- [10] **2.** Consider the problem (from the note sheet) maximize  $x_1$  subject to  $x_1 \le 2$ ,  $x_1 \le \beta$ , and  $x_1 \ge 0$ .
  - (a) Solve this LP for  $\beta = 1$ .

(b) For this final dictionary, write out  $\vec{x}_B$ ,  $\vec{x}_N$ , and  $A_B$ . Find  $A_B^{-1}$ , and using  $A_B^{-1}$  write down a dictionary corresponding to the final dictionary where  $\beta$  is general (rather than  $\beta = 1$ ).

(c) For what values of  $\beta$  is the dictionary in part (b) final?

(d) By performing one dual pivot, give a final dictionary for  $\beta$  slightly bigger than two 2.

(e) Try to do the same for  $\beta$  slightly less than 0. What happens?