

P425/2

Applied Mathematics

Paper 2

July - August, 2024

3 hours



UGANDA MUSLIM TEACHERS' ASSOCIATION

UMTA JOINT MOCK EXAMINATIONS 2024

UGANDA ADVANCED CERTIFICATE OF EDUCATION

Applied Mathematics

Paper 2

3 hours

INSTRUCTIONS:

- Answer **all the eight** questions in section A and any **five** from section B.
- Any additional question(s) answered will **not** be marked.
- **All necessary working must** be shown clearly.
- Begin each number on a fresh sheet of paper.
- Graph paper is provided.
- Silent, non-programmable scientific calculators and mathematical table with a list of formulae may be used.
- In numerical work, take acceleration due to gravity g , to be 9.8ms^{-2}

Include the allocation table on your answer sheet

Question	Marks
Section A	
9	
10	
11	
12	
13	
14	
15	
16	
Total	

SECTION A (40 MARKS)

Answer all questions in this section.

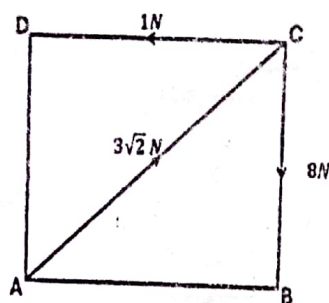
1. Over a period of time, Julian finds that on long-distance flights, he flies economy class on 82% of the flights. On the rest of the flights, he flies first class. When he flies economy class, the probability that he gets a good night's sleep is x . When he flies first class, the probability that he gets a good night's sleep is 0.9.
- (a) The probability that Julian gets a good night's sleep on a randomly chosen flight is 0.285. Find the value of x . (02 marks)
- (b) Given that on a particular flight, Julian does not get a good night's sleep, find the probability that he is flying economy class. (03 marks)
2. A particle is projected from a point O with initial velocity 30 ms^{-1} at an angle $\tan^{-1}(2)$ to the horizontal. Find its height above O when its speed is 20 ms^{-1} . (05 marks)
3. The cost of baking a cake is calculated from the cost of the items in 2022 and 2023.

Item	Price	
	2022 = 100 %	2023
Flour per kg.	6000	7800
Sugar per kg.	5000	4000
Eggs per egg.	500	700
Milk per litre	2000	2500

Calculate the simple price index for the cost of making a cake. Comment on your result. (05 marks)

4. Use trapezium rule with four sub intervals to estimate $\int_{0.2}^{1.0} \frac{x}{2 + \cos x} dx$ correct to two significant figures. (05 marks)

5. Three forces of magnitudes 1N , 8N and $3\sqrt{2}\text{N}$ act along CD , CB and AC respectively as shown. $ABCD$ is a square of side a units.



Consider AB and AD as x and y -axes respectively. Taking moments about A , show that the equation of line of action of the resultant is $2y + 5x - 7a = 0$. (05 marks)

6. The probability density function (pdf) of a Continuous random variable X is given by,

$$f(x) = \begin{cases} \frac{4}{3}x(1-x^2); & -2 \leq x \leq 1 \\ 0 & \text{Otherwise} \end{cases}$$

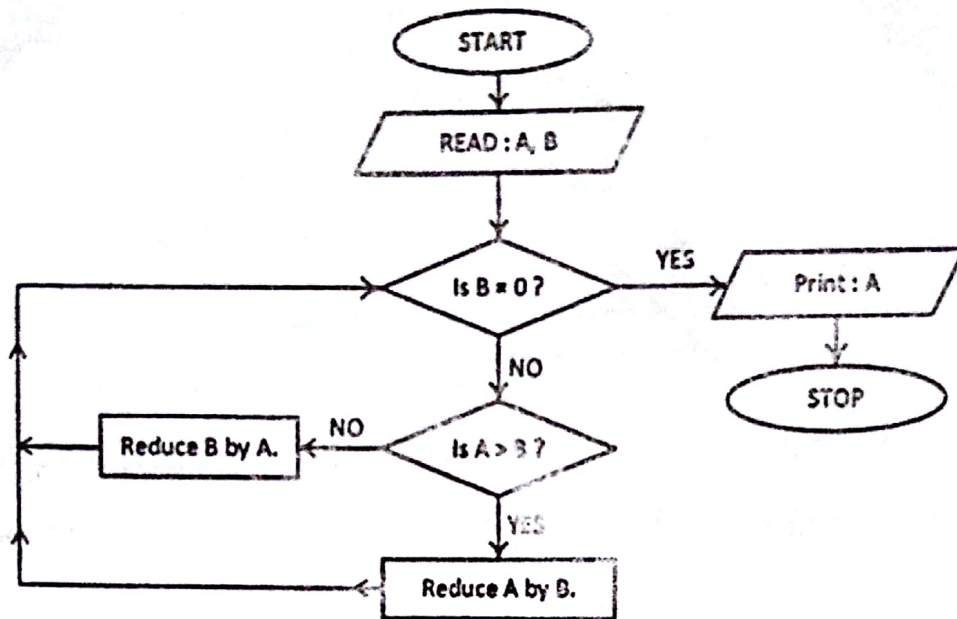
Find the mode of X .

(05 marks)

7. A body of weight 49N lies on a rough plane which is inclined at 35° to the horizontal. The angle of friction between the plane and the body is 20° . Find the magnitude of the least force that must be applied to the body in a direction parallel to and up the plane to hold the body in equilibrium.

(05 marks)

8. Study the flow chart below.



Perform a dry run for $A = 8$ and $B = 10$.

(05 marks)

SECTION B (60 MARKS)

Answer any five questions from this section.

All questions carry equal marks.

9. The patients at a chest clinic were asked to keep a record of the number of cigarettes they smoked every day.

Number of cigarettes	Frequency
0 – 9	5
10 – 14	8
15 – 19	32
20 – 29	41
30 – 39	16
40 – 49	2

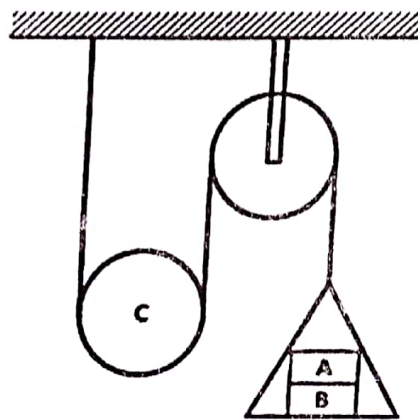
(a) Use the frequency distribution table to estimate the;

(i) Mean.

(ii) Number of patients who smoked 25 cigarettes and below. (07 marks)

(b) Draw a histogram to represent the data. Use it to estimate the mode. (05 marks)

10. The diagram below shows **three** particles **A**, **B** and **C** of mass 3kg, 2kg and 8kg respectively. One end of a light inextensible string is attached to a ceiling. The string passes under a moveable pulley **C** and then over a fixed smooth pulley. To the other end of the string is attached a light scale pan in which two weights **A** and **B** are placed with **A** on top of **B**.



The system is released from rest.

(a) Calculate the;

(i) Acceleration of the particle, **C**.

(09 marks)

(ii) Tension in the string.

(03 marks)

(b) Find the reaction between the weights **A** and **B**.

11 Show that **one** of the roots of the equation $x^2 - 3x + 1 = 0$ lies between 2 and 3.

Hence use linear interpolation to find the root correct to **two** decimal places.

(12 marks)

12. The marks of 400 students in a certain test are normally distributed with a mean of 54 marks and a standard deviation of 9 marks.

(a) Given that the pass mark is 38, estimate the number of students who passed the test. (05 marks)

(b) Find the probability that a student selected at random scored between 49 and 57 marks. (04 marks)

(c) If a sample of 10 students was taken at random, determine the probability that at least one scored between 49 and 57. (03 marks)

13. A ship P steaming at 20 kmh^{-1} in the direction $N50^\circ E$ is 120 km due West of a ship Q steaming at 12 kmh^{-1} in the direction $N30^\circ W$. Find the;

(a) Shortest distance between them in the subsequent motion and the time taken to reach this position. (07 marks)

(b) The time for which the ships are within a range of 50 km from each other. (05 marks)

14. Two decimal numbers X and Y have been approximated by X and Y with errors ΔX and ΔY respectively.

(a) Show that the maximum relative error made in approximating $x\sqrt{y}$ by $X\sqrt{Y}$ is given by $\left| \frac{\Delta X}{X} \right| + \frac{1}{2} \left| \frac{\Delta Y}{Y} \right|$. (08 marks)

(b) Given that X and Y have been measured as 1.824 and 3.9 respectively, determine the percentage error made in the expression $X\sqrt{Y}$. (05 marks)

15. A box contains 3 red, 2 green and 1 yellow balls. When a ball is drawn from the bag, it is returned together with a ball of the same colour. If two such random draws are made,

(a) Construct a probability distribution table for the number of red balls in the bag after the two draws. (06 marks)

(b) Determine the;

(i) Expected number of red balls.

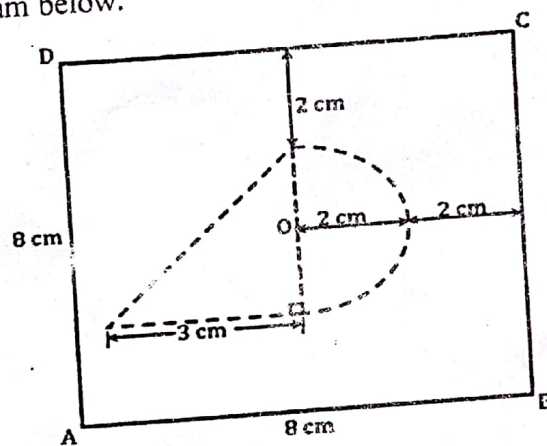
(04 marks)

(ii) Median number of red balls.

(02 marks)

(c) Sketch the Cumulative probability distribution.

16. **ABCD** is a uniform square lamina of side 8 cm. A hole made up of a right-angled triangle and a Semi circle with centre **O** and radius 2 cm was cut off from the square as shown in the diagram below.



(a) Find the position of the centre of gravity of the remaining sheet. (09 marks)

(b) The remaining sheet is then suspended about **B**, determine the angle side **AB** makes with the horizontal. (03 marks)

END