

[12] **2.** Consider the following problem.

$$\begin{aligned} & \text{maximize } c_1x_1 + c_2x_2 + c_3x_3 \\ & \text{subject to } 3x_1 + x_2 - x_3 \leq -2 \\ & \qquad \qquad x_1 - x_2 - 2x_3 \leq -3 \\ & \qquad \qquad x_1 \leq 2 \\ & \qquad \qquad x_1, x_2, x_3 \geq 0 \end{aligned} \tag{*}$$

- (a) Solve problem (\*) when  $(c_1, c_2, c_3) = (-3, -4, -2)$ .
- (b) Solve problem (\*) when  $(c_1, c_2, c_3) = (7, 0, -2)$ .
- (c) Suppose  $(c_1, c_2, c_3) = (7, k, -2)$  in problem (\*). Find a value of  $k$  for which problem (\*) has more than one maximizing point. For this  $k$ , display two different maximizers.