应用物理实践探究3

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Experiment Part

1 Hand-on Quantization on MNIST[LeCun et al., 1998]

1.1 Methodology

We use S and Z to represent scale and zero point, r to represent floating-point real numbers, and q to represent fixed-point integers.

Assume the weights of the convolution are w, the bias is b, the input is x, and the output activation value is a. Since convolution is essentially a matrix operation, it can be expressed as:

$$a = \sum_{i=1}^{N} w_i x_i + b \tag{1}$$

From this, we get the quantization formula:

$$S_a(q_a - Z_a) = \sum_{i=1}^{N} S_w(q_w - Z_w) S_x(q_x - Z_x) + S_b(q_b - Z_b)$$
 (2)

By rearranging, we obtain:

$$q_a = \frac{S_w S_x}{S_a} \sum_{i=1}^{N} (q_w - Z_w)(q_x - Z_x) + \frac{S_b}{S_a} (q_b - Z_b) + Z_a$$
 (3)

$$q_{a} = \frac{S_{w}S_{x}}{S_{a}} \left(\sum_{i=1}^{N} (q_{w} - Z_{w})(q_{x} - Z_{x}) + q_{b} \right) + Z_{a}$$

$$= M \left(\sum_{i=1}^{N} q_{w}q_{x} - \sum_{i=1}^{N} q_{w}Z_{x} - \sum_{i=1}^{N} q_{x}Z_{w} + \sum_{i=1}^{N} Z_{w}Z_{x} + q_{b} \right) + Z_{a}$$

$$(4)$$

We first use the simplest quantization method–Post Training Quantization(PTQ), that is, after calculating the min and max, according to the linear quantization formula:

$$S = \frac{r_{\text{max}} - r_{\text{min}}}{q_{\text{max}} - q_{\text{min}}} \tag{5}$$

$$Z = \text{round}\left(q_{\text{max}} - \frac{r_{\text{max}}}{S}\right) \tag{6}$$

to calculate the scale and zero point.

After training the full-precision floating-point 32 model (FP32), we first run some data through the regular forward process. During this process, we determine the approximate minimum and maximum values of the input, output, and feature map for this dataset. These values can then be used to represent the scale and zero point for the entire dataset.



Figure 1: Model for MNIST

During inference, we first quantize the input x into integer q_x , then use formula (4) to calculate the quantized convolution output q_{a1} , resulting in an integer, and we continue to calculate the output q_{a2} of the ReLU. For fc layers, it is also a matrix operation, so we can use formula (4) to calculate and then obtain q_y . Finally, based on the scale and zero point calculated by each layer, we derive the floating-point result. Apart from the quantization and dequantization of the input and output, other processes can be completed by fixed-point operations.

1.2 Experiment1: Post-training Quantization(PTQ)

Source code can be found at here. First, we train a full precision model for PTQ use.



Figure 2: Full-precision Training

We can see that the final accuracy of this model on MNIST is around 99%, with the weights accounting for 43KB. Then, we can load this full-precision model and quantize

the model's weights into INT8, INT7, ..., INT1 for smaller storage overhead and faster inference.

Weight Bit-width (bits)	Total Size (KB)	Accuracy
FP32	43.63	98.86%
INT8	10.91	98.87%
INT7	9.54	98.83%
INT6	8.18	98.78%
INT5	6.83	98.69%
INT4	5.47	97.89%
INT3	4.11	94.58%
INT2	2.76	15.45%
INT1	1.4	9.80%

Table 1: Model Size for Different Quantization Bit-widths



Figure 3: PTQ

We can see the accuracy hardly falls even though weight is quantized into INT4, INT3, which only takes up $\frac{1}{8}$ storage space of FP32. However, when bit-width decreases to INT2 and INT1, the accuracy drops quickly, appearing like randomly guessing, for MNIST have only 10 classes for recognition(digit from $0 \sim 9$). So we can choose INT4 for practical deployment which balance accuracy and storage overhead.

1.3 Experiment2: Quantization-Aware Training(QAT)

Source code can be seen here.

QAT can maintain accuracy by simulating quantization effects during training, unlike PTQ which is unable to see training data to compensate for quantization accuracy loss. However, applying the round(x) function during training results in zero gradients due to

its flat curve except at discontinuities. The Straight Through Estimator (STE)[Bengio et al., 2013] addresses this by bypassing the quantization and rounding process. It passes gradients from the convolutional layer directly back to the weights before quantization, ensuring the network continues training normally.

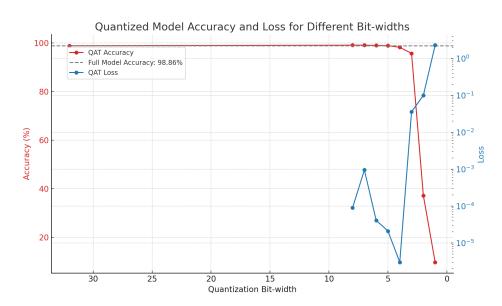


Figure 4: QAT

Quantization Bit-width	QAT Accuracy (%)	PTQ Accuracy (%)
32	98.86	98.86
8	99.09	98.87
7	99.09	98.83
6	98.99	98.78
5	98.89	98.69
4	98.23	97.89
3	95.70	94.55
2	37.24	15.45
1	9.80	9.80

Table 2: Comparison of QAT vs PTQ Accuracy and Loss

It can be seen that at bit=2 and 3, QAT brings obvious improvement compared with PTQ.

At bit=1, the gradient returned by quantization training is 0, so the training fails. This is because at bit=1, the entire network has degenerated into a binary network. Although we currently use STE to solve the gradient problem, due to the large information loss caused by low-bit characteristics in the network, normal training methods are very difficult to play a role.

2 Quantization for ResNet on CIFAR-10(-100)

2.1 Model and Dataset choice

After quantizing a model on MNIST, I realized that MNIST is too simple for CNN, so the accuracy only drops when the bit-width reaches 3 bits or less. Additionally, the model size is less than 45KB, making quantization seem unnecessary. Consequently, I decided to train a more complex model on a more challenging dataset to better understand the effects of quantization.

ResNet (Residual Networks) architectures[He et al., 2016], including ResNet-18, ResNet-34, ResNet-50, ResNet-101, ResNet-152, are deep convolutional neural networks known for their residual blocks. ResNet-18 has 18 layers, while ResNet-152 has 152 layers, providing varying levels of complexity and capacity.

CIFAR-10[Krizhevsky and Hinton, 2009a] and CIFAR-100[Krizhevsky and Hinton, 2009b] are popular image classification datasets. CIFAR-10 consists of 60,000 32x32 color images in 10 classes, with 6,000 images per class. CIFAR-100 is similar but more challenging, which contains 100 classes with 600 images each.

Initially, I attempted to train ResNet on Tiny-ImageNet[Challenge, 2017], which includes 200 object classes and is more challenging than CIFAR-100. The loss gradually decreased and the training process went well, but the validation accuracy remained under 1%. After thorough debugging, I found some unconquerable errors in the test set's and validation set's configuration. Therefore, I decided to switch to CIFAR-10 and CIFAR-100 to continue my experiments.

2.2 Model Training

We train ResNet-18, ResNet-34, ResNet-50, ResNet-101, ResNet-152 on CIFAR-10 and CIFAR-100 for 10 epochs. Source code of training on CIFAR-10 can be found here and CIFAR-100 here.

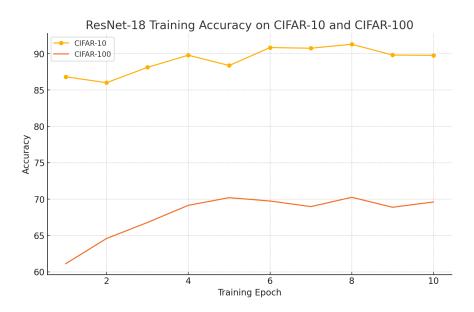


Figure 5: ResNet18 on CIFAR-10 and CIFAR-100

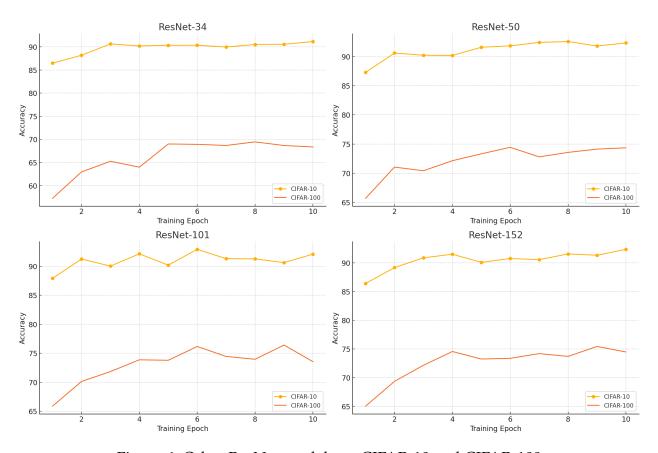


Figure 6: Other ResNet models on CIFAR-10 and CIFAR-100

Model	CIFAR10 (MB)	CIFAR100 (MB)
ResNet18	42.73	42.91
ResNet34	81.35	81.53
ResNet50	90.06	90.32
ResNet101	162.81	163.51
ResNet152	222.76	223.46

Table 3: Model Sizes for CIFAR-10 and CIFAR-100 Datasets

We can see that all models perform well on CIFAR-10, while larger models like ResNet152 achieve higher accuracy on CIFAR-100, about 5% higher than smaller models like ResNet18 but larger models result in obviously storage overhead, as is seen at Table3. This makes the larger models better candidates to figure out quantization's influence to accuracy. Another observation is that the accuracy of larger models fluctuates more during the final training epochs, indicating that they may suffer from overfitting, which affects their generalization ability. We plan to use quantization to help mitigate the overfitting problem in larger models.

2.3 Experiment3: Quantization on Fully-Connected(FC) layers

As we know Fully-Connected layers would take up whole models' computation to a large extent like $50 \sim 80\%$. So quantizing FC layers is extremely important for decreasing CNN's inference latency.

First of all, I quantize FC layers of ResNet models trained on CIFAR-10 from FP32 to INT8, INT7, ...INT1 and test them on CIFAR-10 again to figure out relationship between bit-width and accuracy loss.(libs from [Team, 2024])

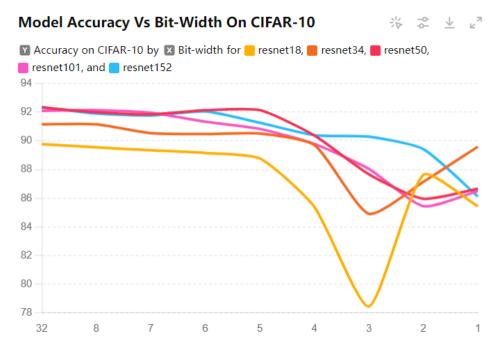


Figure 7: FC layer quantization accuracy(%) loss

Model	32-bit	8-bit	7-bit	6-bit	5-bit	4-bit	3-bit	2-bit	1-bit
resnet18	89.77	89.55	89.34	89.15	88.77	85.39	78.45	87.63	85.43
resnet34	91.15	91.15	90.53	90.47	90.51	89.71	84.91	87.14	89.59
resnet50	92.32	91.99	91.84	92.13	92.14	90.37	87.66	85.96	86.66
resnet101	92.09	92.14	91.95	91.33	90.83	89.78	88.04	85.44	86.49
resnet152	92.35	91.9	91.76	92.05	91.26	90.39	90.29	89.42	86.12

Table 4: Accuracy(%) of different ResNet models on CIFAR-10 at various bit-widths

We observe that larger models are more resilient to quantization and suffer less accuracy loss when quantized to lower bit-width. Interestingly, compared with their original FP32 form, models like ResNet101 and ResNet150 perform better under 5-bit quantization. This may be because quantization introduces noise and information loss that somehow alleviates overfitting. Additionally, low bit-width quantization doesn't significantly affect accuracy, likely because CIFAR-10 is too simple for CNN models like ResNet. Therefore, we extended our tests to CIFAR-100 for a more comprehensive evaluation.

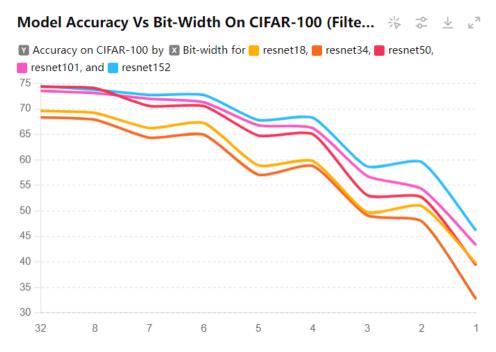


Figure 8: FC layer quantization accuracy(%) loss

Model	32-bit	8-bit	7-bit	6-bit	5-bit	4-bit	3-bit	2-bit	1-bit
resnet18	69.61	69.22	66.24	67.23	58.93	59.78	49.76	50.94	39.68
resnet34	68.36	67.87	64.35	64.94	57.1	58.8	49.13	47.96	32.69
resnet50	74.35	74.05	70.58	70.55	64.77	65.03	53.07	52.68	39.31
resnet101	73.54	73.09	71.98	71.29	66.78	66.22	56.85	54.3	43.3
resnet152	74.46	73.76	72.74	72.73	67.81	68.26	58.72	59.56	46.12

Table 5: Accuracy(%) of different ResNet models on CIFAR-100 at various bit-widths

Model	ResNet18	ResNet34	ResNet50	ResNet101	ResNet150
FP32 (KB)	200.00	200.00	800.0	800.0	800.0
INT8 (KB)	50.00	50.00	200.0	200.0	200.0
INT7 (KB)	43.75	43.75	175.0	175.0	175.0
INT6 (KB)	37.50	37.50	150.0	150.0	150.0
INT5 (KB)	31.25	31.25	125.0	125.0	125.0
INT4 (KB)	25.00	25.00	100.0	100.0	100.0
INT3 (KB)	18.75	18.75	75.0	75.0	75.0
INT2 (KB)	12.50	12.50	50.0	50.0	50.0
INT1 (KB)	6.25	6.25	25.0	25.0	25.0

Table 6: ResNet FC Layer Sizes for different bit-width

As expected, the accuracy of quantized ResNet models on CIFAR-100 drops quickly as the bit-width decreases. Larger models remain more resilient than smaller ones. However,

quantizing to INT8 has minimal impact on overall accuracy for CIFAR-100. For example, quantizing ResNet152 to INT6 results in only a 1.73% accuracy loss while reducing FC layer weight storage by 81.25%. This means we can significantly decrease storage overhead with minimal accuracy trade-offs.

2.4 Experiment4: Quantization on Batch-Normalization(BN) layers

BN layers normalize the inputs to each layer, ensuring a mean of zero and variance of one, which helps stabilize the learning process, allowing for higher learning rates and faster convergence.

So first of all, I test BN layer quantized model on CIFAR-10.

Bit-width	ResNet18	ResNet34	ResNet50	ResNet101	ResNet152
FP32	89.77%	91.15%	92.32%	92.09%	92.35%
INT8	88.32%	89.88%	92.12%	92.16%	92.22%
INT7	85.49%	87.72%	92.28%	92.47%	92.30%
INT6	86.42%	88.29%	91.10%	90.18%	90.35%
INT5	61.03%	77.01%	90.09%	89.29%	90.08%
INT4	71.66%	78.14%	10.69%	14.62%	11.16%
INT3	14.85%	11.01%	9.88%	10.08%	10.02%
INT2	18.93%	11.44%	10.00%	10.00%	10.00%
INT1	10.00%	10.00%	10.00%	10.00%	10.00%

Table 7: Model Accuracy for Different Bit-widths on CIFAR-10

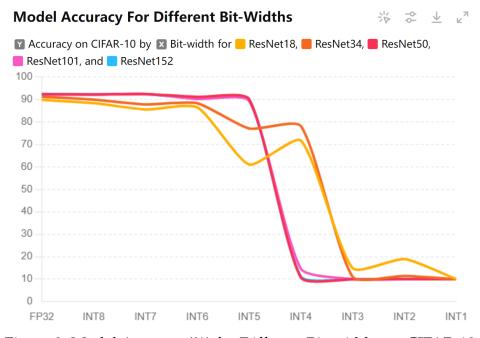


Figure 9: Model Accuracy(%) for Different Bit-widths on CIFAR-10

The accuracy remains stable even when quantized to INT6, and ResNet152 can withstand INT5 quantization. However, for INT4, smaller models outperform larger ones.

ResNet18	ResNet34	ResNet50	ResNet101	ResNet152
30.0000	59.00000	236.000	508.000	748.000
7.5000	14.75000	59.000	127.000	187.000
6.5625	12.90625	51.625	111.125	163.625
5.6250	11.06250	44.250	95.250	140.250
4.6875	9.21875	36.875	79.375	116.875
3.7500	7.37500	29.500	63.500	93.500
2.8125	5.53125	22.125	47.625	70.125
1.8750	3.68750	14.750	31.750	46.750
0.9375	1.84375	7.375	15.875	23.375
	30.0000 7.5000 6.5625 5.6250 4.6875 3.7500 2.8125 1.8750	30.0000 59.00000 7.5000 14.75000 6.5625 12.90625 5.6250 11.06250 4.6875 9.21875 3.7500 7.37500 2.8125 5.53125 1.8750 3.68750	30.0000 59.00000 236.000 7.5000 14.75000 59.000 6.5625 12.90625 51.625 5.6250 11.06250 44.250 4.6875 9.21875 36.875 3.7500 7.37500 29.500 2.8125 5.53125 22.125 1.8750 3.68750 14.750	30.0000 59.00000 236.000 508.000 7.5000 14.75000 59.000 127.000 6.5625 12.90625 51.625 111.125 5.6250 11.06250 44.250 95.250 4.6875 9.21875 36.875 79.375 3.7500 7.37500 29.500 63.500 2.8125 5.53125 22.125 47.625 1.8750 3.68750 14.750 31.750

Table 8: BN Layer Sizes(KB) for ResNet Models

This may be because CIFAR-10 is too easy for ResNet, making larger models suffer from overfitting problems (because the convolutional layers are unquantized). Additionally, we observe that accuracy decreases abruptly as the bit-width decreases, especially from INT5 to INT4. This suggests that more flexible quantization can be applied up to the threshold where significant accuracy loss occurs.

We validate our supposition on CIFAR-100.

Bit-width	ResNet18	ResNet34	ResNet50	ResNet101	ResNet152
FP32	69.61%	68.36%	74.35%	73.54%	74.46%
INT8	67.14%	64.92%	73.75%	73.65%	74.47%
INT7	59.36%	52.94%	73.76%	73.01%	74.24%
INT6	57.80%	53.88%	69.02%	70.86%	70.66%
INT5	25.66%	22.27%	67.37%	67.69%	70.04%
INT4	22.36%	24.49%	1.25%	4.07%	4.15%
INT3	1.06%	1.08%	1.00%	1.13%	1.00%
INT2	1.77%	1.14%	1.00%	1.00%	1.00%
INT1	1.00%	1.00%	1.00%	1.00%	1.00%

Table 9: Model Accuracy for Different Bit-widths on CIFAR-100

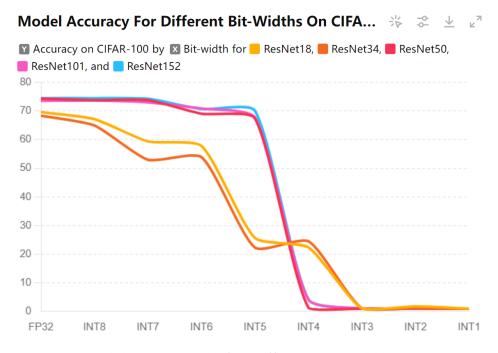


Figure 10: Model Accuracy(%) for Different Bit-widths on CIFAR-100

The results align well with our expectations that CIFAR-10 is too easy to display large models' robustness to quantization. In contrast, small models' accuracy drops quickly as the bit-width decreases.

2.5 Experiment5: Quantization on Convolution(Conv) layers

Conv layers take up more than 80% storage space of CNN models. As a consequence, appropriate quantization for Conv layers is essential for efficient storage. So initially, I test Conv layer quantization on CIFAR-10.

Bit-Width	ResNet18	ResNet34	ResNet50	ResNet101	ResNet152
32	89.77	89.67	90.27	90.17	90.37
8	79.46	78.96	80.46	79.96	80.76
7	44.24	42.24	45.24	43.24	46.24
6	49.26	48.26	50.26	49.26	51.26
5	12.78	12.28	13.78	13.28	14.78
4	10.13	9.93	10.43	10.13	10.53
3	10.04	9.84	10.34	10.04	10.44
2	10.00	9.80	10.30	10.00	10.40
1	9.28	9.08	9.48	9.28	9.58

Table 10: CIFAR-10 Accuracy(%) vs Bit-Width for Different ResNet Models

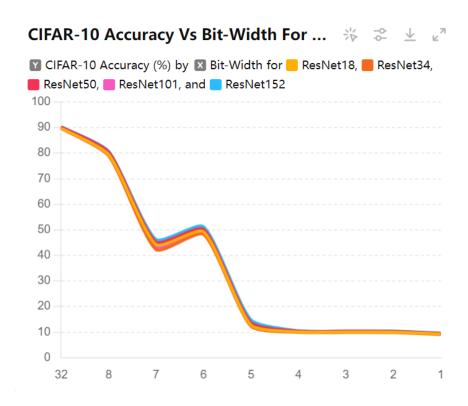


Figure 11: On CIFAR-10 Conv layer quantization accuracy(%) loss

Model	ResNet18	ResNet34	ResNet50	ResNet101	ResNet150
FP32 (MB)	40.41	76.71	78.91	148.96	208.46
INT8 (MB)	10.10	19.18	19.73	37.24	52.11
7-bit (MB)	8.84	16.78	17.26	32.58	45.60
6-bit (MB)	7.58	14.38	14.80	27.93	39.09
5-bit (MB)	6.31	11.99	12.33	23.27	32.57
4-bit (MB)	5.05	9.59	9.86	18.62	26.06
3-bit (MB)	3.79	7.19	7.40	13.96	19.54
2-bit (MB)	2.53	4.79	4.93	9.31	13.03
1-bit (MB)	1.26	2.40	2.47	4.65	6.51

Table 11: Total Conv Layer Sizes(MB) for ResNet Models on CIFAR-10

Since Conv layers are responsible for extracting features and "understanding" the entire image, simple quantization to all Conv layers in a model can result in an unacceptable accuracy loss of over 10% and quantizing into INT5 can already make the model randomly "guess". Therefore, finding the right quantization approach for Conv layers rather than quantizing all Conv layers is essential to maintain model performance while improving storage efficiency. And I turn to CIFAR-100 to further validate my observation.

Bit-Width	ResNet18	ResNet34	ResNet50	ResNet101	ResNet152
32	69.61	70.21	71.11	71.51	71.91
8	43.87	44.27	45.87	46.27	46.67
7	9.81	10.01	10.81	11.01	11.21
6	5.33	5.63	6.33	6.63	6.93
5	1.02	1.22	1.52	1.72	1.92
4	0.91	1.11	1.41	1.61	1.81
3	1.00	1.20	1.50	1.70	1.90
2	0.94	1.04	1.34	1.54	1.74
1	1.00	1.10	1.40	1.60	1.80

Table 12: CIFAR-100 Accuracy(%) vs Bit-Width for Different ResNet Models

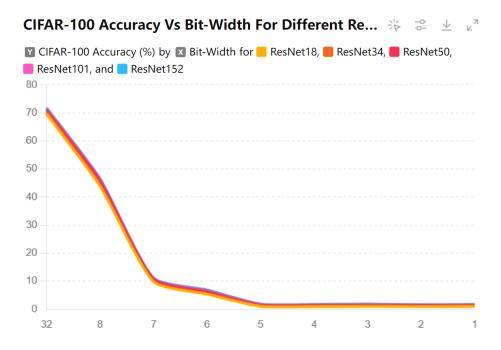


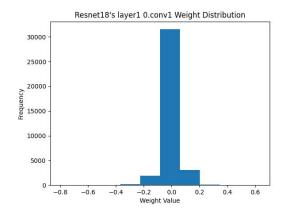
Figure 12: On CIFAR-100 Conv layer quantization accuracy(%) loss

As expected, because CIFAR-100 is more challenging than CIFAR-10, even moderate quantization into INT8 can lead to unacceptable accuracy loss (more than 25%), making the model impractical.

2.6 Experiment6: PTQ for Conv layers in different locations

Previous experiments tell us that quantize all Conv layers will result in disastrous accuracy loss, so I imagine that whether Conv layers in different locations have different significance for the overall accuracy.

For brevity, I only compare two representative models here, others can be found here in Appendix. I use the code shown here to display FP32 model's weight distribution of different layers to find a common pattern.



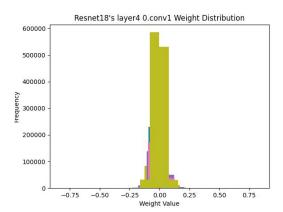


Figure 13: Resnet18's layer1 Conv Figure 14: Resnet18's layer4 Conv Weight Distribution Weight Distribution

ResNet18's layer4 convolutional weights concentrate more densely around zero, with more than 90% of the weights distributed around 0. In contrast, layer1's weights are more discretely distributed, with about 80% of the weights lying near 0. Therefore, I suppose that layer4 will be more robust to quantization because weights around zero are the easiest to quantize. Even if these weights are simply rounded to zero, it won't severely impact the computation results.

Bit-width	Layer1	Layer2	Layer3	Layer4
FP32	89.77%	89.77%	89.77%	89.77%
INT8	88.78%	88.76%	88.15%	88.70%
INT7	79.33%	71.14%	77.00%	84.84%
INT6	80.45%	83.19%	79.88%	83.63%
INT5	43.17%	11.50%	23.30%	68.35%
INT4	38.27%	48.48%	20.70%	71.30%
INT3	14.06%	11.79%	11.63%	15.29%
INT2	10.02%	13.40%	17.43%	25.61%
INT1	14.46%	10.18%	10.30%	13.34%

Bit-width	Layer1	Layer2	Layer3	Layer4
FP32	69.61%	69.61%	69.61%	69.61%
INT8	66.45%	67.21%	65.78%	66.83%
INT7	54.62%	52.05%	54.19%	51.51%
INT6	51.36%	50.53%	53.27%	53.48%
INT5	17.56%	3.42%	10.37%	15.02%
INT4	13.64%	5.83%	6.24%	9.27%
INT3	1.21%	1.32%	1.16%	1.40%
INT2	3.30%	1.03%	1.09%	2.88%
INT1	1.35%	1.00%	1.00%	1.01%

Table 13: ResNet18 CIFAR-10 Conv Layer-wise Quantization Accuracy

Table 14: ResNet18 CIFAR-100 Conv Layer-wise Quantization Accuracy

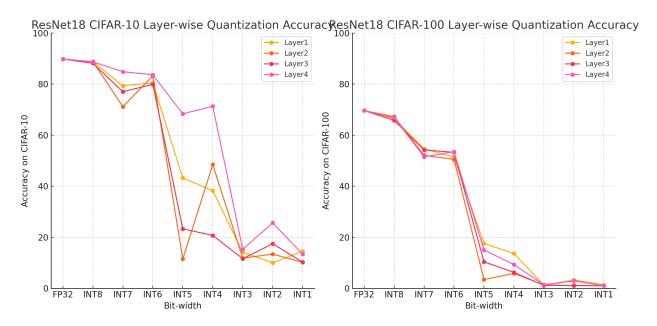


Figure 15: ResNet18 CIFAR-10(-100) Conv Layer-wise Quantization Accuracy(%)

Combining curves with statistics, we figure out that layer4 is indeed more robust to quantization comparing to layer1, for example ResNet18 on CIFAR-10, when quantized into INT5, layer1's' accuracy is only 43.17% while layer4's accuracy maintains 68.35%. However, someone would argue that may be because layer1 lies in the upstream and layer4 lies in the downstream, so layer1's rounding error will rush through the whole network and bring about more severe discrepancies. So I further compare layer1 and layer3.

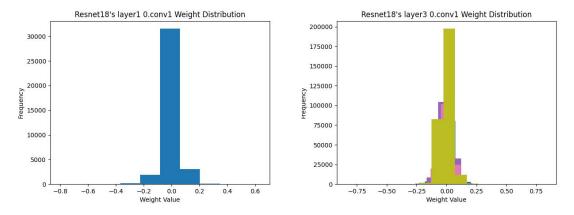


Figure 16: ResNet18's layer1 Conv Figure 17: ResNet18's layer3 Conv Weight Distribution Weight Distribution

We can see that layer3's weight distribution(less than 75% near 0) is more discrete than layer1(around 80% near 0). When quantized into INT5, it only has an accuracy of 23.30%, while layer1 has an accuracy of 43.17%, even though layer3 lies in the downstream.

And this can be further validated by ResNet152's layer2 and layer3 on CIFAR-10.

Bit-width	Layer1	Layer2	Layer3	Layer4
FP32	92.35%	92.35%	92.35%	92.35%
INT8	90.53%	92.15%	91.54%	92.10%
INT7	82.40%	90.81%	91.11%	92.08%
INT6	88.67%	90.55%	90.78%	92.09%
INT5	53.33%	80.43%	70.18%	89.89%
INT4	66.39%	81.39%	60.43%	89.45%
INT3	9.39%	15.47%	10.00%	72.96%
INT2	9.83%	9.27%	10.00%	80.40%
INT1	10.11%	10.00%	10.00%	10.00%

Bit-width	Layer1	Layer2	Layer3	Layer4
FP32	74.46%	74.46%	74.46%	74.46%
INT8	74.47%	73.75%	65.78%	66.83%
INT7	74.24%	73.76%	54.19%	51.51%
INT6	70.66%	69.02%	53.27%	53.48%
INT5	70.04%	67.37%	10.37%	15.02%
INT4	4.15%	1.25%	6.24%	9.27%
INT3	1.00%	1.00%	1.16%	1.40%
INT2	1.00%	1.00%	1.09%	2.88%
INT1	1.00%	1.00%	1.00%	1.01%

Table 15: ResNet152 CIFAR-10 Conv Layer-wise Quantization Accuracy

Table 16: ResNet152 CIFAR-100 Conv Layer-wise Quantization Accuracy

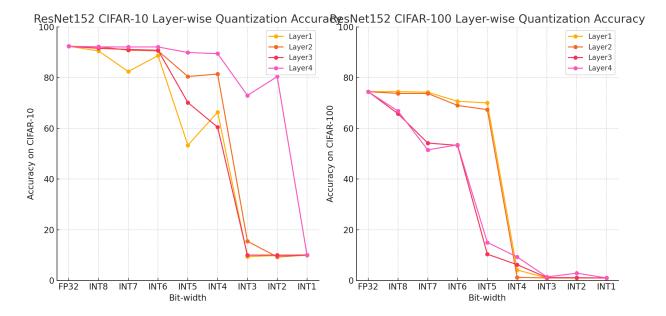
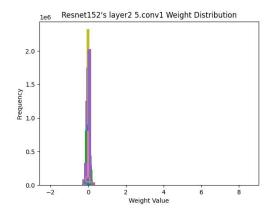


Figure 18: ResNet152 CIFAR-10(-100) Conv Layer-wise Quantization Accuracy(%)



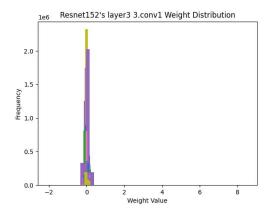


Figure 19: ResNet152's layer2 Conv Figure 20: ResNet152's layer3 Conv Weight Distribution Weight Distribution

2.7 Experiment7: PTQ for BN layers in different locations

Given the previous knowledge, I want to re-validate this weight-distribution vs robustness to quantization pattern on BN layers and again for brevity, I only evaluate two representative models, ResNet18 and ResNet152. Others can be found here in Appendix.

Bit-width	Layer1	Layer2	Layer3	Layer4
FP32	89.77%	89.77%	89.77%	89.77%
INT8	89.63%	89.11%	88.63%	89.71%
INT7	89.14%	89.32%	89.22%	88.95%
INT6	89.82%	89.48%	88.35%	86.97%
INT5	87.13%	87.41%	76.72%	87.41%
INT4	88.93%	78.30%	79.85%	86.87%
INT3	83.56%	71.02%	48.12%	75.02%
INT2	83.56%	62.90%	45.75%	80.02%
INT1	16.75%	10.00%	10.00%	10.00%

Bit-width	Layer1	Layer2	Layer3	Layer4
FP32	69.61%	69.61%	69.61%	69.61%
INT8	69.46%	69.22%	68.93%	68.46%
INT7	69.23%	67.08%	65.73%	62.34%
INT6	69.06%	68.84%	64.36%	64.93%
INT5	67.70%	58.88%	51.08%	51.81%
INT4	67.69%	58.44%	49.84%	54.09%
INT3	54.94%	33.42%	10.90%	25.86%
INT2	50.12%	41.02%	7.40%	24.05%
INT1	2.02%	1.00%	1.00%	1.00%

Table 17: ResNet18 CIFAR-10 BN Layerwise Quantization Accuracy

Table 18: ResNet18 CIFAR-100 BN Layer-wise Quantization Accuracy

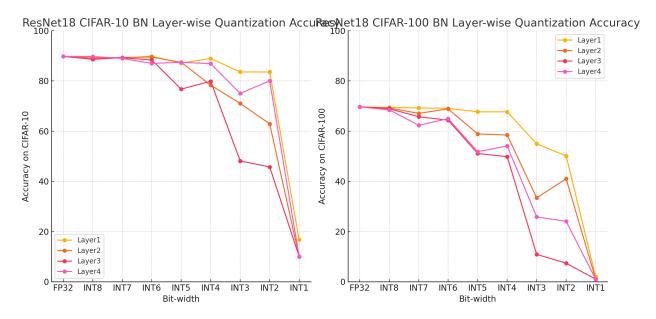


Figure 21: ResNet18 CIFAR-10(-100) BN Layer-wise Quantization Accuracy(%)

We can see layer2 is more robust to quantization to layer3 because of large proportion of weight distributed near zero as follows rather than its location is whether in upstream or downstream.

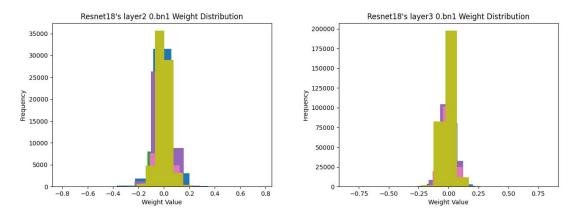


Figure 22: ResNet18's layer2 BN Weight Figure 23: ResNet18's layer3 BN Weight Distribution

Distribution

Then again on CIFAR-100, this pattern remains.

Bit-width	Layer1	Layer2	Layer3	Layer4
FP32	92.35%	92.35%	92.35%	92.35%
INT8	92.28%	92.30%	92.17%	92.33%
INT7	92.34%	92.21%	92.30%	92.32%
INT6	92.43%	92.35%	92.29%	92.25%
INT5	92.27%	92.13%	92.04%	92.41%
INT4	82.89%	89.91%	88.85%	89.55%
INT3	72.00%	81.99%	84.65%	82.57%
INT2	8.09%	10.00%	10.00%	10.00%
INT1	10.00%	10.00%	10.00%	10.00%

Bit-width	Layer1	Layer2	Layer3	Layer4
FP32	74.46%	74.46%	74.46%	74.46%
INT8	74.47%	73.75%	65.78%	66.83%
INT7	74.24%	73.76%	54.19%	51.51%
INT6	70.66%	69.02%	53.27%	53.48%
INT5	70.04%	67.37%	10.37%	15.02%
INT4	4.15%	1.25%	6.24%	9.27%
INT3	1.00%	1.00%	1.16%	1.40%
INT2	1.00%	1.00%	1.09%	2.88%
INT1	1.00%	1.00%	1.00%	1.01%

Table 19: ResNet152 CIFAR-10 BN Layer-wise Quantization Accuracy

Table 20: ResNet152 CIFAR-100 BN Layer-wise Quantization Accuracy

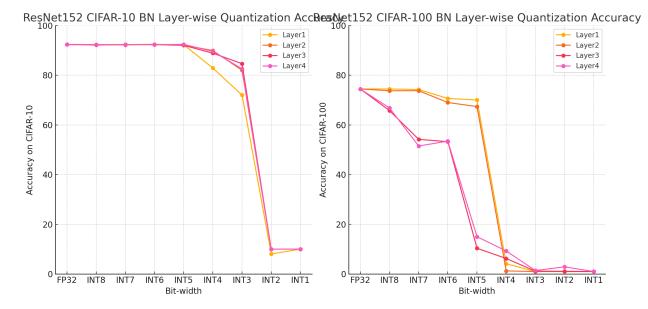
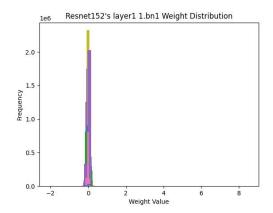


Figure 24: ResNet152 CIFAR-10(-100) BN Layer-wise Quantization Accuracy(%)

We can figure out layer1 is less robust in contrast with layer4 and is correspondingly distributed discretely as follows.



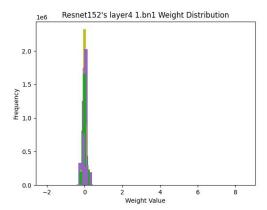


Figure 25: ResNet152's layer1 Weight Distribution

BN Figure 26: ResNet152's layer4 BN Weight Distribution

3 Conclusion

After various quantization on different ResNet models, I realized that quantization can significantly influence storage overhead, inference latency, and inference accuracy. Dataset size and model size also affect the quantization outcome. For example, on the easy CIFAR-10, intensive quantization might not suffer significant accuracy loss compared to moderate quantization but may greatly reduce model size, and large models are more robust to intensive quantization.

Surprisingly, it's not always the best strategy to use largest models . Typically, larger models' storage overhead is exponentially higher than that of smaller models. However, if we quantize a large model to INT8 or INT4, reducing its size to that of a small FP32 model, the accuracy of the large model in INT8 or INT4 will be significantly lower than that of the small FP32 model. Therefore, Quantization-Aware Training (QAT) and other fine-tuning strategies are necessary to compensate for quantization accuracy loss.

4 Prospect

Given that the server in Professor Meng Li's research group, which I used to process and generate all statistics and images, broke down and the deadline is just around the corner, I had to leave some experiments for further exploitation.

- 1. **QAT for ResNet:** All the quantization I finished in this homework is Post-Training Quantization (PTQ). To achieve higher accuracy under more intensive quantization, Quantization-Aware Training (QAT) may be a better choice.
- 2. **Activation Quantization:** I have tried to quantize the weight matrix to minimize storage overhead, but the activations generated by each layer have not been quantized yet for evaluating the influence of quantization on activations to inference latency. For a complete quantization, both weights and activations should be quantized simultaneously to simulate real-world scenarios.

- 3. **Mixed-Precision Quantization:** I realized that different layers have varying robustness to quantization, and Convolutional (Conv), Fully Connected (FC), and Batch Normalization (BN) layers have different sensitivities to quantization as well. I suppose that for robust layers like BN layers, we can apply intensive quantization, and for sensitive layers like Conv layers(layer1's Conv to be more specific), we can apply moderate quantization. By doing so, we can minimize both storage overhead and accuracy loss.
- 4. **Build a state-of-art quantized ResNet Model:** Combining mix of quantization precision method, QAT, Weight-Activation quantization with fine-tuning, I can build a ResNet model boasting storage efficiency and overall accuracy.

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5 Appendix

5.1 Source Code For MNIST

Listing 1: Specific Class Designed for Quantization

```
import math import numpy as np
```

```
import torch
import torch.nn as nn
import torch.nn.functional as F
from torch.autograd import Variable
from function import FakeQuantize, interp
def calcScaleZeroPoint(min_val, max_val, num_bits=8):
    qmin = 0.
    qmax = 2. ** num\_bits - 1.
    scale = (max_val - min_val) / (qmax - qmin)
    zero_point = qmax - max_val / scale
    if zero_point < qmin:</pre>
        zero_point = torch.tensor([qmin], dtype=torch.float32).to(min_val.
       device)
    elif zero_point > qmax:
        zero_point = torch.tensor([qmax], dtype=torch.float32).to(max_val.
       device)
    zero_point.round_()
    return scale, zero_point
def quantize_tensor(x, scale, zero_point, num_bits=8, signed=False):
    if signed:
        qmin = -2. ** (num\_bits - 1)
        qmax = 2. ** (num\_bits - 1) - 1
    else:
        qmin = 0.
        qmax = 2. ** num\_bits - 1.
    q_x = zero_point + x / scale
    q_x.clamp_(qmin, qmax).round_()
    return q_x
def dequantize_tensor(q_x, scale, zero_point):
    return scale * (q_x - zero_point)
def search (M):
    P = 7000
   n = 1
    while True:
        Mo = int(round(2 ** n * M))
        approx_result = Mo * P >> n
        result = int(round(M * P))
        error = approx_result - result
        print("n=%d, Mo=%f, approx=%d, result=%d, error=%f" % \
            (n, Mo, approx_result, result, error))
```

```
if math.fabs(error) < 1e-9 or n >= 22:
            return Mo, n
       n += 1
class QParam(nn.Module):
    def __init__(self, num_bits=8):
        super(QParam, self).__init__()
        self.num_bits = num_bits
        scale = torch.tensor([], requires_grad=False)
        zero_point = torch.tensor([], requires_grad=False)
       min = torch.tensor([], requires_grad=False)
       max = torch.tensor([], requires_grad=False)
        self.register_buffer('scale', scale)
        self.register_buffer('zero_point', zero_point)
        self.register_buffer('min', min)
        self.register_buffer('max', max)
   def update(self, tensor):
        if self.max.nelement() == 0 or self.max.data < tensor.max().data:</pre>
            self.max.data = tensor.max().data
        self.max.clamp_(min=0)
        if self.min.nelement() == 0 or self.min.data > tensor.min().data:
            self.min.data = tensor.min().data
        self.min.clamp_(max=0)
        self.scale, self.zero_point = calcScaleZeroPoint(self.min, self.max,
      self.num_bits)
   def quantize_tensor(self, tensor):
        return quantize_tensor(tensor, self.scale, self.zero_point, num_bits=
      self.num_bits)
   def dequantize_tensor(self, q_x):
        return dequantize_tensor(q_x, self.scale, self.zero_point)
    def _load_from_state_dict(self , state_dict , prefix , local_metadata , strict
      , missing_keys, unexpected_keys, error_msgs):
       key_names = ['scale', 'zero_point', 'min', 'max']
        for key in key_names:
            value = getattr(self, key)
            value.data = state_dict[prefix + key].data
            state_dict.pop(prefix + key)
    def __str__(self):
        info = 'scale: %.10f ' % self.scale
        info += 'zp: %d ' % self.zero_point
        info += 'min: %.6f' % self.min
        info += 'max: %.6f' % self.max
        return info
```

```
class QModule(nn.Module):
   def __init__(self, qi=True, qo=True, num_bits=8):
       super(QModule, self).__init__()
        if qi:
            self.qi = QParam(num_bits=num_bits)
       if qo:
            self.qo = QParam(num_bits=num_bits)
   def freeze(self):
       pass
   def quantize_inference(self, x):
        raise NotImplementedError('quantize_inference should be implemented.')
class QConv2d(QModule):
   def __init__(self, conv_module, qi=True, qo=True, num_bits=8):
       super(QConv2d, self).__init__(qi=qi, qo=qo, num_bits=num_bits)
        self.num_bits = num_bits
        self.conv_module = conv_module
        self.qw = QParam(num_bits=num_bits)
        self.register_buffer('M', torch.tensor([], requires_grad=False))
   def freeze(self, qi=None, qo=None):
        if hasattr(self, 'qi') and qi is not None:
            raise ValueError('qi has been provided in init function.')
        if not hasattr(self, 'qi') and qi is None:
            raise ValueError('qi is not existed, should be provided.')
        if hasattr(self, 'qo') and qo is not None:
            raise ValueError('qo has been provided in init function.')
        if not hasattr(self, 'qo') and qo is None:
            raise ValueError('qo is not existed, should be provided.')
        if qi is not None:
            self.qi = qi
        if go is not None:
            self.go = go
        self.M. data = (self.qw.scale * self.qi.scale / self.qo.scale).data
        self.conv_module.weight.data = self.qw.quantize_tensor(self.
      conv_module.weight.data)
        self.conv_module.weight.data = self.conv_module.weight.data - self.qw.
      zero_point
        self.conv_module.bias.data = quantize_tensor(self.conv_module.bias.
      data, scale=self.qi.scale * self.qw.scale,
                                                      zero_point=0, num_bits
      =32, signed=True)
   def forward(self, x):
```

```
if hasattr(self, 'qi'):
            self.qi.update(x)
            x = FakeQuantize.apply(x, self.qi)
        self.qw.update(self.conv_module.weight.data)
        x = F.conv2d(x, FakeQuantize.apply(self.conv_module.weight, self.qw),
      self.conv_module.bias,
                     stride=self.conv_module.stride,
                     padding=self.conv module.padding, dilation=self.
      conv_module.dilation,
                     groups=self.conv_module.groups)
        if hasattr(self, 'qo'):
            self.qo.update(x)
            x = FakeQuantize.apply(x, self.qo)
        return x
   def quantize_inference(self, x):
        x = x - self.qi.zero_point
        x = self.conv.module(x)
       x = self.M * x
        x.round_()
        x = x + self.qo.zero_point
        x.clamp_(0., 2.**self.num_bits-1.).round_()
        return x
class QLinear(QModule):
   def __init__(self, fc_module, qi=True, qo=True, num_bits=8):
        super(QLinear, self).__init__(qi=qi, qo=qo, num_bits=num_bits)
        self.num_bits = num_bits
        self.fc_module = fc_module
        self.qw = QParam(num_bits=num_bits)
        self.register_buffer('M', torch.tensor([], requires_grad=False))
   def freeze(self, qi=None, qo=None):
        if hasattr(self, 'qi') and qi is not None:
            raise ValueError('qi has been provided in init function.')
        if not hasattr(self, 'qi') and qi is None:
    raise ValueError('qi is not existed, should be provided.')
        if hasattr(self, 'qo') and qo is not None:
            raise ValueError('qo has been provided in init function.')
        if not hasattr(self, 'qo') and qo is None:
            raise ValueError('qo is not existed, should be provided.')
        if qi is not None:
            self.qi = qi
        if qo is not None:
            self.qo = qo
        self.M.data = (self.qw.scale * self.qi.scale / self.qo.scale).data
```

```
self.fc_module.weight.data = self.qw.quantize_tensor(self.fc_module.
      weight.data)
        self.fc_module.weight.data = self.fc_module.weight.data - self.qw.
      zero_point
        self.fc_module.bias.data = quantize_tensor(self.fc_module.bias.data,
      scale=self.qi.scale * self.qw.scale,
                                                    zero_point=0, num_bits=32,
      signed=True)
    def forward(self, x):
        if hasattr(self, 'qi'):
            self.qi.update(x)
            x = FakeQuantize.apply(x, self.qi)
        self .qw. update(self .fc_module .weight .data)
       x = F.linear(x, FakeQuantize.apply(self.fc_module.weight, self.qw),
      self.fc_module.bias)
        if hasattr(self, 'qo'):
            self.qo.update(x)
            x = FakeQuantize.apply(x, self.qo)
        return x
   def quantize_inference(self, x):
       x = x - self.qi.zero_point
       x = self.fc_module(x)
       x = self.M * x
       x.round_()
       x = x + self.qo.zero_point
       x.clamp_(0., 2.**self.num_bits-1.).round_()
        return x
class QReLU(QModule):
   def __init__(self , qi=False , num_bits=None):
        super(QReLU, self).__init__(qi=qi, num_bits=num_bits)
    def freeze(self, qi=None):
        if hasattr(self, 'qi') and qi is not None:
            raise ValueError('qi has been provided in init function.')
        if not hasattr(self, 'qi') and qi is None:
            raise ValueError('qi is not existed, should be provided.')
        if qi is not None:
            self.qi = qi
   def forward(self, x):
        if hasattr(self, 'qi'):
            self.qi.update(x)
            x = FakeQuantize.apply(x, self.qi)
```

```
x = F.relu(x)
       return x
   def quantize_inference(self, x):
       x = x.clone()
       x[x < self.qi.zero_point] = self.qi.zero_point
       return x
class QMaxPooling2d(QModule):
   def __init__(self, kernel_size=3, stride=1, padding=0, qi=False, num_bits=
      None):
       super(QMaxPooling2d, self).__init__(qi=qi, num_bits=num_bits)
        self.kernel_size = kernel_size
        self.stride = stride
        self.padding = padding
   def freeze(self, qi=None):
        if hasattr(self, 'qi') and qi is not None:
            raise ValueError('qi has been provided in init function.')
        if not hasattr(self, 'qi') and qi is None:
            raise ValueError('qi is not existed, should be provided.')
        if qi is not None:
            self.qi = qi
   def forward(self, x):
        if hasattr(self, 'qi'):
            self.qi.update(x)
           x = FakeQuantize.apply(x, self.qi)
       x = F.max_pool2d(x, self.kernel_size, self.stride, self.padding)
       return x
   def quantize_inference(self, x):
        return F.max_pool2d(x, self.kernel_size, self.stride, self.padding)
class QConvBNReLU(QModule):
   def __init__(self, conv_module, bn_module, qi=True, qo=True, num_bits=8):
       super(QConvBNReLU, self).__init__(qi=qi, qo=qo, num_bits=num_bits)
        self.num_bits = num_bits
        self.conv_module = conv_module
        self.bn_module = bn_module
        self .qw = QParam(num_bits=num_bits)
        self.qb = QParam(num\_bits=32)
        self.register_buffer('M', torch.tensor([], requires_grad=False))
   def fold_bn(self, mean, std):
        if self.bn_module.affine:
           gamma_ = self.bn_module.weight / std
```

```
weight = self.conv_module.weight * gamma_.view(self.conv_module.
  out_channels, 1, 1, 1)
        if self.conv module.bias is not None:
            bias = gamma_ * self.conv_module.bias - gamma_ * mean + self.
  bn module.bias
        else:
            bias = self.bn_module.bias - gamma_ * mean
    else:
       gamma_{=} = 1 / std
        weight = self.conv module.weight * gamma
        if self.conv module.bias is not None:
            bias = gamma_ * self.conv_module.bias - gamma_ * mean
        else:
            bias = -gamma_* * mean
    return weight, bias
def forward(self, x):
    if hasattr(self, 'qi'):
        self.qi.update(x)
        x = FakeQuantize.apply(x, self.qi)
    if self.training:
        y = F.conv2d(x, self.conv_module.weight, self.conv_module.bias,
                        stride=self.conv_module.stride,
                        padding=self.conv_module.padding,
                        dilation=self.conv_module.dilation,
                        groups=self.conv_module.groups)
        y = y.permute(1, 0, 2, 3) # NOHW -> ONHW
       y = y.contiguous().view(self.conv_module.out_channels, -1) # CNHW
  -> C,NHW
        mean = y.mean(1).detach()
        var = y.var(1).detach()
        self.bn_module.running_mean = \
            (1 - self.bn_module.momentum) * self.bn_module.running_mean +
            self.bn_module.momentum * mean
        self.bn_module.running_var = \
            (1 - self.bn module.momentum) * self.bn module.running var + \
            self.bn module.momentum * var
    else:
        mean = Variable(self.bn_module.running_mean)
        var = Variable(self.bn_module.running_var)
    std = torch.sqrt(var + self.bn_module.eps)
    weight, bias = self.fold_bn(mean, std)
    self.qw.update(weight.data)
   x = F.conv2d(x, FakeQuantize.apply(weight, self.qw), bias,
            stride=self.conv_module.stride,
```

```
padding=self.conv_module.padding, dilation=self.conv_module.
      dilation,
                groups=self.conv_module.groups)
       x = F.relu(x)
        if hasattr(self, 'qo'):
            self.qo.update(x)
           x = FakeQuantize.apply(x, self.qo)
       return x
   def freeze(self, qi=None, qo=None):
        if hasattr(self, 'qi') and qi is not None:
            raise ValueError('qi has been provided in init function.')
        if not hasattr(self, 'qi') and qi is None:
            raise ValueError('qi is not existed, should be provided.')
        if hasattr(self, 'qo') and qo is not None:
            raise ValueError('qo has been provided in init function.')
       if not hasattr(self, 'qo') and qo is None:
            raise ValueError('qo is not existed, should be provided.')
        if qi is not None:
            self.qi = qi
        if go is not None:
            self.qo = qo
        self.M.data = (self.qw.scale * self.qi.scale / self.qo.scale).data
       std = torch.sqrt(self.bn module.running var + self.bn module.eps)
       weight, bias = self.fold_bn(self.bn_module.running_mean, std)
        self.conv_module.weight.data = self.qw.quantize_tensor(weight.data)
        self.conv_module.weight.data = self.conv_module.weight.data - self.qw.
      zero_point
       self.conv_module.bias.data = quantize_tensor(bias, scale=self.qi.scale
       * self.qw.scale,
                                                     zero_point=0, num_bits
      =32, signed=True)
   def quantize inference(self, x):
       x = x - self.qi.zero_point
       x = self.conv_module(x)
       x = self.M * x
       x.round_()
       x = x + self.qo.zero_point
       x.clamp_(0., 2.**self.num_bits-1.).round_()
       return x
class QSigmoid(QModule):
   def __init__(self, qi=True, qo=True, num_bits=8, lut_size=64):
       super(QSigmoid, self).__init__(qi=qi, qo=qo, num_bits=num_bits)
```

```
self.num_bits = num_bits
    self.lut_size = lut_size
def forward(self, x):
    if hasattr(self, 'qi'):
         self.qi.update(x)
        x = FakeQuantize.apply(x, self.qi)
    x = torch.sigmoid(x)
    if hasattr(self, 'qo'):
        self.qo.update(x)
        x = FakeQuantize.apply(x, self.qo)
    return x
def freeze(self, qi=None, qo=None):
    if hasattr(self, 'qi') and qi is not None:
         raise ValueError('qi has been provided in init function.')
    if not hasattr(self, 'qi') and qi is None:
    raise ValueError('qi is not existed, should be provided.')
    if hasattr(self, 'qo') and qo is not None:
         raise ValueError('qo has been provided in init function.')
    if not hasattr(self, 'qo') and qo is None:
         raise ValueError('qo is not existed, should be provided.')
    if qi is not None:
        self.qi = qi
    if go is not None:
        self.qo = qo
    lut_qx = torch.tensor(np.linspace(0, 2 ** self.num_bits - 1, self.
   lut_size), dtype=torch.uint8)
    lut_x = self.qi.dequantize_tensor(lut_qx)
    lut_y = torch.sigmoid(lut_x)
    lut_qy = self.qo.quantize_tensor(lut_y)
    self.register_buffer('lut_qy', lut_qy)
    self.register_buffer('lut_qx', lut_qx)
def quantize_inference(self, x):
    y = interp(x, self.lut_qx, self.lut_qy)
y = y.round_().clamp_(0., 2.**self.num_bits-1.)
    return y
```

Listing 2: Network Model For MNIST

```
import torch
import torch.nn as nn
import torch.nn.functional as F

from module import *
```

```
class Net(nn.Module):
   def __init__(self , num_channels=1):
        super(Net, self).__init__()
        self.conv1 = nn.Conv2d(num_channels, 40, 3, 1)
        self.conv2 = nn.Conv2d(40, 40, 3, 1, groups=20)
        self.fc = nn.Linear (5*5*40, 10)
    def forward(self, x):
       x = F.relu(self.conv1(x))
       x = F. \max_{pool2d}(x, 2, 2)
       x = F.relu(self.conv2(x))
       x = F. \max_{pool2d}(x, 2, 2)
       x = x.view(-1, 5*5*40)
       x = self.fc(x)
        return x
    def quantize(self, num_bits=8):
        self.qconv1 = QConv2d(self.conv1, qi=True, qo=True, num_bits=num_bits)
        self.qrelu1 = QReLU()
        self.qmaxpool2d_1 = QMaxPooling2d(kernel_size=2, stride=2, padding=0)
        self.qconv2 = QConv2d(self.conv2, qi=False, qo=True, num_bits=num_bits
        self.qrelu2 = QReLU()
        self.qmaxpool2d_2 = QMaxPooling2d(kernel_size=2, stride=2, padding=0)
        self.qfc = QLinear(self.fc, qi=False, qo=True, num_bits=num_bits)
    def quantize forward(self, x):
       x = self.qconv1(x)
       x = self.qrelu1(x)
       x = self.qmaxpool2d_1(x)
       x = self.qconv2(x)
       x = self.qrelu2(x)
       x = self.qmaxpool2d_2(x)
       x = x.view(-1, 5*5*40)
       x = self.qfc(x)
        return x
    def freeze(self):
        self.qconv1.freeze()
        self.qrelu1.freeze(self.qconv1.qo)
        self.qmaxpool2d_1.freeze(self.qconv1.qo)
        self.qconv2.freeze(qi=self.qconv1.qo)
        self.qrelu2.freeze(self.qconv2.qo)
        self.qmaxpool2d_2.freeze(self.qconv2.qo)
        self.qfc.freeze(qi=self.qconv2.qo)
    def quantize_inference(self, x):
        qx = self.qconv1.qi.quantize_tensor(x)
        qx = self.qconv1.quantize_inference(qx)
        qx = self.qrelu1.quantize_inference(qx)
        qx = self.qmaxpool2d_1.quantize_inference(qx)
        qx = self.qconv2.quantize_inference(qx)
```

```
qx = self.qrelu2.quantize_inference(qx)
        qx = self.qmaxpool2d_2.quantize_inference(qx)
        qx = qx.view(-1, 5*5*40)
        qx = self.qfc.quantize_inference(qx)
        out = self.qfc.qo.dequantize_tensor(qx)
        return out
class NetBN(nn.Module):
    def __init__(self , num_channels=1):
        super(NetBN, self).__init__()
        self.conv1 = nn.Conv2d(num_channels, 40, 3, 1)
        self.bn1 = nn.BatchNorm2d(40)
        self.conv2 = nn.Conv2d(40, 40, 3, 1)
        self.bn2 = nn.BatchNorm2d(40)
        self.fc = nn.Linear(5 * 5 * 40, 10)
   def forward(self, x):
       x = self.conv1(x)
       x = self.bn1(x)
       x = F.relu(x)
       x = F. \max_{pool2d}(x, 2, 2)
       x = self.conv2(x)
       x = self.bn2(x)
       x = F.relu(x)
       x = F. \max_{pool2d}(x, 2, 2)
       x = x.view(-1, 5 * 5 * 40)
       x = self.fc(x)
       return x
   def quantize(self, num_bits=8):
        self.gconv1 = QConvBNReLU(self.conv1, self.bn1, qi=True, qo=True,
      num_bits=num_bits)
        self.qmaxpool2d_1 = QMaxPooling2d(kernel_size=2, stride=2, padding=0)
        self.qconv2 = QConvBNReLU(self.conv2, self.bn2, qi=False, qo=True,
      num_bits=num_bits)
        self.qmaxpool2d_2 = QMaxPooling2d(kernel_size=2, stride=2, padding=0)
        self.qfc = QLinear(self.fc, qi=False, qo=True, num_bits=num_bits)
    def quantize forward (self, x):
       x = self.qconv1(x)
       x = self.qmaxpool2d_1(x)
       x = self.qconv2(x)
       x = self.qmaxpool2d_2(x)
       x = x.view(-1, 5*5*40)
       x = self.qfc(x)
        return x
    def freeze(self):
        self.gconv1.freeze()
        self.gmaxpool2d_1.freeze(self.gconv1.go)
        self.qconv2.freeze(qi=self.qconv1.qo)
        self.qmaxpool2d_2.freeze(self.qconv2.qo)
        self.qfc.freeze(qi=self.qconv2.qo)
```

```
def quantize_inference(self, x):
    qx = self.qconv1.qi.quantize_tensor(x)
    qx = self.qconv1.quantize_inference(qx)
    qx = self.qmaxpool2d_1.quantize_inference(qx)
    qx = self.qconv2.quantize_inference(qx)
    qx = self.qmaxpool2d_2.quantize_inference(qx)
    qx = qx.view(-1, 5*5*40)

qx = self.qfc.quantize_inference(qx)

out = self.qfc.qo.dequantize_tensor(qx)
    return out
```

Listing 3: Post-training Quantization(PTQ)

```
from torch.serialization import load
from model import *
import argparse
import torch
import torch.nn as nn
import torch.optim as optim
from torchvision import datasets, transforms
import os
import os.path as osp
import sys
sys.stdout = open("diff_bit_eval.out", "w")
def direct_quantize(model, test_loader, device):
    model.eval()
    model.to(device)
    with torch.no_grad():
        for i, (data, target) in enumerate(test_loader):
            data = data.to(device)
            output = model.quantize_forward(data)
            if i \% 500 == 0:
                break
    print('Direct quantization finish')
def full inference(model, test loader):
    correct = 0
    for i, (data, target) in enumerate(test_loader, 1):
        output = model(data)
        pred = output.argmax(dim=1, keepdim=True)
        correct += pred.eq(target.view_as(pred)).sum().item()
    print('\nTest set: Full Model Accuracy: {:f}%\n'.format(100. * correct /
      len(test_loader.dataset)))
```

```
def quantize_inference(model, test_loader):
    correct = 0
    for i, (data, target) in enumerate(test_loader, 1):
        output = model.quantize_inference(data)
        pred = output.argmax(dim=1, keepdim=True)
        correct += pred.eq(target.view_as(pred)).sum().item()
    print('\nTest set: Quant Model Accuracy: {:f}%\n'.format(100. * correct /
      len(test_loader.dataset)))
if __name__ == "__main__":
    batch\_size = 128
    using_bn = True
    load_quant_model_file = None
    device = torch.device('cpu')
    save_model = True
    train_loader = torch.utils.data.DataLoader(
        datasets.MNIST('data', train=True, download=True,
                       transform=transforms.Compose([
                            transforms. ToTensor(),
                            transforms. Normalize ((0.1307,), (0.3081,))
                       ])),
        batch_size=batch_size, shuffle=True, num_workers=8, pin_memory=True
    test_loader = torch.utils.data.DataLoader(
        datasets.MNIST('data', train=False, transform=transforms.Compose([
            transforms. ToTensor(),
            transforms. Normalize ((0.1307,), (0.3081,))
        batch_size=batch_size, shuffle=False, num_workers=8, pin_memory=True
    )
    if using_bn:
       model = NetBN()
        model.load_state_dict(torch.load('ckpt/mnist_cnnbn.pt', map_location=
        save_file = "ckpt/mnist_cnnbn_ptq.pt"
    else:
       model = Net()
        model.load_state_dict(torch.load('ckpt/mnist_cnn.pt', map_location=
      device))
        save_file = "ckpt/mnist_cnn_ptq.pt"
   model.eval()
    full_inference(model, test_loader)
    if save_model:
        if not osp.exists('ckpt'):
            os.makedirs('ckpt')
        if using_bn:
            torch.save(model.state_dict(), 'ckpt/mnist_cnnbn_ptq.pt')
        else:
            torch.save(model.state_dict(), 'ckpt/mnist_cnn_ptq.pt')
```

```
num bits = 8
for bit in range(num_bits, 0, -1):
    if using_bn:
        model = NetBN()
        model.load_state_dict(torch.load('ckpt/mnist_cnnbn.pt',
  map_location=device))
    else:
        model = Net()
        model.load_state_dict(torch.load('ckpt/mnist_cnn.pt', map_location
  =device))
    model.quantize(num_bits=bit)
    model.eval()
    print('Quantization bit: %d' % bit)
    direct_quantize(model, train_loader, device)
    model.freeze()
    quantize_inference (model, test_loader)
    if save_model:
        if not osp.exists('ckpt'):
            os.makedirs('ckpt')
        if using_bn:
            for name, param in model.named_parameters():
                if param.requires_grad:
                    print(f"Layer: {name} | Size: {param.size()} | Values:
    {param[:4]} \n")
            torch.save(model.state_dict(), f'ckpt/mnist_cnnbn_ptq_{bit}.pt
   ′)
        else:
            torch.save(model.state_dict(), f'ckpt/mnist_cnn_ptq_{bit}.pt')
```

Listing 4: Quantization-Aware Training(QAT)

```
from model import *
import argparse
import torch
import torch.nn as nn
import torch.optim as optim
from torchvision import datasets, transforms
import os
import os.path as osp
import sys
sys.stdout = open("qat_diff_bit_eval.out", "w")
def quantize_aware_training(model, device, train_loader, optimizer, epoch):
    lossLayer = torch.nn.CrossEntropyLoss()
    for batch_idx , (data , target) in enumerate(train_loader , 1):
        data, target = data.to(device), target.to(device)
        optimizer.zero_grad()
        output = model.quantize_forward(data)
        loss = lossLayer(output, target)
        loss.backward()
        optimizer.step()
```

```
if batch idx \% 50 == 0:
            print('Quantize Aware Training Epoch: {} [{}/{}] \ tLoss: {:.6 f}'.
      format(
                epoch, batch_idx * len(data), len(train_loader.dataset), loss.
      item()
            ))
def full inference(model, test loader):
    correct = 0
    for i, (data, target) in enumerate(test_loader, 1):
        data, target = data.to(device), target.to(device)
        output = model(data)
        pred = output.argmax(dim=1, keepdim=True)
        correct += pred.eq(target.view_as(pred)).sum().item()
    print('\nTest set: Full Model Accuracy: {:f}%\n'.format(100. * correct /
      len(test_loader.dataset)))
def quantize_inference(model, test_loader):
    correct = 0
    for i, (data, target) in enumerate(test_loader, 1):
        data , target = data.to(device) , target.to(device)
        output = model.quantize_inference(data)
        pred = output.argmax(dim=1, keepdim=True)
        correct += pred.eq(target.view_as(pred)).sum().item()
    print('\nTest set: Quant Model Accuracy: {:f}%\n'.format(100. * correct /
      len(test_loader.dataset)))
if __name__ == "__main__":
    batch\_size = 64
   seed = 1
   epochs = 3
    1r = 0.01
   momentum = 0.5
    using_bn = True
   load_quant_model_file = None
    torch.manual seed(seed)
    device = torch.device('cuda' if torch.cuda.is_available() else 'cpu')
    train_loader = torch.utils.data.DataLoader(
        datasets.MNIST('data', train=True, download=True,
                       transform=transforms.Compose([
                            transforms. ToTensor(),
                            transforms. Normalize ((0.1307,), (0.3081,))
                       ])),
        batch_size=batch_size, shuffle=True, num_workers=1, pin_memory=False
    )
    test_loader = torch.utils.data.DataLoader(
        datasets.MNIST('data', train=False, transform=transforms.Compose([
```

```
transforms. ToTensor(),
        transforms. Normalize ((0.1307,), (0.3081,))
    batch_size=batch_size, shuffle=True, num_workers=1, pin_memory=False
)
if using_bn:
    model = NetBN()
    model.load_state_dict(torch.load('ckpt/mnist_cnnbn.pt', map_location='
    save_file = "ckpt/mnist_cnnbn_qat.pt"
else:
    model = Net()
    model.load_state_dict(torch.load('ckpt/mnist_cnn.pt', map_location='
    save_file = "ckpt/mnist_cnn_qat.pt"
model. to (device)
optimizer = optim.Adam(model.parameters(), lr=lr)
model.eval()
full_inference(model, test_loader)
num\_bits = 8
for bit in range(num_bits, 0, -1):
    if using_bn:
        model = NetBN()
        model.load_state_dict(torch.load('ckpt/mnist_cnnbn.pt',
  map_location='cpu'))
        save_file = f"ckpt/mnist_cnnbn_qat_{bit}.pt"
    else:
        model = Net()
        model.load_state_dict(torch.load('ckpt/mnist_cnn.pt', map_location
  ='cpu'))
        save_file = f"ckpt/mnist_cnn_qat_{bit}.pt"
    model. to (device)
    optimizer = optim.SGD(model.parameters(), lr=lr, momentum=momentum)
    model.quantize(num bits=bit)
    print('Quantization bit: %d' % bit)
    if load_quant_model_file is not None:
        model.load_state_dict(torch.load(load_quant_model_file))
        print("Successfully load quantized model %s" %
  load_quant_model_file)
    model.train()
    for epoch in range (1, epochs + 1):
        quantize_aware_training(model, device, train_loader, optimizer,
  epoch)
    model.eval()
```

```
torch.save(model.state_dict(), save_file)
model.freeze()
quantize_inference(model, test_loader)
```

Listing 5: Train full-precision ResNet on CIFAR-10

```
import torch
import torch.nn as nn
import torch.optim as optim
from torch.utils.data import DataLoader
import torchvision
from torchvision import datasets, transforms
from torchvision.models import resnet18, resnet34, resnet50, resnet101,
       resnet152
from torchvision.models import ResNet18_Weights, ResNet34_Weights,
       ResNet50_Weights, ResNet101_Weights, ResNet152_Weights
import os
import os.path as osp
from tqdm import tqdm
import sys
sys.stdout = open("eval resnet18 cifar10 quantization.out", "w")
device = torch.device("cuda" if torch.cuda.is_available() else "cpu")
weights = ResNet18_Weights.DEFAULT
model = resnet18(weights=weights)
num classes = 10
model.fc = nn.Linear(model.fc.in_features, num_classes)
model = model.to(device)
preprocess = transforms.Compose([
    transforms. Resize (256),
    transforms. CenterCrop (224),
    transforms. ToTensor(),
    transforms.Normalize(mean = [0.485, 0.456, 0.406], std = [0.229, 0.224,
       0.225]),
])
data_dir = '/data/home/qyjh/Quantization_evaluation/cifar -10'
train_dataset = datasets.CIFAR10(
    root=data_dir, train=True, download=True, transform=preprocess
)
test_dataset = datasets.CIFAR10(
    root=data_dir, train=False, download=True, transform=preprocess
train_loader = DataLoader(
    train_dataset,
    batch_size=128,
```

```
shuffle=True,
    num workers=4
test_loader = DataLoader(
    test_dataset,
    batch_size=128,
    shuffle=False,
    num workers=4
)
criterion = nn.CrossEntropyLoss()
optimizer = optim.Adam(model.parameters(), lr=1e-3)
def train_model(model, train_loader, criterion, optimizer, device, num_epochs
      =10):
    for epoch in range(num_epochs):
        model.train()
        running_loss = 0.0
        progress_bar = tqdm(enumerate(train_loader), total=len(train_loader))
        for idx, (inputs, labels) in progress_bar:
            inputs, labels = inputs.to(device), labels.to(device)
            optimizer.zero_grad()
            outputs = model(inputs)
            loss = criterion(outputs, labels)
            loss.backward()
            optimizer.step()
            running loss += loss.item()
            progress_bar.set_description(f"Epoch [{epoch+1}/{num_epochs}],
      Loss: {loss.item():.4 f}")
        with torch.no_grad():
            accuracy = compute_accuracy(model, test_loader, device)
            print(f'Epoch{epoch+1}: Accuracy on CIFAR-10 test set: {accuracy *
        100:.2 f}%')
def compute_accuracy(model, data_loader, device):
    model.eval()
    correct = 0
    total = 0
    with torch.no_grad():
        for inputs, labels in data_loader:
            inputs, labels = inputs.to(device), labels.to(device)
            outputs = model(inputs)
            _, predicted = torch.max(outputs, 1)
            total += labels.size(0)
            correct += (predicted == labels).sum().item()
    return correct / total
num\_epochs = 10
train_model(model, train_loader, criterion, optimizer, device, num_epochs)
if not osp.exists('model'):
```

```
os.makedirs('model')
torch.save(model.state_dict(), 'model/Resnet18_CIFAR10.pt')

accuracy = compute_accuracy(model, test_loader, device)
print(f'Accuracy on CIFAR-10 test set: {accuracy * 100:.2f}%')
```

Listing 6: Train full-precision ResNet on CIFAR-100

```
import torch
import torch.nn as nn
import torch.optim as optim
from torch.utils.data import DataLoader
import torchvision
from torchvision import datasets, transforms
from torchvision.models import resnet18, resnet34, resnet50, resnet101,
       resnet152
from torchvision.models import ResNet18_Weights, ResNet34_Weights,
       ResNet50_Weights, ResNet101_Weights, ResNet152_Weights
import os
import os.path as osp
from tqdm import tqdm
import sys
sys.stdout = open("eval resnet18 cifar100.out", "w")
device = torch.device("cuda" if torch.cuda.is_available() else "cpu")
weights = ResNet18_Weights.DEFAULT
model = resnet18(weights=weights)
num classes = 100
model.fc = nn.Linear(model.fc.in_features, num_classes)
model = model.to(device)
preprocess = transforms.Compose([
    transforms. Resize (256),
    transforms. CenterCrop (224),
    transforms. ToTensor(),
    transforms.Normalize(mean = [0.485, 0.456, 0.406], std = [0.229, 0.224,
       0.225]),
])
data_dir = '/data/home/qyjh/Quantization_evaluation/cifar -100'
train_dataset = datasets.CIFAR100(
    root=data dir, train=True, download=True, transform=preprocess
)
test_dataset = datasets.CIFAR100(
    root=data_dir, train=False, download=True, transform=preprocess
train_loader = DataLoader(
    train_dataset,
    batch_size = 256,
```

```
shuffle=True,
    num workers=4
test_loader = DataLoader(
    test_dataset,
    batch_size=256,
    shuffle=False,
    num workers=4
)
criterion = nn.CrossEntropyLoss()
optimizer = optim.Adam(model.parameters(), lr=1e-3)
def train_model(model, train_loader, criterion, optimizer, device, num_epochs
      =10):
    for epoch in range(num_epochs):
        model.train()
        running_loss = 0.0
        progress_bar = tqdm(enumerate(train_loader), total=len(train_loader))
        for idx, (inputs, labels) in progress_bar:
            inputs, labels = inputs.to(device), labels.to(device)
            optimizer.zero_grad()
            outputs = model(inputs)
            loss = criterion (outputs, labels)
            loss.backward()
            optimizer.step()
            running loss += loss.item()
            progress_bar.set_description(f"Epoch [{epoch+1}/{num_epochs}],
      Loss: {loss.item():.4 f}")
        with torch.no_grad():
            accuracy = compute_accuracy(model, test_loader, device)
            print(f'Epoch{epoch+1}: Accuracy on CIFAR-100 test set: {accuracy
      * 100:.2 f}%')
def compute_accuracy(model, data_loader, device):
    model.eval()
    correct = 0
    total = 0
    with torch.no_grad():
        for inputs, labels in data_loader:
            inputs, labels = inputs.to(device), labels.to(device)
            outputs = model(inputs)
            _, predicted = torch.max(outputs, 1)
            total += labels.size(0)
            correct += (predicted == labels).sum().item()
    return correct / total
num_{epochs} = 10
train_model(model, train_loader, criterion, optimizer, device, num_epochs)
```

```
if not osp.exists('model'):
    os.makedirs('model')
torch.save(model.state_dict(), 'model/Resnet18_CIFAR100.pt')

accuracy = compute_accuracy(model, test_loader, device)
print(f'Accuracy on CIFAR-100 test set: {accuracy * 100:.2f}%')
```

Listing 7: Weight Distribution Print

```
import torch
import torch.nn as nn
import torch.optim as optim
from torch.utils.data import DataLoader
import torchvision
from torchvision import datasets, transforms
from torchvision.models import resnet18, resnet34, resnet50, resnet101,
      resnet152
from torchvision.models import ResNet18_Weights, ResNet34_Weights,
      ResNet50_Weights, ResNet101_Weights, ResNet152_Weights
import os
import os.path as osp
from tqdm import tqdm
import sys
from qtorch import FixedPoint
from qtorch.quant import Quantizer, quantizer
import matplotlib.pyplot as plt
num_{classes} = 10
def plot_weight_distribution(layer, block_name, idx_block, idx_model):
    if not osp.exists(f'Weight Distribution CIFAR{num_classes}'):
        os.makedirs(f'Weight Distribution CIFAR{num_classes}')
    weights = layer.weight.data.cpu().numpy()
    plt.hist(weights.flatten(), bins=10)
    plt.title(f'Resnet{idx_model}\'s layer{idx_block} {block_name} Weight
      Distribution ')
    plt.xlabel('Weight Value')
    plt.ylabel('Frequency')
    plt.savefig(f'Weight Distribution CIFAR{num_classes}/Resnet{idx_model}\'s
      layer{idx_block} {block_name} Weight Distribution.jpg')
resnet_models = [resnet18, resnet34, resnet50, resnet101, resnet152]
idx list = [18, 34, 50, 101, 152]
for idx, resnet_model in enumerate(resnet_models):
   model = resnet_model()
   model.fc = nn.Linear(model.fc.in_features, num_classes)
    state_dict = torch.load(f'/data/home/qyjh/Quantization_evaluation/
      Resnet_Test/model/Resnet{idx_list[idx]}_CIFAR{num_classes}.pt')
   model.load_state_dict(state_dict)
    block_list = [model.layer1, model.layer2, model.layer3, model.layer4]
    for idx_block, block in enumerate(block_list):
```