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# "ELECTROSTATICS"

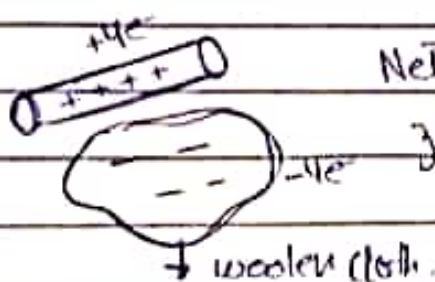
## CHARGE:

=> property which produced Electric field  
 => This is conserved & quantized.

$$q = ne \rightarrow \text{charges are quantized i.e. } 1e, 2e, 3e, \dots$$

↳ smallest charge in nature

$$e = 1.6 \times 10^{-19} \text{ C}$$



Net charge produced is always zero i.e. conserved  
 $+4e - 4e = 0e$

## ELECTRIFICATION:

=> process of charging of bodies

① => By conduction → physical contact is used

② => By Induction → just field interaction.

## CHARGE DENSITY:

charges per unit dimension (l, A, V)

### ① LINEAR CHARGE DENSITY:

$$\lambda = \frac{q}{l} \rightarrow \lambda \propto q$$

$$\rightarrow \lambda \propto 1/l$$

### ② SURFACE CHARGE DENSITY:

$$\sigma = \frac{q}{A} \rightarrow \sigma \propto q$$

$$\rightarrow \sigma \propto 1/A$$



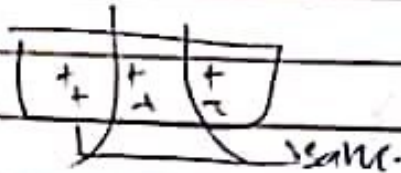
### ⑤ VOLUME CHARGE DENSITY:

$$\rho_v = \frac{q_v}{V} \quad \rho_v \propto \frac{q}{V}$$

### Uniform charge Distribution:

→ charge density is constant

If we divide a sheet → and sheet is uniformly charge distributed & we divide the sheet into 3 parts then the surface charge density on all the parts will be same.

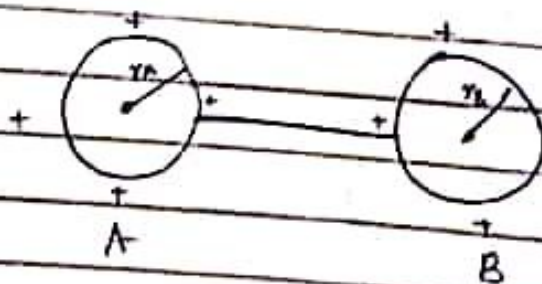


on all the parts will be same!

CHARGES → cause →  $\Delta V$  → difference in charge density

→ charges will flow b/w 2 bodies unless charge density becomes same.

### MCA:



no potential diff b/w the spheres

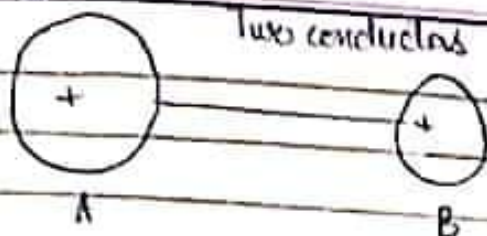
$$q_A = q_B \text{ same charges density}$$

So; no charges flow coz  $\Delta V = 0$  so potential = const and  $I = 0$

If  $r \neq \text{constant}$  then  $\Delta V \neq 0$



MCQ:-



(b)

mag of  $\rightarrow Q_A = Q_B$   
 $r_A > r_B$

more radius  $\rightarrow$  less charge density so charges will flow from B to A

Correct statement:

(a) charges flow from A to B

(b) from B to A

(c) no charges flow

(d) none

$$\rho \propto \frac{1}{r}$$

less size  $\rightarrow$  more charge density so flow is from high charge density to low charge density

## COULOMB'S LAW:

$$F \propto q_1 q_2 \quad (\epsilon \text{ d medium} = \text{constant})$$

$$F \propto \frac{1}{r^2} \quad (q_1, q_2 \text{ \& } \epsilon_m = \text{constant})$$

$$F \propto \frac{1}{\epsilon_r} \quad \text{or} \quad F \propto \frac{1}{\epsilon_m} \quad (q_1, q_2 \text{ \& } r = \text{constant})$$

$\epsilon_m$  - permittivity of medium

$$F = \frac{k q_1 q_2}{r^2}$$

:- P.D.M

$$F = \frac{1}{4\pi\epsilon_0} \times \frac{q_1 q_2}{r^2}$$

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$$F_m = \frac{1}{4\pi\epsilon_m} \times \frac{q_1 q_2}{r^2}$$

OR //

$$F_m = \frac{1}{4\pi\epsilon_0\epsilon_m} \times \frac{q_1 q_2}{r^2}$$

$$F_m = \frac{F_v}{\epsilon_r}$$

$$\epsilon_r = \frac{1}{\text{med.}}$$

$\epsilon_r = \epsilon_m$	→ permittivity of medium
$\epsilon_s$	→ permittivity of free space / vacuum

relative permittivity

$$\epsilon_m = \epsilon_r \epsilon_0$$

for vacuum

$$\epsilon_r = 1$$

for air

$$\epsilon_r = 1.0006$$

for all other mediums

$$\epsilon_r > 1$$

$$\epsilon_r = \frac{F_v}{F_m}$$

$$\epsilon_r^{-1} = \frac{1}{\epsilon_r} = \frac{F_m}{F_v}$$

M.C.Q:

$$F_v = 40 \text{ N} \quad F_m = 5 \text{ N}$$

(a)

$$\epsilon_r = ? \quad \epsilon_r = \frac{F_v}{F_m} = 8$$

(a) 8    (b) 16    (c) 40    (d) 5



$\epsilon_1$  ~~is~~ dimensionless

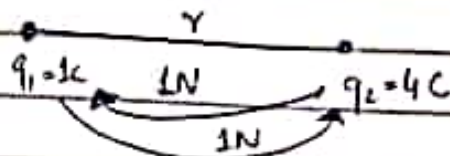
$\epsilon_m$  = not dimensionless

$$\hookrightarrow \epsilon_m = \frac{q_1 q_2}{F r^2}$$

Coulomb's law also obey Newton's 3rd law:

$$\vec{F}_{12} = -\vec{F}_{21}$$

Coulombic force is a mutual force.



If  $q_1$  exerts  $1N$  force on  $q_2$  then  $q_2$  will exert same force on  $q_1$  i.e.  $F_{12} = -F_{21}$  &  $q_2$  will not exert  $4N$  force.

MQA:

$$q_1 = 8C \quad \text{---} \quad x = 5C$$

$$q_2 = 3C \quad \text{---} \quad x = 5C$$

$$F_1 = F$$

$$F_2 = ?$$

$$q_1' = 3C$$

$$q_2' = -2C$$

$$q_1 \times q_2 = 24C$$

$$q_1' \times q_2' = -6C$$

$$\frac{24}{-6} = 4$$

$$\text{so: } 24 = 6 \times 4$$

4

$q_1' q_2'$  decreases 4 times so

force will be decrease 4 times so;

$$F_2 = F/4$$

or

$$F_2 = -F/4$$

## • ELECTRIC FIELD INTENSITY:

$$E = F/q_0 \quad \begin{array}{l} q_0 \rightarrow \text{test charge.} \\ q \rightarrow \text{source charge.} \end{array}$$

field strength of source charge.

To test field of source charge.

$$q_0 \ll q$$

$$\vec{E} = \lim_{q_0 \rightarrow 0} \vec{F}/q_0$$

$$\boxed{E = F/q_0} \rightarrow \text{analogue of } \boxed{g = w/m} \rightarrow \text{gr. field strength}$$

$$\text{Unit: } N/C = V/m$$

$\vec{E}$  is a vector

① has mag  $E = F/q_0$

② direction  $\rightarrow$  as that of  $\vec{F}$  force.

**Electric field intensity due to pt charge**

$$E = Kq/r^2$$

or

$$E = \frac{1}{4\pi\epsilon_0} \times q/r^2$$

or

$$E_m = \frac{1}{4\pi\epsilon_m} \times q/r^2$$

$$E_m = \frac{1}{4\pi\epsilon_0\epsilon_r} \times q/r^2$$

$$\rightarrow E \propto q$$

$$\rightarrow E \propto 1/r^2$$

$$\rightarrow E \propto 1/\epsilon_r \quad \text{or} \quad E \propto 1/\epsilon_m$$



- Primary source to observe electric field is by charge.



$\Phi$

$$E_m = \frac{E_v}{\epsilon_r}$$

$\epsilon_r$

$$\Rightarrow \epsilon_r = \frac{E_{vacc}}{E_{med}}$$

$$E_{med} < E_{vacc}$$

- Electric polarization:



slightly displacement b/w nucleus & electrons of an atom known as electric polarization.

- permittivity:

The capability of medium to polarize  $\rightarrow$  permittivity.

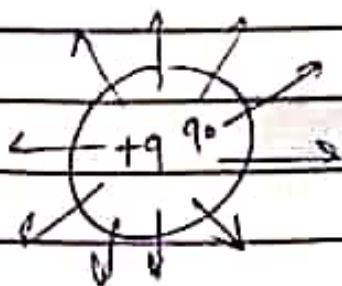
Coulombs law is only applicable for pt charges & is always known as "Action at distance Law".

## ELECTRIC FIELD LINES:

### Electric field.

$\Rightarrow$  This is a vector field & a real field

$\Rightarrow$  The imaginary lines drawn in the direction of force  $\rightarrow$  electric field lines.



for +ve test charge: positive source charge is source of field lines & -ve source charge is sink of field lines. & opp for -ve char



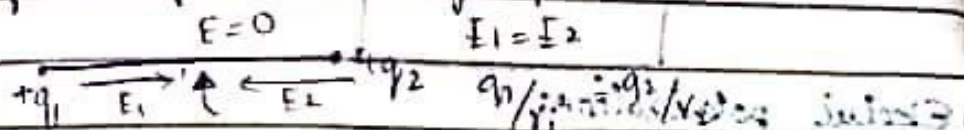
→ Infinite field lines can be drawn around a single charge -

→ Field lines are discrete and not continuous.

→ field lines can be straight or curved -

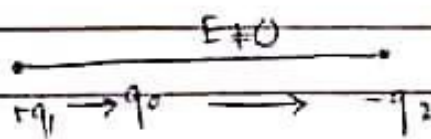


B/w 2 similar charges → there is a pt where  $E = 0$  but only at a single pt -



B/w similar charges, there will be single point on a line joining two charges where  $E = 0$  (null pt)

but b/w 2 opposite charge & null pt don't lie on line joining two opp charges. B/w 2 charges -



Similar to ...

$$E_1 = E_2$$

$$\frac{q_1}{r_1^2} = \frac{q_2}{r_2^2}$$

$\frac{q_1}{r^2} = \text{constant (at null pt)}$

$$q \propto r^2$$

$$r \propto \sqrt{q}$$

$$\frac{r_1}{r_2} = \sqrt{\frac{q_1}{q_2}}$$

MCQ-

$$q_1 = 10$$

$$q_2 = 4$$

$$r = 3 \text{ m}$$

$$\frac{r_1}{r_2} =$$

$$r_2 =$$

$$\frac{r_1}{r_2} =$$

$$\frac{r_1}{r_2} =$$

$$\frac{r_1}{r_2} =$$

$$\frac{r_1}{r_2} =$$

$$\frac{r_1}{r_2} =$$

$$\frac{r_1}{r_2} =$$

MCQ- field

q1

q2

u

electric

(a) 2cm

(b) 6cm

(c) 3cm

(d) None

∴ r

divide 11  
given



MCQ

$$q_1 = 1C$$

$$q_2 = 4C$$

$$r = 3m$$

$$\frac{r_1}{r_2} = \sqrt{\frac{1}{4}}$$

$$\frac{r_1}{r_2} = \frac{1}{2}$$

$$r_1 = 1m : 2m$$

$$r_2 = 2m : 1m$$

$$r_1 = 1m : r_2 = 2m$$

(dist. ratio)

MCQ. Pick → divide the given distance in ratio

$$q_1 = 6C$$

$$q_2 = 2C$$

where distance b/w charges is 8cm then pt where electric field intensity will be 0 will be —

(a) 2cm from  $q_2$  & 6cm from  $q_1$

(b) 6cm from  $q_2$  & 2cm from  $q_1$

(c) 3cm from  $q_2$  & 5cm from  $q_1$

(d) None

$$\frac{r_1}{r_2} = \sqrt{\frac{q_1}{q_2}}$$

$$\frac{r_1}{r_2} = \sqrt{\frac{6}{2}} = \sqrt{\frac{6}{2}} = \sqrt{3}$$

$$\frac{r_1}{r_2} = \frac{\sqrt{3}}{1} = \sqrt{3} : 1$$

$$\frac{r_1}{r_2} = \sqrt{3} : 1$$

$$q_1 = 9C$$

$$q_2 = 1C$$

$$\frac{r_1}{r_2} = 3 : 1$$

$$\text{sum} = 4$$

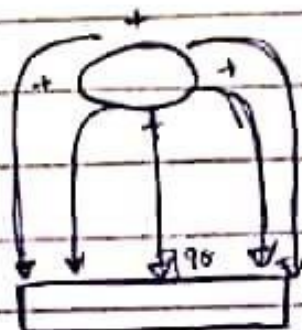
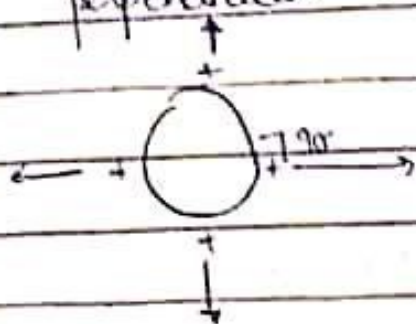
give  $r = 8cm$  so  
x 4 with a no so we  
get 8 i.e.  $\frac{8}{4} = 2cm$

$$\frac{r_1}{r_2} = 6cm : 2cm$$

divide the given distance in the given ratio simply



→ Electric field lines will always originate perpendicular & also terminate perpendicular.



cos if other  $\theta$  (angle) the lines will overlap.

### Uniform field:

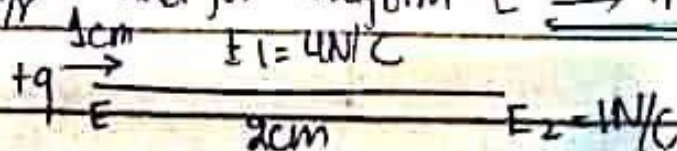
→ constant magnitude & constant direction  
( $E = \text{constant}$ )

⇒ 100% uniform field can't be produced but electric field b/w 2 oppositely charged plates having infinite length & negligibly small separation is approximately uniform.



If field is uniform the ' $E$ ' will be independent of ' $r$ ' (distance)

→ Electric field around a pt charge can never be zero. then  $E \propto 1/r^2$  and for uniform  $E \rightarrow$  independent of ' $r$ '



$$F_k = \frac{1}{k} \cdot \frac{1}{r^2}$$



## APPLICATION OF ELECTROSTATICS:

### XEROGRAPHY.

#### Working Principles

- neutralization of charges / electrostatic interaction
- > Aluminium drum -> part of Photocopier machine.
- > page is more +vely charged than aluminium drum.

#### Electric Flux :

$$\Phi_e = \vec{E} \cdot \vec{A}$$

$$\Phi_e = EA \cos \theta$$

$$E = \frac{\Phi_e}{A \cos \theta}$$

- ve flux  $\rightarrow$  inward flux.

$$\theta = 0^\circ$$

$$\cos 0^\circ = 1$$

$$E = \frac{\Phi_e}{A} \quad \text{field lines density}$$

$$E \propto \text{field lines density} \rightarrow \Phi_e / A$$

$$\Phi_e = 10 \text{ Nm}^2 / \text{C}$$

$$A = 1 \text{ m}^2$$

$E = 10$  field lines per  $1 \text{ m}^2$  area.

$$E \propto q$$

$$\text{Electric field line density} \propto \text{charge (q)}$$



of  
**GAUSS'S LAW** (Generalized form of Coulomb's Law)  
 $\Phi_E = \vec{E} \cdot \vec{A}$  for open flat area

flat area  $\rightarrow$  vector area  
closed area  $\rightarrow$  never a vector

flux through closed surface

$$\Phi_{ET} = \sum_{i=1}^n \vec{E}_i \cdot \Delta \vec{A}_i$$

$$\Phi_{ET} = \vec{E}_1 \cdot \Delta \vec{A}_1 + \vec{E}_2 \cdot \Delta \vec{A}_2 + \dots + \vec{E}_n \cdot \Delta \vec{A}_n$$

- $\rightarrow$  Coulomb's law is only for point charges.
- $\rightarrow$  Gauss's law is for point charges + distribution of charges.

Total flux is equal to  $1/\epsilon_0$  the total charge enclosed

$$\Phi_{ET} = 1/\epsilon_0 (Q) \quad \text{et} \rightarrow \text{total electric flux!}$$

$$\Phi_{ET} = \frac{Q}{\epsilon_m}$$

$\rightarrow$  Gauss's for 1<sup>st</sup> time measured magnitude of charge from flux -  
 source

$$Q = \epsilon_0 \Phi_{ET}$$

$$Q = q\epsilon_0$$



$$Q = \epsilon_m \phi_{ei}$$

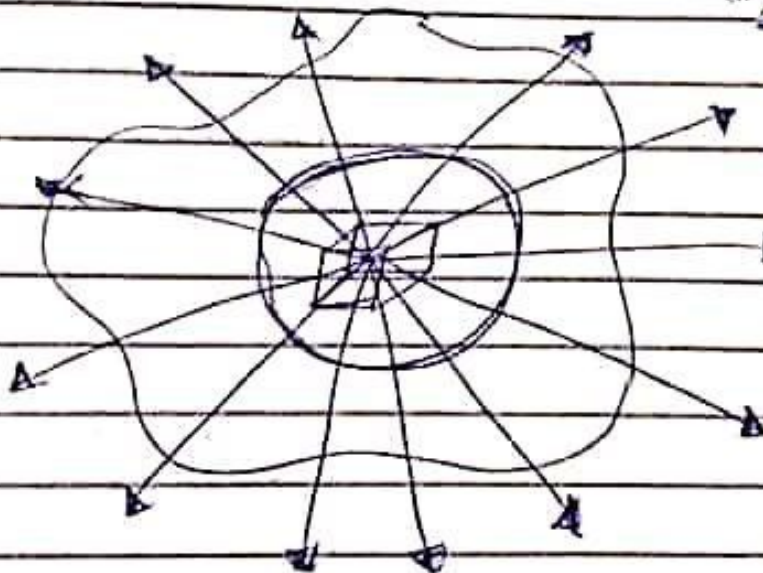
$$Q = \epsilon_r \epsilon_0 \phi_{ei}$$

→ Gauss's law is only for closed surfaces

$$\phi_{ei} \propto Q \quad (\epsilon_m = \text{constant})$$

$$\phi_{ei} \propto \frac{1}{\epsilon_m} \quad (Q = \text{constant})$$

→ Independent of shape of closed surface  
(ii) size of closed surface



flux through all the surfaces is same either cube sphere or arbitrary body

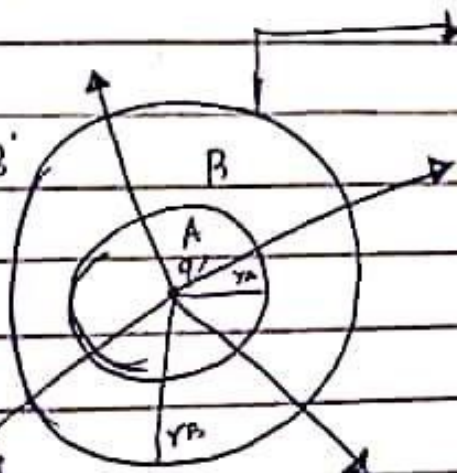
If 2 spheres 'A' & 'B' and  $r_B > r_A$

then and charge

lie at the centre of

sphere then correct statement -

→ Net flux through both spheres



∴ Correct Statement (a)

- (a) ~~flux~~  $\phi_A = \phi_B$
- (b)  $\phi_A > \phi_B$
- (c)  $\phi_A < \phi_B$
- (d) None



Two spheres of radius  $r_A$  &  $r_B$  which is concentric & "q" charge lie at the centre of 2 spheres then which statement is correct about flux through unit area of both sphere.  $r_B > r_A$   $\Phi \propto 1/r^2$  (b)

(a)  $\Phi_A = \Phi_B$

(b)  $\Phi_A > \Phi_B$

(c)  $\Phi_A < \Phi_B$

(d) None

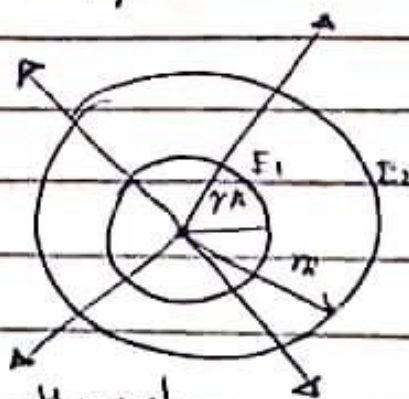
Flux:

as unit area  $\rightarrow$  do same area and not mentioned ~~is a~~ ~~or~~ ~~open~~ ~~surface~~.

$$\Phi = EA = \frac{kq}{r^2} \times A$$

$$\Phi \propto 1/r^2$$

$$\Phi_A > \Phi_B$$

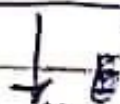


$$E_1 \neq E_2$$

$$E \propto 1/r^2$$

$$E_1 > E_2 \quad (r_B > r_A)$$

flux through both sphere = same  
flux through unit area is not same



flat area is given

close area = same flux  $\rightarrow$  independent on "r"  
unit / flat area - diff flux  $\rightarrow$  depends on "r"

is this  
gh  
(b)

$$r_A = 1 \text{ cm}$$

$$E_A = 4 \text{ N/C}$$

$$E_B = ?$$

$$r_B = 2 \text{ cm}$$

$$E_B = 1 \text{ N/C}$$

$$E_B = r_A^2$$

$$E_A = r_B^2$$

$$E \propto 1/r^2$$

Flux:

$$(a) \quad \Phi_{\text{net}} = +q/\epsilon_0$$

$$\rightarrow \text{If flux} = +ve$$

$$\rightarrow \text{outward flux}$$

$$\rightarrow Q = +ve$$

$$(b) \quad \Phi_{\text{net}} = -q/\epsilon_0$$

$$\rightarrow \text{If flux} = -ve$$

$$\rightarrow \text{inward flux}$$

$$\rightarrow Q \text{ enclosed is } -ve.$$

Imp Concept:



$$\Phi_{\text{net}} = -ve \text{ (flux)}$$

$$Q_{\text{enc}} = -ve \text{ (charge)}$$

∴ inward flux is more than outward flux.

∴ inward flux < outward flux



$$\Phi_{\text{net}} = +ve$$

$$Q_{\text{enc}} = +ve$$

inward flux > outward flux


$$-ve > +ve$$



$$\Phi_{\text{net}} = 0$$

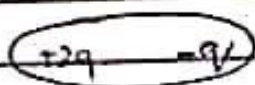
$$Q_{\text{enc}} = 0$$



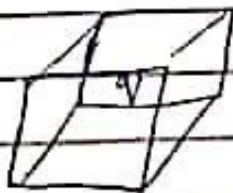

 $\theta = 0$   
 $\Phi_{\text{net}} = 0$        $\Phi_{\text{net}} = \frac{q}{\epsilon_0}$   
 no charge enclosed so  $Q = 0$  &  $\Phi = 0$



$\Phi_{\text{net}} = 0$        $q_{\text{net}} = -q + q = 0$



$\oplus$   $q_{\text{net}} = +ve$   
 $\Phi_{\text{net}} = +ve$



$\Phi_{\text{net}} = \frac{q}{\epsilon_0}$

$\Phi = \frac{1}{6} \left( \frac{q}{\epsilon_0} \right)$       "by symmetry"

from 2 faces

$\Phi = \frac{2}{6} \left( \frac{q}{\epsilon_0} \right)$

from 3 faces

$\Phi = \frac{3}{6} \left( \frac{q}{\epsilon_0} \right)$

from 4 faces

$\Phi = \frac{4}{6} \frac{q}{\epsilon_0}$  or  $\frac{1}{2} \left( \frac{q}{\epsilon_0} \right)$

Application

(i)  $r$

$\therefore E = \frac{q}{4\pi\epsilon_0 r^2}$

$\downarrow$   
 $E_{\text{net}}$   
 $\rightarrow$  Electric field

(ii)  $r$   $E_{\text{net}}$

If charge is uniformly distributed  
 in a cylinder of radius  $r$   
 then  $E$  is independent of distance

Dependence



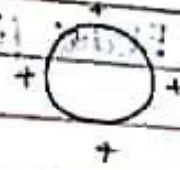
# Application Of Gauss's Law:

(i) :-

$E = 0$  inside a charged conductor.

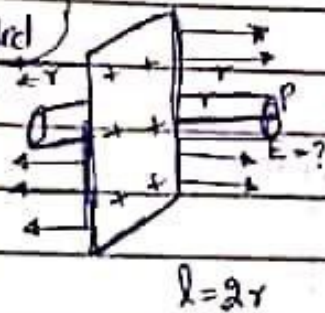
Electrostatic Equilibrium:

→ Electric field lines don't pass through conductor.



(ii) :- Electric field intensity due to Infinite sheet of charges:

If charges are distributed uniformly then  $E$  is independent on distance ' $r$ '



$$E = \frac{\sigma}{2\epsilon_0}$$

Dependence:

① magnitude of charge, ② surface area, ③ medium.

$$\sigma = q/A$$

$$E = \frac{Q}{2A\epsilon_0}$$

$$E_m = \frac{Q}{2A\epsilon_m}$$

$$E = \frac{Q}{2A\epsilon_r\epsilon_0}$$

$$E = -\frac{\sigma}{2\epsilon_0} \quad (\text{-ve charge distribution})$$

$E$  is always normal to the surface.

$$\vec{E} = \frac{\sigma}{2\epsilon_0} \hat{n}$$



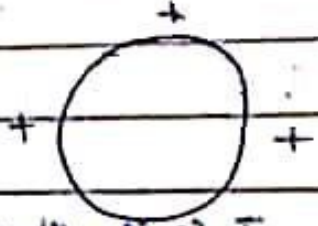
If charge distribution is : uniform & symmetrical then field enb/s will be same.

∴ (i)

ciii): Electric field intensity inside + outside a shell:

Case a:

a hollow body.



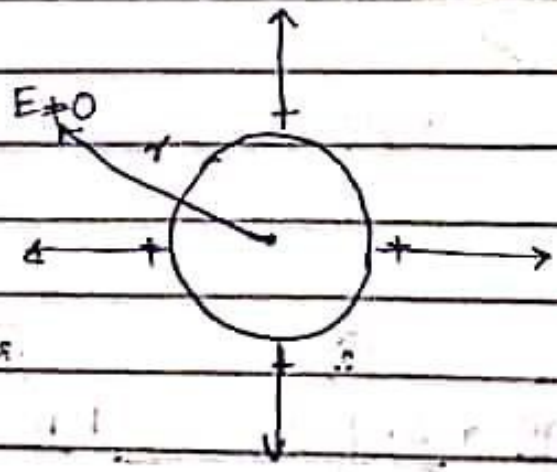
∴ (ii)

∴ (iii)

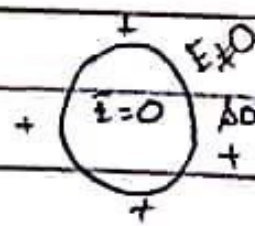
Inside  $\Rightarrow E=0$  ( $q=0$ )

Case b:

Outside: a shell:



$\Rightarrow$  for outside points charge conductor will behave like a point charge lie at the centre of charged: shell



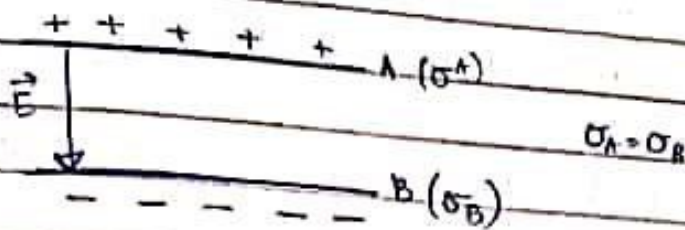
solid cylinder

$E_{\text{inside}} = 0$

$E_{\text{outside}} \neq 0$



(iv) Electric field intensity due to oppositely charged sheet:



$$E = \frac{\sigma}{\epsilon_0} \quad \text{If } \sigma_A = \sigma_B$$

$$E = Q$$

$$A \epsilon_0$$

If  $\sigma_A \neq \sigma_B$   
Then

$$E = \frac{\sigma_A}{2\epsilon_0} + \frac{\sigma_B}{2\epsilon_0}$$

If  $\sigma_A = \sigma_B$

$$E = \frac{\sigma}{2\epsilon_0} + \frac{\sigma}{2\epsilon_0}$$

$$E = \frac{2\sigma}{2\epsilon_0}$$

$$E = \frac{\sigma}{\epsilon_0}$$

→ If oppositely charged sheets  
E

$$E = 2E_s \text{ (single sheet)}$$

2 opp charged sheets →  $E = 2E_s$  (single sheet)

$$E = 2$$

$$E_s$$



study formulae relating to electric field between parallel plates

opposite  
plates

due to 2 opp charge plates =  $E$  then if  
we remove 1 sheet then  $E/2$

and if 1 sheet + other is ~~removed~~ added then  
 $E = 2E$

some  $E = 0$

(i)  $E = 0$

if  $\sigma_A = \sigma_B$

(ii) if  $\sigma_A > \sigma_B$

then  $E_A > E_B$

$E_{net}$  is directed along  $E_A$

if  $\sigma_A < \sigma_B$   
then  $E_B > E_A$

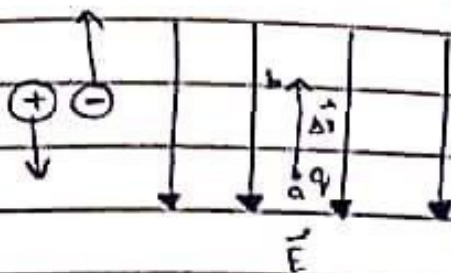
• ELECTRIC FIELD





If we construct a surface below the -ve charge then  $E \neq 0$  cos charge enclosed  $\neq 0$

## • ELECTRIC POTENTIAL ENERGY:



If we do work against field then work will be store as energy - (P.E).

$$W_{a \rightarrow b} = \Delta U = 0$$

If  $v = \text{constant}$  electric potential energy

If  $(+q) \rightarrow$  in direction of Electric field

If  $v \neq \text{constant (velocity)}$

$$a \neq 0$$

$$W_{a \rightarrow b} \neq \Delta U$$

Wc of energy lost.

Electric Potential is the work done per unit charge

or  
P.E change per unit charge.

$$\Delta V = \frac{W_{a \rightarrow b}}{q_0}$$

or

$$\Delta V = \frac{\Delta U}{q_0}$$

$V = \frac{W}{q_0}$
---------------------

$$1 \text{ volt} = \frac{1 \text{ J}}{1 \text{ C}}$$



Potential Energy = Total work done =  $w$

Potential = work done per unit charge =  $w/q_0$

→ ABSOLUTE ELECTRIC POTENTIAL:

$$V = k \frac{q}{r}$$

$$V = \frac{1}{4\pi\epsilon_0} \frac{q}{r}$$

$$V_{med} = \frac{1}{4\pi\epsilon_m} \frac{q}{r}$$

or

$$V_m = \frac{1}{4\pi\epsilon_r\epsilon_0} \frac{q}{r}$$

$$V_m = \frac{V_v}{\epsilon_r}$$

$$V_m < V_v$$

$V \propto q$  → source charge.

$$V \propto \frac{1}{r}$$

$$V \propto \frac{1}{\epsilon_m} \quad \text{or} \quad V \propto \frac{1}{\epsilon_r}$$

$$\epsilon_r = \frac{V_{vac}}{V_{med}}$$

$$\frac{1}{\epsilon_r} = \frac{V_{med}}{V_{vac}}$$

MCQ: At some pt 1 at 'r' distance source charge 'q' (c)  
 Electric field intensity were "E" and electric potential  
 were "V". Now at some other point electric field  
 intensity is  $E/4$  then potential at this point will be —

(a)  $V/4$

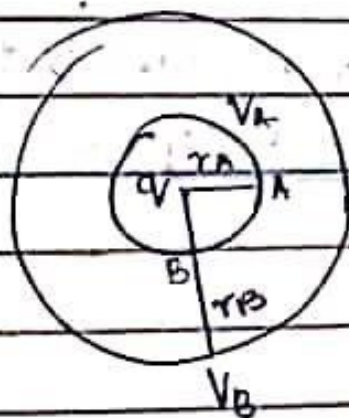
(b)  $4V$

(c)  $V/2$

(d)  $V$

$E \propto 1/r^2$  &  $V \propto 1/r$

$E \propto 1/(2)^2$  &  $V \propto 1/2$



$V_A > V_B$

CO2

~~$r_B > r_A$~~

$V \propto 1/r$

$r_B > r_A$

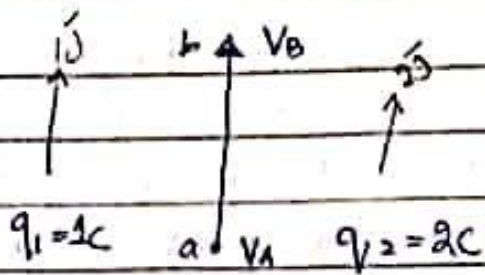
If  $r_B = 2r_A$  then

$V_B = V_A/2$

$V \rightarrow$  independent of magnitude of test charge.

but  $E \rightarrow$  depends upon mag of test charge.





$$V = \frac{W}{q}$$

$$E = q_0 E$$

$$W = q_0 E \Delta r \text{ or } W = q_0 E \Delta r \cos \theta$$

$W \propto q_0$
$W \propto E$
$W \propto \Delta r$

Work done depends on mag of test charge.

$$\Delta V = W/q_0$$

$$\text{If } \Delta V = 1J / 1C = 1V$$

$$\Delta V = 2J / 2C = 1V$$

$$\Delta V = 10J / 10C = 1V$$

cos if we do work 1J on 1C charge then if we do work 10J then charge will be 10C cos

$$W \propto q_0$$

here 'W' & P.E will not be same but 'V' = 0

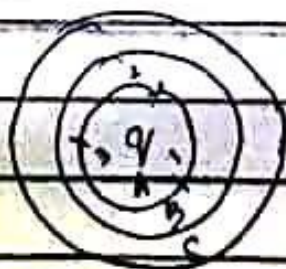
cos independent of  $q_0$  but depends on mag of 'V' will be same for source charge  $q_1$ .

### Equipotential Surface:

Surface at which electric potential is constant or same.

### Equipotential lines/circles:

$$V = \text{constant}$$



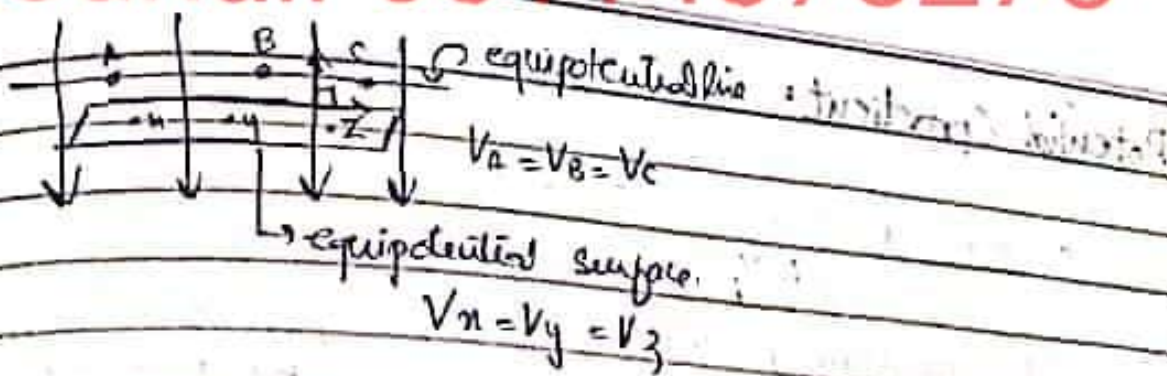
$$V_1 > V_2 > V_3 \text{ (as } r_1 < r_2 < r_3 \text{)}$$

$$\text{but } V_1 = V_2 = V_3$$

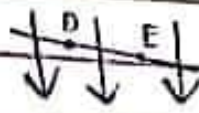
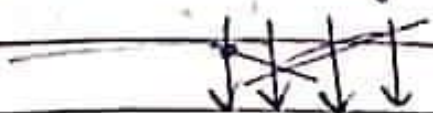
cos 'r' is same 'q' is



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equipotential line & surface is always perpendicular to electric field line.



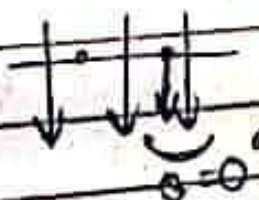
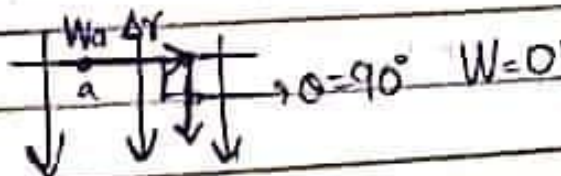
$$V_D \neq V_E$$

they can't overlap and are not perpendicular.

\* Work done to move a charge on equipotential surface or equipotential line is zero.

$$\cos \theta = 90^\circ$$

\* But if we move charge b/w 2 equipotential surface or line/circle, then work done will be non-zero.





## Potential Gradient:

Gradient  $\rightarrow$  change w.r.t distance / displacement  
( $\Delta/\Delta r$ )

$E =$  negative gradient of electric potential.

$$E = -\frac{\Delta V}{\Delta r}$$

$$E = -\frac{\Delta V}{\Delta r}$$

$E \rightarrow -ve$  (opp to direction of  $\vec{E}$ )

$\Delta V = +ve$   
 $V \rightarrow$  increases

$$-E = \frac{\Delta V}{\Delta r}$$

$E \rightarrow +ve$  (in the direction of  $\vec{E}$ ).

$\Delta V = -ve$   
 $V \rightarrow$  decreases

we know

if +ve test charge in the direction of  $E$  then

$V \rightarrow$  decreases & opp to  $E$  then  $V \rightarrow$  increases.

and if perpendicular then  $V=0$

and if -ve test charge then along  $\vec{E}$  then  $V \rightarrow$  increases and opp  $V \rightarrow$  decreases.

gradient (scalar) = vector

$$\Delta V (d) = E$$

$$E = \frac{\Delta V}{\Delta r}$$

$$\Delta V = E \Delta r$$

$$V = Ed$$

K. Energy

K. Energy of Charge:  $\rightarrow$  accelerating by using potential difference

$$K.E = q \Delta V$$

$$E.E = qV$$

for speed:

$$\frac{1}{2}mv^2 = qV$$

$$v = \sqrt{\frac{2qV}{m}}$$

Electron Volt:  $\rightarrow$  unit of energy (smaller)

$$1\text{eV} = 1.6 \times 10^{-19} \text{J}$$

$$n(1\text{eV}) = n(1.6 \times 10^{-19} \text{J})$$

$$1\text{J} = 1 \text{ eV}$$

$$1.6 \times 10^{-19}$$

$$n(1\text{J}) = n\left(\frac{1}{1.6 \times 10^{-19} \text{eV}}\right)$$

$$E = qV$$

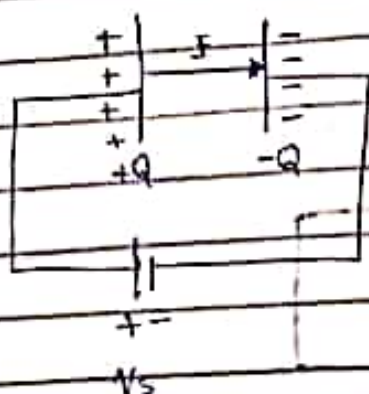
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## CAPACITOR:

Device used to store electrical charges & electric energy.

$$V_c = E_c d_c$$



net  $\uparrow$

$$Q_{\text{net}} = Q - Q = 0$$

$$|Q|$$

$$|Q| = |-Q| = Q$$

magnitude of  
total charge  $\uparrow$

during charging  $V_c < V_s$

but when capacitor is fully charged

$$V_c = V_s$$

$$V_{\text{max}} = V_s \quad (V_c = V_s = V_{\text{max}})$$

$$Q \propto V$$

$$Q = CV$$

unit  $\rightarrow$  farad  $\rightarrow$  larger unit

$$1F = \frac{1C}{1V}$$

$C \rightarrow$  independent of  $Q$  &  $V$

$$C = Q/V \rightarrow \text{always constant.}$$

$C \rightarrow$  depends upon

(a) geometric shape

(b) dimension ( $l, A, v$ )

(c) separation b/w plates

(d) medium

$$\epsilon_r = \frac{F_v}{F_m}$$

$$\epsilon_r = \frac{V_v}{V_m}$$

$$\epsilon_r = \frac{E_v}{E_m}$$

$$\epsilon_r = \frac{C_m}{C_v}$$

$$\epsilon_r = \kappa_v / \kappa_m$$

$$\epsilon_r = \frac{\epsilon_m}{\epsilon_v}$$

Capacitance of a capacitor and its dependence

$$C = A \epsilon_0 \epsilon_r / d$$

$$C = \frac{A \epsilon_0}{d}$$

$$C_m = \frac{A \epsilon_m}{d} = \frac{A \epsilon_r \epsilon_0}{d}$$

$$C_m = \epsilon_r C_v$$

$$\epsilon_r = \frac{C_m}{C_v}$$

$$C_m > C_v$$

$$C = \frac{A \epsilon_0}{d} \quad \left( \epsilon_0 = \frac{1}{4\pi k} \right)$$

$$C = \frac{A}{4\pi k d}$$

$$C \propto A$$

$$C \propto \epsilon_m \quad C \propto \epsilon_r \quad C \propto \epsilon_0$$

$$C \propto \frac{1}{d}$$



## Energy stored in a capacitor:

$$U = \frac{1}{2} QV$$

$$\text{or } U = \frac{1}{2} \frac{Q^2}{C}$$

$$\Delta U = \frac{1}{2} CV^2$$

$$\text{or } U = \frac{1}{2} \epsilon_0 E^2 (Ad)$$

$$U = \frac{1}{2} \epsilon_0 E^2 (Vol)$$

$$U = \epsilon_m E^2 (Ad)$$

$$U_m = \frac{1}{2} \epsilon_0 \epsilon_r E^2 (Vol)$$

If we put the medium  $\rightarrow$  energy stored will be increases  $\rightarrow$  mag of charges increases on each plate.

$$U \propto Q^2$$

$$U \propto \text{Volume}$$

$$U \propto C$$

$$U \propto A$$

$$U \propto V^2 \quad (\text{also})$$

$$U \propto E^2$$

$$U \propto \epsilon_m \quad \text{or } U \propto \epsilon_r$$

$$\text{If } V_c = E d \epsilon$$

If  $d \epsilon \rightarrow$  increases

$V_c$  increases then battery discharges

during charging  $\Delta V_{\text{error}} = V_s - V_c$

$\hookrightarrow V_c$  - increases

so  $\Delta V$  - decreases

when capacitor is fully charged

$$\Delta V_{\text{circuit}} = 0$$