P425/2 Applied Mathematics Paper 2 July - August, 2024 3 hours



# UGANDA MUSLIM TEACHERS' ASSOCIATION UMTA JOINT MOCK EXAMINATIONS 2024 UGANDA ADVANCED CERTIFICATE OF EDUCATION

## **Applied Mathematics**

Paper 2 3 hours

#### **INSTRUCTIONS:**

- Answer all the eight questions in section A and any five from section B.
- Any additional question(s) answered will not be marked.
- All necessary working must be shown clearly.
- Begin each number on a fresh sheet of paper.
- Graph paper is provided.
- Silent, non-programmable scientific calculators and mathematical table with a list of formulae may be used.
- In numerical work, take acceleration due to gravity g, to be 9.8ms-2

### Include the allocation table on your answer sheet

Question	Marks
Section A	
9	
10	
11	
12	
13	
14	
15	
16	
Total	

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#### **SECTION A (40 MARKS)**

Answer all questions in this section.

- 1. Over a period of time, Julian finds that on long-distance flights, he flies economy. class on 82% of the flights. On the rest of the flights, he flies first class. When he flies economy class, the probability that he gets a good night's sleep is x. When he flies first class, the probability that he gets a good night's sleep is 0.9.
  - (a) The probability that Julian gets a good night's sleep on a randomly chosen flight is 0.285. Find the value of x. (02 marks)
  - (b) Given that on a particular flight, Julian does not get a good night's sleep, find the probability that he is flying economy class. (03 marks)

2. A particle is projected from a point O with initial velocity 30 ms<sup>-1</sup> at an angle tan<sup>-1</sup>(2) to the horizontal. Find its height above **O** when its speed is 20 ms<sup>-1</sup>.

Item	Price		Jx x 14
	2022 = 100 %	2023	S. Julius
Flour per kg.	6000	7800	5
Sugar per kg.	5000	4000	77
Eggs per egg.	500	700	M
Milk per litre	2000	2500	20

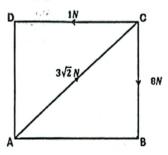
Calculate the simple price index for the cost of making a cake. Comment on your result. (05 marks)

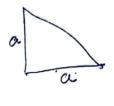
Use trapezium rule with four sub intervals to estimate  $\int_{0.2}^{1.0} \frac{x}{2 + \cos x} dx$  correct to two (2) (2) (2) (05 marks) significant figures.

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5. Three forces of magnitudes 1N, 8N and  $3\sqrt{2}$  N act along CD, CB and AC respectively as shown. ABCD is a square of side a units.





Consider AB and AD as x and y-axes respectively. Taking moments about A, show that the equation of line of action of the resultant is 2y + 5x - 7a = 0. (05 marks)

6. The probability density function (pdf) of a Continuous random variable X is given by,

$$f(x) = \begin{cases} \frac{4}{9}x(1-x^2); -2 \le x \le 1\\ 0; \text{ Otherwise} \end{cases}$$

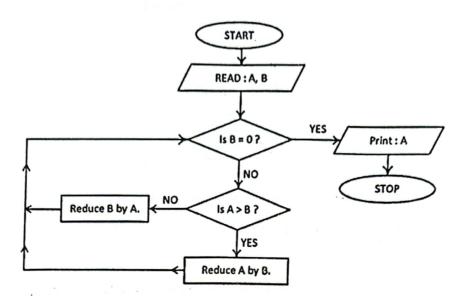
Find the mode of X.

(05 marks)

7. A body of weight 49N lies on a rough plane which is inclined at 35° to the horizontal. The angle of friction between the plane and the body is 20°. Find the magnitude of the least force that must be applied to the body in a direction parallel to and up the plane to hold the body in equilibrium. (05 marks)



8. Study the flow chart below.



Perform a dry run for A = 8 and B = 10.

(05 marks)

# **SECTION B (60 MARKS)**

Answer any five questions from this section.

All questions carry equal marks.

9. The patients at a chest clinic were asked to keep a record of the number of cigarettes they smoked every day.

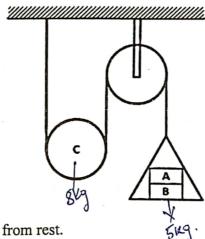
Number of cigarettes	Frequency
0-9	5
10 – 14	8
15 – 19	32
20 – 29	41
30 – 39	16
40 – 49	2

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- (a) Use the frequency distribution table to estimate the;
  - (i) Mean.
  - (ii) Number of patients who smoked 25 cigarettes and below. (07 marks)
- (b) Draw a histogram to represent the data. Use it to estimate the mode. (05 marks)
- √10. The diagram below shows three particles A, B and C of mass 3kg, 2kg and 8kg respectively. One end of a light inextensible string is attached to a ceiling. The string passes under a moveable pulley C and then over a fixed smooth pulley. To the other end of the string is attached a light scale pan in which two weights A and B are placed with A on top of B.



The system is released from rest.

- (a) Calculate the;
  - (i) Acceleration of the particle, C.

(09 marks)

(ii) Tension in the string.

(03 marks)

- (b) Find the reaction between the weights A and B.
- 11. Show that one of the roots of the equation  $x^2 3x + 1 = 0$  lies between 2 and 3.

Hence use linear interpolation to find the root correct to two decimal places.

(12 marks)

**3**-4

3-2.5 = 3-7

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- 12. The marks of 400 students in a certain test are normally distributed with a mean of 54 marks and a standard deviation of 9 marks.
  - (a) Given that the pass mark is 38, estimate the number of students who passed the test. (05 marks)
  - (b) Find the probability that a student selected at random scored between 49 and 57 marks. (04 marks)
  - (c) If a sample of 10 students was taken at random, determine the probability that at least one scored between 49 and 57. (03 marks)
  - 13. A ship P steaming at 20 kmh<sup>-1</sup> in the direction N50°E is 120 km due West of a ship Q steaming at 12 kmh<sup>-1</sup> in the direction N30°W. Find the;
    - (a) Shortest distance between them in the subsequent motion and the time taken to reach this position. (07 marks)
    - (b) The time for which the ships are within a range of 50 km from each other.

(05 marks)

- $\checkmark$ 14. Two decimal numbers X and Y have been approximated by X and Y with errors  $\Delta X$  and  $\Delta Y$  respectively.
  - (a) Show that the maximum relative error made in approximating  $x\sqrt{y}$  by  $X\sqrt{Y}$  is given by  $\left|\frac{\Delta X}{X}\right| + \frac{1}{2}\left|\frac{\Delta Y}{Y}\right|$ . (08 marks)
  - (b) Given that **X** and **Y** have been measured as 1.824 and 3.9 respectively, determine the percentage error made in the expression  $X\sqrt{Y}$ . (05 marks)
- 15. A box contains 3 red, 2 green and 1 yellow balls. When a ball is drawn from the bag, it is returned together with a ball of the same colour. If two such random draws are made,
  - (a) Construct a probability distribution table for the number of red balls in the bag after the two draws. (06 marks)

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(20) (2+8x) Tyrox 6017
(21 82) 2 xy

(b) Determine the;

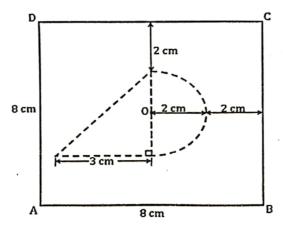
- (i) Expected number of red balls.
- (ii) Median number of red balls.

(04 marks)

(c) Sketch the Cumulative probability distribution.

(02 marks)

16. ABCD is a uniform square lamina of side 8cm. A hole made up of a right-angled triangle and a Scmi circle with centre O and radius 2cm was cut off from the square as shown in the diagram below.



- (a) Find the position of the centre of gravity of the remaining sheet. (09 marks)
- (b) The remaining sheet is then suspended about **B**, determine the angle side **AB** makes with the horizontal. (03 marks)

**END**