

KAMSSA 2022 SUBSIDIARY MTC

MARKING GUIDE

$$\begin{aligned}
 1. \quad & \frac{(\sqrt{10}+\sqrt{5})^2 - (\sqrt{10}-\sqrt{5})^2}{2\sqrt{5}} \\
 &= \frac{(\sqrt{10}+\sqrt{5}+\sqrt{10}-\sqrt{5})(\sqrt{10}+\sqrt{5}-\sqrt{10}+\sqrt{5})}{2\sqrt{5}} \\
 &= \frac{2\sqrt{10}(\sqrt{5}+\sqrt{5})}{2\sqrt{5}} \\
 &= 2 \frac{\sqrt{10} \cdot 2\sqrt{5}}{2\sqrt{5}} \\
 &= 2\sqrt{10}
 \end{aligned}$$

$$\begin{aligned}
 2. \quad & \frac{(145 \times 2) + (125 \times 3) + (x \times 5) + (130 \times 4) + (120 \times 1)}{2+3+5+4+1} = 130 \\
 & \frac{290 + 375 + 5x + 520 + 120}{15} = 130
 \end{aligned}$$

$$\begin{aligned}
 1305 + 5x &= 1950 \\
 x &= 129
 \end{aligned}$$

$$\begin{array}{rcl}
 -a + 4d = 18 & \dots\dots\dots i \\
 -4a + 14d = 93 & \dots\dots\dots ii \\
 \hline
 3 \text{ eqn } i - \text{eqn } ii & & \\
 -4a + 16d = 72 & & \\
 -4a + 14d = 93 & & \\
 \hline
 \end{array}$$

$$2d = -21$$

$$d = \frac{-21}{2}$$

$$a + 4\left(\frac{-21}{2}\right) = 18$$

$$a = 60$$

(4) . Let $p(A) = x$ and $P(B) = y$

$$P(A \cap B) = P(A), P(B)$$

$$\frac{1}{4} = x, y \dots\dots\dots (i)$$

$$P(A \cup B) = P(A) + P(B) - P(A \cap B)$$

$$\frac{3}{4} = x + y - xy.$$

$$X + y = 1$$

$$X = 1 - y.$$

$$(1 - y)y = \frac{1}{4}$$

$$Y - y^2 = \frac{1}{4}$$

$$4y - 4y^2 = 1$$

$$4y^2 - 4y + 1 = 0$$

$$Y = \frac{1}{2}.$$

$$P(B) = \frac{1}{2}.$$

$$xy = \frac{1}{4}$$

$$\frac{x}{y} = \frac{1}{4}$$

$$X = \frac{1}{2}.$$

$$P(A) = \frac{1}{2}.$$

$$5) 3\cos^2 \theta = \frac{8\sin \theta}{\cos \theta}$$

$$3\cos^2 \theta - 8\sin \theta = 0$$

$$3(1 - \sin^2 \theta) - 8\sin \theta = 0$$

$$3\sin^2 \theta + \sin \theta - 3 = 0$$

$$\left(\sin \theta - \frac{1}{2}\right)(\sin \theta + 3) = 0.$$

Either

$$\sin \theta = \frac{1}{3}$$

$$\theta = 19.5^\circ, 160.5^\circ.$$

$$6) \mu = 1.8 \quad \sigma = 0.3 \quad n = 1000$$

$$P(1.68 < x < 2.10) = P\left(\frac{1.68-1.8}{0.3} < z < \frac{2.10-1.8}{0.3}\right)$$

$$= P(-0.4 < z < 1)$$

$$=P(0 < z < 0.4) + P(0 < z < 1)$$

$$= 0.15542 + 0.34134$$

$$= 0.49676 \times 1000$$

$$= 496.76$$

$$\approx 497 \text{ Mangoes.}$$

7) sum of roots

$$x\beta = \frac{3}{2} \quad x + \beta = -\frac{9}{2}$$

$$x^2 - 1 + \beta^2 - 1 = (x + \beta)^2 - 2x\beta - 2$$

$$= \left(-\frac{9}{2}\right)^2 - 2\left(\frac{3}{2}\right) - 2$$

$$= \frac{61}{4}$$

Product of roots.

$$(x^2 - 1)(\beta^2 - 1) = (\alpha\beta)^2 - (\alpha + \beta)^2 - 2\alpha\beta + 1$$

$$= \left(\frac{3}{2}\right)^2 - \left(-\frac{9}{2}\right)^2 - 2\left(\frac{3}{2}\right)$$

$$= -21$$

$$\text{Equation} \Rightarrow 4x^2 - 61 - 84 = 0$$

8)

DIAGRAM

For 5kg mass

$$5g - T = 5a \dots\dots\dots (1)$$

For 10kg mass

$$T - 7.5 = 10a \dots\dots\dots (2)$$

From eqn (1)

$$T = 5g - 5a$$

$$\text{Then } 5g - 5a - 7.5 = 10a$$

$$5 \times 9.8 - 5a - 7.5 = 10a$$

$$a = 2.766 \text{ m/s}^2$$

QN 9 (a)

$$(i) \quad \sum p(X = x) = 1$$

$$0.4 + a + 0.3 + 0.2 = 1$$

$$a = 0.1$$

$$(ii) \quad ECT(-2x0.4) + (0x0.1) + (1x0.3) + (4x0.2)$$

$$= -0.8 + 0.3 + 0.8$$

$$= 0.3$$

$$(iii) \text{Var}(x) = (4x0.4) + (1x 0.3) + 0 + (16 x 0.2)$$

$$= 1.6 + 0.3 + 3.2$$

$$= 5.1$$

9(b)

$$(i) \quad \int_1^3 ky^2 dy = 1$$

$$\left. \frac{ky^3}{3} \right|_1^3 = 1$$

$$K \left[9 - \frac{1}{3} \right] = 1$$

$$K = \frac{3}{26}$$

(ii)

$$P\left(x > \frac{2}{3}\right) = \frac{3}{26} \int_{\frac{2}{3}}^1 y^2 dy$$

$$= \frac{3}{26} \left[\frac{1}{3} - \frac{\left(\frac{2}{3}\right)^3}{3} \right]$$

$$= \frac{19}{702} \text{ or } 0.02707$$

$$(iii) \quad E(y) = k \int_1^3 y^3 dy$$

$$= \frac{3}{26} \left[\frac{y^4}{4} \right]_1^3 = \frac{3}{26} \left(\frac{3^4}{4} - \frac{1}{4} \right)$$

$$= \frac{60}{26}$$

$$= \text{OR } 2.3076$$

$$10(a) \quad Y = 2X^2 + 5X^{-1}$$

$$\frac{dy}{dx} = 4x - 5x^{-2}$$

$$\left. \frac{dy}{dx} \right|_{x=-2} = 4(-2) - 5(-2)^{-2}$$

$$= \frac{-37}{4}$$

(b) (i)

$$Y = (x-2)(4-x)$$

$$Y = 6x - x^2 - 8$$

$$\frac{dy}{dx} = 6 - 2x$$

At turning point $\frac{dy}{dx} = 0$

$$6 - 2x = 0$$

$$X = 3$$

When $x = 3$

$$Y = (3 - 2)(4 - 3) = 1$$

\therefore point (3, 1)

Nature of turning point

$$\frac{dy}{dx} = 6 - 2x$$

$$\frac{d^2y}{dx^2} = -2, \frac{d^2y}{dx^2} < 0$$

$\therefore (3, 1)$ is a maximum point

(ii)

Intercepts

$$X - 0, y = -8(0, -8)$$

$$y = 0, x = 2 \text{ or } x = 4 (2, 0)(4, 0)$$

graph

(iii)

$$\text{Area} = \int_2^4 6x - x^2 - 8 \, dx$$

$$= \left[3x^2 - \frac{x^3}{3} - 8x \right]_2^4$$

$$= \left(-\frac{16}{3} \right) - \left(-\frac{20}{3} \right)$$

$$\frac{4}{3} \text{ square units}$$

Qn 11

(a) $n = 12$

$$= \frac{12!}{2!2!2!2!} = \frac{479001600}{16}$$

$$= 29,937,600$$

$$\frac{1 \times 10!}{2!2!2!} = 453,600$$

$$P(E) = \frac{453,600}{29,937,600} = \frac{1}{66}$$

$$\text{OR } = 0.01515$$

(b) 2 boys can be chosen from 4 in ${}^4C_2 = 6$ ways

3 girls can be chosen from 7 in ${}^7C_3 = 35$ ways

Number of ways = 6×35

$$= 210 \text{ ways}$$

(c) Atleast 3 boys Type equation here.

$$\frac{4 \text{ boys } 7 \text{ girls}}{}$$

$$3 \quad 2$$

$$4 \quad 1$$

$${}^4C_3 \times {}^7C_2 + {}^4C_4 \times {}^7C_1$$

$$84 + 7$$

$$= 91 \text{ ways}$$

Marks	F	X	fx	c.b	c.f
0 - < 40	2	5	10	10-10	2
10 - < 20	8	15	120	10-20	10
20 - < 30	10	25	250	20-30	20
30 - < 40	14	35	490	30-40	34
40 - < 50	5	45	225	40-50	39
50 - < 60	1	55	55	50-60	50

$$\sum f = 50$$

$$\sum fx = 1150$$

(i)

$$\text{Mean} = \frac{\sum fx}{\sum f} = \frac{1150}{50}$$

$$= 23 \text{ marks}$$

(ii)

$$\text{Mode} = L_1 + \left(\frac{d_1}{d_1 + d_2} \right) \times c$$

$$= 30 + \left(\frac{4}{4+9} \right) \times 10$$

$$= 30 + 3.0769$$

$$= 33.0769 \quad (3 \text{ dp}^{atleast})$$

QN 13

$$(a) \quad 2 \begin{pmatrix} 2 & x \\ 3 & y \end{pmatrix} + \begin{pmatrix} 1 & 2 \\ 4 & 1 \end{pmatrix} = \begin{pmatrix} 0 & 6 \\ 2 & 4 \end{pmatrix}$$

$$\begin{pmatrix} 4 & 2x \\ 6 & 2y \end{pmatrix} + \begin{pmatrix} 1 & 2 \\ 4 & 1 \end{pmatrix} = \begin{pmatrix} 0 & 6 \\ 2 & 4 \end{pmatrix}$$

$$2x + 2 = 6$$

$$x = 2$$

$$2y = 4$$

$$y = 2$$

$$(b) \quad (i) \quad \begin{matrix} A \\ B \\ C \end{matrix} \begin{pmatrix} 30 & 20 \\ 40 & 15 \\ 35 & 10 \end{pmatrix} \quad 3 \times 2$$

$$(ii) \quad \begin{matrix} small \\ large \end{matrix} \begin{pmatrix} 30,000 \\ 40,000 \end{pmatrix} \quad 2 \times 1$$

$$(iii) \quad \begin{pmatrix} 30 & 20 \\ 40 & 15 \\ 35 & 10 \end{pmatrix} \begin{pmatrix} 30,000 \\ 40,000 \end{pmatrix}$$

$$= \begin{pmatrix} 900,000 + 800,000 \\ 1200,000 + 600,000 \\ 1050,000 + 400,000 \end{pmatrix}$$

$$= \begin{matrix} A \\ B \\ C \end{matrix} \begin{pmatrix} 1700,000 \\ 1800,000 \\ 1450,000 \end{pmatrix}$$

$$\text{Total sales} = 1700,000 + 1800,000 + 1450,000$$

$$= \text{shs } 495,000$$

Qn 14

Diagram

At equilibrium

$$\text{Horizontally } p \cos \theta = 20 \cos 50 + 15$$

$$P \cos \theta = 27.8575 \dots\dots\dots(i)$$

$$\text{Vertically } p \sin \theta = 20 \sin 50$$

$$P \sin \theta = 15.32088 \dots\dots\dots(ii)$$

$$(ii) \dots\dots\dots(i)$$

$$\tan \theta = \frac{15.32088}{27.8575}$$

$$\theta = 28.8^\circ$$

$$P \cos 28.8^\circ = 27.8575$$

$$P = 31.79 \text{ N}$$

(b) part 1

$$t = 30\text{S}, \text{ at } 1.5 \text{ ms}^{-2}$$

$$u = 0$$

$$u = u + at$$

$$v = 0 + 1.5 \times 30$$

$$v = 45 \text{ ms}^{-1}$$

Part (ii)

$$t = 60\text{S}, a = 0.3 \text{ ms}^{-2}$$

$$U = 45 \text{ ms}^{-1}, v = u + at$$

$$V = 45 + 0.3 \times 60$$

$$V = 63 \text{ ms}^{-1}$$

Part (iii)

$$t = 25\text{S}$$

$$V = U = 63 \text{ ms}^{-1}$$

Acceleration = slope

$$= \frac{DV}{Dt} = \frac{0-65}{25}$$

$$= -2.6 \text{ ms}^2$$

$$=$$