

P425/2
APPLIED
MATHEMATICS
Paper 2
Jul./Aug. 2024
3 hours



BRIGHT EXAMINATIONS BOARD
Uganda Advanced Certificate of Education
APPLIED MATHEMATICS

Paper 1

3 hours

INSTRUCTIONS TO CANDIDATES:

*Answer **all** the eight questions in section A and any **five** questions from section B.*

*Any additional question(s) answered will **not** be marked.*

*All necessary working **must** be shown clearly.*

Begin each answer on a fresh sheet of paper.

Graph paper is provided.

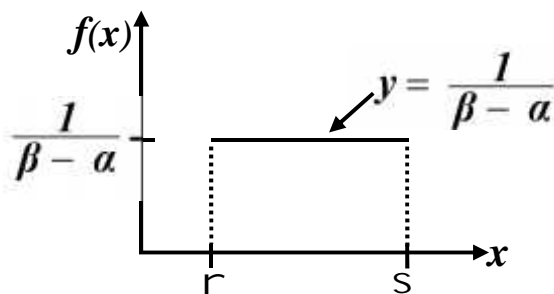
*In numerical work, take **g** to be **9.81ms^{-2}***

Silent, non-programmable scientific calculators and mathematical tables with a list of formulae may be used.

SECTION A: (40 MARKS)

Answer **all** the questions in this section.

- Given that $P(A) = 0.59$, $P(B) = 0.45$ and $P(A \cap B) = 0.15$, find:
 (a) $P(A \cup B)$
 (b) $P(\bar{A} \cap \bar{B})$ (05 marks)
- A particle moving with S.H.M has velocity $V^2 = 16(9 - x^2)$ when at a distance x from the Centre of its path O . Find the
 (a) amplitude and period of its motion
 (b) speed as it passes O (05 marks)
- Use the trapezium rule with 4 ordinates to evaluate the integral of $x \cos x$ between 60° and 90° correct to 4 decimal places (05 marks)
- A uniformly distributed r.v X on the interval $[r, s]$ is illustrated as follows:



Given that X has a lower quartile of 5 and an upper quartile of 9, use a graphical procedure to find the values of r and s (05 marks)

- Forces of magnitude 5N and 8N are acting away from each other at an angle of 60° . Given that their resultant is 7N, find the:
 (a) value of θ
 (b) angle θ makes with the resultant (05 marks)
- The table below shows the prices of items for the years 2016 and 2017

Item	PRICE (£)		Weights
	IN 2016	IN 2017	
A	25	28	5
B	x	y	3
C	30	36	2

Given that the simple aggregate price index and weighted mean price index for 2017 based on 2016 are 120 and 119 respectively, find the values of x and y (5 marks)

7. The iterative formula $x_{n+1} = \frac{1}{x_n^2} - 1$ or $x_{n+1} = \frac{1}{\sqrt{1+x_n}}$ is to be used as a solution to an equation. Using $x_0 = 0.75$, show without iterating that one of the choices is not suitable

(05 marks)

8. At 10:30 am, the position vector of ship P relative to ship Q at time t hours is

$$\mathbf{r}_{PQ} = (14 - 3t)\mathbf{i} + (12 - 5t)\mathbf{j} \text{ km}$$

- (a) Write down the velocity of P relative to Q

(01 mark)

- (b) Find the time at which the ships are closest together.

(04 marks)

SECTION B (60 MARKS)

Answer any **five** questions in this section.

All questions carry equal marks.

9. The weights in kg of 25 boys were as follows:

Weights	20 – 24	25 – 29	30	31 – 34	35 – 49
Frequency	3	5	2	6	9

- (a) Calculate the:

- (i) mean weight

(03 marks)

- (ii) number of boys weighing between 26.5kg and 32.5kg

(02 marks)

- (b) Display the data on a histogram and use it to estimate the mode

(7 marks)

10. A car of mass **m**kg has a maximum speed of **u**kmh⁻¹ up a hill inclined at an angle θ to the horizontal. It attains a maximum speed of **v**kmh⁻¹ when descending the same hill with the engine cut off. If the resistance to motion is proportional to the square of the speed,

- (a) Show that the power output of the engine is $\frac{5umg}{18v^2}(u^2 + v^2)\sin\theta$ (5 marks)

- (b) Find the power output of the engine if **m** = 900kg, **u** = 36kmh⁻¹, **v** = 40kmh⁻¹ and $\sin\theta = \frac{1}{21}$ (12 marks)

11. (a) The lower limit of a measurement is 4.05 and its upper limit is 6.75. Find the relative error of the measurement (05 marks)

- (b) A decimal number **x** was approximated with an error **U****x**. Show that the relative error in

$$\mathbf{x}^p \text{ is } \frac{|p||\mathbf{x}|}{|\mathbf{x}|}. \text{ Hence if } \mathbf{x} = 2.50, \text{ find the percentage error in } \mathbf{x}^3 \text{ (07 marks)}$$

12. A ball projected at an angle with a speed of $14\sqrt{10}\text{ms}^{-1}$ from the top of a tower **200m** high hits the ground at a point **200m** away from the foot of the tower.
- (a) Show that the two possible directions of projection are at right angles to each other (06 marks)
- (b) Find the two possible times of flight (06 marks)
13. A continuous r.v **X** has the following p.d.f
- $$f(x) = \begin{cases} x(x-2) & , \quad 2 \leq x \leq 3 \\ 0 & , \quad \text{otherwise} \end{cases}$$
- (a) Find the:
- (i) Value of (04 marks)
- (ii) Cumulative distribution function of **X** (04 marks)
- (b) Show that the median of **X** lies between **2.70** and **2.75** (04 marks)
14. (a) Use Newton Raphson formula to show that the root of the equation
- $$x^3 + 2^x = 0 \text{ is } x_{n+1} = x_n - \frac{x_n^3 + 2^{x_n}}{3x_n^2 + 2^{x_n} \ln 2} \quad (02 \text{ marks})$$
- (b) Draw a flow chart that:
- (i) Reads the initial approximation x_0 .
- (ii) Computes and prints the root in (a) above correct to **3** decimal places (06 marks)
- (c) Perform a dry run for your flow chart using $x_0 = -0.7$ (04 marks)
15. A uniform ladder **PQ** of length **2a** and weight **w** is inclined at an angle of $\tan^{-1} 2$ to the horizontal with its end **Q** resting against a smooth vertical wall and end **P** on a rough horizontal ground with which the coefficient of friction is $\frac{5}{12}$. If a boy of weight **W** can safely ascend a distance **x** up this ladder before it slips,
- (a) show that $x = \frac{a(2w + 5W)}{3W}$ (09 marks)
- (b) deduce that the boy can only reach the top of the ladder if **W = 2w** (03 marks)
16. (a) A family has **25** children. The probability of having a boy is **0.64**. Find the probability of having more girls than boys (05 marks)
- (b) A random sample of **50** readings taken from a normal population gave the following data: $\sum x = 163$ and $\sum x^2 = 548$. Calculate the:
- (i) unbiased estimate for the population variance (02 marks)
- (ii) **99%** confidence interval for the population mean (05 marks)