P425/1
Pure Mathematics
Paper 1
July - August, 2024
3 hours



UGANDA MUSLIM TEACHERS' ASSOCIATION UMTA JOINT MOCK EXAMINATIONS - 2024 UGANDA ADVANCED CERTIFICATE OF EDUCATION

Pure Mathematics

Paper 1

3 hours

INSTRUCTIONS TO CANDIDATES

- Attempt all the eight questions in section A and five questions from section B.
- Any additional question(s) answered will not be marked.
- All working must be shown clearly. Begin each question on a fresh sheet of paper.
- Silent, nonprogrammable scientific calculators and mathematical tables with a list of formulae may be used.

SECTION A

1. $\int x^4 \ln x dx$

(05 marks)

2. Find the acute angle between the following lines, 2x + 3y = 7, x = 6y + 5

(05 marks)

3. If $y = \sqrt{\frac{1-\cos 2x}{1+\cos 2x}}$ show that $\frac{dy}{dx} = \sec^2 x$

(05 marks)

4. Show that the vectors 2i - j + k, i - 3j - 5k and 3i - 4j - 4k are coplanar.

(05 marks)

5. Solve for **x** from 0^0 to 360^0 Given that $\tan x + \tan 2x + \tan x \tan 2x = 1$

(05 marks)

6. Solve for **X** given $9 \log_x 5 = \log_5 x$.

(05 marks)

7. Find the area bounded by the curve y = (1-x)(x+2) and the x-axis.

(05 marks)

8. Solve for **X** Given $3^{2x+1} - 3^{x+1} - 3^x + 1 = 0$

(05 marks)

SECTION B

- 9. Given the curve $y = \frac{3x+3}{x(3-x)}$;
 - (a) Find the region where the curve does not lie, hence determine the turning points and their nature.
 - (b) State the asymptotes and find the intercepts.
 - (c) Sketch the curve.

(12 marks)

10. (a) Solve the equation $\sqrt{3-x} - \sqrt{7+x} = \sqrt{16+2x}$.

(06 marks)

(b) Solve for \mathbf{x} , \mathbf{y} , and \mathbf{z} given $\frac{x+2y}{-3} = \frac{y+2z}{4} = \frac{2x+z}{5}$ and x+y+z=2.

(06 marks)

- 11. (a) Show that $\frac{(\cos 4\theta + i\sin 4\theta)^3 (\cos 2\theta i\sin 2\theta)^5}{(\cos 3\theta + i\sin 3\theta)^4 (\cos 5\theta i\sin 4\theta)^6} = \cos 20\theta + i\sin 20\theta. \quad (06 \text{ marks})$
 - (b) Shade the region on Argand diagram of |z 1 i| < 3.

(06 marks)

12. Sketch the curves $y = 2x^2$ and $y = 10x - x^2$ on the same graph.

Find the volume generated when the area enclosed between the curves is rotated through 360° (12 marks)

13. (a) Prove that
$$\frac{\sin 5x - \sin 7x + \sin 8x - \sin 4x}{\cos 4x - \cos 5x - \cos 8x + \cos 7x} = \cot 6x.$$
 (06 marks)

- (b) Find all the possible values of **X** from 0^0 to 360^0 of the equation $4\cos x 6\sin x = 5$. (06 marks)
- 14. Partialise $f(x) = \frac{3x^3 + x + 1}{(x-2)(x+1)^3}$ Hence evaluate $\int_3^4 f(x) dx$. (12 marks)
- 15. (a) The gradient of the tangent at any point (x,y) of the curve is $x \frac{2y}{x}$.

 Given that the curve passes through (2,4). Find the equation of the curve. (06 marks) (b) Use substitutions y = vx to solve the differential equation

$$x^2 \frac{dy}{dx} = x^2 + y^2 + xy \tag{06 marks}$$

- 16. (a) Find the point of intersection between the line r = i + j 3k + t (2i + 2j + k) and the plane $r \cdot (6i 3j + 2k) = 13$ and find the angle between the two. (06 marks)
 - (b) Show that the following vectors form a right angled triangle

$$a = (3i - 2j + k), b = (i - 3j + 5k), c = (2i + j - 4k).$$
 (06 marks)

END