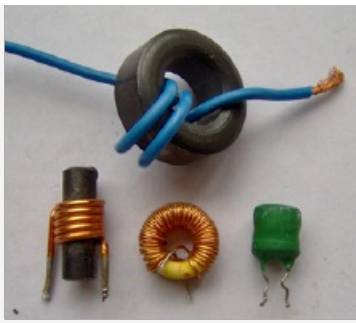
$$X_C = \frac{1}{2\pi fC} = \frac{1}{2\pi \times 50 \times 100 \times 10^{-6}} = 31.8\Omega$$

a.c through an inductor

An inductor, also called a coil, choke, or reactor, is a passive two-terminal electrical component that stores energy in a magnetic field when electric current flows through it.

An inductor typically consists of an insulated wire wound into a coil

Example of inductors



Example 38

Show that in a coil placed in an a.c circuit, the voltage across the coil leads the current by a phase angle of $\pi/2$ radian or 90°

Instantaneous voltage, $V = V_0 \sin 2\pi f t$,

$$E_s = -L \frac{dI}{dt}$$

But for finite current, $V = -E_s$

$$V = \frac{L dI}{dt}, \text{ but } V = V_0 \sin 2\pi f t,$$

$$\frac{dI}{dt} = \frac{-V_0}{L} \sin 2\pi f t$$

$$\int dI = \frac{V_0}{L} \int \sin 2\pi f t dt$$

$$I = \frac{-V_0}{2\pi f t L} \cos 2\pi f t$$

From trigonometry, $\cos \theta = \sin (\theta + \frac{\pi}{2})$

$$I = \frac{-V_0}{2\pi f t L} \sin (2\pi f t + \frac{\pi}{2})$$

$$\Rightarrow I \text{ lags } V \text{ by } \frac{\pi}{2} \text{ or } 90^\circ$$

(ii) Using the axes, sketch graphs to show the relative phases of the current and voltage across the inductor. (02marks)



Note that the current starts at zero and rises to its peak after the voltage that drives it, i.e., the voltage across an inductor leads the current because the Lenz's Law behavior resists the build up of current and it takes a finite time for an imposed voltage to force the buildup of current to its maximum.

Derivation of an expression for reactance of an inductor

Method I

$$\text{Induced e.m.f} = -L \frac{dI}{dt}$$
$$E = -L \frac{d(I_0 \sin \omega t)}{dt} = -\omega L I_0 \cos \omega t$$

Current flow in a pure inductor, $V = -E \omega L I_0 \cos \omega t$

Hence $V = V_0 \cos \omega t$ where $V_0 = \omega L I_0$

$$\text{Inductance} = X_L = \frac{V_0}{I_0} = \frac{\omega L I_0}{I_0} = \omega L$$

Method II

$$V = V_0 \cos \omega t$$
$$\text{Induced e.m.f } E = -L \frac{dI}{dt}$$

Since the inductor is a coil of zero resistance (for finite current) $V = -E$

$$V_0 \cos \omega t = L \frac{dI}{dt}$$
$$dI = \frac{V_0}{L} \cos \omega t \cdot dt$$
$$\int dI = \frac{V_0}{L} \int \cos \omega t \cdot dt$$
$$I = \frac{V_0}{L} \sin \omega t$$

But $I_0 = \frac{V_0}{\omega L}$

$$I = I_0 \sin \omega t$$
$$X_L = \frac{V_0}{I_0} = \frac{V_0}{V_0 / \omega L} = \omega L$$

Ballistic galvanometer

It is also called a moving coil galvanometer used for estimating the quantity of charge flow whose deflection of the coil is directly proportional to the charge that passes through it.

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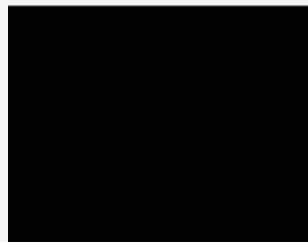
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