

Business Analytics Regression Diagnostics

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Course Content

- Introduction
- Regression Analysis
- Regression Diagnostics
- Logistic and Poisson Regression
- Naive Bayes and Bayesian Networks
- Decision Tree Classifiers
- Data Preparation and Causal Inference
- Model Selection and Learning Theory
- Ensemble Methods and Clustering
- High-Dimensional Problems
- Association Rules and Recommenders
- Neural Networks



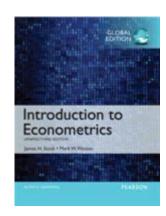


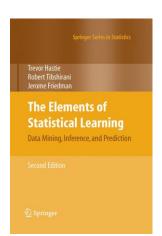
Recommended Literature

- Introduction to Econometrics
 - Stock, James H., and Mark W. Watson
 - Chapter 6, 7, 10, 17, 18
- The Elements of Statistical Learning

(Trevor Hastie, Robert Tibshirani, Jerome Friedman)

- http://statweb.stanford.edu/~tibs/ElemStatLearn/printings/ESLII_print10.pdf
- Section 3: Linear Methods for Regression
- An Introduction to Statistical Learning: With Applications in R (Gareth James, Trevor Hastie, Robert Tibshirani)
 - http://www-bcf.usc.edu/~gareth/ISL/
 - Section 3: Linear Regression







Gauss-Markov Theorem

The Gauss-Markov theorem states that in a linear regression model in which the errors

- have expectation zero and
- are uncorrelated and
- have equal variances,

the best linear unbiased estimator (BLUE) of the coefficients is given by the ordinary least squares (OLS) estimator.

- "Unbiased" means $E(\hat{\beta}_j) = \beta_j$
- "Best" means giving the <u>lowest variance</u> of the estimate as compared to other linear unbiased estimators.
 - Restriction to unbiased estimation is not always the best
 (will be discussed in the context of the ridge regression later)



Bias, Consistency, and Efficiency

Unbiased

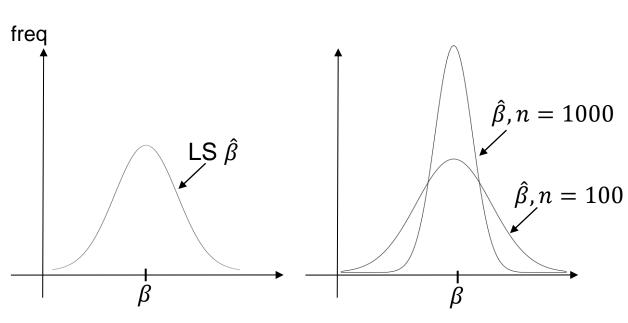
 $E(\hat{\beta}) = \beta$ Expected value for estimator "is true"

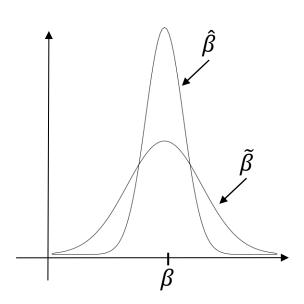
Consistent

 $var(\hat{\beta})$ decreases with increasing sample size n

Efficient

 $var(\hat{\beta}) < var(\tilde{\beta})$ estimator $\hat{\beta}$ has lower variance than any other estimator, $\tilde{\beta}$







Gauss-Markov Assumptions in Detail

The OLS estimator is the best linear unbiased estimator (BLUE), iff

1) Linearity

Linear relationship in parameters β

2) No multicollinearity of predictors

No linear dependency between predictors

3) Homoscedasticity

The residuals exhibit constant variance

4) No autocorrelation

There is no correlation between the ith and jth residual terms

5) **Expected value** of the residual vector, given X, is 0 ($E(\varepsilon|X) = 0$)

(i.e. exogeneity $(cov(\varepsilon, X) = 0)$)



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When Linearity Does Not Hold: Try to Reformulate



Polynomial regression (still a linear model):

$$Y = \beta_0 + \beta_1 X + \beta_2 X^2 + \dots + \varepsilon$$

Transform either X or Y or both variables, e.g.:

$$Log(Y) = \beta_0 + \beta_1 Log(X) + \varepsilon$$

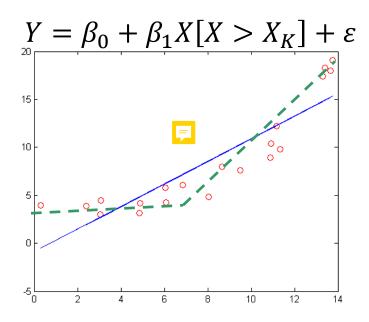
• Non-linear regression, e.g. with constant *c*:

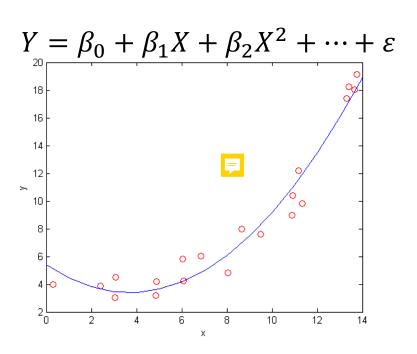
$$Y = c + \exp(\beta_0 + \beta_1 X) + \varepsilon$$

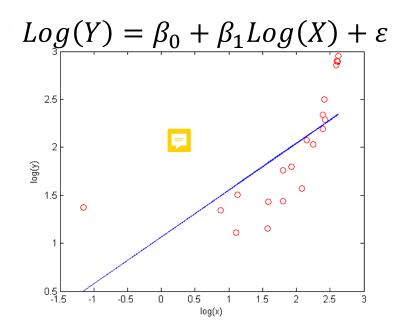
• Piecewise linear regression:

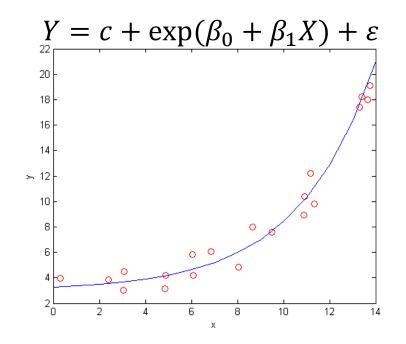
$$Y = \beta_0 + \beta_1 X[X > X_K] + \varepsilon$$

, where $[X > X_K] = 0$ if $X \le X_K$ and $[X > X_K] = 1$ if $X > X_K$





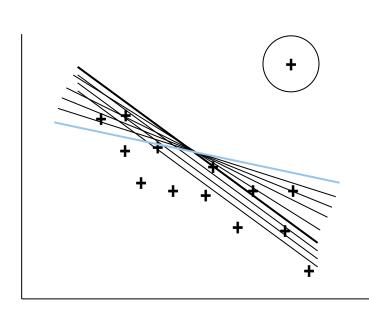






Outliers

- An outlier is an observation that is unusually small or large
 Several possibilities need to be investigated when an outlier is observed:
 - There was an error in recording the value
 - The point does not belong in the sample
 - The observation is valid
- Identify outliers from the scatter diagram
- There are also methods for "robust" regression





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Multicollinearity 5

- The rank of the data matrix X is p, the number of columns
- p < n, the number of observations
- If there is no exact linear relationships among independent variables $rank(\mathbf{X}) = p$, \mathbf{X} has full column rank
- If rank(X) < p, X is singular -> impossible to calculate the inverse
- Remember: $\hat{y} = \mathbf{X}\hat{\beta} = \mathbf{X}(\mathbf{X}^T\mathbf{X})^{-1}\mathbf{X}^Ty \rightarrow \hat{\beta} = (\mathbf{X}^T\mathbf{X})^{-1}\mathbf{X}^T\mathbf{y}$
 - Not possible to solve -> We can not compute $\hat{\beta}$
 - Intuition: If two independent variables are the same, measuring the impact of the first, holding the second constant is impossible
- Imperfect, yet high, correlation between independent variables leads to issues with significance of predictors



Check for Multicollinearity

- A basic check of multicollinearity is to calculate the correlation coefficient for each pair of predictor variables
 - Large correlations (both positive and negative) indicate problems
 - large means greater than the correlations between predictors and response
 - It is possible that the pairwise correlations are small, and yet a linear dependence exists among three or even more variables.
- Alternatively use the variance inflation factor (VIF)



Check - Variance Inflation Factor



- VIF $=\frac{1}{1-R_k^2}$, where the R_k^2 value here is the value when the predictor in question (k) is set as the dependent variable
- For example, if the VIF = 10, then the respective R_k^2 would be 90%. This would mean that 90% of the variance in the predictor in question can be explained by the other independent variables
- Because so much of the variance is captured elsewhere, removing the predictor in question should not cause a substantive decrease in overall \mathbb{R}^2
 - The rule of thumb is to remove variables with VIF scores greater than 10



Consequence - Non-Significance



- If a variable has a non-significant t-value, then either
 - The variable is not related to the response, or (-> Small t-value, small VIF, small correlation with response)
 - The variable is related to the response, but it is not required in the regression because it is strongly related to a third variable that is in the regression, so we don't need both
 - (-> Small t-value, big VIF, big correlation with response)
- The usual remedy is to drop one or more variables from the model



Example

- Measurements on batches of cement
- Response variable: Heat (heat emitted)
- Explanatory variables
 - X1: amount of tricalcium aluminate (%)
 - X2: amount of tricalcium silicate (%)
 - X3: amount of tetracalcium aluminaoferrite (%)
 - X4: amount of dicalcium silicate (%)



Example

Heat	X1	X2	X3	X4
78.5	7	26	6	60
74.3	1	29	15	52
104.3	11	56	8	20
87.6	11	31	8	47
95.9	7	52	6	33
109.2	11	55	9	22
102.7	3	71	17	6
72.5	1	31	22	44
93.1	2	54	18	22
115.9	21	47	4	26
83.8	1	40	23	34
113.3	11	66	9	12
109.4	10	68	8	12



Example

X4

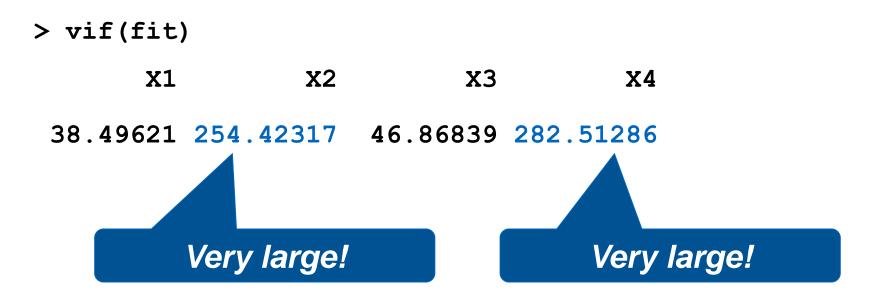
```
Estimate Std. Error t value Pr(>|t|)
                                                        Large p-
             62.4054
                        70.0710
                                   0.891
                                           0.3991
(Intercept)
                                                         values
                         0.7448 2.083
                                           0.0708
X1
              1.5511
X2
              0.5102
                         0.7238 0.705
                                           0.5009
X3
              0.1019
                         0.7547 0.135
                                           0.8959
                                  -0.203
             -0.1441
                         0.7091
X4
                                           0.8441
Residual standard error: 2.446 on 8 degrees of freedom
Multiple R-Squared: 0.9824,
                                Adjusted R-squared: 0.9736
F-statistic: 111.5 on 4 and 8 DF, p-value: 4.756e-07
              > round(cor(cement.df),2)
     Big R-
                            X1
                                   X2
                                         X3
                    Heat
                                               X4
    squared
              Heat 1.00 0.73 0.82 -0.53 -0.82
                                                         Big
                    0.73 1.00
                                0.23 - 0.82 - 0.25
              X1
                                                      correlation
              X2
                    0.82 \quad 0.23 \quad 1.00 \quad -0.14 \quad -0.97
                   -0.53 - 0.82 - 0.14 1.00 0.03
              x3
```

-0.82 - 0.25 - 0.97 0.03

1.00



Data





Drop X4

> vif(fit)

X1

X2

X3

3.251068 1.063575 3.142125

VIF's now small

```
Estimate Std. Error t value Pr(>|t|)
(Intercept) 48.19363
                        3.91330
                                 12.315 6.17e-07 ***
             1.69589
                        0.20458
                                  8.290 1.66e-05
X1
X2
             0.65691
                        0.04423
                                 14.851 1.23e-07 ***
             0.25002
                        0.18471
                                  1.354
X3
                                           0.209
```

X1, X2 now signif

Residual standard error: 2.312

Multiple R-Squared: 0.9823,

F-statistic: 166.3 on 3 and 9 b

R-squared hardly decreased

of freedom

squared: 0.9764

3.367e-08



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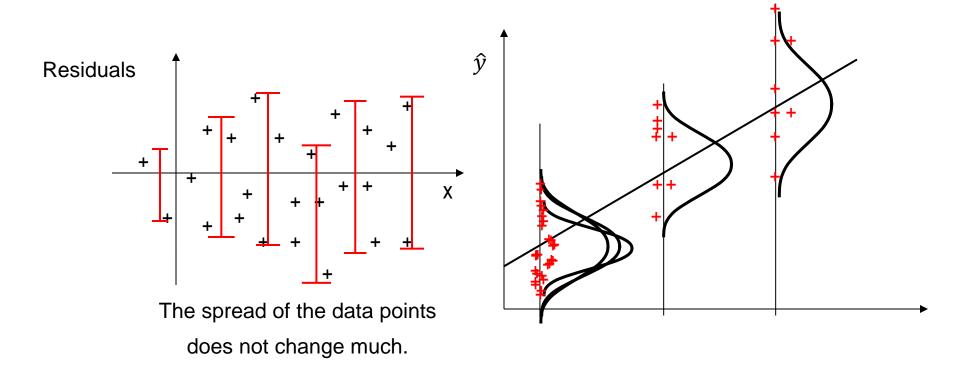
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(i.e. exogeneity $(cov(\varepsilon, X) = 0)$)



Homoscedasticity

 When the requirement of a constant variance is not violated we have homoscedasticity



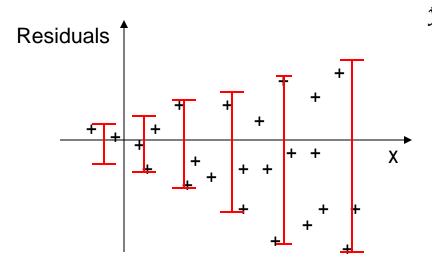


Heteroscedasticity

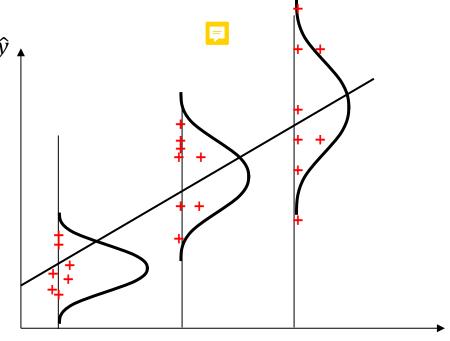
• When the requirement of a constant variance is violated we have heteroscedasticity $(var(\varepsilon_i|x_{1i},...,x_{pi}))$ not constant)

Breusch-Pagan test or White test are used to check for

heteroscedasticity



The spread increases with *x*





White Test



• The test is based on an auxiliary regression of e^2 on all the explanatory variables (X_i) , their squares (X_i^2) , and all their cross products

$$e^{2} = \beta_{0} + \beta_{1}X_{1} + \beta_{2}X_{2} + \beta_{3}X_{1}^{2} + \beta_{4}X_{2}^{2} + \beta_{5}X_{1}X_{2} + v$$

or only $e^2 = \beta_0 + \beta_1 \hat{y} + \beta_2 \hat{y}^2 + v$ to have less degrees of freedom

- $\chi^2 = nR^2$, where n is the sample size and R^2 is the unadjusted R-squared from the auxiliary OLS regression.
- The statistic $\chi^2 = nR^2$, has an asymptotic chi-square (χ^2) distribution with d.f. = p, where p is the no. of all explanatory variables in the auxiliary model.
- H_0 : All the variances σ_i^2 are equal (i.e., homoscedastic)
- Reject H_0 if $\chi^2 > \chi_{cr}^2$
- If there is heteroscedasticity, the estimated $Var(\hat{\beta})$ is biased and OLS might not be efficient anymore



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Applications of Linear Regressions to Time Series Data

Average hours worked per week by manufacturing workers:

Period	Hours	Period I	Hours	Period	Hours	Period I	Hours
1	37.2	11	36.9	21	35.6	31	35.7
2	37.0	12	36.7	22	35.2	32	35.5
3	37.4	13	36.7	23	34.8	33	35.6
4	37.5	14	36.5	24	35.3	34	36.3
5	37.7	15	36.3	25	35.6	35	36.5
6	37.7	16	35.9	26	35.6		
7	37.4	17	35.8	27	35.6		
8	37.2	18	35.9	28	35.9		
9	37.3	19	36.0	29	36.0		
10	37.2	20	35.7	30	35.7		



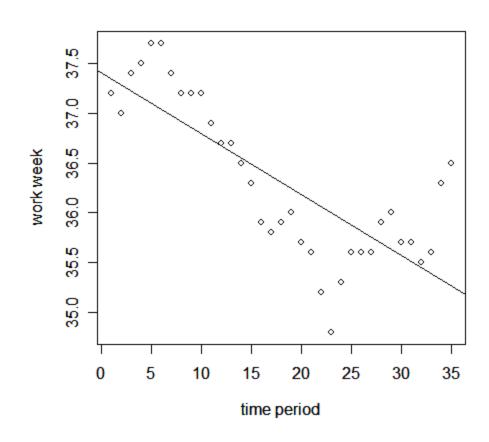
Forecasting Linear Trend using the Multiple Regression

```
, where: Y_i = data value for period i
Call:
                                             \hat{Y} = 37.416 - 0.0614X_i
lm(formula = y \sim x)
Residuals:
     Min 10 Median 30
                                            Max
-1.20297 -0.28361 0.04711 0.30798 1.23048
                                     Probability that the null hypothesis (\beta = 0) is true
Coefficients:
             Estimate Std. Error t value Pr(>|t|)
(Intercept) 37.40874 0.17502 213.744 < 2e-16\sqrt{***}
  -0.06112 0.00848 -7.208 2.9e-08 ***
X
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 0.5067 on 33 degrees of freedom
Multiple R-Squared: 0.6116, Adjusted R-squared: 0.5998
F-statistic: 51.95 on 1 \stackrel{\triangleright}{\triangleright}d 33 DF, p-value: 2.901e-08
```

 $Y_i = \beta_0 + \beta_1 X_i + \varepsilon_i$



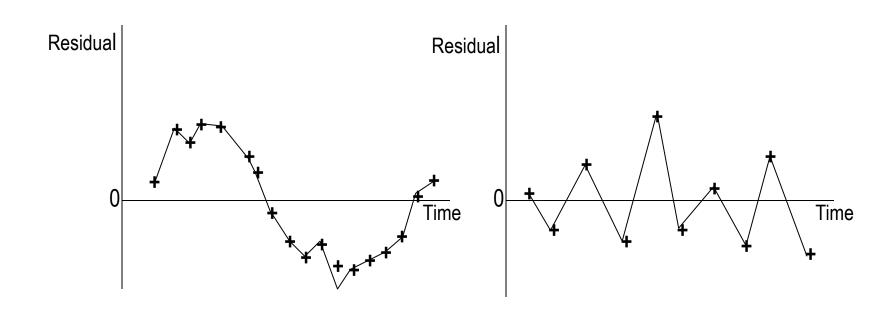
Hours Worked Data - A Linear Trend Line





Autocorrelation

- Examining the residuals over time, no pattern should be observed if the errors are independent
- Autocorrelation can be detected by graphing the residuals against time, or Durbin-Watson statistic





Autocorrelation

- Reasons leading to autocorrelation:
 - Omitted an important variable
 - Functional missfit
 - Measurement error in independent variable
- Use Durbin-Watson (DW) statistic to test for first order autocorrelation. DW takes values within [0, 4]. For no serial correlation, a value close to 2 (e.g., 1.5-2.5) is expected

$$DW = \frac{\sum_{i=2}^{n} (e_i - e_{i-1})^2}{\sum_{i=1}^{n} e_i^2}$$

- DW = 2 no autocorrelation
- DW = 0 perfect positive autocorrelation
- DW = 4 perfect negative autocorrelation



Test for Autocorrelation in R

```
0
                                          residuals.Im(mod)
> plot(residuals.lm(mod))
> library(car)
> durbin.watson(mod)
                                                  5
                                                     10
                                                        15
                                                           20
                                                              25
                                                                  30
                                                                     35
                                                         Index
lag Autocorrelation D-W Statistic p-value
             0.7705505
                              0.2775895
 Alternative hypothesis: rho != 0
```



Breusch-Godfrey Test



The BG test also considers higher-order autoregressive schemes:

$$Y_t = \beta_1 + \beta_2 X_t + \epsilon_t$$

$$\epsilon_t = \rho_1 u_{t-1} + \rho_2 u_{t-2} \dots + \rho_p u_{t-p} + u_t$$

Estimate the regression using OLS and obtain the R^2

If the sample size is large, Breusch and Godfrey have shown that $(n - p) R^2$ follow a chi-square distribution

If $(n - p) R^2$ exceeds the critical value at the chosen level of significance, we reject the null hypothesis, in which case at least one rho is statistically different from zero.



Modeling Seasonality



- A regression can estimate both the trend and additive seasonal indexes
 - Create dummy variables which indicate the season
 - Regress on time and the seasonal variables
 - Use the multiple regression model to forecast
- For any season, e.g. season 1, create a column with 1 for time periods which are season 1, and zero for other time periods (only season – 1 dummy variables are required)



Dummy Variables

	Trend variable Seasonal variables						
	Quarterly Input Data						
	Sales	t	Q1	Q2	Q3		
	3497	1	Spring	0	0		
Year 1	3484	2	0	Summer	0		
	3553	3	0	0	Fall		
	3837	4	Not Spring	Not Summer	Not Fall 📃		
Year 2	3726	5	1	0	0		
	3589	6	0	1	0		



Modelling Seasonality

The model which is fitted (assuming quarterly data) is

$$y = \beta_0 + \beta_1 t + \beta_2 Q_1 + \beta_3 Q_2 + \beta_4 Q_3$$

- Only 3 quarters are explicitly modelled. Otherwise:
 - $Q_1 = 1 (Q_2 + Q_3 + Q_4)$, for all 4 quarters -> Multicollinearity
- Allows to test for seasonality



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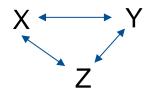
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Exp. value of the residual vector, given X, is 0

- Assumption: Other factors, which are not explicitly accounted for in the model but are contained in ε , are not correlated with X (exogeneity)
- Endogeneity $(corr(\varepsilon_i, X_i) \neq 0) \rightarrow E(\varepsilon_i | X_i) \neq 0$
- Reason for endogeneity: e.g. omitted variable (here Z)



Why is an omitted variable a problem?



Omitted Variables

 Consider the acceptance rates for the following groups of men and women who applied to college

Counts	Accepted	Not accepted	Total	Percents	Accepted	Not accepted
Men	198	162	360	Men	55%	45%
Women	88	112	200	Women	44%	56%
Total	286	274	560			

 A higher percentage of men were accepted: Is there evidence of discrimination?



Omitted Variables

Consider the acceptance rates broken down by type of school.

Computer Science

Counts	Accepted	Not accepted	Total
Men	18	102	120
Women	24	96	120
Total	42	198	240

Percents	Accepted	Not accepted	
Men	15%	85%	
Women	20%	80%	

School of Management

Counts	Accepted	Not accepted	Total
Men	180	60	240
Women	64	16	80
Total	244	76	320

	Not	
Accepted	accepted	
75%	25%	
80%	20%	
	75%	



Explanations?

- Within each school a higher percentage of women were accepted!
 - There was no discrimination against women
 - Women rather applied to schools with lower acceptance rates
 - Men applied in schools with higher acceptance rates
- This is an example of Simpson's paradox:



- When the omitted (aka. confounding) variable (Type of School) is ignored the data seem to suggest discrimination against women
- However, when the type of school is considered, the association is reversed and suggests discrimination against men
- see also https://en.wikipedia.org/wiki/Simpson%27s_paradox
- But we often do not have all relevant variables in the data ...?



Omitted Variable Bias

- Endogeneity is given when an independent variable is correlated with the error term and the covariance is not null
 - A reason for endogeneity might be that relevant variables are omitted from the model
 - For example, enthusiasm or willingness to take risks of an individual describe unobserved heterogeneity
- Various techniques have been developed to address endogeneity in <u>panel data</u>
 - see https://en.wikipedia.org/wiki/Omitted-variable_bias
 - see https://en.wikipedia.org/wiki/Endogeneity_(econometrics)

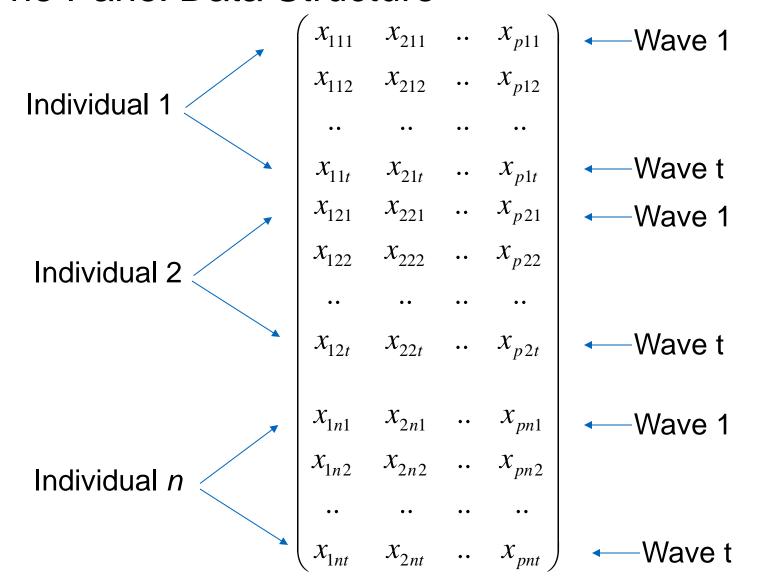


Panel Data vs. Cross-Section Data

- <u>Cross-section data</u> refers to data observing many subjects (such as individuals, firms or countries/regions) at the same point of time, or without regard to differences in time
 - There might be <u>omitted variables</u> (aka. confounder) describing important characteristics of individuals
- A <u>panel data set</u>, or longitudinal data set, is one where there are repeated observations on the same units
 - They may make it possible to overcome a problem of an omitted variable bias caused by unobserved heterogeneity
 - A balanced panel is one where every unit is surveyed in every time period
 - In an unbalanced panel some individuals have not been recorded in some time period



The Panel Data Structure



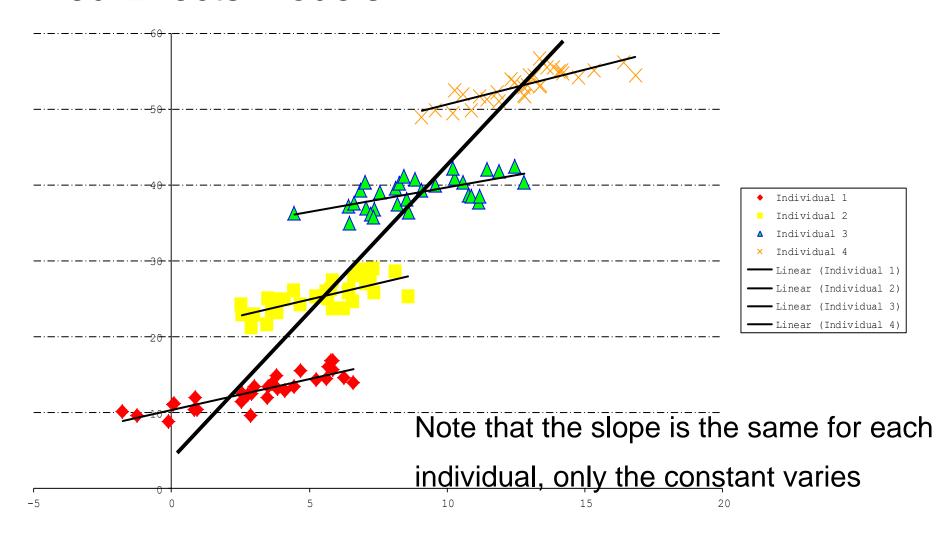


Treatment of Individual Effects

- There are two main options for the treatment of individual effects in panel data:
 - Fixed effects assume λ_i are constants (there is endogeneity)
 - Individual-specific effects are correlated to the other covariates
 - see also https://en.wikipedia.org/wiki/Fixed_effects_model
 - Random effects assume λ_i are drawn independently from some probability distribution
 - Individual-specific effects are uncorrelated to the other covariates
 - see also https://en.wikipedia.org/wiki/Random_effects_model
 - The Hausman test can help decide on one or the other
- Specific packages in R are available for fixed, random, and mixed effects models, which combine both (e.g., plm)



Fixed Effects Models





The Fixed Effect Model

Treat λ_i (the individual-specific heterogeneity) as <u>a constant</u> for each individual.

$$y_{it} = (\beta_0 + \lambda_i) + \beta_1 x_{1it} + \beta_2 x_{2it} + ... + \beta_p x_{pit} + \varepsilon_{it}$$

 λ is part of constant, but varies by individual i

Various estimators for fixed effect models: first differences, within, between, least squares dummy variable estimator



First-Differences Estimator

Eliminating unobserved heterogeneity by taking first differences

Original equation

$$y_{it} = \beta_0 + \lambda_i + \beta_1 x_{1it} + \beta_2 x_{2it} + \dots + \beta_p x_{pit} + \varepsilon_{it}$$

Lag one period and subtract

$$y_{it} - y_{it-1} = \beta_0 + \lambda_i + \beta_1 x_{1it} + \beta_2 x_{2it} + \dots + \beta_p x_{pit} + \varepsilon_{it}$$
$$-\beta_0 - \lambda_i - \beta_1 x_{1it-1} - \beta_2 x_{2it-1} - \dots - \beta_p x_{pit-1} - \varepsilon_{it-1}$$

Constant and individual effects eliminated

$$y_{it} - y_{it-1} = \beta_1 (x_{1it} - x_{1it-1}) + \beta_2 (x_{2it} - x_{2it-1}) + \dots$$
$$+ \beta_p (x_{pit} - x_{pit-1}) + (\varepsilon_{it} - \varepsilon_{it-1})$$

Transformed equation

$$\Delta y_{it} = \beta_1 \Delta x_{1it} + \beta_2 \Delta x_{2it} + \dots + \beta_p \Delta x_{pit} + \Delta \varepsilon_{it}$$



Alternative Estimators

- Within estimator (for more than two periods)
 - Take deviations from individual means and apply least squares

$$y_{it} - \bar{y}_i = \beta_1(x_{1it} - \bar{x}_{1i}) + \dots + \beta_p(x_{pit} - \bar{x}_{pi}) + (\varepsilon_{it} - \bar{\varepsilon}_i)$$
 relies on variations within individuals

- Least squares dummy variable estimator
 - uses a dummy variable for each individual



Random Effects Model

- The **fixed effect assumption** is that the individual specific effect is correlated with the independent variables $(cov(\lambda_i, x_{jit}) \neq 0)$.
- The random effects assumption (in a random effects model) is that the individual specific effects are *uncorrelated* with the independent variables $(cov(\lambda_i, x_{iit}) = 0$, but λ_i might be correlated).

$$y_{it} = \beta_0 + \beta_1 x_{1it} + \beta_2 x_{2it} + \dots + \beta_p x_{pit} + \varepsilon_{it}$$

$$y_{it} = \beta_0 + \beta_1 x_{1it} + \beta_2 x_{2it} + \dots + \beta_p x_{pit} + \lambda_i + u_{it}$$

 λ_i is part of error term in random effects models



The Hausman Test

- Test of whether the fixed effects (FE) or random effects (RE) model is appropriate, i.e. a test for endogeneity.
- The test takes into account the covariance matrix of the FE and RE estimators as well as the estimates and follows a chi-square (χ^2) distribution.
- Null hypothesis: no correlation between *X* and the residuals.



Gauss-Markov Assumptions in Detail

The OLS estimator is the best linear unbiased estimator (BLUE), iff

1) Linearity

Linear relationship in parameters β

2) No multicollinearity of predictors

No linear dependency between predictors



3) Homoscedasticity

The residuals exhibit constant variance

4) No autocorrelation

There is no correlation between the ith and jth residual terms

5) **Expected value** of the residual vector, given X, is 0 ($E(\varepsilon|X) = 0$)

(i.e. exogeneity $(cov(\varepsilon, X) = 0)$)



Guest Lecture on December 19, 2019

There will be a guest lecture in this class by

Markus Heimann

Director Digital & Data Competence Center, Telefónica Germany GmbH & Co. OHG,



This guest lecture will be part of the WITS conference to take place in the H4 Hotel in Munich at **9am on December 19, 2019**.

Venue: H4 Hotel München Messe, Konrad-Zuse-Platz 14, 81829 München, Germany

There is restricted room capacity, and need you to **register for this guest lecutre via Moodle**. Please only sign up, if you really intend to come. The registration form will be opened today.