

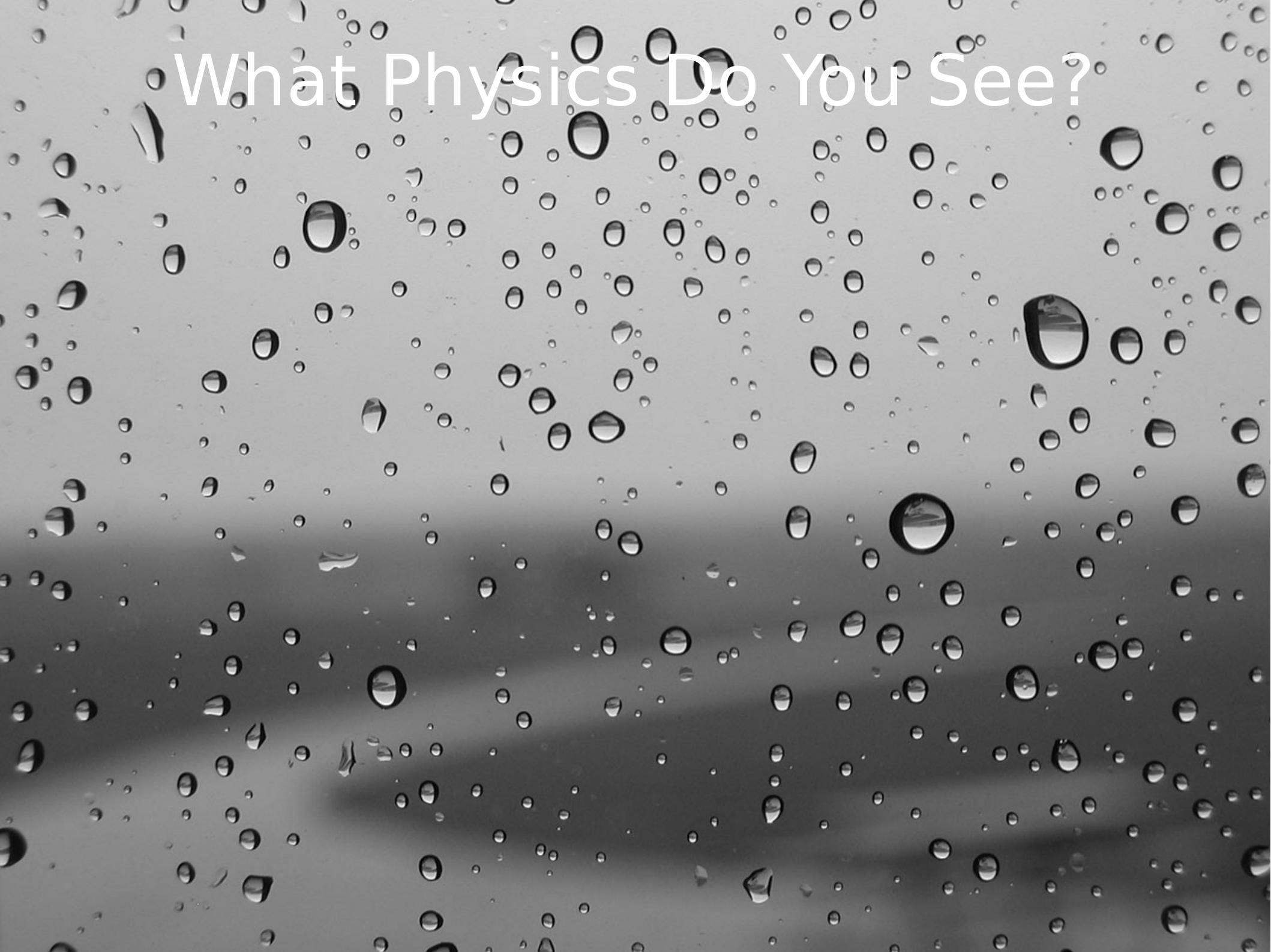


# From Heavy-Ion Collisions to Quark-Gluon matter

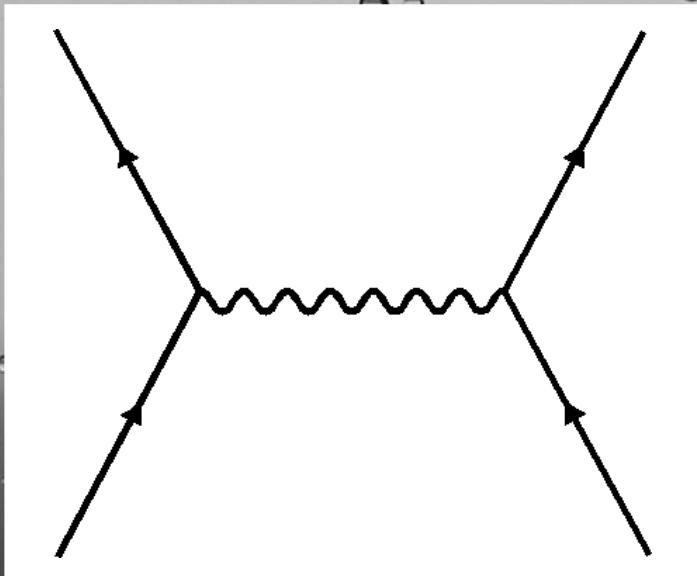
Constantin Loizides  
(LBNL)

- Part I: Introduction and background
- Part II: Results mainly related to bulk properties
- Part III: Results mainly related to hard probes

# What Physics Do You See?

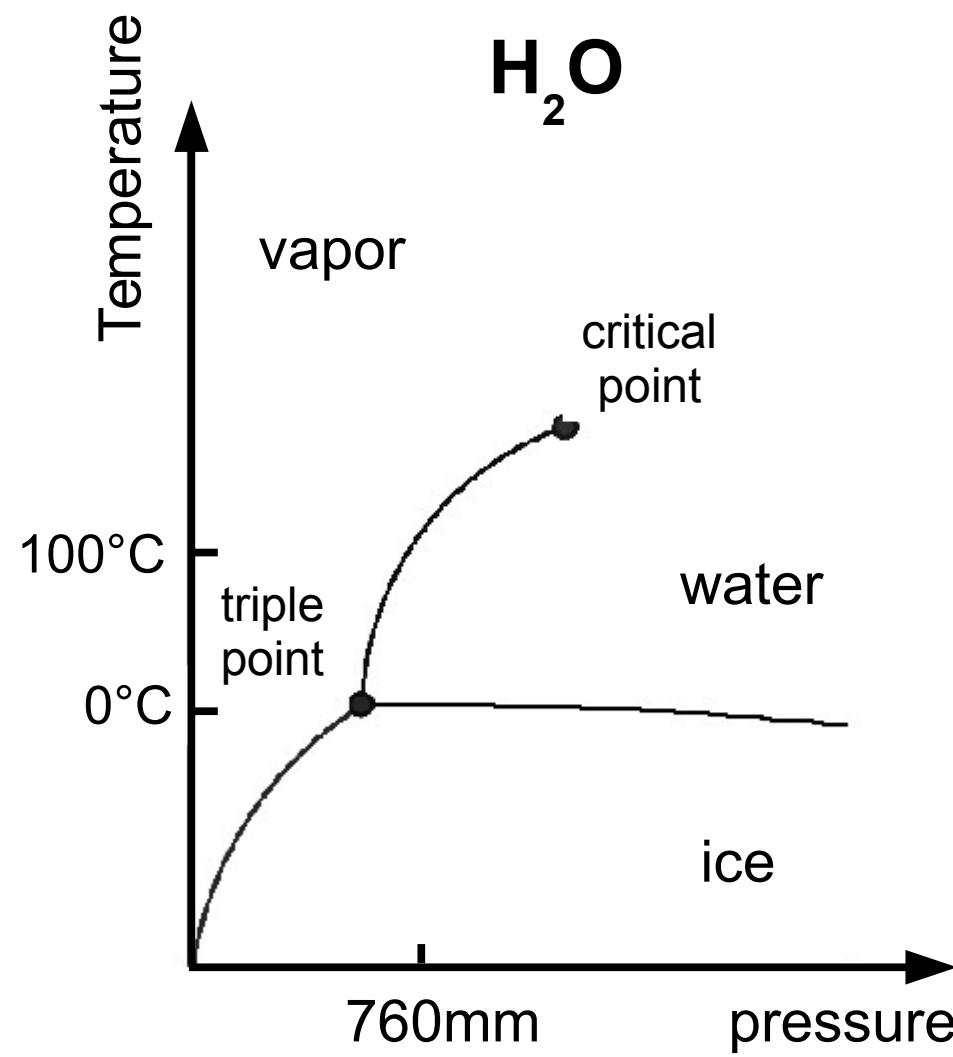
A black and white photograph showing numerous water droplets of various sizes scattered across a dark, textured surface. The droplets reflect light, creating bright highlights on their tops and darker areas below, giving them a three-dimensional appearance. Some droplets are larger and more prominent, while others are smaller and more numerous, creating a sense of depth and texture.

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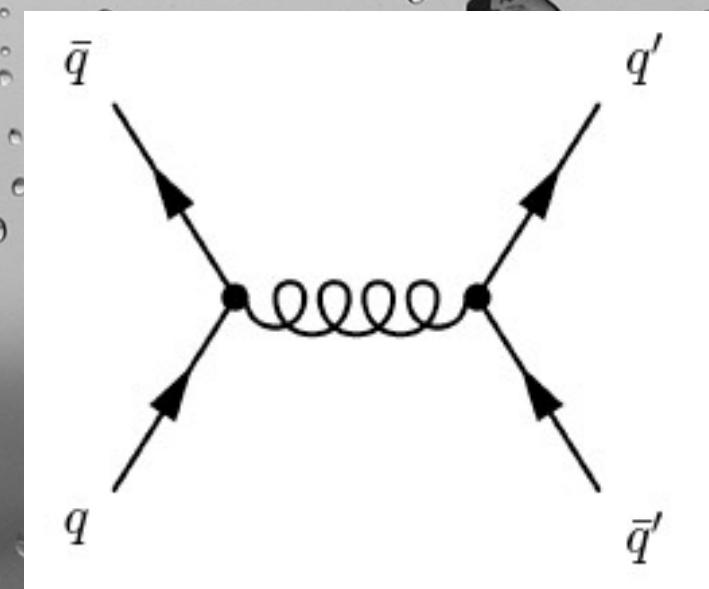
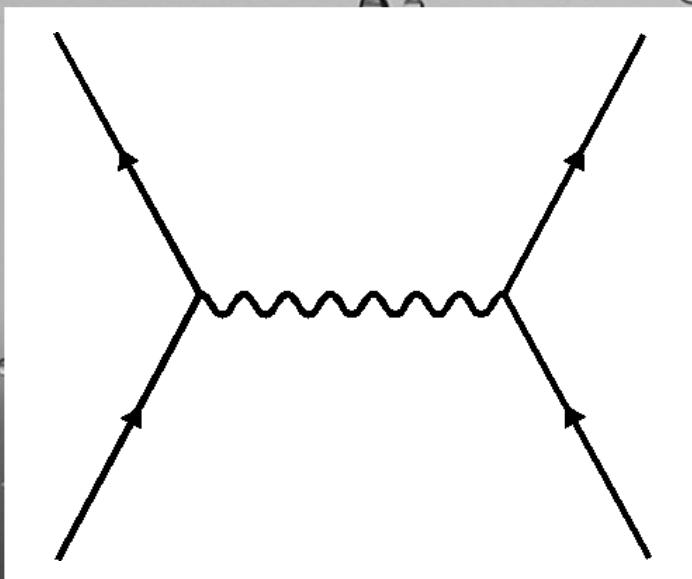


- The water droplets on the window demonstrate a principle:
- Truly beautiful and complex physics emerges in systems whose underlying dynamics is given by QED

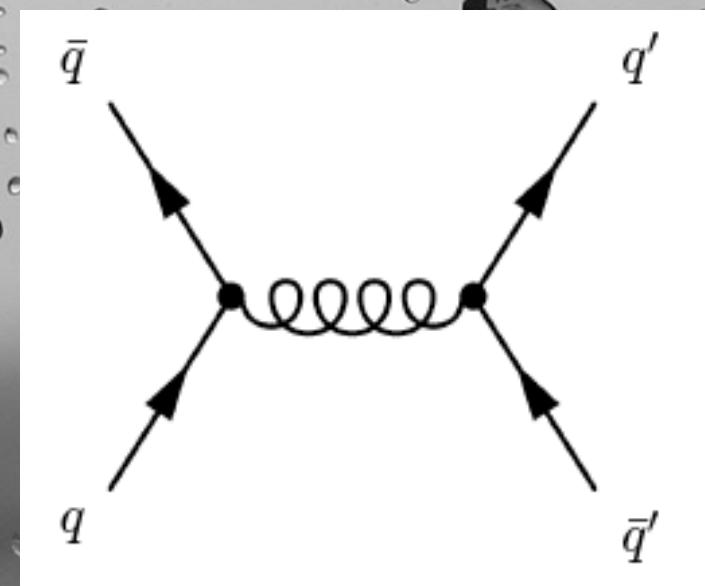
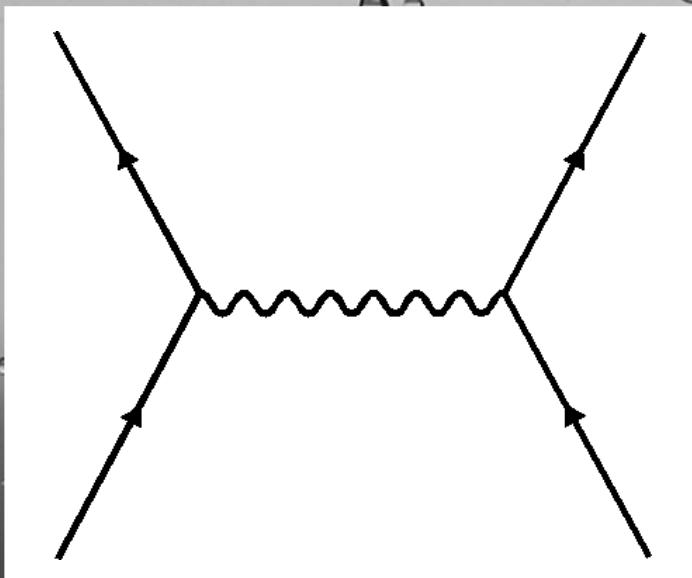
# What Physics Do You See?



Does QCD exhibit equally  
beautiful properties when  
looked at as bulk matter?



# Does QCD exhibit equally beautiful properties when looked at as bulk matter?



Of course, the answer is yes  
as we will see ...

# Quantum Chromo Dynamics

(see e.g. arXiv:hep-ph/9505231)

# The standard model and QCD

## FERMIIONS

matter constituents  
spin = 1/2, 3/2, 5/2, ...

Leptons spin = 1/2		
Flavor	Mass GeV/c <sup>2</sup>	Electric charge
$\nu_e$ electron neutrino	$<1 \times 10^{-8}$	0
e electron	0.000511	-1
$\nu_\mu$ muon neutrino	<0.0002	0
$\mu$ muon	0.106	-1
$\nu_\tau$ tau neutrino	<0.02	0
$\tau$ tau	1.7771	-1

## Quarks

spin = 1/2

Flavor	Approx. Mass GeV/c <sup>2</sup>	Electric charge
u up	0.003	2/3
d down	0.006	-1/3
c charm	1.3	2/3
s strange	0.1	-1/3
t top	175	2/3
b bottom	4.3	-1/3

## BOSONS

force carriers  
spin = 0, 1, 2, ...

Unified Electroweak spin = 1		
Name	Mass GeV/c <sup>2</sup>	Electric charge
$\gamma$ photon	0	0
$W^-$	80.4	-1
$W^+$	80.4	+1
$Z^0$	91.187	0

Strong (color) spin = 1		
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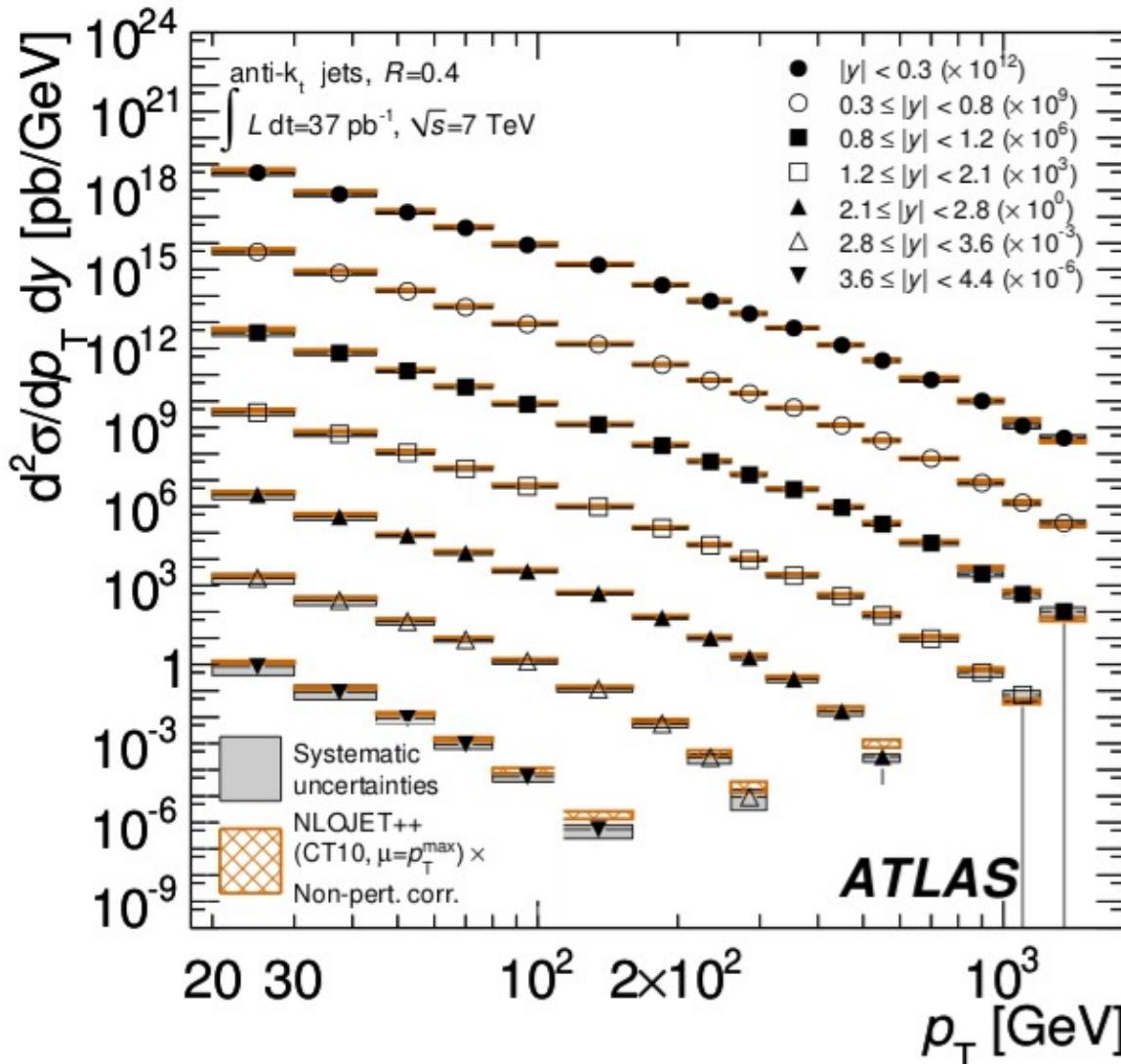
  

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- Strong interactions
  - Binds quarks into hadrons
  - Binds nucleons into nuclei
- Described by QCD
  - Interactions between quarks and gluons carrying color charge
  - Mediated by gluons, the strong force carriers

# The standard model and QCD

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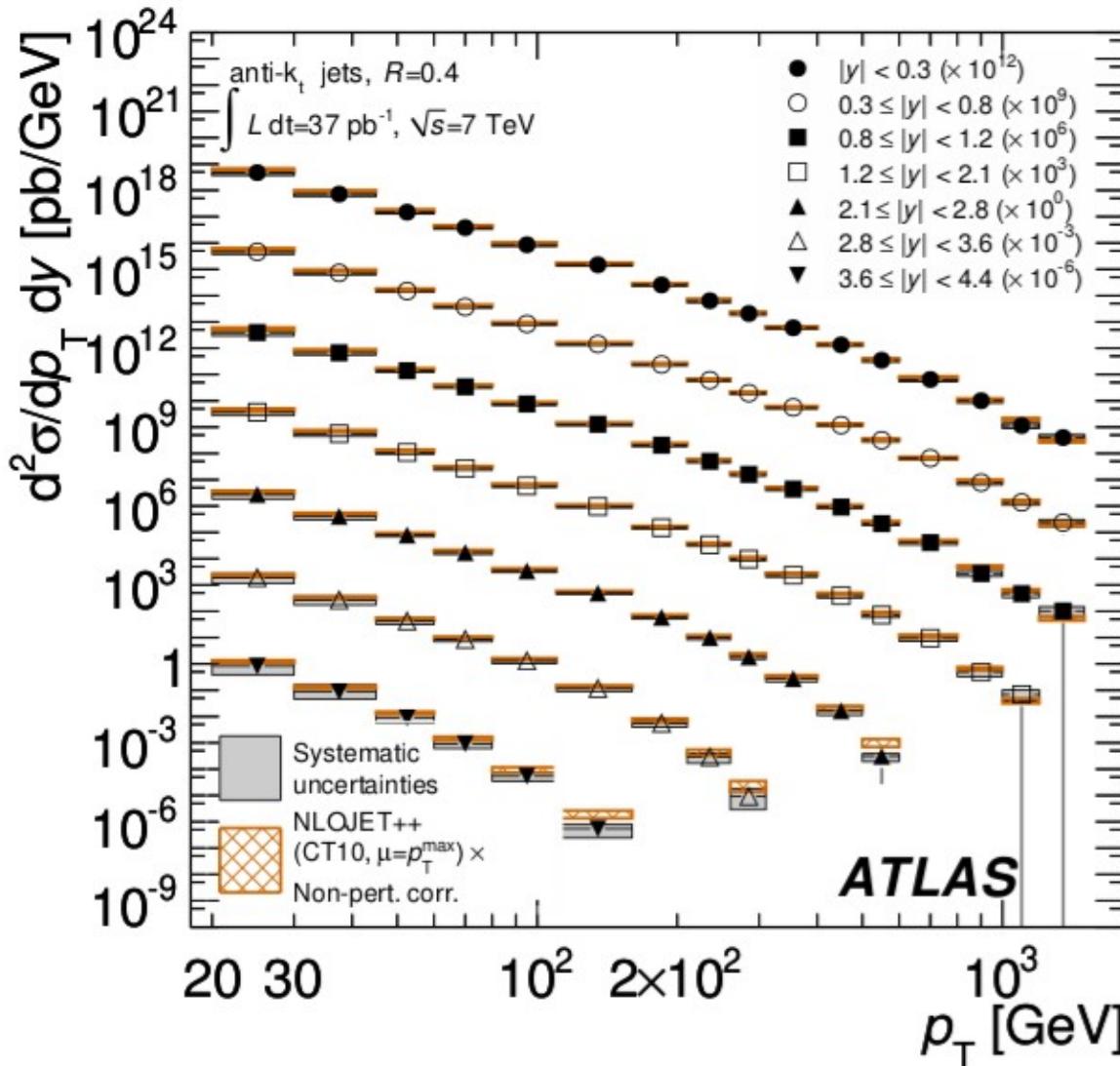


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ATLAS, Phys.Rev. D86 (2012) 014022

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- Very successful theory
  - e.g. pQCD vs production of high energy jets
- But with outstanding puzzles!

# Two puzzles in QCD:

## i) hadron masses

- A proton is thought to be composed out of uud
- The proton mass is about  $938.3 \text{ MeV}/c^2$
- Sum of bare quark masses is only about  $12 \text{ MeV}/c^2$
- How is the extra mass generated?

Usually among the list of top most unsolved problems in physics  
([List of unsolved problems on wikipedia](#))

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## ii) confinement

- Nobody ever succeeded in detecting an isolated quark
- Instead, quarks seem to be confined within hadrons
- It looks like one half of the fundamental fermions are not directly observable.  
Why?

Usually among the list of top most unsolved problems in physics  
([List of unsolved problems on wikipedia](#))

# Quantum Chromo Dynamics (QCD)

14

Elementary fields:

Quarks

Gluons

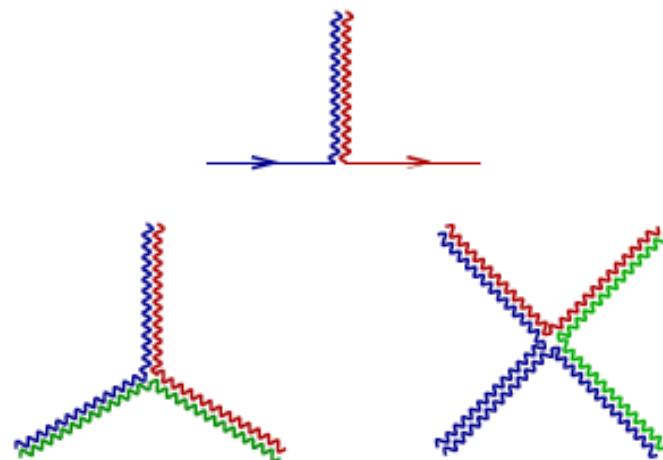
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Dynamics: Generalized Maxwell (Yang-Mills) + Dirac theory

$$\boxed{\mathcal{L} = \bar{q}_f (i \not{D} - m_f) q_f - \frac{1}{4} G_{\mu\nu}^a G_{\mu\nu}^a}$$

$$G_{\mu\nu}^a = \partial_\mu A_\nu^a - \partial_\nu A_\mu^a + g f^{abc} A_\mu^b A_\nu^c$$

$$i \not{D} q = \gamma^\mu (i \partial_\mu + g A_\mu^a t^a) q$$



# Quantum Chromo Dynamics (QCD)

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Same basic structure as  
QED (electro-magnetism) ...

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Gluons

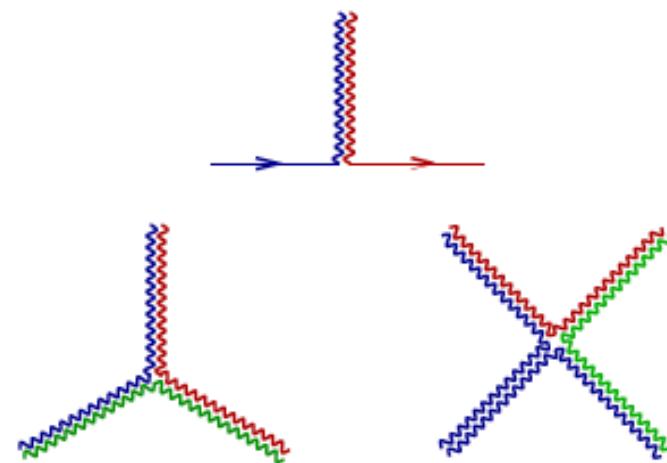
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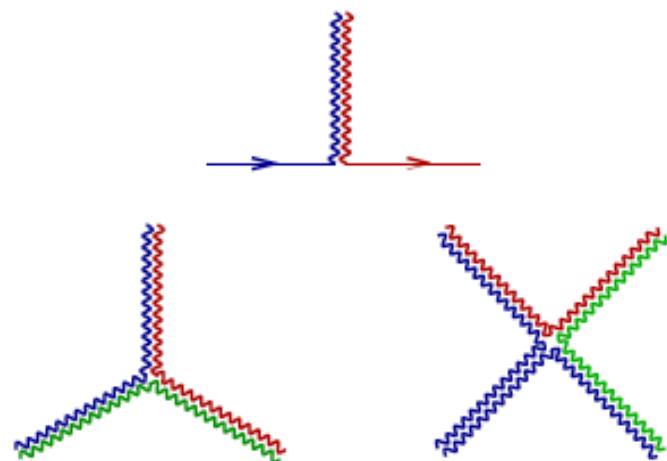
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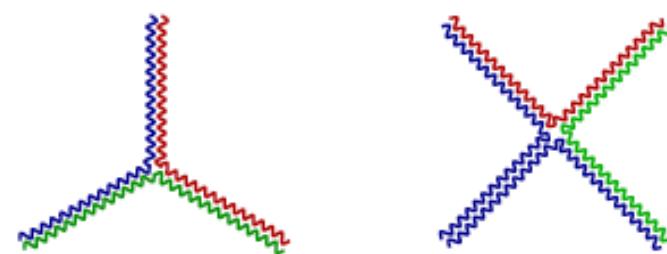
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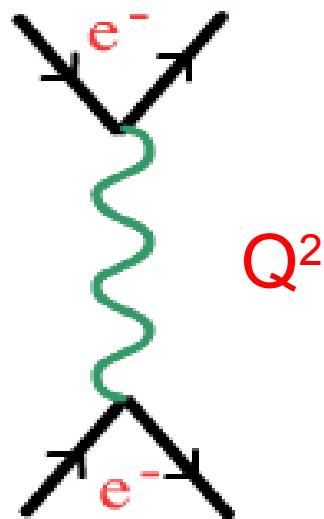
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$$A_\mu^a \left\{ \begin{array}{l} \text{color } a = 1, \dots, 8 \\ \text{spin } \epsilon_\mu^\pm \end{array} \right.$$

... so they interact also  
among themselves,  
generating much more  
complex structures



Consider the interaction of two elementary particles



Momentum transfer  $Q^2$ :  
Small  $Q^2 \Rightarrow$  large distance scales  
Large  $Q^2 \Rightarrow$  small distance scales

Quantum mechanics:  
Virtual pairs (loops) screen the bare interaction resulting in momentum-transfer dependent interaction strength

# “Running” of the coupling: QED vs QCD

19

$$\alpha \equiv \frac{g^2}{4\pi}$$

negative

$$\text{QED: } \alpha(Q^2) \approx \alpha(\mu^2) / \left( 1 - \frac{1}{3\pi} \alpha(\mu^2) \log \frac{|Q^2|}{\mu^2} \right)$$

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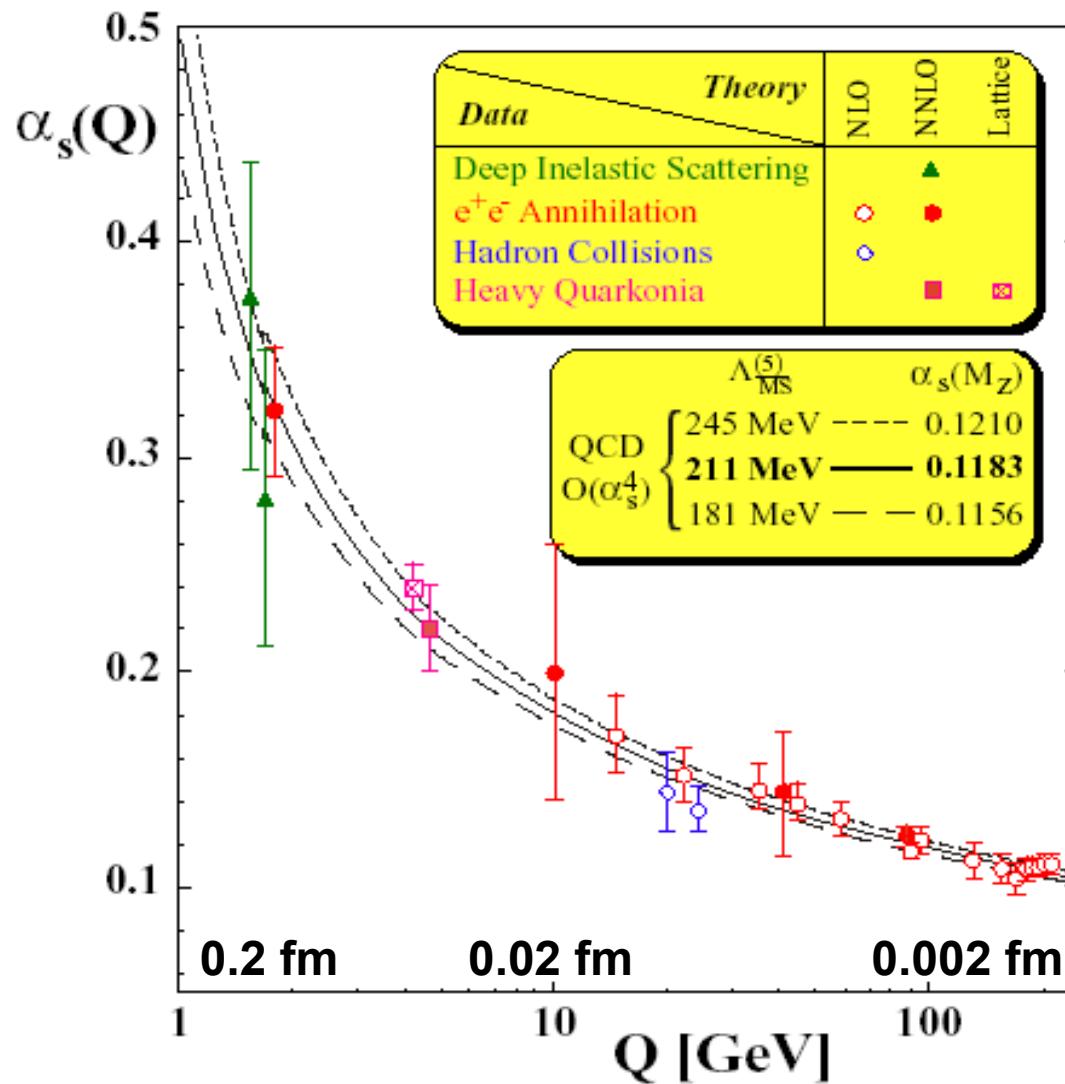
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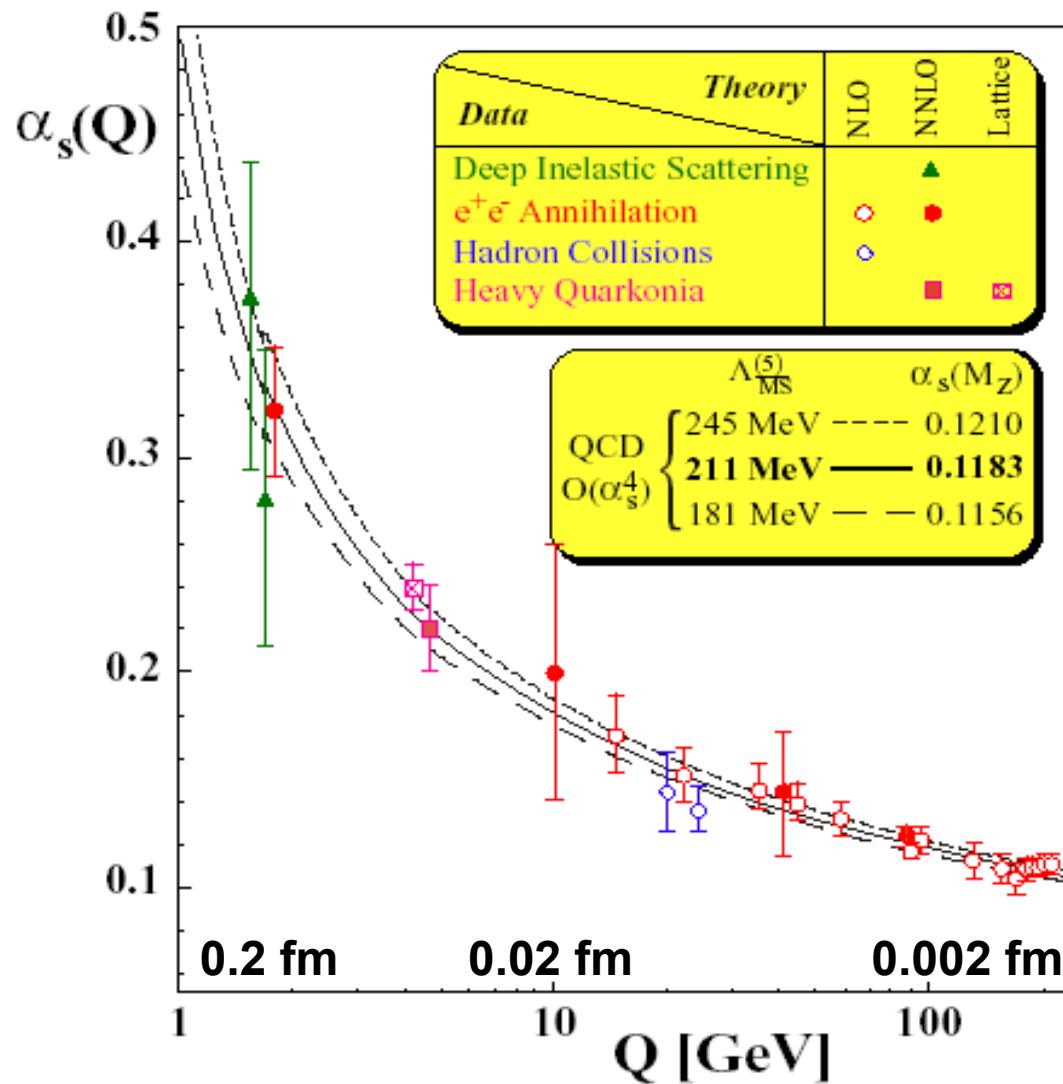
And that makes a huge difference!

# “Running” of the coupling: QCD

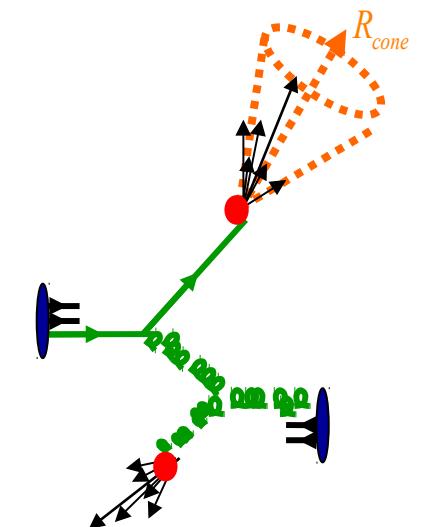


# “Running” of the coupling: QCD

23

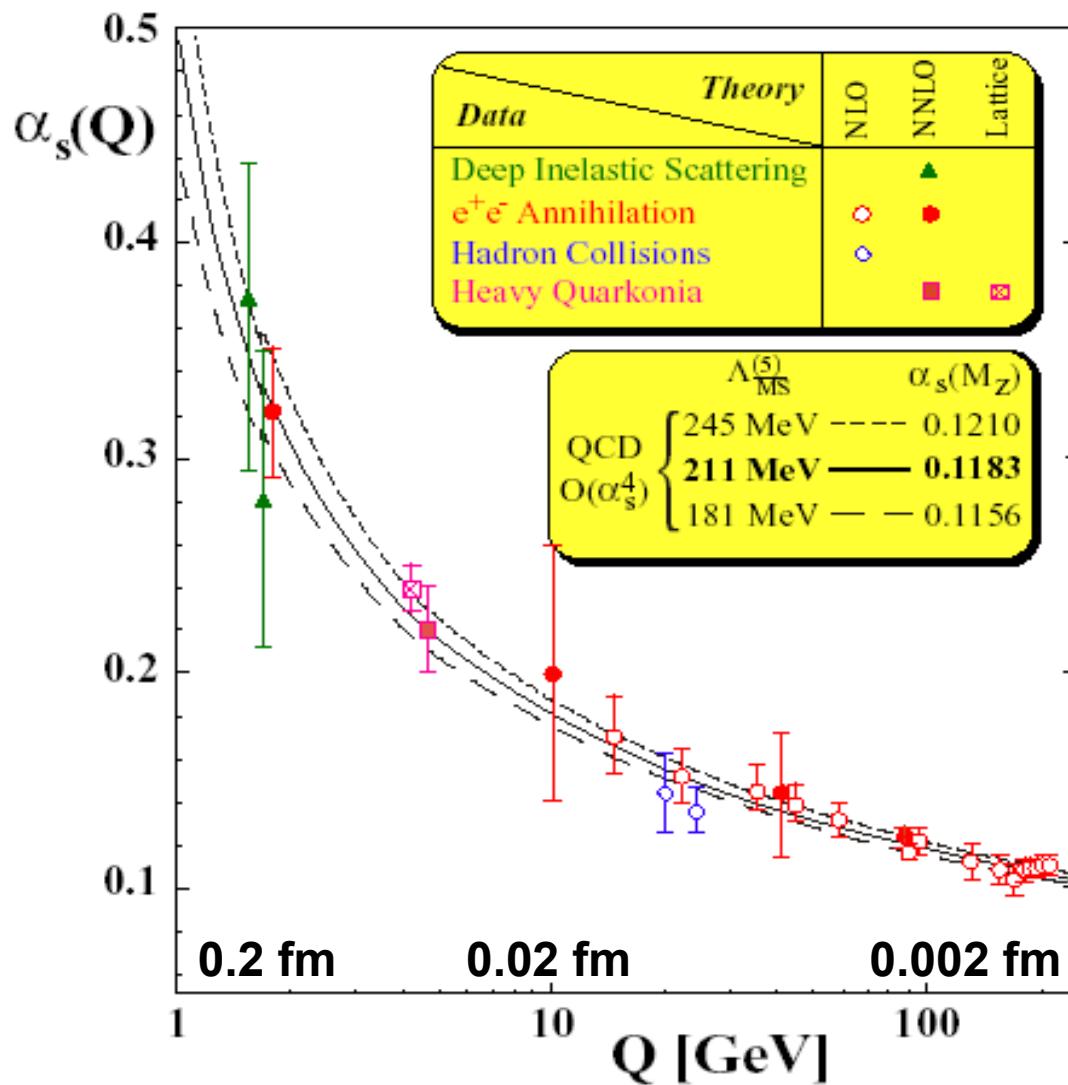
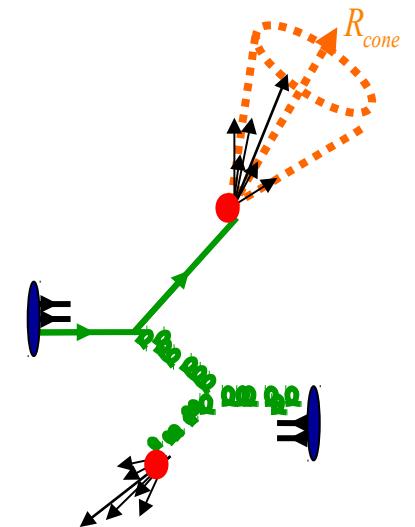


Asymptotic freedom



# “Running” of the coupling: QCD

Asymptotic freedom



2004  
Nobel  
Prize

PHYSICAL REVIEW D

VOLUME 8, NUMBER 10

15 NOVEMBER 1973

## Asymptotically Free Gauge Theories. I\*

David J. Gross†

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and Joseph Henry Laboratories, Princeton University, Princeton, New Jersey 08540



VOLUME 30, NUMBER 26

PHYSICAL REVIEW LETTERS

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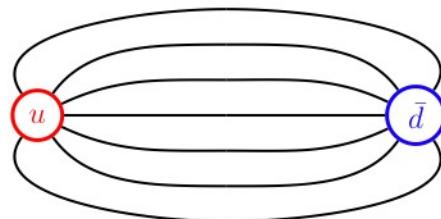
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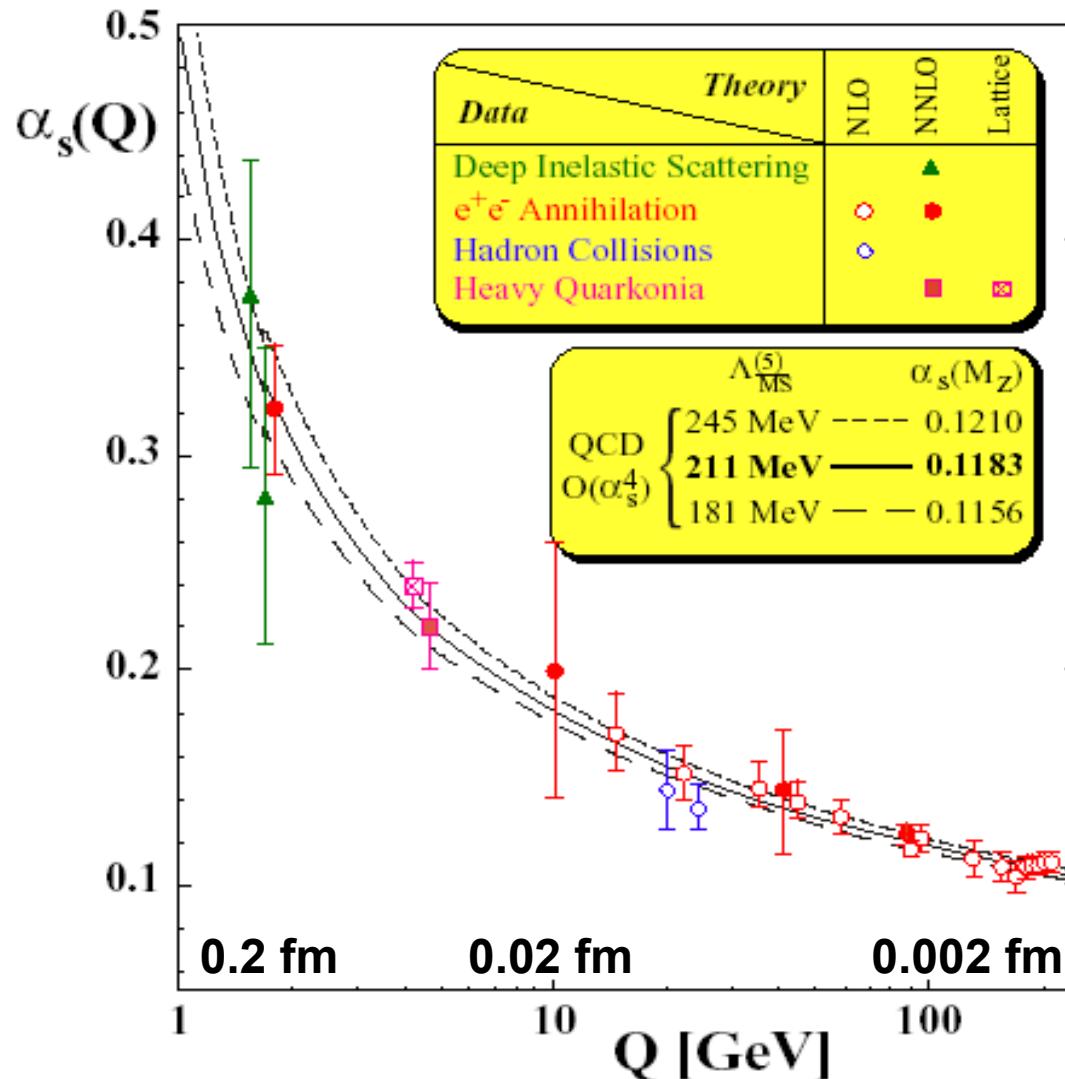
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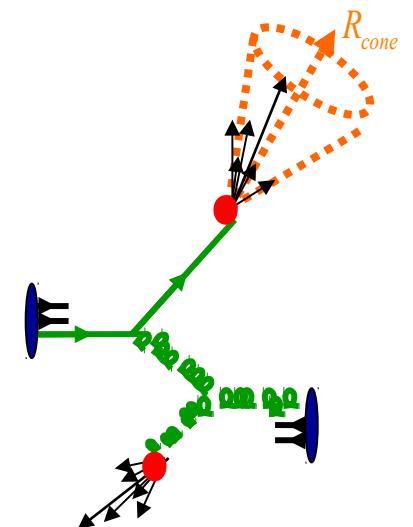
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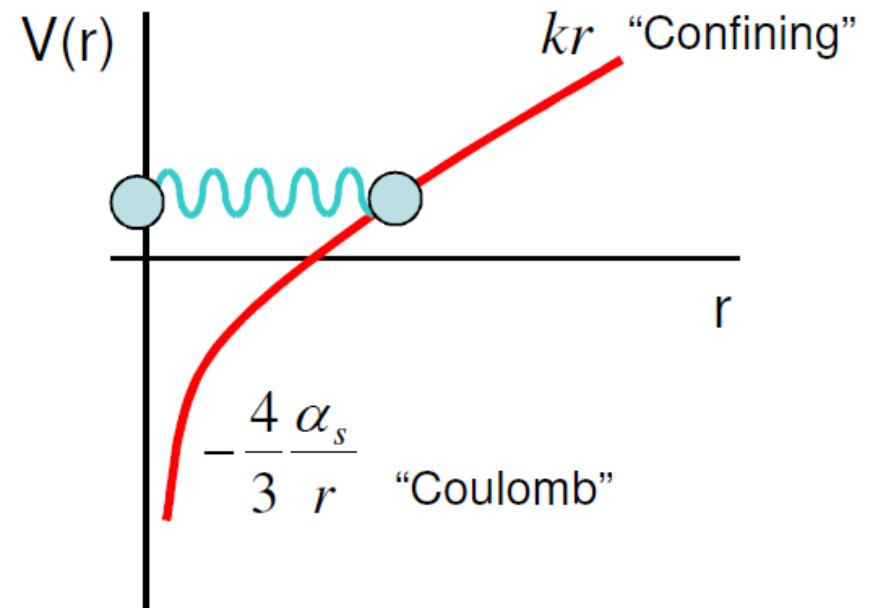


# Confinement

- The increase of the interaction strength (for a  $q\bar{q}$  pair) can be approximated by the Cornell potential

$$V(r) = -\frac{4}{3} \frac{\alpha_s}{r} + K r$$

- $Kr$  parametrizes the effects of confinement

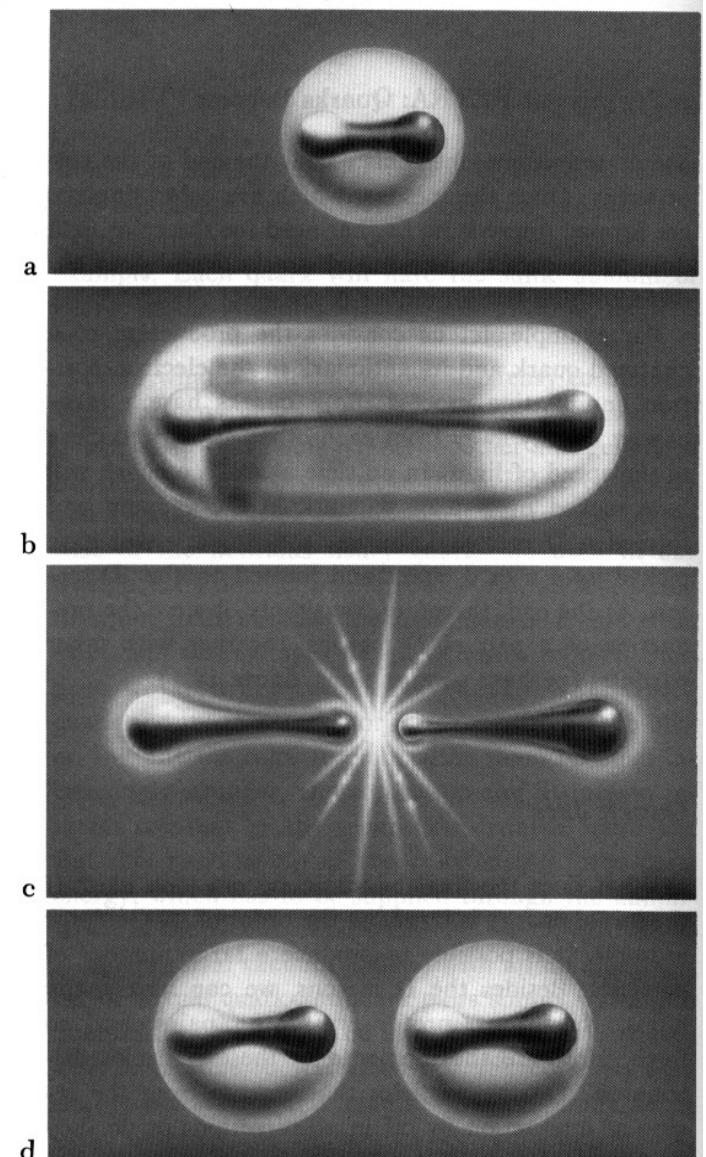


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- $Kr$  parametrizes the effects of confinement
- When  $r$  increases, the color field can be seen as a tube
- At large  $r$ , it becomes energetically favorable to convert the stored energy into a new  $q\bar{q}$  pair
- Confinement cannot be described perturbatively, but with lattice QCD or bag models inspired by QCD



(Illustration from Fritzsch)

# QCD deconfinement phase transition

# Deconfinement phase transition

29

- Since the interactions between quarks and gluons become weaker at small distances, it might be possible to create a deconfined phase of matter composed out of a large number of free quarks and gluons
- First ideas in the mid 1970's

Experimental hadronic spectrum  
and quark liberation

Cabibbo and Parisi, PLB59 (1975) 67

Superdense matter: Neutrons or  
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Collins and Perry, PRL 34 (1975) 1353

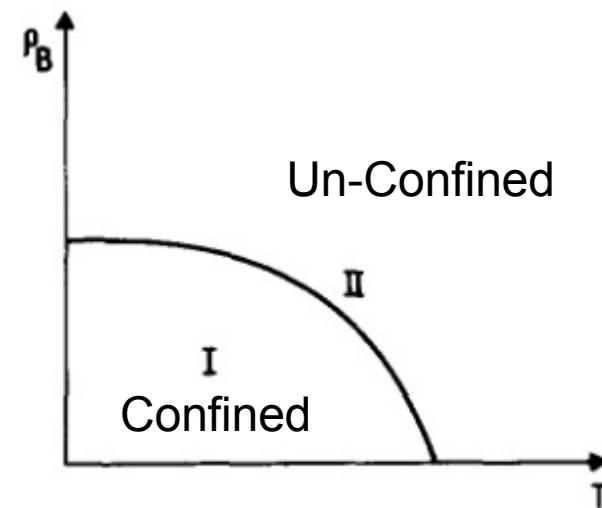


Fig. 1. Schematic phase diagram of hadronic matter.  $\rho_B$  is the density of baryonic number. Quarks are confined in phase I and unconfined in phase II.

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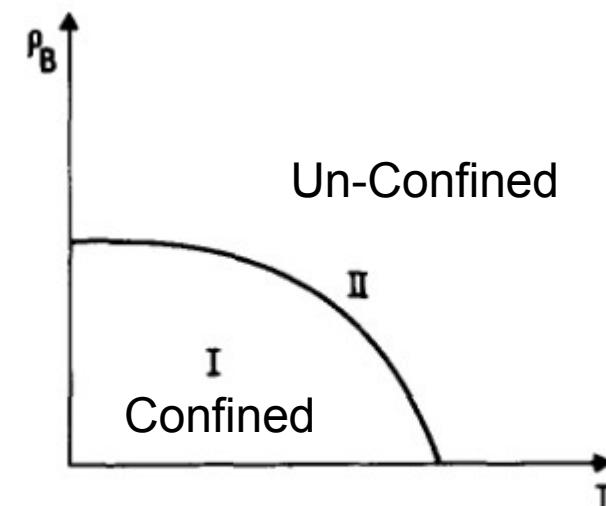


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Phase transition  
at large  $T$



We expect models of this kind to give rise to a phase transition at a temperature  $kT \approx m_\pi$ , the high temperature phase being one where quarks can move freely in space.

# Deconfinement phase transition

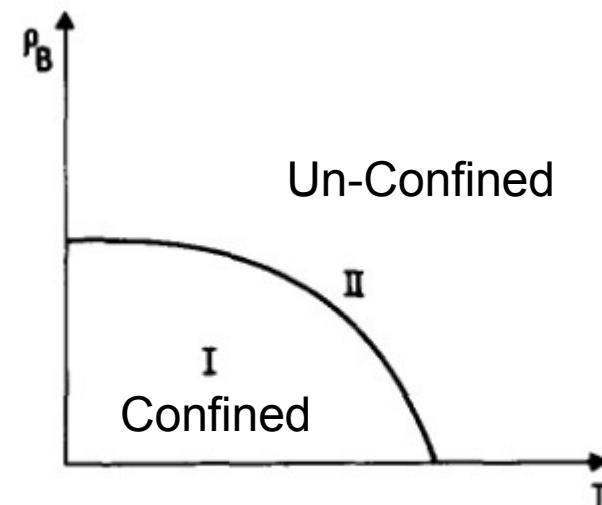
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We expect the same transition to be also present at low temperature but high pressure, for the same reason, i.e. we expect a phase diagram of the kind indicated in fig. 1.

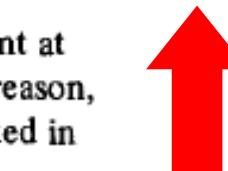


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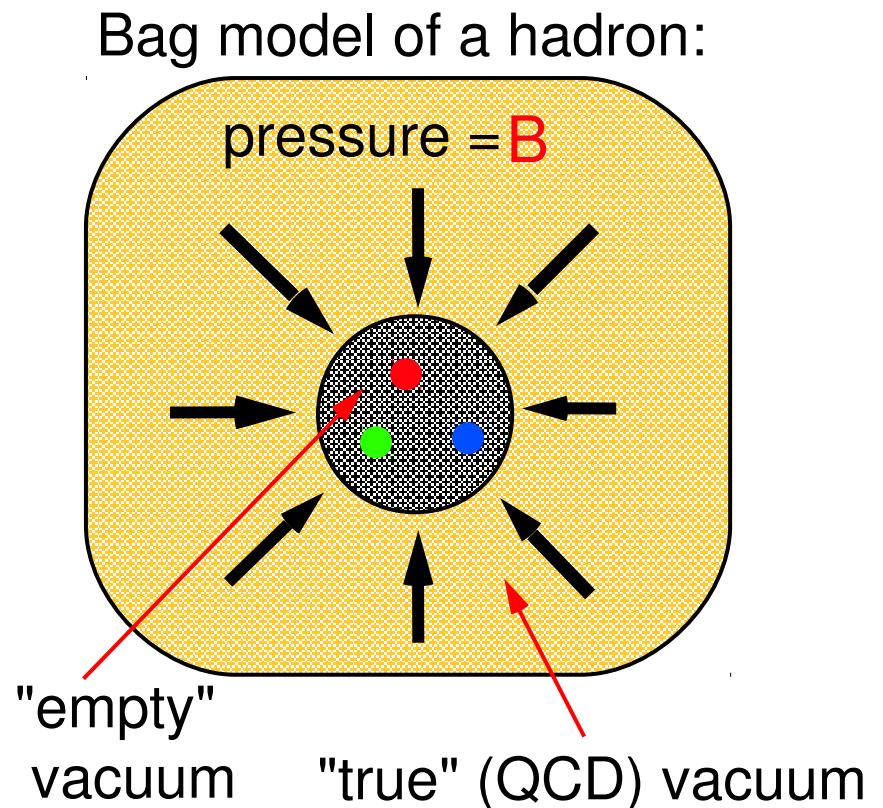
Phase transition  
at large  $T$  and/or  $\rho_B$



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# The MIT Bag model

- The MIT bag model assumes that quarks are confined within bags of perturbative (empty) vacuum of radius  $R$ , in which they are free to move
- The QCD (true) vacuum creates a confining bag pressure  $B$
- The bag constant is obtained by balancing the vacuum with the kinetic pressure of the quarks
  - By minimizing
$$E \approx \frac{2N}{R} + \frac{4}{3}\pi R^3 B$$
- $B \approx (200 \text{ MeV})^4 = 0.2 \text{ GeV/fm}^3$   
with  $N=3$  quarks in  $R=0.8\text{fm}$



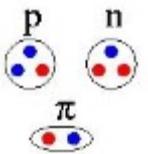
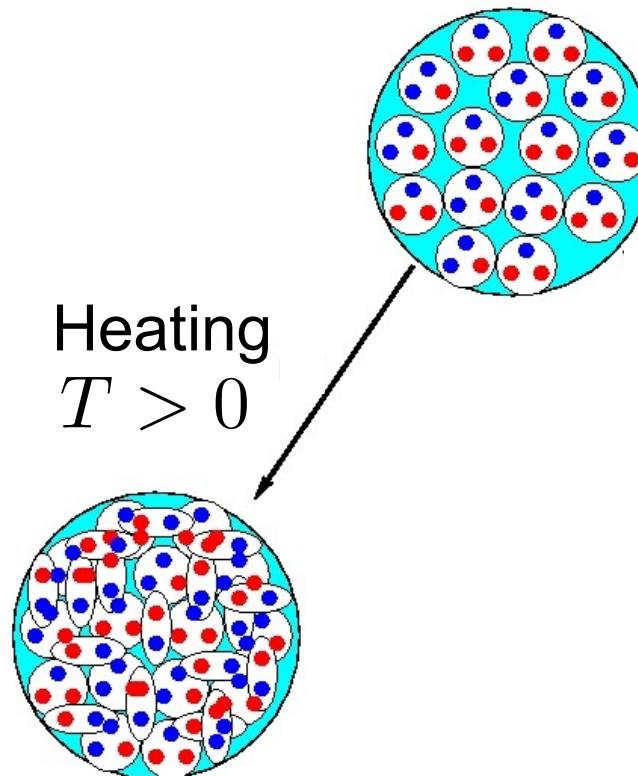
$B = \text{"bag constant"} \quad B \approx 0.2 \text{ GeV/fm}^3$

# Deconfinement: A toy model

- Heat matter so much that individual hadrons start to overlap
- From statistical mechanics for an ideal gas

$$p = \frac{\epsilon}{3} = \left( g_B + \frac{7}{8} g_F \right) \frac{\pi^2 T^4}{90}$$

$$g_B = 0, \quad g_F = 2$$



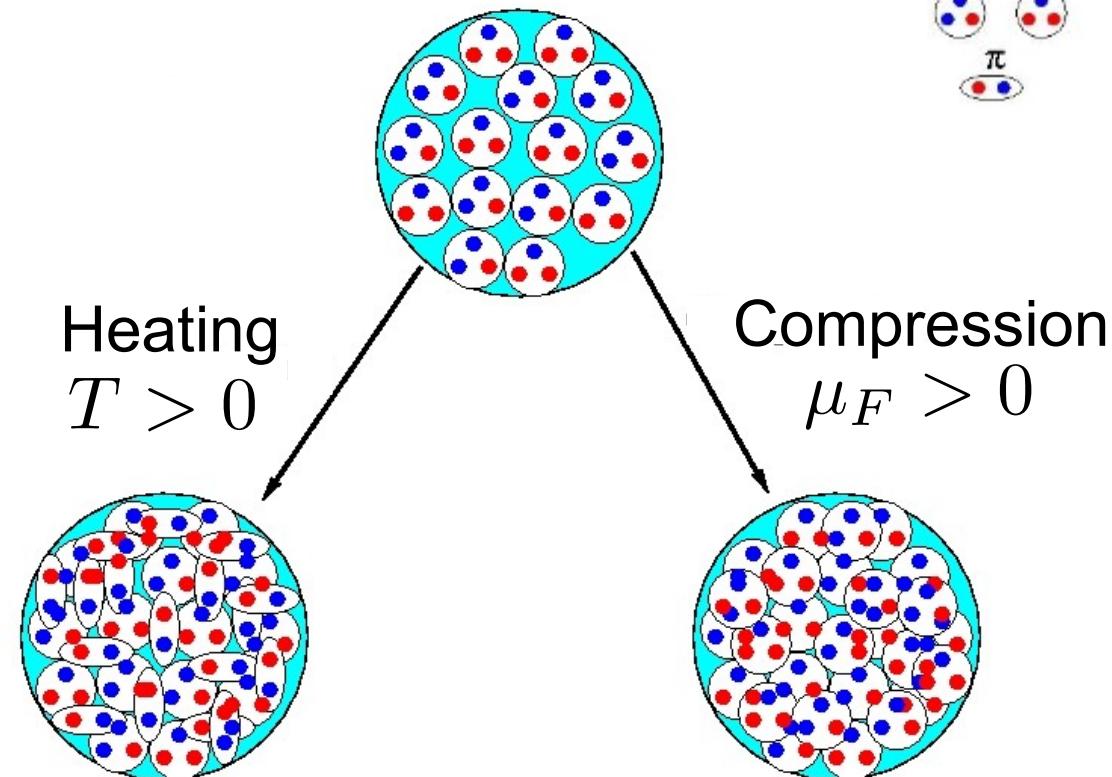
B=Boson  
F=Fermion

# Deconfinement: A toy model

- Heat or compress matter so much that individual hadrons start to overlap
- From statistical mechanics for an ideal gas

$$p = \frac{\epsilon}{3} = \left( g_B + \frac{7}{8}g_F \right) \frac{\pi^2 T^4}{90} + g_F \left( \frac{\mu_F^2 T^2}{12} + \frac{\mu_F^4}{24\pi^2} \right)$$

$$g_B = 0, \quad g_F = 2$$



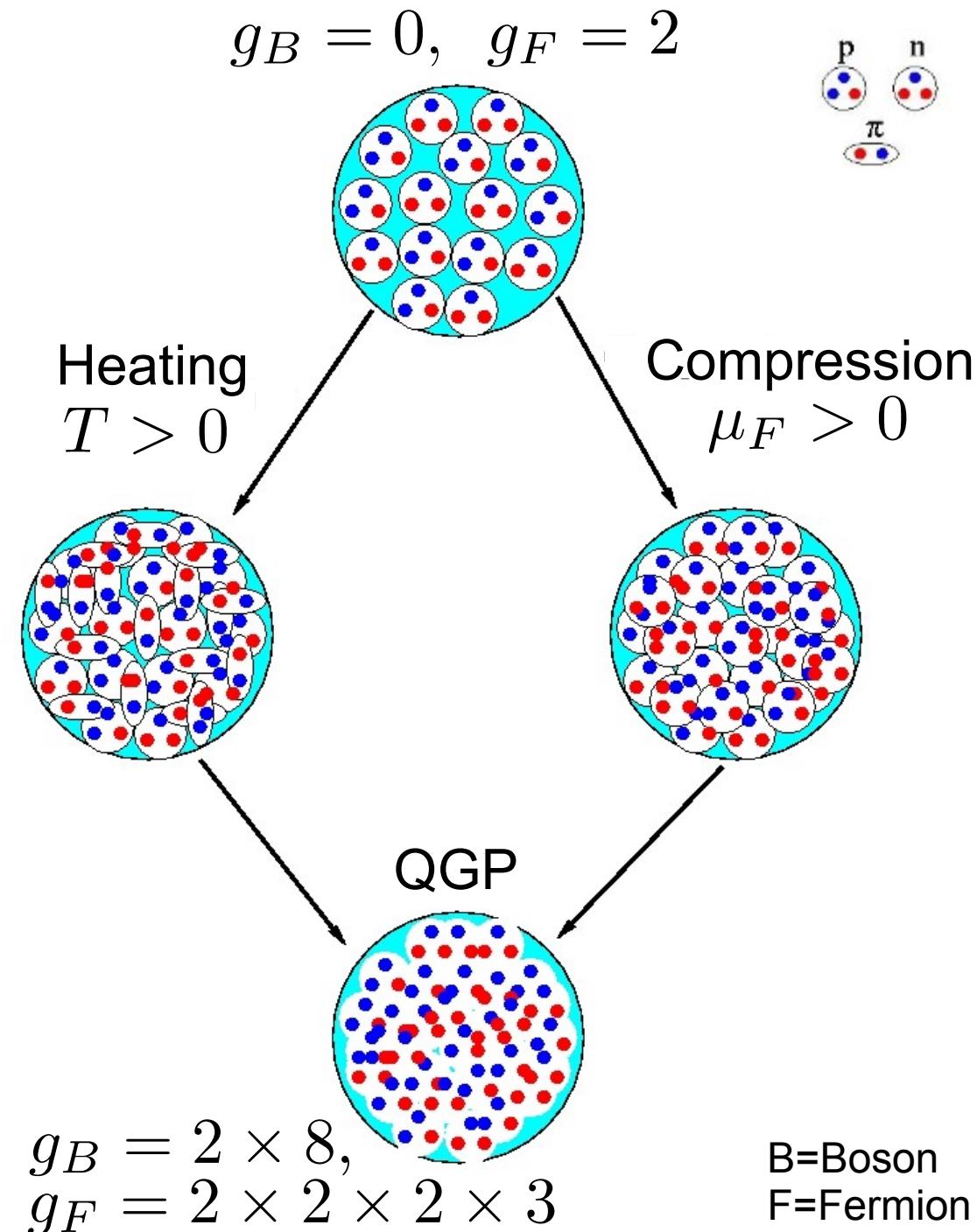
B=Boson  
F=Fermion

# Deconfinement: A toy model

35

- Heat or compress matter so much that individual hadrons start to overlap
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$$p = \frac{\epsilon}{3} = \left( g_B + \frac{7}{8} g_F \right) \frac{\pi^2 T^4}{90} + g_F \left( \frac{\mu_F^2 T^2}{12} + \frac{\mu_F^4}{24\pi^2} \right)$$



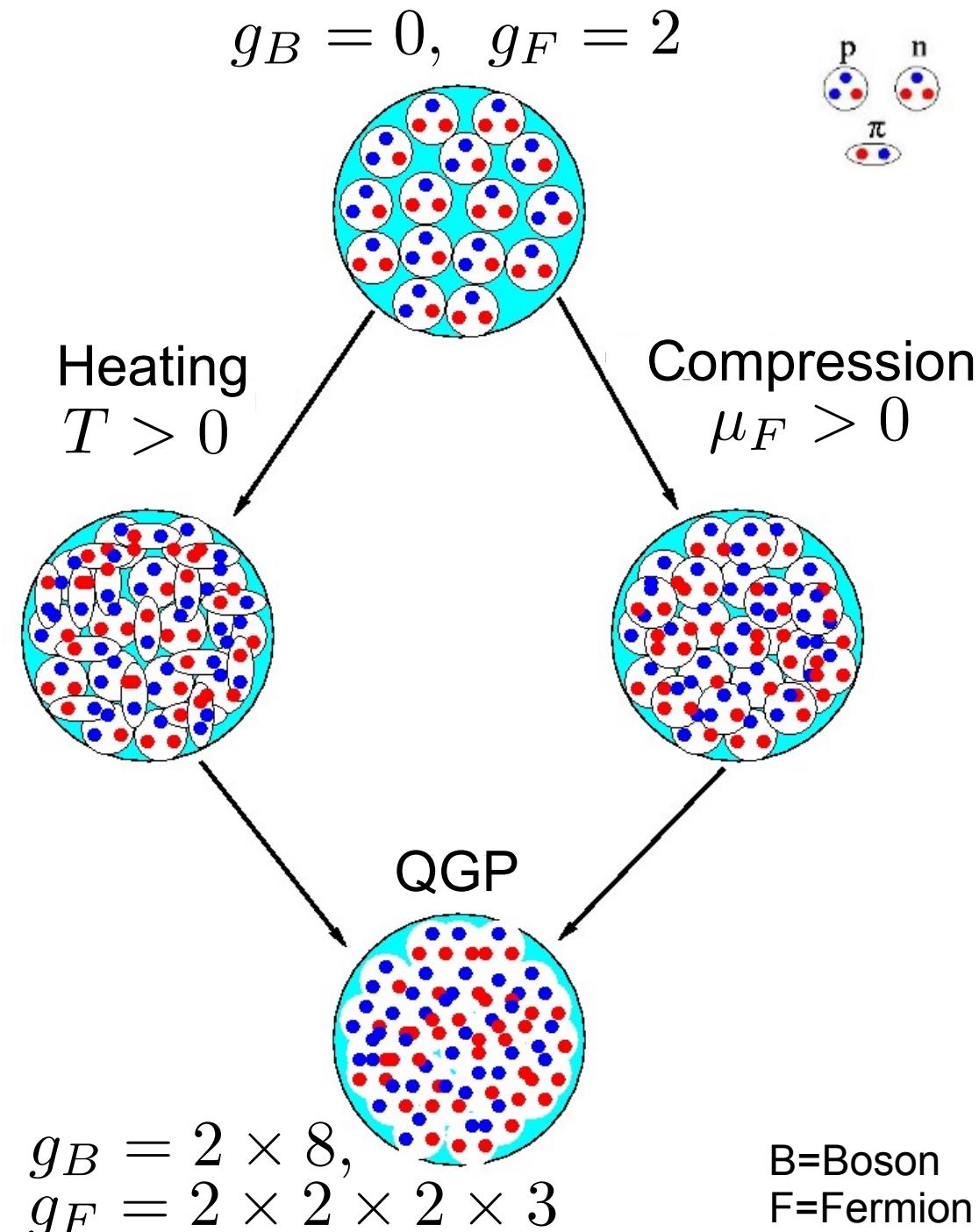
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- Condition for QGP: Pressure  $\geq B$

$$p = \frac{\epsilon}{3} \stackrel{!}{=} B \Rightarrow T_c(\mu_F)$$

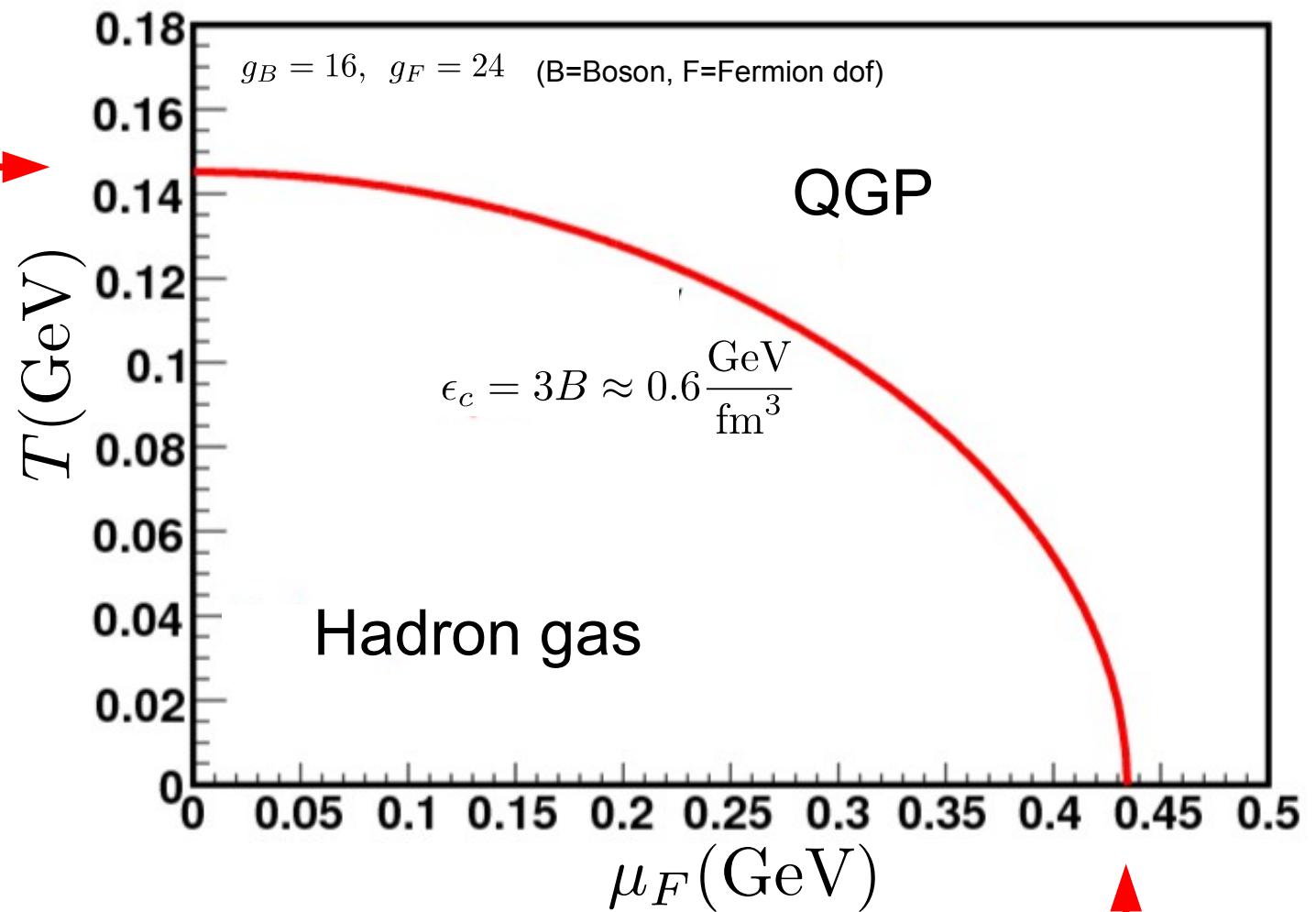


# Phase diagram of non-interacting QGP

37

$$T_c \approx 2 \cdot 10^{12} \text{ K}$$

( $10^5$  times core of sun)



- Condition for QGP:  
Pressure  $\geq B$

$$p = \frac{\epsilon}{3} \stackrel{!}{=} B \Rightarrow T_c(\mu_F)$$

(see Reygers and Schweda)

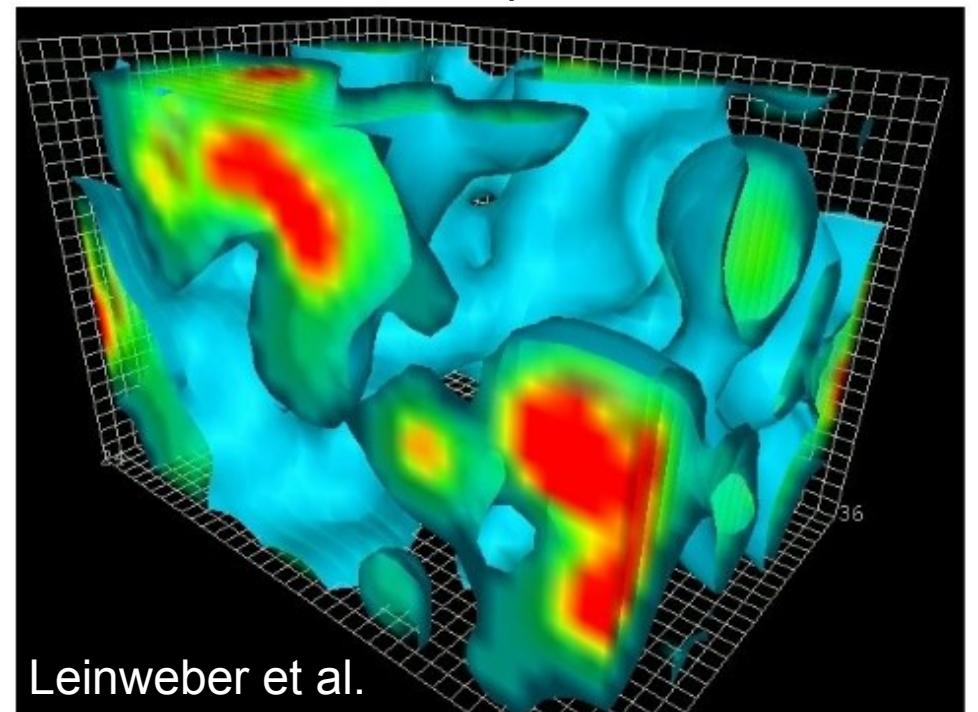
$n_c^B = 0.72 \text{ fm}^{-3}$   
(net-baryon density of about 5 x nucleus)

# Lattice QCD

# Lattice QCD

- As QCD is asymptotically free at small distances, cannot use perturbation theory to calculate properties of e.g. hadrons
- Instead solve QCD numerically by putting fields on a space-time lattice (lattice QCD)
- First principle non-perturbative calculation
- Computationally demanding as lattice needs to be big, e.g.  $16^3 \times 32$

Snapshot of fluctuating quark and gluon fields on a discrete space-time lattice



JUGENE in Jülich  
(294,912 cores,  $\sim 1$  PetaFLOPSS)



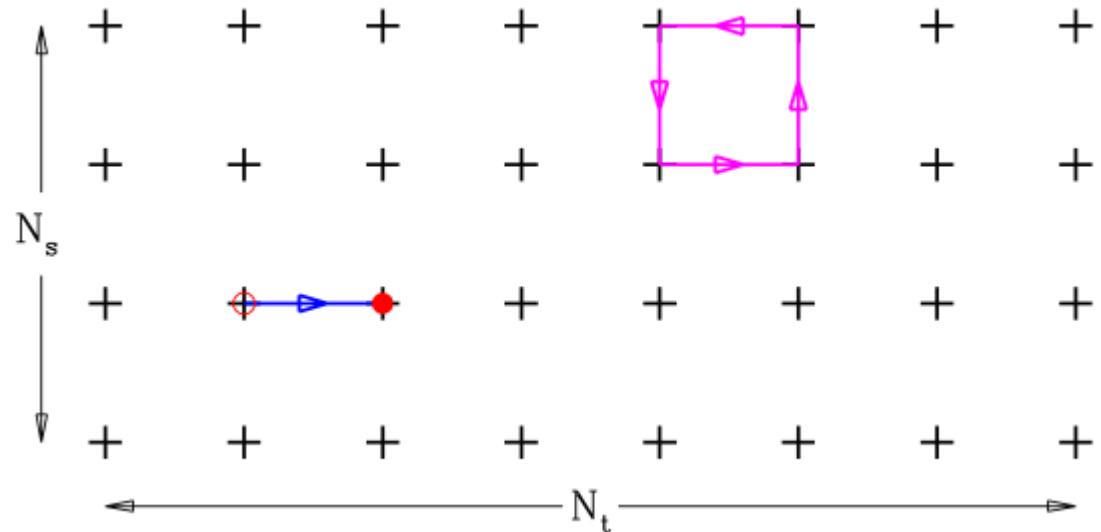
Leinweber et al.

# Lattice QCD: the approach

- Solve path integrals numerically in discretized Euclidean space-time

$$e^{iS} \rightarrow e^{-S_E}$$

Lattice spacing  $a$ ,  $a^{-1} \sim \Lambda_{\text{UV}}$ ,  $x_\mu = n_\mu a$   
 Finite volume  $L^3 \cdot T$ ,  $N_s = L/a$ ,  $N_t = T/a$



(anti)quarks:  $\psi(x), \bar{\psi}(x)$   
 gluons:  $U_\mu(x) = e^{aA_\mu(x)} \in \text{SU}(3)$   
 field tensor:  $P_{\mu\nu}(x) = U_\mu(x)U_\nu(x + a\hat{\mu})$   
 $U_\mu^\dagger(x + a\hat{\nu})U_\nu^\dagger(x)$

$$S[U, \bar{\psi}, \psi] = S_G[U] + S_F[U, \bar{\psi}, \psi]$$

(see, e.g. Wittig)

# Lattice QCD: the approach

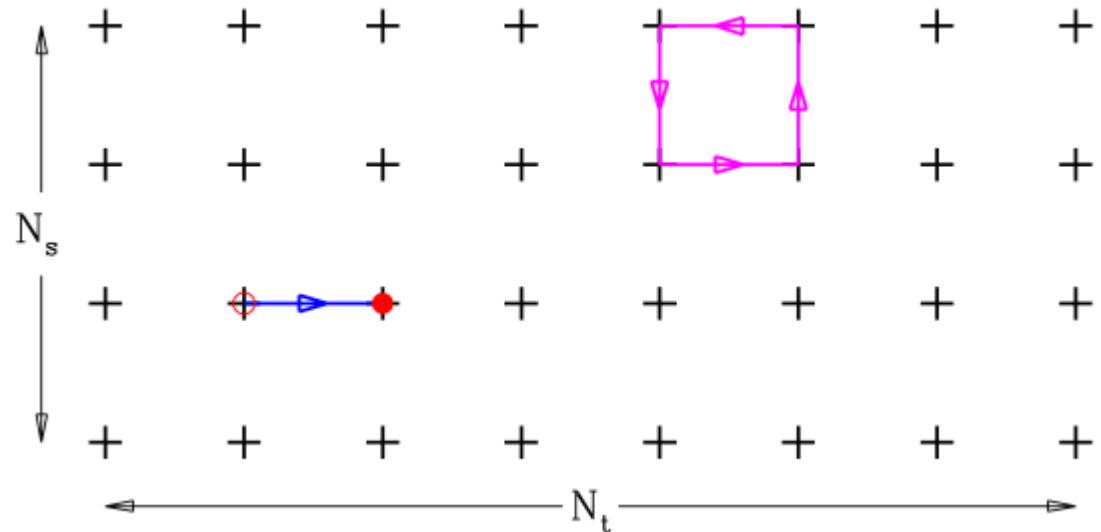
- Solve path integrals numerically in discretized Euclidean space-time

$$e^{iS} \rightarrow e^{-S_E}$$

- Physical results

- Continuum limit ( $a \rightarrow 0$ )
- Infinite volume limit ( $V \rightarrow \infty$ )
- Set scale(s) using data  
e.g. hadron mass(es)

Lattice spacing  $a$ ,  $a^{-1} \sim \Lambda_{\text{UV}}$ ,  $x_\mu = n_\mu a$   
 Finite volume  $L^3 \cdot T$ ,  $N_s = L/a$ ,  $N_t = T/a$



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# Lattice QCD: the approach

42

- Solve path integrals numerically in discretized Euclidean space-time

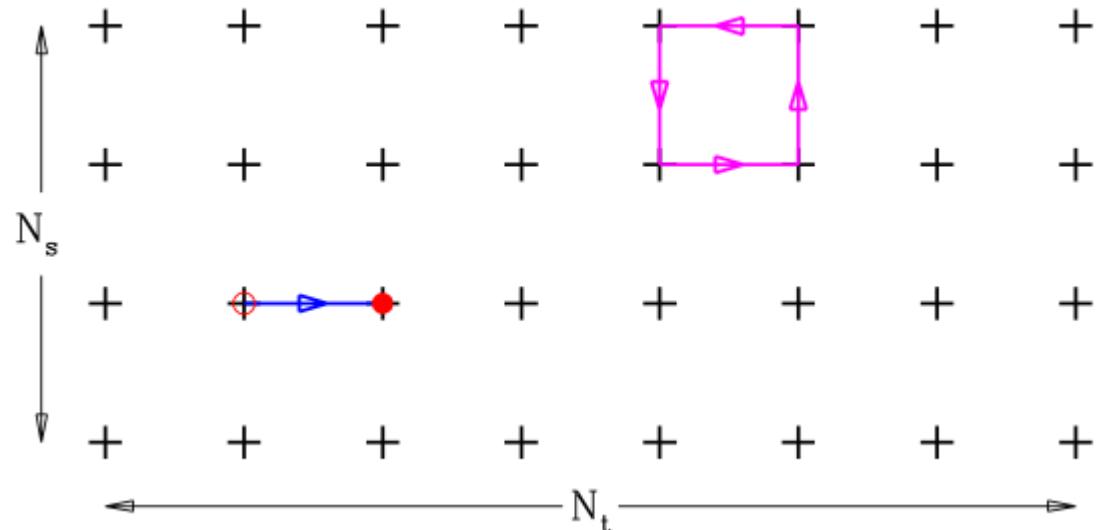
$$e^{iS} \rightarrow e^{-S_E}$$

- Physical results

- Continuum limit ( $a \rightarrow 0$ )
- Infinite volume limit ( $V \rightarrow \infty$ )
- Set scale(s) using data  
e.g. hadron mass(es)

- Problems of approach
  - Fermion doubling
  - Small physical quark masses computationally demanding
  - Sign problem for finite  $\mu$

Lattice spacing  $a$ ,  $a^{-1} \sim \Lambda_{\text{UV}}$ ,  $x_\mu = n_\mu a$   
 Finite volume  $L^3 \cdot T$ ,  $N_s = L/a$ ,  $N_t = T/a$



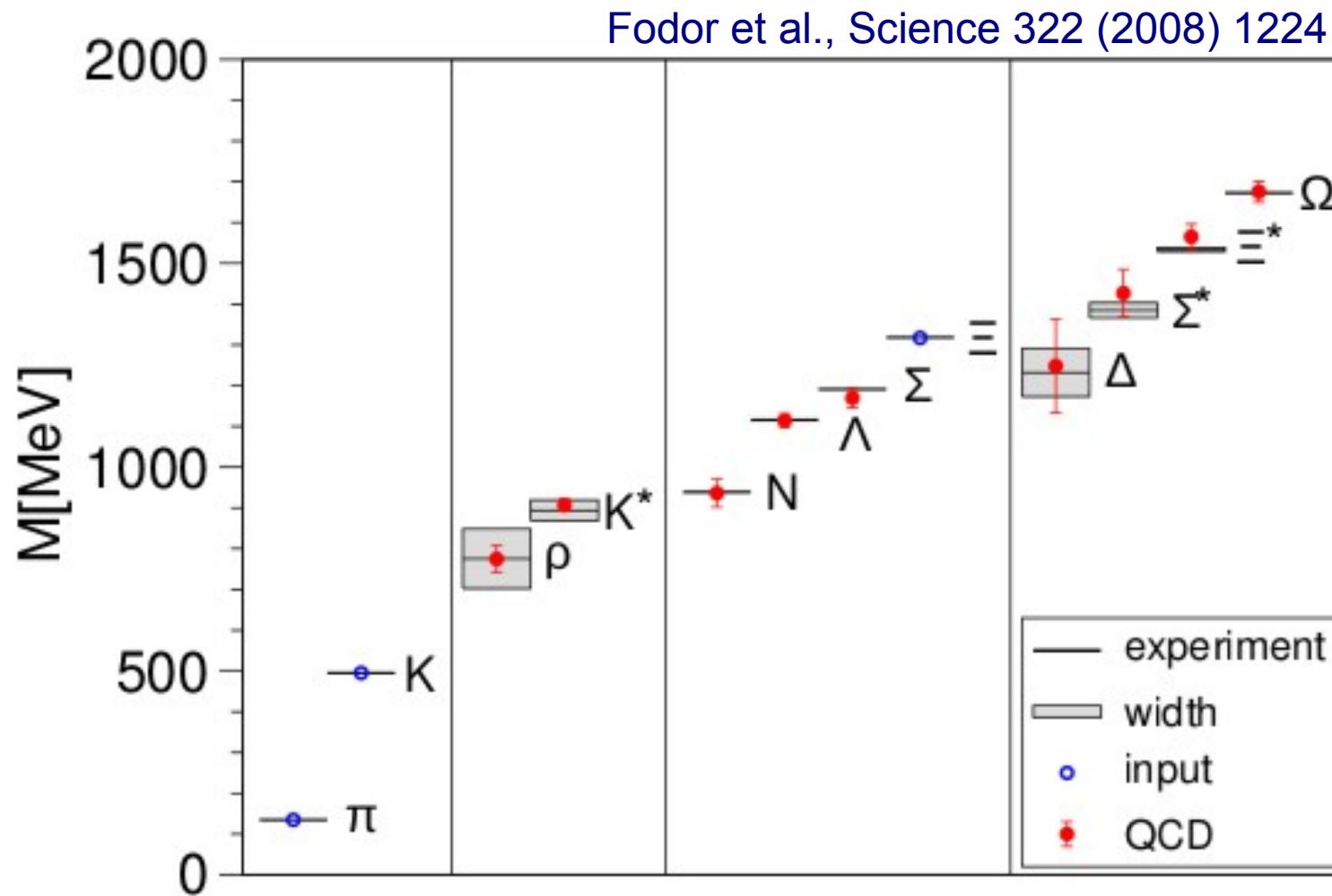
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$$S[U, \bar{\psi}, \psi] = S_G[U] + S_F[U, \bar{\psi}, \psi]$$

(see, e.g. Wittig)

# Lattice QCD: hadron spectrum

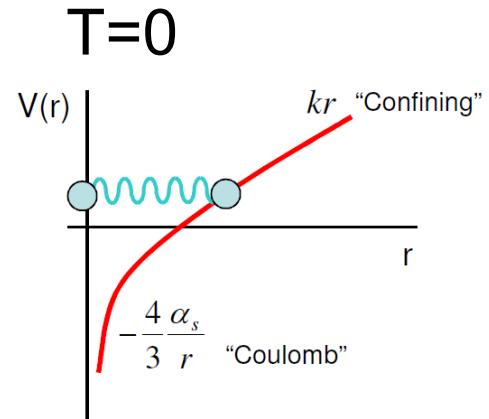
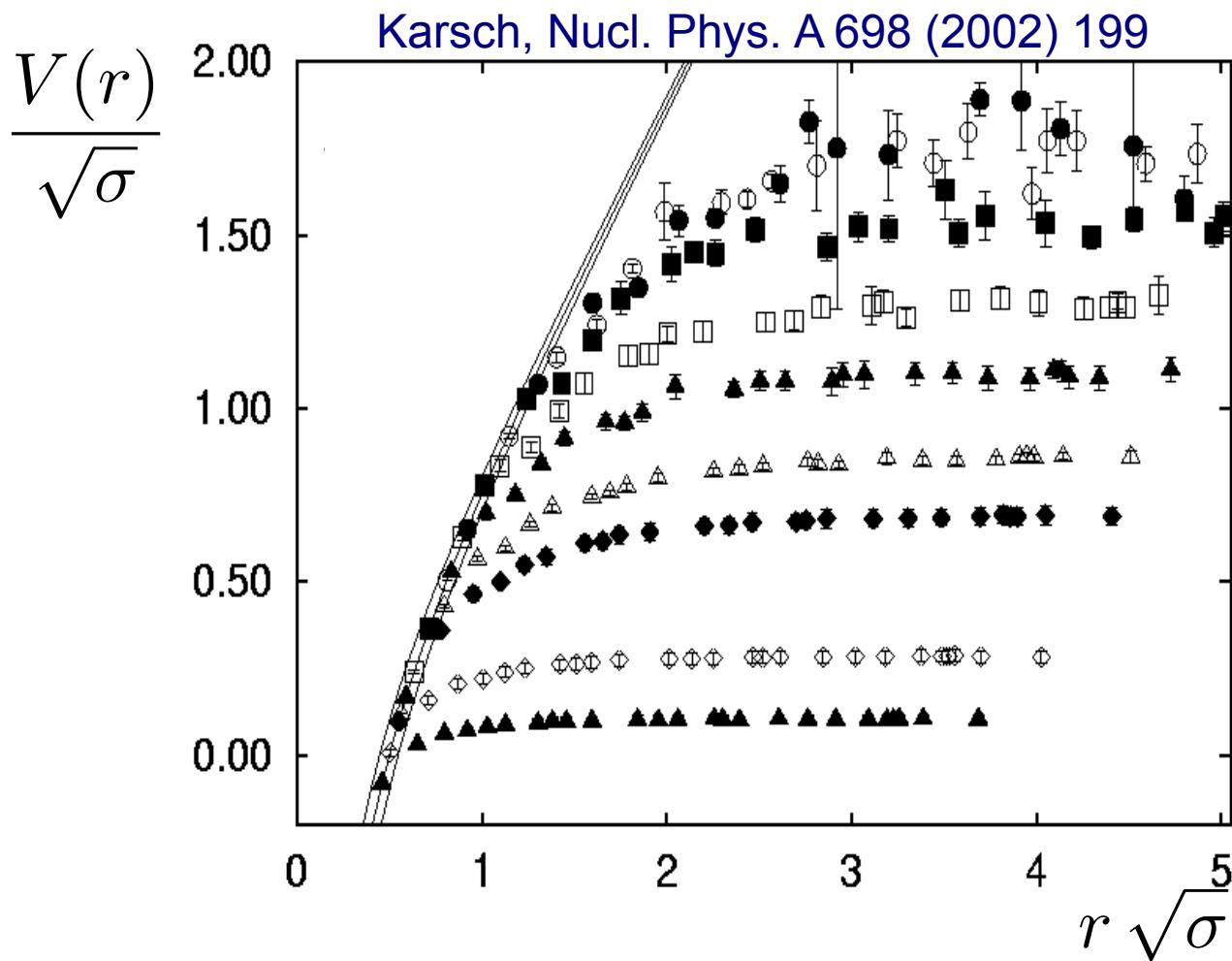
43



Full calculation using 2 quark flavors  
in excellent agreement with experimental data

# Lattice QCD: Static potential

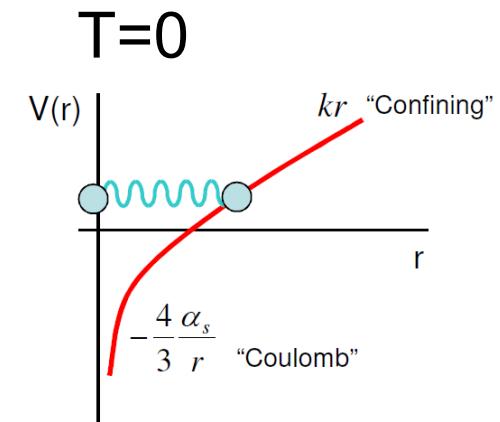
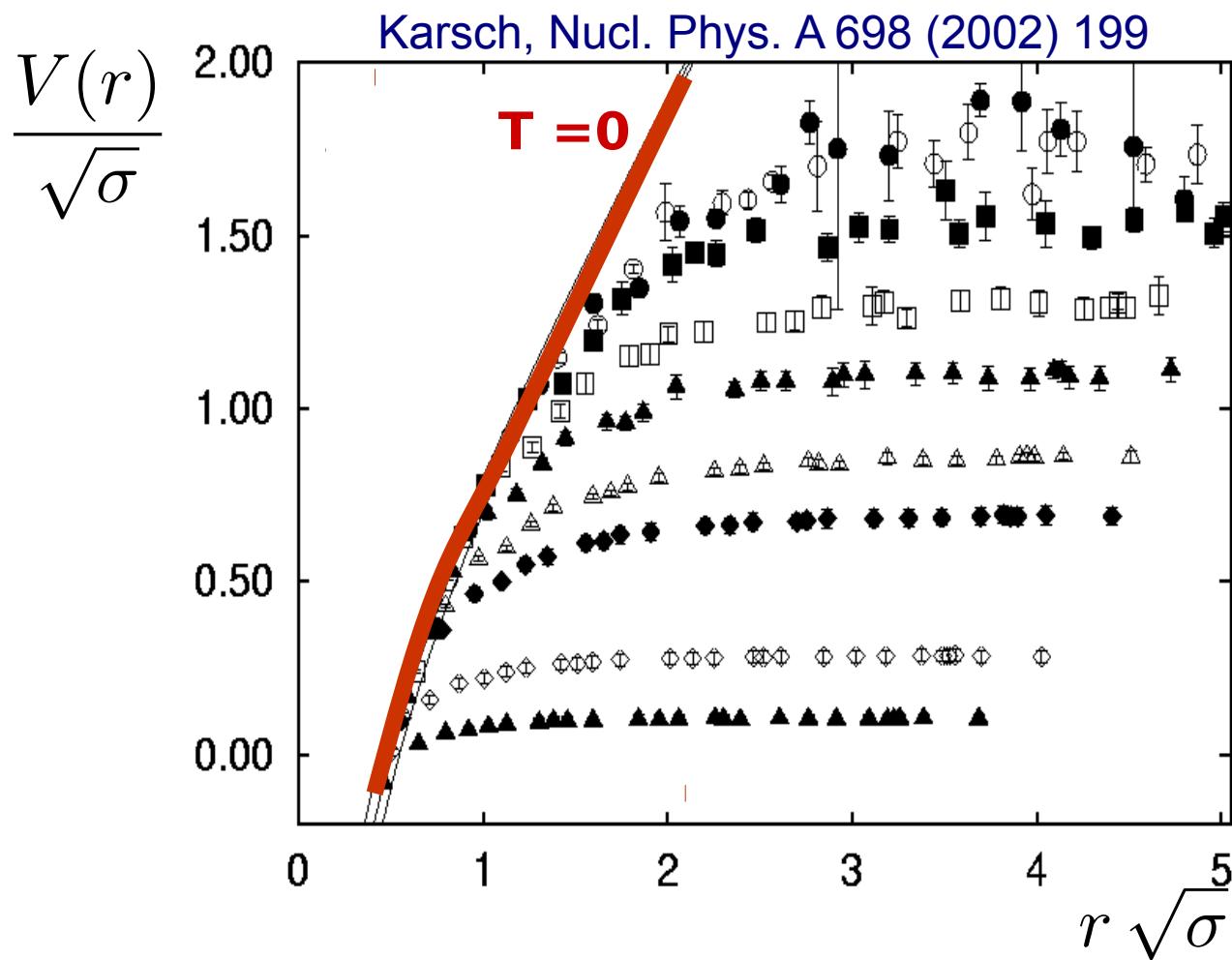
44



Lattice calculation (for a heavy quark pair) exhibits screening of long range confining potential with increasing temperature

# Lattice QCD: Static potential

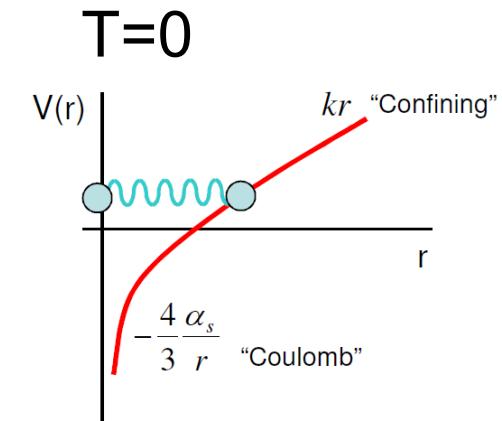
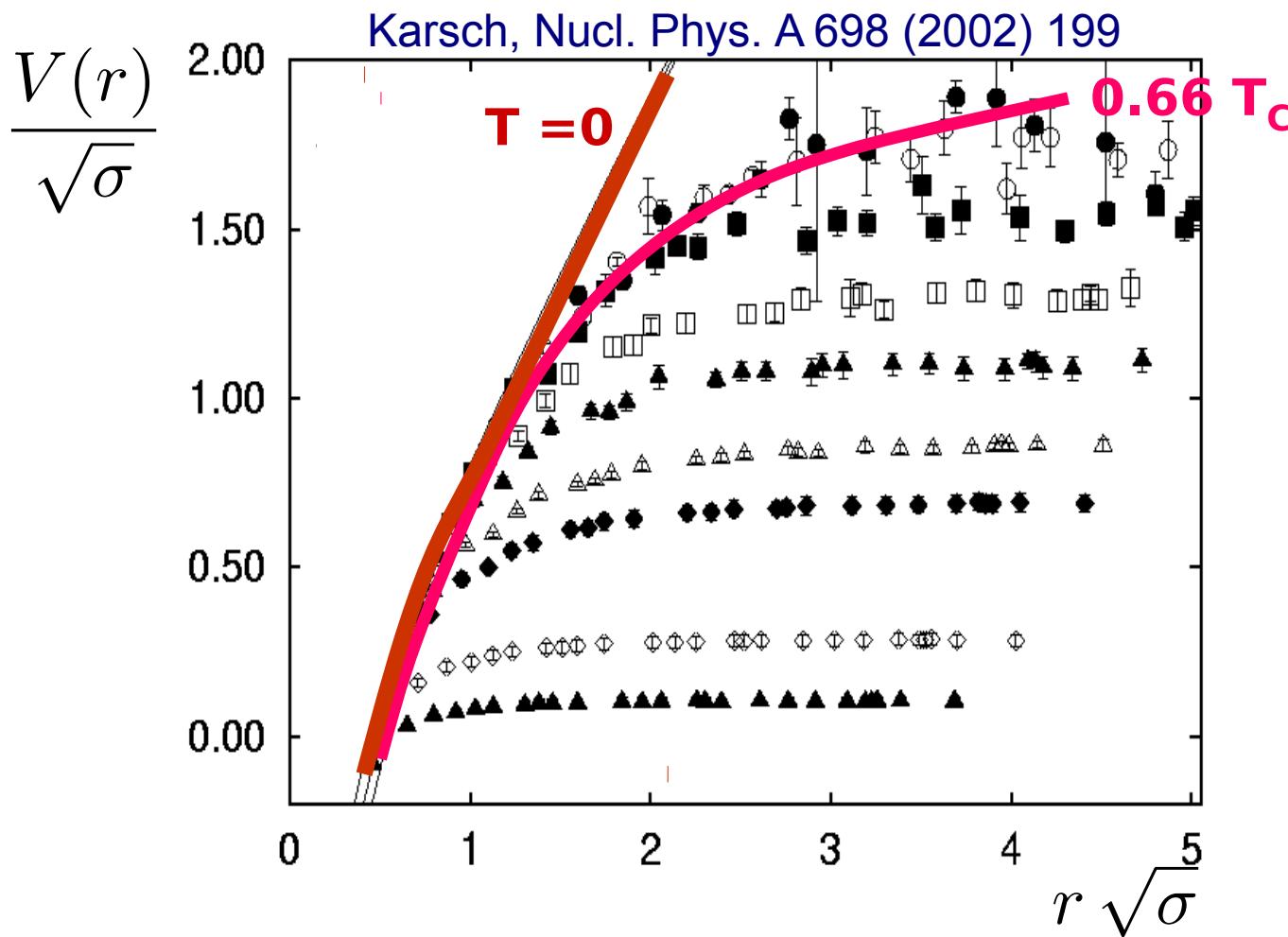
45



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# Lattice QCD: Static potential

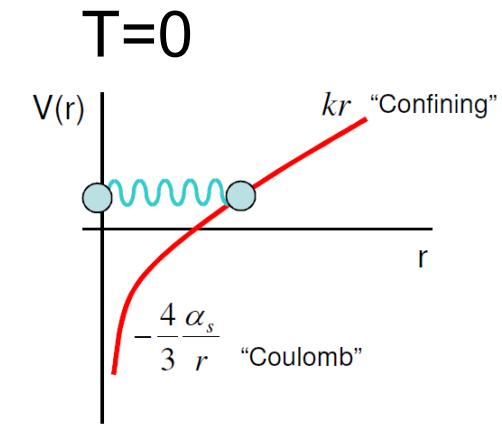
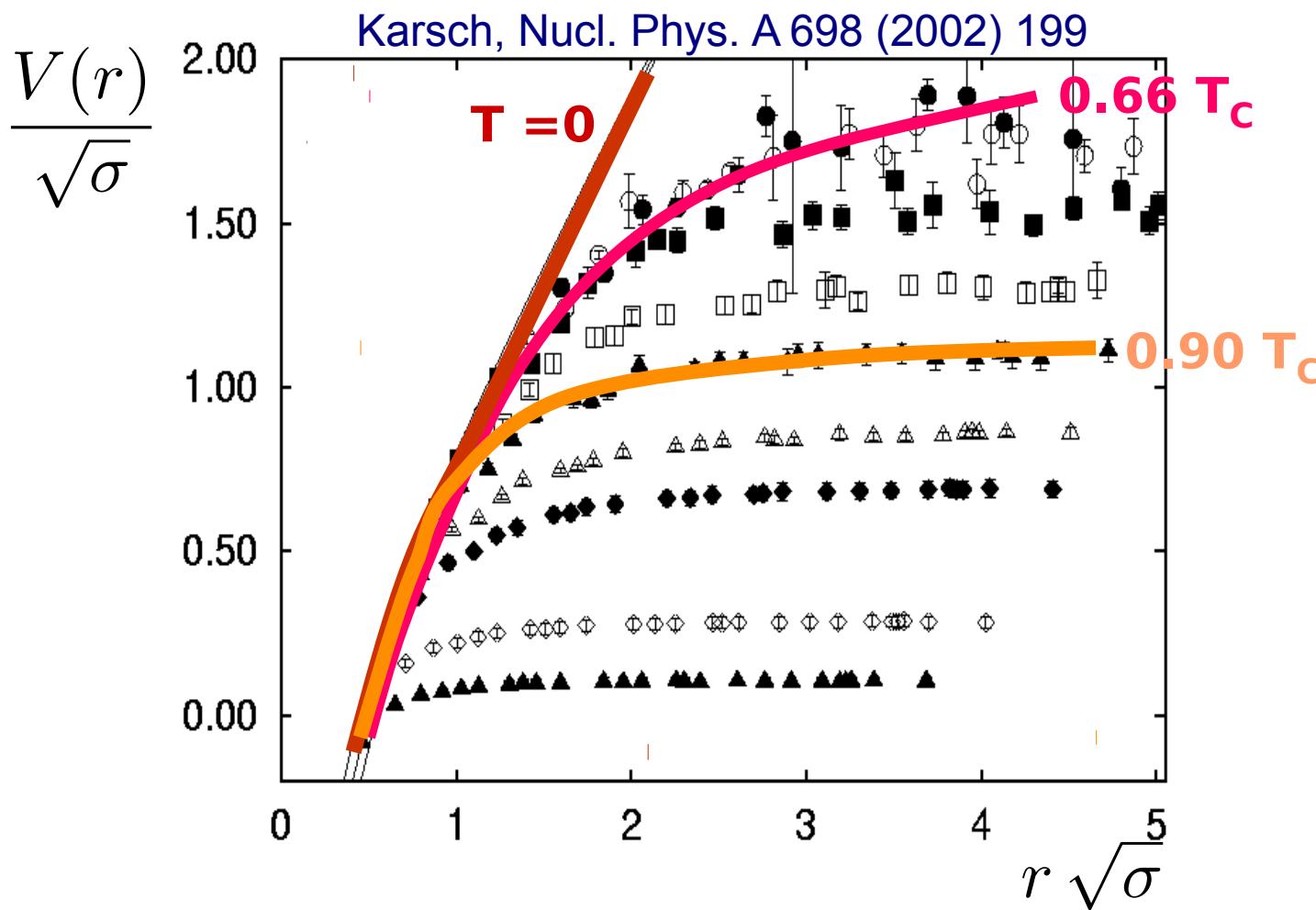
46



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# Lattice QCD: Static potential

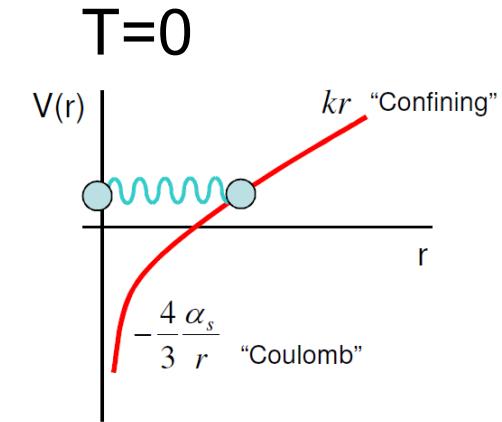
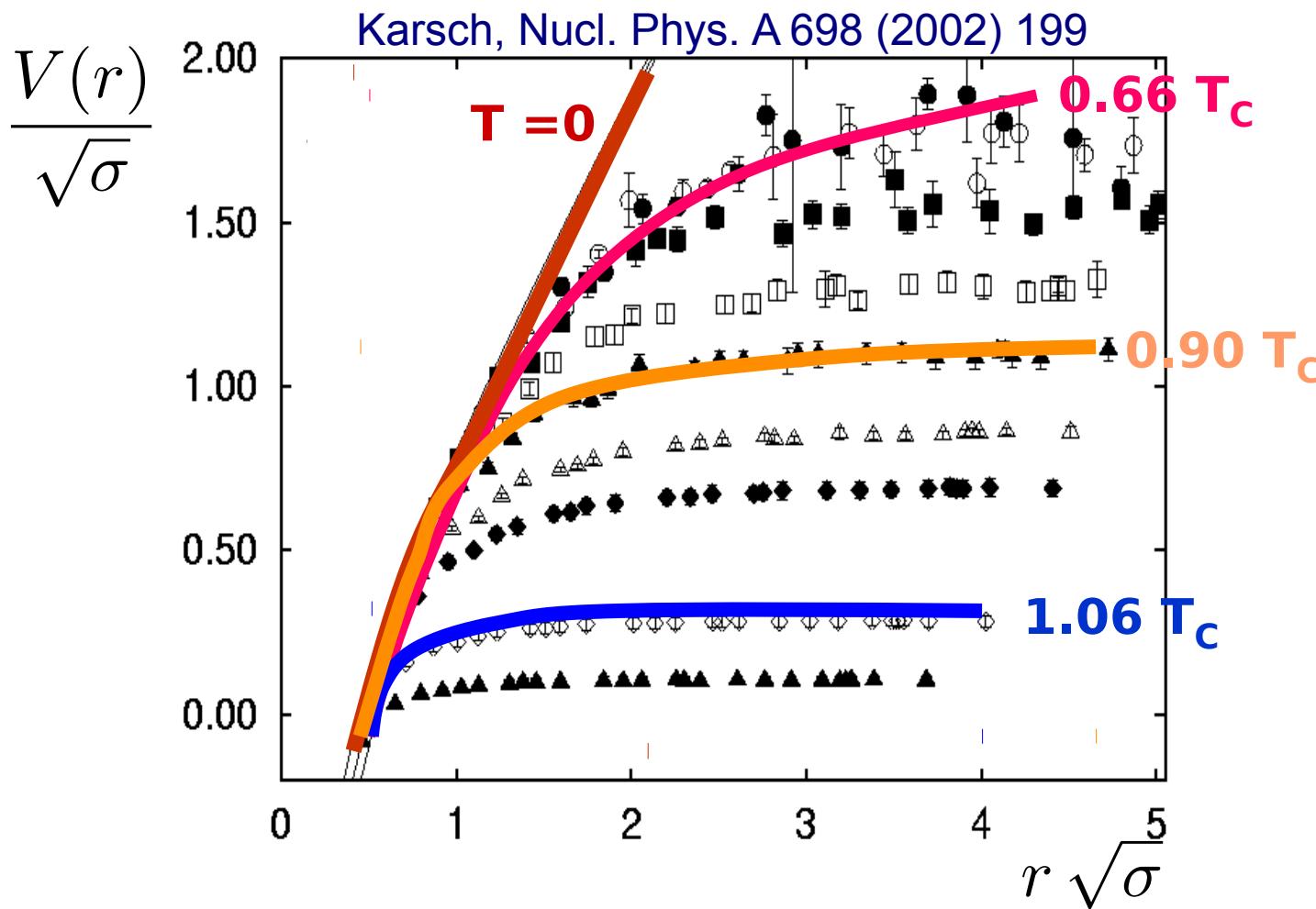
47



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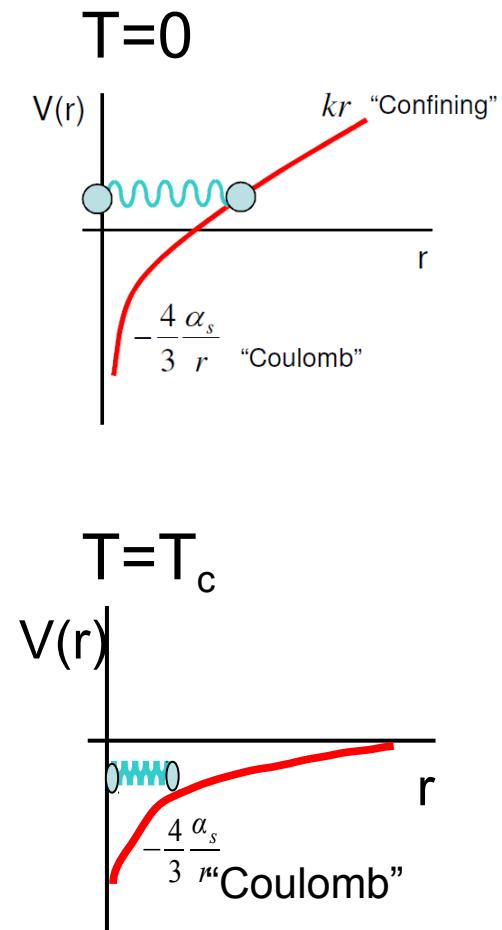
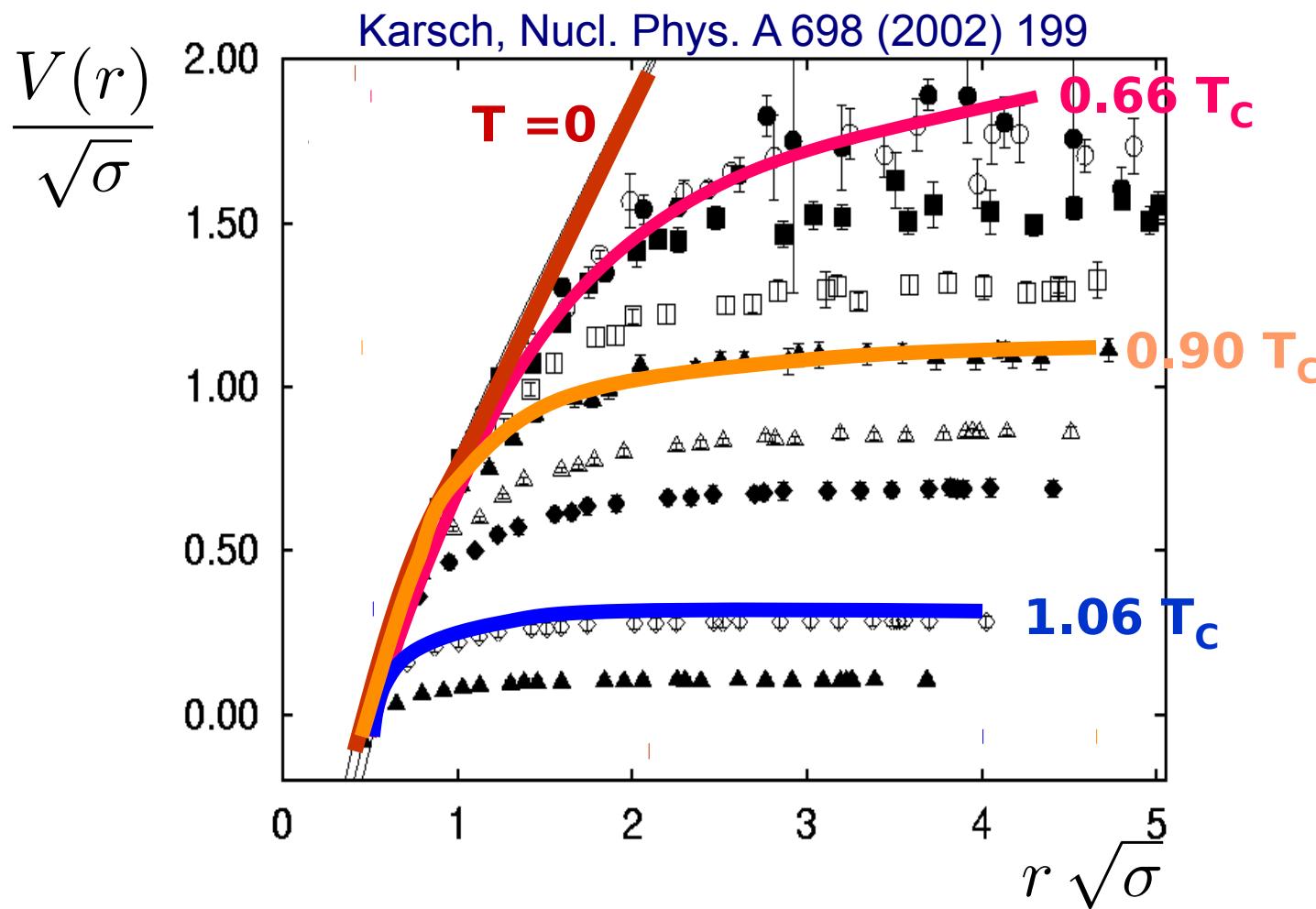
48



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# Lattice QCD: Static potential

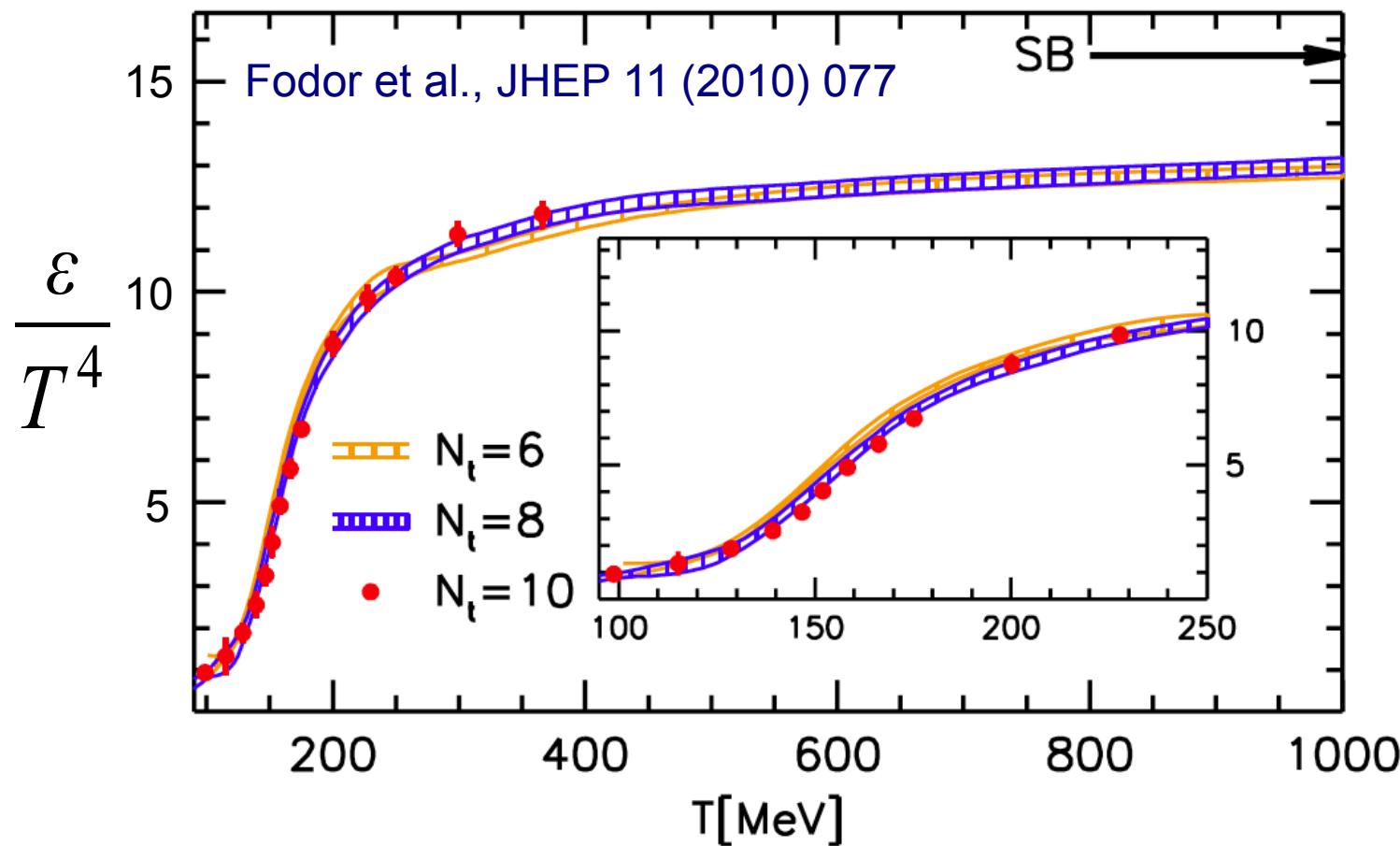
49



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# Lattice QCD: Energy density

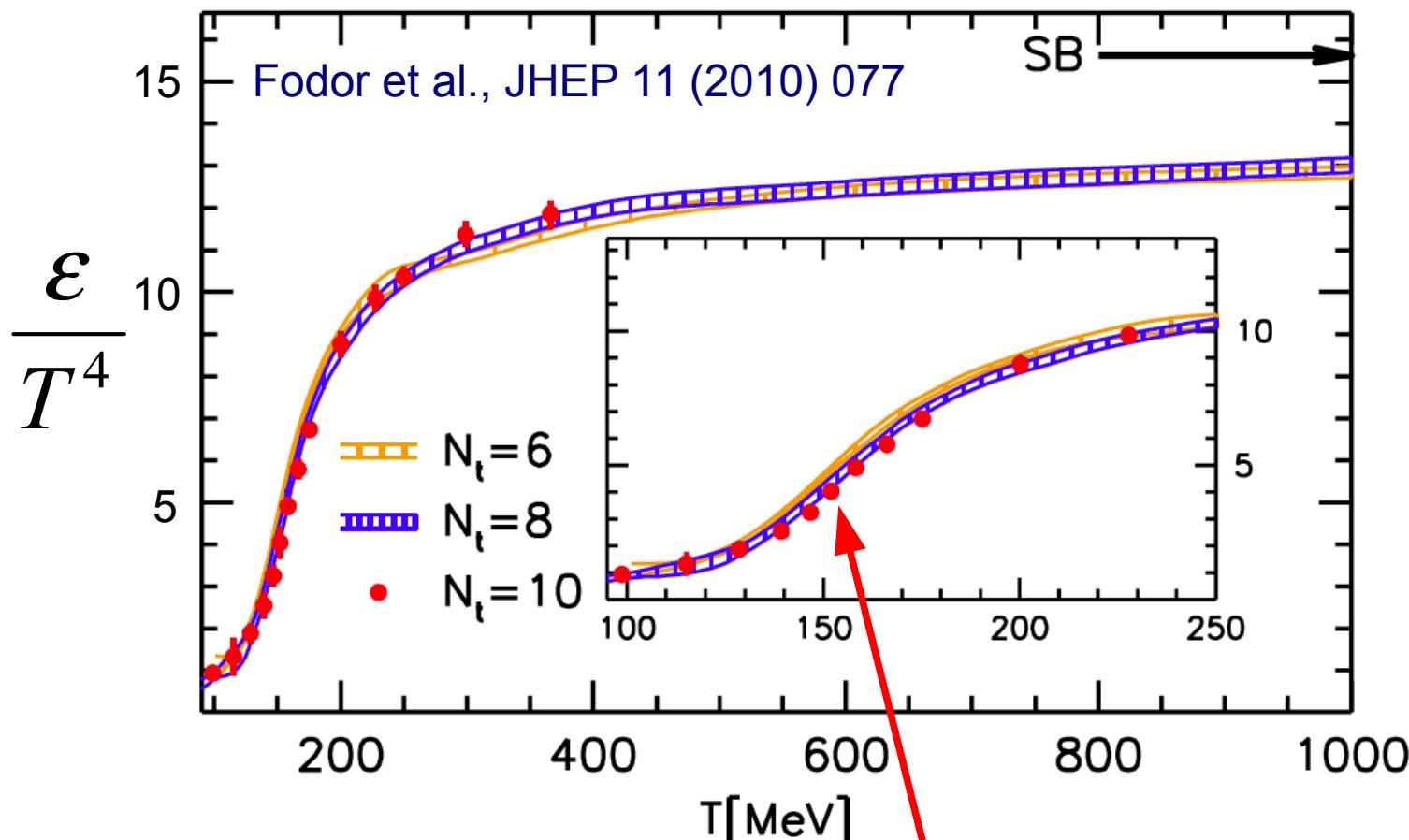
50



Cross-over transition temperature region between 140 and 200 MeV  
with range of energy density between 0.2 and 1.8 GeV/fm<sup>3</sup>  
Remember:  $T_c \approx 170$  MeV and  $\varepsilon_c \approx 1$  GeV/fm<sup>3</sup>

# Lattice QCD: Energy density

51

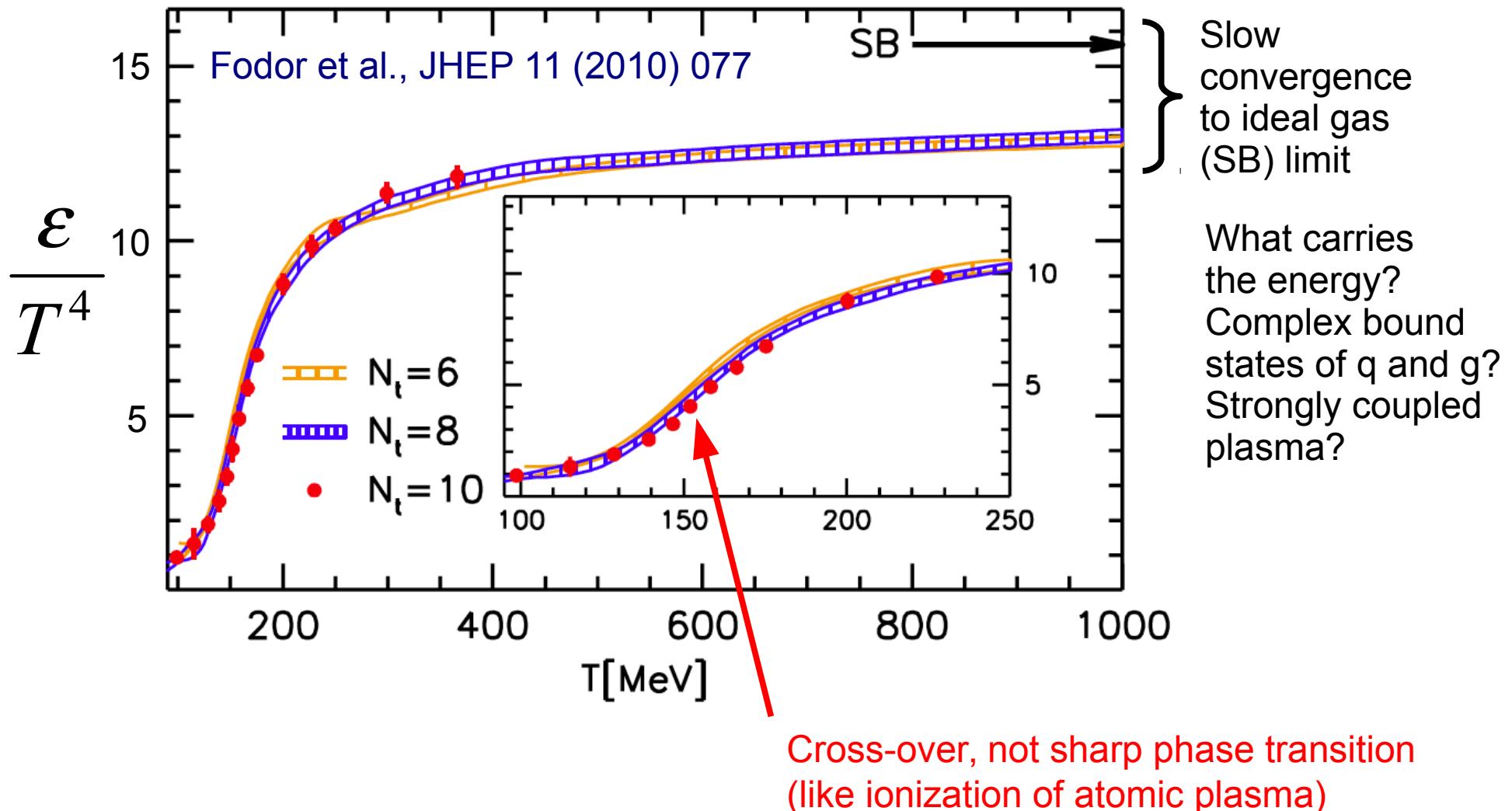


Cross-over, not sharp phase transition  
(like ionization of atomic plasma)

Cross-over transition temperature region between 140 and 200 MeV  
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# Lattice QCD: Energy density

52



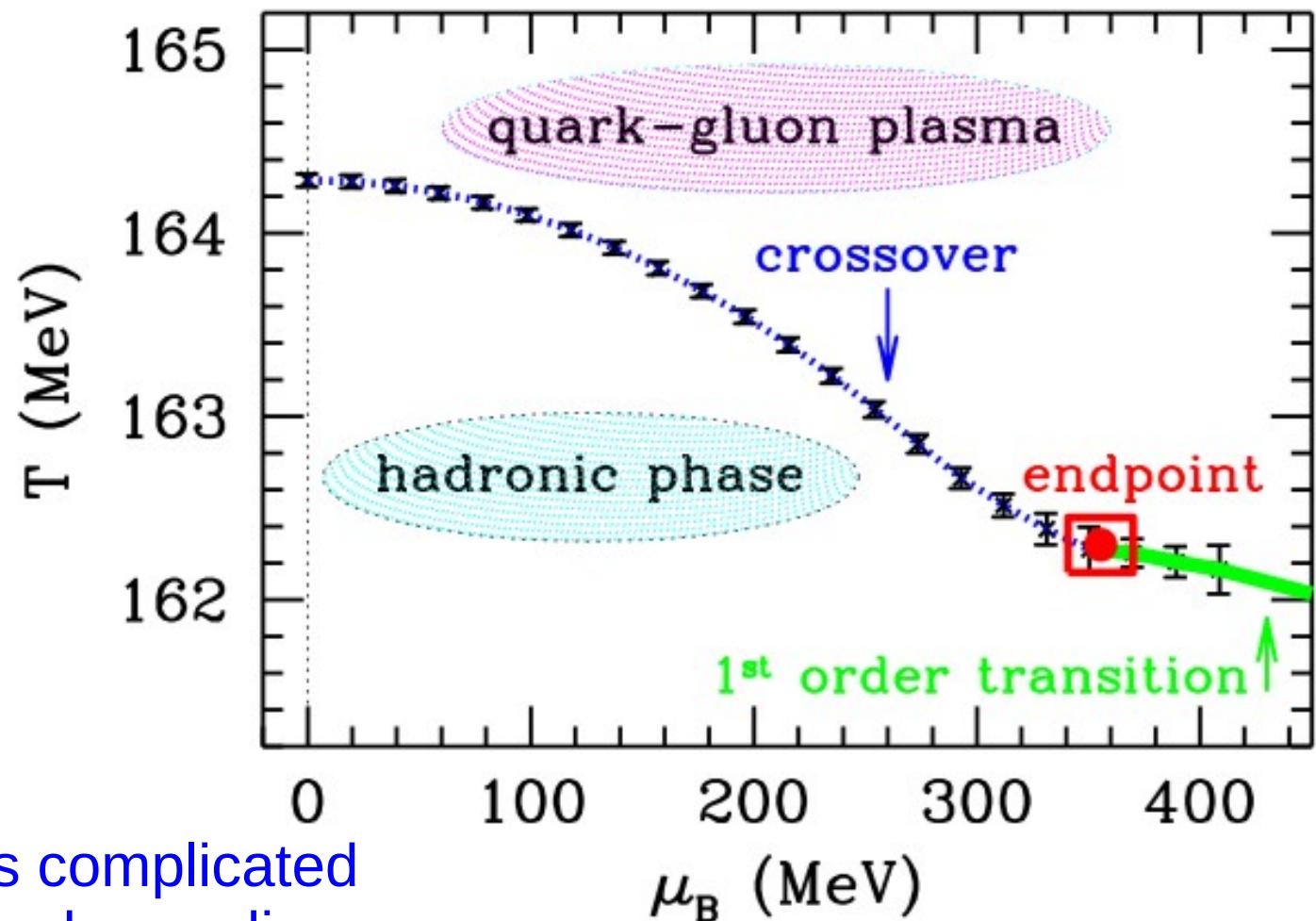
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Remember:  $T_c \approx 170$  MeV and  $\epsilon_c \approx 1$  GeV/fm<sup>3</sup>

# Lattice QCD: phase diagram

53

Fodor and Katz,  
JHEP 0404 (2004) 050

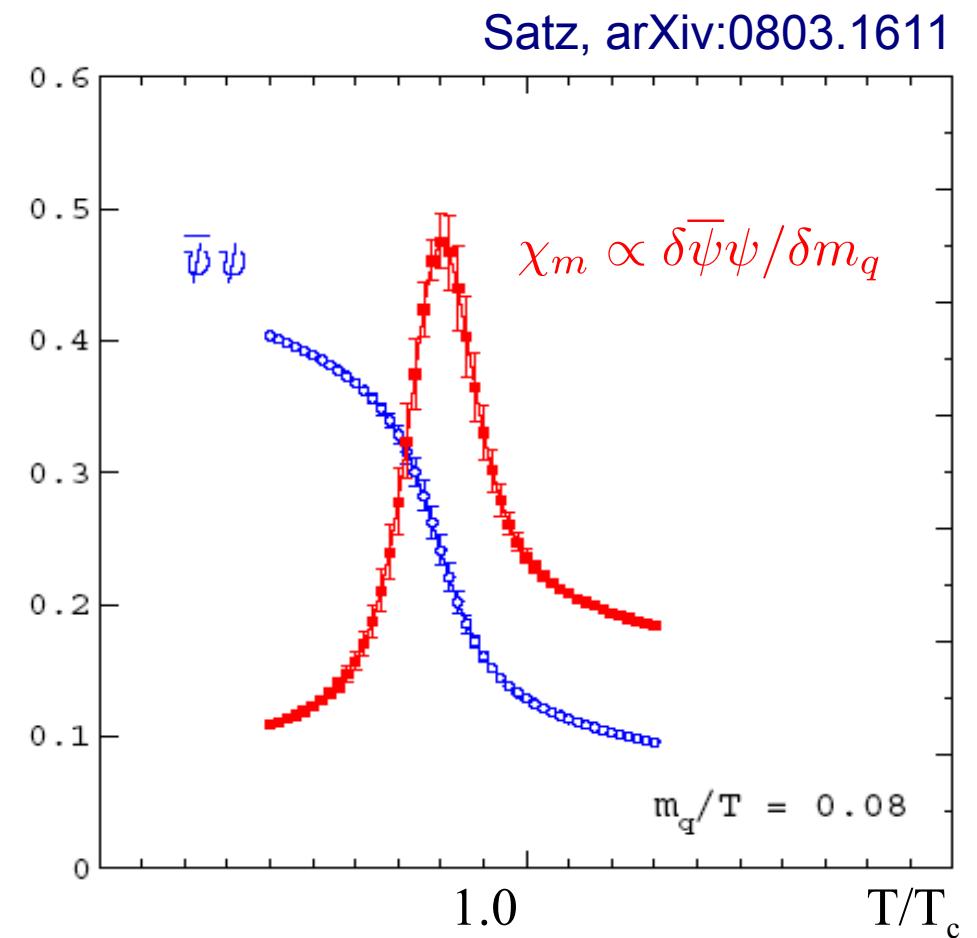


- Finite  $\mu$  calculations complicated and computationally demanding
- Some calculations suggest a critical endpoint at  $T=162$  MeV,  $\mu_B=340$  MeV with large theoretical uncertainties
- Critical endpoint existence and exact location are subject to exciting ongoing experimental and theoretical research

# Restoration of bare masses

54

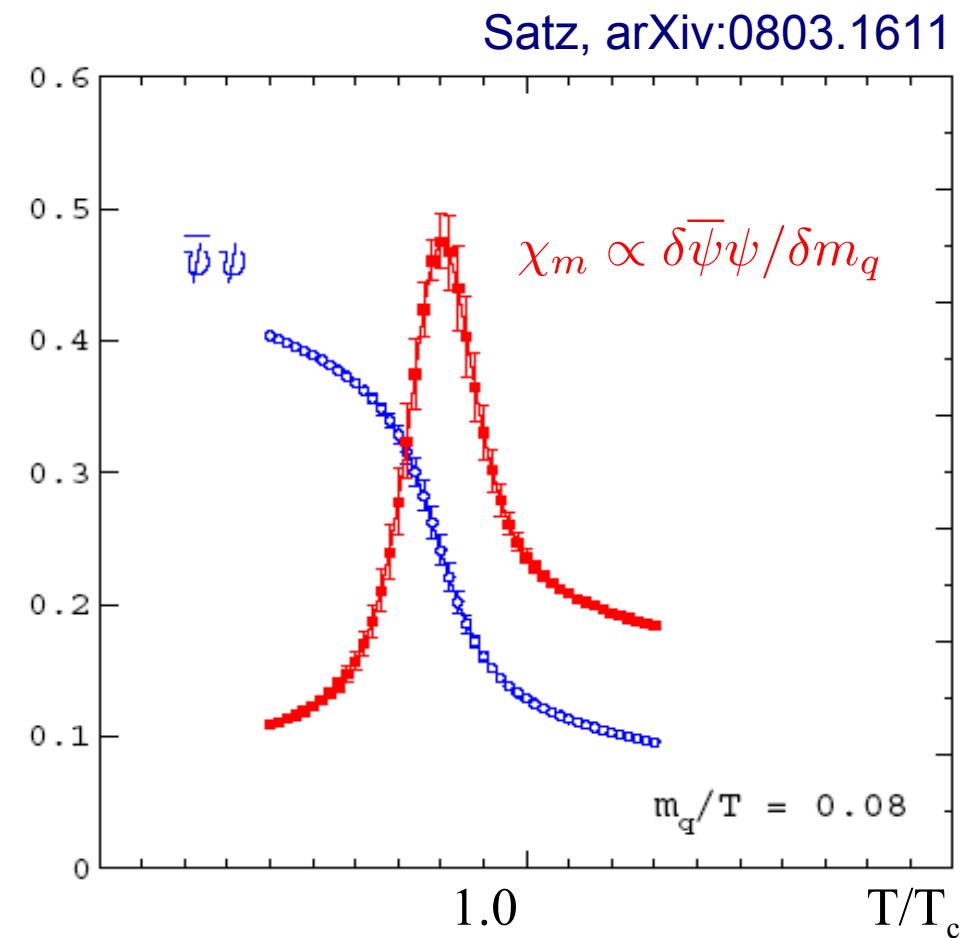
- Up and down quarks have very small ( $< 10$  MeV) bare masses (generated from the coupling to the Higgs)
- Confined quarks however require about 300 MeV dynamically through the effect of the strong interactions



# Restoration of bare masses

55

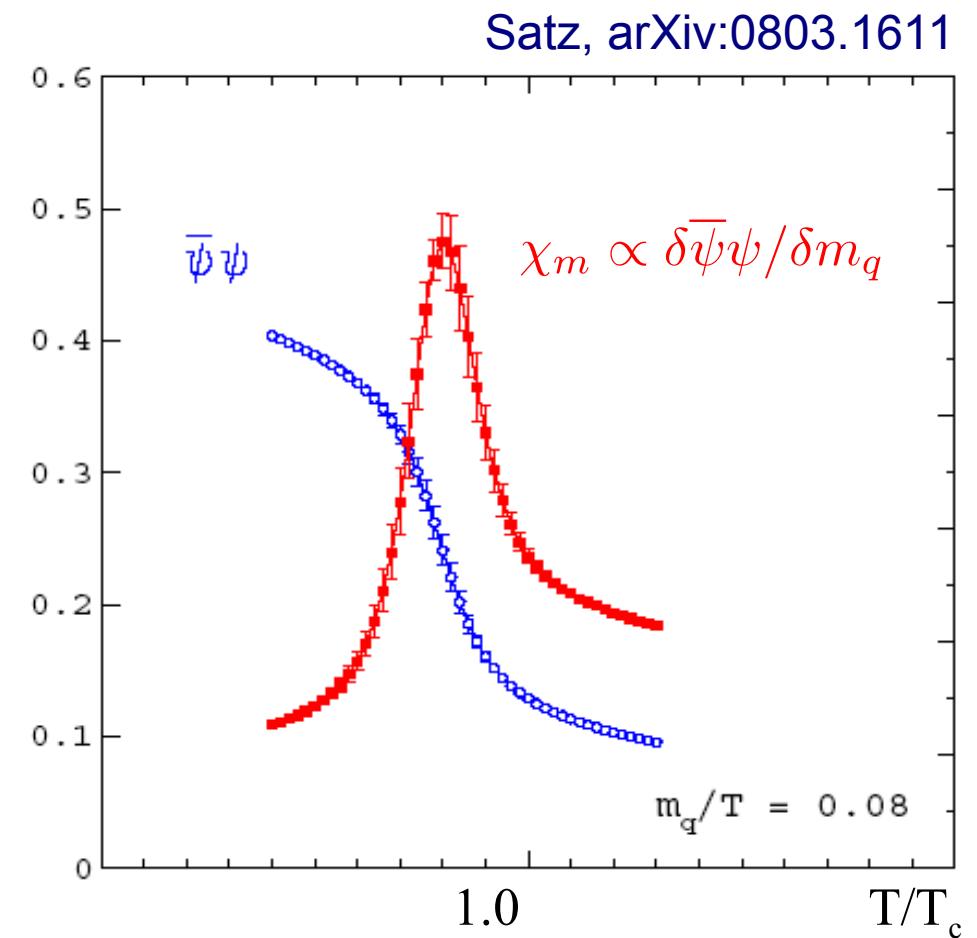
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  - Usually called “Partial restoration of chiral symmetry”



# Restoration of bare masses

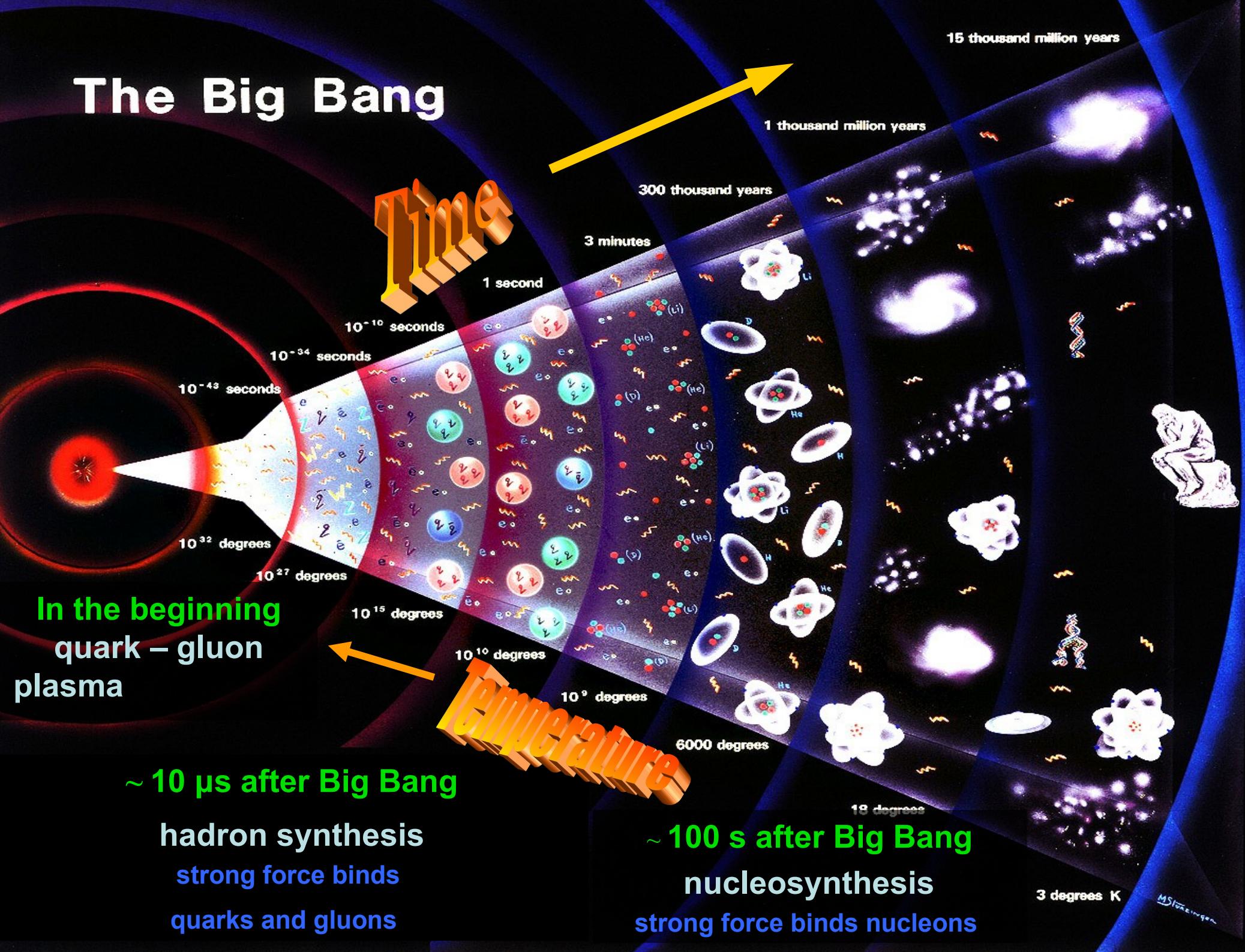
56

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- Confined quarks however require about 300 MeV dynamically through the effect of the strong interactions
- Deconfinement should be accompanied by a restoration of the masses to the bare masses of the Lagrangian
  - Usually called “Partial restoration of chiral symmetry”
  - Effective quark mass from  $\langle \bar{\psi} \psi \rangle$  computed on lattice confirms expected behavior



# Natural appearance of QCD phase transition

# The Big Bang



Effective degrees  
of freedom per  
relativistic particle

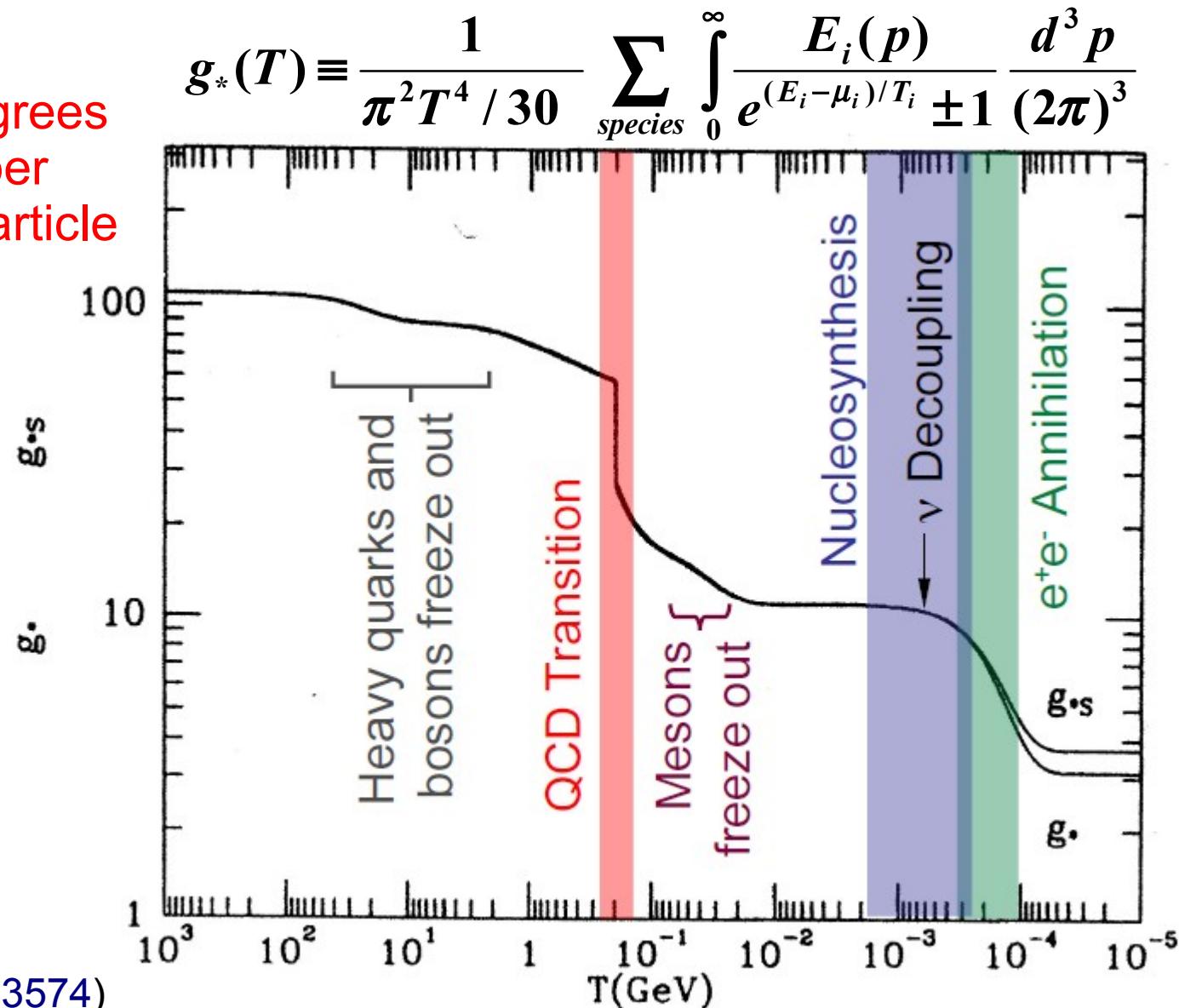


Figure from  
The Early Universe,  
Kolb and Turner  
(see also  
Schwarz, astro-ph/0303574)

Fig. 3.5: The evolution of  $g_*(T)$  as a function of temperature in the  $SU(3)_C \otimes SU(2)_L \otimes U(1)_Y$  theory.

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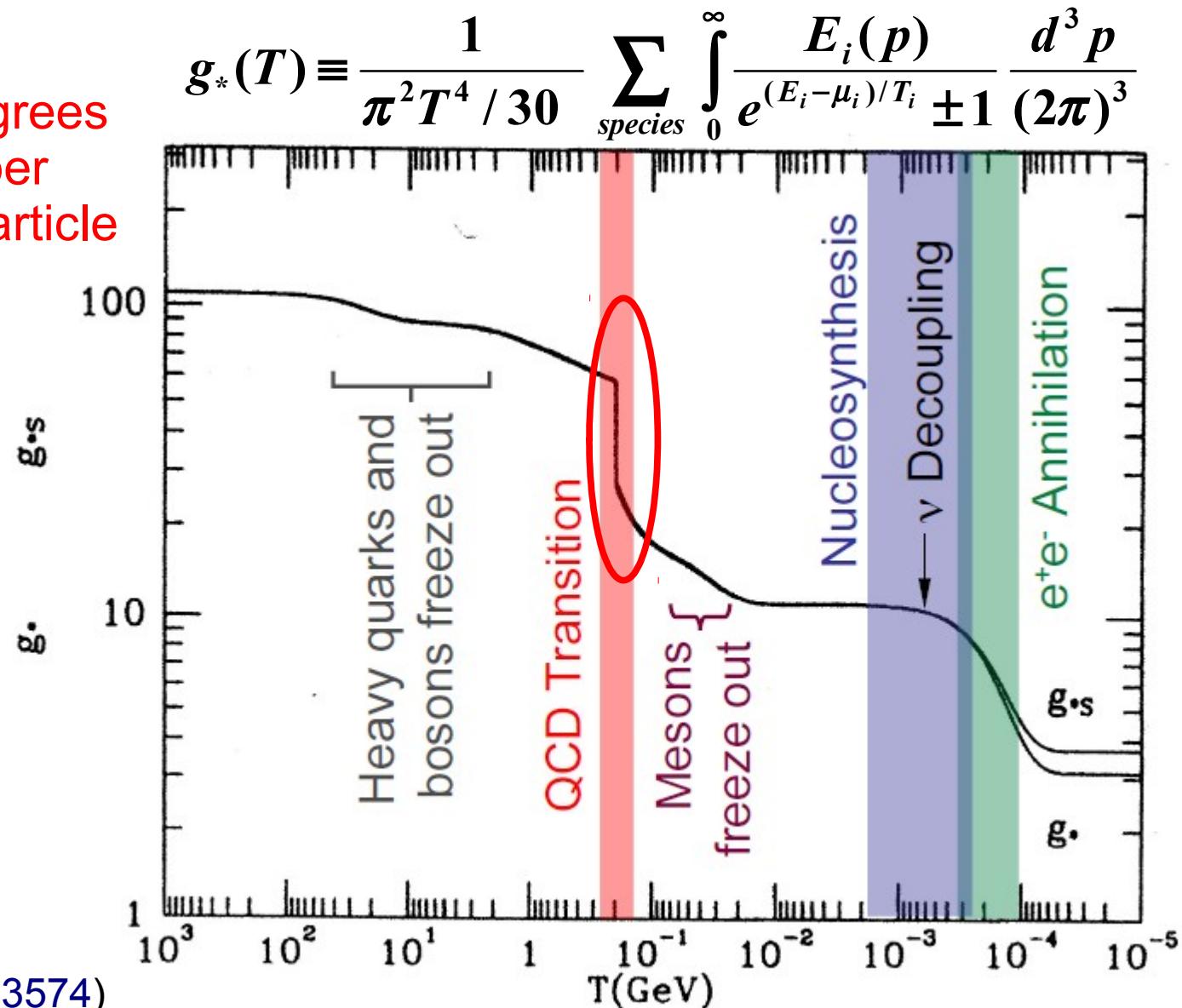


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How to create the QGP in the laboratory?

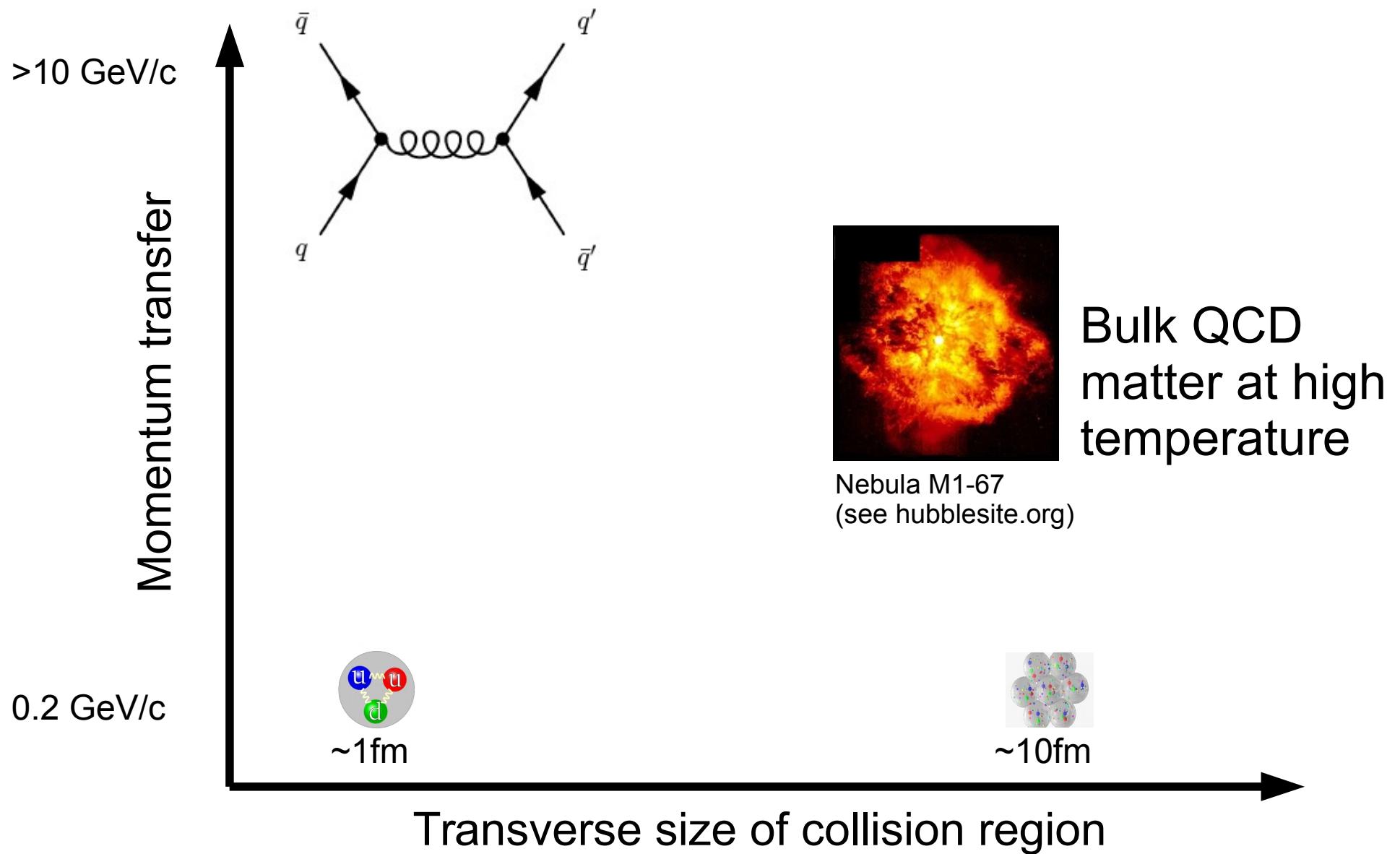
# Study QCD bulk matter at high temperature 62



T.D.Lee,  
Rev.Mod.Phys. 47 (1975) 267

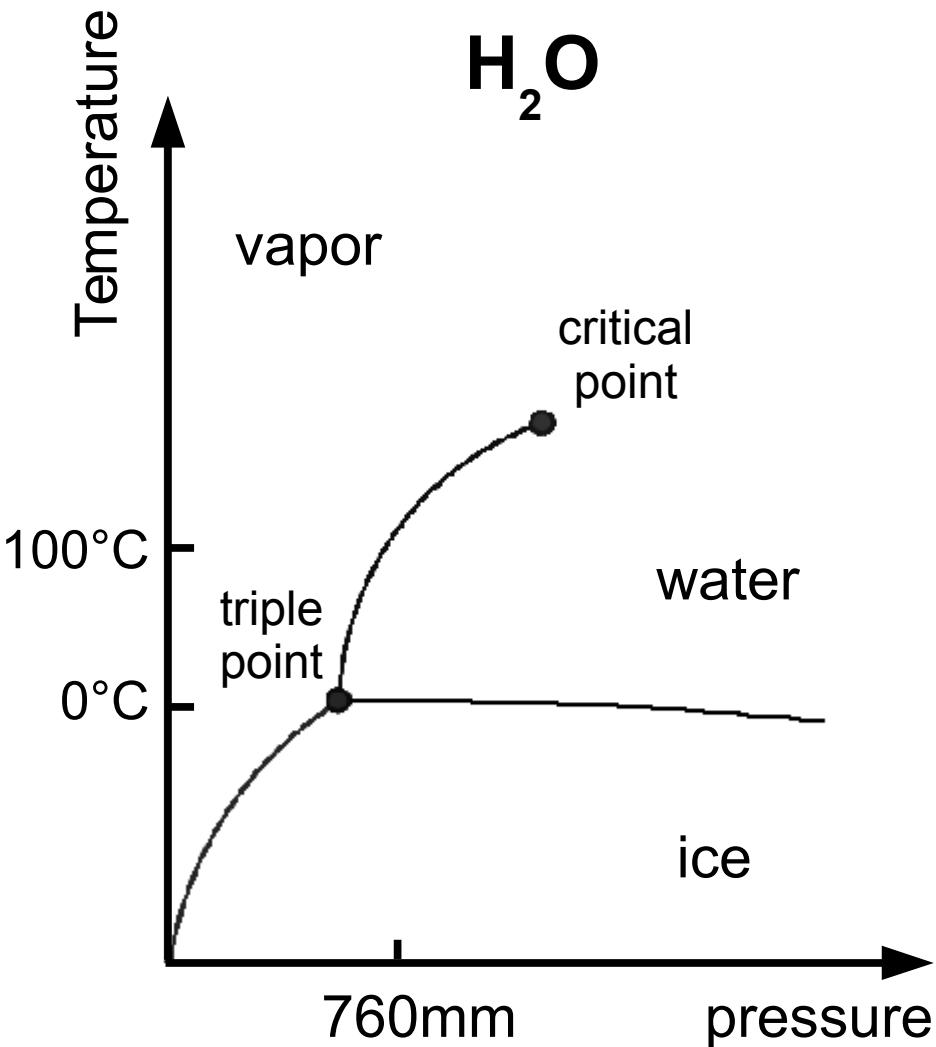
In high energy physics we have concentrated on experiments, in which we distribute a higher and higher amount of energy into a region with smaller and smaller dimensions. In order to study the question of “vacuum”, we must turn to a different direction; **we should investigate some “bulk” phenomena by distributing high energy over a relatively large volume.**

# Study QCD bulk matter at high temperature 63



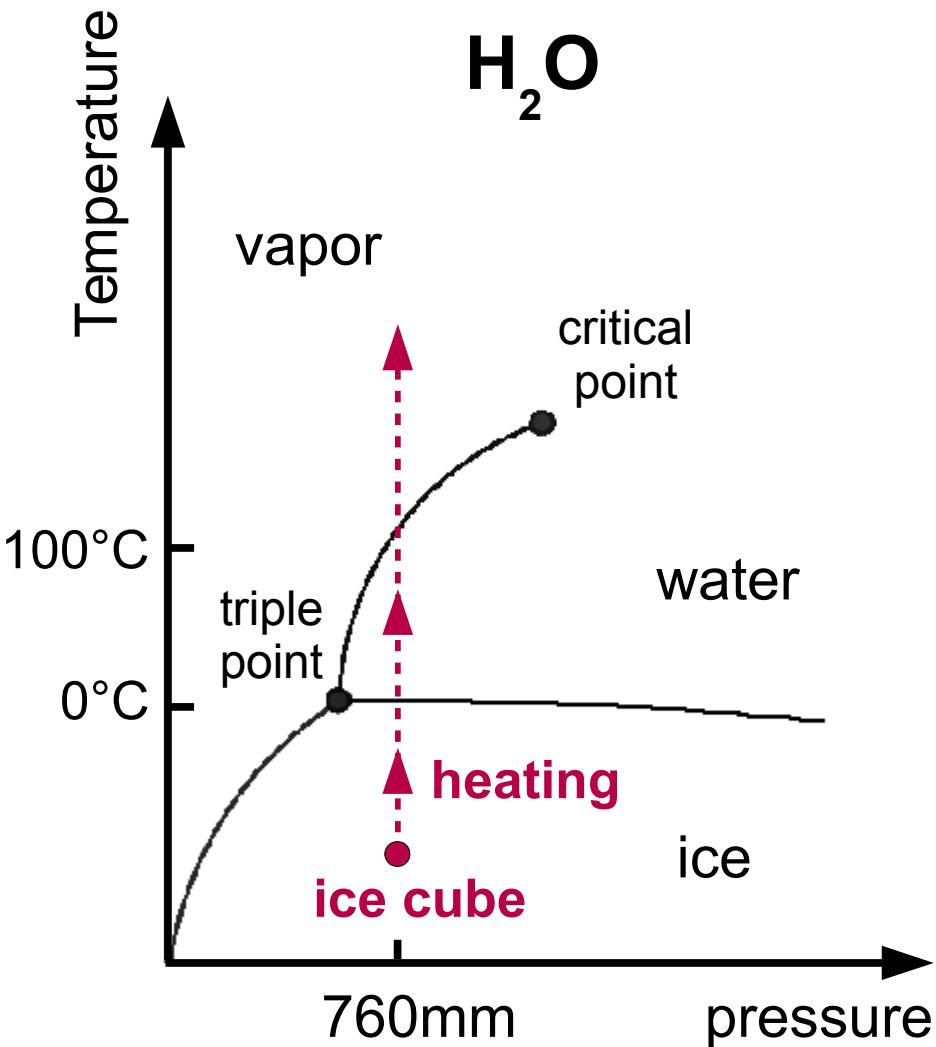
# How can we create QCD matter?

64



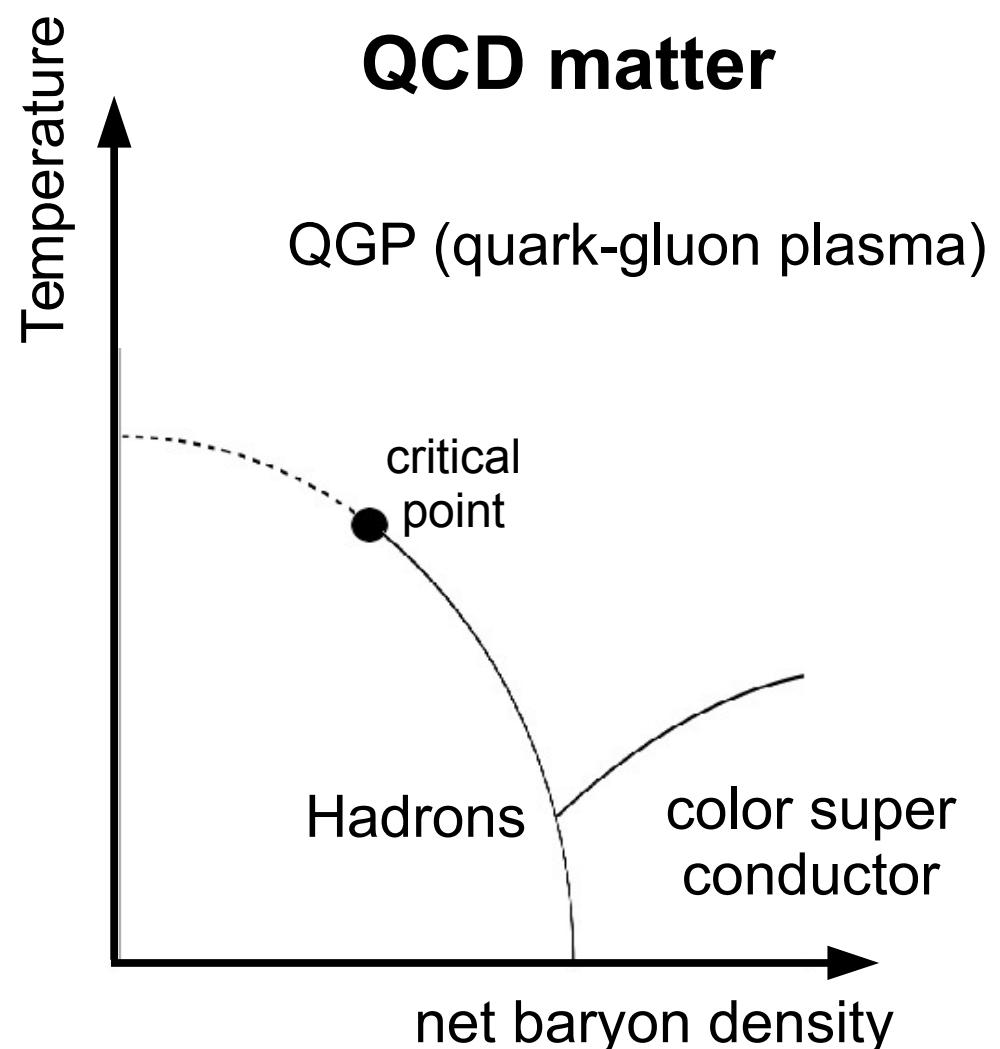
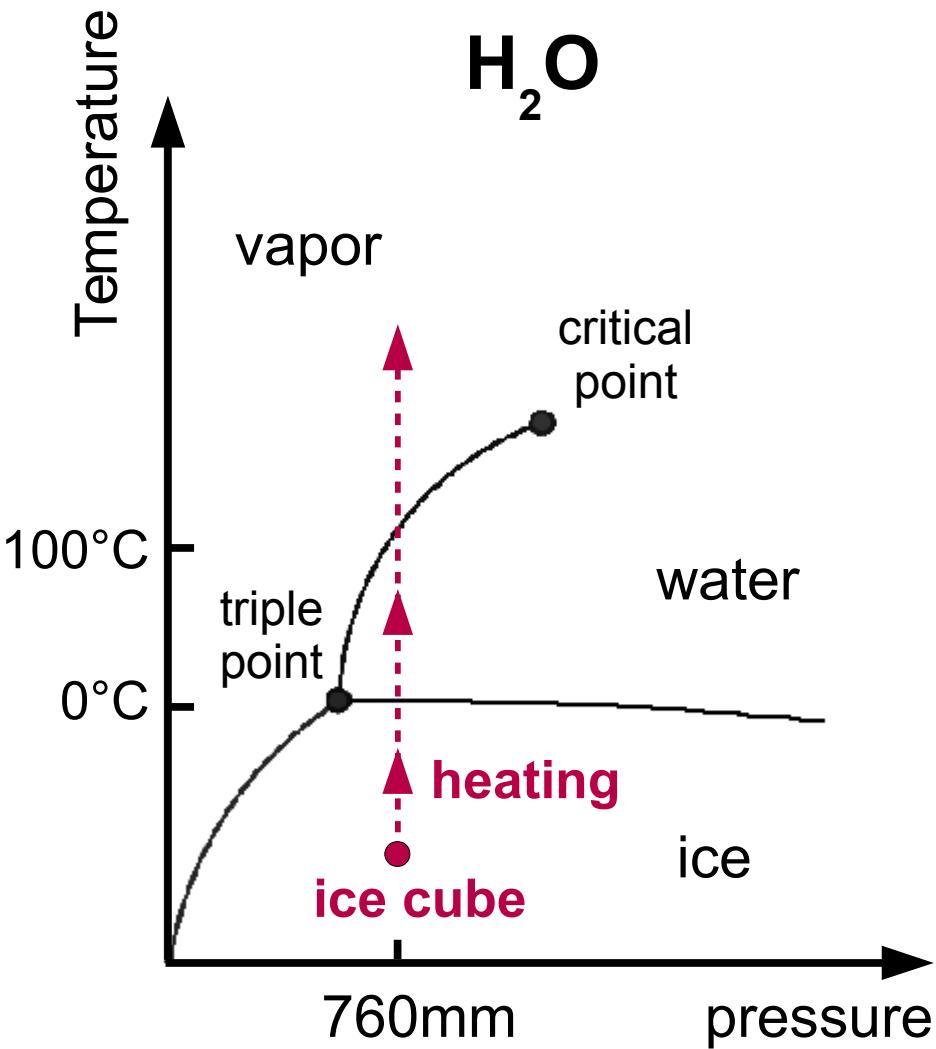
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65



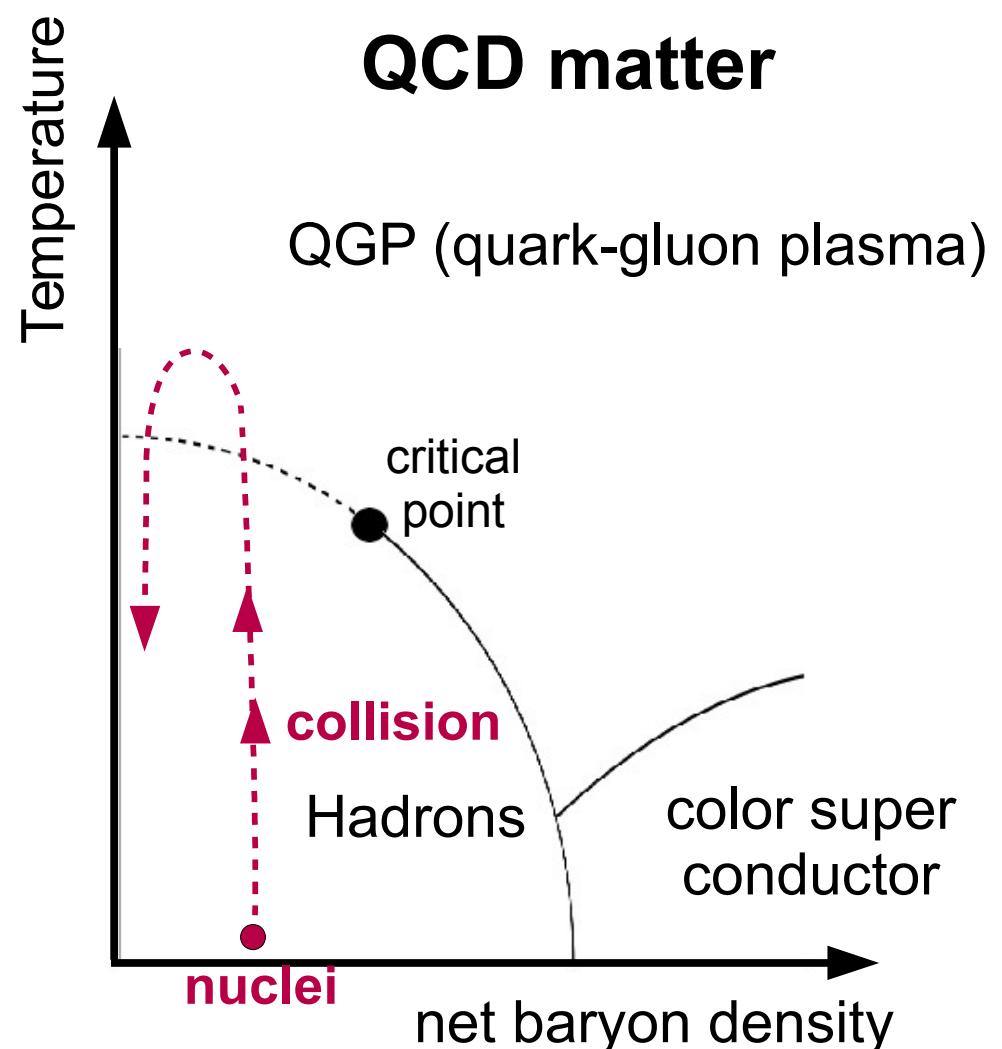
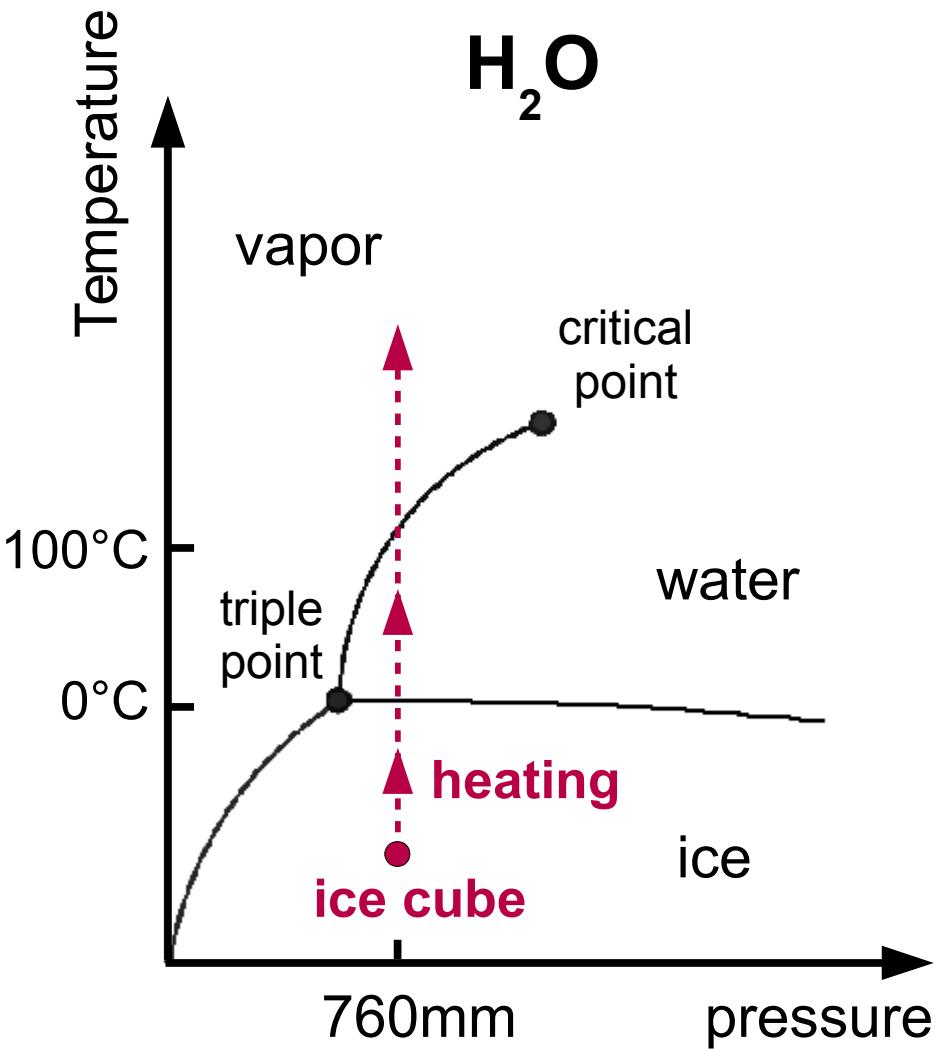
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66



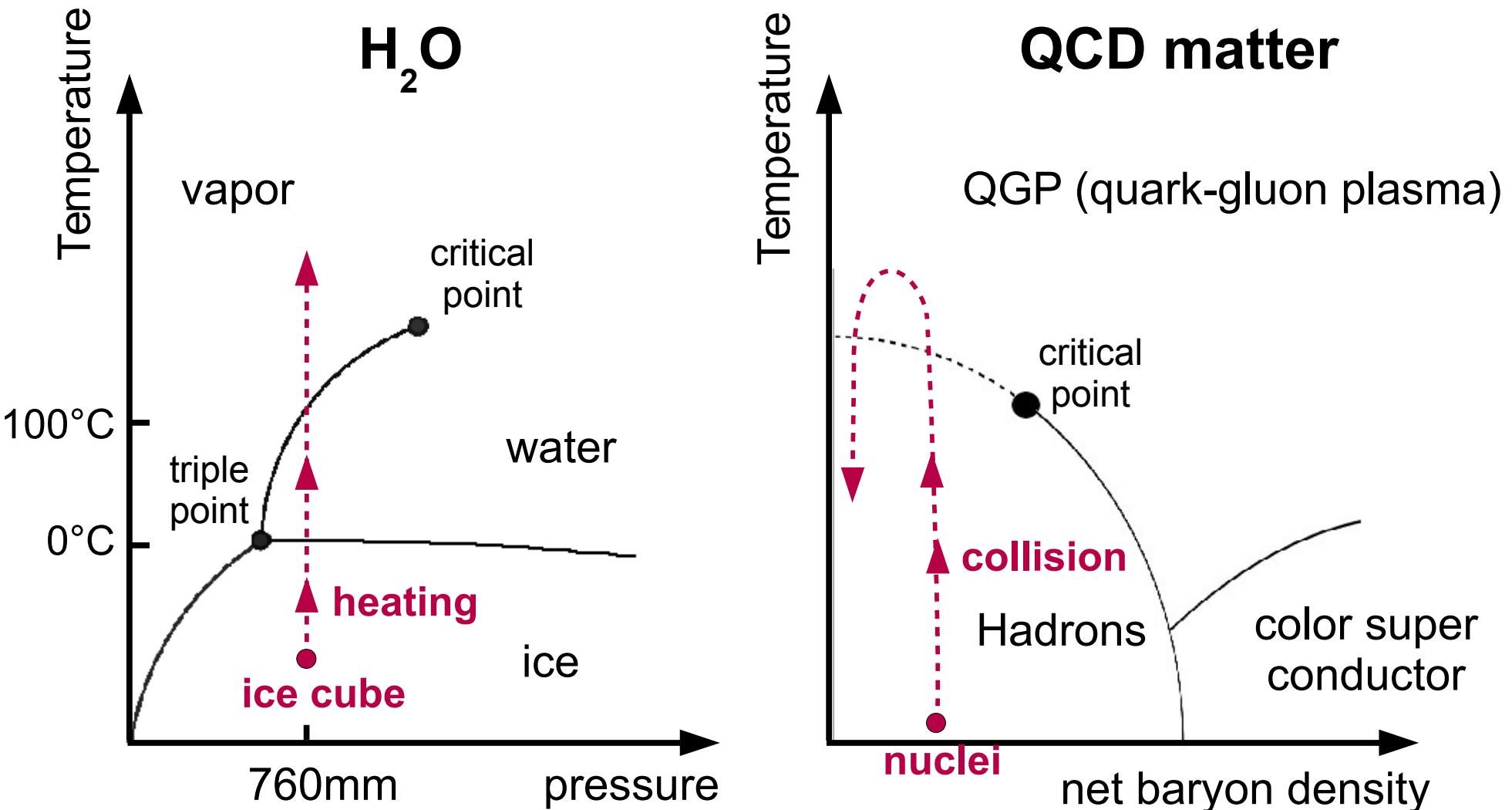
# How can we create QCD matter?

67



# How can we create QCD matter?

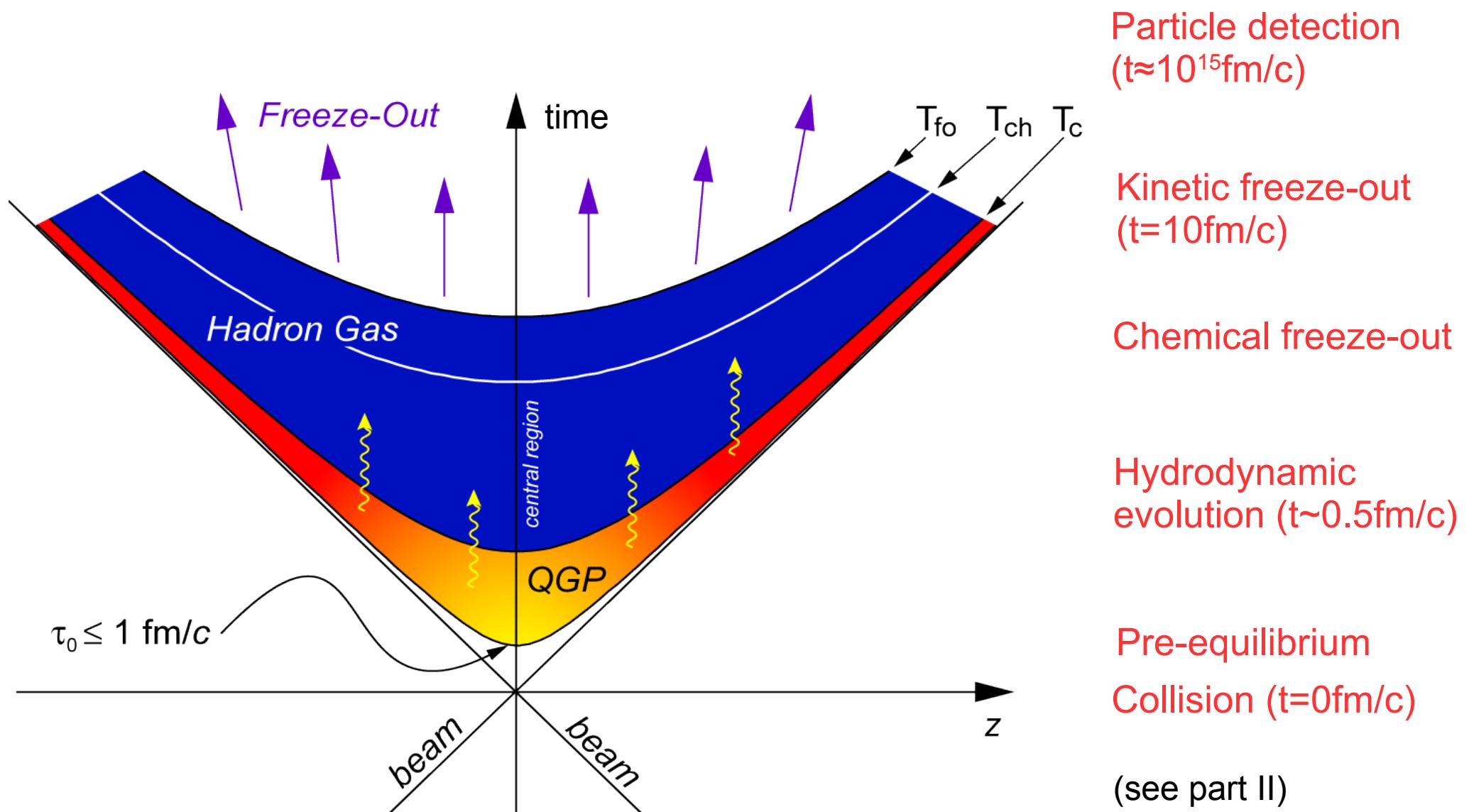
68



Experimental study of QCD phase diagram by colliding ultra-relativistic nuclei head-on to convert cold nuclear matter into a fireball of partons

# System evolution in heavy-ion collisions

69



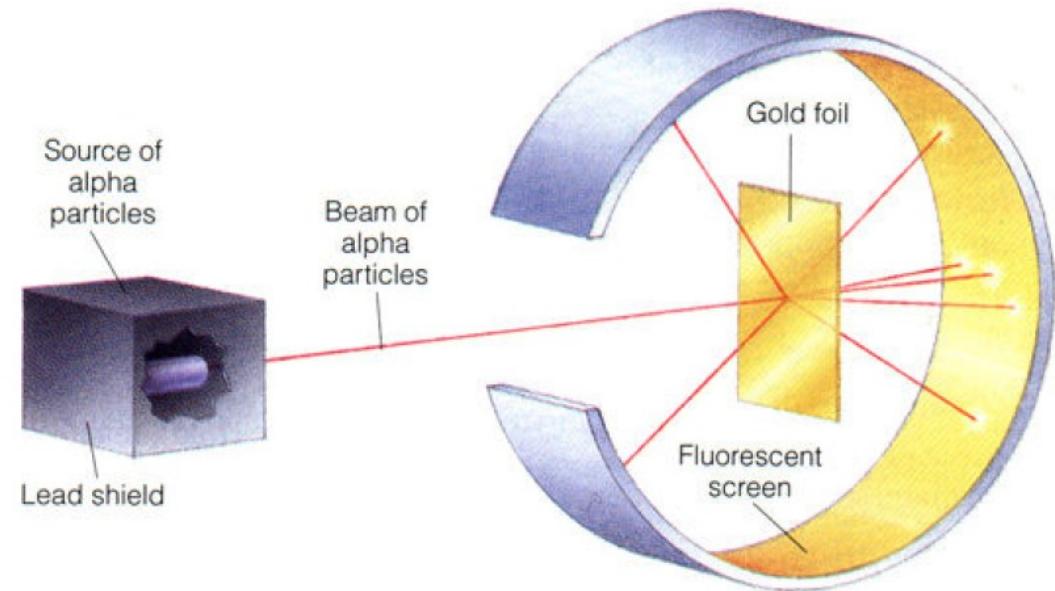
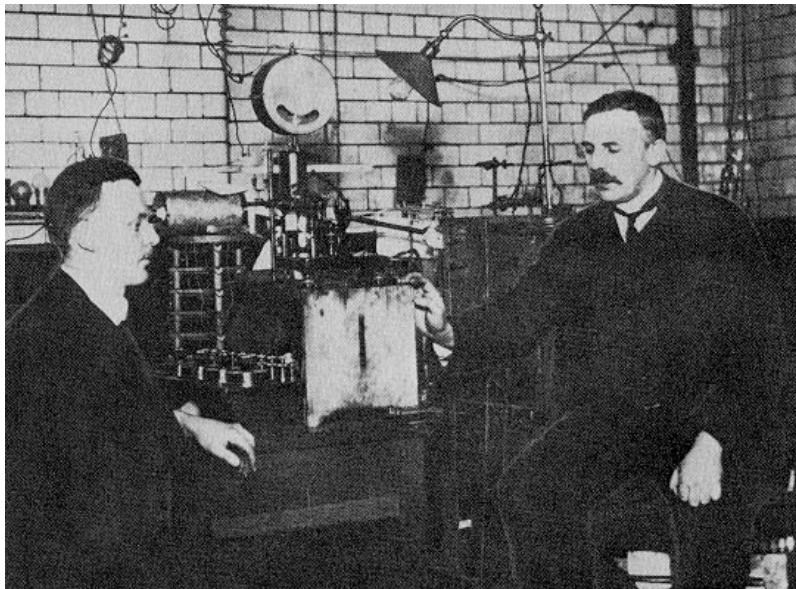
In reality, strong dynamical evolution of the system

# How to probe the QGP?

# Exploring the structure of atoms

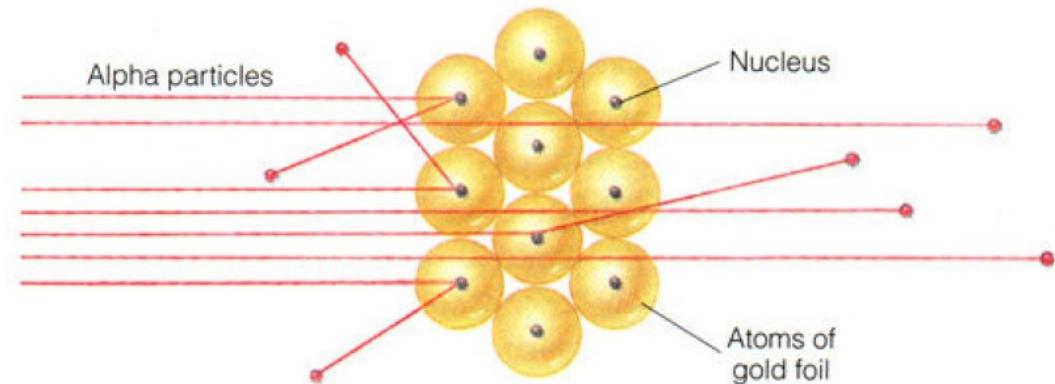
71

The first exploration of subatomic structure, by Rutherford, used Au atoms as targets and  $\alpha$  particles as probes



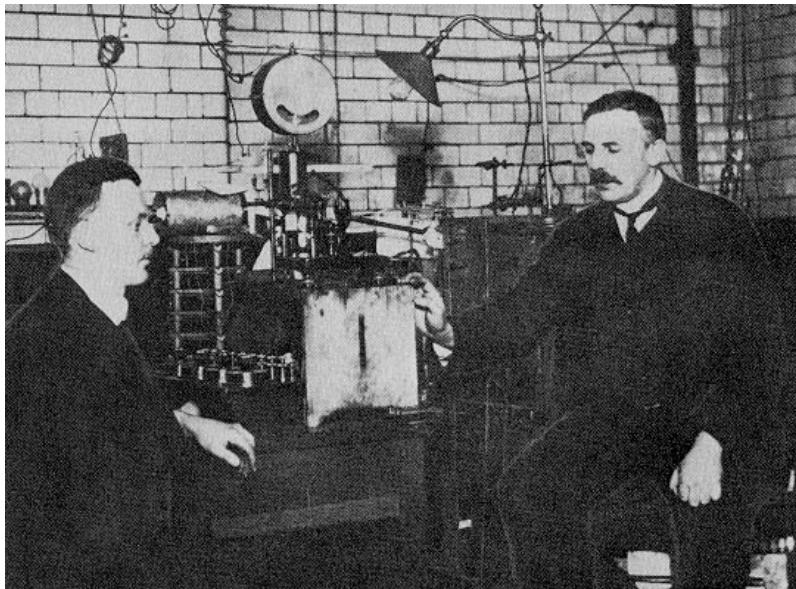
## Interpretation:

Positive charge is concentrated in a tiny volume with respect to the atomic dimensions



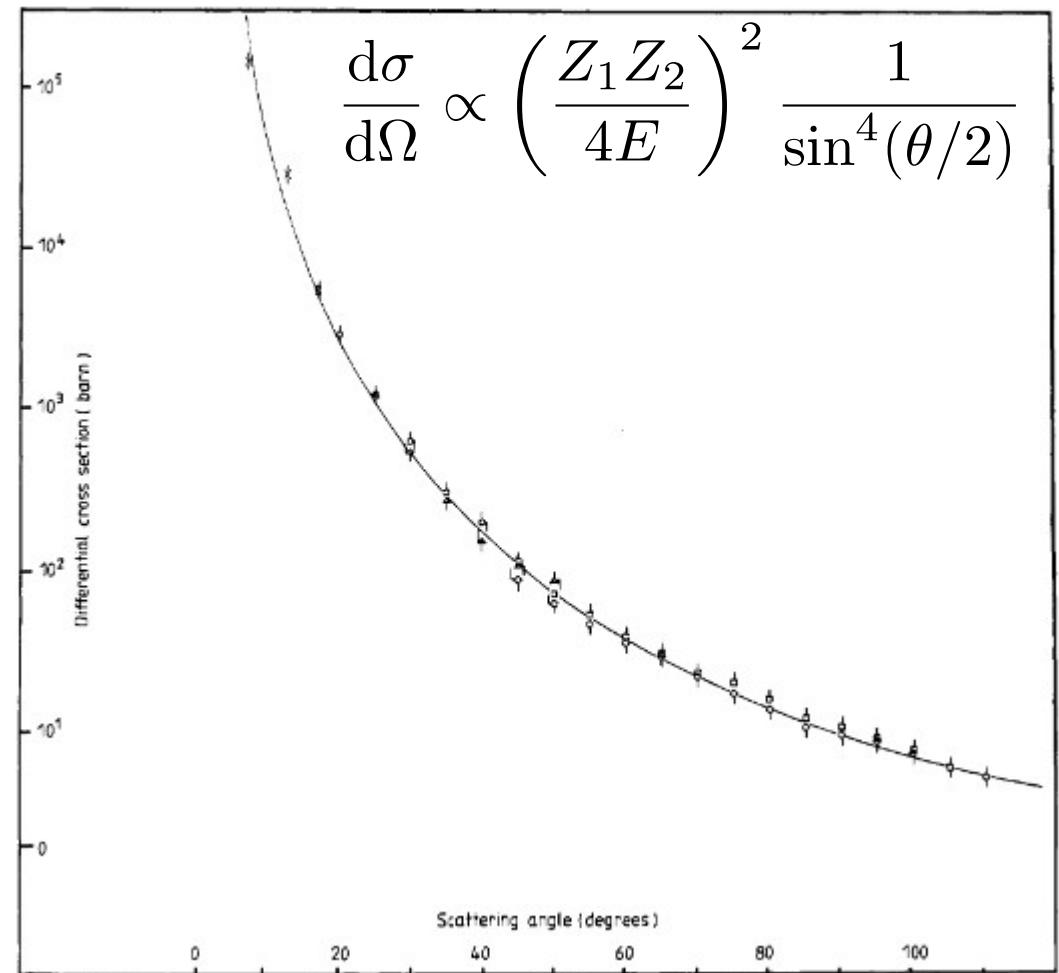
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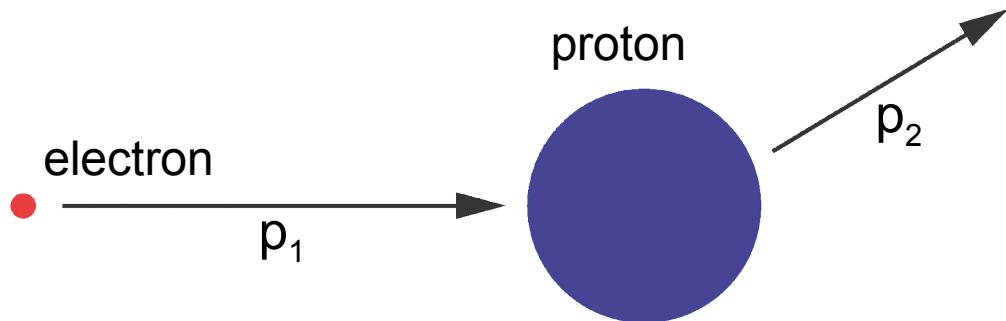


Hoppenau and Eggers, Eur.J.Phys. 6 (1985) 86

# Exploring the structure of protons

73

Deep inelastic scattering experiments at SLAC in the 1960s established the quark-parton model:

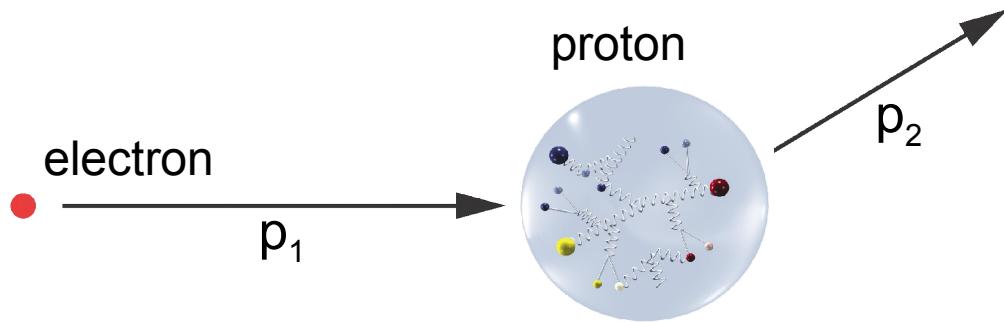


The angular distribution of the scattered electrons reflects the distribution of charge inside the proton

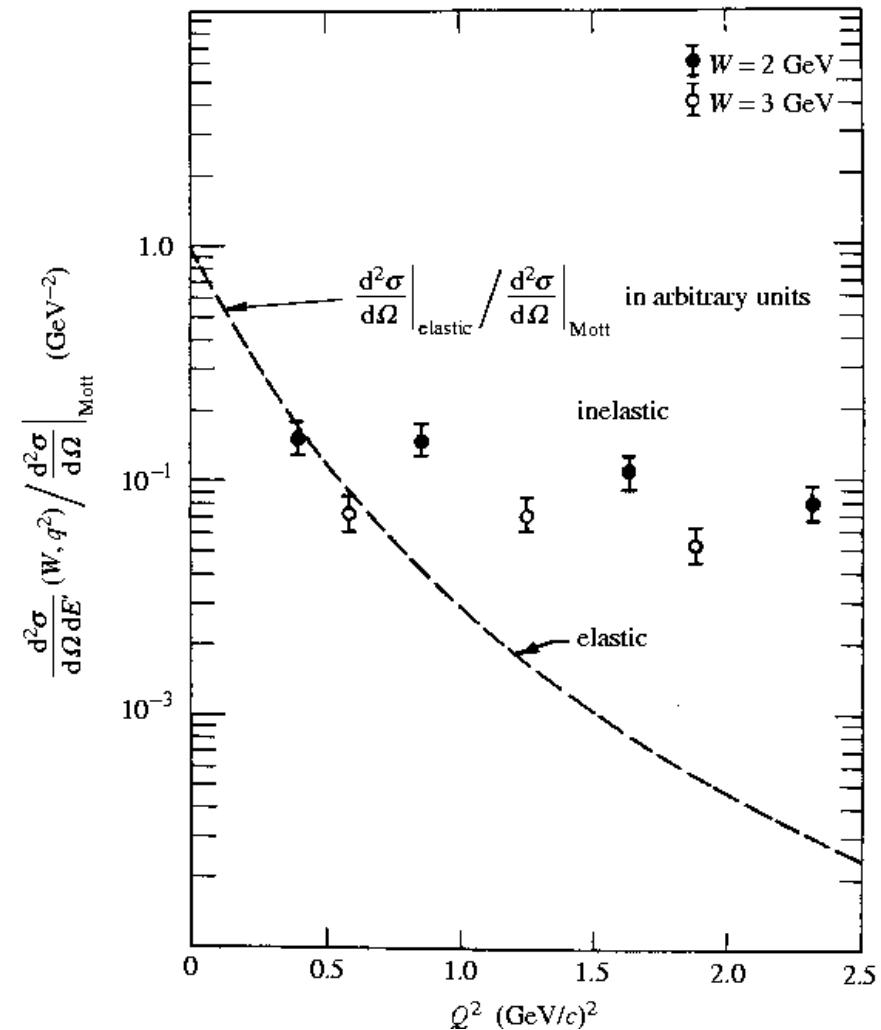
# Exploring the structure of protons

74

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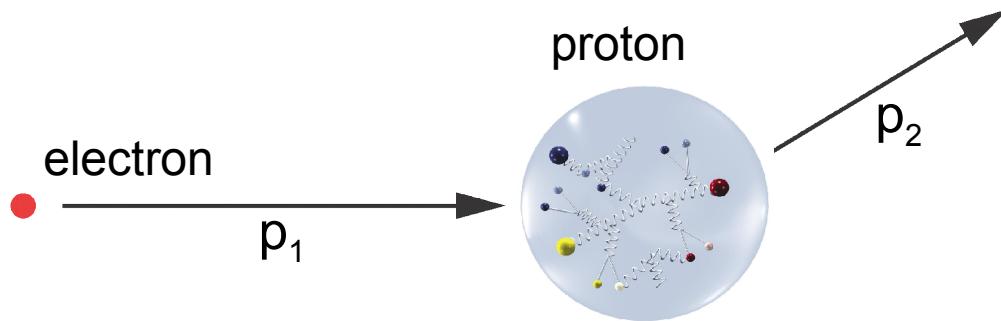
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# Exploring the structure of protons

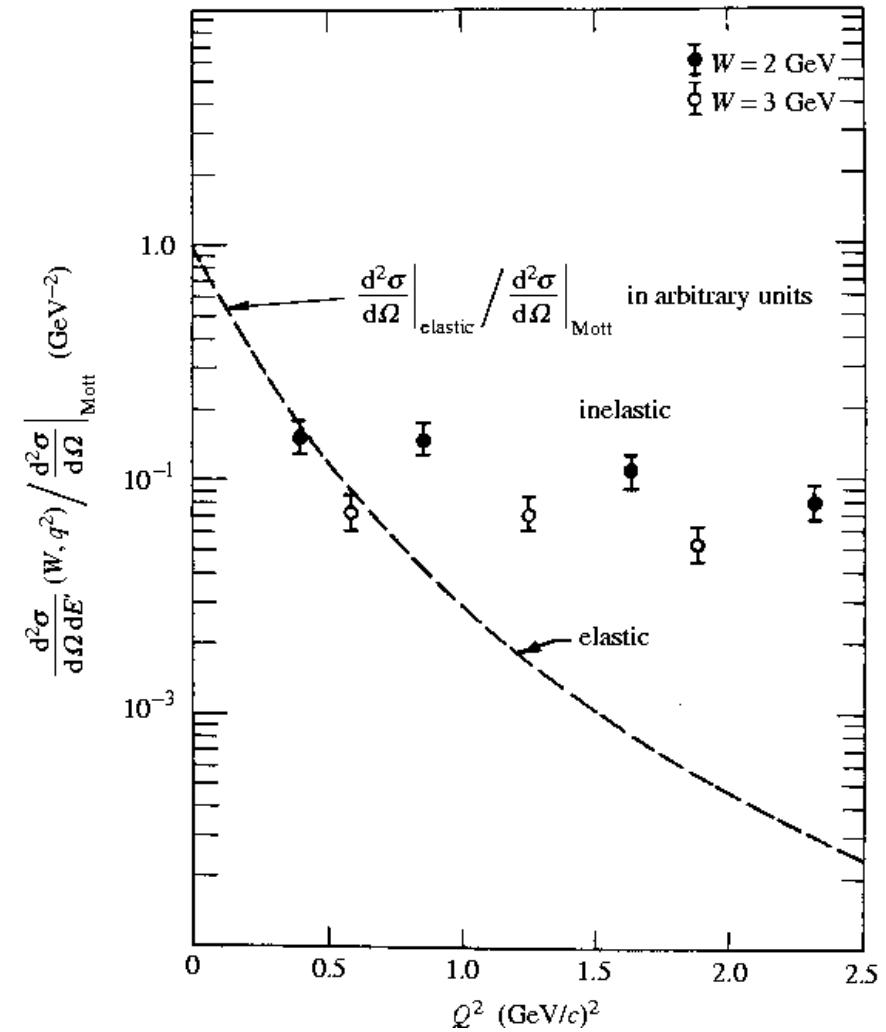
75

Deep inelastic scattering experiments at SLAC in the 1960s established the quark-parton model:



The angular distribution of the scattered electrons reflects the distribution of charge inside the proton

Approximately constant form factor  
⇒ scattering on point-like constituents  
⇒ **quarks**



1990 Nobel Prize in Physics

# Exploring the structure of QCD matter

76

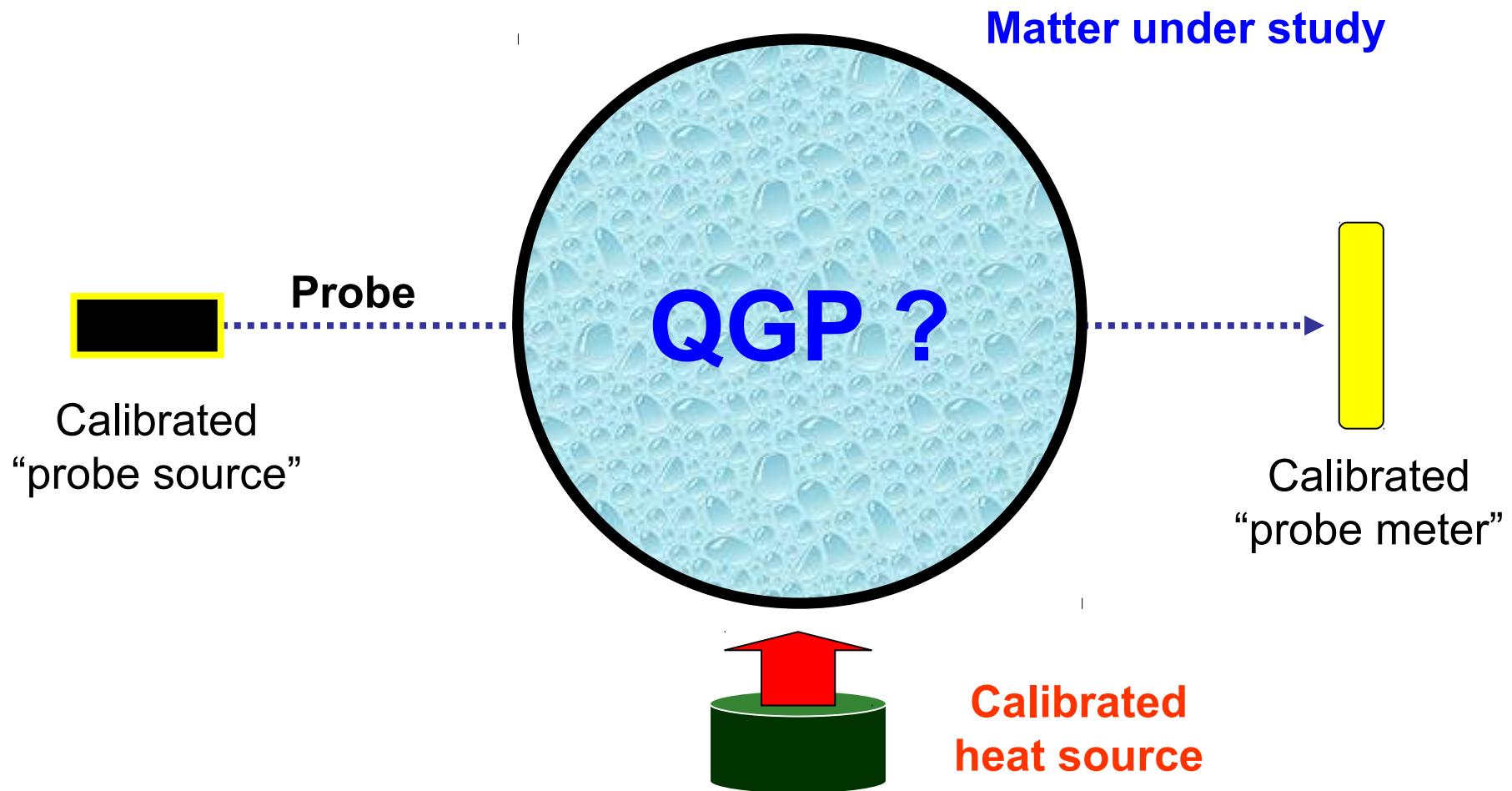
In analogy, we study the QCD matter produced in HI collisions by measuring how it affects well understood probes, as a function of the temperature of the system



# Exploring the structure of QCD matter

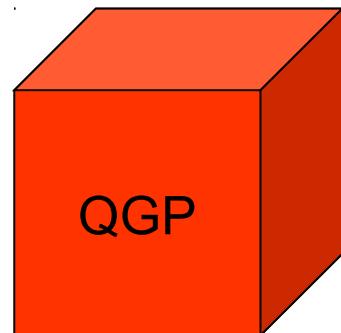
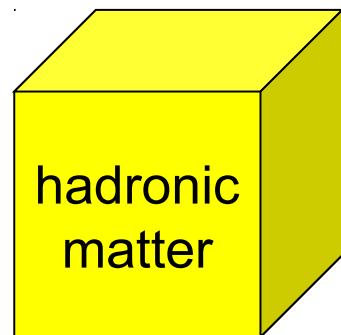
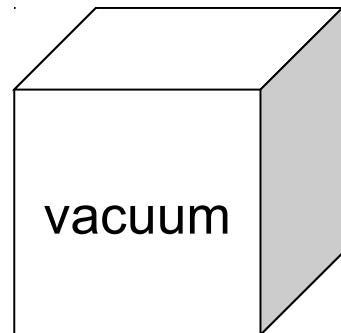
77

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# Good probes of QCD matter

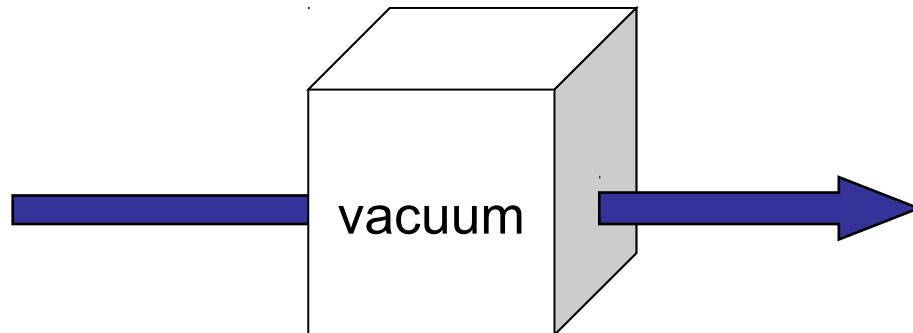
78



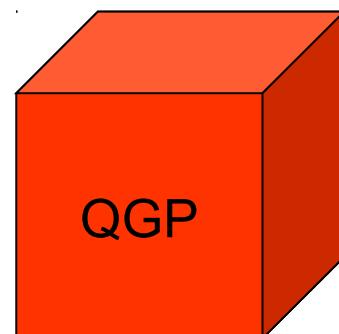
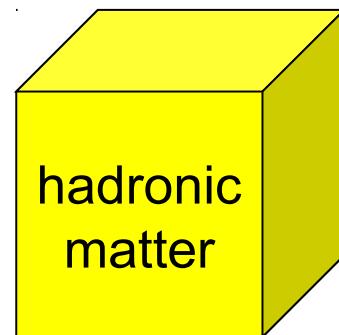
(see part III)

# Good probes of QCD matter

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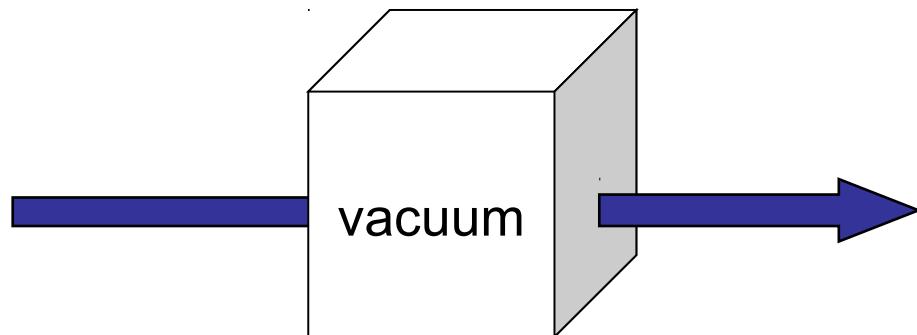
Well understood in “pp collisions”,  
and/or in control systems like pA



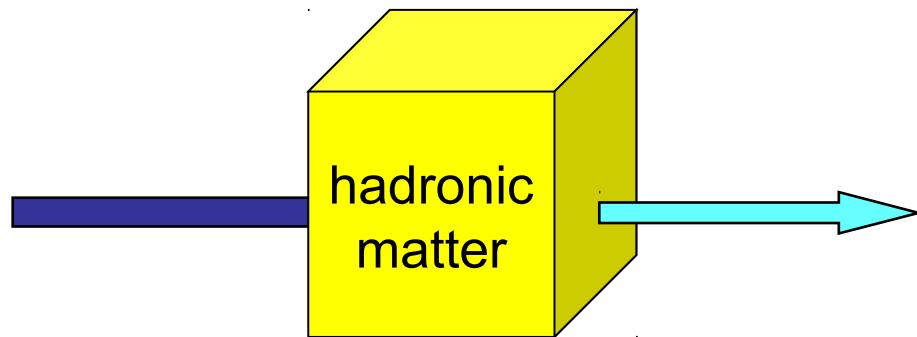
(see part III)

# Good probes of QCD matter

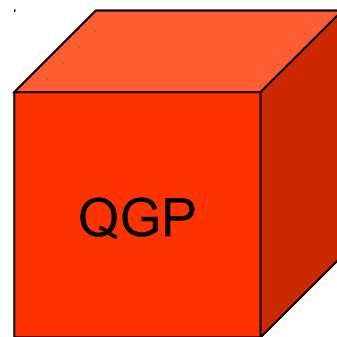
80



Well understood in “pp collisions”,  
and/or in control systems like pA



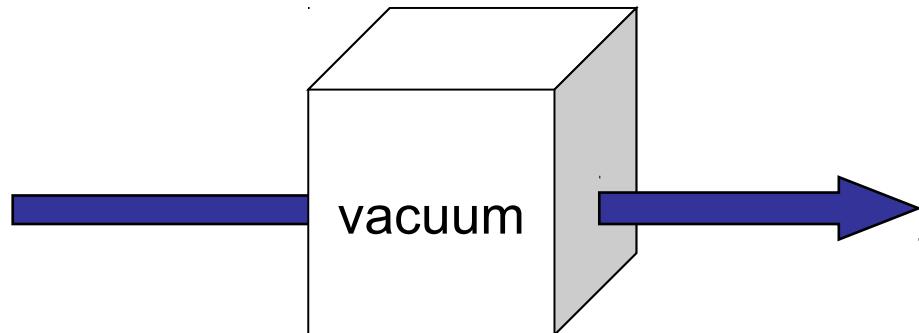
Affected by hadronic matter,  
in a well understood way, which  
can be accounted for (or neglected)



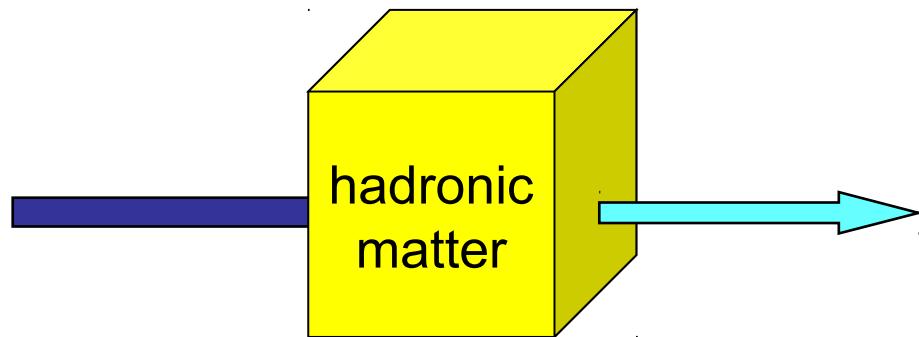
(see part III)

# Good probes of QCD matter

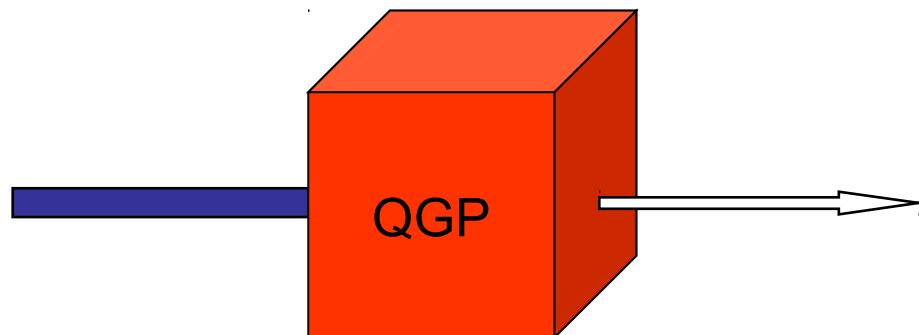
81



Well understood in “pp collisions”,  
and/or in control systems like pA



Affected by hadronic matter,  
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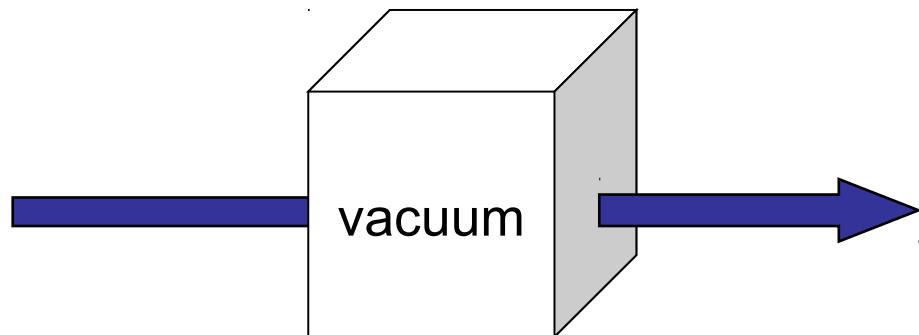


Strongly affected by the dense and  
deconfined QCD medium... and  
generated early in the collision!

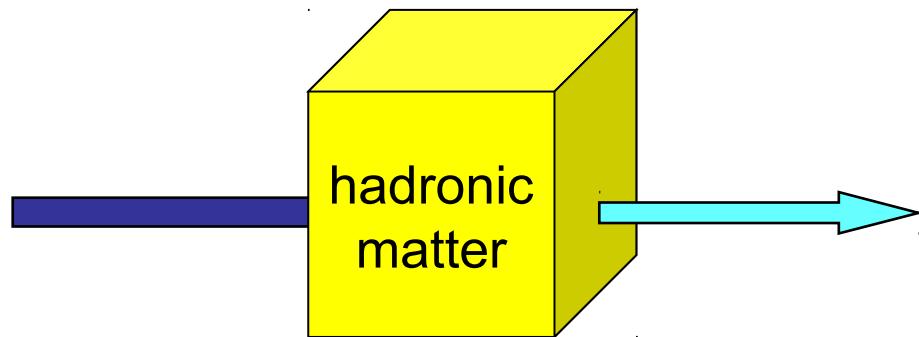
(see part III)

# Good probes of QCD matter

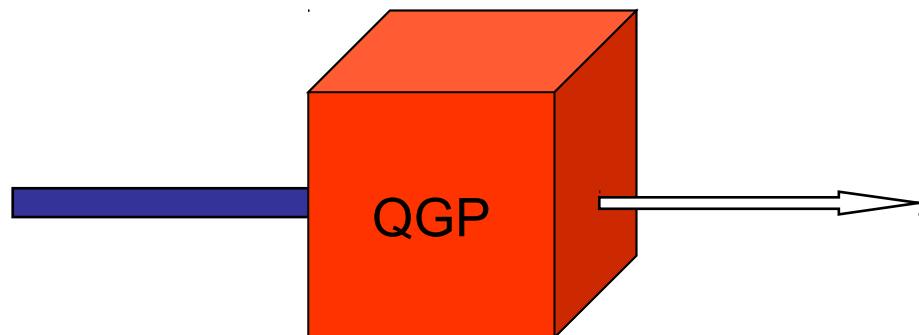
82



Well understood in “pp collisions”,  
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Affected by hadronic matter,  
in a well understood way, which  
can be accounted for (or neglected)



Strongly affected by the dense and  
deconfined QCD medium... and  
generated early in the collision!

Jets and heavy quarkonia ( $J/\psi$ ,  $\chi_c$ ,  $Y$ ,  $Y'$ , etc)  
are good QCD matter probes !

(see part III)

# Heavy-ion experiments

# Two main laboratories for heavy-ion collisions 84



**AGS** : 1986 – 2000

- Si and Au beams ;  $\sqrt{s} \sim 5$  GeV
- only hadronic variables

**RHIC** : 2000 – ?

- He3, Cu, Au beams ;  
up to  $\sqrt{s} = 200$  GeV
- 4 experiments (only two remain)

# Two main laboratories for heavy-ion collisions 85



**AGS** : 1986 – 2000

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- He3, Cu, Au beams ;  
up to  $\sqrt{s} = 200$  GeV
- 4 experiments (only two remain)

**SPS** : 1986 – 2003 + 2009 – ?

- O, S, In, Pb beams ;  $\sqrt{s} \sim 20$  GeV
- Various experiments in North Area

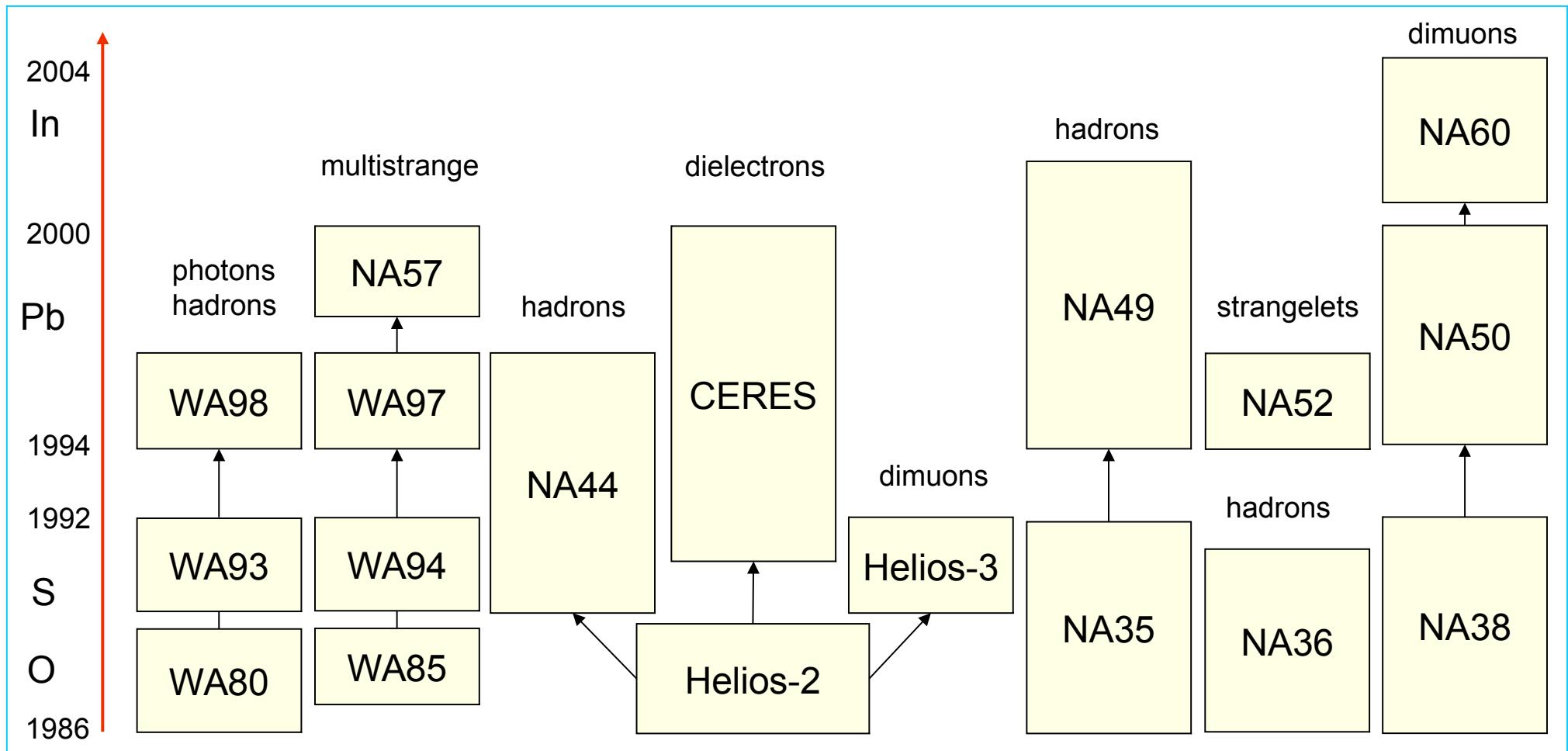
**LHC** : 2009 – ?

- Pb beams ; up to  $\sqrt{s} = 5000$  GeV
- ALICE, CMS, ATLAS and LHCb

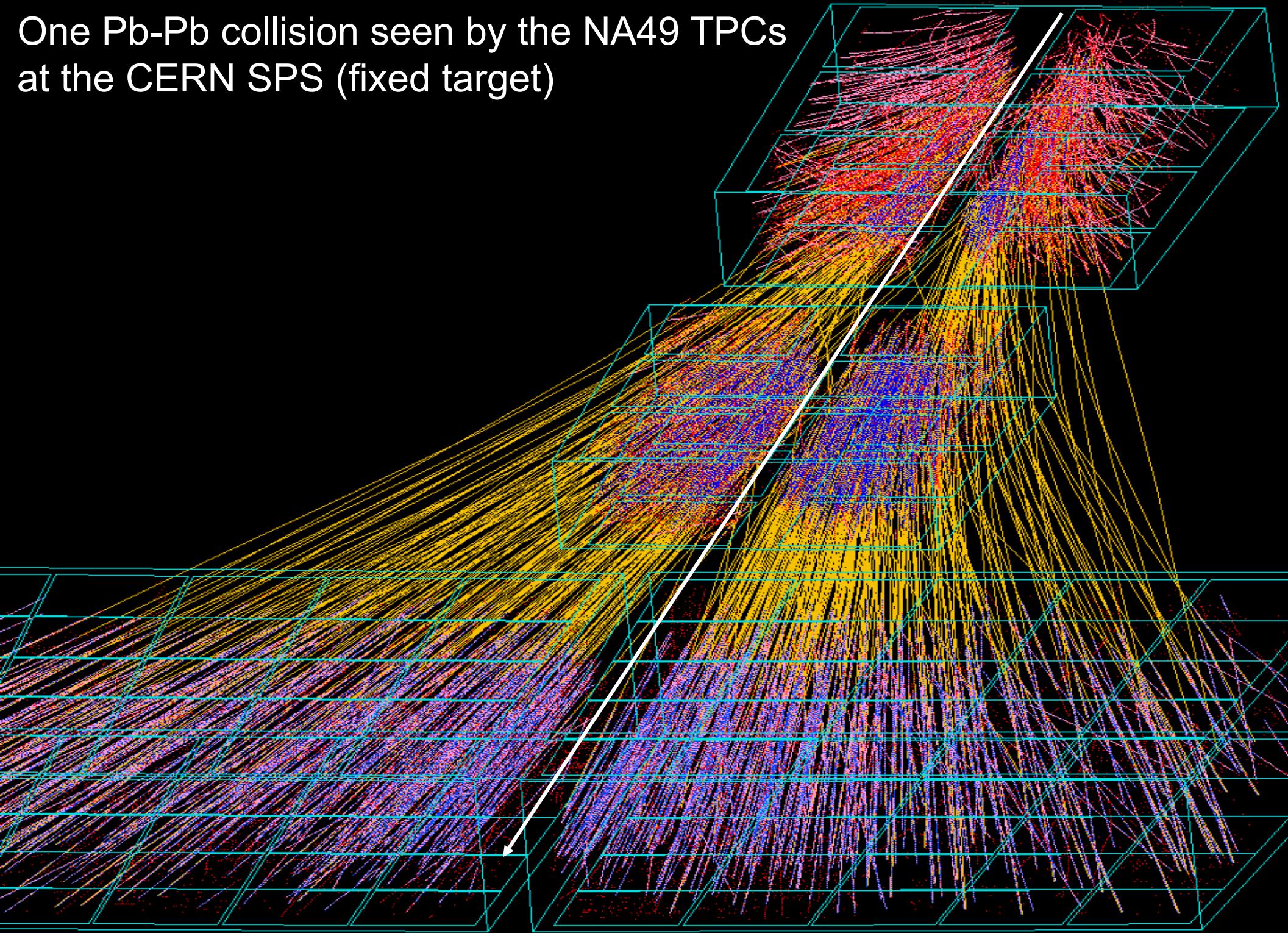
# The CERN SPS physics program

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Between 1986 and 2004, many experiments studied high-energy nuclear collisions at the CERN SPS, to probe hot QCD matter

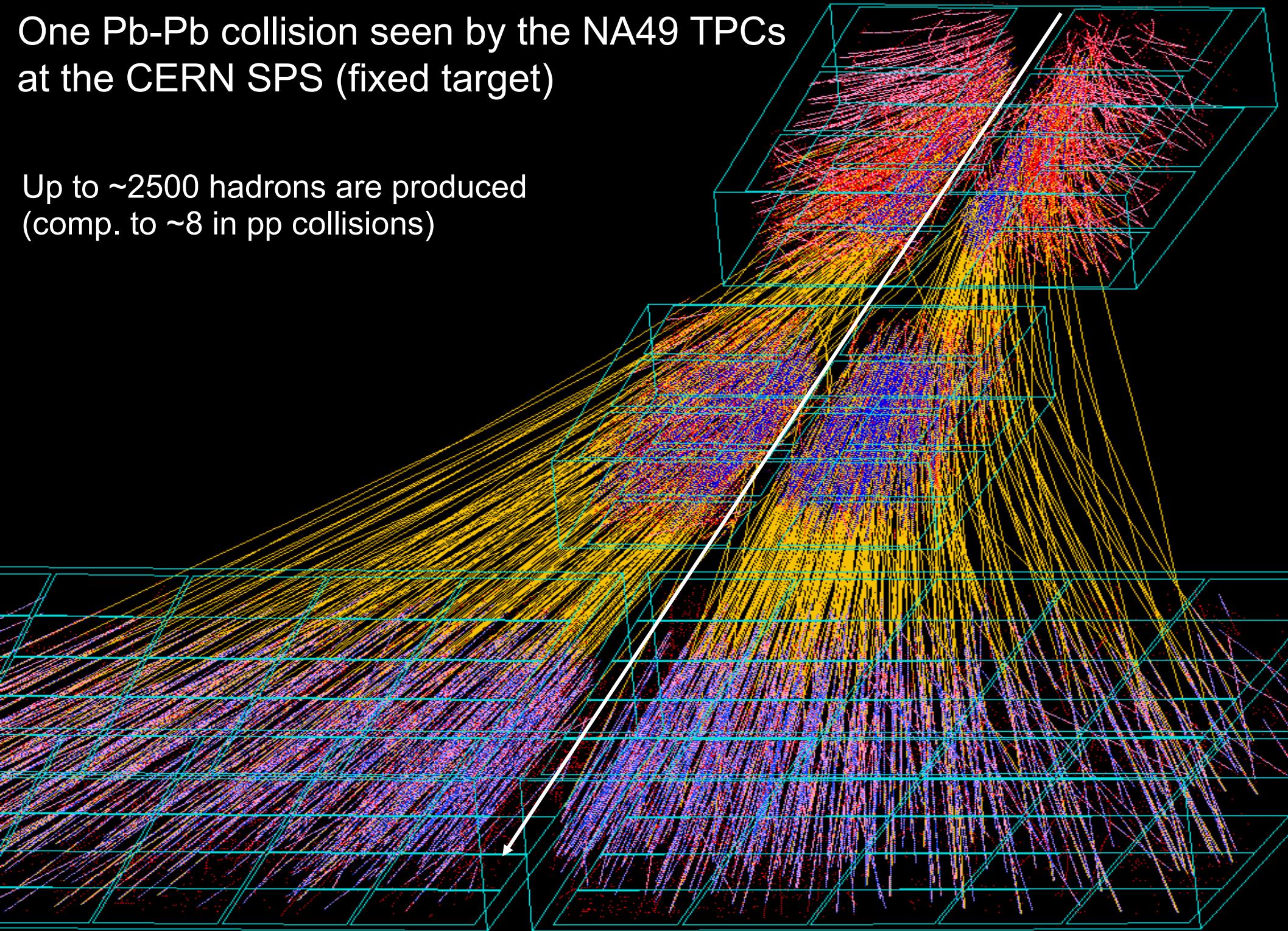


One Pb-Pb collision seen by the NA49 TPCs  
at the CERN SPS (fixed target)



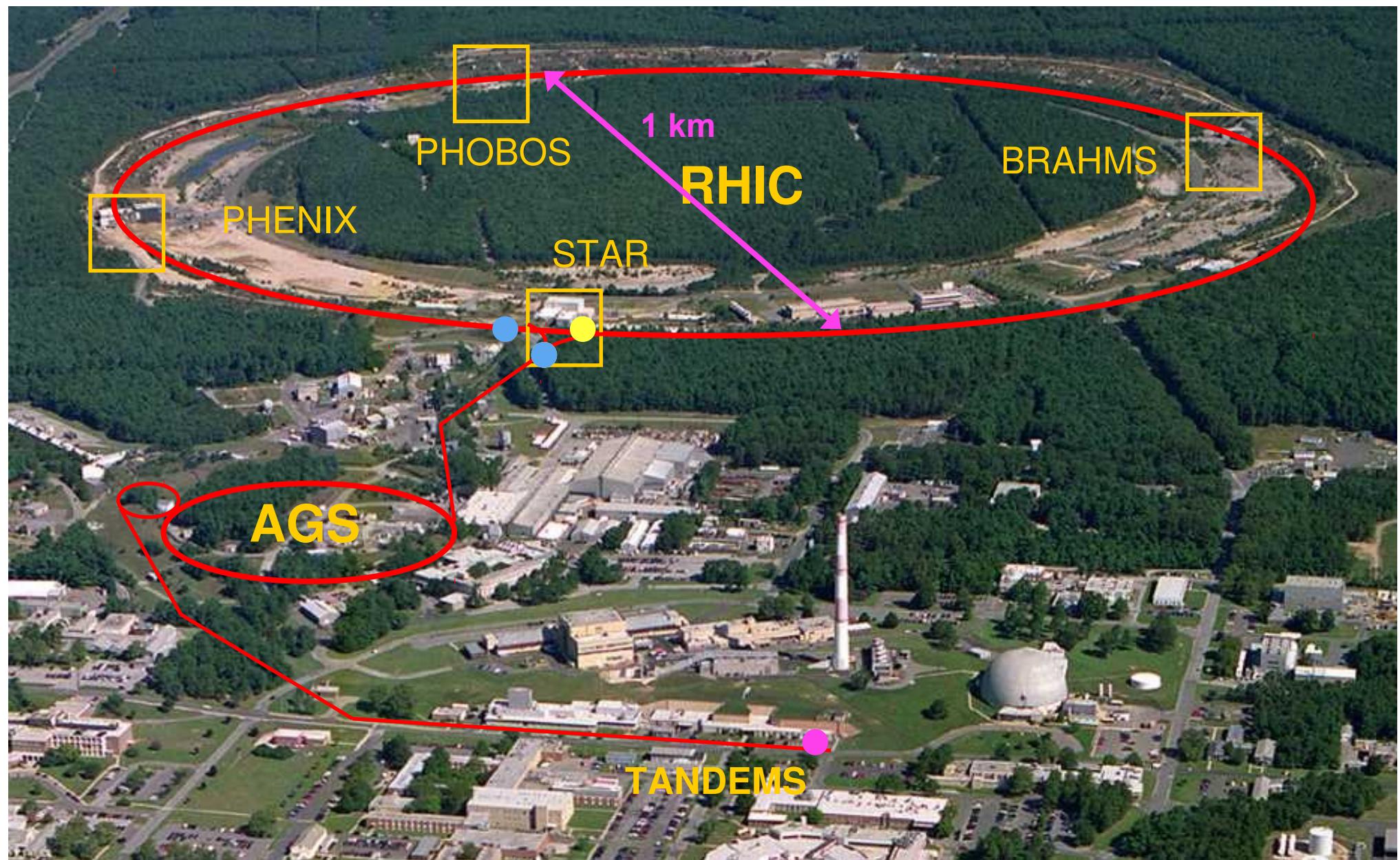
One Pb-Pb collision seen by the NA49 TPCs  
at the CERN SPS (fixed target)

Up to  $\sim$ 2500 hadrons are produced  
(comp. to  $\sim$ 8 in pp collisions)



# The Relativistic Heavy Ion Collider (RHIC)

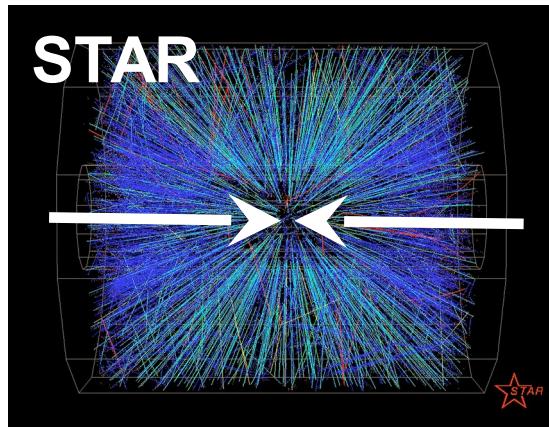
89



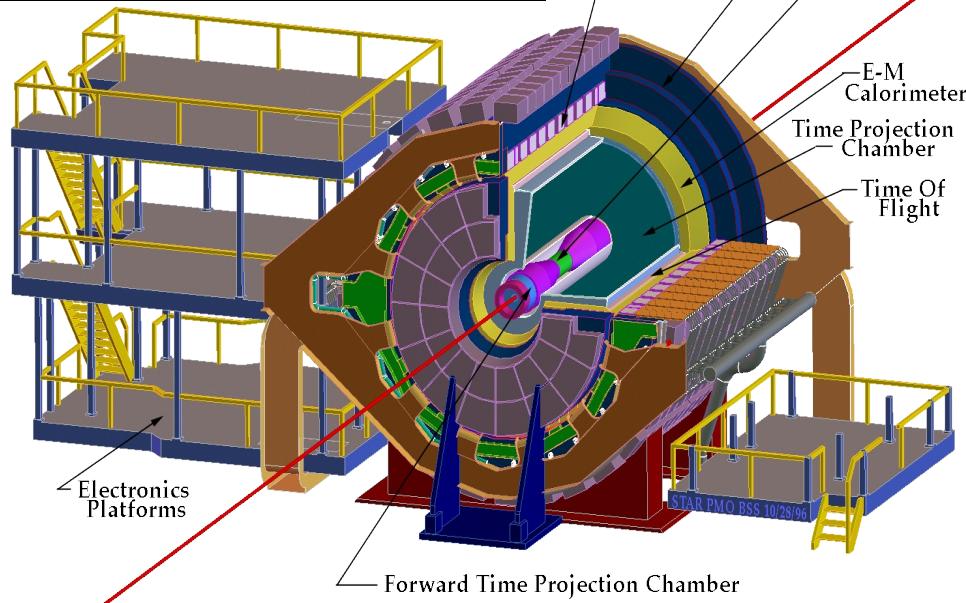
# STAR and PHENIX at RHIC

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**STAR**

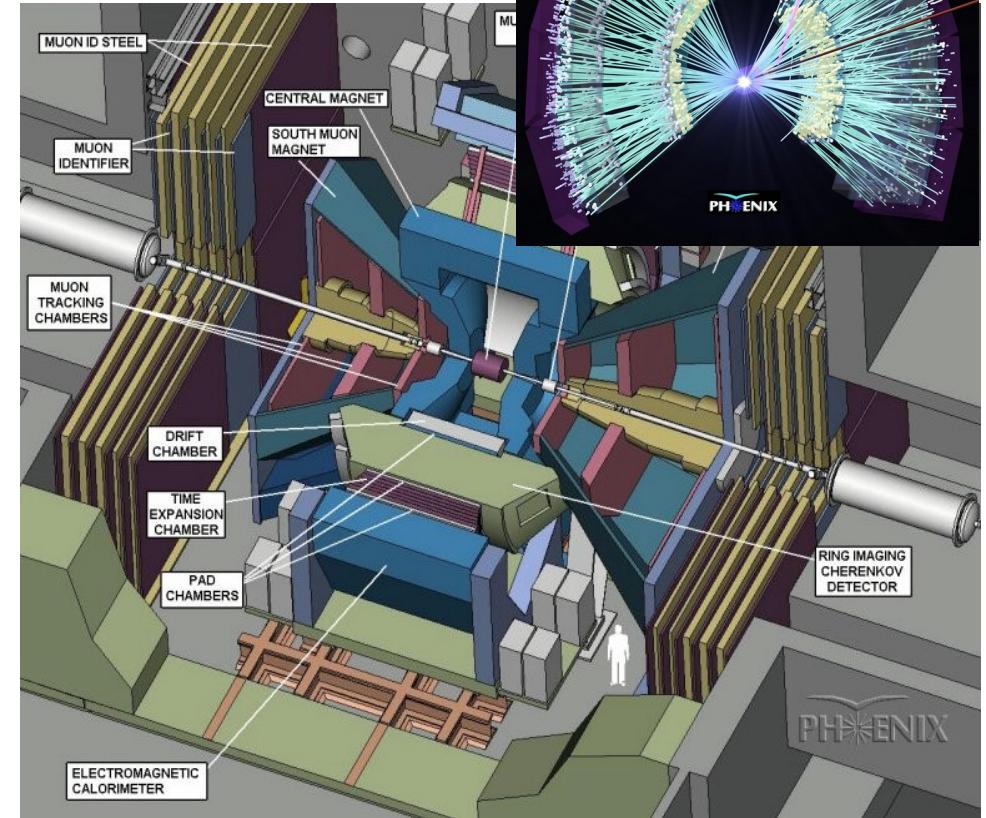


(PHOBOS, BRAHMS more specialized)



$2\pi$  coverage,  $-1 < \eta < 1$   
for tracking + (coarse) EMCAL  
PID by TOF,  $dE/dx$

Optimized for acceptance  
(correlations, jet-finding)



Partial cov.  $2 \times 0.5\pi$ ,  $-0.35 < \eta < 0.35$  for tracking + (finely) segmented calorimeter + forward muon arm, PID by RICH

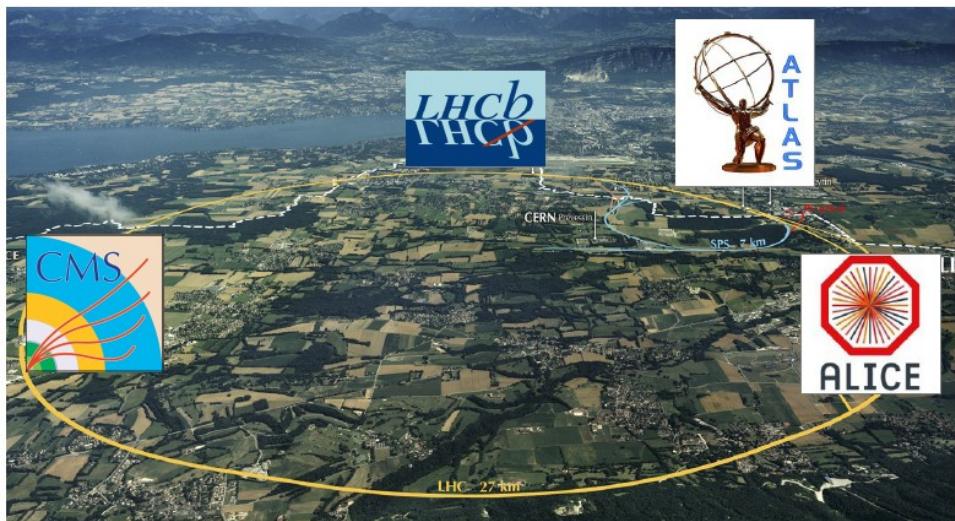
Optimized for high-pt  $\pi^0$ ,  $\gamma$ ,  $e$ ,  $J/\psi$   
(EMCal, high trigger rates)

# (Heavy-)Ion data-taking experiments at the LHC 91

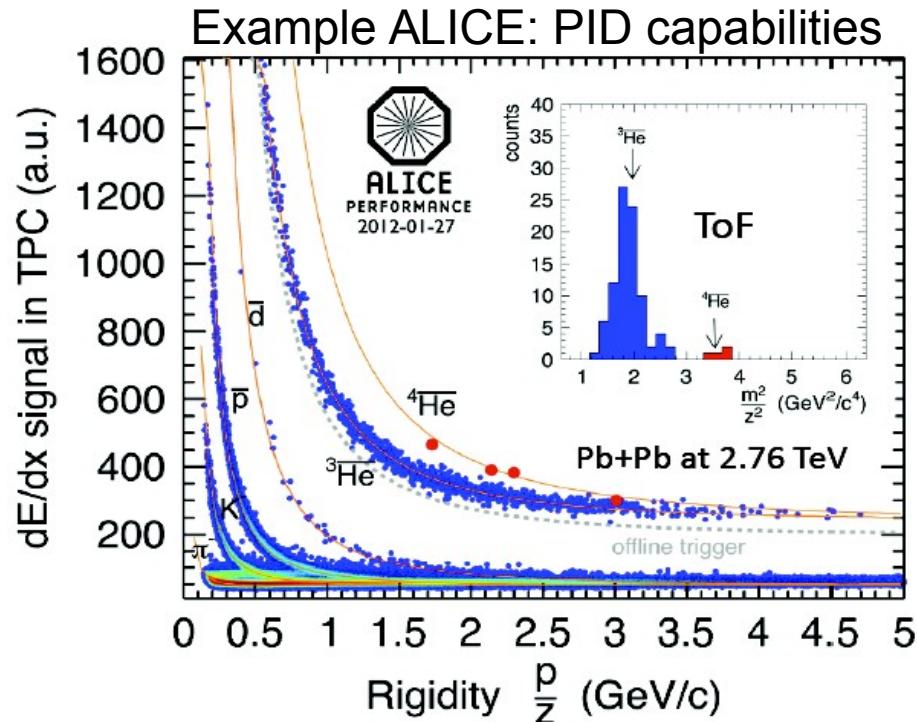


- ALICE dedicated HI experiment
  - Low- $p_T$  tracking, PID, mid-rapidity
  - Forward-muon spectrometer
- ATLAS/CMS large HEP experiments
  - Large acceptance, full calorimetry
- LHCb (pPb in 2013, PbPb since 2015)
  - Forward tracking, PID, calorimetry

# (Heavy-)Ion data-taking experiments at the LHC 92



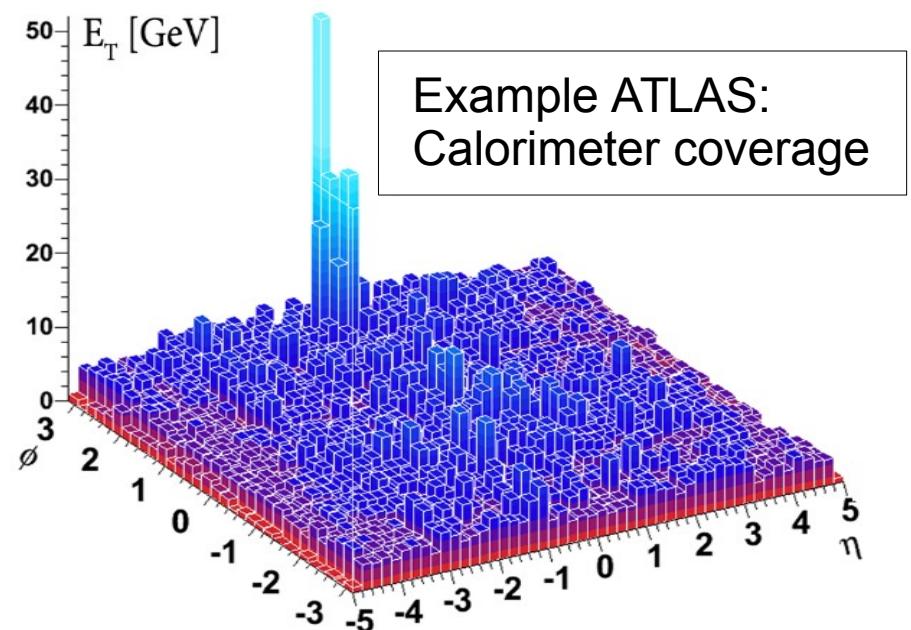
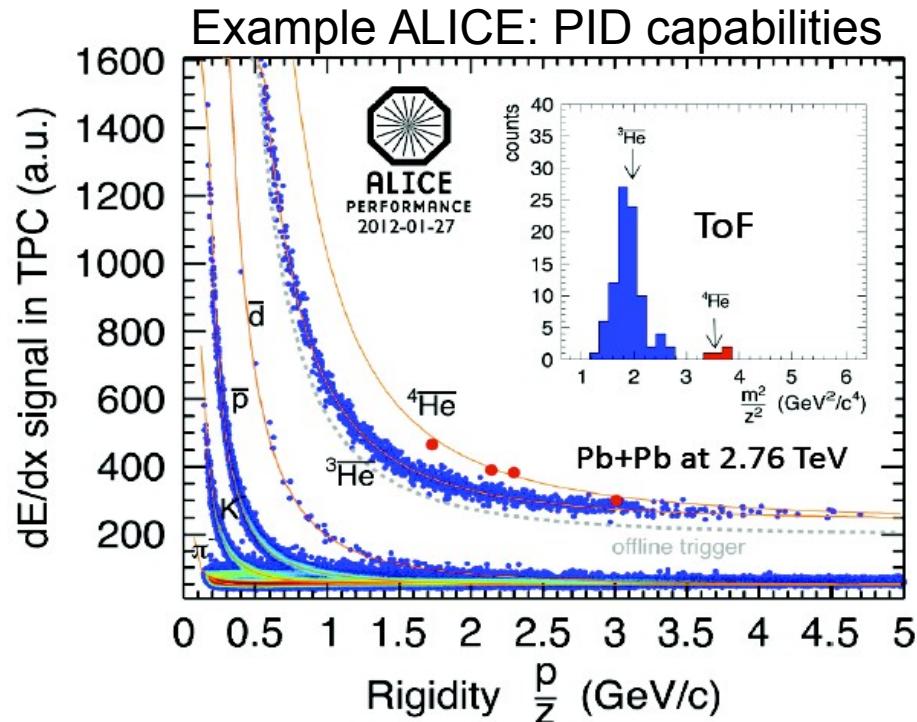
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# (Heavy-)Ion data-taking experiments at the LHC 93



- ALICE dedicated HI experiment
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  - Forward tracking, PID, calorimetry



- QCD is a quantum field theory with rich dynamical content, complex phase structure, and important open questions
- Heavy-ion collision experiments attempt to create and probe QCD matter at high temperature and energy density
- The scientific approach is conceptually similar to conventional scattering experiments, and relies on a series of well calibrated probes and a variety of collision systems

In the next two lectures we will look at a set of important results obtained from heavy-ion collisions at RHIC and LHC

If you have questions about today's lecture please send them to “cloizides atlbl dot gov”

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