

UGANDA NATIONAL EXAMINATIONS BOARD
UGANDA ADVANCED CERTIFICATE OF EDUCATION
NOVEMBER - DECEMBER, 2022

Page 3 of 16

UACE

Do not write in this margin

Candidate's Name

Signature

Random No.

| | | | | |
|--|--|--|--|--|
| | | | | |
|--|--|--|--|--|

Subject Paper code/.....

Personal Number

| | | | | |
|--|--|--|--|--|
| | | | | |
|--|--|--|--|--|

MARKING GUIDE, P425/2, APPLIED

MATHEMATICS

①

| | | | |
|----------------------|----------------------------|--------------|--------------------|
| $P(T) = \frac{2}{3}$ | $P(\bar{T}) = \frac{1}{3}$ | | |
| $P(G) = 0.9$ | $P(\bar{G}) = 0.1$ | $P(G) = 0.6$ | $P(\bar{G}) = 0.4$ |

(a) $P(G) = \frac{2}{3} \times 0.9 + \frac{1}{3} \times 0.6 = 0.8 = \frac{4}{5}$ (B1) (M1) (A1)

(b) $P(T|G) = \frac{P(T \cap G)}{P(G)} = \frac{\frac{2}{3} \times 0.9}{0.8} = 0.75 = \frac{3}{4}$ (M1) (A1)

| Horizontal motion | Vertical motion |
|---------------------------|----------------------------|
| $u_x = 5 \text{ ms}^{-1}$ | $u_y = 0 \text{ ms}^{-1}$ |
| $a_x = 0 \text{ ms}^{-2}$ | $a_y = 10 \text{ ms}^{-2}$ |
| $s_x = x \text{ m}$ | $s_y = 80 \text{ m}$ |
| $t_x = t \text{ s}$ | $t_y = t \text{ s}$ |

(a) $s = ut + \frac{1}{2}at^2$, $80 = 0 \times t + \frac{1}{2} \times 10 \times t^2$ (B1)
 $5t^2 = 80$, $t^2 = 16$ $\therefore t = 4 \text{ s}$ (M1) (A1)

(b) $x = 5 \times 4 + \frac{1}{2} \times 0 \times (4)^2 = 20 \text{ m}$ (M1) (A1)

③ let $P = \frac{xy}{z} = \frac{4 \times 16.2}{2.53} = 25.6126$

$P_{\max} = \frac{x_{\max} y_{\max}}{z_{\min}} = \frac{4.5 \times 16.2}{2.523} = 29.0012$ (M1) (B1)

$P_{\min} = \frac{x_{\min} y_{\min}}{z_{\max}} = \frac{3.5 \times 16.14}{2.537} = 22.2665$ (B1)

$\Delta P = \frac{1}{2} (P_{\max} - P_{\min}) = \frac{1}{2} (29.0012 - 22.2665)$ (M1)

$\Delta P = 3.36735$

(A1)



UGANDA NATIONAL EXAMINATIONS BOARD
UGANDA ADVANCED CERTIFICATE OF EDUCATION
NOVEMBER - DECEMBER, 2022

Page 4 of 16

Candidate's Name

Signature

Random No.

| | | | | |
|--|--|--|--|--|
| | | | | |
|--|--|--|--|--|

Subject Paper code 2 /

Personal Number

| | | | | |
|--|--|--|--|--|
| | | | | |
|--|--|--|--|--|

UACE

Do not write in this margin

Do not write in this margin

4

H : T

$$2 : 1 = 3$$

$$P(H) = \frac{2}{3} : P(T) = \frac{1}{3} \text{ (B1) } n = 6$$

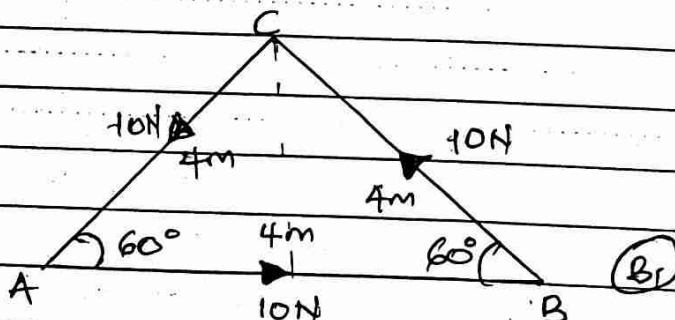
$$(a) P(X_H \geq 5) = P(X_H = 5) + P(X_H = 6)$$

$$= {}^6C_5 \left(\frac{2}{3}\right)^5 \left(\frac{1}{3}\right)^1 + {}^6C_6 \left(\frac{2}{3}\right)^6 \left(\frac{1}{3}\right)^0 = \frac{256}{729} = 0.3512 \text{ (M1) (A1)}$$

$$(b) P(X_T \leq 1) = P(X_T = 1) + P(X_T = 0)$$

$$= {}^6C_1 \left(\frac{1}{3}\right)^1 \left(\frac{2}{3}\right)^5 + {}^6C_0 \left(\frac{1}{3}\right)^0 \left(\frac{2}{3}\right)^6 = \frac{256}{729} = 0.3512 \text{ (M1) (A1)}$$

5



$$\rightarrow R_x = 10 - 10 \cos 60^\circ - 10 \cos 60^\circ = 0 \text{ (M1)}$$

$$\uparrow R_y = 10 \sin 60^\circ - 10 \sin 60^\circ = 0 \text{ (M1) } R = \begin{pmatrix} 0 \\ 0 \end{pmatrix} \text{ N}$$

$$\text{A) } A.C.M = 4 \times 10 \sin 60^\circ = 20\sqrt{3} \text{ Nm. (B1)}$$

Since $R = \begin{pmatrix} 0 \\ 0 \end{pmatrix} \text{ N}$ and $A.C.M = 20\sqrt{3} \text{ Nm}$, \therefore HS a couple. (B1)

6

| | | | |
|-----|-----|-----|-----|
| (a) | 60 | C | 40 |
| | 150 | 170 | 200 |

$$C - 60 = 40 - 60 \text{ (M1)}$$

$$170 - 150 = 200 - 150$$

$$e = 52 \text{ (A1)}$$

| | | | |
|-----|-----|----|-----|
| (b) | 100 | 90 | 75 |
| | S | 50 | 100 |

$$S - 50 = 50 - 100 \text{ (M1)}$$

$$100 - 90 = 90 - 75$$

$$S = 16.6667 = \frac{50}{3} \text{ (A1)}$$



UGANDA NATIONAL EXAMINATIONS BOARD
UGANDA ADVANCED CERTIFICATE OF EDUCATION
NOVEMBER - DECEMBER, 2022

Page 5 of 16

UACE

Candidate's Name

Signature

Subject Paper code 3

| | | | | |
|-----------------|--|--|--|--|
| Random No. | | | | |
| Personal Number | | | | |

Do not write in this margin

| <u>7</u> | x | $F(x)$ | $P(X=x)$ | $x P(X=x)$ | $x^2 P(X=x)$ |
|----------|-----|--------|----------|------------|--------------|
| | 3 | 0.01 | 0.01 | 0.03 | 0.09 |
| | 4 | 0.23 | 0.22 | 0.88 | 3.52 |
| | 5 | 0.64 | 0.41 | 2.05 | 10.25 |
| | 6 | 0.85 | 0.21 | 1.26 | 7.56 |
| | 7 | 1 | 0.15 | 1.05 (M1) | 7.35 |

(B1) $ECX = 5.27$ (M1) $ECX^2 = 28.77$ (B1)

$Var(x) = ECX^2 - (ECX)^2 = 28.77 - (5.27)^2 = 0.997$ (B1)

8

$F = \frac{P}{Y} = \frac{19.2 \times 10^3}{10} = 1,920N$ (B1)

$\theta = 1.9^\circ$

$900g \cos 1.9^\circ = 8,820N$

$1,920 - 360 - 294 = 900a$ (M1) (B1)

$900a = 1,266$ (B1)

$a = \frac{211}{150} ms^{-2} = 1.4067 ms^{-2}$ (M1) (B1)

9 (a) $\int_a^b \frac{1}{x} dx = \frac{1}{4}$

$\int_a^b \frac{1}{x} dx = \frac{1}{4}$

$\frac{1}{b-a} - \frac{1}{a} = \frac{1}{4}$ (M1) $\frac{1}{5-a} - \frac{1}{a} = \frac{1}{4}$ (B1) $20 - 4a = b - a$

$3a + b = 20$ (*)

$\int_a^b \frac{1}{x} dx = \frac{3}{4}$

$\frac{1}{b-a} - \frac{1}{a} = \frac{3}{4}$ (M1) $\frac{1}{9-a} - \frac{1}{a} = \frac{3}{4}$ (B1) $36 - 4a = 3b - 3a$

$a + 3b = 36$ (M1) $3a + 9b = 108$ (B1)

$3a + b = 20$ (*) $3a + b = 20$ (M1)



3

UGANDA NATIONAL EXAMINATIONS BOARD
UGANDA ADVANCED CERTIFICATE OF EDUCATION
NOVEMBER - DECEMBER, 2022

Page 6 of 16

UACE

Do not write in the margin

Candidate's Name

Signature

Random No.

| | | | | |
|--|--|--|--|--|
| | | | | |
|--|--|--|--|--|

Subject Paper code/.....

Personal Number

| | | | | |
|--|--|--|--|--|
| | | | | |
|--|--|--|--|--|

$8b = 88$, (M1) $b = 11$ (A1)

from (-) $a = 36 - 3 \times 11 = 3$ (A1)

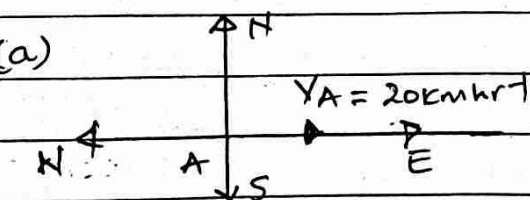
$$f(x) = \begin{cases} \frac{1}{8} & ; 3 < x < 11 \\ 0 & ; \text{otherwise} \end{cases}$$

(b) $P(4 < x < 7) = \int_4^7 \frac{1}{8} dx = \left| \frac{x}{8} \right|_4^7 = \frac{7-4}{8} = \frac{3}{8}$ (M1) (A1)

(c) $E(x) = \frac{1}{2} (3 + 11) = 7$ (B1)

$Var(x) = \frac{1}{12} (11-3)^2 = \frac{64}{12} = \frac{16}{3} = 5.3333$ (M1) (A1)

(10) (a)



$$\vec{V}_A = \begin{pmatrix} 20 \cos 0^\circ \\ 20 \sin 0^\circ \end{pmatrix} = \begin{pmatrix} 20 \\ 0 \end{pmatrix} \text{ km/hr} \quad (B1)$$

$$\vec{V}_B = \begin{pmatrix} 15 \cos 30^\circ \\ 15 \sin 30^\circ \end{pmatrix} = \begin{pmatrix} 7.5\sqrt{3} \\ 7.5 \end{pmatrix} \text{ km/hr} \quad (B1)$$

EITHER $\vec{AB} = \vec{r}_{B \leftarrow A(t=0)} = \begin{pmatrix} 30 \cos 270^\circ \\ 30 \sin 270^\circ \end{pmatrix} = \begin{pmatrix} 0 \\ -30 \end{pmatrix} \text{ km} \quad (B1)$

OR $\vec{AB} = \vec{r}_{A \leftarrow B(t=0)} = \begin{pmatrix} 0 \\ 30 \end{pmatrix} \text{ km}$

OR $\vec{BA} = \vec{r}_{A \leftarrow B(t=0)} = \begin{pmatrix} 30 \cos 90^\circ \\ 30 \sin 90^\circ \end{pmatrix} = \begin{pmatrix} 0 \\ 30 \end{pmatrix} \text{ km}$

$$\vec{BA} = \vec{r}_{A \leftarrow B(t=0)} = \begin{pmatrix} 0 \\ 30 \end{pmatrix} \text{ km}$$

$$\vec{r}_{A \leftarrow B(t=t)} = \vec{r}_{A \leftarrow B(t=0)} + (\vec{V}_A - \vec{V}_B)t$$

$$= \begin{pmatrix} 0 \\ 30 \end{pmatrix} + \begin{pmatrix} 7.5\sqrt{3} \\ 7.5 \end{pmatrix} t = \begin{pmatrix} 7.0096t \\ 30 - 7.5t \end{pmatrix} \text{ km} \quad (M1) (B1)$$



UGANDA NATIONAL EXAMINATIONS BOARD
UGANDA ADVANCED CERTIFICATE OF EDUCATION
NOVEMBER - DECEMBER, 2022

Page 7 of 16

UACE

Do not write in this margin

Candidate's Name

Signature

Subject Paper code/.....

Random No.

| | | | | |
|--|--|--|--|--|
| | | | | |
|--|--|--|--|--|

Personal Number

| | | | | |
|--|--|--|--|--|
| | | | | |
|--|--|--|--|--|

$$\vec{A} \cdot \vec{B} (t=t) \cdot \vec{A} \cdot \vec{B} = 0$$

$$\begin{pmatrix} 7.0096t \\ 30-7.5t \end{pmatrix} \cdot \begin{pmatrix} 7.0096 \\ -7.5 \end{pmatrix} = 0 \quad (M1)$$

$$105.384t - 225 = 0 \quad (B1)$$

$$t = 2.135 \text{ hr} \approx 2.14 \text{ hr} \approx 2 \text{ hrs } 0.14 \times 60 \text{ min}, \therefore t = 14:08 \text{ hrs} \quad (A1)$$

$$(b) \vec{r}_{A \rightarrow B} (t=2.14 \text{ hr}) = \begin{pmatrix} 7.0096 \times 2.14 \\ 30-7.5 \times 2.14 \end{pmatrix} = \begin{pmatrix} 15.0005 \\ 13.95 \end{pmatrix} \text{ km} \quad (B1)$$

$$|\vec{r}_{A \rightarrow B} (t=2.14 \text{ hr})| = \sqrt{(15.0005)^2 + (13.95)^2} = 20.48 \text{ km} \quad (M1) \quad (A1)$$

$$(11) (a) h = \frac{6-1}{6} = \frac{5}{6} \quad (B1)$$

| x | $f(x) = x \ln x$ | $f(x) = x \ln x$ |
|----------------|------------------|------------------|
| 1 | 0.0000 | |
| $\frac{11}{6}$ | | 1.1112 |
| $\frac{8}{3}$ | | 2.6156 |
| $\frac{7}{2}$ | | 4.3847 |
| $\frac{13}{3}$ | | 6.3540 |
| $\frac{31}{6}$ | | 8.4848 |
| 6 | 10.7506 | |
| Sum (B1) | 10.7506 (B1) | 22.9504 (B1) |

$$\int_1^6 x \ln x \, dx \approx \frac{5}{12} (10.7506 + 2 \times 22.9504) \approx 23.6036 \quad (M1) \quad (A1)$$

$$\approx 23.60 \text{ (3d.p.s)} \quad (A1)$$

$$(b) E.V = \int_1^6 x \ln x \, dx, \quad u = \ln x, \quad \frac{du}{dx} = \frac{1}{x}$$

$$\frac{dx}{dx} = x, \quad v = \frac{x^2}{2}$$

$$= \frac{x^2}{2} \ln x - \int \frac{1}{x} \cdot \frac{x^2}{2} \, dx = \frac{x^2}{4}$$

$$= \left[\frac{x^2}{2} \ln x - \frac{x^2}{4} \right]_1^6 = (18 \ln 6 - 9) - \left(\frac{1}{2} \ln 1 - \frac{1}{4} \right) \quad (M1) \quad S$$

$$= 23.5017 \approx 23.50 \text{ (3d.p.s)} \quad (A1)$$

UGANDA NATIONAL EXAMINATIONS BOARD
UGANDA ADVANCED CERTIFICATE OF EDUCATION
NOVEMBER - DECEMBER, 2022

Page 8 of 16

Candidate's Name

Signature

Subject Paper code/.....

| | | | | | |
|-----------------|--|--|--|--|--|
| Random No. | | | | | |
| Personal Number | | | | | |

$$A.E = |E.V - A.V| = |23.502 - 23.608| = 0.103 \text{ (B)}$$

$$P.E = \frac{A.E}{E.V} \times 100 = \frac{0.103}{23.502} \times 100 = 0.438 \text{ (B)}$$

Increase number of strips or sub-intervals or ordinates. (B)

| (12)(b) | R_x | R_y | d^2 |
|---------|-------|-------|-------|
| | 4 | 3.5 | 0.25 |
| | 9.5 | 8 | 2.25 |
| | 7 | 3.5 | 12.25 |
| | 6 | 7 | 1 |
| | 2.5 | 5 | 6.25 |
| | 9.5 | 9 | 0.25 |
| | 1 | 1 | 0 |
| | 2.5 | 2 | 0.25 |
| | 8 | 10 | 4 |
| | 5 | 6 | 1 |

$$\text{(B)} \sum d^2 = 27.5 \text{ (B)}$$

$$P_c = \frac{-6 \sum d^2}{n(n^2-1)} = \frac{-6 \times 27.5}{10 \times 99} = 0.8333 \text{ (A)}$$

$$P_c = 0.8333 > P_T = 0.65, \therefore \text{Significant at 5\% (B)}$$

$$(13) (a) \quad \underline{v} = \begin{pmatrix} 3t \\ -4t \\ t^2 \end{pmatrix} \text{ ms}^{-1}$$

$$s(t_2-t_1) = \int \underline{v} dt = \begin{pmatrix} \frac{3}{2}t^2 \\ -2t^2 \\ \frac{t^3}{3} \end{pmatrix} + c \text{ (M)}$$

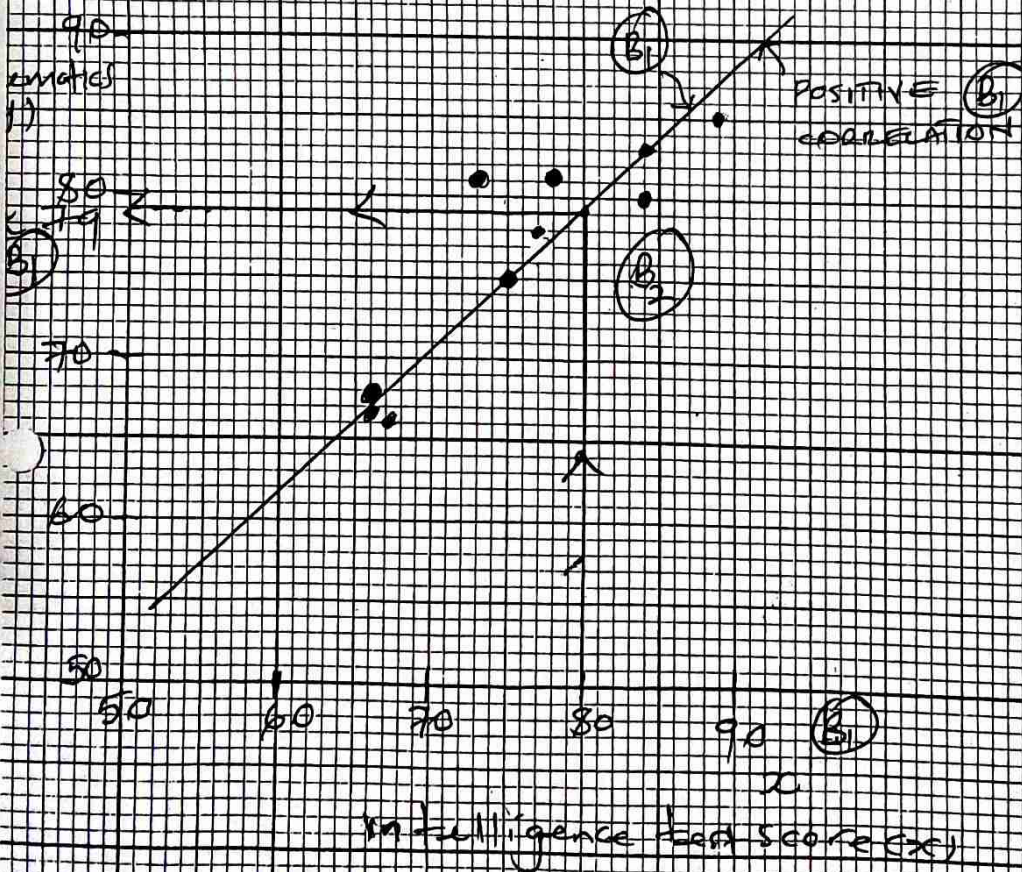
6

Student's Name
 Signature
 Subject Name Paper code 7 /

Random No.

Personal Number

mathematics grade (y) against Intelligence test score (x)



UGANDA NATIONAL EXAMINATIONS BOARD

(To be fastened together with other answers to paper)

UACE

Candidate's Name

Signature

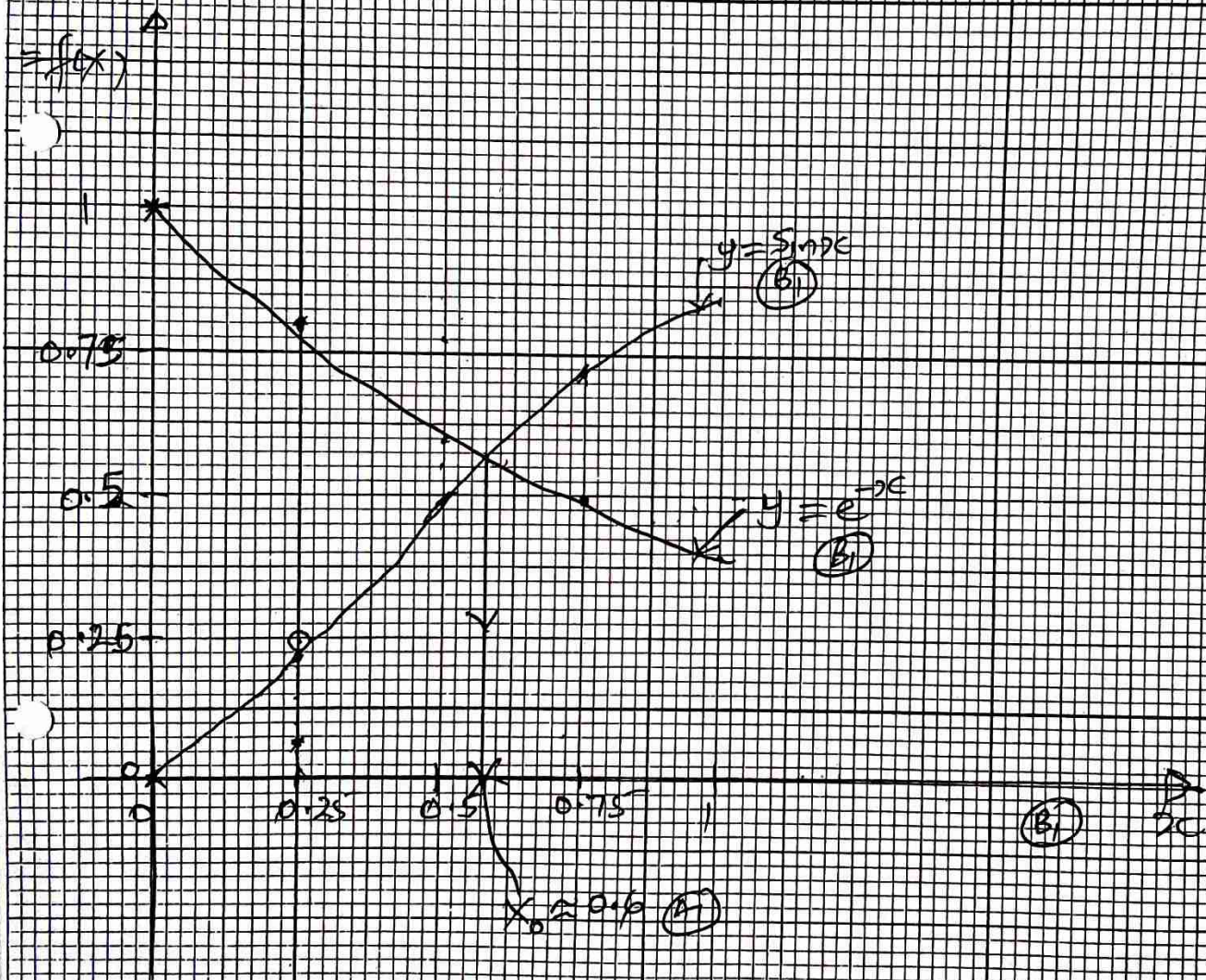
Subject Name Paper code/.....

Random No.

Personal Number

| | | | | | | | |
|----------|--------------|---|------|------|------|------|------|
| (14) (a) | x | 0 | 0.25 | 0.5 | 0.75 | 1 | (B1) |
| | $y = e^x$ | 1 | 0.78 | 0.61 | 0.47 | 0.37 | (B1) |
| | $y = \sin x$ | 0 | 0.25 | 0.48 | 0.68 | 0.81 | (B1) |

$y = e^x$ and $y = \sin x$ against values.



Candidate's Name

Signature

Subject Paper code 8 /

Random No.

| | | | | |
|--|--|--|--|--|
| | | | | |
|--|--|--|--|--|

Personal Number

| | | | | |
|--|--|--|--|--|
| | | | | |
|--|--|--|--|--|

UACE

Do not write in this margin

at $t=0$, $r_{(t=0)} = \begin{pmatrix} 1 \\ 0 \\ 1 \end{pmatrix}$, $\begin{pmatrix} 1 \\ 0 \\ 1 \end{pmatrix} = \begin{pmatrix} 0 \\ 0 \\ 0 \end{pmatrix} + c$, $c = \begin{pmatrix} 1 \\ 0 \\ 1 \end{pmatrix}$ (B1)

$r_{(t=2)} = \begin{pmatrix} \frac{3}{2}t^2 + 1 \\ -2t^2 \\ \frac{t^3}{3} + 1 \end{pmatrix} m$ (B1)

$r_{(t=2s)} = \begin{pmatrix} \frac{3}{2}(2)^2 + 1 \\ -2(2)^2 \\ \frac{(2)^3}{3} + 1 \end{pmatrix} = \begin{pmatrix} 7 \\ -8 \\ 1\frac{1}{3} \end{pmatrix} m$ (B1)

$|r_{(t=2s)}| = \sqrt{(7)^2 + (-8)^2 + (1\frac{1}{3})^2} = 11.2448 m$ (A1)

(b) $a_{(t=2s)} = \frac{dv}{dt} = \begin{pmatrix} 3 \\ -4 \\ 2t \end{pmatrix} ms^{-2}$ (M1)

$a_{(t=2s)} = \begin{pmatrix} 3 \\ -4 \\ 2 \times 2 \end{pmatrix} = \begin{pmatrix} 3 \\ -4 \\ 4 \end{pmatrix} ms^{-2}$ (B1)

$|a_{(t=2s)}| = \sqrt{(3)^2 + (-4)^2 + (4)^2} = 7.8102 ms^{-2}$ (A1)

(c) $F = ma = 3 \begin{pmatrix} 3 \\ -4 \\ 4 \end{pmatrix} = \begin{pmatrix} 9 \\ -12 \\ 12 \end{pmatrix} N$ (M1) (A1)

(b) $e^{-x} = \sin x$, $\sin x - e^{-x} = 0$, $f(x) = 0$

$f(x) = \sin x - e^{-x}$

$f'(x) = \cos x + e^{-x}$ (M1)

$x_{n+1} = x_n - \frac{f(x_n)}{f'(x_n)} = x_n - \frac{\sin x_n - e^{-x_n}}{\cos x_n + e^{-x_n}}$

$x_0 = 0.6$

$x_1 = 0.6000 - \frac{\sin 0.6000 - e^{-0.6000}}{\cos 0.6000 + e^{-0.6000}} = 0.5885$ (M1) 9

UGANDA NATIONAL EXAMINATIONS BOARD
UGANDA ADVANCED CERTIFICATE OF EDUCATION
NOVEMBER - DECEMBER, 2022

Page 10 of 16

Do not
write
in this
margin

Candidate's Name

Signature

Subject Paper code 10 /

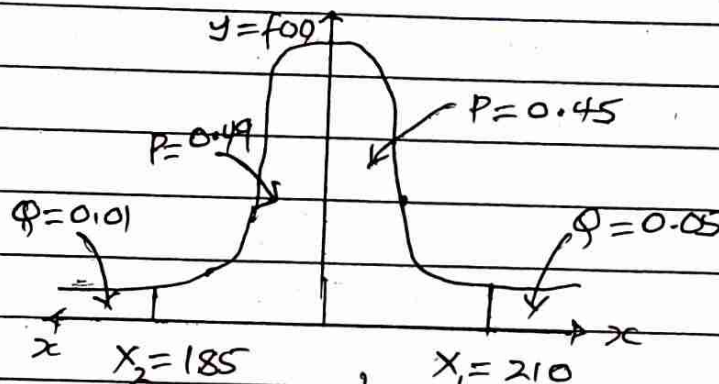
| | | | | |
|-----------------|--|--|--|--|
| Random No. | | | | |
| Personal Number | | | | |

$$x_2 = 0.5885 - \left(\frac{\sin 0.5885 - e^{-0.5885}}{\cos 0.5885 + e^{-0.5885}} \right) - 0.5885 \quad (M_1)$$

$$|x_1 - x_2| = 0 \quad (B_1)$$

$$\text{root } x \approx 0.589 \text{ (3 d.p.s)} \quad (A_1)$$

(15) (a)



$$-Z_{0.49} = -2.326 \quad (B_1) \quad Z_{0.45} = 1.645 \quad (B_1) \quad Z = \frac{x - \mu}{\sigma}$$

$$1.645 = \frac{210 - \mu}{\sigma} \quad (M_1)$$

$$1.645\sigma + \mu = 210$$

$$-2.326 = \frac{185 - \mu}{\sigma} \quad (M_1)$$

$$\mu - 2.326\sigma = 185 \quad (1) \quad \text{and} \quad \mu = 199.6437$$

$$\mu + 1.645\sigma = 210 \quad (2) \quad \sigma = 6.2956$$

$$(2) - (1) \quad 3.971\sigma = 25 \quad (M_1)$$

$$\sigma = 6.2956 \quad (A_1)$$

$$\text{from (2)} \quad \mu = 210 - 1.645 \times 6.2956 = 199.6437 \quad (M_1) \quad (A_1)$$

(b) $P(182 < X < 195)$

$$= P\left(\frac{182 - 199.6437}{6.2956} < Z < \frac{195 - 199.6437}{6.2956}\right) \quad (M_1)$$

$$= P(-2.8025 < Z < -0.7376) = P(Z < -0.7376) -$$

$$P(Z < -2.8025) = 0.2304 - 0.0025 = 0.2279 \quad (B_1) \quad (M_1) \quad (A_1)$$

$$\text{OR } \Phi(-2.8025) - \Phi(-0.7376) = 0.4975 - 0.2696 = 0.2279$$

1.49746
2.6962
2.2784



10

UGANDA NATIONAL EXAMINATIONS BOARD
UGANDA ADVANCED CERTIFICATE OF EDUCATION
NOVEMBER - DECEMBER, 2022

Page 11 of 16

UACE

Do not
write
in this
margin

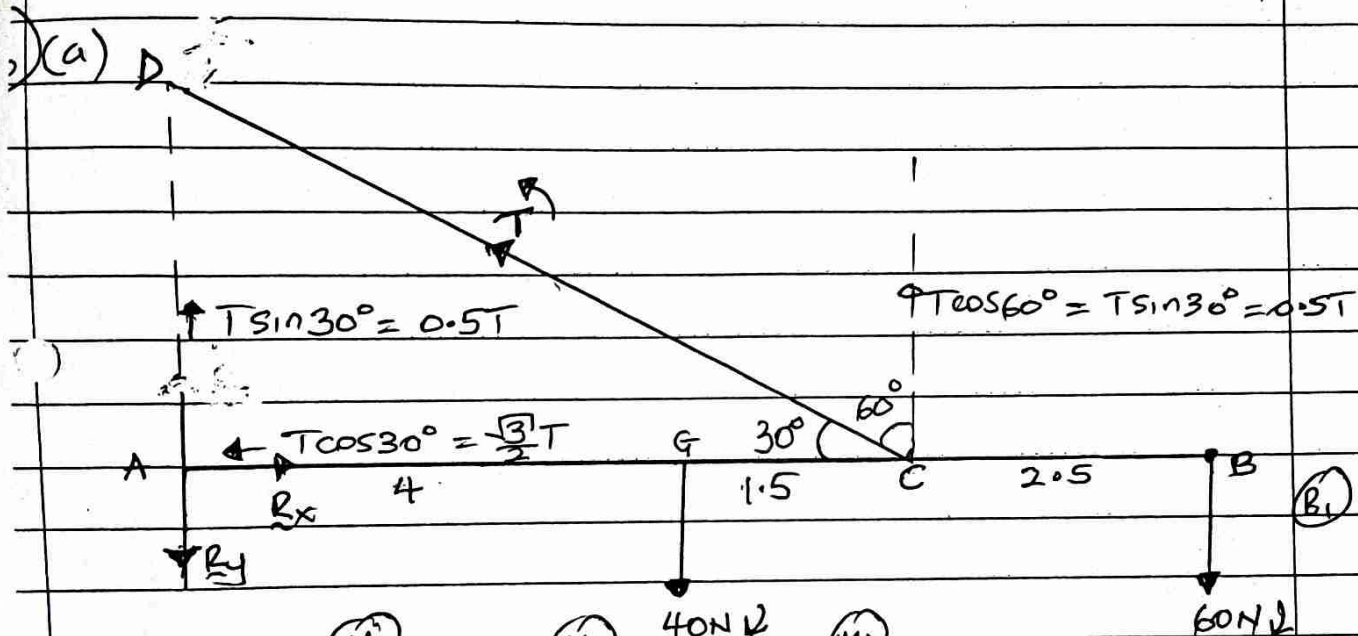
Candidate's Name

Signature

Subject Paper code/.....

Random No.

Personal Number



$$\sum \tau_A = 0 \quad (M_1) \quad (M_1) \quad (M_1) \quad (B_1)$$

$$5.5 \times 0.5T = 4 \times 40 + 8 \times 60$$

$$T = 232.7273 \text{ N} \quad (A_1)$$

$$(b) \quad \uparrow \quad 0.5T = R_y + 40 + 60 \quad (B_1)$$

$$R_y = 0.5 \times 232.7273 - 100 = 16.3636 \text{ N}$$

$$\rightarrow \quad R_x = \frac{\sqrt{3}}{2}T = \frac{\sqrt{3}}{2} \times 232.7273 = 201.5478 \text{ N} \quad (B_1)$$

$$|R| = \sqrt{(R_x)^2 + (R_y)^2} = \sqrt{(201.5478)^2 + (16.3636)^2} = 202.211 \text{ N} \quad (M_1) \quad (A_1)$$

$$\theta = \tan^{-1} \left(\frac{16.3636}{201.5478} \right) = 4.64^\circ \text{ below AB or } 4.64^\circ \text{ S} \quad (B_1) \quad (A_1)$$

$$\text{OR } 85.36^\circ \text{ E}$$

