Topic 2 Basic Logic Gates

Electronic Switch – Transistors

• Transistors are the basis of binary digital circuits

Transistors operate at 2 values
 H / L or
 On / Off or
 1 / 0

Evolution of electronic switches

- 1930s: Relays

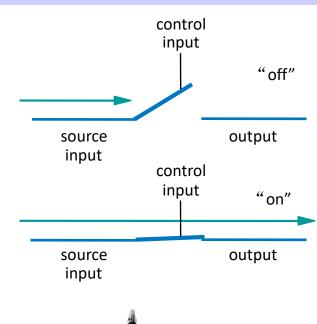
- 1940s: Vacuum tubes

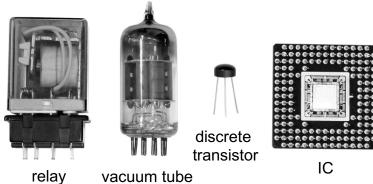
1950s: Discrete transistor

- 1960s: Integrated circuits (ICs)

Initially just a few transistors on IC

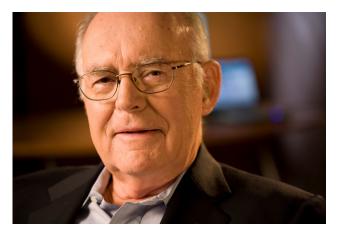
• Then tens, thousands, millions...

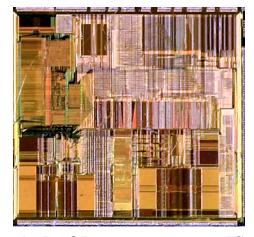




Moore's Law

- IC capacity doubling about every 18 months for several decades
 - Known as "Moore's Law" after Gordon Moore, co-founder of Intel
 - Predicted in 1965 predicted that components per IC would double roughly every 18 months or so
 - For a particular number of transistors, the IC shrinks by half every 18 months
 - Enables incredibly powerful computation in incredibly tiny devices
 - Today's ICs hold billions of transistors
 - The first Pentium processor (early 1990s) had only 3 million

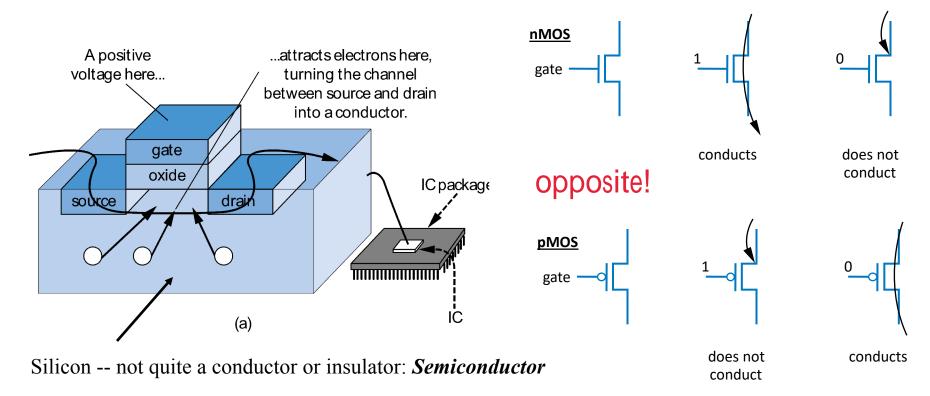




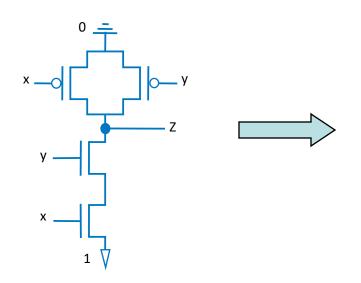
An Intel Pentium processor IC having millions of transistors

CMOS Transistor

- CMOS Complementary Metal-Oxide-Semiconductor
- Transistors with CMOS technology



AND Logic

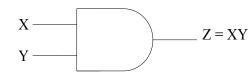


X	Y	Z = XY
0	0	0
0	1	0
1	0	0
1	1	1

Truth Table

Definition of AND operation

 $Z = X \cdot Y$ means Z = 1 if and only if both X = 1 and Y = 1; AND operator Variable



2-input AND gate

Truth Table

• Truth table creates the relationship between the inputs and outputs

- Must include all the inputs to the device in the left columns
- Must include all the outputs of the device in the right columns
- The behavior of the circuit is implied by the table

Inputs $\begin{cases} I1 \longrightarrow \\ I2 \longrightarrow \\ I3 \longrightarrow \end{cases}$	Digital Circuit	O1 > O2 -	Outputs
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Number of combinations is 2^N; N is the number of the inputs

ΟI	e _I	nputs		Outp	uts
	Ĭ1	I2	I3	O1	O_2
(0	0	0	?	?
	0	0	1	?	?
	0	1	0	?	?
	0	1	1	?	?
	1	0	0	?	?
	1	0	1	?	?
	1	1	0	?	?
	1	1	1	?	?

Example of Truth Table

а	b	F				
0	0					
0	1					
1	0					
1	1					
(a)						

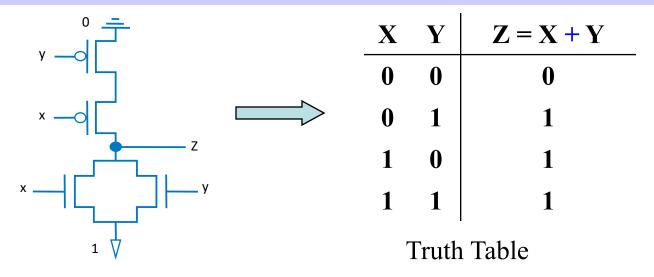
а	b	С	F			
0	0	0				
0	0	1				
0	1	0				
0	1	1				
1	0	0				
1	0	1				
1	1	0				
1	1	1				
(h)						

(a)

а	b	С	d	F
0	0	0	0	
0	0	0	1	
0	0	1	0	
0	0	1	1	
0	1	0	0	
0	1	0	1	
0	1	1	0	
0	1	1	1	
1	0	0	0	
1	0	0	1	
1	0	1	0	
1	0	1	1	
1	1	0	0	
1	1	0	1	
1	1	1	0	
1	1	1	1	
		(c))	

(C)

OR Logic

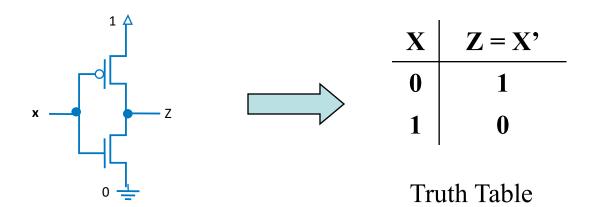


• Definition of OR operation

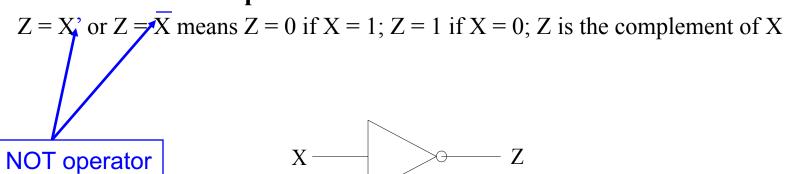
Z = X + Y means Z = 1 if either X = 1 or Y = 1, or both;

OR operator X = X + Y Y = 12-input OR gate

NOT Logic

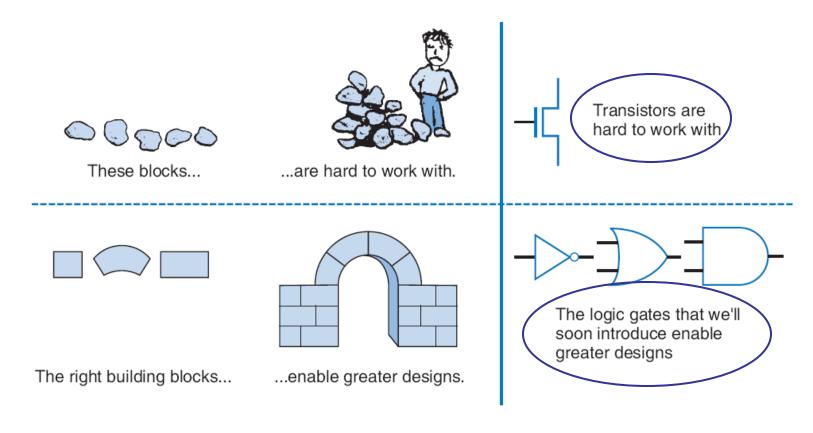


Definition of NOT operation



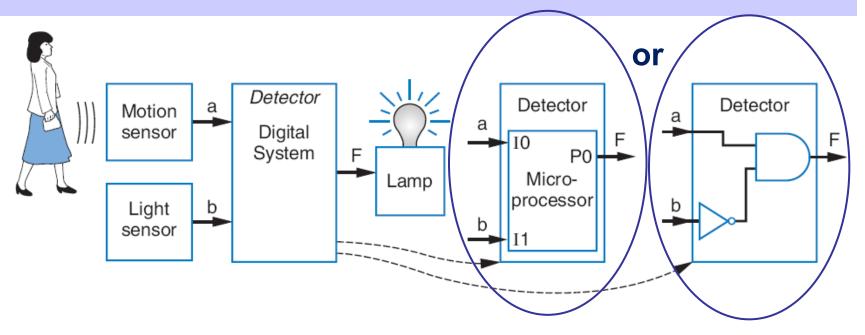
NOT gate/Inverter

Logic Gates



• "Logic gates" are better digital circuit building blocks than switches (transistors)

Logics in Human Language



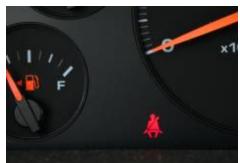
Motion-in-dark example

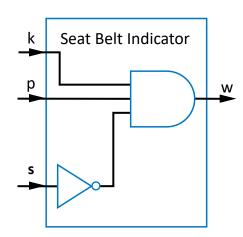
- Human language: Turn on lamp (F=1) when motion sensed
 (a) and no light (not b)
- Logic Equation: F = a AND NOT(b) = ab'
- Logic circuit: implementation using logic gates, AND and NOT, as shown

Example: Seat Belt Warning Light System

- Design circuit for warning light
- Sensors
 - − s=1: seat belt fastened
 - − k=1: key inserted
 - p=1: person in seat
- Function description
 - Light on if person in seat,
 and seat belt not fastened,
 and key inserted
- Logic equationw = p AND NOT(s) AND k

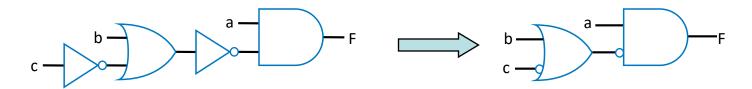






Example: Represent Logic Equation with Logic Gates

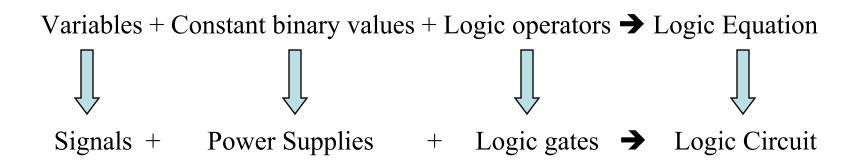
• Q: Convert the following equation to logic gates: F = a AND NOT(b OR NOT(c))



Precedence of Logic Operations

From Logic Equation to Logic Circuit

• There exists a correspondence between a Logic Equation and its logic circuit.

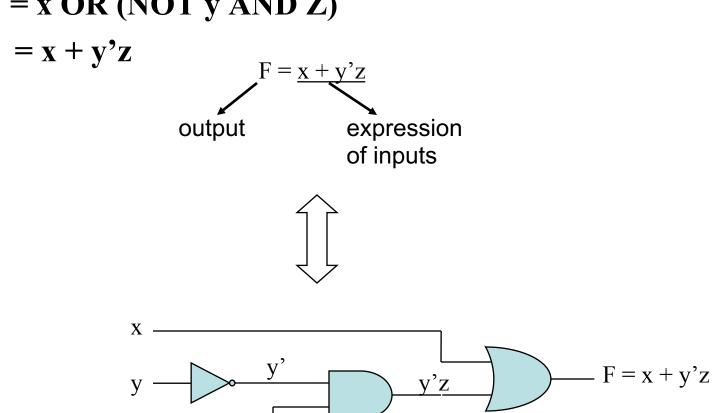


Logic Circuit:

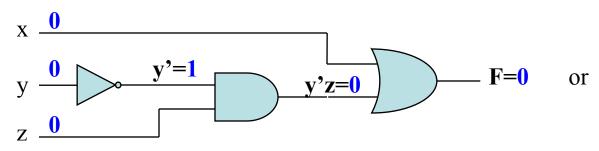
A net of logic gates.

Logic Equation and Logic Circuit

• F = x OR (NOT y AND Z)



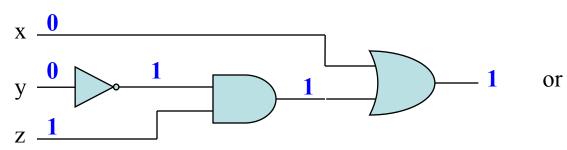
• $\mathbf{F} = \mathbf{x} + \mathbf{y}^{2}\mathbf{z}$



$F = 0 + 0^{\circ} \bullet 0$
$= 0 + 1 \cdot 0$
= 0 + 0
=0

X	у	Z	y'	y'z	F
0	0	0	1	0	0
0	0	1	?	?	?
0	1	0	?	?	?
0	1	1	?	?	?
1	0	0	?	?	?
1	0	1	?	?	?
1	1	0	?	?	?
1	1	1	?	?	?

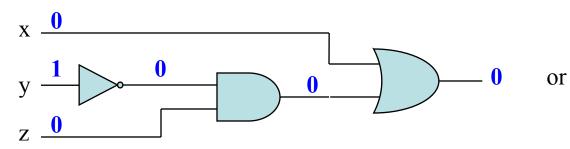
• $\mathbf{F} = \mathbf{x} + \mathbf{y}^{2}\mathbf{z}$



F = 0 + 0• 1	-
$=0+1 \bullet 1$	
= 0 + 1	
= 1	

X	у	Z	y'	y'z	F
0	0	0	1	0	0
0	0	1	1	1	1
0	1	0	?	?	?
0	1	1	?	?	?
1	0	0	?	?	?
1	0	1	?	?	?
1	1	0	?	?	?
1	1	1	?	?	?

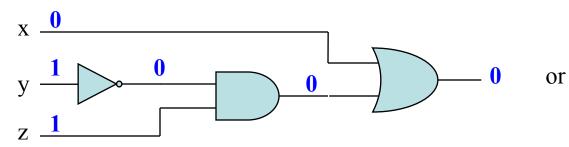
• $\mathbf{F} = \mathbf{x} + \mathbf{y}^{2}\mathbf{z}$



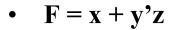
$F = 0 + 1' \bullet 0$
$=0+0 \bullet 0$
= 0 + 0
=0

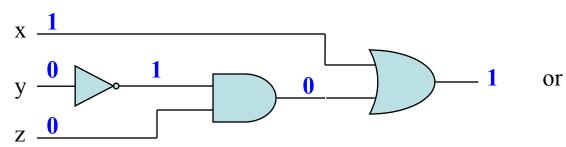
X	у	Z	y'	y'z	F
0	0	0	1	0	0
0	0	1	1	1	1
0	1	0	0	0	0
0	1	1	?	?	?
1	0	0	?	?	?
1	0	1	?	?	?
1	1	0	?	?	?
1	1	1	?	?	?

• $\mathbf{F} = \mathbf{x} + \mathbf{y}^{2}\mathbf{z}$



X	у	Z	y'	y'z	F
0	0	0	1	0	0
0	0	1	1	1	1
0	1	0	0	0	0
0	1	1	0	0	0
1	0	0	?	?	?
1	0	1	?	?	?
1	1	0	?	?	?
1	1	1	?	?	?

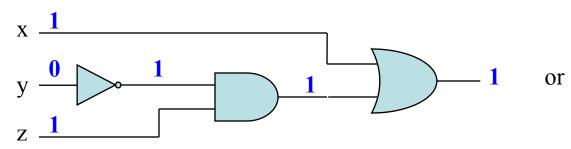




$F = 1 + 0' \bullet 0$
$=1+1 \bullet 0$
= 1 + 0
= 1

X	у	Z	y'	y'z	F
0	0	0	1	0	0
0	0	1	1	1	1
0	1	0	0	0	0
0	1	1	0	0	0
1	0	0	1	0	1
1	0	1	?	?	?
1	1	0	?	?	?
1	1	1	?	?	?

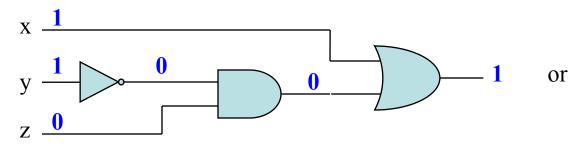
• $\mathbf{F} = \mathbf{x} + \mathbf{y}^{2}\mathbf{z}$



$F = 1 + 0^{\circ} 1$	
$= 1 + 1 \bullet 1$	
= 1 + 1	
= 1	

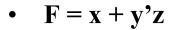
X	у	Z	y'	y'z	F
0	0	0	1	0	0
0	0	1	1	1	1
0	1	0	0	0	0
0	1	1	0	0	0
1	0	0	1	0	1
1	0	1	1	1	1
1	1	0	?	?	?
1	1	1	?	?	?

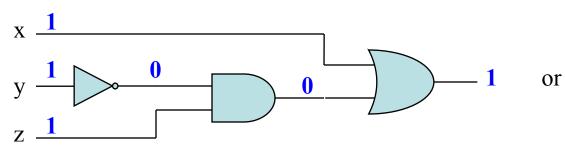
• $\mathbf{F} = \mathbf{x} + \mathbf{y}^{2}\mathbf{z}$



$F = 1 + 1' \bullet 0$
$=1+0 \bullet 0$
= 1 + 0
= 1

X	у	Z	y'	y'z	F
0	0	0	1	0	0
0	0	1	1	1	1
0	1	0	0	0	0
0	1	1	0	0	0
1	0	0	1	0	1
1	0	1	1	1	1
1	1	0	0	0	1
1	1	1	?	?	?



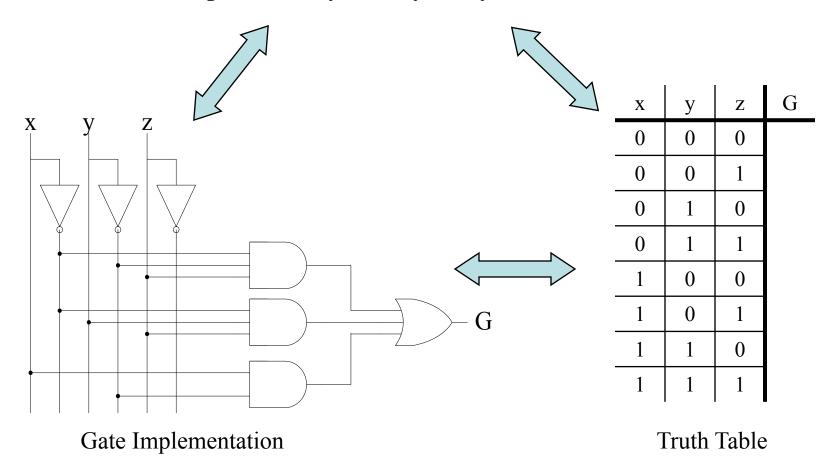


F = 1 + 1 '• 1
$= 1 + 0 \bullet 1$
= 1 + 0
= 1

X	У	Z	y'	y'z	F
0	0	0	1	0	0
0	0	1	1	1	1
0	1	0	0	0	0
0	1	1	0	0	0
1	0	0	1	0	1
1	0	1	1	1	1
1	1	0	0	0	1
1	1	1	0	0	1

Logic Equation, Truth Table, & Logic Circuit

• Another example: G = x'y'z + x'yz + xy'



Create Truth Table

а	b	F		
0	0			
0	1			
1	0			
1	1			
(a)				

а	b	С	F		
0	0	0			
0	0	1			
0	1	0			
0					
	1	1			
1	0	0			
1	0	1			
1	1	0			
1	1	1			
(b)					

b С

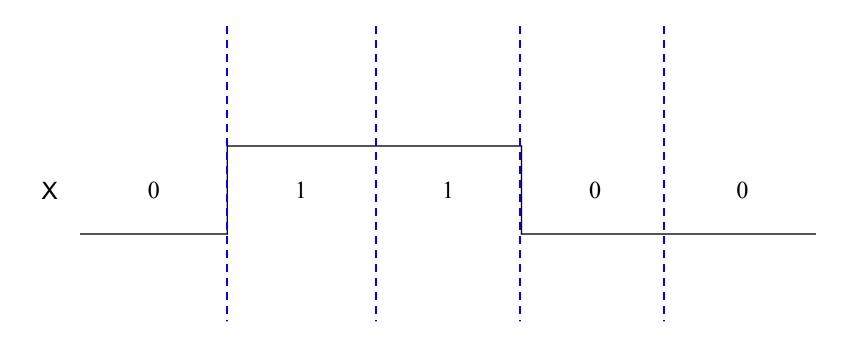
(c)

 Q: Use truth table to define function F(a,b,c) that is 1 only when abc is 5 or greater in binary

а	b	С	F	
0	0	0	0	
0	0	1	0	
0	1	0	0	
0	1	1	0	
1	0	0	0	
1	0	1	1	
1	1	0	1	
1	1	1	1	

Timing Diagram

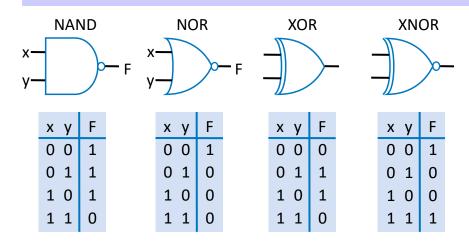
• Timing diagrams show the response to changes on a signal in voltage levels with time



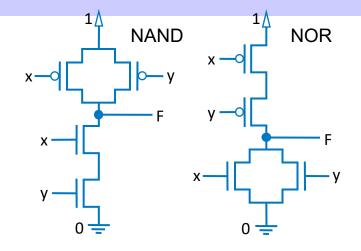
Timing Diagrams for Gates

xy	7	F						
0	0	0	X	0	1	1	0	0
0 1	1	0	Λ		-	-		
1 (0	0						
1	1	1	Υ	0	0	1	1	0
x + <u>x</u>	y	F						
0	0	0	X•Y	0	0	1	0	0
0	1	1						
1 (0	1	\ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \	0	1	1	1	0
1 1	1	1	X+Y	0	1	1	1	0
3	x	F						
	0	1	Χ'	1	0	0	1	1
	1	0						

More Gates



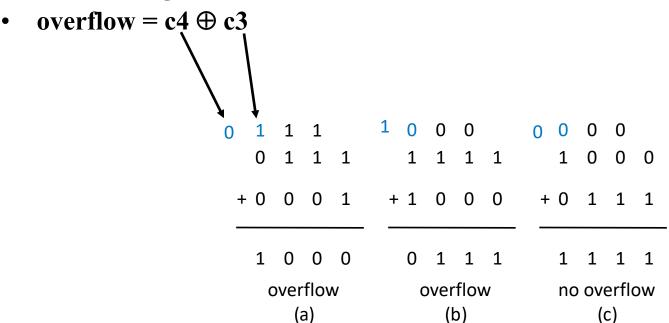
- NAND: Opposite of AND ("NOT AND")
- NOR: Opposite of OR ("NOT OR")
- XOR: outputs 1 when inputs have odd number of 1's
- XNOR: Opposite of XOR ("NOT XOR")



- AND in CMOS: NAND with NOT
- OR in CMOS: NOR with NOT
- So NAND/NOR more common

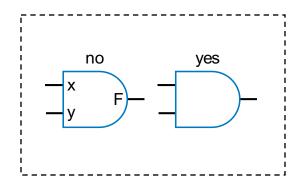
Detecting Overflow: Method 2

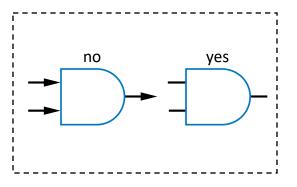
• Simpler method: Detect difference between carry-in to sign bit and carry-out from sign bit

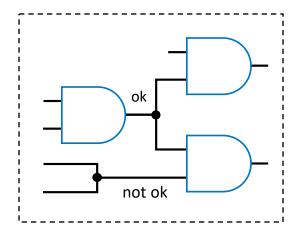


If the carry into the sign bit column differs from the carry out of that column, overflow has occurred.

Some Circuit Drawing Conventions







Avoid multi-driver problem!

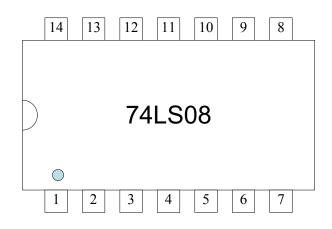
Integrated Circuit

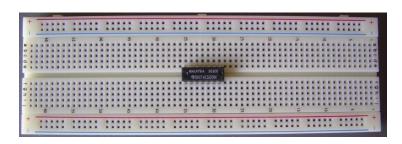
- Integrated Circuit (IC) chip
 - Contains logic components and/or devices for constructing digital circuits
- Integration Levels
 - Small-Scale Integration (SSI)
 - Fewer than 10 gates
 - Medium-Scale Integration (MSI)
 - 10 to 1000 gates
 - Large-Scale Integration (LSI)
 - Thousands of gates
 - Very Large-Scale Integration (VLSI)
 - Millions of gates
 - Ultra Large-Scale Integration (ULSI)
 - Billions of gates

— ...

Integrated Circuit

- TTL Transistor-Transistor Logic
- **ECL** Emitter-Coupled Logic
- **MOS** Metal-Oxide Semiconductor
- **CMOS** Complementary MOS





Chip placed on breadboard

