

# UGANDA ADVANCED CERTIFICATE OF EDUCATION

## S.5 APPLIED MATHEMATICS P425/2

TIME: 2½HOURS

Answer all questions in this paper

1. The sum of squares of 50 lengths measured to the nearest  $m$  is  $40,000m^2$  and the square of their sum is  $150,000m^2$ . Find the mean length and the standard deviation. (5marks)
2. Forces **P** and **R** of magnitudes 30N and 78N act in the directions of the unit vectors  $\frac{4}{5}\mathbf{i} - \frac{3}{5}\mathbf{j}$  and  $\frac{1}{13}(12\mathbf{i} - 5\mathbf{j})$  respectively. Find their resultant force. (5marks)
3. A bag contains 5 yellow, 4 black and 8 red cards. If three cards are picked at random, one after the other without replacement, find the probability that:
  - a. all are of different colours (2marks)
  - b. all the 3 cards are of the same colour (3marks)
4. Find the magnitude and direction of the resultant of the velocities  $15ms^{-1}$  and  $25ms^{-1}$  which are inclined at an angle  $60^\circ$  to each other. (5marks)
5. A discrete random variable  $X$  has a pdf defined by  $2P(X = 3) = 3P(X = 0) = \frac{1}{2}P(X = 1) = \frac{1}{2}P(X = 2)$ , if the  $P(X = 1) = 6k$ , find the value of  $k$  and the expected value of  $X$ . (5marks)
6. The resultant of the forces  $\begin{pmatrix} c+1 \\ 2 \end{pmatrix}N$ ,  $\begin{pmatrix} -3 \\ 2c \end{pmatrix}N$ ,  $\begin{pmatrix} 1-2c \\ 5 \end{pmatrix}N$  and  $\begin{pmatrix} 2 \\ -c \end{pmatrix}N$  is acting in the direction due NorthEast. Find the value of  $c$  and magnitude of the resultant. (5marks)
7. Below were the grades of six A-level students in Mathematics( $x$ ) and Physics ( $y$ )

$x$	D	E	F	A	E	B
$y$	A	D	B	C	F	E

Calculate the rank correlation coefficient for the data. (5marks)

8.  $A$  and  $B$  are two events such that  $P(A \cup B) = 0.75$ ,  $P(A \cap B') = 0.16$  and  $P(A \cup B') = 0.52$ . Find the  $P(A \cap B)$  and  $P(A'/B)$  (5marks)

### SECTION B

9. (a) A coin is biased such that the chances of getting a head are thrice those of getting a tail. If this coin is tossed three times and  $X$  is the random number of heads that show up in these throws,
  - (i) Construct a pdf for  $X$
  - (ii) Find the mean and variance for the number of heads. (7marks)(b) Given a random variable  $Y \sim B(20, 0.45)$  Find
  - (i)  $P(Y > 7)$
  - (ii)  $P(6 \leq Y \leq 13)$  (5marks)

10. The table below gives yearly earnings in millions of shillings, of a group of workers in a certain factory

<b>yearly earnings(in millions Ush)</b>	<b>No of workers</b>
10 – < 15	6
15 – < 20	27
20 – < 25	45
25 – < 30	30
30 – < 35	15
35 – < 40	16
40 – < 45	11

- (a) Calculate the: (i) mean yearly earning (3marks)  
(ii) standard deviation of the distribution (4marks)
- (b) Draw an ogive for the data and use it to find the percentage of workers earning sh43m and below (5marks)

**END**