## Automatas Celulares

March 8, 2021

## 0.1 Autómatas Celulares

https://matplotlib.org/matplotblog/posts/elementary-cellular-automata/

Una celda C solo conoce el estado de sus vecinos izquierdo y derecho, llamados L y R respectivamente. Podemos definir la función o regla f(L,C,R) que mapea el estado de la celda a 0 o 1.

```
[6]: #"Rule 30" could be constructed by first converting to binary and then building

→ an array for each bit

rule_number = 30

rule_string = np.binary_repr(rule_number, 8)

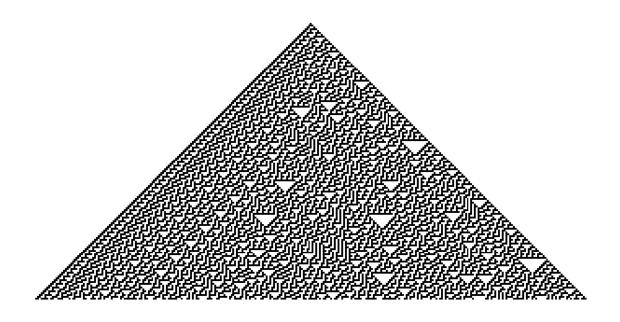
rule = np.array([int(bit) for bit in rule_string])

print(rule)
```

[0 0 0 1 1 1 1 0]

```
[7]: #By convention the Wolfram code associates the leading bit with '111' and the
       \rightarrow final bit with '000'.
      #For rule 30 the relationship between the input, rule index and output is as |
      → follows:
      for i in range(8):
          triplet = np.binary_repr(i, 3)
          print(f"input:{triplet}, index:{7-i}, output {rule[7-i]}")
     input:000, index:7, output 0
     input:001, index:6, output 1
     input:010, index:5, output 1
     input:011, index:4, output 1
     input:100, index:3, output 1
     input:101, index:2, output 0
     input:110, index:1, output 0
     input:111, index:0, output 0
 [9]: #We can define a function which maps the input cell information with the
      \rightarrow associated rule index.
      #Essentially we are converting the binary input to decimal and adjusting the
      \rightarrow index range.
      def rule index(triplet):
          L, C, R = triplet
          index = 7 - (4*L + 2*C + R)
          return int(index)
[11]: rule[rule_index((1, 0, 1))]
[11]: 0
[12]: rule[rule_index((0, 0, 1))]
[12]: 1
[15]: #Finally, we can use Numpy to create a data structure containing all the
      → triplets for our state array
      #and apply the function across the appropriate axis to determine our new state.
      all_triplets = np.stack([
          np.roll(data, 1),
          data,
          np.roll(data, -1)]
      new_data = rule[np.apply_along_axis(rule_index, 0, all_triplets)]
      print(new_data)
      #That is the process for a single update of our cellular automata.
```

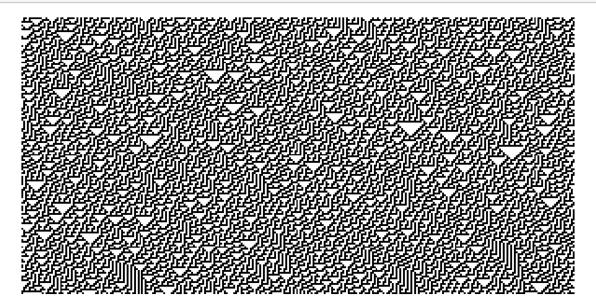
```
[16]: #To do many updates and record the state over time, we will create a function.
      def CA_run(initial_state, n_steps, rule_number):
          rule_string = np.binary_repr(rule_number, 8)
          rule = np.array([int(bit) for bit in rule_string])
          m_cells = len(initial_state)
          CA_run = np.zeros((n_steps, m_cells))
          CA_run[0, :] = initial_state
          for step in range(1, n_steps):
              all triplets = np.stack(
                  Γ
                      np.roll(CA_run[step - 1, :], 1),
                      CA_run[step - 1, :],
                      np.roll(CA_run[step - 1, :], -1),
                  ]
              CA run[step, :] = rule[np.apply_along axis(rule_index, 0, all_triplets)]
          return CA_run
[17]: initial = np.array([0, 1, 0, 0, 0, 1, 0, 0, 0, 1, 0, 0, 0, 1, 0, 1, 1, 1, 0])
      data = CA_run(initial, 10, 30)
      print(data)
     [[0. 1. 0. 0. 0. 1. 0. 0. 0. 1. 0. 0. 0. 0. 1. 0. 1. 1. 1. 0.]
      [1. 1. 1. 0. 1. 1. 1. 0. 1. 1. 0. 0. 1. 1. 0. 0. 1. 1. 0. 1. 0. 1.]
      [0. 0. 0. 0. 1. 0. 0. 0. 1. 0. 0. 1. 1. 1. 0. 0. 1. 1. 1. 1.]
      [1. 0. 0. 1. 1. 1. 0. 1. 1. 1. 1. 1. 0. 0. 1. 1. 1. 0. 0. 0.]
      [1. 1. 1. 1. 0. 0. 0. 1. 0. 0. 0. 1. 1. 1. 1. 0. 0. 1. 0. 1.]
      [0. 0. 0. 0. 1. 0. 1. 1. 1. 0. 0. 1. 1. 0. 0. 1. 1. 1. 0. 1.]
      [1. 0. 0. 1. 1. 0. 1. 0. 0. 1. 1. 1. 0. 1. 1. 1. 0. 0. 0. 1.]
      [0. 1. 1. 1. 0. 0. 1. 1. 1. 1. 0. 0. 0. 1. 0. 0. 1. 0. 1. 1.]
      [0. 1. 0. 0. 1. 1. 1. 0. 0. 0. 1. 0. 1. 1. 1. 1. 1. 0. 1. 0.]
      [1. 1. 1. 1. 1. 0. 0. 1. 0. 1. 1. 0. 1. 0. 0. 0. 0. 0. 1. 1.]]
[19]: | #A single 1 is initialized, with all other values set to zero.
      initial = np.zeros(300)
      initial[300//2] = 1
      data = CA run(initial, 150, 30)
      fig, ax = plt.subplots(figsize=(16, 9))
      ax.matshow(data)
      ax.axis(False);
```



```
[18]: #With random initial state
import matplotlib.pyplot as plt
plt.rcParams['image.cmap'] = 'binary'

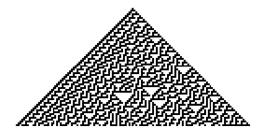
rng = np.random.RandomState(0)
data = CA_run(rng.randint(0, 2, 300), 150, 30)

fig, ax = plt.subplots(figsize=(16, 9))
ax.matshow(data)
ax.axis(False);
```



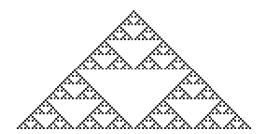
```
[40]: #A single 1 is initialized, with all other values set to zero.
initial = np.zeros(300)
initial[300//2] = 1
data = CA_run(initial, 64, 30)

fig, ax = plt.subplots(figsize=(16, 9))
ax.matshow(data)
ax.axis(False);
```



```
[39]: #A single 1 is initialized, with all other values set to zero.
initial = np.zeros(300)
initial[300//2] = 1
data = CA_run(initial, 64, 26)

fig, ax = plt.subplots(figsize=(16, 9))
ax.matshow(data)
ax.axis(False);
```

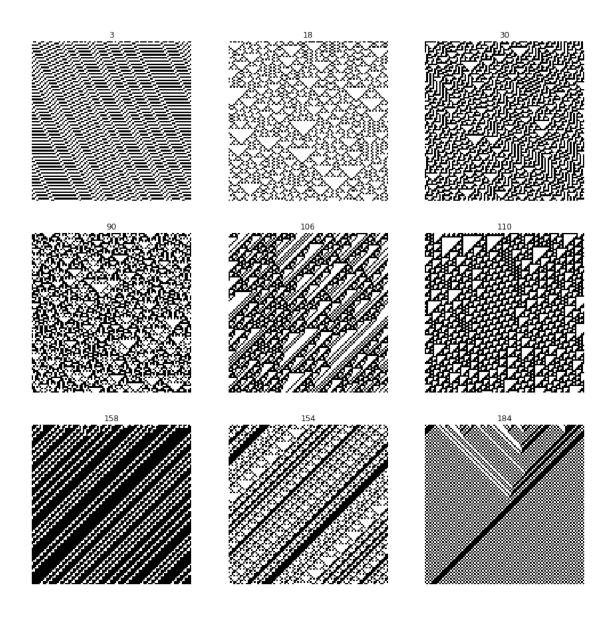


https://ipython-books.github.io/122-simulating-an-elementary-cellular-automaton/

```
[45]: import numpy as np import matplotlib.pyplot as plt
```

```
[49]: u = np.array([[4], [2], [1]])
```

```
def step(x, rule_b):
    """Compute a single step of an elementary cellular automaton"""
    # The columns contain the L, C, R values of all cells
    y = np.vstack((np.roll(x, 1), x,
                   np.roll(x, -1))).astype(np.int8)
    # We get the LCR pattern numbers between 0 and 7
    z = np.sum(y * u, axis=0).astype(np.int8)
    # We get the patterns given by the rule
    return rule b[7 - z]
def generate(rule, size=100, steps=100):
    """Simulate an elementary cellular automaton given its rule (number between\sqcup
→0 and 255)"""
    # Compute the binary representation of the rule.
    rule_b = np.array(
        [int(_) for _ in np.binary_repr(rule, 8)],
        dtype=np.int8)
    x = np.zeros((steps, size), dtype=np.int8)
    # Random initial state.
    x[0, :] = np.random.rand(size) < .5
    # Apply the step function iteratively.
    for i in range(steps - 1):
        x[i + 1, :] = step(x[i, :], rule_b)
    return x
rules = [3, 18, 30,
        90, 106, 110,
        158, 154, 184]
```



## 0.1.1 Autómatas Celulares en 2D con regla de solidificación

https://youtu.be/xgZuW6Jz5dc

```
[1]: import matplotlib.pyplot as plt
import numpy as np
import sys, pygame
pygame.init()

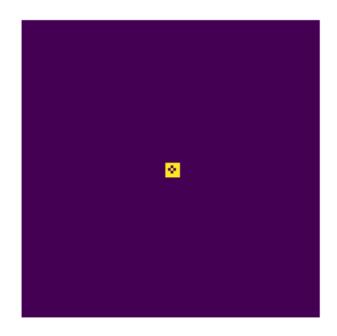
#Tamaño de pantalla
size = width, height = 1000, 1000

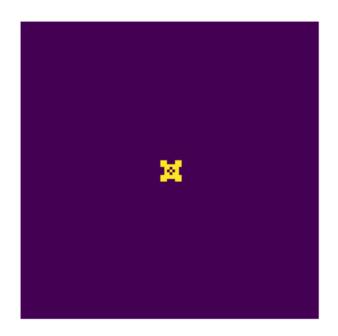
#Número de celdas
```

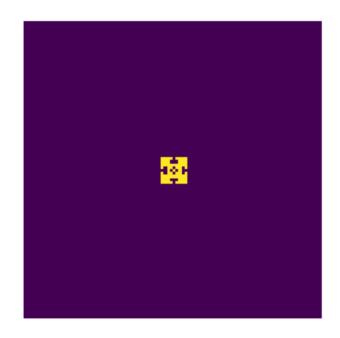
```
n = 100
nX = n
nY = n
dimCW = (width - 1)/nX
dimCH = (height- 1)/nY
bg = 25, 25, 25
screen = pygame.display.set_mode(size)
screen.fill(bg)
\#gameState = np.random.randint(0, 2, (nX, nY))
gameState = np.zeros((nX, nY))
gameState[int(n/2)-1,int(n/2)-1] = 1
gameState[int(n/2)-1,int(n/2)+1] = 1
gameState[int(n/2),int(n/2)] = 1
gameState[int(n/2)+1,int(n/2)-1] = 1
gameState[int(n/2)+1,int(n/2)+1] = 1
#print(gameState)
#Ciclo para crear las celdas y la malla
#Fronteras periódicas
for i in range(62):
    #pygame.event.pump()
    new_gameState = np.copy(gameState)
    screen.fill(bg)
    for y in range(0, nY):
        for x in range(0, nX):
            #Regla de Solidificación:
            #1. Si la celda está activa (estado 1) permanece activa
            #2. Si la celda está inactiva (estado 0) entonces se suman los_{\sqcup}
 →estados de las celdas vecinas,
            # si el número de celdas activadas en su entorno es 1 o 2, \sqcup
 →entonces la celda se activa,
                en caso contrario permanecerá desactivada
            ######FUNCIÓN PARA VER CUANTOS VECINOS DE [X,Y] ESTAN VIVOS
```

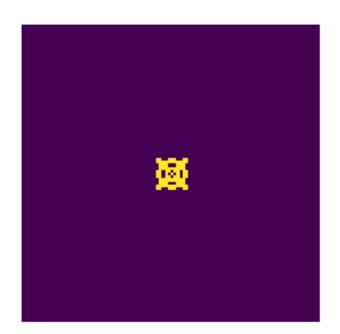
```
n_{\text{neigh}} = \text{gameState}[(x-1) \% nX, (y-1) \% nY] + 
                     gameState[(x) \% nX, (y-1) \% nY] + \
                     gameState[(x+1) % nX, (y-1) % nY] + \
                     gameState[(x-1) % nX, (y) % nY] + \
                     gameState[(x+1) % nX, (y) % nY] + \
                     gameState[(x-1) % nX, (y+1) % nY] + \
                     gameState[(x) \% nX, (y+1) \% nY] + \
                     gameState[(x+1) % nX, (y+1) % nY]
           #print(n neigh)
           ######APLICACIÓN DE LAS REGLAS
           if gameState[x,y] == 1:
               new_gameState[x,y] = 1
           elif gameState[x,y] == 0 and (n_neigh == 1 or n_neigh == 2):
               new_gameState[x,y] = 1
           poly = [((x)*dimCW,(y)*dimCH),
                  ((x+1)*dimCW, (y)*dimCH),
                  ((x+1)*dimCW, (y+1)*dimCH),
                  ((x)*dimCW,(y+1)*dimCH)
           pygame.draw.polygon(screen, (128, 128, 128), poly,
→int(abs(1-new_gameState[x,y])))
   gameState = new_gameState
   plt.matshow(gameState)
   plt.axis('off')
   plt.show()
   #pygame.display.flip()
```

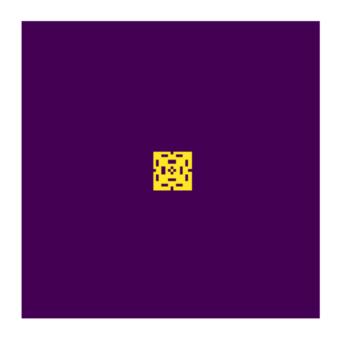
pygame 2.0.1 (SDL 2.0.14, Python 3.8.5)
Hello from the pygame community. https://www.pygame.org/contribute.html

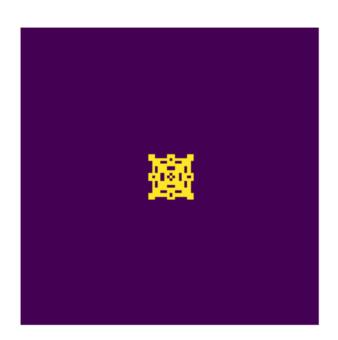


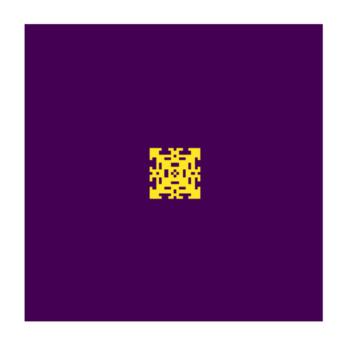


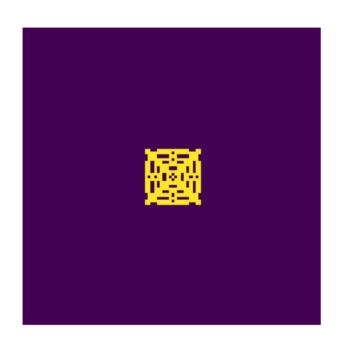


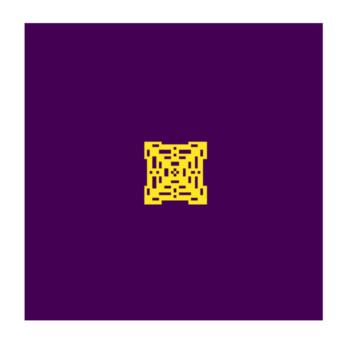


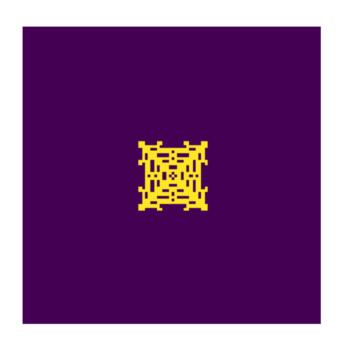


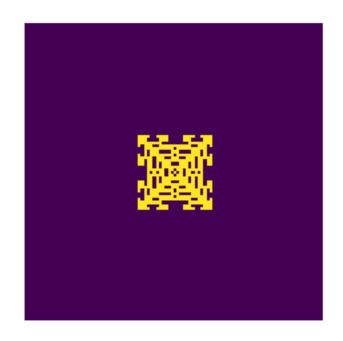


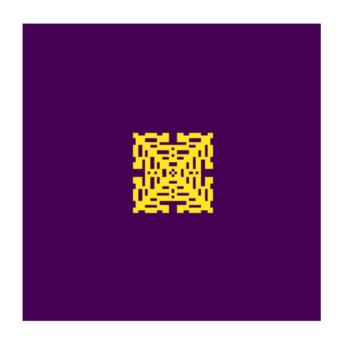


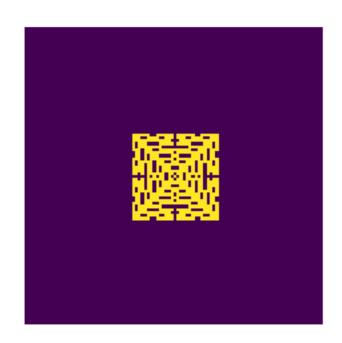


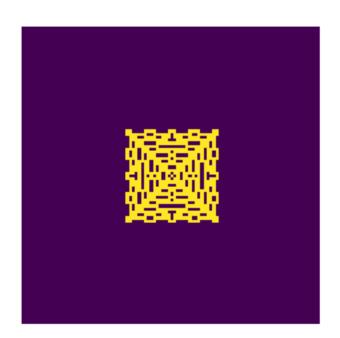


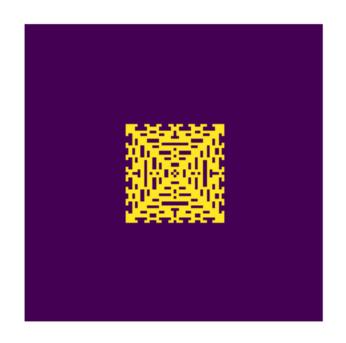


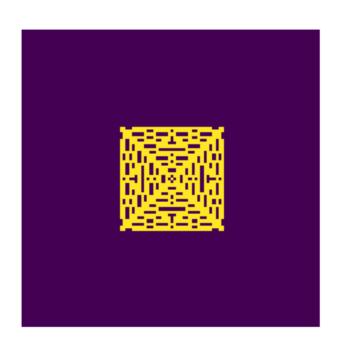


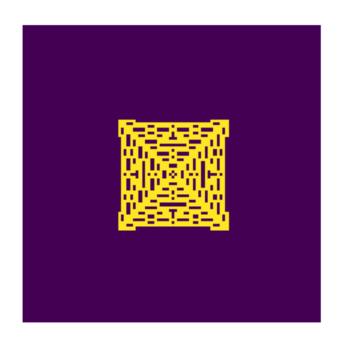


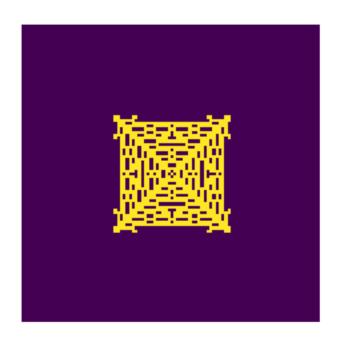


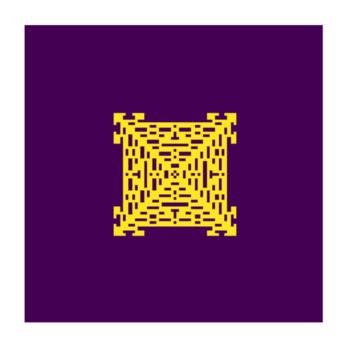


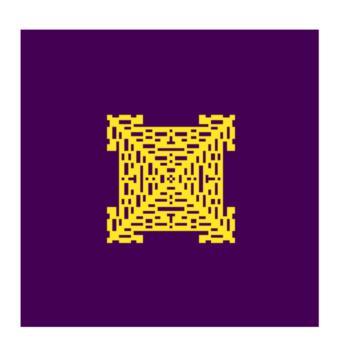


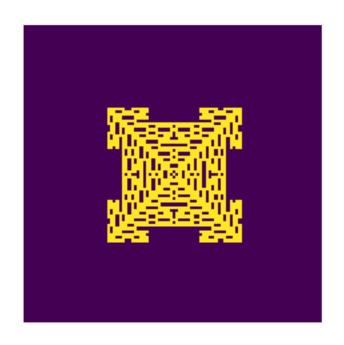


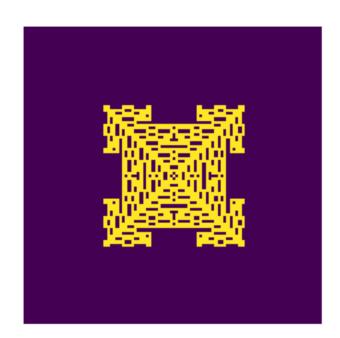


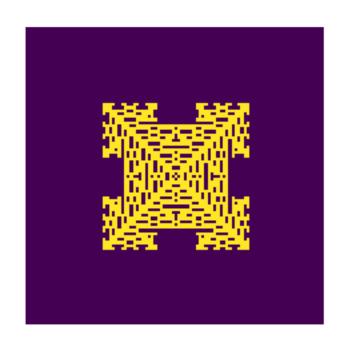


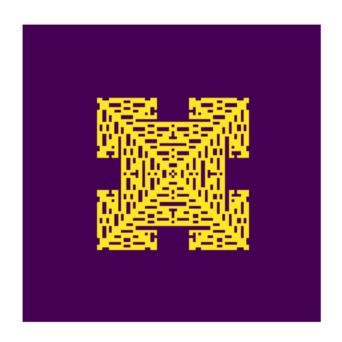


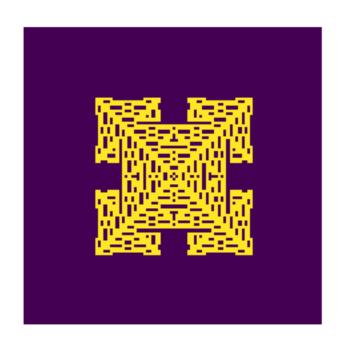


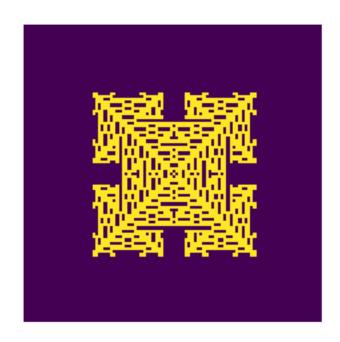


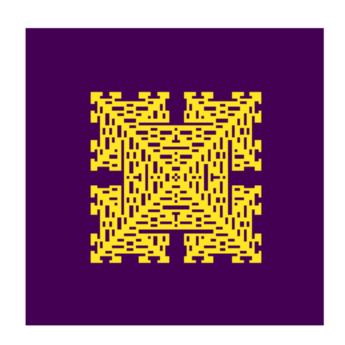


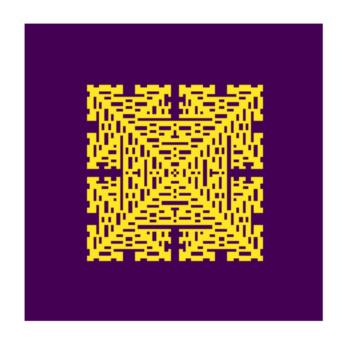


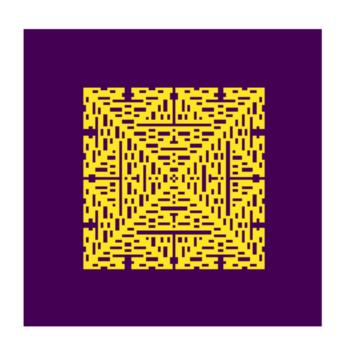


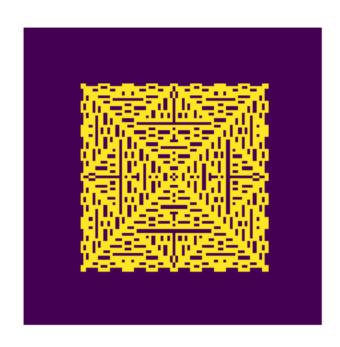


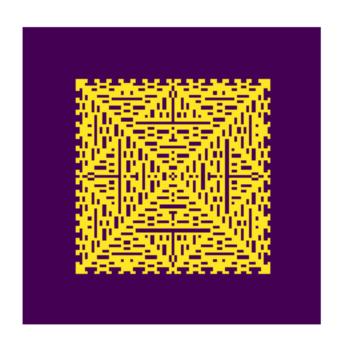


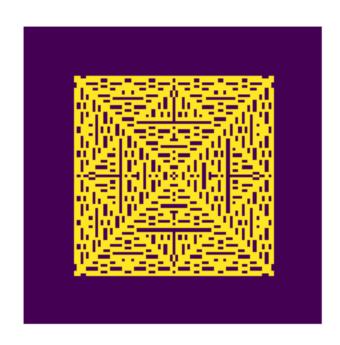


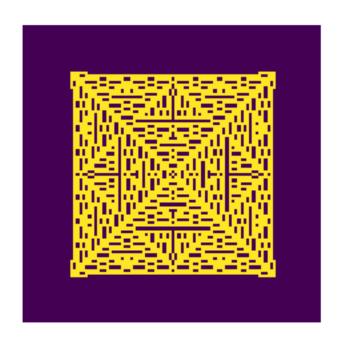


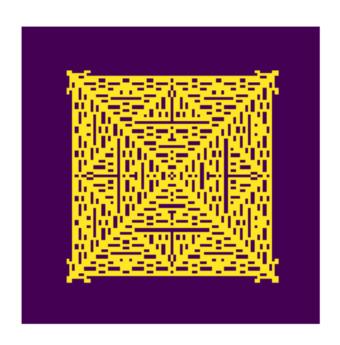


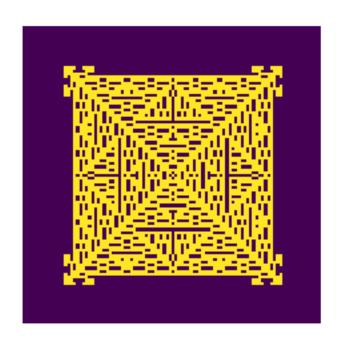


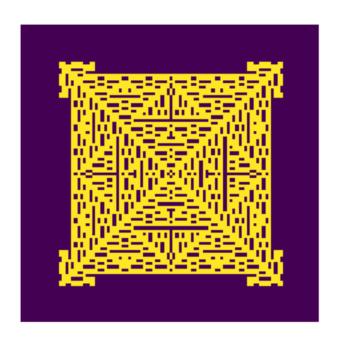


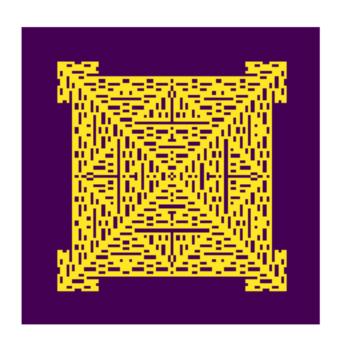


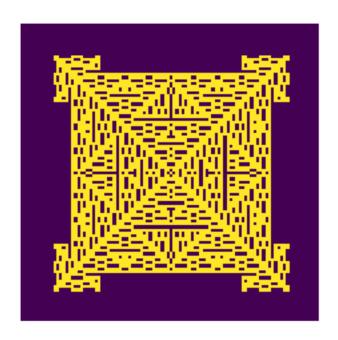


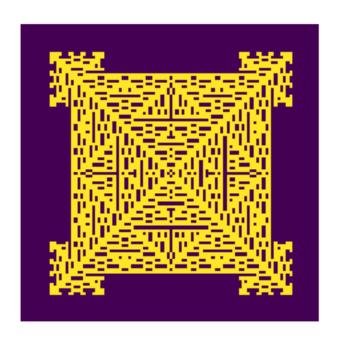


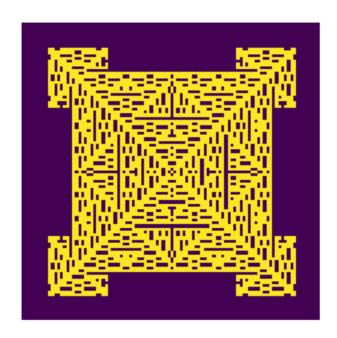


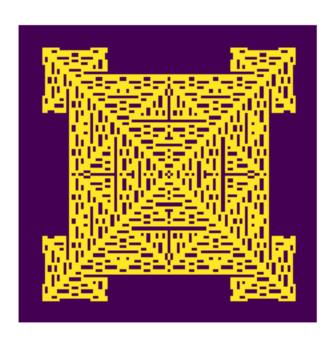


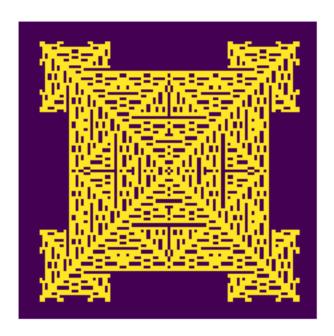


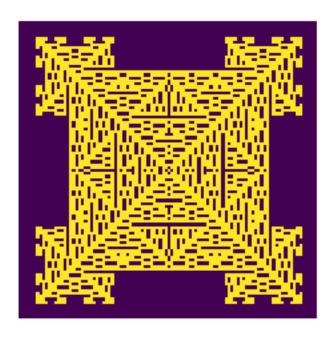


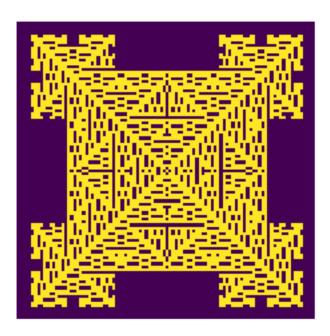


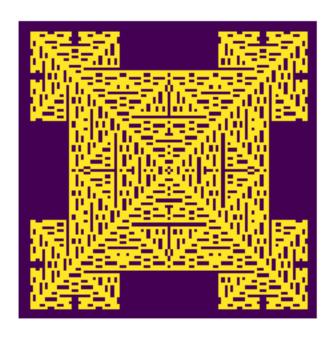


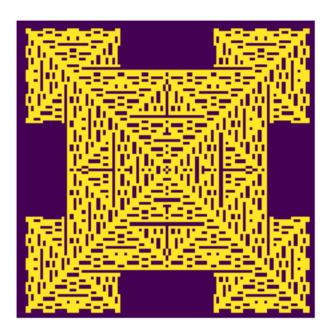


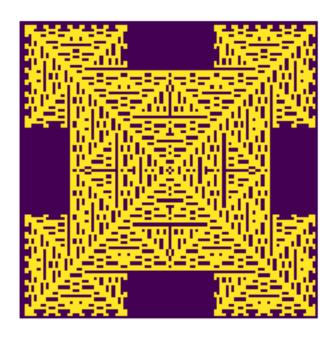


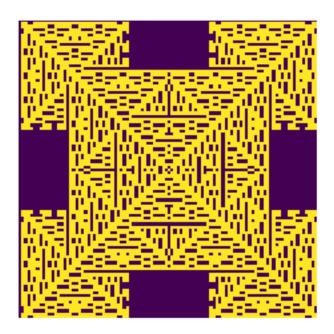


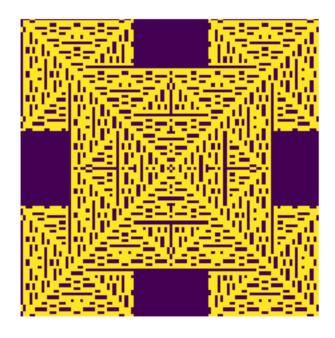


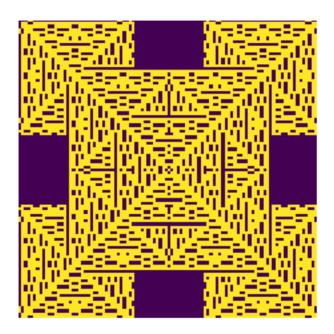


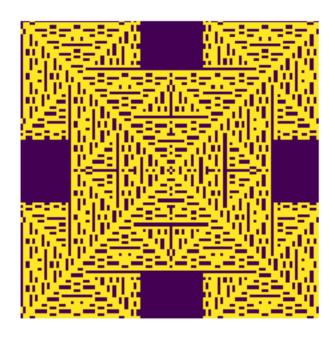


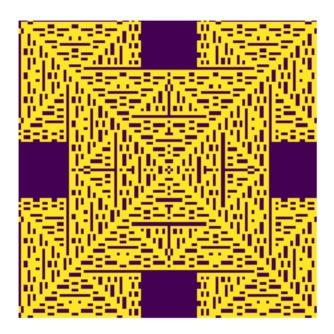


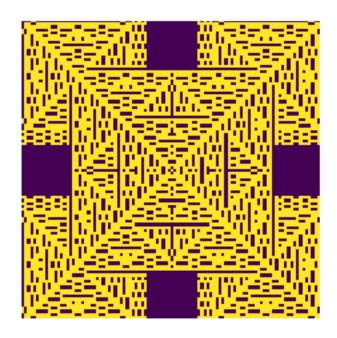


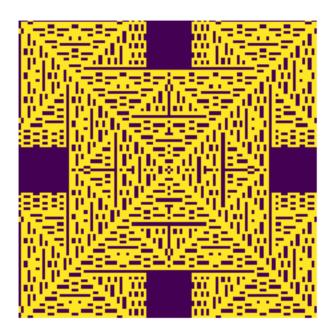


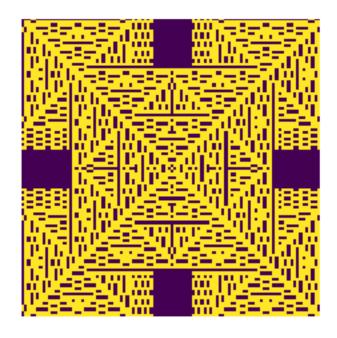


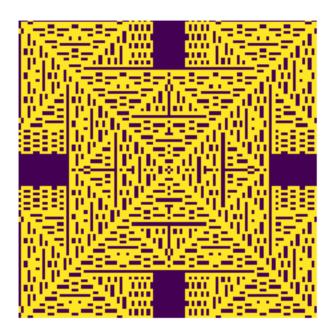


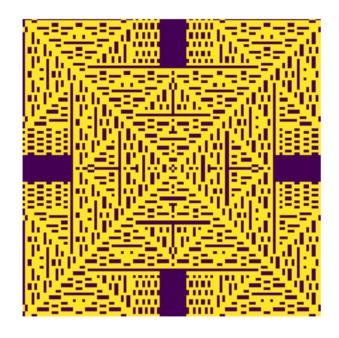


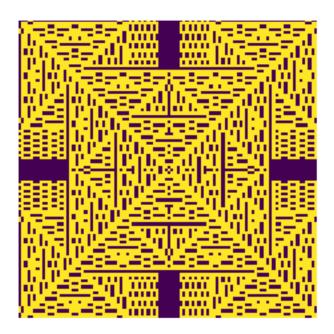


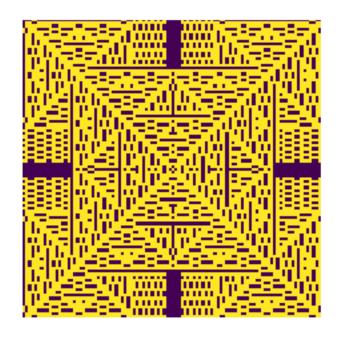


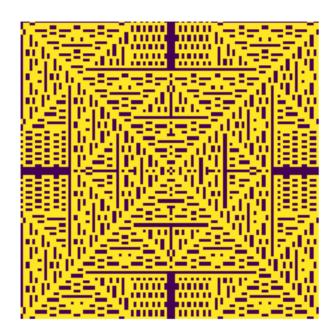


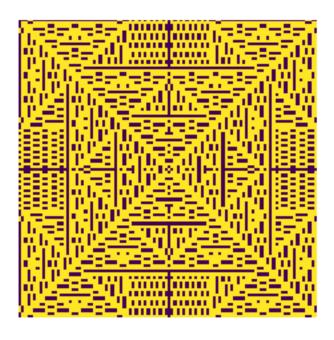


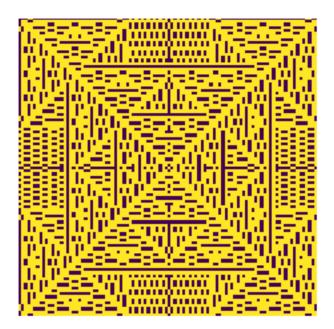












Hay patrones muy interesantes en 2D

```
[41]: import cellpylib as cpl

# initialize a 60x60 2D cellular automaton
cellular_automaton = cpl.init_simple2d(60, 60)
```

