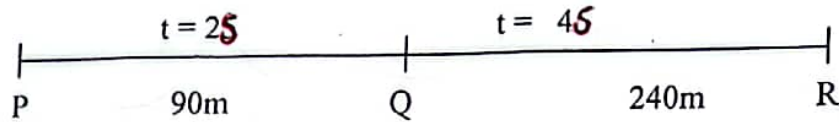


$$= P(A \cap B) + P(A \cap B)$$

li)	$P(A \cup B) - P(A \cap B) = \frac{1}{3}$ $P(A) + P(B) - 2P(A \cap B) = \frac{1}{3}$ $\frac{1}{2} + \frac{1}{4} - 2P(A \cap B) = \frac{1}{3}$ $2P(A \cap B) = \frac{3}{4} - \frac{1}{3}$ $P(A \cap B) = \frac{5}{24} \text{ or } 0.2083 \text{ (at least 4dp)}$	<p>M<sub>1</sub> for defining A or B but not both</p> <p>M<sub>1</sub> substitution in the formula</p> <p>A<sub>1</sub> out put</p>								
(ii)	$P\left(\frac{\bar{B}}{A}\right) = \frac{P(\bar{B} \cap A)}{P(A)}$ $= \frac{\frac{1}{2} - \frac{5}{24}}{\frac{1}{2}}$ $= \frac{7}{12} \text{ or } 0.5833 \text{ (at least 4dp)}$	<p>M<sub>1</sub> Substitution</p> <p>A<sub>1</sub> output correct.</p>								
2i)	<table border="1"> <tr> <td>Old</td> <td>35</td> <td>40</td> <td>x</td> </tr> <tr> <td>New</td> <td>50</td> <td>65</td> <td>80</td> </tr> </table> $\frac{80-50}{x-35} = \frac{65-50}{40-35}$ $\frac{30}{x-35} = \frac{15}{5}$ $x = 45\% \text{ (with units)}$	Old	35	40	x	New	50	65	80	<p>B<sub>1</sub> (mobile for location)</p> <p>M<sub>1</sub> equating gradients</p> <p>A<sub>1</sub> correct output with units</p>
Old	35	40	x							
New	50	65	80							
ii)	<table border="1"> <tr> <td>Old</td> <td>35</td> <td>37</td> <td>40</td> </tr> <tr> <td>New</td> <td>50</td> <td>y</td> <td>65</td> </tr> </table> $\frac{65-50}{40-35} = \frac{y-50}{37-35}$ $\frac{15}{5} = \frac{y-50}{2}$ $y = 56\%$	Old	35	37	40	New	50	y	65	<p>M<sub>1</sub> equating gradients</p> <p>A<sub>1</sub> correct output. with units</p>
Old	35	37	40							
New	50	y	65							

3.



From P to Q

$$S = ut + \frac{1}{2}at^2$$

$$90 = 2u + \frac{1}{2}a(2)^2$$

$$45 = u + a \quad \text{(i)}$$

M<sub>1</sub> correct substitution

From P to R

$$S = 330 \quad t = 65$$

$$330 = 6u + \frac{1}{2}a(6)^2$$

$$55 = u + 3a \quad \text{(ii)}$$

$$(i) - (ii)$$

M<sub>1</sub> correct substitution

$$45 = u + a$$

$$\begin{array}{r} (55 - u + 3a) \\ - (45 - u + a) \\ \hline 10 = 2a \end{array}$$

M<sub>1</sub> attempt to solve equations

$$a = 5 \text{ ms}^{-2}$$

A<sub>1</sub> correct output with units

$$U = 45 - a$$

$$= 45 - 5$$

$$= 40 \text{ ms}^{-1}$$

A<sub>1</sub> correct output with units

5 marks

4

y	1	2	3	4	5
P(y = y)	K	4K	9K	5K	6K
y p(y = y)	K	8K	27K	20K	30K

(i)

$$K + 4K + 9K + 5K + 6K = 1$$

$$25K = 1$$

$$K = \frac{1}{25} \quad \text{or } 0.04$$

M<sub>1</sub> summationA<sub>1</sub> correct output

(ii)

$$E(y) = K + 8K + 27K + 20K + 30K$$

$$= 86K$$

$$= 86 \times \frac{1}{25}$$

$$= \frac{86}{25} \quad \text{or } 3.44$$

M<sub>1</sub> summation of productsA<sub>1</sub> correct output

(iii)  $P(2 < X \leq 4) = P(x=3) + P(x=4)$   
 $= 9K + 5K$   
 $= 14 \times \frac{1}{25}$   
 $= \frac{14}{25}$   
 Or (0.56)

R.E = std  
exact

A1 correct output

5

5 marks

$$P = \frac{KT}{V}$$

$$P + ep = K \frac{(T+e_1)}{(V+e_2)}$$

$$= K \frac{(T+e_1)(V-e_2)}{(V+e_2)(V-e_2)}$$

$e_1 \ll T$  and  $e_2 \ll V$

$e_1$  and  $e_2$  are too small then  $e_1 e_2 \approx 0$  and  $e_2^2 \approx 0$

$e_1 e_2 \approx 0$   
 $e_2^2 \approx 0$

M1 definition of error.

$$P + ep = K \left( \frac{TV - Te_2 + Ve_1}{V^2} \right)$$

$$= K \left[ \frac{T}{V} - \frac{Te_2}{V^2} + \frac{e_1}{V} \right]$$

$$P = \frac{KT}{V} + K \left[ \frac{e_1}{V} - \frac{Te_2}{V^2} \right] - \frac{KT}{V}$$

$$|P| = \left| K \left[ \frac{e_1}{V} - \frac{Te_2}{V^2} \right] \right|$$

$$\text{But } \left| \frac{e_1}{V} - \frac{Te_2}{V^2} \right| \leq \left| \frac{e_1}{V} \right| + \left| \frac{Te_2}{V^2} \right|$$

B1 for the correct assumptions

$$|P| = K \left[ \left| \frac{e_1}{V} \right| + \left| \frac{Te_2}{V^2} \right| \right]$$

$$R.E_{\max} = \frac{|P|}{P}$$

$$= \frac{K \left[ \left| \frac{e_1}{V} \right| + \left| \frac{Te_2}{V^2} \right| \right]}{\frac{KT}{V}}$$

B1 for triangular inequality

M1 for relative error

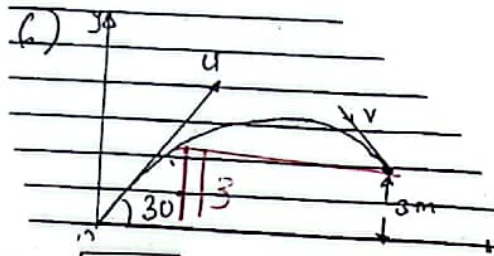
$$= \left| \frac{e_1}{V} \right| \times \frac{V}{T} + \left| \frac{Te_2}{V^2} \right| \times \frac{V^2}{T}$$

$$= \left| \frac{e_1}{T} \right| + \left| \frac{e_2}{V} \right| \text{ as required}$$

B1 correct expression



6.



$$y = ut \sin \theta - \frac{gt^2}{2}$$

$$\text{Speed } V = \sqrt{V_x^2 + V_y^2}$$

$$\text{But horizontal velocity } V_x = U \cos \alpha$$

$$= 21 \cos 30^\circ$$

$$= 18.1865 \text{ ms}^{-1}$$

$$\approx 18.19 \text{ ms}^{-1}$$

B1 correct  $V_x$  with or without units

$$\text{Vertical velocity } V_y = U \sin \alpha - gt$$

$$= 21 \sin 30^\circ - 9.8 t$$

$$\text{But } y = U \sin \alpha t - \frac{1}{2} gt^2$$

$$4.9 t^2 - 10.5 t + 3$$

$$\Rightarrow t = 1.8034$$

$$\text{Or } t = 0.3395$$

B1 any value of t.

$$\text{Thus } V_y = 10.5 - 9.8 \times 1.8034$$

$$= -17.33 \text{ ms}^{-1}$$

$$-17.1733 \text{ ms}^{-1}$$

B1 correct  $V_y$  magnitude

$$\text{Allow } V_y = 10.5 - 3.3271$$

$$= +7.173 \text{ ms}^{-1}$$

M1 calculating the magnitude

Negative means the ball is moving downwards  
Speed at impact;

$$V = \sqrt{(18.1865)^2 + (-7.1733)^2}$$

$$= 19.55 \text{ ms}^{-1}$$

A1 correct output with or without units

7.i)

Cost of living;

$$= (125 \times 35) + (121 \times 11) + (112 \times 8) + (108 \times 6)$$

$$+ 118 \times 22$$

$$35 + 11 + 8 + 6 + 22$$

$$\frac{9846}{82} = 120.0732$$

The expenditure increased by 20.0732% in 2004

5 marks

M1 correct substitution

A1 correct output

B1 correct comment

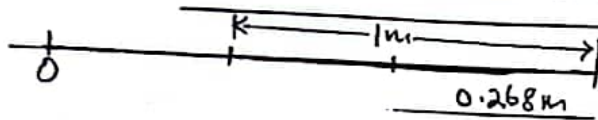
ii)  $\frac{P_{2004}}{P_{2000}} \times 100 = 120.0732$   
 $P_{2004} = \frac{120.0732 \times 11200}{100}$   
 $= 13448.195$   
 $\approx \text{UGX } 13448$

M<sub>1</sub> correct substitution

A<sub>1</sub> correct output

8

05 Marks



From  $V^2 = w^2 (a^2 - x^2)$   
 At  $1m$   $V = 3\sqrt{3} \text{ ms}^{-1}$

$(3\sqrt{3})^2 = w^2 (a^2 - (a-1)^2)$   
 $27 = w^2 (2a - 1)$  (i)  
 At  $0.268m$   $V = 3ms^{-1}$

$(3)^2 = w^2 (a^2 - (a - 0.268)^2)$   
 $9 = w^2 (0.536a - 0.071824)$  (ii)

$\frac{27}{9} = \frac{w^2 (2a - 1)}{w^2 (0.536a - 0.071824)}$

$3(0.536a - 0.071824) = (2a - 1)$   
 $(1.608 - 2)a = -1 + 0.0215472$

$\frac{-0.392a}{0.392} = \frac{-0.784452}{0.392}$

$a \approx 2m$

$a = 2.0013m$   
 $a \approx 2m$

B<sub>1</sub> attempt to find distance from O

M<sub>1</sub> correct substitution

M<sub>1</sub> correct substitution

M<sub>1</sub> attempt to solve

A<sub>1</sub> correct output with or without units.

5 Marks

9

Time/mm	Freq	X	Fx	C.f	C.B
80- 84	10	82	820	10	79.5 - 84.5
85 - 89	15	87	1305	25	84.5 - 89.5
90 - 94	35	92	3220	60	89.5 - 94.5
95 - 99	40	97	3880	100	94.5 - 99.5
100 - 104	28	102	2856	128	99.5 - 104.5
105 - 109	15	107	1605	143	104.5 - 109.5
110 - 114	4	112	448	147	109.5 - 114.5
115 - 119	3	117	351	150	114.5 - 119.5

$\sum f = 150$

$\sum fx = 14485$

B<sub>1</sub> all values of C.f correct

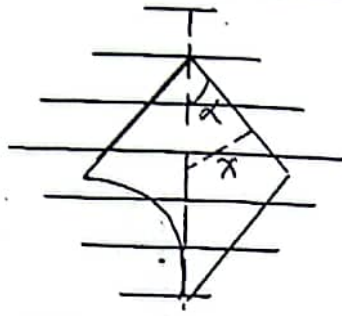
B<sub>1</sub> All values of Fx correct

B<sub>1</sub> all values of X correct

(i)	$\text{Mean} = \frac{\sum fx}{\sum f}$ $\frac{14485}{150}$ $= 96.56$ $= \approx 97 \text{ minutes}$	<p>M<sub>1</sub> correct substitution</p> <p>A<sub>1</sub> correct output (≥ 2 dp)</p>																
(ii)	$\text{Medium} = l + \left[ \frac{N/2 - Cf_b}{f_m} \right] xi$ $= 94.5 + \left( \frac{75-60}{40} \right) X5$ $= 94.5 + \frac{15}{40} X5$ $= 96.375 \text{ minutes}$	<p>M<sub>1</sub> correct substitution</p> <p>A<sub>1</sub> correct output (≥ 2 dp)</p> <p>With or without units</p>																
b)(ii)	<p>Number of times = 148 - 28</p> <p>= 120 times <math>\pm 2</math></p>	<p>B<sub>1</sub> any value read correctly from graph</p> <p>M<sub>1</sub> Subtraction</p> <p>A<sub>1</sub> Correct out put</p>																
b)(i)	On graph paper at the back																	
10a)	Let $\delta$ be the <del>weight</del> <sup>now</sup> per unit area.																	
	<table border="1"> <thead> <tr> <th>Portion</th><th>Area (m<sup>2</sup>)</th><th>Weight <sup>now</sup></th><th>C.O.G from AB</th></tr> </thead> <tbody> <tr> <td>Square</td><td>4m<sup>2</sup></td><td>4m<sup>2</sup> δ</td><td>M</td></tr> <tr> <td>Semi-circle</td><td><math>\pi/2 m^2</math></td><td><math>\pi/2 m^2 \delta</math></td><td><math>4M/3\pi</math></td></tr> <tr> <td>Remainder</td><td><math>4m^2 - \pi/2 m^2</math></td><td><math>(4m^2 - \pi/2 m^2) \delta</math></td><td><math>\bar{X}</math></td></tr> </tbody> </table>	Portion	Area (m <sup>2</sup> )	Weight <sup>now</sup>	C.O.G from AB	Square	4m <sup>2</sup>	4m <sup>2</sup> δ	M	Semi-circle	$\pi/2 m^2$	$\pi/2 m^2 \delta$	$4M/3\pi$	Remainder	$4m^2 - \pi/2 m^2$	$(4m^2 - \pi/2 m^2) \delta$	$\bar{X}$	<p>B<sub>1</sub> correct column of area</p> <p>B<sub>1</sub> correct column of weight</p> <p>B<sub>1</sub> Correct column of C.O. <del>M</del> from AB</p>
Portion	Area (m <sup>2</sup> )	Weight <sup>now</sup>	C.O.G from AB															
Square	4m <sup>2</sup>	4m <sup>2</sup> δ	M															
Semi-circle	$\pi/2 m^2$	$\pi/2 m^2 \delta$	$4M/3\pi$															
Remainder	$4m^2 - \pi/2 m^2$	$(4m^2 - \pi/2 m^2) \delta$	$\bar{X}$															
	$AB \ 4m^2m - \pi/2 m^2 4m/3\pi = (4m^2 - \pi/2 m^2) \bar{X}$ $4m - \frac{2}{3}m = (4 - \pi/2) \bar{X}$ $\frac{12m - 2m}{3} = \left( \frac{8 - \pi}{2} \right) \bar{X}$ $\bar{X} = \frac{10m^2 X2}{3(8 - \pi)}$ $= \frac{20M}{3(8 - \pi)}$	<p>M<sub>1</sub> Correct moments</p> <p>M<sub>1</sub> equating moments</p> <p>M<sub>1</sub> Simplification</p> <p>B<sub>1</sub> Correct expression</p>																



b)



$$X = 2M - \frac{20M}{3(8-\Pi)}$$

$$= \frac{6m(8-\Pi) - 20m}{3(8-\Pi)}$$

$$= \frac{28m - 6m\Pi}{3(8-\Pi)}$$

$$= \frac{2(14-3\Pi)m}{3(8-\Pi)}$$

$$\tan \alpha = \frac{x}{m}$$

$$= \frac{2(14-3\Pi)m}{3(8-\Pi)}$$

$$= \frac{m}{3(8-\Pi)}$$

B<sub>1</sub>M<sub>1</sub> obtaining differenceM<sub>1</sub> simplificationM<sub>1</sub> correct substitutionB<sub>1</sub> correct expression

11a)

$$h = \frac{2-1}{6-1} = \frac{1}{5} = 0.2$$

X	y <sub>0</sub> , y <sub>5</sub>	Y <sub>1</sub> -----y <sub>4</sub>
1.0	0.2500	
1.2		0.16949
1.4		0.13060
1.6		0.10724
1.8		0.091463
2.0	0.0800	
Sum = 0.3300		Sum = 0.498793

$$\int_1^2 \left( \frac{x}{7x^2-3} \right) dx \cong \frac{1}{2} X \frac{1}{5} (0.3300 + 2(0.498793))$$

$$\cong 0.1328(4\text{sfs})$$

$$= 0.1327$$

B<sub>1</sub> attempt to find hB<sub>1</sub> values of xB<sub>1</sub> correct values of y ≥ 5sfsM<sub>1</sub> correct substitutionA<sub>1</sub> correct output (4sfs)

bi)	$\text{Exact value} = \frac{1}{14} \ln [7x^2 - 3]^2$ $= \frac{1}{14} [125 - 14]$ $= 0.1309 \text{ (4sfgs)}$	<p>M<sub>1</sub> correct integration</p> <p>M<sub>1</sub> correct substitution of limits</p> <p>A<sub>1</sub> correct output (4sf)</p>
ii)	$\text{Percentage error} = \left  \frac{0.1309 - 0.1328}{0.1309} \right  \times 100$ $= 1.45\%$	<p>M<sub>1</sub> Absolute error</p> <p>M<sub>1</sub> percentage error</p> <p>A<sub>1</sub> Correct output with or without the % sign</p>
iii)	By increasing the number of ordinates	B <sub>1</sub> Correct comment if all the 11 marks above are earned
<b>12 Marks</b>		
12i)	<p> <math>P(x) = 2P(y)</math>            But <math>P(x) + P(y) = 1</math>  <math>2P(y) + P(y) = 1</math>  <math>P(y) = \frac{1}{3}</math>            Hence <math>P(x) = \frac{2}{3}</math>            Tree diagram         </p>	B <sub>1</sub> Probilities of x and y
a)	$\left( \frac{2}{3} \times \frac{4}{7} \times \frac{3}{6} \right) + \left( \frac{2}{3} \times \frac{3}{7} \times \frac{2}{6} \right) +$ $\left( \frac{1}{3} \times \frac{5}{11} \times \frac{4}{10} \right) + \left( \frac{1}{3} \times \frac{6}{11} \times \frac{5}{10} \right)$ $= 0.4372 (\geq 4 \text{ drops})$	<p>M<sub>1</sub> any two arms correct</p> <p>M<sub>1</sub> adding the arms</p> <p>A<sub>1</sub> Correct output <math>\geq</math> dps</p>



	$P(x=0) = \left(\frac{2}{3} \times \frac{3}{7} \times \frac{2}{6}\right) + \left(\frac{1}{3} \times \frac{6}{11} \times \frac{5}{10}\right)$ $P(x=0) = \frac{43}{231}$ $P(x=1) = 2\left(\frac{43}{3} \times \frac{4}{7} \times \frac{3}{6}\right) + \left(\frac{2}{3} \times \frac{3}{7} \times \frac{4}{6}\right)$ $+ \left(\frac{1}{3} \times \frac{5}{11} \times \frac{6}{10}\right) + \left(\frac{1}{3} \times \frac{6}{11} \times \frac{5}{10}\right)$ $P(x=1) = \frac{130}{231}$ $P(x=2) = \left(\frac{2}{3} \times \frac{4}{7} \times \frac{3}{6}\right) + \left(\frac{1}{3} \times \frac{5}{11} \times \frac{4}{10}\right)$ $= \frac{174}{693} = \frac{58}{231}$ <table border="1"> <tr> <td>x</td><td>0</td><td>1</td><td>2</td></tr> <tr> <td>P(X = x)</td><td><math>\frac{43}{231}</math></td><td><math>\frac{130}{231}</math></td><td><math>\frac{174}{693}</math></td></tr> </table>	x	0	1	2	P(X = x)	$\frac{43}{231}$	$\frac{130}{231}$	$\frac{174}{693}$	<p>M<sub>1</sub> both arms correct and added</p> <p>M<sub>1</sub> both arms correct and added</p> <p>M<sub>1</sub> both arms correct and added</p> <p>B<sub>1</sub> for all P(X = x) values correct (≥ 4 dp)</p>
x	0	1	2							
P(X = x)	$\frac{43}{231}$	$\frac{130}{231}$	$\frac{174}{693}$							
(c)	$\text{Mean} = \left(0 \times \frac{43}{231}\right) + \left(1 \times \frac{130}{231}\right) + \left(2 \times \frac{174}{693}\right)$ $\text{Mean} = \frac{738}{693} = \frac{82}{77}$	<p>M<sub>1</sub> products</p> <p>M<sub>1</sub> addition</p> <p>A<sub>1</sub> correct output ≥ 2dp</p>								
		12 Marks								
13(a)	$a = 4e^{-3t}i + 12S \sin t j - 7C \cos t k$ $a_{t=0} = 4e^{-3(0)}i + 12S \sin 0 j - 7C \cos 0 k$ $= 4i + 7k$ $ a_{t=0}  = \sqrt{16 + 49}$ $= \sqrt{65} \text{ms}^{-2} \text{ or } 8.062 \text{ms}^{-2}$	<p>M<sub>1</sub> magnitude</p> <p>A<sub>1</sub> Correct out put with units or <del>without</del></p>								
(b)	$V = \int a dt$ $= \int (4e^{-3t}i + 12S \sin t j - 7C \cos t k) dt$ $= -\frac{4}{3}e^{-3t}i - 12C \cos t j - 7S \sin t k + C$ <p>at t = 0, V = 11i - 8j + 3k</p> $11i - 8j + 3k = -\frac{4}{3}i - 12j + C$	<p>M<sub>1</sub> Correct integration with the constant C seen</p> <p>M<sub>1</sub> attempt to solve for C</p>								

$$C = \frac{37}{3}i + 4j + 3k$$

$$V = \left( \left( -\frac{4}{3}e^{-3t} + \frac{37}{3} \right) i + (-12\cos t + 4)j + (-7\sin t + 3)k \right) \text{ m/s}$$

(C)

$$S = \int v dt$$

$$= \int \left[ \left( -\frac{4}{3}e^{-3t} + \frac{37}{3} \right) i + (-12\cos t + 4)j + (-7\sin t + 3)k \right] dt$$

$$= \left( \frac{4}{9}e^{-3t} + \frac{37}{3}t \right) i + (-12\sin t + 4t)j + (7\cos t + 3t)k + C$$

$$\text{at } t = 0, S = 5i - 6j + 2k$$

$$5i - 6j + 2k = \frac{4}{9}i + 7k + C$$

$$C = \frac{41}{9}i - 6j - 5k$$

$$S = \left( \frac{4}{9}e^{-3t} + \frac{37}{3}t + \frac{41}{9} \right) i + (-12\sin t + 4t - 6)j + (7\cos t + 3t - 5)k$$

$$S_{t=1}$$

$$= 1 \left( \frac{4}{9}e^{-3} + \frac{37}{3} + \frac{41}{9} \right) i + (-12\sin(1) + 4 - 6)j + (7\cos(1) + 3 - 5)k$$

$$= (16.91i - 12.0977j + 8.2179k) \text{ m}$$

B<sub>1</sub> Correct value of C

A<sub>1</sub> Correct expression for V

M<sub>1</sub> correct integration with constant C seen

attempt to  
M<sub>1</sub> correct integration with C seen  
score for C

B<sub>1</sub> correct value for S

M<sub>1</sub> correct substitution

A<sub>1</sub>-Correct value of S

12 Marks

14

$$e^x + x - 4 = 0$$

$$e^x = 4 - x$$

$$f(x) = e^x, f(x) = 4 - x$$

$$\text{for } f(x) = e^x$$

x	-1	0	1	2	3
y = e <sup>x</sup>	0.367	1	2.718	7.3	20.08

$$f(x) = 4 - x$$

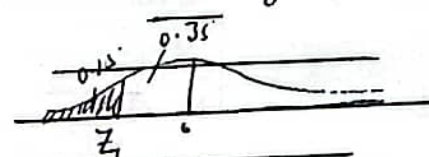
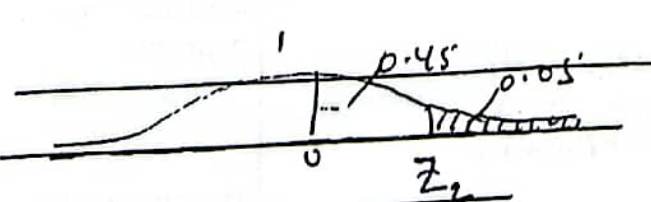
X	-1	0	1	2	3
f(x) = 4 - x	5	4	3	2	1

$$X_0 = 1.1 \pm 0.1$$

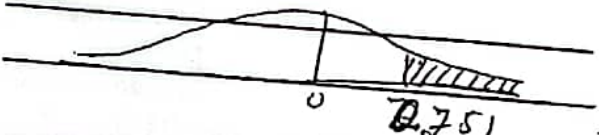
B<sub>1</sub> at least 3 coordinate values seen b/n (0 and 2)

B<sub>1</sub> at least 3 coordinate values seen between 0 and 2

B<sub>1</sub> for correct X<sub>0</sub> ≥ 0 to 1dp

(b)	$F(x) = e^x + x - 4$ $f'(x) = e^x + 1$ $X_{n+1} = X_n - \frac{f(X_n)}{f'(X_n)}$ $= X_n - \frac{e^{x_n} + x_n - 4}{e^{x_n} + 1}$ $= X_n - \frac{(e^{x_n} + 1) - e^{x_n} - x_n + 4}{e^{x_n} + 1}$ $= \frac{e^{x_n}(x_n - 1) + 4}{e^{x_n} + 1}$ $x_0 = 1.1$ $x_1 = \frac{e^{1.1}(1.1 - 1) + 4}{e^{1.1} + 1}$ $= 1.074 \text{ (3dp)}$ $x_2 = \frac{e^{1.074}(1.074 - 1) + 4}{e^{1.074} + 1}$ $= 1.074 \text{ (3dp)}$ <p>The root is 1.07 (3 s.f)</p>	<p>M<sub>1</sub> correct derivative</p> <p>M<sub>1</sub> correct substitution</p> <p>A<sub>1</sub> correct expression</p> <p>B<sub>1</sub> correct <math>x_1 \geq 4</math> s.f</p> <p>B<sub>1</sub> correct <math>x_2 \geq 4</math> s.f</p> <p>A<sub>1</sub> correct output 3(s.f)</p>
		12 Marks
15	<p>Let <math>x</math> be a random variable for number of goats covered by the people</p> <p><math>P(X &lt; 60) = 15\%</math></p> <p><math>P(X &gt; 90) = 5\%</math></p> <p><math>P(X &lt; 60) = P(Z &lt; \frac{60 - \mu}{\delta}) = 0.15</math></p>  <p><math>Z_1 = -1.036</math></p> <p><math>\frac{60 - \mu}{\delta} = -1.036</math></p> <p><math>60 - \mu = -1.036\delta \text{ ----- (1)}</math></p> <p><math>P(X &gt; 90) = P(Z &gt; \frac{90 - \mu}{\delta}) = 0.05</math></p> 	<p>B<sub>1</sub> correct <math>Z_1</math></p> <p>B<sub>1</sub> correct substitution and equating</p>



	$Z_2 = 1.645$ $90 - M = 1.645 \delta$ ----- (ii)	B <sub>1</sub> correct Z <sub>2</sub> B <sub>1</sub> correct substitution and equating
	Eqn (i) and eqn (ii) $60 - N = -1.036 \delta$ $90 - N = 1.645 \delta$ $\frac{-30.0}{-2.681} = \frac{-2.681 \delta}{-2.681}$ $\delta = 11.1899$ $M = 90 - 1.645 \times 11.1899$ $= 71.592$	M <sub>1</sub> attempt to solve equations A <sub>1</sub> correct output $\geq 3$ dp M <sub>1</sub> Attempt to solve equations A <sub>1</sub> correct output $\geq 3$ dp
b)	$P(X > 80) = P(Z > \frac{80 - 71.592}{11.1899})$ $P(Z > 0.751)$  $= 0.5 - \phi(0.751)$ $= 0.5 - 0.2737$ $= 0.2263$ Number of resultant = $300 \times 0.2263$ $= 67.89$ $= 68$	M <sub>1</sub> correct substitution A <sub>1</sub> correct probability $\geq 4$ dps M <sub>1</sub> correct multiplication A <sub>1</sub> correct output $\geq 4$ dps
12 Marks		
16.a)	$\underline{R} = (-2\hat{i} + 3\hat{j}) + (-\hat{i} + 2\hat{j}) + (4\hat{i} - 2\hat{j}) + (-\hat{i} - 3\hat{j})$ $= (-2 - 1 + 4 - 1)\hat{i} + (3 + 2 - 2 - 3)\hat{j}$ $\underline{R} = 0\hat{i} + 0\hat{j}$ The system either forms a couple or is in equilibrium Taking moments ; $\begin{vmatrix} x_1 & x \\ y_1 & y \end{vmatrix}$ moment of constituent forces $G = \begin{vmatrix} -2 & -2 \\ 3 & 3 \end{vmatrix} + \begin{vmatrix} 3 & -1 \\ 1 & 2 \end{vmatrix} + \begin{vmatrix} -1 & 4 \\ -3 & -2 \end{vmatrix} + \begin{vmatrix} 3 & -1 \\ 1 & -3 \end{vmatrix}$ $= (-6 + 6) + (6 + 1) + (2 + 12) + (-9 + 1)$ $= 13 \text{ Nm}$	M <sub>1</sub> addition of forces B <sub>1</sub> correct output M <sub>1</sub> for all correct moments B <sub>1</sub> correct values of G with units

Therefore the system forms a couple of torque 13NM Since $F = 0$ and $G \neq 0$ , the system forms a couple (of torque 13NM)	B <sub>1</sub> correct conclusion
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<p>b)</p> <p>Resultant force</p> $\underline{R} = (-2\hat{i} + 3\hat{j}) + (-\hat{i} + 2\hat{j}) + (4\hat{i} - 2\hat{j}) + (2\hat{i} + \hat{j})$ $= (-2 - 1 + 4 + 2)\hat{i} + (3 + 2 - 2 + 1)\hat{j}$ $\underline{R} = (3\hat{i} + 4\hat{j}) \text{ N}$ <p>Let <math>(x\hat{i} + y\hat{j})</math> be the general point of the equation of the line of action of the resultant force.</p> <p>Moment of resultant force = sum of moments of constituent forces.</p> $\begin{vmatrix} x & 3 \\ y & 4 \end{vmatrix} = (-6 + 6) + (6 + 1) + (2 + 12) + \begin{vmatrix} 3 & 2 \\ 1 & 1 \end{vmatrix}$ $4x - 3y = 21 + (3 - 2)$ $4x - 3y = 22$ <p>Therefore <math>4x - 3y - 22 = 0</math> (line of action)</p> <p>When the line crosses the X - axis, <math>y = 0</math>, <math>4x - 22 = 0</math></p> <p>Therefore <math>x = 5.5</math> units from origin</p>	<p>M<sub>1</sub> addition of forces.</p> <p>B<sub>1</sub> correct resultant</p> <p>M<sub>1</sub> obtaining moments M<sub>1</sub> equating moments. B<sub>1</sub> correct equation of the line of action</p> <p>M<sub>1</sub> substitution of <math>y = 0</math></p> <p>A<sub>1</sub> correct output</p>
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$(5.5, 0)$



