

**P425/1**  
**PURE MATHEMATICS.**  
**Paper 1.**  
**July/August 2024**  
**3 Hours**



**ERETA EDUCATION CONSULT LTD**  
**JOINT MOCK EXAMINATIONS 2024**  
*Uganda Advanced Certificate Of Education*  
**PURE MATHEMATICS**

**PAPER 1**

**3HOURS**

**Instructions to Candidates:**

- Attempt **all** the **eight** questions in section **A** and any **Five** from section **B**.
- All the working must be clearly shown.
- Mathematical tables with list of formulae and squared papers are provided.
- Silent, non-programmable calculator should be used.
- State the degree of accuracy at the end of each answer using **CAL** for calculates and **TAB** for tables.

*Turn Over*

### SECTION A (40 marks)

- 1) Expand  $(1 + x + x^2)^6$  as far as the term in  $x^2$ . (05 marks)
- 2) The line  $y=mx$  and the curve  $y=x^2 - 2x$  intersect at the origin o and meet again at point A .If P is the midpoint of OA ,find the equation of the locus of P as m varies. (05 marks)
- 3) Given that  $x=2$  is the repeated root of the equation  $2x^3+px^2+qx-4=0$ , find the values of p and q. (05 marks)
- 4) A line through the point A (1,-2, 3) parallel to the line  $\frac{x}{3}=\frac{y+1}{-1}=z+1$  meets the plane  $x+2y+2z=8$  at Q, find the coordinates of Q. (05 marks)
- 5) Prove that  $\cos^4 A = \frac{1}{8}(3+4\cos 2A+\cos 4A)$ . (05 marks)
- 6) Solve the differential equation  $x(1-y)\frac{dy}{dx} + y = 0$ , given that  $y=1$  when  $x=e$  (05 marks)
- 7) Find the volume generated when the area bounded by the curve  $y=1+2x-x^2$  and the line  $y=1$  is rotated through  $360^\circ$  about the line  $y=1$ . (05 marks)
- 8) If  $y=e^x \ln x$ , show that  $x\frac{d^2y}{dx^2} = (2x-1)\frac{dy}{dx} + (1-x)y$ . (05 marks)

### SECTION B (60 marks)

- 9) (a) Express  $\frac{x^2+5x+10}{(x+1)(x^2-4)}$  in partial fractions (07 marks)
- (b) Show that  $\int_3^4 \frac{x^2+5x+10}{(x+1)(x^2-4)} dx = \ln\left(\frac{384}{125}\right)$  (05 marks)

- 10) (a) The sum of the first seven terms of a G.P is 7 and the sum of the next seven terms is 896. Find the common ratio of the progression. If the  $k^{th}$  term is the first term of the G.P which is greater than 1, find k. (06 marks)

(b) Jack operates an account with a certain bank which pays a compound interest of 13.5% per annum. He opened the account at the beginning of the year with sh.500, 000 and deposits the same amount at the beginning of every year. Calculate how much he will receive at the end of 9 years. After how long will the money have accumulated to sh.3, 320,000? **(06 marks)**

11) (A) Express  $(-1 - \sqrt{3} i)^6$  in the form  $x+iy$  **(06 marks)**

(b) Given that  $z(5+5i) = a(1+3i) + b(2-i)$  where  $a$  and  $b$  are real numbers and  $\arg z = \frac{\pi}{2}$  and  $|z|=7$ , find the values of  $a$  and  $b$ . **(06 marks)**

12) The points  $A$  and  $B$  have position vectors  $\mathbf{a}$  and  $\mathbf{b}$  with respect to the origin  $O$ . The points  $P$ ,  $Q$  and  $R$  are defined such that  $3OP=OA$ ,  $3OQ=2OB$ ,  $2PR=RQ$  and  $S$  is the point of intersection of  $AB$  and  $OR$  produced. Find the position vector of  $R$  in terms of  $\mathbf{a}$  and  $\mathbf{b}$ . If  $AS=kAB$  and  $OS=lOR$ , find the values of  $k$  and  $l$ . Hence write down the position vector of  $S$ . **(12 marks)**

13) (a) Find the maximum and minimum values of the function  $\frac{1}{3+\sin x - 2\cos x}$ , stating clearly the values of  $x$ . **(06 marks)**

(b) Prove that in any triangle  $ABC$ ,  $\cot\left(\frac{A-C}{2}\right) = \frac{a+c}{a-c} \tan\frac{B}{2}$ . **(06 marks)**

14) The differential equation  $\frac{dp}{dt} = kp(c-p)$  shows the rate at which information flows in the student population  $c$ .  $P$  represents the number who have heard the information in  $t$  days and  $k$  is a constant

(a) Solve the differential equation. **(06 marks)**

(b) A school has a population of 1000 students. Initially 20 students had heard the information. A day later 50 students had heard the information. How many students had not heard the information by the tenths day? **(06 marks)**

15) Sketch the curve  $y = \frac{5x^2 + 8x + 4}{x^2 + x}$ , by finding the turning points and clearly state the asymptotes. **(12 marks)**

16) Prove that the equation of the chord joining the points  $P(cp, \frac{c}{p})$  and  $Q(cq, \frac{c}{q})$  on rectangular hyperbola  $xy = c^2$  is  $pqy + x = c(p + q)$ . It is given that PQ subtends at right angle at the point  $R(cr, \frac{c}{r})$  on the curve.

Prove that: (i) PQ is parallel to the normal at R to the curve

(ii) The midpoint of PQ lies on the straight line  $y + r^2x = 0$  **(12 marks)**

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