1.a Geometric interpretation of gradient descent

Let *C* be the cost function we are aiming to minimize. Then the update rule for gradient descent takes the form

$$v \to v' = v - \eta \nabla C = v - \varepsilon \frac{\nabla C}{||\nabla C||}.$$

For the one-dimensional case this simplifies to

$$v \to v' = v - \varepsilon \cdot \operatorname{sgn}(C'(v)).$$

Geomtrically speaking, this implies we are always going ε to the left or the right. The direction depends on whether the cost function is increasing or decreasing at our current location.

1.b b

The use of mini-batches is justified by the following heuristic:

$$\frac{\sum_{j=1}^{m} \nabla C_{X_j}}{m} \approx \frac{\sum_{x} \nabla C_{x}}{n} = \nabla C, \tag{1}$$

where n is the full size of the training data set and m is the size of the mini-batch. Let's compare m=1 to m=20. The validity of approximation (3) depends on m, with a higher m implying a better approximation (there are established concentration-inequalities to support this claim). For m=1 the estimate of the gradient will frequently be worse than for m=20. Consequently, each step with m=1 will generally not decrease the cost as much as m=20. In worst cases, we might have a terrible approximation and might increase the cost

On the other hand, evaluating m = 1 is faster than m = 20, so we will be able to do more steps with the same time and resources.

2 Problem

2.a

Following the notation in the Nelson Book consider (BP2):

$$\delta^l = \left(\left(w^{l+1} \right)^T \delta^{l+1} \right) \odot \sigma' \left(z^l \right)$$

In component form, this is

$$\delta_j^l = \sum_k w_{kj}^{l+1} \delta_k^{l+1} \sigma' \left(z_j^l \right).$$

If we replace the activation function at a single neuron by f, this becomes for a fixed l, j

$$\delta_j^l = \sum_k w_{kj}^{l+1} \delta_k^{l+1} f'\left(z_j^l\right).$$

Accordingly, $\delta^1, \ldots, \delta^{l-1}$, which depend on δ^l_j , will change. By (BP3) and (BP4), the step estimate for b^l_j , the biases and weights in all the layers before the change will have to be adjusted.

2.b

Let *f* the softmax activation function i.e.

$$a_j^L = \frac{e^{z_j^L}}{\sum_k e^{z_k^L}},$$

Let *y* be the one-hot encoding of the correct label and *C* be the log-likelihood cost

$$C = -\sum_{i=1}^{c} y_i \cdot \log\left(a_i^L\right)$$

Then we have for the cost in the outputlayer: Consider first

$$\begin{split} \frac{\partial - \log(a_j^L)}{\partial z_i^L} &= \frac{\partial}{\partial z_i^L} - \log\left(\frac{e^{z_j^L}}{\sum_k e^{z_k^L}}\right) \\ &= \frac{\partial}{\partial z_i^L} \left(-z_j^L + \log\left(\sum_k e^{z_k^L}\right)\right) \\ &= -\mathbb{1}(i=j) + \frac{\partial}{\partial z_i^L} \left(\log\left(\sum_k e^{z_k^L}\right)\right) \\ &= -\mathbb{1}(i=j) + \frac{1}{\sum_k e^{z_k^L}} \left(\frac{\partial}{\partial z_i^L} \left(\sum_k e^{z_k^L}\right)\right) \\ &= -\mathbb{1}(i=j) + \frac{e^{z_i^L}}{\sum_k e^{z_k^L}} \\ &= -\mathbb{1}(i=j) + a_i^L \end{split}$$

Combining, we have

$$\begin{split} \delta_i^L &= \frac{\partial C}{\partial z_i^L} \\ &= \frac{\partial}{\partial z_i^L} - \sum_{j=1}^c y_j \cdot \log \left(a_j^L \right) \\ &= -\sum_{j=1}^c y_j \cdot \frac{\partial}{\partial z_i^L} \log \left(a_j^L \right) \\ &= \sum_{j=1}^c y_j \cdot \left(-\mathbb{1}(i=j) + a_i^L \right) \\ &= -y_i + a_i^L \sum_{j=1}^c y_j \\ &= a_i^L - y_i. \end{split}$$

2.c

If we replace the sigmoid layer with a linear identity layer, the neural network simplifies to a single big matrix multiplication from the input layer to the output layer. We will always have $\sigma'(z^L) = 1$. Accordingly, we have:

$$\delta^{L} = \nabla_{a}C$$

$$\delta^{l} = \left(w^{l+1}\right)^{T} \delta^{l+1} = \prod_{i=l+1}^{L-1} \left(w^{i}\right)^{T} \nabla_{a}C$$

$$\frac{\partial C}{\partial b_{j}^{l}} = \delta_{j}^{l} = \left(w_{j}^{l+1}\right)^{T} \prod_{i=l+2}^{L-1} \left(w^{i}\right)^{T} \nabla_{a}C$$

$$\frac{\partial C}{\partial w_{jk}^{l}} = a_{k}^{l-1} \delta_{j}^{l} = a_{k}^{l-1} \left(w_{j}^{l+1}\right)^{T} \prod_{i=l+2}^{L-1} \left(w^{i}\right)^{T} \nabla_{a}C$$

$$(2)$$

The upgrade step of the gradient descent will be governed by the last two lines.

3 Problem

3.a Problem

Consider

$$-[y \ln a + (1-y) \ln(1-a)], \tag{3}$$

and

$$-[a \ln y + (1-a) \ln(1-y)]. \tag{4}$$

We know that $a = \sigma(z) \in (0, 1)$, because σ only takes values in (0, 1). On the other hand, $y \in [0, 1]$. We will use $a \in (0, 1)$ in the following. For y = 0 we have in equation (3):

$$-[y \ln a + (1-y) \ln(1-a)] = \ln(1-a).$$

This makes sense. For y = 1 we have in equation (3):

$$-[y \ln a + (1-y) \ln(1-a)] = \ln a.$$

This makes sense. For y = 0 we have in equation (4):

$$-[a \ln y + (1-a) \ln(1-y)] = -[a \cdot (-\infty) + (1-a) \cdot 0] = \infty.$$

This makes no sense. For y = 1 we have in equation (4):

$$-[a \ln y + (1-a) \ln(1-y)] = -[a \cdot (0) + (1-a) \cdot (-\infty)] = \infty.$$

This makes no sense. Those problems do not arise in equation (3), because $a \in (0, 1)$.

3.b Problem

Let σ be the sigmoid function and C the cross-entropy cost. By equations (3.7) and (3.8) in the Nielson book we have:

$$\begin{split} \frac{\partial C}{\partial w_j} &= \frac{1}{n} \sum_x x_j (\sigma(z) - y), \\ \frac{\partial C}{\partial b} &= \frac{1}{n} \sum_x (\sigma(z) - y). \end{split}$$

Note, that the derivation for those equations in the Nielson book is valid for general $y,a\in[0,1]$. Consequently, if we have $\sigma(z)=y$ for all training inputs, we have $\frac{\partial C}{\partial w_j}=\frac{\partial C}{\partial b}=0$ for all j. This shows that $\sigma(z)=y$ is a critical point of the cost function. It remains to verify that it is a minimum. Note, that

$$\frac{\partial C}{\partial w_j \partial w_k} = \frac{\partial C}{\partial w_j \partial z} \frac{\partial z}{\partial w_k}$$

$$= \left(\frac{1}{n} \sum_{x} x_j \sigma'(z)\right) (a_k) > 0.$$

$$\frac{\partial C}{\partial w_j \partial b} = \frac{\partial C}{\partial w_j \partial z} \frac{\partial z}{\partial b}$$

$$= \left(\frac{1}{n} \sum_{x} x_j \sigma'(z)\right) > 0.$$

$$\frac{\partial C}{\partial b \partial b} = \frac{\partial C}{\partial b \partial z} \frac{\partial z}{\partial b}$$
$$= \left(\frac{1}{n} \sum_{x} \sigma'(z)\right) > 0.$$

This concludes the proof. Furthermore, plugging in $\sigma(z) = y$ yields

this does not seem right

$$C = -\frac{1}{n} \sum_{x} [y \ln y + (1 - y) \ln(1 - y)].$$

3.c Problem

Let

$$\begin{split} W^2 &= \begin{bmatrix} 0.15 & 0.25 \\ 0.2 & 0.3 \end{bmatrix} = \begin{bmatrix} w_{1,1}^2 & w_{1,2}^2 \\ w_{2,1}^2 & w_{2,2}^2 \end{bmatrix}, \\ b^2 &= \begin{bmatrix} 0.35 \\ 0.35 \end{bmatrix} = \begin{bmatrix} b_1^1 \\ b_2^1 \end{bmatrix}, \\ W^3 &= \begin{bmatrix} 0.4 & 0.5 \\ -0.45 & 0.55 \end{bmatrix} = \begin{bmatrix} w_{1,1}^3 & w_{1,2}^3 \\ w_{2,1}^3 & w_{2,2}^3 \end{bmatrix}, \\ b^3 &= \begin{bmatrix} 0.6 \\ 0.6 \end{bmatrix} = \begin{bmatrix} b_1^2 \\ b_2^2 \end{bmatrix}. \end{split}$$

Then the output of the neural network for an input x is

$$\sigma(W^2(\sigma(W^1x + b^1)) + b^2).$$

We can calculate the δ^1 , δ^2 , δ^3 with the central equations of the back-propagation algorithm:

$$\begin{split} \delta^L &= \nabla_a C \odot \sigma' \left(z^L \right) \\ \delta^l &= \left(\left(w^{l+1} \right)^T \delta^{l+1} \right) \odot \sigma' \left(z^l \right) \end{split}$$

The cross-entropy function *C* is defined by

$$C = -\frac{1}{n} \sum_{x} [y \ln a + (1 - y) \ln(1 - a)].$$

This yields

$$\nabla_a C = -\frac{1}{n} \sum_{x} \left[\frac{y}{a} - \frac{1-y}{1-a} \right].$$

$$\begin{split} \frac{\partial C}{\partial z} &= -\frac{1}{n} \sum_{x} \left(\frac{y}{\sigma(z)} - \frac{1 - y}{1 - \sigma(z)} \right) \frac{\partial \sigma}{\partial z} \\ &= -\frac{1}{n} \sum_{x} \left(\frac{y}{\sigma(z)} - \frac{1 - y}{1 - \sigma(z)} \right) \sigma(z) (1 - \sigma(z)) \\ &= -\frac{1}{n} \sum_{x} y (1 - \sigma(z)) - \sigma(z) (1 - y) \end{split}$$

```
In []: import matplotlib.pyplot as plt
import numpy as np
import torch
import torch.nn as nn
from IPython.display import Image
from prob5_AE import AE
from prob6_CAE import CAE
from prob6_CAE_skip import CAE_skip, train_log, test, main_wrapper
from torchvision import datasets
```

Problem 3

Let

$$x = egin{bmatrix} 0.05 \ 0.1 \end{bmatrix}, \ y = egin{bmatrix} 0.01 \ 0.99 \end{bmatrix}, \ W^2 = egin{bmatrix} 0.15 & 0.25 \ 0.2 & 0.3 \end{bmatrix} = egin{bmatrix} w_{1,1}^2 & w_{1,2}^2 \ w_{2,1}^2 & w_{2,2}^2 \end{bmatrix}, \ b^2 = egin{bmatrix} 0.35 \ 0.35 \end{bmatrix} = egin{bmatrix} b_1^1 \ b_2^1 \end{bmatrix}, \ W^3 = egin{bmatrix} 0.4 & 0.5 \ -0.45 & 0.55 \end{bmatrix} = egin{bmatrix} w_{1,1}^3 & w_{1,2}^3 \ w_{2,1}^3 & w_{2,2}^3 \end{bmatrix}, \ b^3 = egin{bmatrix} 0.6 \ 0.6 \end{bmatrix} = egin{bmatrix} b_1^2 \ b_2^2 \end{bmatrix}. \ \end{pmatrix}$$

```
In []: # x matrix
x = np.array([[0.05], [0.1]])

# y matrix
y = np.array([[0.01], [0.99]])

# W2 matrix
W2 = np.array([[0.15, 0.25], [0.2, 0.3]])

# b2 matrix
b2 = np.array([[0.35], [0.35]])

# W3 matrix
W3 = np.array([[0.4, 0.5], [-0.45, 0.55]])

# b3 matrix
b3 = np.array([[0.6], [0.6]])
```

Then the output of the neural network for an input x is

$$\sigma(W^2(\sigma(W^1x+b^1))+b^2).$$

The intermediate values are

```
In []: z2 = np.dot(W2, x) + b2
a2 = 1 / (1 + np.exp(-z2))
z3 = np.dot(W3, a2) + b3
a3 = 1 / (1 + np.exp(-z3))
```

We can calculate the $\delta^1, \delta^2, \delta^3$ with the central equations of the back-propagation algorithm:

$$egin{aligned} \delta^{L} &=
abla_{a} C \odot \sigma'\left(z^{L}
ight) \ \delta^{l} &= \left(\left(w^{l+1}
ight)^{T} \delta^{l+1}
ight) \odot \sigma'\left(z^{l}
ight) \end{aligned}$$

For the cross entropy-loss in combination with the sigmoid activation function, we have

$$\begin{split} \frac{\partial C}{\partial z} &= -\frac{1}{n} \sum_{x} \left(\frac{y}{\sigma(z)} - \frac{1 - y}{1 - \sigma(z)} \right) \frac{\partial \sigma}{\partial z} \\ &= -\frac{1}{n} \sum_{x} \left(\frac{y}{\sigma(z)} - \frac{1 - y}{1 - \sigma(z)} \right) \sigma(z) (1 - \sigma(z)) \\ &= -\frac{1}{n} \sum_{x} y (1 - \sigma(z)) - \sigma(z) (1 - y) \end{split}$$

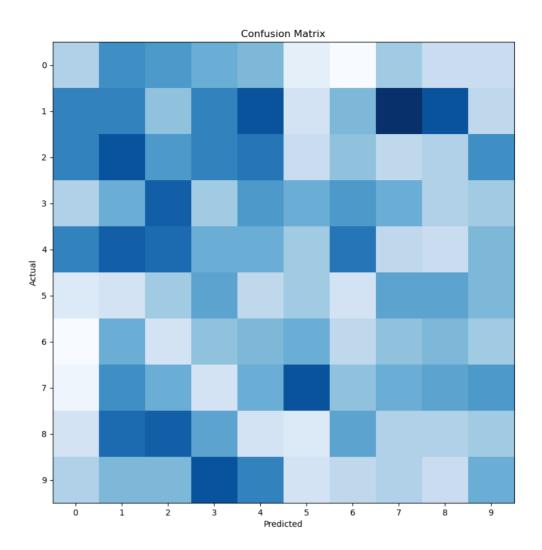
Now for the intermediate values we have

Problem 4

sample input data

```
print(output.shape)
        torch.Size([1, 9, 9])
In [ ]: #max-pooling
        m = nn.MaxPool2d(kernel_size= 10, stride=2, padding = 2)
        output = m(input)
        print(output.shape)
        torch.Size([1, 23, 23])
In [ ]: #max-pooling
        m = nn.MaxPool2d(kernel size= 2, stride=1, padding = 0)
        output = m(input)
        print(output.shape)
        torch.Size([1, 49, 49])
        Problem 4.2
In [ ]: mnist_testset = datasets.MNIST(root='./data', train=False, download=True, tr
        ntest = 2000
        test data = (mnist testset.data.to(dtype=torch.float32)[:ntest]/255).view(-1
        test labels = mnist testset.targets.to(dtype=torch.long)[:ntest]
        after runnign the code we have
In [ ]: #show prob4 CNN.png
        Image(filename='prob4_CNN.png', width=800)
Out[]:
In []: Image(filename='prob4 confusion matrix.png', width=800)
```

Out[]:



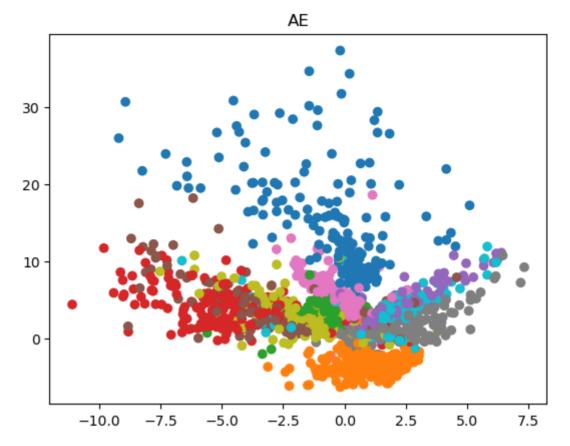
1 and 7 are confused, which makes sense. 9 and 3 are confused, which makes sense.

```
In []: test_data_flat = test_data.reshape(-1, 28*28)

model = AE()
model.load_state_dict(torch.load('mnist_ae.pt'))

embedded_ae = model.encoder(test_data_flat)
embedded_ae = embedded_ae.detach().numpy()

plt.figure()
plt.scatter(embedded_ae[:,0], embedded_ae[:,1], c=test_labels, cmap='tab10')
plt.title('AE')
plt.show()
```



We see that 5 and 3 are harder to seperate which agrees with our domain knowledge. 7 is similar to 9.

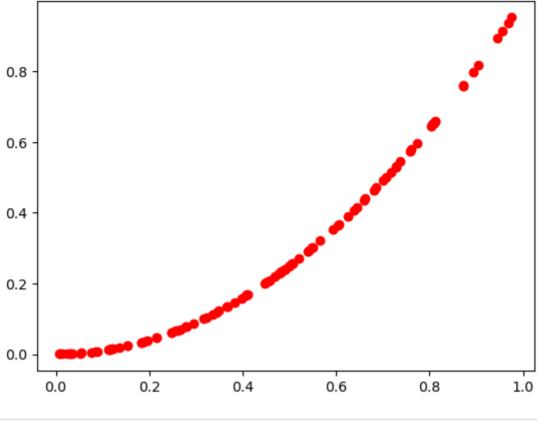
For Problem 5.4,

Problem 5

Problem 5.1 1) In a classical auto encoder, bow tie architercutre the middle layer is called the bottlenec. The dimension of the bottleneck is chosen to be drastically different from the input and output layer. This way it is impossible for the NN to simply copy the input to the output. 2) By introducing regularisation/corruption, we introduce a preference for some solution compared to others. Typically this prohibits the NN from simply copying the input to the output. 3) For an input sample X, we can perturb it to $\tidle X$. We train the NN to compare the output of X to $\tidle X$. This way the NN learns to ignore the perturbations and focus on the important features of the input.

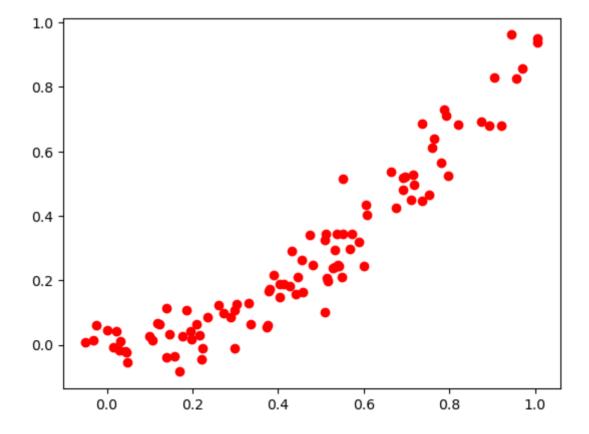
Problem 5.2 We can add gaussian noise to a sample to corrupt it.

```
In []: #generate 1000 random numbers uniformly distributed between 0 and 1
    x = np.random.rand(100)
    y = x**2
    plt.plot(x,y, 'ro')
Out[]: [<matplotlib.lines.Line2D at 0x7f965a888d60>]
```



```
In []: #add gaussian noise to x and y
x_corrupt = x + np.random.randn(100)*0.05
y_corrupt = y + np.random.randn(100)*0.05
plt.plot(x_corrupt, y_corrupt, 'ro')
```

Out[]: [<matplotlib.lines.Line2D at 0x7f965a9e4400>]



Problem 5.3 It can mathematically be shown that an autoencoder with a single linear layer is equivalent to PCA. This is because PCA is a linear transformation that tries to find

the directions of maximum variance in the data. The autoencoder with a single linear layer tries to find a subspace which preserves as much information as possible, s.t. the reconstruction loss is reduced.

Problem 5.4

Regular autoencoder

```
In []: model = AE()
  model.load_state_dict(torch.load('mnist_ae.pt'))
Out[]: <All keys matched successfully>
In []: test_data_flat = test_data.reshape(-1, 28*28)
  embedded_ae = model.encoder(test_data_flat)
  decoded = model.decoder(embedded_ae)
```

Problem 6

Convolutional auto encoder without skip connections

```
In []: model_cae = CAE()
    model_cae.load_state_dict(torch.load('mnist_cae.pt'))
Out[]: <All keys matched successfully>
In []: embedded_cae = model_cae.encoder(test_data)
    decoded_cae = model_cae.decoder(embedded_cae)

Convolutional auto encoder with skip connections
```

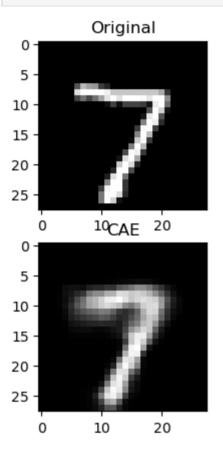
```
In [ ]: model_cae_skip = CAE_skip()
  model_cae_skip.load_state_dict(torch.load('mnist_cae_skip.pt'))
```

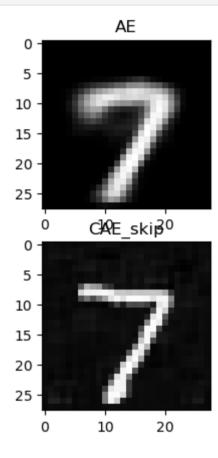
Out[]: <All keys matched successfully>

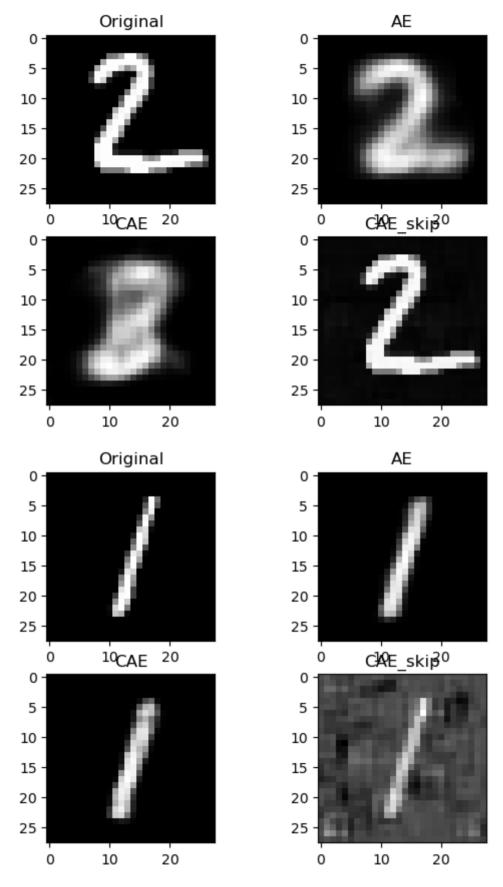
```
In [ ]: embedded_cae_skip, x4, x1 = model_cae_skip.encoder(test_data)
decoded_cae_skip = model_cae_skip.decoder(embedded_cae, x4, x1)
```

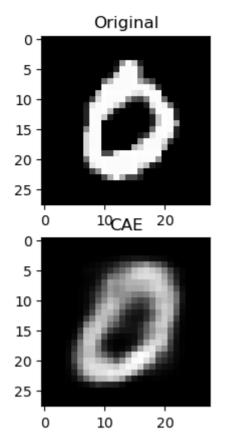
```
In [ ]: #plot test data and reconstructed images
        for i in range(4):
                #original image
                input i = test data[i].detach().numpy()
                #ae
                output i ae = decoded[i].detach().numpy()
                output_i_cae = decoded_cae[i].detach().numpy()
                #cae skip
                output i cae skip = decoded cae skip[i].detach().numpy()
                input i = input i.reshape(28,28)
                output i ae = output i ae.reshape(28,28)
                output_i_cae = output_i_cae.reshape(28,28)
                output i cae skip = output i cae skip.reshape(28,28)
                #plot data and output next to each other
                plt.figure()
                plt.subplot(2,2,1)
```

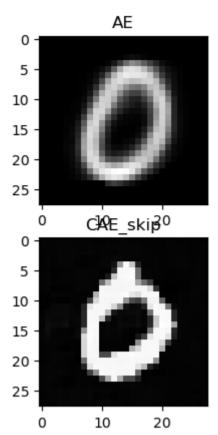
```
plt.imshow(input_i, cmap='gray')
plt.title('Original')
plt.subplot(2,2,2)
plt.imshow(output_i_ae, cmap='gray')
plt.title('AE')
plt.subplot(2,2,3)
plt.imshow(output_i_cae, cmap='gray')
plt.title('CAE')
plt.subplot(2,2,4)
plt.subplot(2,2,4)
plt.imshow(output_i_cae_skip, cmap='gray')
plt.title('CAE_skip')
plt.title('CAE_skip')
plt.show()
```





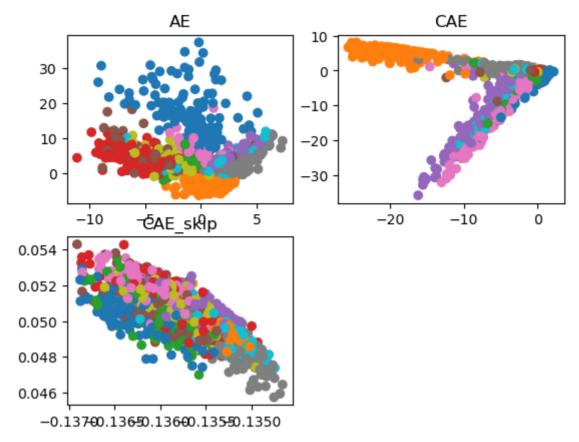






```
In []: embedded_ae = embedded_ae.detach().numpy()
    embedded_cae = embedded_cae.detach().numpy()
    embedded_cae_skip = embedded_cae_skip.detach().numpy()
In []: #plot_embedded_embedded_cae_skip.detach().numpy()
```

```
In []: #plot embedded, embedded_cae, embedded_cae_skip
    plt.figure()
    plt.subplot(2,2,1)
    plt.scatter(embedded_ae[:,0], embedded_ae[:,1], c=test_labels, cmap='tab10')
    plt.title('AE')
    plt.subplot(2,2,2)
    plt.scatter(embedded_cae[:,0], embedded_cae[:,1], c=test_labels, cmap='tab10
    plt.title('CAE')
    plt.subplot(2,2,3)
    plt.scatter(embedded_cae_skip[:,0], embedded_cae_skip[:,1], c=test_labels, c
    plt.title('CAE_skip')
    plt.show()
```



TODO write We see that 5 and 3 are harder to seperate which agrees with our domain knowledge. 7 is similar to 9.

With Corruption

```
In [ ]:
        args =
                dict(batch size=64,
                test batch size=1000,
                epochs=10,
                momentum=0.5,
                no cuda=False,
                seed=1,
                log interval=10,
                save model=True)
        kwargs = {'num workers': 1, 'pin memory': True} if not args['no cuda'] else
In [ ]: # Download the MNIST dataset
        mnist_trainset = datasets.MNIST(root='./data', train=True, download=True, tr
        mnist testset = datasets.MNIST(root='./data', train=False, download=True, tr
        # training data
        ntrain = 60000
        train_data = (mnist_trainset.data.to(dtype=torch.float32)[:ntrain]/255).view
        train_labels = mnist_trainset.targets.to(dtype=torch.long)[:ntrain]
            # testing data
        ntest = 2000
        test data = (mnist testset.data.to(dtype=torch.float32)[:ntest]/255).view(-1
        test labels = mnist testset.targets.to(dtype=torch.long)[:ntest]
            # Load into torch datasets
        train dataset = torch.utils.data.TensorDataset(train data, train labels)
        test dataset = torch.utils.data.TensorDataset(test data, test labels)
        train_loader = torch.utils.data.DataLoader(
```

```
train_dataset, batch_size=args['batch_size'], drop_last=True, shuffle=Tr
)

test_loader = torch.utils.data.DataLoader(
    test_dataset, batch_size=args['test_batch_size'], drop_last=True, shuffl
)
```

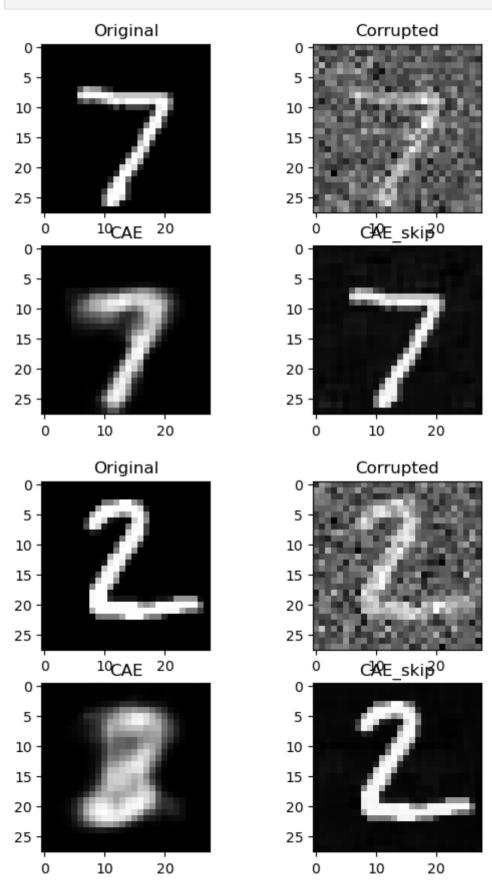
Training the autoencoder with corruption

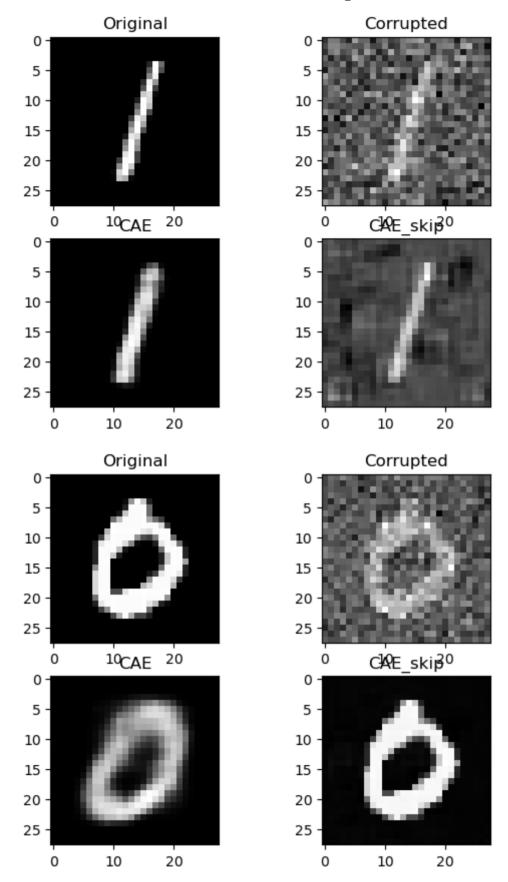
Training the convolutional autoencoder with corruption

TTraining the convolutional autoencoder with skip with corruption

```
Train Epoch: 1 | Train set: Average loss: 0.0136
        Test set: Average loss: 1.0454
        Train Epoch: 2
                               Train set: Average loss: 0.0009
        Test set: Average loss: 0.3776
        Train Epoch:
                      3
                               | Train set: Average loss: 0.0003
        Test set: Average loss: 0.1074
                               Train set: Average loss: 0.0001
        Train Epoch: 4
        Test set: Average loss: 0.0284
                     5
                              Train set: Average loss: 0.0000
        Train Epoch:
        Test set: Average loss: 0.0089
        Train Epoch: 6
                           Train set: Average loss: 0.0000
        Test set: Average loss: 0.0036
        Train Epoch: 7
                                | Train set: Average loss: 0.0000
        Test set: Average loss: 0.0019
                              | Train set: Average loss: 0.0000
        Train Epoch: 8
        Test set: Average loss: 0.0011
                              Train set: Average loss: 0.0000
        Train Epoch:
                     9
        Test set: Average loss: 0.0006
        Train Epoch: 10
                               Train set: Average loss: 0.0000
        Test set: Average loss: 0.0004
Out[]: <All keys matched successfully>
In [ ]: embedded cae corrupt = mnist cae corrupt.encoder(test data corrupt)
        decoded cae corrupt = mnist cae corrupt.decoder(embedded cae corrupt)
In []: embedded cae skip corrupt, x4, x1 = mnist cae skip corrupt.encoder(test data
        decoded cae skip corrupt = mnist cae skip corrupt.decoder(embedded cae skip
In [ ]: #plot test data and reconstructed images
        for i in range(4):
                #original image
                input i = test data[i].detach().numpy()
                #corrupted image
                input i corrupt = test data corrupt[i].detach().numpy()
                #cae
                output i cae = decoded cae[i].detach().numpy()
                #cae skip
                output i cae skip = decoded cae skip[i].detach().numpy()
                input i = input i.reshape(28,28)
                input_i_corrupt = input_i_corrupt.reshape(28,28)
                output i cae = output i cae.reshape(28,28)
                output i cae skip = output i cae skip.reshape(28,28)
                #plot data and output next to each other
                plt.figure()
                plt.subplot(2,2,1)
                plt.imshow(input_i, cmap='gray')
                plt.title('Original')
                plt.subplot(2,2,2)
                plt.imshow(input i corrupt, cmap='gray')
                plt.title('Corrupted')
```

```
plt.subplot(2,2,3)
plt.imshow(output_i_cae, cmap='gray')
plt.title('CAE')
plt.subplot(2,2,4)
plt.imshow(output_i_cae_skip, cmap='gray')
plt.title('CAE_skip')
plt.show()
```



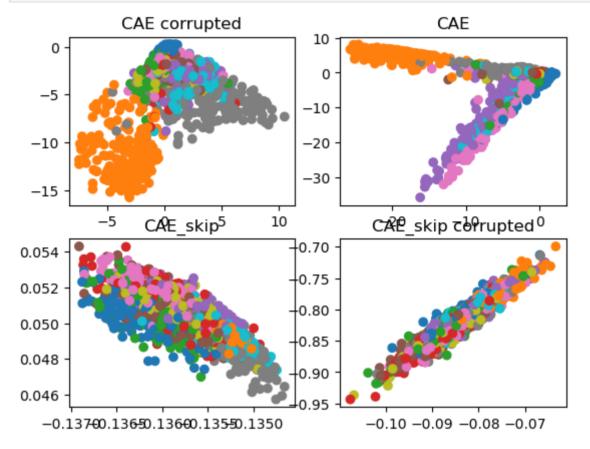


For most pictures, the CAE with skip conncetions performs a lot better!

```
In []: embedded_cae_corrupt = embedded_cae_corrupt.detach().numpy()
    embedded_cae_skip_corrupt = embedded_cae_skip_corrupt.detach().numpy()

In []: #plot embedded, embedded_cae, embedded_cae_skip
    plt.figure()
    plt.subplot(2,2,1)
```

```
plt.scatter(embedded_cae_corrupt[:,0], embedded_cae_corrupt[:,1], c=test_lab
plt.title('CAE corrupted')
plt.subplot(2,2,2)
plt.scatter(embedded_cae[:,0], embedded_cae[:,1], c=test_labels, cmap='tab10
plt.title('CAE')
plt.subplot(2,2,3)
plt.scatter(embedded_cae_skip[:,0], embedded_cae_skip[:,1], c=test_labels, c
plt.title('CAE_skip')
plt.subplot(2,2,4)
plt.scatter(embedded_cae_skip_corrupt[:,0], embedded_cae_skip_corrupt[:,1],
plt.title('CAE_skip corrupted')
plt.show()
```



The emdedding of the CAE with skip connections is a lot more compact than the other two.