



Multiple View Geometry: Exercise Sheet 1

Prof. Dr. Daniel Cremers, Robert Maier, Rui Wang, TU Munich

<http://vision.in.tum.de/teaching/ss2016/mvg2016>

Exercise: April 28th, 2016

Part I: Theory

The following exercises have to be **solved at home**. You will present your answer during the tutorials.

1. Show for each of the following sets (1) whether they are linearly independent, (2) whether they span \mathbb{R}^3 and (3) whether they form a basis of \mathbb{R}^3 :

- $B_1 = \left\{ \begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix}, \begin{pmatrix} 0 \\ 1 \\ 1 \end{pmatrix}, \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix} \right\}$

- $B_2 = \left\{ \begin{pmatrix} 2 \\ 1 \\ 0 \end{pmatrix}, \begin{pmatrix} 1 \\ 1 \\ 0 \end{pmatrix} \right\}$

- $B_3 = \left\{ \begin{pmatrix} 2 \\ 1 \\ 0 \end{pmatrix}, \begin{pmatrix} 3 \\ 1 \\ 0 \end{pmatrix}, \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix}, \begin{pmatrix} 1 \\ 0 \\ 1 \end{pmatrix} \right\}$

2. Which of the following sets forms a group (with matrix-multiplication)? Prove or disprove!

- $G_1 := \{A \in \mathbb{R}^{n \times n} \mid \det(A) \neq 0 \wedge A^T = A\}$
- $G_2 := \{A \in \mathbb{R}^{n \times n} \mid \det(A) = -1\}$
- $G_3 := \{A \in \mathbb{R}^{n \times n} \mid \det(A) > 0\}$

3. Prove or disprove: There exist non-zero vectors $v_1, \dots, v_4 \in \mathbb{R}^3 \setminus \mathbf{0}$, which are pairwise orthogonal (i.e., $\forall i, j: \langle v_i, v_j \rangle = 0$).

Part II: Practical Exercises

1. Basic image processing

- (a) Download `ex1.zip`
- (b) Load the image `lena.png`.
- (c) Determine the size of the image and show the image.
- (d) Convert the image to gray scale and determine the maximum and the minimum value of the image.
- (e) Apply a gaussian smoothing filter (e.g. using the Matlab-functions `imfilter`, `fspecial`) and save the output image
- (f) Show 1) the original image, 2) the gray scale image and 3) the filtered image in one figure.
- (g) Compare the gray scale image and the filtered image for different values of the smoothing.

2. Basic operations

- (a) Let $A = \begin{pmatrix} 2 & 2 & 0 \\ 0 & 8 & 3 \end{pmatrix}$ and $b = \begin{pmatrix} 5 \\ 15 \end{pmatrix}$. Solve $Ax = b$ for x .

- (b) Define a matrix B equal to A .

- (c) Change the second element in the first row of A to 4.

- (d) Compute the following:

```
c = 0;
for i ∈ {-4, 0, 4}
    c = c + i * AT * b
end
print c
```

- (e) Compare a) $A \cdot * B$ and b) $A' \cdot * B$ and explain the difference.

- 3. Write a function `approxequal(x, y, ε)` comparing two vectors x and y if they are almost equal, i.e.: $\forall i : |x_i - y_i| \leq \epsilon$.

The output should be logical 1 or 0.

If the input consists of two matrices, your function should compare the columns of the matrices if they are almost equal. In this case, the output should be a vector with logical values 1 or 0.

- 4. Write a function `addprimes(s, e)` returning the sum of all prime numbers between s and e .

Use the Matlab-function `isprime`.