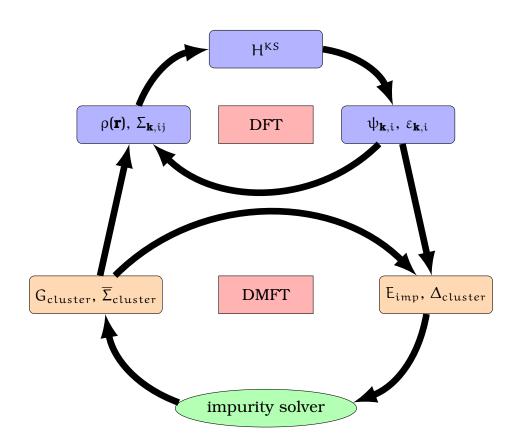
# User's Guide, DFTWIEN2k\_14.1+DMFT-Wien2K\_2012(2014)

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### Part I

# Introduction

One of the most challenging topics in condensed matter physics is the simulation and prediction of strongly correlated materials. The density functional theory plus dynamical mean-field theory (DFT+DMFT) method introduced in this userguide has been proven successful in fulfilling this target. The DFT+DMFT method is a combination of the traditional well-tested DFT method, in which the crystal problem is treated as the functional of electron density, and the DMFT method, where the local correlated physics is included in local self-energy. The DFT+DMFT method has been used in realistic simulations of strongly correlated materials, such as transition metals, lanthanides, actinides, as well as their compounds. We will give a detailed step-to-step introduction to the DFT+DMFT code in this userguide, from preparing the input files, checking whether the codes have arrived at converged and high-quality outputs, to how to extract realistic physical properties that can be compared with experiments.

This userguide is separated into four chapters: in the first chapter we give an introduction of the DFT+DMFT formalism; in the second chapter we present how to install the DFT+DMFT code; in the third chapter we present how to run the DFT+DMFT code, how to monitor the running, how to check if the outputs are converged, and how to improve the quality of your data; in the fourth chapter we use realistic examples to show the analysis of the DFT+DMFT output data, e.g.

derivation of physical properties, such as density of states (DOS), momentum resolved spectra, optical conductivity, etc.

The DFT+DMFT code has two parts: the DFT code and the DMFT code. In the DFT code, the inputs are atomic species and unit cell parameters. Its outputs are converged DFT Hamiltonian matrix at each k point and other parameters of the DFT Hamiltonian which are needed to construct local Green's function. The second part is the DMFT code. Inputs of DMFT are a choice of correlated orbitals and double counting, converged DFT Hamiltonian matrix and self-energy of previous iteration. After solving the DMFT equations with impurity solver, the local Green's function and new self-energy are fed back to the DFT iterations. There are three cycles in the DFT+DMFT codes, the DFT iterations, the DMFT iterations, and the DFT+DMFT charge self-consistent iterations. The final convergence is reached after the convergence of these three iterations.

- 1. The websites for downloading the source codes are shown below,
  - Where to download the *WIEN2k* source code for DFT calculations (version WIEN2k\_14.1):

```
http://www.wien2k.at/
```

Where to download the *DMFT-Wien2K* source code for DMFT calculations (version 2012):

```
http://hauleweb.rutgers.edu/downloads/
```

2. The major references for WIEN2k and DFT+DMFT are listed below,

• The major reference for WIEN2k is shown here,

(Haule et al., 2010)

 $\bullet$  The major references for DFT+DMFT are shown here,

(Blaha et al., 2001; Kotliar and Vollhardt, 2004; Kotliar et al., 2006)

### I.1 Electronic structure of crystal

### and Density Functional Theory (DFT)

Density Functional Theory (DFT) is an exact way to solve the many-body problem for weakly interacting electronic systems with nuclei at fixed positions, for instance, atoms, molecules, nanosystems and crystals. Even though DFT is formally exact, but the exact functional is still unknown, and presumably the functional has a non-closed form and would be extremely non-local. Generally, DFT is good for vibrational properties, structural stability, elasticity and equations of states. Many systems are treated well using DFT, whereas DFT does not work well for other systems which have uncontrolled approximations. Below summarizes the variables and equations to construct exact functional for time-independent standard DFT. (see Tables 1, 2)

Solving Kohn Sham equations is one of the primary computational tasks, and it requires a self-consistent iterative process since the external potentials are dependent on rounds of calculating spin electron densities and orbitals. In summary, DFT is the exact theory to determine the ground state properties of electronic systems by spin electron densities. (Kotliar et al., 2006)

Table 1: Variables for DFT

ρ ( <b>r</b> )	local electronic charge density of the solid
Ψ	exact many body wavefunction
V	external potential
V <sub>KS</sub>	Kohn Sham potential
$T_s[\rho(\mathbf{r})]$	kinetic energy of noninteracting electron gas
Exc	local exchange correlation energies
Ψί	Kohn-Sham wave functions for single particle orbitals

Table 2: Formulas for DFT

$\rho(\boldsymbol{r}) = <\Psi^*\Psi>$	Groud state spin electron density
$E_{tot} = T_s[\rho(\boldsymbol{r})] + E_{xc}[\rho(\boldsymbol{r})] + V$	Total energy equation
$H = \sum_{i=1}^{N} (-\nabla^2) + \sum_{i} (V(r_i)) + \frac{1}{2} \sum_{i \neq j} (\frac{e^2}{ r_i - r_j })$	Exact Hamiltonian
$[-\bigtriangledown^2 + V_{KS}(\mathbf{r})]\Psi_i = \varepsilon_i \Psi_i$	Kohn-Sham equations
$V_{KS}(\mathbf{r}) = v_{ext}(\mathbf{r}) + v_{H}(\mathbf{r}) + v_{xc}(\mathbf{r})$	Kohn-Sham potential
	External potential
$ u_{H}(\mathbf{r}) = \int rac{\mathfrak{n}(\mathfrak{r}')}{ \mathbf{r} - \mathfrak{r}' } $	Hatree potential
$ u_{\mathrm{xc}}(\mathbf{r}) = \frac{\delta E_{\mathrm{xc}}[n(\mathbf{r})]}{\delta n(\mathbf{r})} $	Exchange correlation potential
$\rho (\mathbf{r}) = \sum_{i=1}^{N} \Psi_i^*(\mathbf{r}) \Psi_i(\mathbf{r})$	Kohn Sham interacting density

# I.2 Strongly correlated systems and Dynamical Mean\_Field Theory (DMFT)

### I.2.1 Strongly correlated systems

Materials could be categorized into conductors, semiconductors and insulators based on their easiness of conducting electricity. Almost all the metals are conductors, but the physical properties of the metals and their oxides could be different if they belong to different groups in the periodic table.

Main-group metals, such as aluminum and silicon, have weakly correlated electrons, and we can assume their electrons are delocalized and independent. In this case, DFT allows us to compute the total energy of the materials with high accuracy.

On the other hand, we can not ignore the interactions between the electrons in the d and f shells in transition metals and their oxides, e.g., iron, vanadium and their oxides, because these electrons which occupy the partially filled shells are too close to each other in the narrow orbitals, and Coulomb repulsion among d and f electrons are too strong. In this case, the strongly correlated electrons cannot be viewed as being immersed in the static mean field generated by other electrons. Consequently, the strongly correlated materials are more sensitive to change of external parameters, for example, temperature, pressure or doping. While it is hard to exactly calculate the full many-body model Hamiltonians for strongly correlated systems, various analytical and numerical methods

have been developed to handle those challenges. Dynamical Mean-Field Theory (DMFT) is one of them.

### I.2.2 DMFT formulism

To simplify the many-body lattice problem, theorists mapped the single-site lattice model (e.g., Hubbard model) onto a self-consistent quantum impurity model (e.g., Anderson impurity model), which forms the basis of DMFT. They apply the analytic and numerical techniques such as quantum Monte Carlo to solve the impurity models.

DMFT simplifies the spatial dependence of the correlations among electrons and yet accounts fully for their dynamics - that is, the local quantum fluctuations missed in static mean-field treatments. One can extract the density of states of the strongly correlated systems from the impurity model. One key point is DMFT reproduces the local part of the Green's function of the system. A more system-specific modeling of strongly correlated materials requires both band theory and many-body theory. Below summarizes the variables and formulas to derive the exact functionals, (see Tables 3, 4) (Kotliar et al., 2006)

Table 3: Variables for DMFT

i,j	lattice site
au, au'	time
t <sub>if</sub>	matrix element, describes hopping of electrons
σ	electron spin (↑ or ↓)
u	local Coulomb interaction
$n_{i\sigma}$	density of electrons at site i with spin $\sigma$
h.c.	Hermitian conjugate
H <sub>AIM</sub>	Anderson impurity model Hamiltonians
$H_{atom}$	a general Hamiltonian, a lattice site's atomic degrees of freedom
$\varepsilon_{\nu}^{ m bath}$	a bath of electrons with energy levels
$V_{\gamma}$	hybridization
$c_{0,\sigma}$	atomic electrons
$\mathfrak{a}_{\nu,\sigma}^{\text{bath}}$	bath electrons
$\Delta(\omega)$	mean field
$t_k$	Fourier transform of the hopping matrix $t_{ij}$

Table 4: Formulas for DMFT

$\label{eq:Giscontinuous} \boxed{ G_{\text{i}\sigma}(\tau - \tau') \equiv - < c_{\text{i}\sigma}(\tau) c_{\text{i}\sigma}^{\dagger}(\tau') > . }$	Green function specifies the probability
$H = \sum_{ij,\sigma} t_{ij} c^{\dagger}_{i\sigma} c_{j\sigma} + U \sum_{i} n_{i\uparrow} n_{i\downarrow}$	Hubbard model
$H_{AIM} = H_{atom} + \sum_{\nu,\sigma} \epsilon_{\nu}^{bath} n_{\nu,\sigma}^{bath} +$	
$\sum_{\nu,\sigma} (V_{\nu} c_{0,\sigma}^{\dagger} a_{\nu,\sigma}^{\text{bath}} + \text{h.c})$	Anderson impurity model
$\Delta(\omega) = \sum_{\mathbf{v}} rac{( \mathbf{V}_{\mathbf{v}} )^2}{\omega - \varepsilon_{\mathbf{v}}^{\mathrm{bath}}}$	hybridization function
$G[\Delta(\omega)] = \sum_{k} \omega - \sum_{k} [\Delta(\omega)] - t_{k}^{-1}$	self-consistency condition
$E_{\text{tot}} = T_s[\rho(\mathbf{r})] + E_{\text{xc}}[\rho(\mathbf{r}), G] + V$	total energy equation

### I.3 DFT + DMFT

### I.3.1 Basics of DFT + DMFT

To take into account the strong correlation effects in a more accurate way, a combined DFT + DMFT method has been proposed for studying the extended strongly correlated systems. In this approach, the first step is to do DFT approximations on system geometry and electron band structure of 'non-correlated' quasi-particles. In the DFT + DMFT approach for extended systems, the central quantity is the local Green's function, which is a particular case of the general time-ordered Green's function. In practice, DFT calculations give the optimized structure, then DMFT shows its Green's functions, includes the dynamical effects, implements self-consistency conditions and consequently physical properties of finite systems where electron-electron correlation effects play an important role.

Below summarizes the variables and formulas for DFT + DMFT, (see Tables 5, 6) (Kotliar et al., 2006; Kotliar and Vollhardt, 2004)

Table 5: Variables for DFT + DMFT

$c_{i\sigma l}^{\dagger}$	creation operator of the fermion at site i with spin $\boldsymbol{\sigma}$
$c_{j\sigma m}$	annihilation operator of the fermion at site j with spin $\boldsymbol{\sigma}$
$n_{i\sigma l} = c^{\dagger}_{i\sigma l} c_{i\sigma l}$	corresponding particle number operator
$t_{il;jm}$	matrix elements, hopping parameters
$U_{\sigma\overline{\sigma}}^{lm}n_{i\sigma l}$	Coulomb repulsion matrix
$\omega - \varepsilon_{DFT}(\mathbf{k})$	free quasi-particle spectrum
μ	chemical potential
$\mu - \sum_{\omega}(\omega)$	quasi-particle self-energy
$G_{\sigma l;\sigma'm}^{-1}(\omega)$	effective dynamical mean field
$\psi,\psi^*$	Grassmann variables

Table 6: Formulas for DFT + DMFT

$H = -\sum_{i,j,\sigma,l,m} t_{il;jm} c_{i\sigma l}^{\dagger} + \sum_{i,\sigma,\sigma',l,m} U_{\sigma\overline{\sigma}}^{lm} n_{i\sigma l} n_{i\overline{\sigma}m}$	typical DMFT Hamiltonian
$G_{\mathfrak{i}\sigma\mathfrak{l};\mathfrak{j}\sigma\mathfrak{m}}(t,t') = -\mathfrak{i} < Tc_{\mathfrak{i}\sigma\mathfrak{l}}(t)c_{\mathfrak{j}\sigma\mathfrak{m}}^{\dagger}(t') >$	local Green's function
$G_{\sigma l;\sigma' m(\omega)} = \int \frac{d\boldsymbol{k}}{(2\pi)^d} (\frac{1}{\omega - \epsilon_{DFT}(\boldsymbol{k}) + \mu - \sum(\omega)})$	local Green's function
$n_{\sigma l} = -\int \frac{\mathrm{d}\omega}{2\pi} \int \frac{\mathrm{d}\boldsymbol{k}}{(2\pi)^d} Im G_{\sigma l;\sigma l}(\omega)$	orbital spin density
$G_{\sigma l;\sigma' m}^{-1}(\omega) = (G^{-1}(\omega) + \sum_{\sigma l;\sigma' m})^{-1}_{\sigma l;\sigma' m}$	effective dynamical mean field
$G_{\sigma l;\sigma' m}(\omega) = \int D[\psi] D[\psi^*] \psi_{\sigma l} \psi_{\sigma^* m}^* e^{A[\psi,\psi^*,Q^{-1}]}$	quantum impurity problem

### I.3.2 Flow chart (Figure 1)

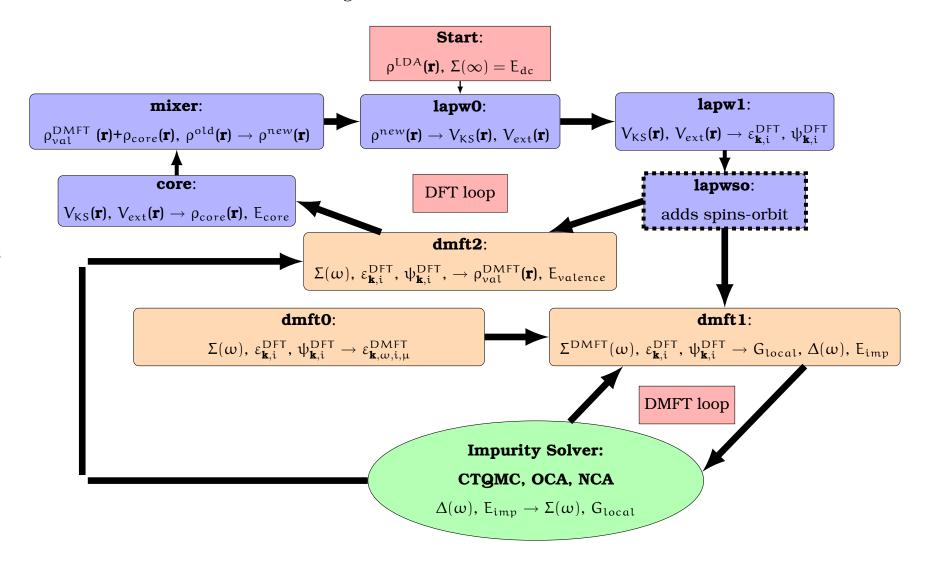
The following flow chart for DFT + DMFT code shows the two sections of the code, DFT code and DMFT code.

DFT code has the following inputs, atomic species and unit cell parameters. Its outputs are local, orthogonalized, converged DFT Hamiltonian matrix on a local axis at each k point, parameters of the unperturbed Hamiltonian which are needed to construct local Green's function.

DMFT code has the following inputs, choices of correlated orbitals and double counting, convereged Hamiltonian matrix and self-energy. Its outputs are the bath function and a new self-energy. The output of the recomputed density will be used as input for the DFT calculations.

These two self-consistency processes (DFT self-consistency process and DMFT self-consistency process) will continue until both the total density and the local Green's function have converged.

Figure 1: Flow chart of DFT+DMFT



### Part II

# Installation

For detailed information about how to download, properly install and configure the *WIEN2k* source code for DFT calculations (version WIEN2k\_14.1, please refer to *WIEN2k User's Guide*, *WIEN2k\_14.1*.

```
http://www.wien2k.at
```

Furthermore, below illustrates how to properly install and configure the *DMFT-Wien2K* source code for DMFT calculations (version 2012).

The program consists of many independent programs and executables, which are written in C++, fortran 90 and Python. Before you start the installation, you must make sure that the following packages are installed in the system.

- intel mkl library
- gnu C++ compiler
- intel fortran compiler or gnu fortran compiler
- gsl library: gnu scientific library
- Python with numpy and scipy
- Python CXX package

Except for some Python packages, these are quite standard codes, which are likely already installed.

The compilation consists of six simple steps:

• download the code here:

```
http://hauleweb.rutgers.edu/downloads/,
unpack it (tar xzvf dmft_w2k.tgz) and cd to directory main.
```

- Edit the file *Makefile.in* under the main directory to set the path to compilers on the system, their options, and libraries (see description below)
- set the environment variable *WIEN\_DMFT\_ROOT* (in /.bashrc) to point to the directory you plan to install the binaries code
- type **make**
- type make install
- for execution, also make sure that the following variables are properly set in .bashrc:
  - WIENROOT: should be set during *WIEN2k* installation to *WIEN2k* executables.
  - PATH=\$WIENROOT:\$WIEN\_DMFT\_ROOT:\$PATH: add both dmft and wien executables to your path.
  - PYTHONPATH=:\$WIEN\_DMFT\_ROOT::\$PYTHONPATH: add dmft binary dir to PYTHONPATH.
  - OMP\_NUM\_THREADS=< n >: you might want to set number of cores for multithreading. Note that dmft1 and dmft2 steps support multi-

threading. ctqmc uses only mpi (which is very efficient in Monte Carlo). For ctqmc, it is best to have OMP\_NUM\_THREADS=1 to avoid collision between independent Monte Carlo walkers parallelized by MPI. For dmft1 and dmft2 steps, one can use double parallelization: k-point parallelization with MPI and extra parallelization with open\_mpi, setting OMP\_NUM\_THREADS to number of cores on a node. For non-experts, set OMP\_NUM\_THREADS=1.

- EDITOR: environment variable EDITOR should be set (during WIEN2k installation) to preferred editor, for example "emacs -nw" or "vi".
- SCRATCH: environment variable SCRATCH should be set to current dir, i.e., export SCRATCH=./

Here we will briefly describe the options which are set in *Makefile.in* and might need to be changed. Note that this file *Makefile.in* is included in all other makefiles located in subdirectories (there are around 20 makefiles in total), hence no other makefile needs to be edited.

### *Makefile.in* contains:

- DESTDIR = \$ (WIEN\_DMFT\_ROOT) : Here we expect that environment variable \$WIEN\_DMFT\_ROOT is set on the system (likely in .bashrc).
- F90 = ifort : non parallel version of fortran compiler, which is used to compile smaller modules.
- F77 = ifort : some older modules need non-parallel fortran77 compiler.

- preproc = cpp : preprocessor, which ca preprocess source code (in this case fortran files).
- WFOPT = -xHOST -03 -ipo -no-prec-div -traceback -FR -override-limits openmp -I\$(MKLROOT)/include/intel64/lp64 -I\$(MKLROOT)/include: fortran options for both dmft1 (ksum) and dmft2 (chargesc) codes. More detailed explanation of some options.
  - -03 -override-limits -pad -mavx : These options are for maximal optimization, regardless of memory required, and using intels avx technology, etc... These options most likely need some changes on different platforms.
  - -pre\_div -mpl -pc80 : controls floating point precision. Might need to be changed.
  - -FR: is needed to tell compiler that fortran code is written in free format even when extension of files is ".f".
  - openmp: the code is using multi-threading techniques, hence it is
     wise to enable them.
  - -DINTEL\_VML defines to use Intel's vector math library (if available).
- FFLAGS = -O3 -fPIC : similar fortran options than above. These are used in some fortran codes which are packed into python modules (.so) and they need extra option "-fPIC". This option ensures position independent code, which can be packed into shared libraries.

- C++ = icpc : both g++ and intel icpc should work here. It is used for smaller impurity modules.
- OFLAGS = -O3: options for C++ compiler for these small impurity modules.
- GFLAGS = -g -C : options for C++ compiler for these small impurity modules.
- CMP = f2py -fcompiler=intelem: name of the fortran to python converter.

  The option "-fcompiler=intelem" might need to be changed, because it depends on the platform.
- WLDFLAGS = -i-static \$(FOPT) : linking flags for many fortran codes, such as dmft1 step.
- WLIBS = -L\$(MKLROOT)/lib/intel64 \$(MKLROOT)/lib/intel64/
   libmkl\_blas95\_lp64.a \$(MKLROOT)/lib/intel64/ libmkl\_lapack95\_lp64.a
   -lmkl\_cdft\_core -lmkl\_intel\_lp64 -lmkl\_intel\_thread -lmkl\_core
   -lmkl\_blacs\_intelmpi\_lp64 -liomp5 -lpthread -lm
   : linking options for dmft2 steps, which does not use WLDFLAGS, and also requires intel math library.
- PFLAGS = -D\_MPI -DMPICH\_IGNORE\_CXX\_SEEK -I/home/user/gsl/include : compilation flags for ctqmc code compiled with PC++. Here "-D\_MPI" enables parallel version, "-DMPICH\_IGNORE\_CXX\_SEEK" avoids some name-conflict between mpich and standard libraries. The rest of the options are for optimization.

- PC++ = mpicxx : parallel C++ compiler used for compiling ctqmc code.
- pcc = mpicc : parallel c-compiler
- PLIBS = -L\$(MKLROOT)/lib/intel64 \$(MKLROOT)/lib/intel64/
   libmkl\_blas95\_lp64.a \$(MKLROOT)/lib/intel64/libmkl\_lapack95\_lp64.a
   -lmkl\_cdft\_core -lmkl\_intel\_lp64 -lmkl\_intel\_thread -lmkl\_core
   -lmkl\_blacs\_intelmpi\_lp64 -liomp5 -lpthread -lm -L/home/rcohen/lib
   -L/share/apps/intel/impi/4.0.1.007/intel64/lib -lmpich -lgsl
   : linking options for ctqmc. We need gsl library for random number generator.
- LLIBS = -L\$(MKLROOT)/lib/intel64 \$(MKLROOT)/lib/intel64/
  libmkl\_blas95\_lp64.a \$(MKLROOT)/lib/intel64/libmkl\_lapack95\_lp64.a
  -lmkl\_cdft\_core -lmkl\_intel\_lp64 -lmkl\_intel\_thread -lmkl\_core
  -lmkl\_blacs\_intelmpi\_lp64 -liomp5 -lpthread -lm
  -L/share/apps/intel/impi/4.0.1.007/intel64/lib -lmpich
  : linking options for other C++ utility modules.
- CMPLIBS = -opt='-fast' -link-lapack\_opt : options for f2py compiler. We
   need to link lapack and blas to several f2py modules.
- CMPLIBS2 = -f90flags='-openmp' -opt='-fast' -link-lapack\_opt: some python modules written in fortran can support multithreading, hence we allow openmp.

Note: When installing numpy on a linux distribution, make sure to use gnu c++ compiler (as opposed to intel c++ compiler). Before installing numpy and scipy, you should set environment variables CC and CXX to CC=gcc and CXX=g++. Otherwise, f2py might use intel c++ compiler (icc and icpc), which does NOT work properly in some versions of python. (Haule et al., 2010)

### Part III

# General steps for running

# self-consistent cycles in DFT +

# **DMFT**

### III.1 DFT part

### III.1.1 Prepare struct-files

### III.1.1.1 Gather all the required information

- The lattice parameters, lengths a, b, c in Bohr or Ångstrom and angles  $\alpha$ ,  $\beta$ ,  $\gamma$ .
- The space group according to the "International Tables for Crystallography",
   http://it.iucr.org/.
- The positions of all equivalent atoms (number them 1, 2, 3, ..., e.g., Fe 1, Fe 2, if there are many) and the positions of all inequivalent atoms in fractions of the unit cell. Alternatively you can utilize *StructGen* in WIEN2k to generate all the equivalent positions automatically by providing only the inequivalent positions and the space group.

#### III.1.1.2 Generate struct-files

A new struct-file should be generated on which we can run DFT and DMFT calculations. There are many approaches, such as by hand (using a simple command, converting other files into struct-files and manipulating example struct-files) and by using *w2web*.

### • Use a simple command, makestruct\_lapw

In the newest version of WIEN2k, i.e., WIEN2k\_14.1, we can easily create struct-files by a simple command shown below and then interactively type in all the required input information.

### "makestruct\_lapw"

Note that this command can only generate a struct-file named *init.struct*. Copy it to your desired name *case.struct* by the command,

### "cp init.struct case.struct"

Also, please be reminded that *makestruct\_lapw* command is only suitable for small to medium sized cells. For large sized cells, *cif2struct* is recommended which will be introduced next.

• Convert other files into struct-files using *cif2struct* 

Besides the *makestruct\_lapw* command, converting established *.cif, .txt* files into *.struct* files is sometimes more convenient.

Store structural data in *case.cif* or *case.txt* files, then convert them into the *case.struct* files using the commands,

### "cif2struct case.cif" or

#### "cif2struct case.txt"

Some .cif files are available for download from Crystallographic databases (e.g., the Inorganic Crystal Structure DataBase).

.txt files can be created by hand. Type in the following command to make a new .txt file.

### "vi case"

Make sure that the *.txt* file contains all the data in the correct format, and one example of the contents of the *.txt* file is given below, (see Table 7)

Table 7: Example .txt file to be converted into .struct file

b						"aAng, bBohr"
0.0	0.0	0.0				"shift of origin"
8.1450	8.1450	8.1450	90	90	90	"a, b, c, angles $\alpha, \beta, \gamma$ "
Fm-3m						"space-group symbol"
Fe						"atom- name"
0.000000	0.000000	0.000000				"atomic position"

• Manipulate existing example struct-files

When the elements in the compounds are very similar and presumably the

unit cell structures are quite similar, it is also acceptable to make some mi-

nor modifications on the parameters in the existing example struct-files. You

can find and download some example struct-files in the installed WIEN2k

folder, i.e., example\_struct\_files folder, or from the Input Files/struct column

on Haule's website,

http://hauleweb.rutgers.edu/database\_w2k/

### • Use *w2web* to set up struct-files

The new interface w2web provides a more user-friendly environment to make struct-files and derive some properties thereafter.

For the first-time user, set up your username and password by the command,

### "w2web -p xxxx"

in which "xxxx" stands for the default port number (7890) or a different port number between 1024 and 65536.

If you forget your portnumber, simply use the command,

### "ps -ef | grep w2web"

If the remote server machine, e.g., mw, does not have the browser installed, you can establish a tunnel between mw server and your local server by the command.

### "ssh -X -L 5890:localhost:7890 mw"

In the above case, 7890 and 5890 are considered as port 1 on the *mw* side and port 2 on the local side (any random number you want) respectively. Once the tunnel is established, you can start using *w2web* interface by opening your local browser, e.g., *firefox*, and typing in the following address and your username and password,

#### "username@localhost:5890"

In the w2web interface, there are three steps to set up the session part. The first step is to *Create new session* if you don't have one, choose your session

name (*case*) and click *Create*. The second step is to change into or create a new directory in which all your output files will be stored, and click *Select current directory*. The last step is to click *Click to restart session*, and the main window of *w2web* will show up. (see Figure 2)

10:21:49 idle Session: [FCC Fe at 1500K 0atm] /home/aliu/WIFN2k w2web, the fully web-enabled interface to WIEN2k Session Name: FCC Fe at 1500K 0atm Session ID: 467052 Directory: /home/aliu/WIEN2k Last changed: Mon Jul 21 10:20:43 2014 Comments: single prog. ] spin polarized calculation [ mini. positions ] AFM calculation B complex calculation (no inversion) [ Utils. >> ] parallel calculation [ Tasks >> ] Change session information [ struct file(s) ] [ input files ]
[ output files ]
[ SCF files ] Session Mgmt. >> ] w2web © luitz.at [ change dir ] W2web Usersquide [ html-Version ] [ pdf-Version ]

Figure 2: Main window of *w2web* 

On the left side of the w2web main window, start the struct-file generator by clicking on  $StructGen^{TM}$  under the directory Execution >>. It will ask for the necessary information to create case.struct. The questions asked and some actions taken are listed below.

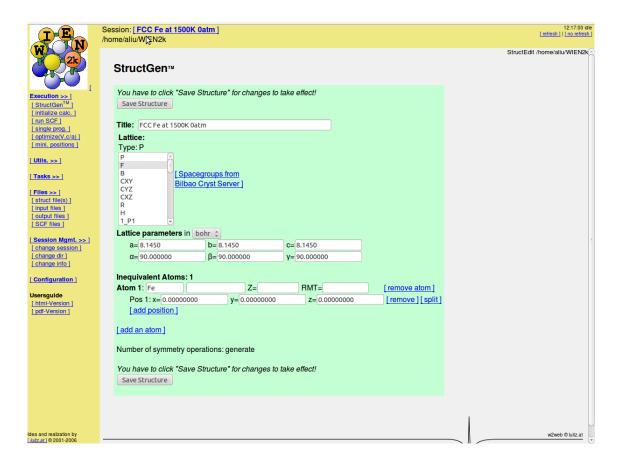
- Please specify the number of independent atoms of your initial structure

- Click Generate template
- Title
- Lattice Type
- Lattice parameters (lengths: a, b, c in Å or bohr) (angles:  $\alpha$ ,  $\beta$ ,  $\gamma$ )
- Inequivalent Atoms:

Atom n: Atom-name

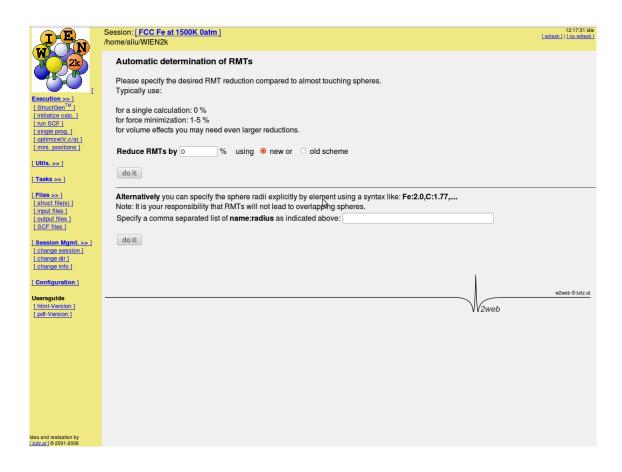
Pos n: Atomic position of atom n (see Figure 3)

Figure 3: StructGen screen before clicking "Save Structure"



- Click Save Structure
- Click set automatically RMT and continue editing (do it at least once!) (RMT: muffin-tin radius, atomic sphere radius) (see Figure 4)

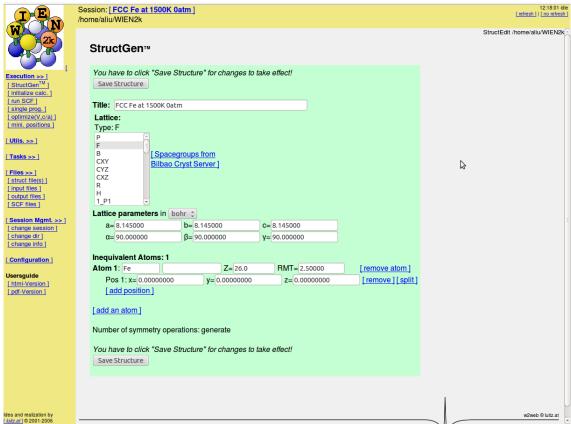
Figure 4: Choosing options for Automatic determination of Radius of Muffin-Tin (RMT)



 Click do it! (Z and RMT values will be calculated automatically for each atom) (figure 5)

Figure 5: StructGen screen after saving

Session: [FCC Fe at 1500K 0atm]



- Click Save Structure
- Click save file and clean up (when you are done) (View only mode of Struct-file will show up) (see Figure 6)

Figure 6: StructGen screen after cleaning up



To double check if your *case.struct* is in your specified directory, go to *show* all files under the directory Files >>.

• One example of .struct file

Below illustrates the head part of one example of the generated struct-file for FCC Fe. (see Table 8)

Table 8: Head of example struct-file generated for FCC Fe

FCC Fe					
F LATTICE, NONEQUIV. ATOMS		1	225	Fm-3m	
MODE OF CALC=RELA unit=bohr					
8.145000	8.145000	8.145000	90.00	90.00	90.00
ATOM 1:	X=0.0000	Y=0.0000	Z=0.0000		
	MULT= 1	ISPLIT= 2			
Fe	NPT= 781	R0=.000050	RMT= 2.5000	Z: 26.000	
LOCAL ROT MATRIX:	1.00000	0.00000	0.00000		
	0.00000	1.00000	0.00000		
	0.00000	0.00000	1.00000		
48 NUMBER OF SYMMETRY OPERATIONS					
1	0	0	0.000		
0	-1	0	0.000		
0	0	-1	0.000		

# III.1.2 Initialize DFT calculations using init\_lapw

case.struct file contains all the information needed for the DFT calculations of the crystal structures. Run the following command,

## "init\_lapw"

The following shows all the subsequent questions and corresponding answer choices.

#### 1. The screen first shows:

next is setrmt.

Automatic determination of RMTs. Please specify the desired RMT reduction compared to almost touching spheres.

Typically, for a single calculation just hit enter, for force minimization use 1-5; for volume effects you may need even larger reductions.

### 2. Answers choices to a series of questions,

- (a) Use old or new scheme (o/N)
- (b) accept these radii; discard them; or rerun setRmt (a/d/r)
- (c) nn-bondlength factor (usually=2)
- (d) continue with sgroup or edit the case.struct file (c/e)
- (e) continue with symmetry (old case.struct) or use/edit case.struct\_sgroup

  (c/e)
- (f) continue with lstart or edit the case.struct\_st file (c/e/x)

- (g) Eventually specify switches for instgen\_lapw (or press ENTER): -up (default) -dn -nm (non-magnetic) -ask
- (h) SELECT XCPOT, 13:PBE-GGA (Perdew\_Burke-Ernzerhof 96) 5:LSDA 11:WC-GGA (Wu-Cohen 2006) 19:PBEsol-GGA (Perdew etal.2008)
- (i) SELECT ENERGY to separate core and valence states: -6.0 Ry (check how much core charge leaks out of MT-sphere)
- (j) continue with kgen or edit the case.inst file and rerun lstart (c/e)
- (k) number of k-points in whole cell, usually 200-500
- (l) continue with dstart or execute kgen again or exit (c/e/x)
- (m) do you want to perform a spinpolarized calculation (n/y)

# III.1.3 Run the self-consistency cycles (SCF) of DFT calculations

After *init\_lapw*, there are many new files generated in the *case* folder. The next step is to run self-consistency cycles (SCF) of DFT calculations. It is strongly suggested to submit the DFT calculations job via *submit\_dft.scr* script utilizing services provided by a parallel computing machine (e.g., *mw* server). An example of *submit\_dft.scr* file is shown below,

```
#!/bin/bash
#$ -N /test
#$-S /bin/bash
#$-cwd
#$-j y
#$-r no
#$-m abes
#$-M user@carnegiescience.edu
#$-pe mpi 8
#$-P GL
#$-1 vf=2G
#$-1 h_vmem=2G
ulimit -l unlimited
. /home/user/.bashrc
pwd
```

```
###echo "env mpirun –verbose -n 4" > mpi_prefix.dat
echo $jobdir
export HOME=/san2/user
###export TMPDIR=/san3/smandal/main_July_2012
export OMP_NUM_THREADS=2
set -x
pwd
echo $jobdir
export OMP_NUM_THREADS=2
env
cat $PE_HOSTFILE
let n='mkmachinefile.sh $PE HOSTFILE'
cat .machines
echo n=$n
###export MY_NSLOTS=$n
echo "env OMP_NUM_THREADS=1 mpirun -n 8 " > mpi_prefix.dat
echo "env OMP_NUM_THREADS=1 mpirun -n $n " > mpi_prefix.dat2
#which mpirun
/share/apps/intel13/composer_xe_2013.0.079/bin/compilervars.sh intel64
#export INTEL_LICENSE_FILE=27000@troy.tacc.utexas.edu
#echo ${INTEL_LICENSE_FILE}
#ls -1 /etc/redhat -release
$WIENROOT/run_lapw -p
```

The command to submit the DFT calculation job to mw server is as follows,

## "qsub submit\_dft.scr"

Another way to run SCF is to use the command "**run\_lapw**", but it is not recommended.

The self-consistency cycles (SCF) consist of the following parts:

LAPWO (POTENTIAL) generates potential from density

LAPW1 (BANDS) calculates valence bands (eigenvalues and eigenvectors)

LAPW2 (RHO) computes valence densities from eigenvectors

LCORE computes core states and densities

MIXER mixes input and output densities

After SCF of DFT calculations, good charge densities have been converged.

You can save your results by the command "save\_lapw".

# III.2 DMFT part

## III.2.1 Initialize DMFT calculations

Following init\_lapw and SCF of DFT, proceed to the command,

## "init\_dmft.py"

to invoke DMFT calculations in the current directory.

Answer choices thereafter are shown below,

- Specify correlated atoms (e.g. 1-4, 7, 8):
- Do you want to continue; or edit again? (c/e):
- For each atom, specify correlated orbital(s) (e.g. d, f):
- Do you want to continue; or edit again? (c/e):
- Specify qsplit for each correlated orbital (default = 0):
- Do you want to continue; or edit again? (c/e):
- Do you want to group any of these orbitals into cluster-DMFT problems? (y/n):
- Enter the correlated problems forming each unique correlated problem, separated by spaces (e.g. 1, 3 2, 4 5-8):
- Do you want to continue; or edit again? (c/e):
- Broken symmetry run? (y/n):

- Range (in eV) of hybridization taken into account in impurity problems; default -6.0, 6.0: -10, 10:
- Perform calculations on real; or imaginary axis? (r/i):
- Is this a spin-orbit run? (y/n):
- Generate blank sig.inp? (y/n):

## III.2.2 Prepare all files

## III.2.2.1 Prepare input files (case.indmfl, case.indmfl) and output files

The initialization of DMFT calculations by <code>init\_dmft.py</code> will generate two input files, <code>case.indmfi</code> and <code>case.indmfl</code>. These two files will connect the solid and impurity with DMFT equations.

Create a new folder that is in the parent directory,

## "mkdir case\_backup"

then move all the files from the *case* folder into the *case\_backup* folder by the command,

## "mv ./\* ../case\_backup/"

then type in the following command in the current directory (case/),

### "dmft\_copy.py <parent directory>/case\_backup/ -a"

-a: files for both DFT and DMFT will be copied.

This command makes a copy of all the output files of DFT calculation results and DMFT initialization results into the folder *case*. These files are needed for the following DMFT calculations. Examples of copied files are listed below,

struct-file, WIEN2k files (.in0, .in1, .in2, .inm, .inso, .inc), charge density file (.clmsum), input files (.indmfi, .indmfl) and other files (.klist, .kgen, .scf2).

## III.2.2.2 Prepare params.dat and sig.inp files

We need to prepare two more files needed for DMFT calculations in the folder, params.dat and sig.inp.

## • params.dat

Construct *params.dat* file. Below illustrates one example of the *params.dat* file.

```
solver = 'CTQMC'
finish=20
                        # how many charge self-consistent iterations
max_dmft_iterations=1 # how many DMFT iterations inside charge loop
max_lda_iterations=1
                        # how many DMFT iterations inside charge loop
UpdateAtom=0
                        # the impurity cix file needs to be recomputed?
DCs='fixn'
                        # Double counting scheme
mix_delta=1.0
wbroad=0.005
                        # Broadening of the hybridization function
kbroad=0.1
                        # Broadening of the hybridization function
ntail=300
recomputeEF=2
saver=1.0
# Impurity problem number 0
iparams0= {
"exe"
        : ["ctqmc", "# Name of the executable"],
        : [8.0, "# Coulomb repulsion (F0)"],
"U"
"beta": [38.68333333], "# Inverse temperature"],
        : [0.0, "# Spin-orbit"],
"cx"
        : [10000000 , "# Total number of Monte Carlo steps"],
"M"
```

"Ncout": [1000000, "# How often to print out info"],

"Naver" : [100000000, "# How often to print out debug info"],

"nf0" : [6.0, "# Double counting parameter"],

"nc" : [[4,5,6,7,8], "# Impurity occupancies"],

"nom" : [40, "# Number of Matsubara frequency points"],

"aom" : [5 , "# Number of frequency points'],

"sderiv" : [0.02, "# Maximum derivation mismatch accepted"],

"Ntau" : [1000, "# Number of imaginary time points"],

"SamlpeGtau" : [1000, "# How often to update G(tau)"],

"GlobalFlip" : [1000, "# How often to try a global flip"],

"tsample" : [10, "# How often to record measurements"],

"warmup" : [1000000, "# Warmup number of QMC steps"],

"CleanUpdate" : [100000, "# How often to make clean update"],

"minM" : [1e-10, "# The smallest atomic trace"],

"minD" : [1e-10, "# The smallest determinant"],

"Ncorrect" : [-1, "# Which baths should not be corrected"],

"PChangeOrder": [0.9, "# Ratio between trial steps"],

"ChooseRandom": [0.8, "# How often to choose kink"],

"CoulombF" : ["'Georges'", "# Full Coulomb repulsion"],

"OCA\_G" : [False , "# No OCA diagrams"],

}

Or you can download example *params.dat* files from Haule's W2K Database website,

http://hauleweb.rutgers.edu/database\_w2k/

Move it from your local server to mw work directory and use the command,

"scp <local\_directory> <mw\_work\_directory>/FCC\_Fe/"

params.dat file contains information about the program flow and impurity solver. Leave the params.dat file name as it is. In the params.dat file, you can change the following parameters,

- finish=

The number of charge self-consistent iterations in *params.dat* file, e.g., **finish=60** means there are 60 iterations in DFT+DMFT calculations.

- iparams0={"beta"}

"beta" is the inverse temperature. It is derived from the absolute temperature in Kelvin,  $\beta = \frac{1(eV)}{T(K)}$  in which 1eV = 11604K. For example, if absolute temperature T is 300 K, then  $\beta = \frac{11604K}{300K} = 38.68$ . "beta": 38.68.

- iparams0={"M"}

"M" is the Total number of Monte Carlo steps. Typical M is 5 million (5e6), i.e., "M": **5e6**. Total Monte Carlo measurements (N) is calculated by the equation,  $N = (Number\ of\ CPU) * M$ . (Number of CPU) could be changed in mpi value in the  $submit\_dmft.scr$  file.

## • sig.inp

sig.inp is a blank self-energy file, and it is generated by the command,

## "szero.py -e 35.7 -T 0.026 -n 3000"

Make sure that the T value here (0.026) is the same as the *beta* value in *params.dat* file. The meanings of the characters (e, T, n) are as follows,

**-** e

Double counting energy, calculated by the equation:

$$E_{DC}$$
= $U(n-\frac{1}{2})$ - $J/2(n-1)$ 

**-** T

Effective temperature in DMFT which should be consistent with *beta* in the *params.dat* file. For example, if we have *beta=38.68333*, then  $T = \frac{1}{beta} = \frac{1}{38.68333} = 0.026$ . Please notice that T here is the effective temperature in DMFT derived from *beta* which is different from absolute temperature.

**-** n

The number of Matsubara frequency points

# III.3 Run DFT + DMFT codes

# III.3.1 Submit the job and run DFT + DMFT iterations

Copy *submit\_dmft.scr* script file into the current directory (*case*). An example of *submit\_dmft.scr* file is shown below.

```
#! /bin/bash
#$ -N test
#$-S /bin/bash
#$-cwd
#$-j y
#$-r no
#$-m abes
#$-M user@carnegiescience.edu
#$-pe mpi 8
#$-P GL
#$-1 vf=2G
#$-1 h_vmem=2G
ulimit -l unlimited
. /home/user/.bashrc
pwd
###echo "env mpirun –verbose -n 4 " > mpi_prefix.dat
echo $jobdir
export HOME=/san2/user
```

```
###export TMPDIR=/san3/smandal/main_July_2012
export OMP_NUM_THREADS=2
set -x
pwd
echo $jobdir
export OMP_NUM_THREADS=2
env
cat $PE HOSTFILE
let n='mkmachinefile.sh $PE_HOSTFILE'
cat .machines
echo n=$n
###export MY_NSLOTS=$n
echo "env OMP_NUM_THREADS=1 mpirun -n 8 " > mpi_prefix.dat
echo "env OMP_NUM_THREADS=1 mpirun -n $n " > mpi_prefix.dat2
#which mpirun
/share/apps/intel13/composer_xe_2013.0.0.79/bin/compilervars.sh intel64
#export INTEL_LICENSE_FILE=27000@troy.tacc.utexas.edu
#echo ${INTEL_LICENSE_FILE}
#ls -l /etc/redhat-release
$WIEN_DMFT_ROOT/run_dmft.py > wnohup.dat 2>&1
The final step is to type in the command,
"qsub submit_dmft.scr"
```

Using remote powerful machine (mw) is very efficient when computing large

number of Monte Carlo cycles due to the large number of CPU cores it has. The command above is going to create a .dat file for mpi parallel execution, mpi\_prefix.dat.

# III.3.2 Monitor running of DFT + DMFT

During the run, we can monitor the information file and update the parameters, if necessary. The files we can monitor are listed below,

• info.iterate

It contains information about chemical potential, impurity levels, exchange energies and total fillings, etc.

• :log

It helps monitor the modules that are running.

• dmft\_info.out, case.dayfile

To monitor the DMFT calculations and convergence levels.

• imp.0/nohup\_imp.out, imp.0/Sig.out, imp.0/Gf.out

To monitor the impurity levels.

• dmft1\_info.out, case.outputdmf1.0

To monitor the dmft1 step.

 $\bullet \ dmft2\_info.out, \ case.outputdmf2.0$ 

To monitor the dmft2 step.

# III.3.3 Check convergence of DFT + DMFT cycles and plot the results

To check convergence of DFT + DMFT cycles, you need to plot several output files, for example, *info.iterate*, *sig.inp.\*.1*, *sig.inp* and *imp.0/Sig.outb*. Here we use the *Test Case 0: FCC Fe* as an example.

## • Plot info.iterate v.s. iterations

There are seven columns in the *info.iterate* file representing the following information respectively, (see Table 9)

Table 9: Columns of info.iterate file

mu	chemical potential
E <sub>imp</sub>	impurity level
E <sub>imp</sub> [-1]	impurity level
E <sub>dc</sub>	exchange energy
nf	total filling

Note that if you change the parameters in the *params.dat* file and resubmit the DMFT calculations, the *info.iterate* file will recount the number of DMFT loops finished.

Use gnuplot to plot the chemical potential, impurity level as a function of the number of DMFT loops.

- Plot chemical potential v.s. number of DMFT loops in info.iterate (see

Figure 7). In this graph, from iteration 0 to iteration 10, fluctuations of chemical potentials are noticeable. From iteration 10 to iteration 20, it starts flatting out. From iteration 20 to iteration 90, it becomes quite stable.

Figure 7: Chemical Potential v.s. number of DMFT loops in *info.iterate* 0

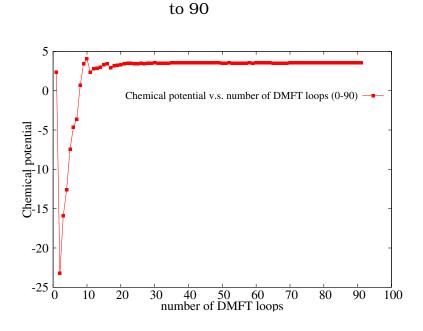


Figure 8 and Figure 9 show the zoomed-in significant improvement feature of convergence by increasing the Monte Carlo number "M" from 12e6 (iteration 20-60) to 120e6 (iteration 60-90). M number could be changed in *params.dat* file. Also, you can keep M number the same, but increase number of CPU cores by 10 times instead.

Figure 8: Chemical Potential v.s. number of DMFT loops in info.iterate 20

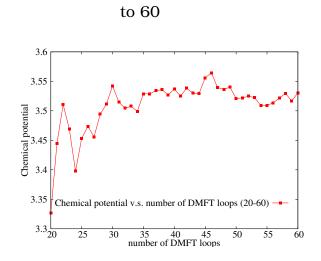
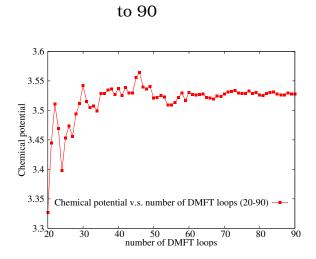
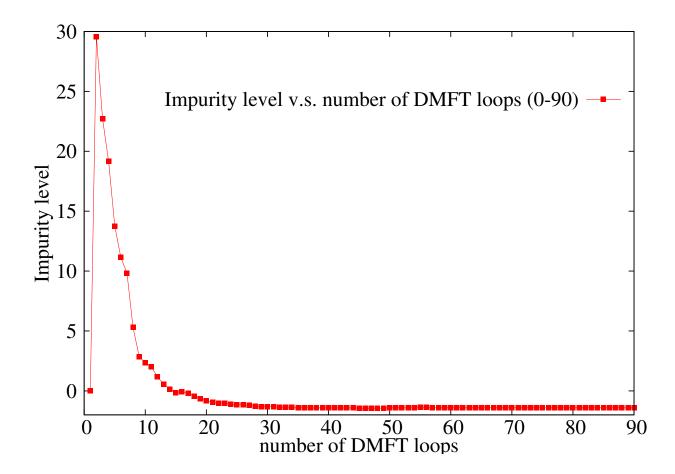


Figure 9: Chemical Potential v.s. number of DMFT loops in *info.iterate* 20



Plot impurity level v.s. number of DMFT loops in info.iterate (see Figure
 10)

Figure 10: Impurity level v.s. number of DMFT loops in info.iterate 0 to 90



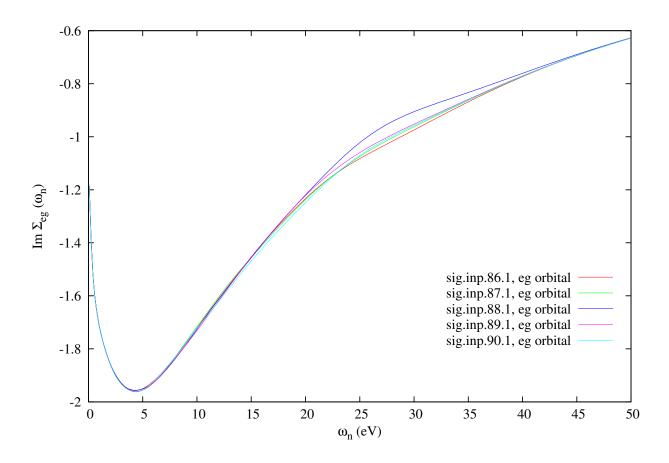
## • Plot self-energies in sig.inp.\*.1

We can check the convergence of DFT + DMFT iterations from self-energy files. Suppose we have finished 90 iterations, then we plot the last 5 self-energy files, sig.inp.86.1, sig.inp.87.1, sig.inp.88.1, sig.inp.89.1 sig.inp.90.1.

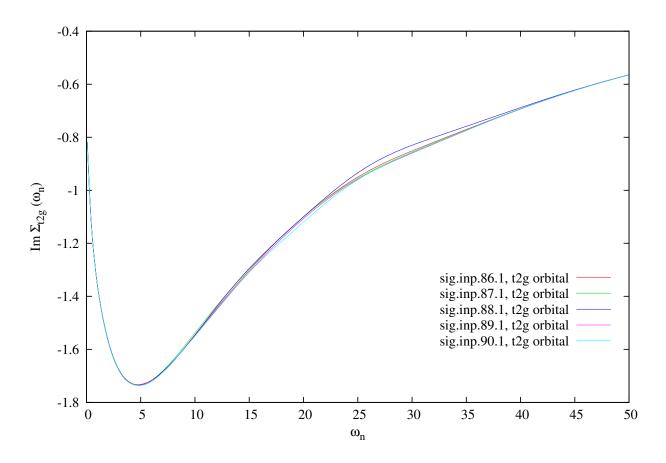
The self-energies of  $e_g$  orbitals in sig.inp.\*.1 files are shown in Figure 11.

The self-energies of  $t_{2g}$  orbitals in sig.inp.\*.1 files are shown in Figure 12.

Figure 11: Self-energy v.s. number of DMFT loops in sig.inp.\*.1 for  $e_g$  orbitals







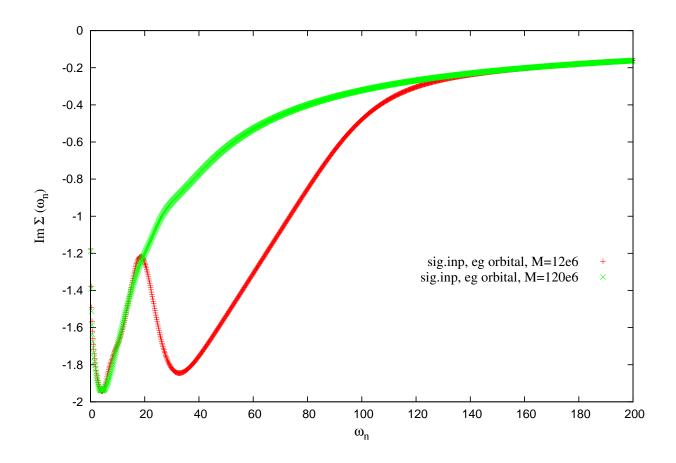
## • Plot self-energies in sig.inp and Sig.outb

Alternatively, you can check the quality of self-energy convergence by plotting the self-energy results in the following files, *sig.inp* and *imp.0/Sig.outb*. As can be seen, unconditioned self-energy pattern in *Sig.outb* is quite scattered. There are two solutions to solve this problem, 1. Increase number of Monte Carlo cycle measurements by simply changing "M" value in the *params.dat* file. 2. Increase number of CPU cores by modifying *mpi* value in DMFT submit script.

Plot conditioned self-energy in sig.inp before and after augmenting Monte
 Carlo numbers

Here illustrates conditioned self-energies before we increase the total Monte Carlo measurements (red line) and after the increase (green line) in *sig.inp* (see Figure 13)

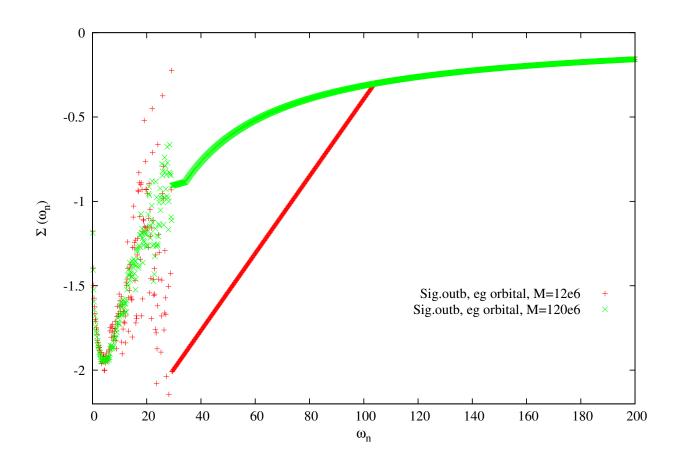
Figure 13: Conditioned self-energy v.s. number of DMFT loops in sig.inp before and after augmenting Monte Carlo measurements for  $e_q$  orbitals



Plot unconditioned self-energy in imp.0/Sig.outb before and after augmenting Monte Carlo numbers

Here shows unconditioned self-energies before we increase the total Monte Carlo measurements (red line) and after the increase (green line) in *Sig.outb* (see Figure 14). It is obvious that the quality of unconditioned self-energy has been improved tremendously.

Figure 14: Unconditioned self-energy v.s. number of DMFT loops in Sig.outb before and after augmenting Monte Carlo measurements for  $e_{\rm g}$  orbitals



## - Conditioning of self-energy in Sig.out

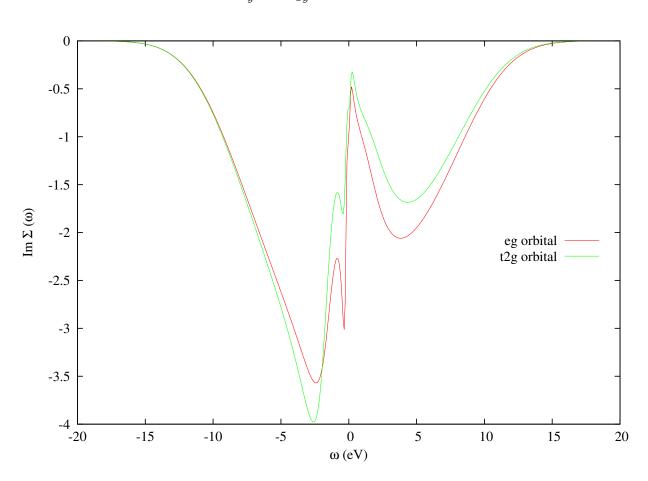
In DFT + DMFT, only the first "nom" Matsubara frequency points are directly from Quantum Monte Carlo (QMC) outputs using the Dysons' calculated equations.

$$\Sigma(i\omega n) = G^{o-1}(i\omega n) - G^{-1}(i\omega n)$$

Green's function has a  $\frac{1}{i\omega n}$  asymptotic behavior and at the high frequency/energy region,  $G(i\omega n)$  and  $G^o(i\omega n)$  will be close to zero value. Due to the systematic error in QMC measurements,  $\Sigma(i\omega n)$  at high frequency will have a very large scattering, as can be seen in imp.0/Sig.outb at frequencies near  $\omega_n=65$ . (see Figure 15).

Since we know the high frequency asymptotic behavior of self-energy, then the high frequency tail of self-energy at number of  $\omega_n$  > "nom" is given by the high frequency asymptotic functional; and the self-energy points from [non-nom, nom] is used to fix the parameters of asymptotic functional.

Figure 15: Imaginary part of self-energy v.s. real frequency in Sig.out for  $e_{\tt g} and \ t_{\tt 2g} \ orbitals$ 



# Part IV

# **Test cases**

## IV.1 FCC Fe at 1500 K 0 GPa

First, we want to test the DFT + DMFT calculations on a simple test case, FCC Fe at 1500 K 0 GPa, which has 1 atom per primitive cell and paramagnetic.

## IV.1.1 Run DFT+DMFT codes

# IV.1.1.1 Prepare struct-files

- Gather all the required information
  - The lattice parameters, lengths a, b, c in Bohr or Ångstrom and angles  $\alpha$ ,  $\beta$ ,  $\gamma$ .
  - The space group according to the "International Tables for Crystallography",

```
http://it.iucr.org/
```

- The positions of all inequivalent atoms in fractions of the unit cell.

# • Manually set up the struct-files

Create a new .txt file by the command

## "vi FCC\_Fe"

in your new folder *FCC\_Fe*. Next, type in all the prepared lattice information, (see Table 10)

Table 10: Lattice parameters in FCC\_Fe text file

b						"aAng, bBohr"
0.0	0.0	0.0				"shift of origin"
8.1450	8.1450	8.1450	90	90	90	"a, b, c, angles $\alpha, \beta, \gamma$ "
Fm-3m						"space-group symbol"
Fe						"atom- name"
0.000000	0.000000	0.000000				"atomic position"

Exit editing and save the text file, then the *FCC\_Fe* text file has been made.

Next task is to create your struct-file, *FCC\_Fe.struct*, by the command

### "cif2struct FCC\_Fe"

in your current directory. You can further modify the title and the automatically calculated values in the established struct-file.

## IV.1.1.2 Initialize calculations using init\_lapw

FCC\_Fe.struct file contains all the information needed for the crystal structure calculations that WIEN2k uses. Run the following command,

## "init\_lapw"

The following shows all the subsequent questions and corresponding default answers.

1. The screen first shows:

next is setrmt.

Automatic determination of RMTs. Please specify the desired RMT reduction compared to almost touching spheres.

Typically, for a single calculation just hit enter, for force minimization use 1-5; for volume effects you may need even larger reductions.

Press "Enter"

2. You will choose answers to a series of questions, typically you will enter the default setting values that WIEN2k uses as follows,

which stands for the following meanings respectively:

- o: use old scheme;
- a: accept these radii;
- 2: nn-bondlength factor;

*c*: continue with sgroup;

*c*: continue with symmetry;

c: continue with lstart;

-up: switches for instgen\_lapw -up(default);

13: SELECT XCPOT, 13:PBE-GGA (Perdew\_Burke-Ernzerhof 96);

-6: SELECT ENERGY to separate core and valence states: -6.0 Ry (check how much core charge leaks out of MT-sphere);

c: continue with kgen;

200: number of k-points in whole cell, usually 200-500;

c: continue with dstart;

n: not perform a spin polarized calculation.

## IV.1.1.3 Run the self-consistency cycles (SCF) of DFT calculations

After *init\_lapw*, there are many new files generated in the *FCC\_Fe* folder. The next step is to run self-consistency cycles (SCF) of DFT calculations. It is strongly suggested to submit the DFT calculations job via the *submit\_dft.scr* script utilizing services provided by a parallel computing machine (e.g., *mw* server). An example of *submit\_dft.scr* is shown in the Part III. The command to submit the DMFT calculation job to *mw* server is as follows,

### "qsub submit\_dft.scr"

Another way to run SCF is to use the command "**run\_lapw**", but it is not recommended.

The self-consistency cycles (SCF) consist of the following parts:

LAPWO (POTENTIAL) generates potential from density

LAPW1 (BANDS) calculates valence bands (eigenvalues and eigenvectors)

LAPW2 (RHO) computes valence densities from eigenvectors

LCORE computes core states and densities

MIXER mixes input and output densities

After SCF of DFT calculations, good charge densities have been converged. You can save your results by the command "save\_lapw".

### IV.1.1.4 Initialize DMFT calculations

Following init_lapw and SCF of DFT, proceed to the commar

to invoke DMFT calculations in the current directory.

Suggestions on the choices thereafter are shown below,

- Specify correlated atoms (e.g. 1-4, 7, 8): 1
- Type "**c**"
- For each atom, specify correlated orbital(s) (e.g. d, f): d
- Type "**c**"
- Specify qsplit for each correlated orbital (default = 0): 7 (cubic symmetry in real harmonics)
- Type "**c**"
- Do you want to group any of these orbitals into cluster-DMFT problems? (y/n): **n**
- Enter the correlated problems forming each unique correlated problem, separated by spaces (e.g. 1, 3 2, 4 5-8) **1**
- Type "**c**"
- Broken symmetry run? (y/n): **n**

- Range (in eV) of hybridization taken into account in impurity problems; default -6.0, 6.0: -10, 10: **-10, 10**
- Perform calculations on real; or imaginary axis? (r/i): i
- Is this a spin-orbit run? (y/n): **n**
- Generate blank sig.inp? (y/n): **y**

### IV.1.1.5 Prepare all files

• Prepare input files (FCC\_Fe.indmfl, FCC\_Fe.indmfi) and output files

The initialization of DMFT calculations by *init\_dmft.py* will generate two input files, *FCC\_Fe.indmfi* and *FCC\_Fe.indmfl*. These two files will connect the solid and impurity with DMFT equations.

Create a new folder that is in the parent directory,

## "mkdir FCC\_Fe\_backup"

then move all the files from *FCC\_Fe* folder into the *FCC\_Fe\_backup* folder by the command.

### "mv ./\* ../FCC\_Fe\_backup/"

then type in the following command in the current directory ( $FCC\_Fe/$ ),

### "dmft\_copy.py <parent directory>/FCC\_Fe\_backup/ -a"

-a: files for both DFT and DMFT will be copied.

This command makes a copy of all the output files of DFT calculation results and DMFT initialization results into the folder *FCC\_Fe*. These files are needed for the following DMFT calculations. Examples of copied files are listed below, struct-file, WIEN2k files (.in0, .in1, .in2, .inm, .inso, .inc), charge density file (.clmsum), input files (.indmfi, .indmfl) and other files (.klist, .kgen, .scf2)

• Prepare params.dat and sig.inp files

We need to prepare two more files needed for DMFT calculations in the *FCC\_Fe* folder, *params.dat* and *sig.inp*.

## - params.dat

Manually set up the *params.dat* file or download the *params.dat* file from Haule's W2K Database website,

http://hauleweb.rutgers.edu/database\_w2k/

The *params.dat* file contains information about the program flow and impurity solver. Leave the *params.dat* file name as it is. In the *params.dat* file, you can change the following parameters,

#### \* finish=

The number of charge self-consistent iterations in *params.dat* file, e.g., **finish=60** means there are 60 iterations in DFT+DMFT calculations.

# \* iparams0={"beta"}

"beta" is the inverse temperature. It is derived from the absolute temperature in Kelvin,  $\beta = \frac{1(eV)}{T(K)}$  in which 1eV = 11604K. For example, if absolute temperature T is 300 K, then  $\beta = \frac{11604K}{300K} = 38.68$ . "beta": 38.68.

# \* iparams0={"M"}

"M" is the Total number of Monte Carlo steps. Typical M is 5 million (5e6), i.e., "M": **5e6**. Total Monte Carlo measurements (N) is calculated by the equation,  $N = (Number\ of\ CPU) * M$ . (Number\ of\ CPU) could be changed in mpi value in the  $submit\_dmft.scr$  file.

- sig.inp

sig.inp is a blank self-energy file, it is generated by the command

### "szero.py -e 35.7 -T 0.026 -n 3000"

Make sure that the T value here (0.026) is the same as the *beta* value in *params.dat* file. The meanings of the characters (e, T, n) are as follows,

\* e

Double counting energy, calculated by the equation

$$E_{DC}=U(n-\frac{1}{2})-J/2(n-1)$$

in which U = 6 eV; J = 0.8 eV

\* T

Effective temperature in DMFT which should be consistent with *beta* in the *params.dat* file. For example, if we have *beta=38.68333*, then  $T = \frac{1}{beta} = \frac{1}{38.68333} = 0.026$ . Please notice that T here is the effective temperature in DMFT derived from *beta* which is different from the absolute temperature.

\* n

The number of Matsubara frequency points

### IV.1.1.6 Submit the job and run DFT + DMFT iterations

Copy *submit\_dmft.scr* script file into the current directory (*FCC\_Fe*). An example of *submit\_dmft.scr* file is shown in Part III. The final step is to type in the command,

# "qsub submit\_dmft.scr"

Using the remote powerful machine (mw) is handy in terms of computing a large number of Monte Carlo cycles due to a large number of CPU cores it has. The command above is going to create a .dat file for mpi parallel execution, mpi\_prefix.dat.

## IV.1.1.7 Monitor running of DFT + DMFT

During the run, we can monitor the information file and update parameters, if necessary. The files we can monitor are listed below,

• info.iterate

It contains information about chemical potential, impurity levels, exchange energies and total fillings, etc.

• :log

It helps monitor the modules that are running.

• dmft\_info.out, FCC\_Fe.dayfile

To monitor the DMFT calculations and convergence levels.

• imp.0/nohup\_imp.out, imp.0/Sig.out, imp.0/Gf.out

To monitor the impurity levels.

• dmft1\_info.out, FCC\_Fe.outputdmf1.0

To monitor the dmft1 step.

• dmft2\_info.out, FCC\_Fe.outputdmf2.0

To monitor the dmft2 step.

# IV.1.2 Properties based on DMFT calculations

Once the SCF cycle has converged one can calculate various properties, such as Probabilities, Density of States (DOS), Partial Density of States (Partial DOS), spectral functions, optics (including conductivity) and Fermi surface.

Let's continue with our simplest test case, FCC Fe at 1500 K 0 GPa, and calculate properties based on it.

### IV.1.2.1 histogram.dat and Probability.dat

## histogram.dat

To check whether the parameter "Nmax" in the *params.dat* file is large enough, we should plot "imp.0/histogram.dat", which should be gaussian, and should look like figure 16.

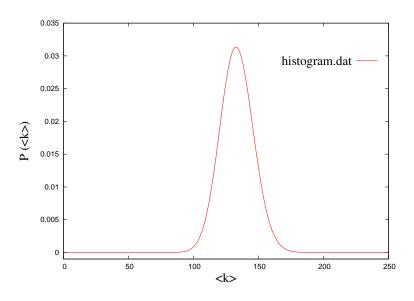


Figure 16: Plot histogram.dat file

This shows the distribution of the perturbation order. The perturbation

order around 200 has almost no probability, hence Nmax=400 (two kinks for each perturbation order) would be sufficient. We used substantially larger Nmax=600, so that we could reduce the temperature for factor of 3. Notice that larger Nmax only slightly slows down the execution of the code, and uses only a bit more memory, hence it is a good idea to use large Nmax.

## • imp.0/Probability.dat

We can also check what the probability for each atomic state is, i.e., probability that a Fe-d electron is in any of the atomic states. This information is written in "imp.0/Probability.dat". The first and the second column correspond to the index of each spin configuration, as defined in "actqmc.cix" (which enumerates all atomic states). The third column is the probability for a state. Here is the plot of probability for first 170 states, see figure 17,

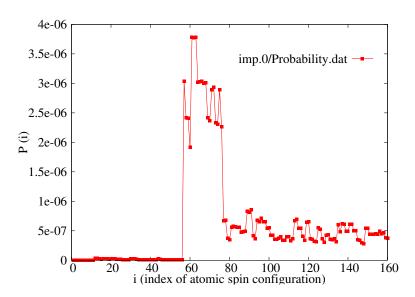
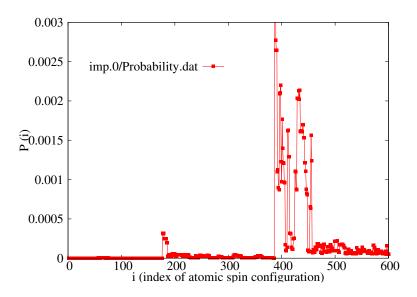


Figure 17: Plot imp.0/Probability.dat file

The first state corresponds to the empty 4f ion. The next 80 states (from

1...80) correspond to nominal occupancy N=1, and the values between 80 and 170 correspond to occupancy N=2. At N=1, there are two sets of probabilities, 6 take the value around 4e-6, and 8 take the value of 2e-6. The first and the second set corresponds to j=5/2 and j=7/2 multiplet, respectively. The next 90 states, which correspond to occupancy N=2, have probability around 5e-7. They can be grouped into multiplets, the lowest being J=4, followed by J=2 and J=5. Notice that the lowest multiplet satisfies Hunds rules (largest S=1, largest L=5, and J=L-S=4). Notice also that although FCC Fe is a very itinerant metal, the projection to the atomic states still satisfies atomic rules, such as Hunds rules. The cumulative probability for N=2 states is around 0.086. Compare this to N=1 probability of 0.836, and N=0 probability of 0.077. The next 430 states correspond to N=3 occupancy, and their histogram looks like figure 18.



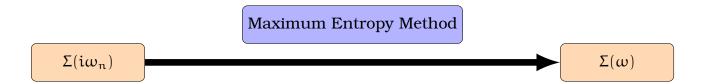


Typical probability of N=3 state is 1e-6, and cumulative probability is 0.0012. Clearly, the probability falls off very rapidly with particle number N, hence we can safely restrict occupancy in params.dat file to nc=[0, 1, 2, 3].

# IV.1.2.2 Density of States (DOS) and Partial Density of States (Partial DOS)

• Analytical continuation of self energies

We are going to do analytical continuation to calculate the self energy on the real axis after acquiring our results on the imaginary axis.



- Preparation: make several new directories under the parent directory
   (FCC\_Fe) before we do any calculations on DOS, DOS/FCC\_Fe, mem/Sig\_real
   and mem/Gf\_real
- Average the self-energies from the last few iterations to minimize the noise,
   saverage.py sig.inp.86.1 sig.inp.87.1 sig.inp.88.1 sig.inp.89.1
   sig.inp.90.1 sig.inpx

Here it averages the last five *sig.inp.\*.1* files and creates an output file *sig.inpx* in the current directory *FCC\_Fe*.

- 3. Copy the averaged self energy file sig.inpx into the new folder  $mem/Sig\_real$ .
- 4. Download and modify maxent\_params.dat file from Haule's website, http://hauleweb.rutgers.edu/downloads/.

Make sure 'Ntau' value in *maxent\_params.dat* file matches *beta* value in *params.dat* file. Copy modified *maxent\_params.dat* file into the same direc-

tory *mem/Sig\_real*. This file contains the parameters needed for analytical continuation process.

## 5. Run the maximum entropy method (mem).

Now there are two files in mem/Sig\_real folder, sig.inpx and maxent\_params.dat. Next execute the command,

# maxent\_run.py sig.inpx

to produce the self energy file *Sig.out* on the real axis. Results in *Sig.out* file are plotted in Figure 15, 19.

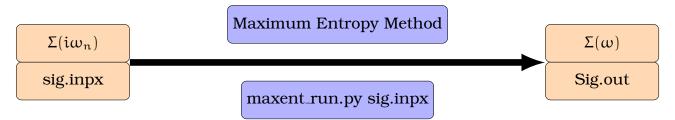
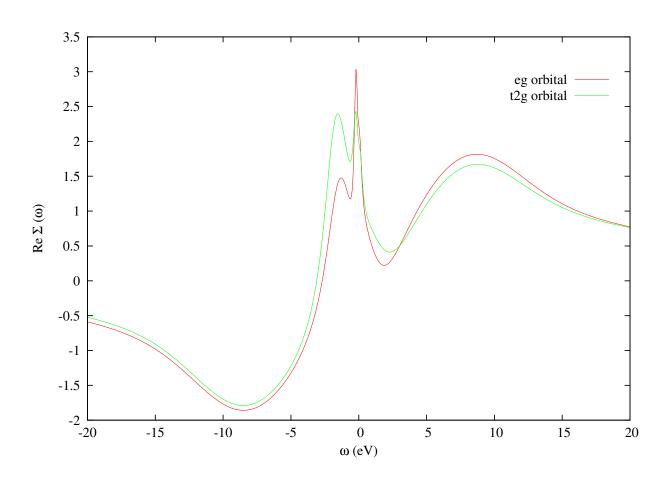


Figure 19: Real part of self-energy v.s. real frequency in Sig.out for  $\varepsilon_{\text{g}} \text{and } t_{2\text{g}}$  orbitals



### • Plot Total DOS

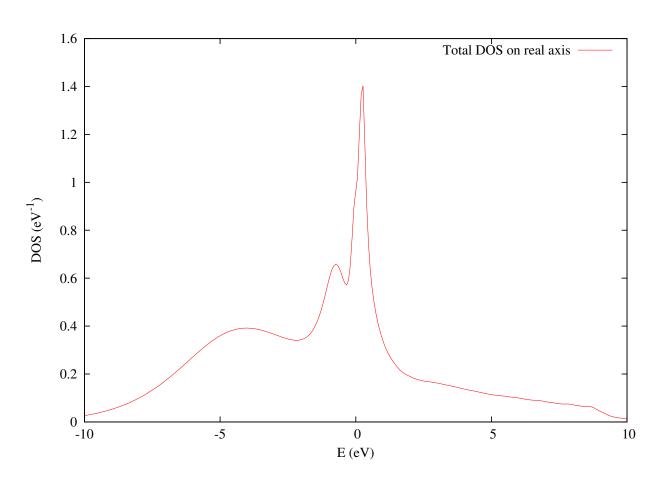
To plot Total Density of States (DOS), we need to run one more dmft1 calculation to obtain Green's function and DOS on the real axis.

1. Now we are going to work in the directory /FCC\_Fe/DOS/FCC\_Fe/, first, copy all the DMFT output files,

dmft\_copy.py ../../ -a

- Copy the generated Sig.out file to sig.inp in current directory (/DOS/FCC\_Fe/)
   cp ../../mem/Sig\_real/Sig.out sig.inp
- 3. Modify FCC\_Fe.indmfl file by changing 'Matsubara' value on the second line from imaginary axis "1" to real axis "0".
- 4. Run x kgen and specify number of k-points in whole cell, 8000
- 5. Run dmft1 calculations once.
  - x lapw0
  - x lapw1
  - x\_dmft.py dmft1
- 6. Plot the Total Density of States (DOS) which is stored in the *FCC\_Fe.cdos* file. Results of Total DOS are shown in Figure 20.

Figure 20: Total Density of States on the real axis for FCC Fe



### • Plot Partial DOS

Now we move on to calculate and plot the partial (d-orbital) Density of States (DOS).

- We are going to work in the new directory FCC\_Fe/mem/Gf\_real
- Copy maxent\_params.dat and Gf.out files into Gf\_real directory from directories, /FCC\_Fe/mem/Sig\_real/maxent\_params.dat and /FCC\_Fe/imp.0/Gf.out respectively.
- Run **maxent\_S.py Gf.out** in the current *mem/Gf\_real* directory.
- Plot 'Sig.out' file generated. Note that partial DOS is given by dividing the imaginary part of the Green's function by  $-\pi$ .

$$A(\omega) = -1/\pi * (ImG(\omega))$$

So the commands should resemble the following,

plot 'Sig.out' u 1:(-\$3/3.14) w l ":DOS of 
$$e_g$$
 d orbital" plot 'Sig.out' u 1:(-\$5/3.14) w l ":DOS of  $t_{2g}$  d orbital"

 The results of all partial d orbital DOS are shown in Figure 21. The comparison between the partial DOS and total DOS is shown in Figure 22.

Figure 21: Partial Density of States ( $e_{g}$  and  $t_{2g}$ ) on the real axis for FCC Fe

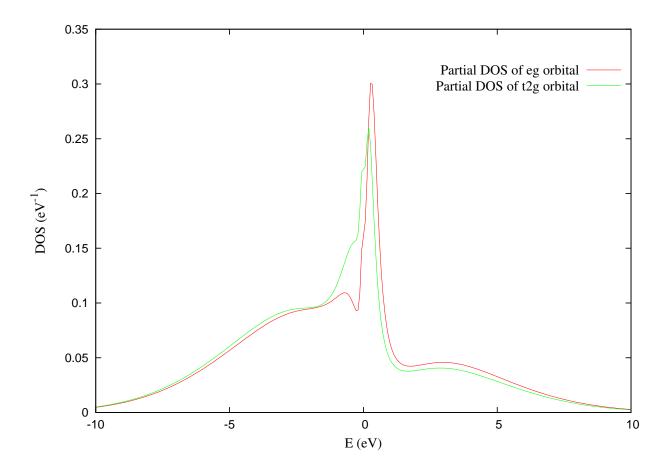
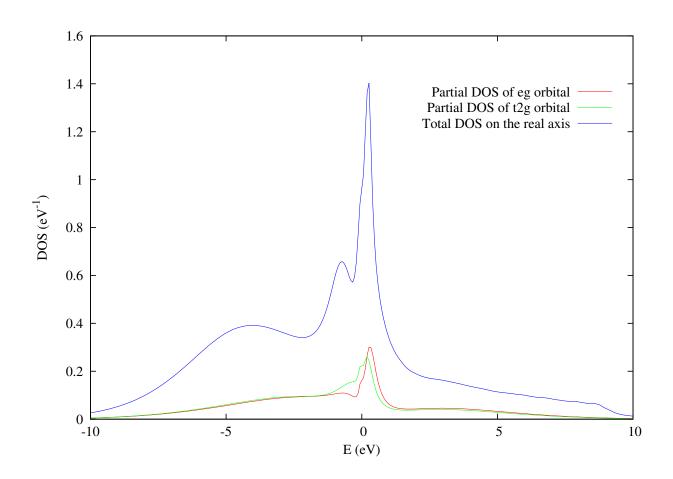


Figure 22: Partial Density of States and Total Density of States on the real axis for FCC Fe



### IV.1.2.3 Spectral functions

1. Preparation: Make a new folder containing all the results of calculations on Spectral functions (momentum resolved spectral function, equivalent to band structures in DFT).

### mkdir -p /FCC\_Fe/spectra/FCC\_Fe

2. Copy all the required files from DMFT calculations to the current directory.

# dmft\_copy.py ../../ -a

Here make sure you have *EF.dat* file, if you don't, find the Fermi Energy and store the Fermi Energy to *EF.dat* file in eV.

3. Replace the imaginary self-energy by self-energy in real frequency.

### cp /FCC\_Fe/mem/Sig\_real/Sig.out sig.inp

4. Edit FCC\_Fe.indmfl file.

On the second line of FCC\_Fe.indmfl file, you will see,

1 0.025 0.025 600 -3.0000000 1.0000000 # matsubara, broadening-corr, broadening-noncorr, nomega, omega\_min, omega\_max (in eV)

Change the "*matsubara*" value from **1** to **0** in order to switch from imaginary axis to real axis. Change the frequency range: "*omega\_min*" from **-3** to **-5**; "*omega\_max*" from **1** to **5**.

5. Create *FCC\_Fe.klist\_band* file to choose the path in momentum space (first brillouin zone).

Figure 23 illustrates the first Brillouin zone of a face centered cubic lattice, e.g. FCC Fe.

There are two ways to create this file. One is to write it by hand. The other method is to make a copy from WIEN2k prepared templates. Because FCC iron is the current system, we can simply copy *fcc.klist* from WIEN2k templates.

### cp \$WIENROOT/SRC\_templates/fcc.klist FCC\_Fe.klist\_band

6. Run the following commands to execute DMFT calculations on the mesh in the current /spectra/FCC\_Fe/ directory.

x lapw0

x lapw1 -band

ssplit.py -i sig.inp

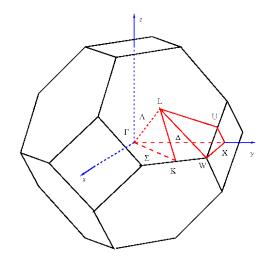
x\_dmft.py dmftp

7. Plot the band structures by,

## wakplot.py

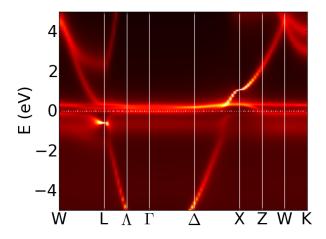
You can increase the intensity of brightness by reducing it from 0.2 (default) to any smaller number. Here shows how the plot looks like (see Figure 24),

Figure 23: First Brillouin Zone of FCC Fe lattice



Source: http://commons.wikimedia.org/wiki/File:Fcc\_brillouin.png

Figure 24: Spectral functions of FCC Fe



## IV.1.2.4 Optics including conductivity

1. Preparation: make a new folder in FCC\_Fe,

mkdir -p FCC\_Fe/optics/FCC\_Fe

2. Copy all the required files from DMFT calculations to the current directory,

dmft\_copy.py ../../ -a

3. Prepare FCC\_Fe.inop file. Refer to WIEN2k userguide for example of .inop file. It should contain the following information.

99999 1: NKMAX, NKFIRST

-5.0 5.0 : EMIN, EMAX, NBvalMAX

3 : number of choices (columns in \*symmat)

1 : Re xx

2 : Re yy

3 : Re zz

ON: ON/OFF writes MME to unit 4

4. Prepare *dmftopt.in* file. Make sure "# dwindow" value is large enough to get better results. Below shows the contents of this file.

0 # updn: [0—up—dn] – 0 for non-magnetic calculation

Fe # case

0.01 # gamma – broadening of all bands / we recommend to keep nonzero value

```
0.0 # gammac – broadening of the correlated bands (in addition to the self-
energy)
15 # ommax – maximum frequency for the optics calculation
1e-2 # delta – minimum separation of frequency for logarithmic mesh in
frequency
8 # Nd – number of points in each linear mesh, a subset of logarithmic mesh
T # Qsym: [F—T]. Do we need to symmetrize? (over all irreducible only or
over all.)
F # InterbandOnly [F—T] (F – all, T–interband)
20 # dwindow - Not all bands are used in computation of optics, but only
those from [-omeg-dwindow, omega+dwindow].
3 # Ndirection - How many optics type do you want to compute: xx, yy,
ZZ....
1.0 0.0 0.0 # alphaV(1,:)
0.0 0.0 0.0 # alphaV(2,:)
0.0 0.0 0.0 # alphaV(3,:)
0.0 0.0 0.0 # alphaV(1,:)
0.0 1.0 0.0 # alphaV(2,:)
0.0 0.0 0.0 # alphaV(3,:)
0.0 0.0 0.0 # alphaV(1,:)
```

```
0.0 0.0 0.0 # alphaV(2,:)
0.0 0.0 1.0 # alphaV(3,:)
```

5. Replace the imaginary self-energy by self-energy in real frequency.

cp /FCC\_Fe/mem/Sig\_real/Sig.out sig.inp

6. Edit FCC\_Fe.indmfl file.

On the second line of *FCC\_Fe.indmfl* file, Change the "*matsubara*" value from **1** to **0** in order to switch from imaginary axis to real axis.

- 7. Run **x kgen** and specify number of k-points in whole cell, **8000**
- 8. Run the following commands to execute DMFT calculations in the /optics/FCC\_Fe/ directory.

x lapw0

x lapw1

x optic

cp FCC\_Fe.mommat2 FCC\_Fe.mommat

ssplit.py -i sig.inp

x\_dmft.py dmftu

dmftopt

9. Plot the results stored in files, *optics.dat* and *optdos.dat*. See Figures 25, 26.

Figure 25: Optical conductivity of FCC Fe

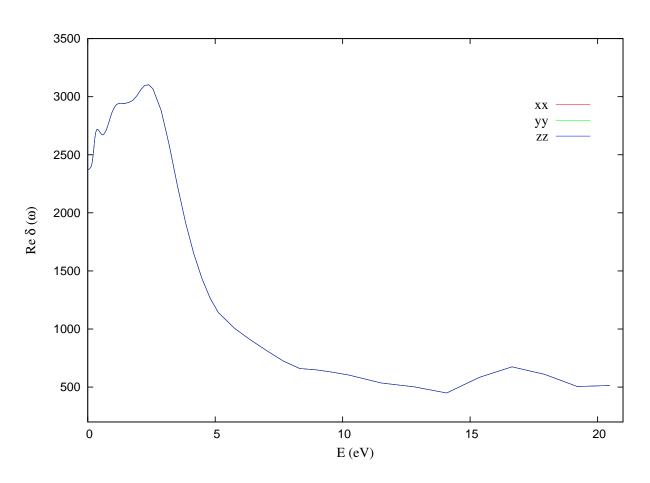
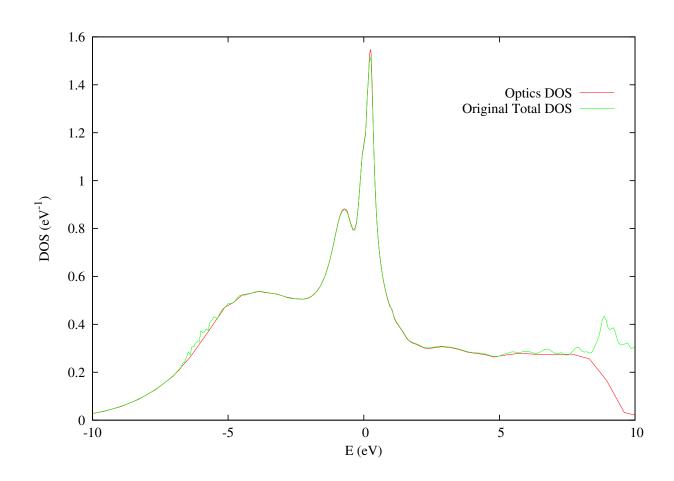


Figure 26: Density of States based on optics calculations and comparison with Total DOS for FCC Fe



# IV.1.2.5 Fermi Surface

# References

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