

# Mathematics Formula

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## Algebra Formula

- $(a + b)^2 = a^2 + 2ab + b^2$
- $(a - b)^2 = a^2 - 2ab + b^2$
- $a^2 + b^2 = (a + b)^2 - 2ab$
- $a^2 + b^2 = (a - b)^2 + 2ab$
- $(a + b)^3 = a^3 + b^3 + 3ab(a + b)$
- $(a - b)^3 = a^3 - b^3 - 3ab(a - b)$
- $a^3 + b^3 = (a + b)^3 - 3ab(a + b)$

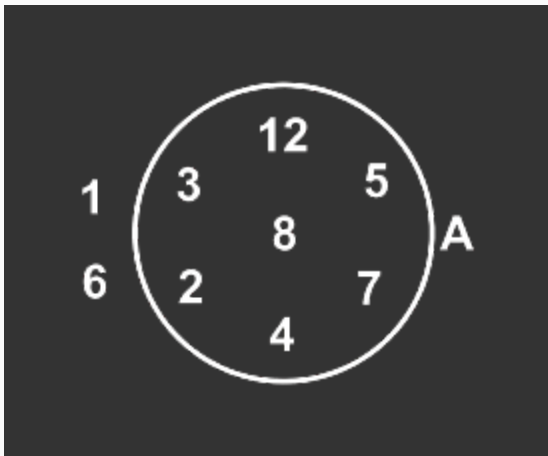
- $a^3 - b^3 = (a - b)^3 + 3ab(a - b)$
- $a^2 - b^2 = (a + b)(a - b)$
- $a^3 - b^3 = (a - b)(a^2 + ab + b^2)$
- $a^3 + b^3 = (a + b)(a^2 - ab + b^2)$
- $a^4 - b^4 = (a^2 - b^2)(a^2 + b^2) = (a + b)(a - b)(a^2 + b^2)$
- $a^4 + b^4 = (a^2 + b^2)^2 - 2a^2b^2 = (a^2 + \sqrt{2}ab + b^2)(a^2 - \sqrt{2}ab + b^2)$
- $a^5 + b^5 = (a + b)(a^4 - a^3b + a^2b^2 - ab^3 + b^4)$
- $a^5 - b^5 = (a - b)(a^4 + a^3b + a^2b^2 + ab^3 + b^4)$
- $a^n - b^n = (a - b)(a^{n-1} + a^{n-2}b + a^{n-3}b^2 + \dots + b^{n-1})$
- $(a + b + c)^2 = a^2 + b^2 + c^2 + 2(ab + bc + ca)$

- $a^3 + b^3 + c^3 - 3abc = (a + b + c)(a^2 + b^2 + c^2 - ab - bc - ca)$

If  $a + b + c = 0$ , then the above identity reduces to  $a^3 + b^3 + c^3 = 3abc$

## Statistics Math Formulas

### SETS :



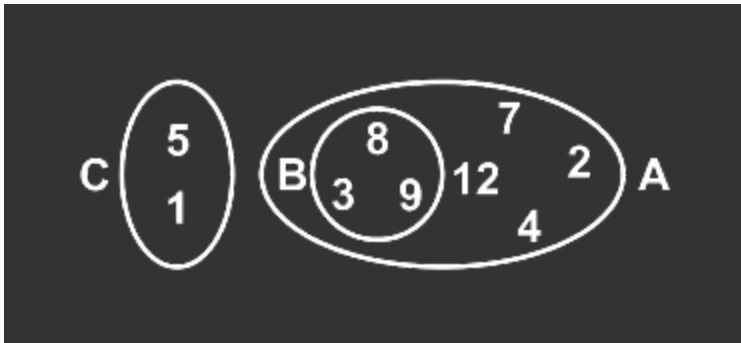
$$A = \{2, 3, 4, 7, 8, 9, 12\}$$

$$3 \in A$$

$5 \notin A$

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## SUBSET:



$$B = \{3, 8, 9\} \Rightarrow B \subseteq A$$

$$C = \{1, 5\} \Rightarrow C \not\subseteq A$$

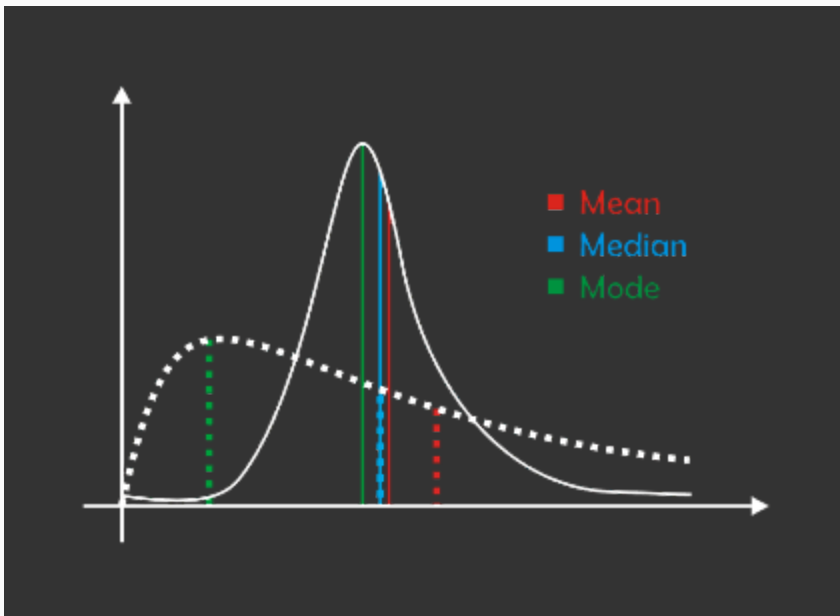
## STATISTICS :

**MEAN :** The mean value is obtained the arithmetic mean or average of a set of numbers

is expected value.

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The mean value is calculated by adding up all the values, and then dividing that sum by the number of values .



Mean = Sum of all data values / Number of data values

Symbolically ,

Where  $\bar{x}$  (read as "x bar") is the mean of the set of x values,  $\sum x$  is the sum of all the x values, and n is the number of x values.

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**MEDIAN** : The median is the middle value in a set of values. So to find the median you need to order the numbers from largest to smallest and then you have to choose the value in the middle.

**MODE** : Mode is the value that the highest frequency in the data set. means values that occur most frequently and there can be more than one mode in a set.

**numerical value that occurs most of the times.**

$$F(X_{\text{mode}}) = \max$$

## **INTERSECTION :**



In intersection  $A \cap B$  of two sets A and B is the set that contains all elements of B also belong to A (or similarly all elements of B that also belong to A) but no other elements. The symbol intersection is inverted U.

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If Set A contain element  $A = \{1, 2, 3\}$  and set B contains  $B = \{2, 3, 4\}$  and the element in having common are 2 and 3 and this intersection area formed a new set containing 2 and 3.

## UNION :



The union of two sets A and B includes all elements which are members of either A or B. If sets A and B have any elements in common then this elements which are members of both sets are only include one in the union.



**For example :** If sets A contains the elements

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1,2, and 3 and set B contains 2,3 and 4 the elements which are members of A or B are 1,2,3 and 4. This form a new set containing 1,2,3 and 4. when we write the union 2 and 3 are only listed once.

## **RELATIVE COMPLEMENT OF A IN B :**

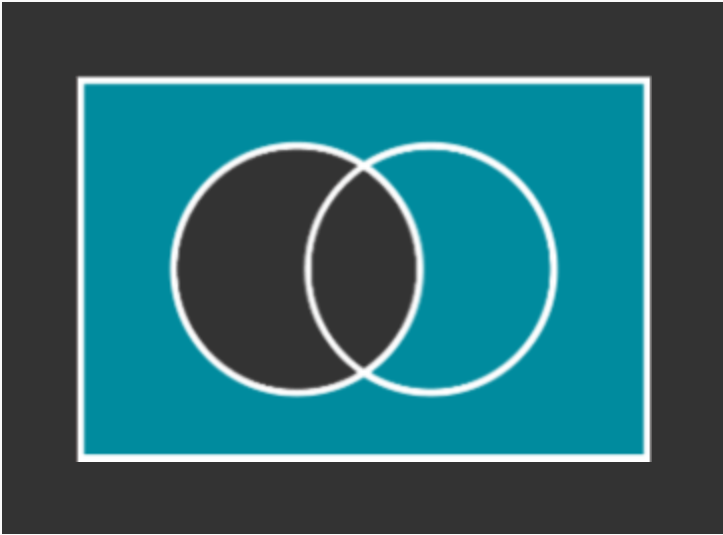


The relative complement of A in B denoted,  $B \setminus A$ , is the set of elements in B but not in A.

Symbolically :  $B \setminus A = \{x \mid x \in B \wedge x \notin A\}$

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## ABSOLUTE COMPLEMENT :



In a Set theory a complement of a set A refers to things not in A.

# SYMMETRIC DIFFERENCE:

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## Operations on sets :

$$A \cup A = A$$

$$A \cap A = A$$

$$A \cup B = B \cap A$$

$$A \cap B = B \cap A$$

$$(A \cup B) \cup C = A \cup (B \cup C)$$

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$$(A \cap B) \cap C = A \cap (B \cap C)$$

$$U' = \emptyset$$

$$(A')' = A$$

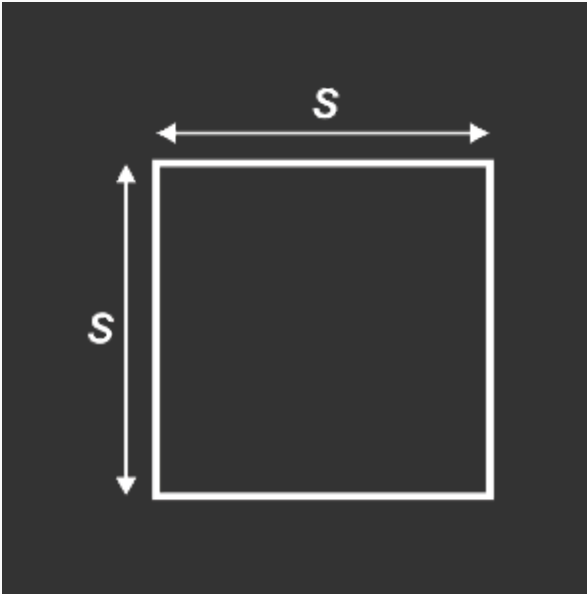
$$A \cap \emptyset = \emptyset$$

$$A \cap U = A$$

$$A \cap A' = \emptyset$$

$$(A \cup B)' = A' \cap B'$$

$$(A \cap B)' = A' \cup B'$$



**P = Perimeter**

**A = Area**

**S = Side**

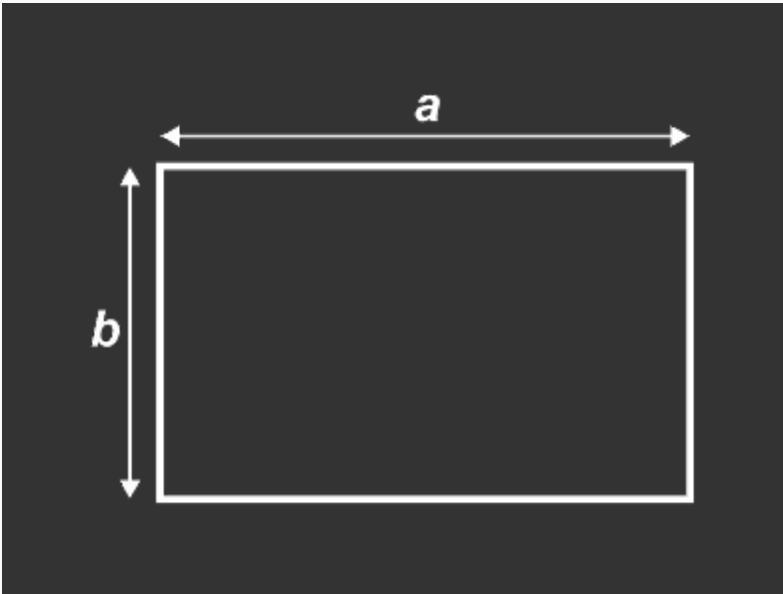
**d = diameter**

$$P = 4 \times s$$

$$A = S^2$$

$$d = a \times \sqrt{2}$$

# Rectangle



**P = Perimeter**

**A = Area**

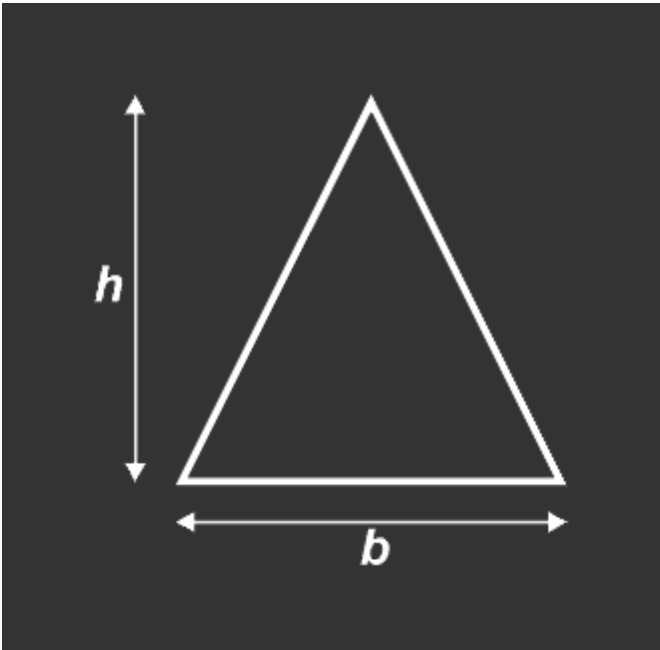
**d = diameter**

$$P = 2 \times (a + b)$$

$$A = a \times b$$

$$d = \sqrt{a^2 + b^2}$$

# Triangle



$P = \text{Perimeter}$

$A = \text{Area}$

$$P = a + b + c$$

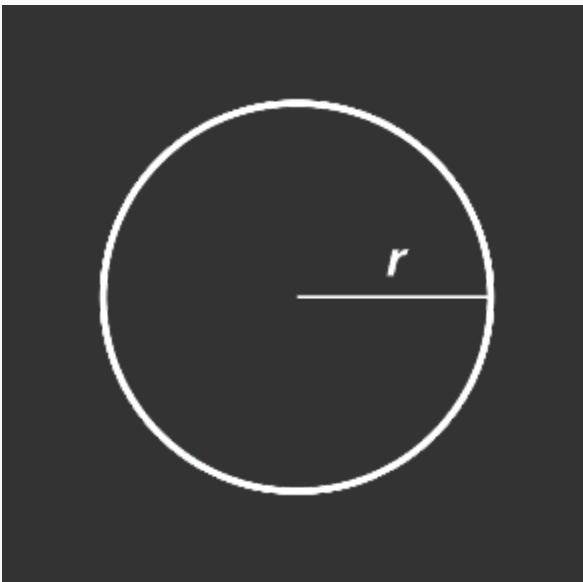
$$A = b \times h / 2$$

$$A = \sqrt{s(s-a)(s-b)(s-c)};$$

$s = \frac{a + b + c}{2} = \frac{p}{2}$ . Visit [www.eduNgr.com](http://www.eduNgr.com) for career and educational resources, guides and tips.

$$\alpha + \beta + \gamma = 180^\circ$$

## Circle



P = Perimeter

A = Area



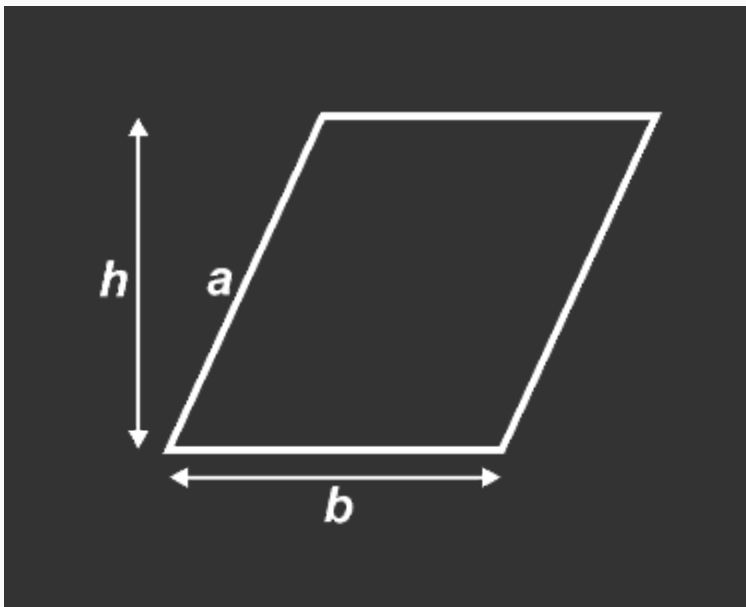
$$P = 2\pi r$$

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$$A = \pi r^2$$

$$\pi = 3.14$$

## Parallelogram



$$P = (a + b) \times 2$$

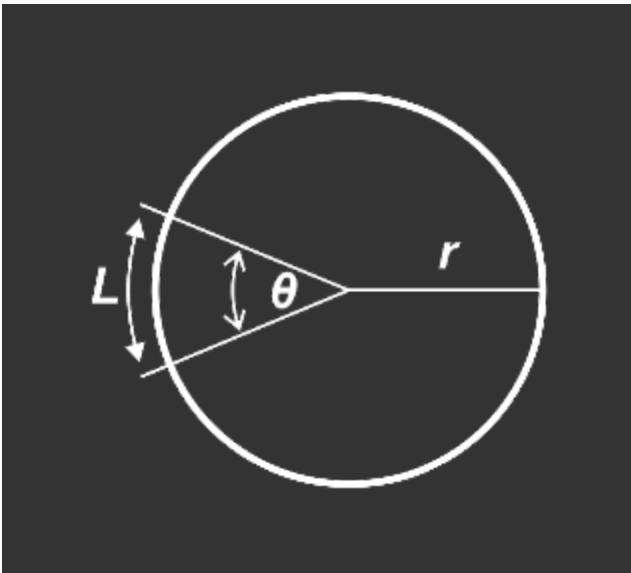
$$P = 2a + 2b$$

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$$A = bh = ab \sin \alpha$$

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## Circular Sector

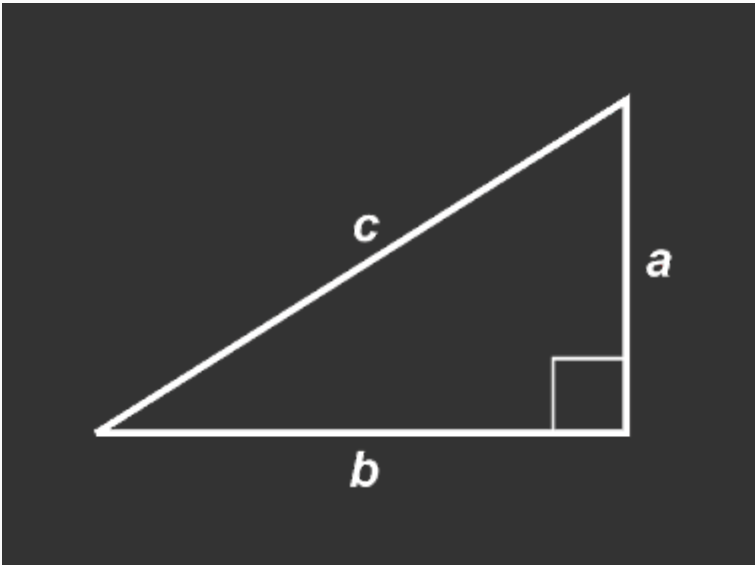


$$L = \pi r = \theta / 180^{\circ}$$

$$A = \pi r^2 \theta / 360^{\circ}$$

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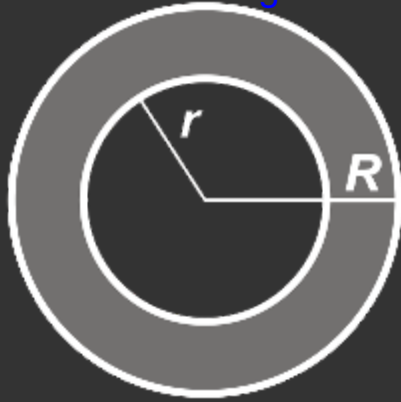
## Pythagorean Theorem :



$$a^2 + b^2 = c^2$$

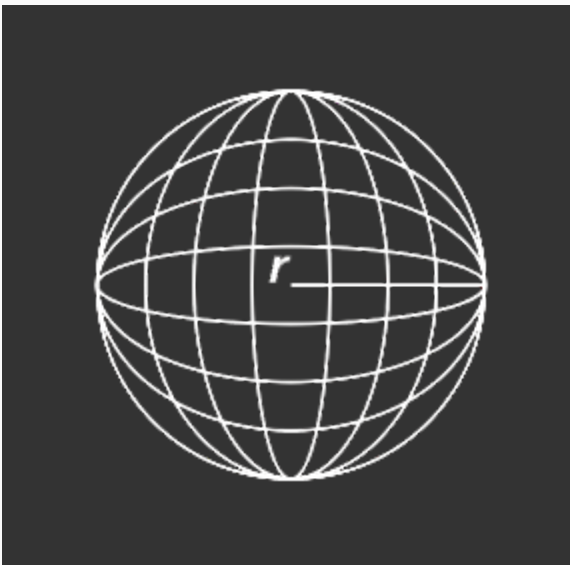
$$c = \sqrt{a^2 + b^2}$$

## Circular Ring



$$A = \pi (R^2 - r^2)$$

## Sphere

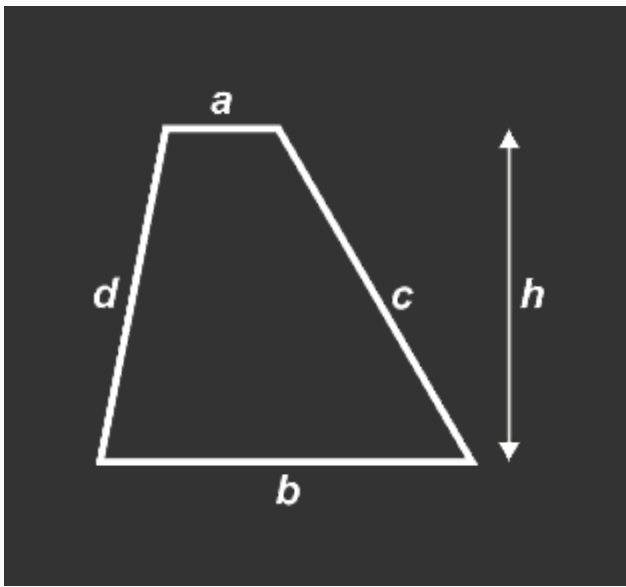


$$S = 4\pi r^2$$

$$V = \frac{4\pi r^2}{3}$$

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## Trapezoid

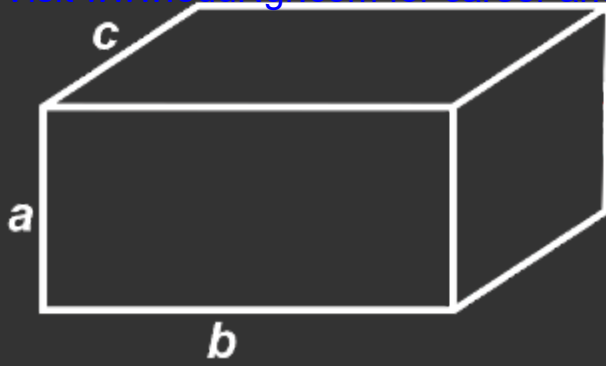


$$P = a + b + c + d$$

$$A = h \times a + b / 2$$

## Rectangular Box

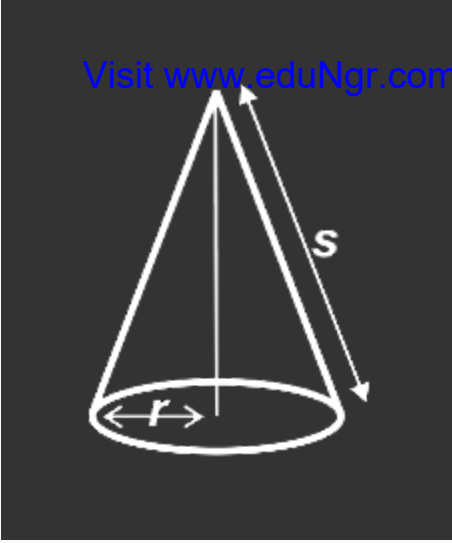
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$$A = 2ab + 2ac + 2bc$$

$$V = abc$$

## **Right Circular Cone :**

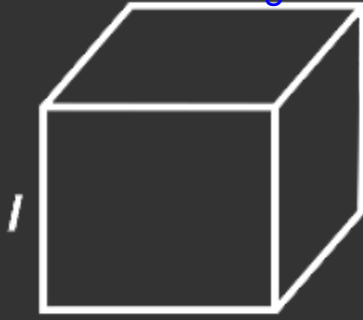


$$A = \pi r^2 + \pi r s$$

$$S = \sqrt{r^2 + h^2}$$

$$V = 1 \times \pi r^2 h / 3$$

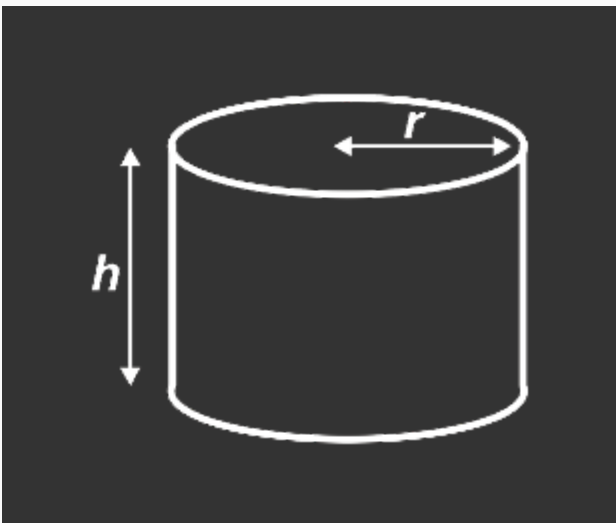
## Cube



$$A = 6l^2$$

$$V = l^3$$

## Cylinder



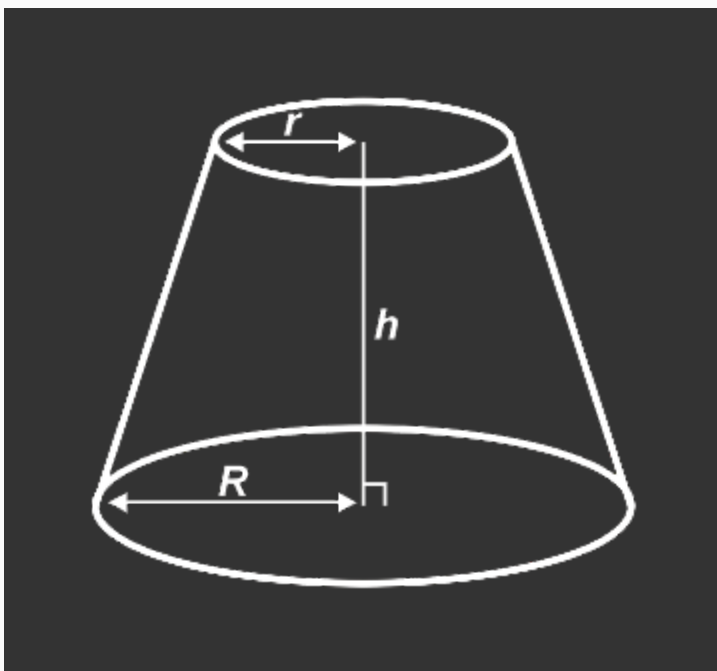
$$A = 2\pi r(r + h)$$



$$V = \frac{1}{3} \pi r^2 h$$

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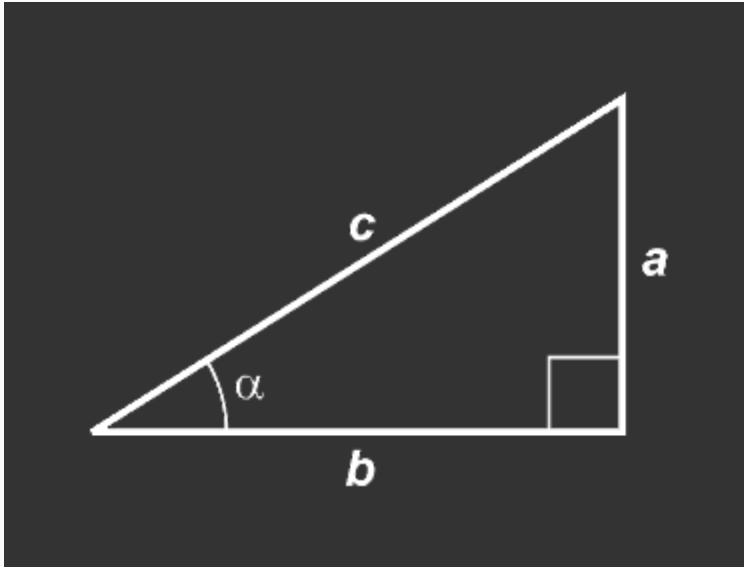
## Frustum of a Cone



$$V = \frac{1}{3} \pi h (r^2 + rR + R^2)$$

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## Trigonometry Function Formulas of a Right Triangle :



$$\sin \alpha = a / c = \text{opposite} / \text{hypotenuse}$$

$$\cos \alpha = b / c = \text{adjacent} / \text{hypotenuse}$$

$$\tan \alpha = a / b = \text{opposite} / \text{adjacent}$$

$$\cot \alpha = b / a = \text{adjacent} / \text{opposite}$$

$$\sec \alpha = c / b$$

$$\operatorname{Cosec} \alpha = c / a$$

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## **Basic Formula :**

$$\sin^2 \alpha + \cos^2 \alpha = 1$$

$$\tan \alpha \cdot \cot \tan \alpha = 1$$

$$\tan \alpha = \sin \alpha / \cos \alpha = 1 / \cot \tan \alpha$$

$$\cot \tan \alpha = \cos \alpha / \sin \alpha = 1 / \tan \alpha$$

$$1 + \tan^2 \alpha = 1 / \cos^2 \alpha = \sec^2 \alpha$$

$$1 + \cot \tan^2 \alpha = 1 / \sin^2 \alpha = \operatorname{cosec}^2 \alpha$$

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# Trigonometric Table

$\alpha$	$0^0$	$30^0$	$45^0$	$60^0$	$90^0$	$120^0$	$180^0$	$270^0$	$360^0$
$\sin \alpha$	0	$1/2$	$\sqrt{2}/2$	$\sqrt{3}/2$	1	$\sqrt{3}/2$	0	-1	0
$\cos \alpha$	1	$\sqrt{3}/2$	$\sqrt{2}/2$	$1/2$	0	$-1/2$	-1	0	1
$\tan \alpha$	0	$1/\sqrt{3}$	1	$\sqrt{3}$	$\infty$	$-\sqrt{3}$	0	$\infty$	0
$\cot \alpha$	$\infty$	$\sqrt{3}$	1	$1/\sqrt{3}$	0	$-1/\sqrt{3}$	$\infty$	0	$\infty$
$\sec \alpha$	1	$2/\sqrt{3}$	$\sqrt{2}$	2	$\infty$	-2	-1	$\infty$	1
$\operatorname{cosec} \alpha$	$\infty$	2	$\sqrt{2}$	$2/\sqrt{3}$	1	$2/\sqrt{3}$	$\infty$	-1	$\infty$

## Co-Ratios

	<b>sin</b>	<b>cos</b>	<b>tan</b>	<b>cot</b>
$-\alpha$	$-\sin \alpha$	$+\cos \alpha$	$-\tan \alpha$	$-\cot \alpha$
$90^0 - \alpha$	$+\cos \alpha$	$+\sin \alpha$	$+\cot \alpha$	$+\tan \alpha$
$90^0 + \alpha$	$+\cos \alpha$	$-\sin \alpha$	$-\cot \alpha$	$-\tan \alpha$
$180^0 - \alpha$	$+\sin \alpha$	$-\cos \alpha$	$-\tan \alpha$	$-\cot \alpha$
$180^0 + \alpha$	$-\sin \alpha$	$-\cos \alpha$	$+\tan \alpha$	$+\cot \alpha$
$270^0 - \alpha$	$-\cos \alpha$	$-\sin \alpha$	$+\cot \alpha$	$+\tan \alpha$
$270^0 + \alpha$	$-\cos \alpha$	$+\sin \alpha$	$-\cot \alpha$	$-\tan \alpha$
$360^0 k - \alpha$	$-\sin \alpha$	$+\cos \alpha$	$-\tan \alpha$	$-\cot \alpha$
$360^0 k + \alpha$	$+\sin \alpha$	$+\cos \alpha$	$+\tan \alpha$	$+\cot \alpha$

# Trigonometry Addition

## Formula:

- $\sin(A + B) = \sin A \cos B + \cos A \sin B$
- $\sin(A - B) = \sin A \cos B - \cos A \sin B$
- $\cos(A + B) = \cos A \cos B - \sin A \sin B$
- $\cos(A - B) = \cos A \cos B + \sin A \sin B$
- $\tan(A + B) = \frac{\tan A + \tan B}{1 - \tan A \tan B}$
- $\tan(A - B) = \frac{\tan A - \tan B}{1 + \tan A \tan B}$

- $\cot(A+B) = \cot A \cot B - 1 / \cot A + \cot B$ .  
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## Product of Trigonometric Functions:

- $\sin \alpha \cos \beta = 1/2 [\sin(\alpha + \beta) + \sin(\alpha - \beta)]$
- $\cos \alpha \cos \beta = 1/2 [\cos(\alpha + \beta) + \cos(\alpha - \beta)]$
- $\sin \alpha \sin \beta = 1/2 [\cos(\alpha - \beta) - \cos(\alpha + \beta)]$

- $\tan \alpha \tan \beta = \tan \alpha + \tan \beta / \cot \tan \alpha + \cot$

$$\tan \beta = - \tan \alpha - \tan \beta / \cot \tan \alpha - \cot \tan \beta$$

Trigonometric Formula with  $t = \tan(x/2)$

$$\sin x = 2t / 1 + t^2$$

$$\cos x = 1 - t^2 / 1 + t^2$$

$$\tan x = 2t / 1 - t^2$$

$$\cot x = 1 - t^2 / 2t$$

# Trigonometric

## Relation Between Functions:

	$\sin \alpha$	$\cos \alpha$	$\tan \alpha$	$\cot \alpha$
$\sin \alpha =$		$\pm \sqrt{1 - \cos^2 \alpha}$	$\pm \frac{\tan \alpha}{\sqrt{1 + \tan^2 \alpha}}$	$\pm \frac{1}{\sqrt{1 + \cot^2 \alpha}}$
$\cos \alpha =$	$\pm \sqrt{1 - \sin^2 \alpha}$		$\pm \frac{1}{\sqrt{1 + \tan^2 \alpha}}$	$\pm \frac{\cot \alpha}{\sqrt{1 + \cot^2 \alpha}}$
$\tan \alpha =$	$\pm \frac{\sin \alpha}{\sqrt{1 - \sin^2 \alpha}}$	$\pm \frac{\sqrt{1 - \cos^2 \alpha}}{\cos \alpha}$		$\frac{1}{\cot \alpha}$
$\cot \alpha =$	$\pm \frac{\sqrt{1 - \sin^2 \alpha}}{\sin \alpha}$	$\pm \frac{\cos \alpha}{\sqrt{1 - \cos^2 \alpha}}$	$\frac{1}{\tan \alpha}$	



# Angle of a Plane Triangle :

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- A, B, C are 3 angles of a triangle
- $\sin A + \sin B + \sin C = 4 \cos(A/2) \cos(B/2) \cos(C/2)$
- $\cos A + \cos B + \cos C = 4 \sin(A/2) \sin(B/2) \sin(C/2) + 1$
- $\sin A + \sin B - \sin C = 4 \sin(A/2) \sin(B/2) \cos(C/2)$

## Sources

Visit the sources:

- [math-shortcut-tricks.com](http://math-shortcut-tricks.com)
- [byjus.com/math-formulas](http://byjus.com/math-formulas)
- [mathportal.org/mathformulas.php](http://mathportal.org/mathformulas.php)