

Siamese Network: Architecture and Applications in Computer Vision

February 9, 2017

Outline

- Metric Learning
- Siamese Architecture
- Siamese Network: Applications in computer vision

Traditional Classification

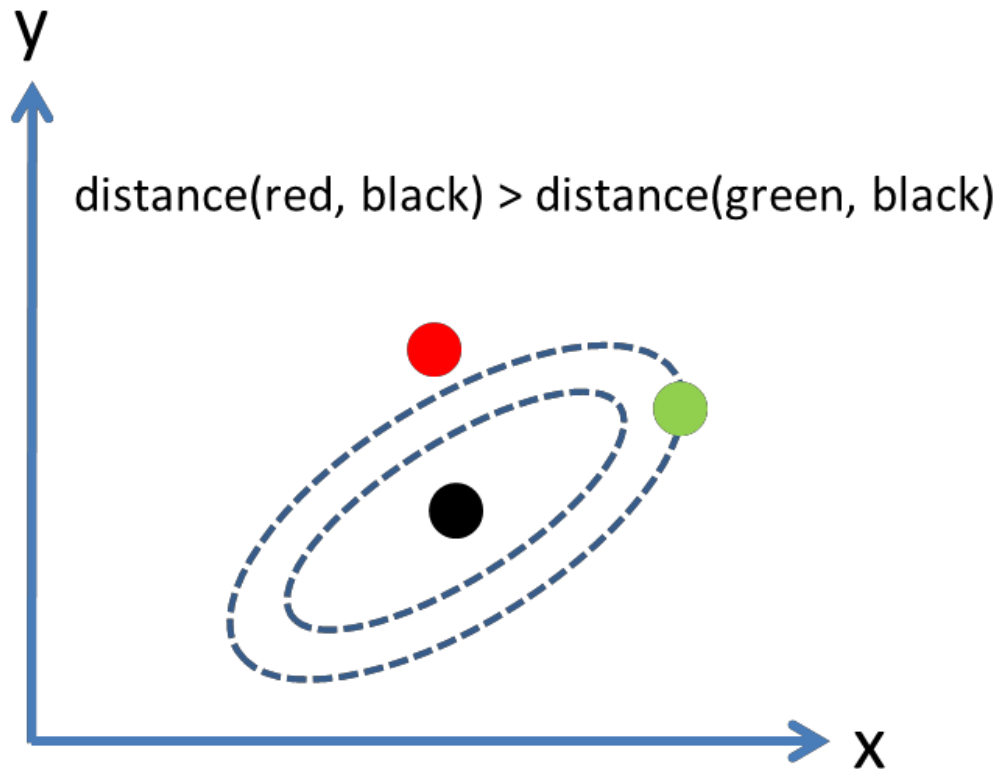
- All classes should be known
- Number of samples per category should be large
- Training samples should have a known class

Distance-based Methods

- Compute a similarity metric between the pattern to be classified or verified and a library of stored prototypes
- Can be used to compare or match new samples from previously-unseen categories (e.g. faces from people not seen during training)

Metric Learning

- Euclidean distance vs Mahalanobis distance



Metric Learning

Mahalanobis Distance Metric Learning

- *Euclidean distance*
- *Mahalanobis distance* $d(\vec{x}, \vec{y}) = \sqrt{(\vec{x} - \vec{y})^T S^{-1} (\vec{x} - \vec{y})}$.
- *Mahalanobis Distance Metric Learning*

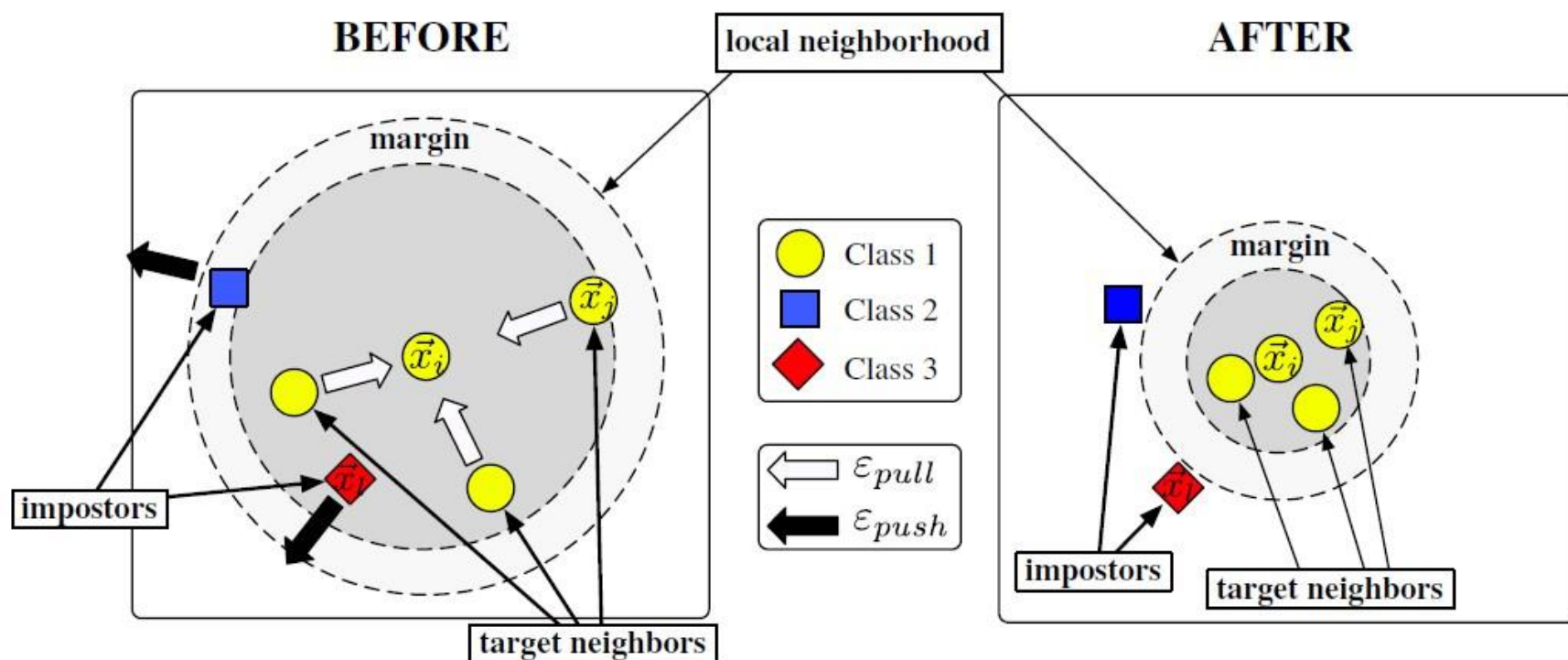
$$d(x, y) = d_A(x, y) = \|x - y\|_A = \sqrt{(x - y)^T A (x - y)}$$

$$\begin{aligned} \min_A \quad & \sum_{(x_i, x_j) \in \mathcal{S}} \|x_i - x_j\|_A^2 \\ \text{s.t.} \quad & \sum_{(x_i, x_j) \in \mathcal{D}} \|x_i - x_j\|_A \geq 1 \\ & A \succeq 0 \end{aligned}$$

Metric Learning

Large-Margin Nearest Neighbors(LMNN)

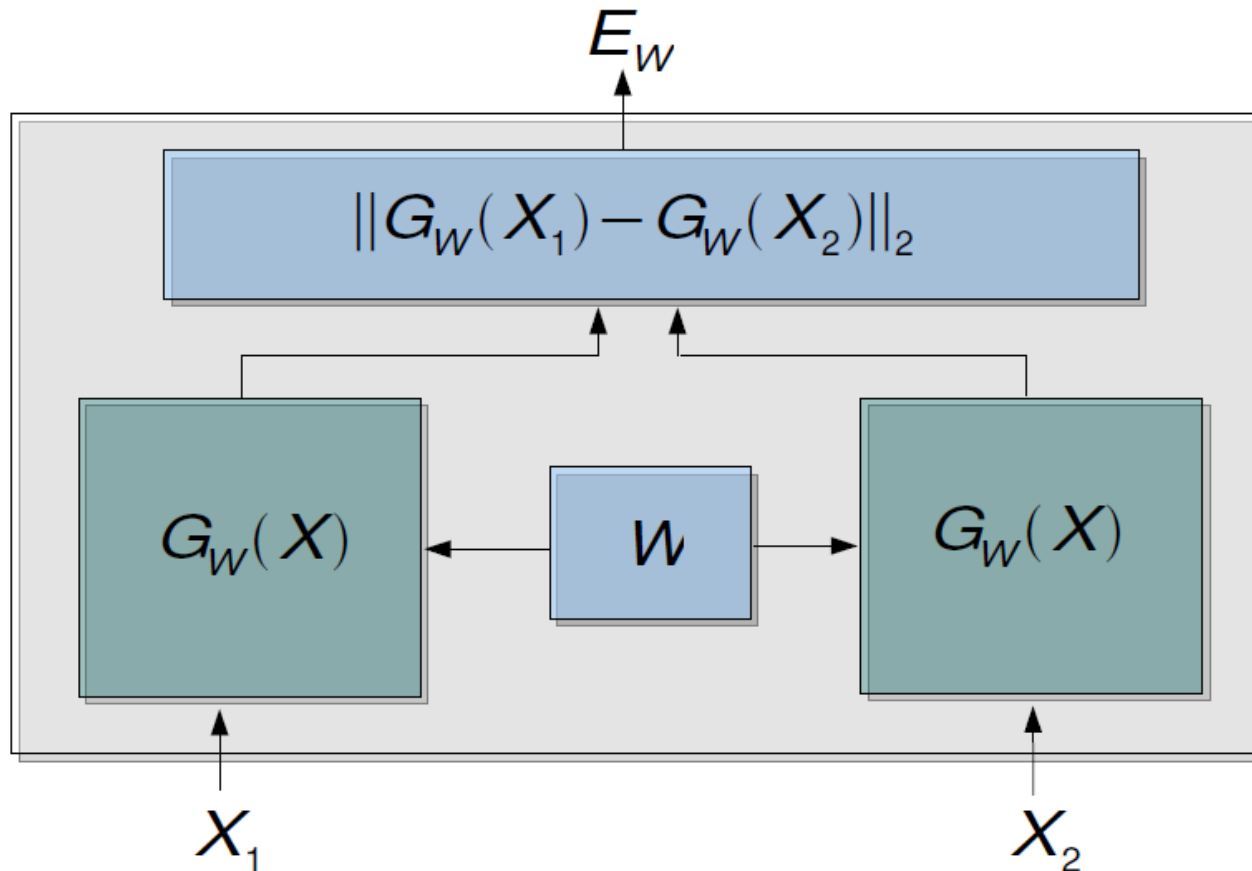
$$\min_{A \succeq 0} \sum_{(i,j) \in \mathcal{S}} d_A(\mathbf{x}_i, \mathbf{x}_j) + \lambda \sum_{(i,j,k) \in \mathcal{R}} [1 + d_A(\mathbf{x}_i, \mathbf{x}_j) - d_A(\mathbf{x}_i, \mathbf{x}_k)]_+$$



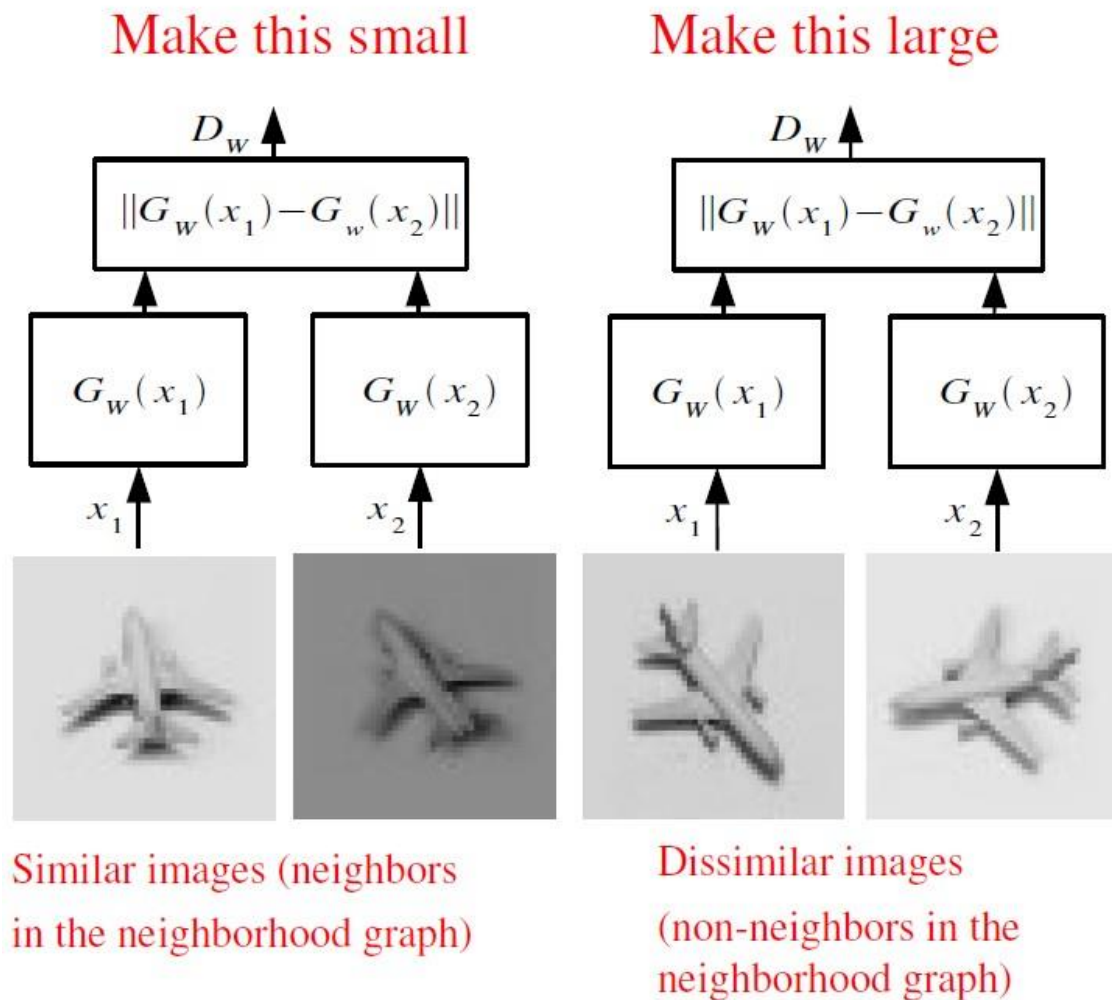
Siamese

- Someone or something from Thailand:
 - The Thai language, The Thai people
- Siamese, an informal term for conjoined or fused:
 - Siamese twins, conjoined twins
 - Siamesing (engineering), the practice, whose name is derived from siamese twins, of combining two devices (such as cylinder ports or cooling jackets) together into a closely coupled pair, so as to save space between them.

Siamese Architecture



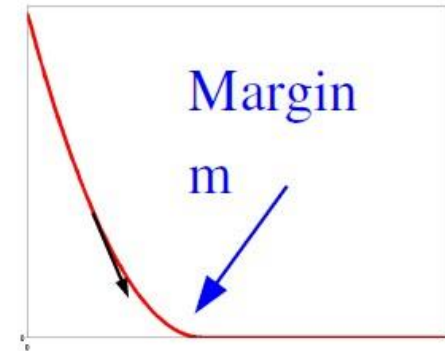
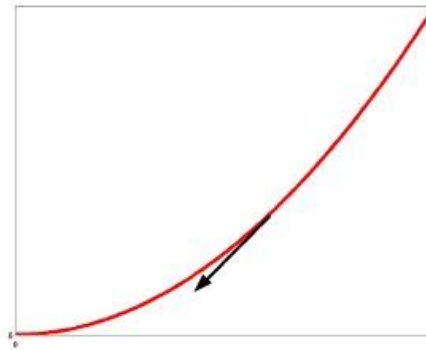
Siamese Architecture and loss function



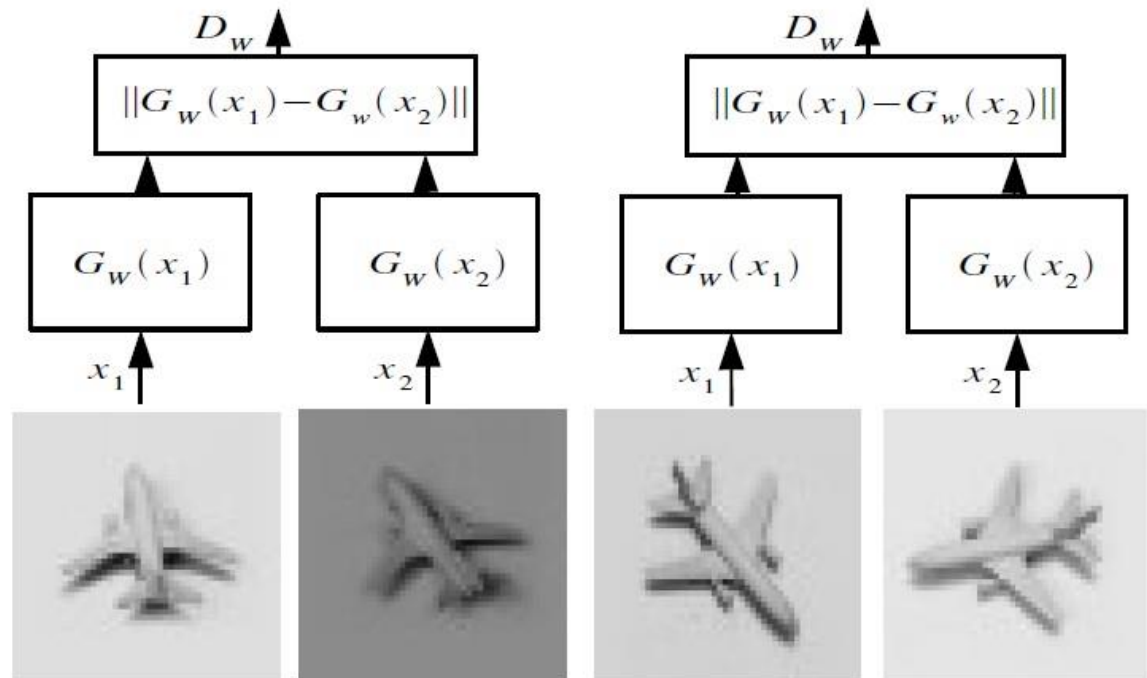
Loss function

$$L_{\text{similar}} = \frac{1}{2} D_w^2$$

$$L_{\text{dissimilar}} = \frac{1}{2} \{ \max(0, m - D_w) \}^2$$



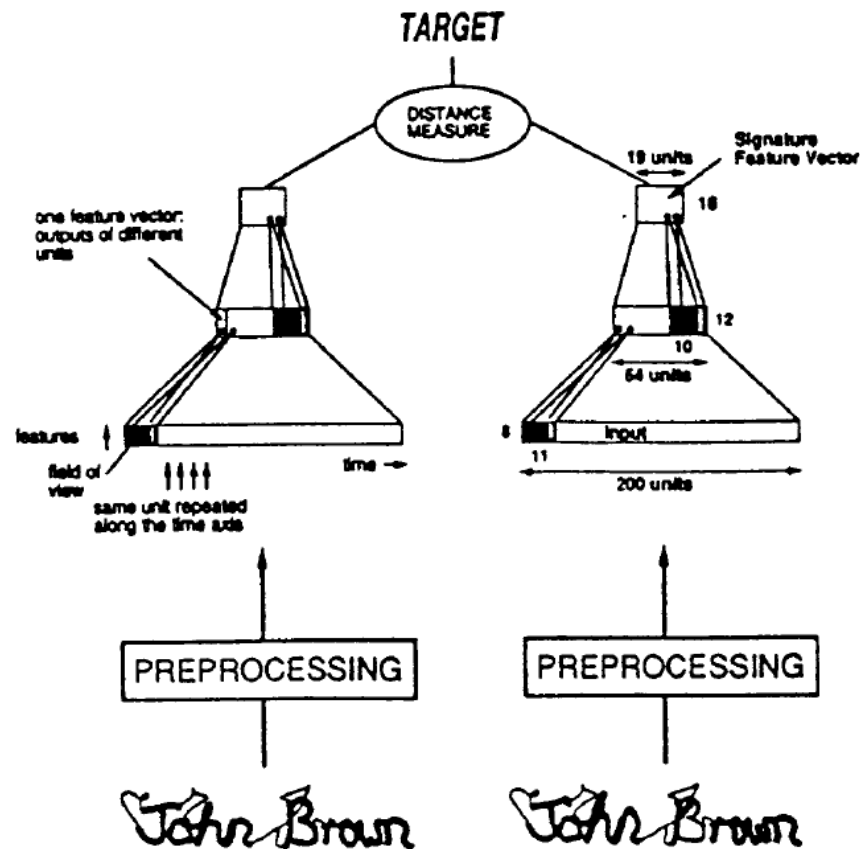
Hinge Loss



Siamese Network

Application in Signature Verification

- The input is 8(feature) x 200(time) units.
- The cosine distance was used, (1 for genuine pairs, -1 for forgery pairs)

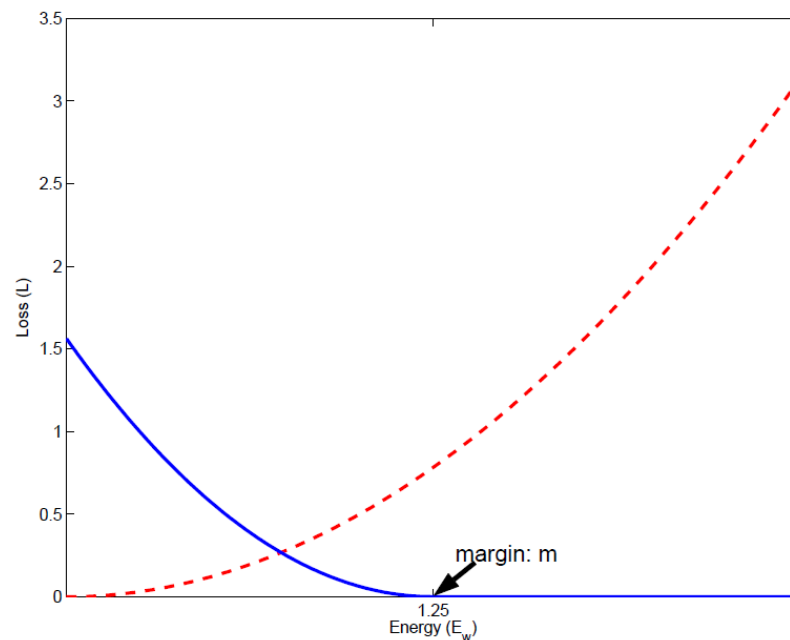
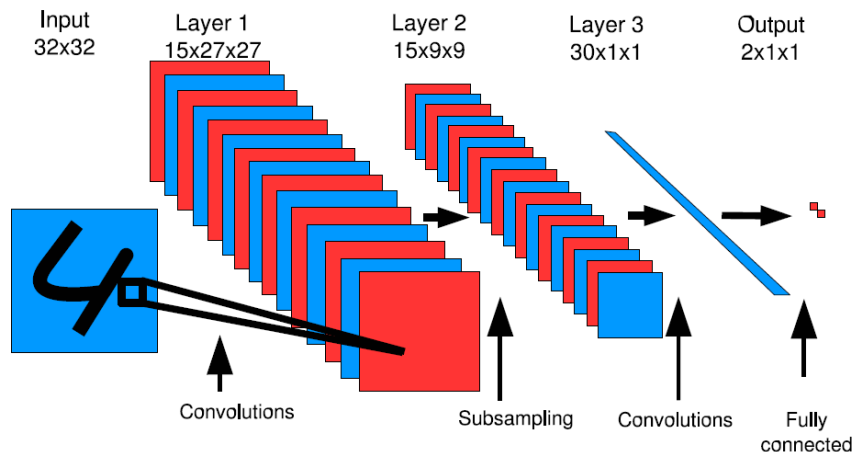


Siamese Network

Application in Dimensionality reduction

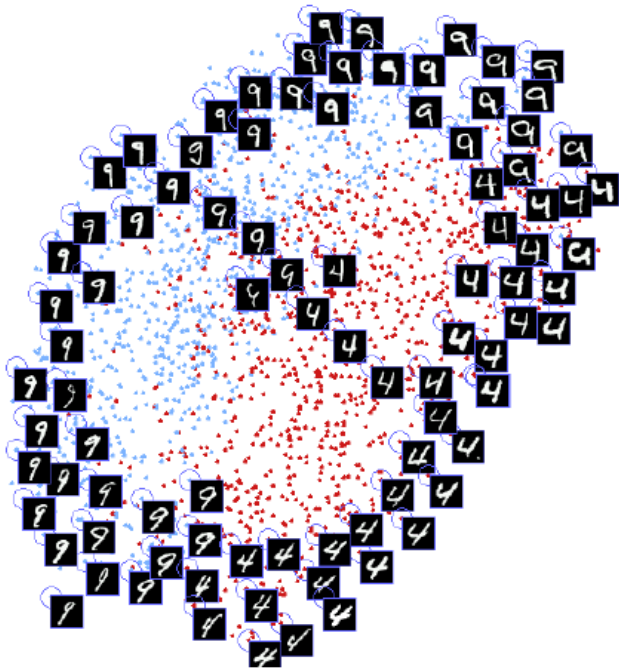
The exact loss function is

$$L(W, Y, \vec{X}_1, \vec{X}_2) = (1 - Y) \frac{1}{2} (D_W)^2 + (Y) \frac{1}{2} \{ \max(0, m - D_W) \}^2$$

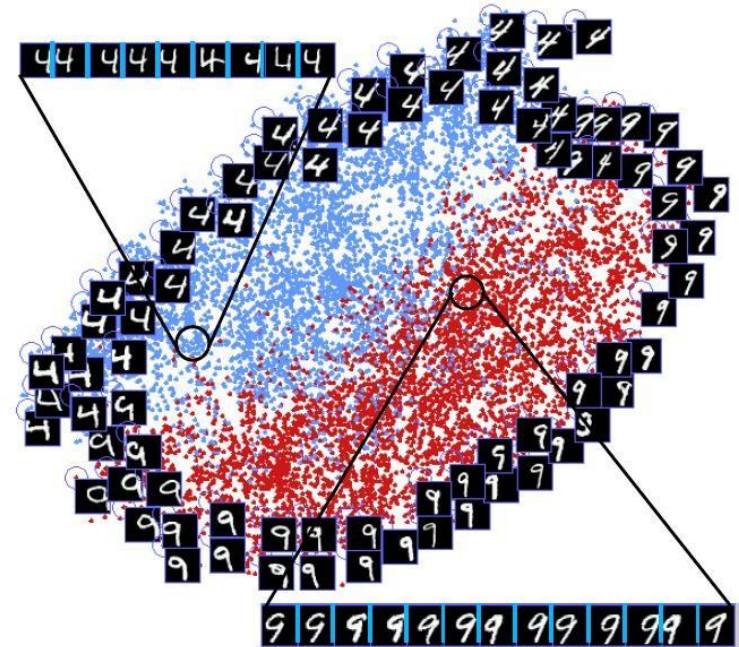


Siamese Network

Application in Dimensionality reduction

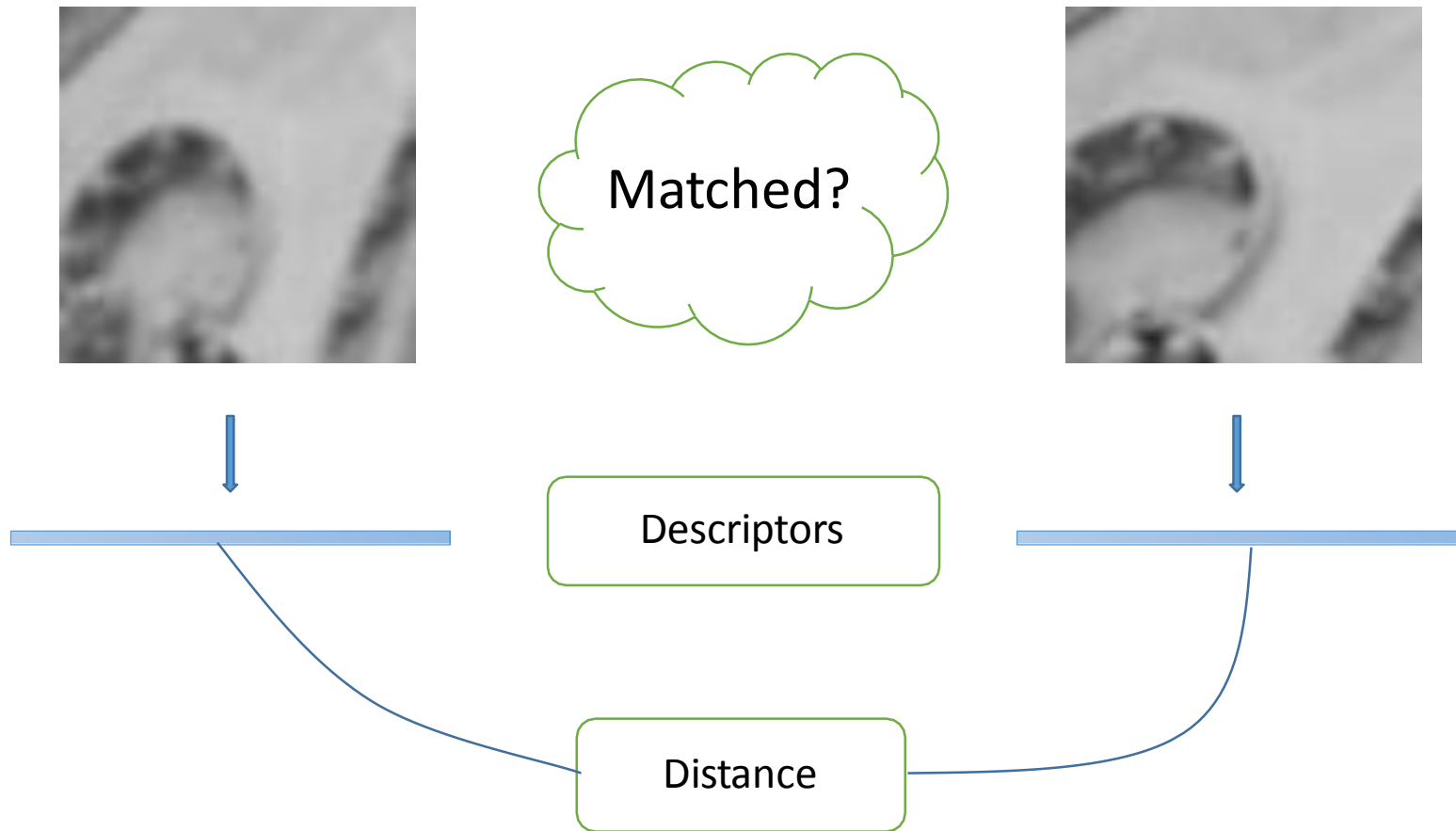


Learned Mapping of MNIST samples



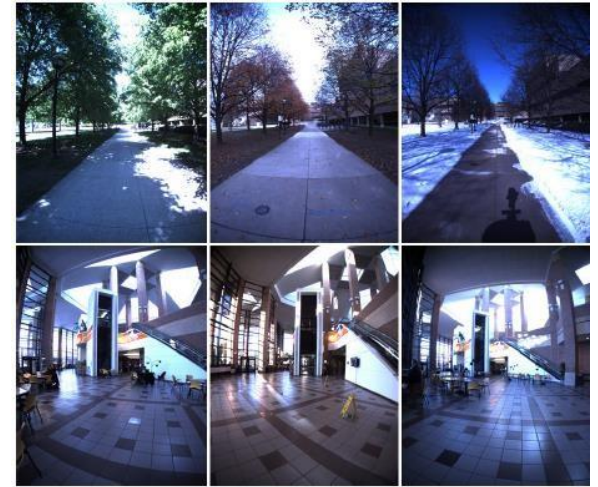
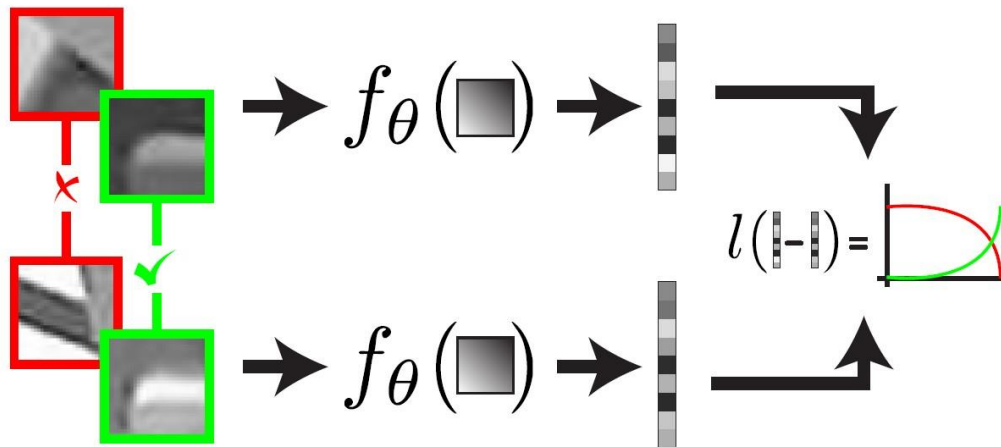
Learning a Shift Invariant Mapping of MNIST samples

Image Descriptors



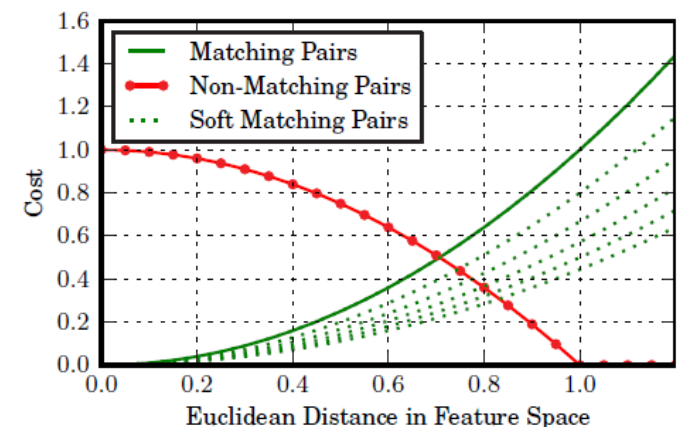
Siamese Network

Application in Learning Image Descriptors (I)



Using the contrastive cost function

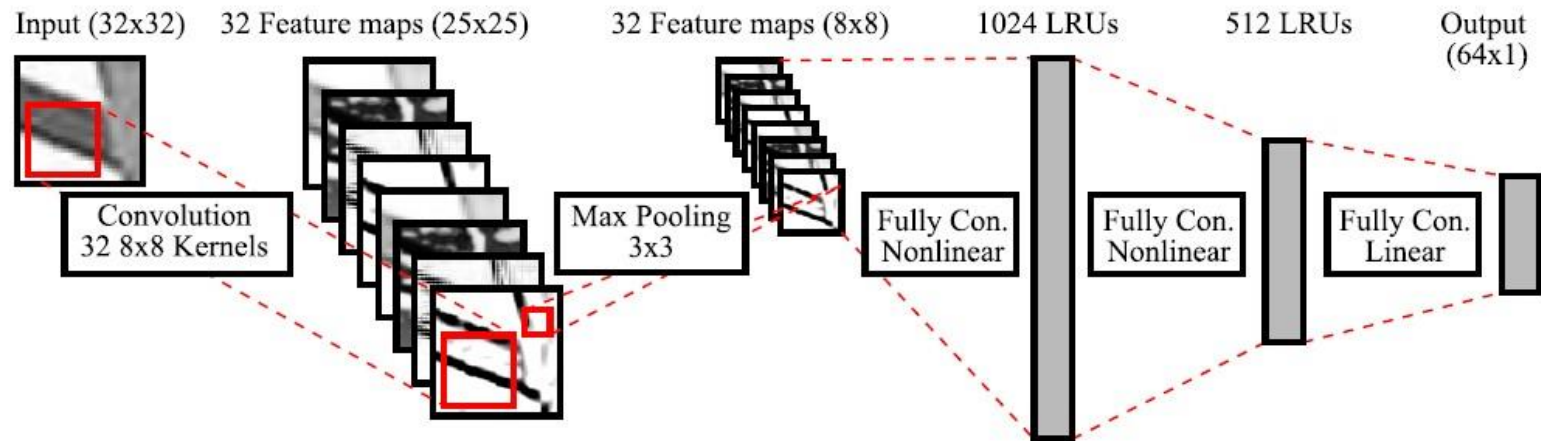
$$l_{\theta}(y_i, y_j) = \begin{cases} s_{ij} d_{ij}^2, & \text{if matching} \\ \max(1.0 - d_{ij}^2, 0), & \text{if non-matching} \end{cases}$$



Nicholas Carlevaris-Bianco and Ryan M. Eustice, *Learning visual feature descriptors for dynamic lighting conditions*. In *Proceedings of the IEEE/RSJ International Conference on Intelligent Robots and Systems*, 2014

Siamese Network

Application in Learning Image Descriptors (I)



CNN Model

Siamese Network

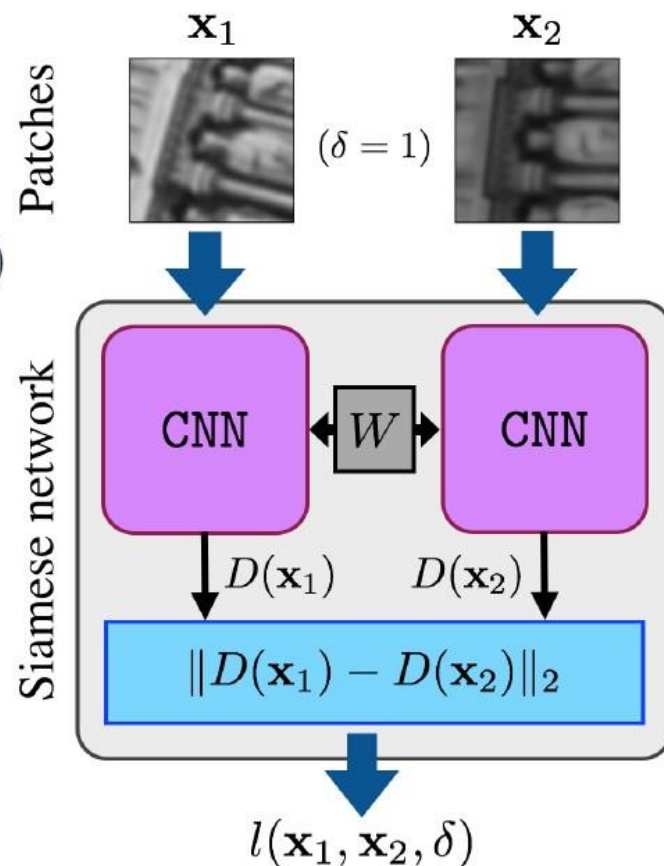
Application in Learning Image Descriptors (II)

$$d_D(\mathbf{x}_1, \mathbf{x}_2) = \|D(\mathbf{x}_1) - D(\mathbf{x}_2)\|_2$$

$$l(\mathbf{x}_1, \mathbf{x}_2, \delta) = \delta \cdot l_P(d_D(\mathbf{x}_1, \mathbf{x}_2)) + (1 - \delta) \cdot l_N(d_D(\mathbf{x}_1, \mathbf{x}_2))$$

$$l_P(d_D(\mathbf{x}_1, \mathbf{x}_2)) = d_D(\mathbf{x}_1, \mathbf{x}_2)$$

$$l_N(d_D(\mathbf{x}_1, \mathbf{x}_2)) = \max(0, m - d_D(\mathbf{x}_1, \mathbf{x}_2))$$

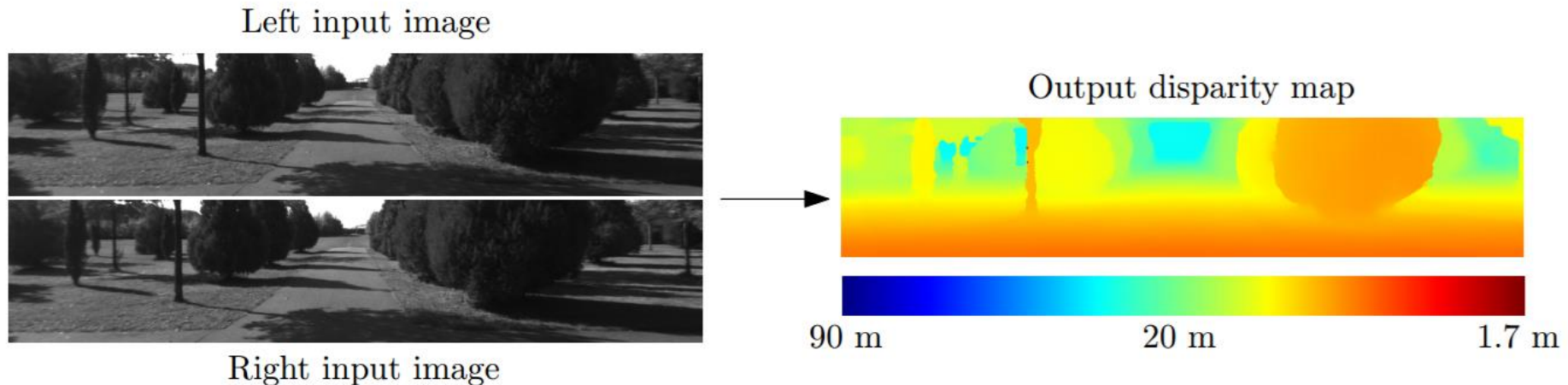


Fracking Deep Convolutional Image Descriptors, <http://arxiv.org/abs/1412.6537>

Convolutional Neural Networks learn compact local image descriptors, <http://arxiv.org/abs/1304.7948>

Siamese Network

Stereo



Zbontar, Jure, and Yann LeCun. "Stereo matching by training a convolutional neural network to compare image patches." *Journal of Machine Learning Research* (2016)

Zbontar, Jure, and Yann LeCun. "Computing the stereo matching cost with a convolutional neural network." *CVPR* 2015.

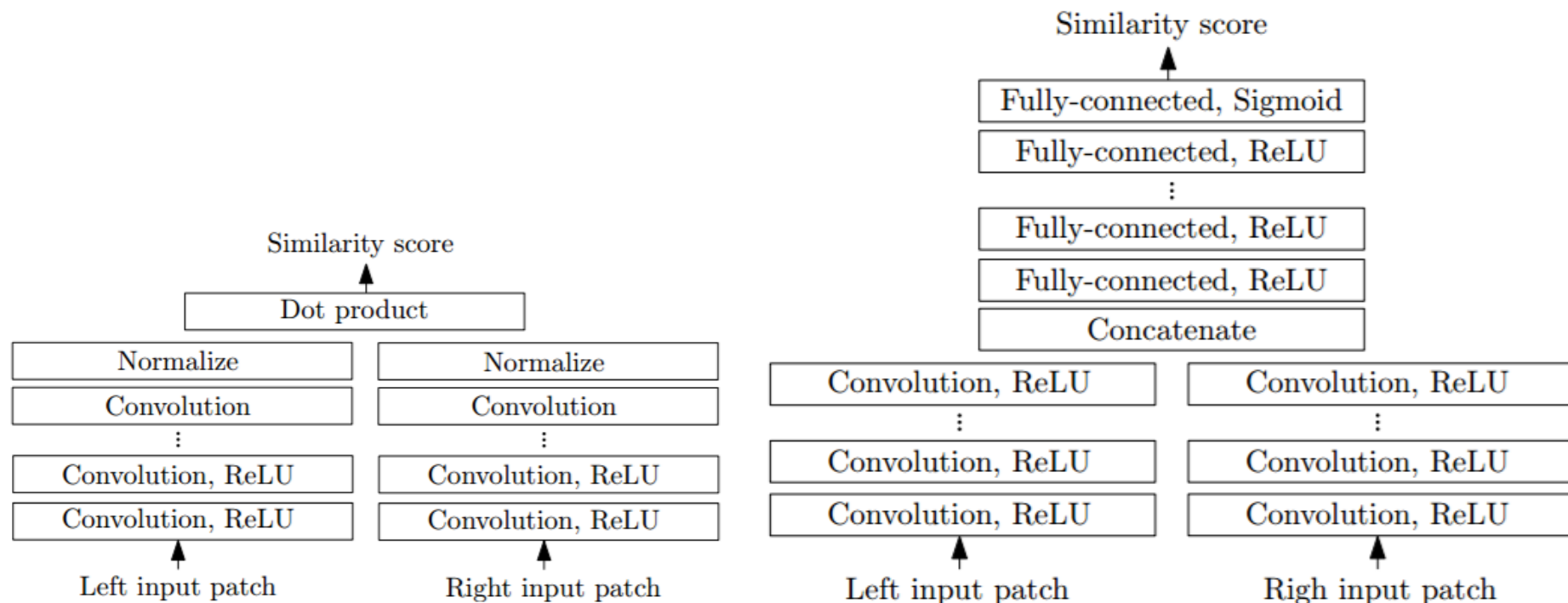
Siamese Network

Stereo

- Correspondences on image locations(Matching)
 - *Good feature*
- Refinement in practice
 - Smoothing

Siamese Network

Stereo

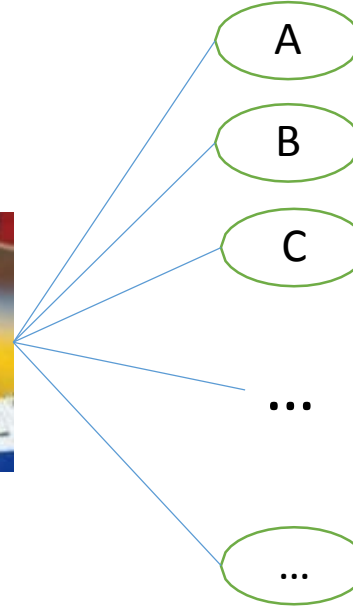


Zbontar, Jure, and Yann LeCun. "Stereo matching by training a convolutional neural network to compare image patches." *Journal of Machine Learning Research* (2016)

Zbontar, Jure, and Yann LeCun. "Computing the stereo matching cost with a convolutional neural network." *CVPR* 2015.

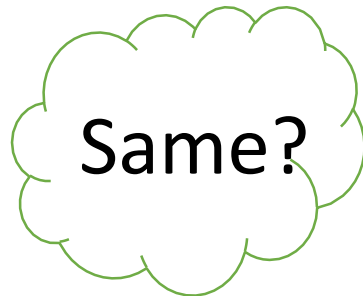
Face recognition

1. Face identification



Multiclass
classification

2. Face verification



Same person or not.

Binary Result

Siamese Network

Application in face verification(I)

Let X_1 and X_2 be a pair of images shown to our learning machine. Let Y be a binary label of the pair, $Y = 0$ if the images X_1 and X_2 belong to the same person (a “genuine pair”) and $Y = 1$ otherwise (an “impostor pair”).

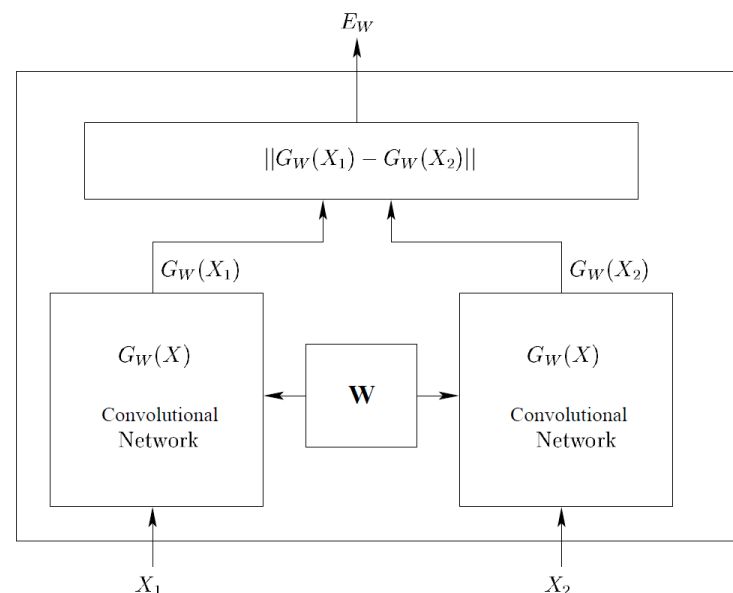
We assume that the loss function depends on the input and the parameters only indirectly through the energy. Our loss function is of the form:

$$\mathcal{L}(W) = \sum_{i=1}^P L(W, (Y, X_1, X_2)^i)$$

$$L(W, (Y, X_1, X_2)^i) = (1 - Y)L_G(E_W(X_1, X_2)^i) + YL_I(E_W(X_1, X_2)^i)$$

$$= (1 - Y)\frac{2}{Q}(E_W)^2 + (Y)2Q e^{-\frac{2.77}{Q}E_W}$$

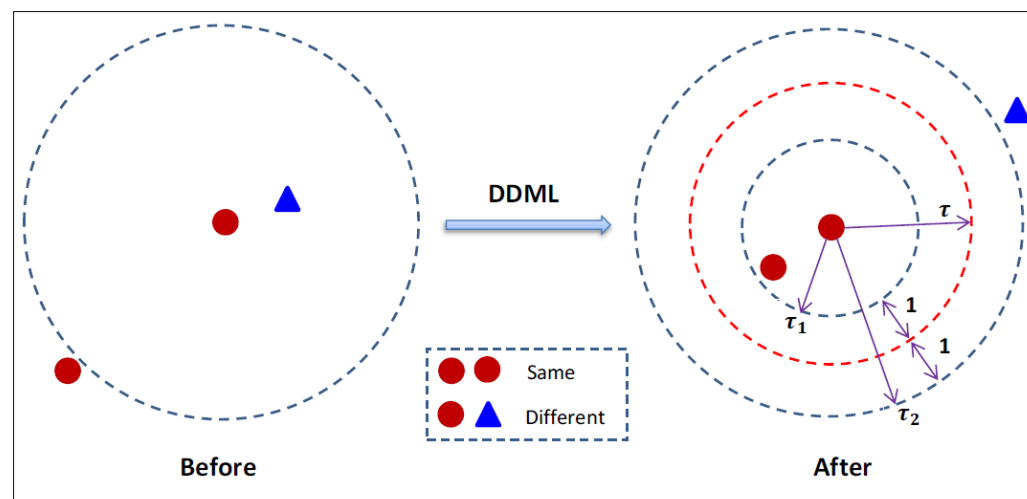
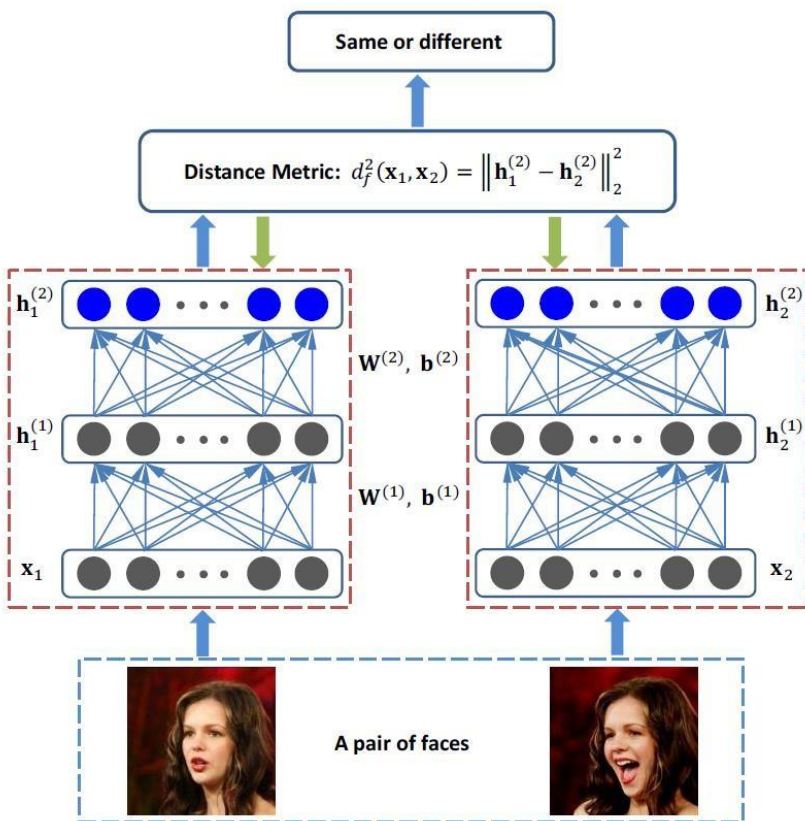
$$E_W = \|G_W(X_1) - G_W(X_2)\|$$



Siamese Network

Application in face verification(II)

LFW:90.68%



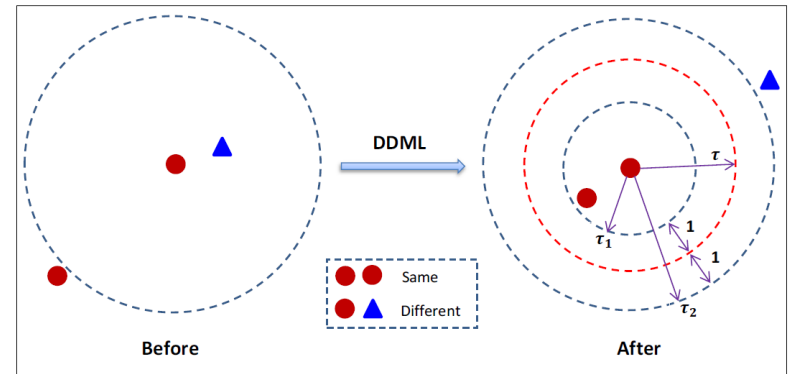
Intuitive illustration of the proposed DDML method

Siamese Network

Application in face verification(II)

$$\begin{aligned} d_f^2(x_i, x_j) < \tau - 1, l_{ij} &= 1 \\ d_f^2(x_i, x_j) > \tau + 1, l_{ij} &= -1 \end{aligned}$$

$$\ell_{ij}(\tau - d_f^2(\mathbf{x}_i, \mathbf{x}_j)) > 1$$

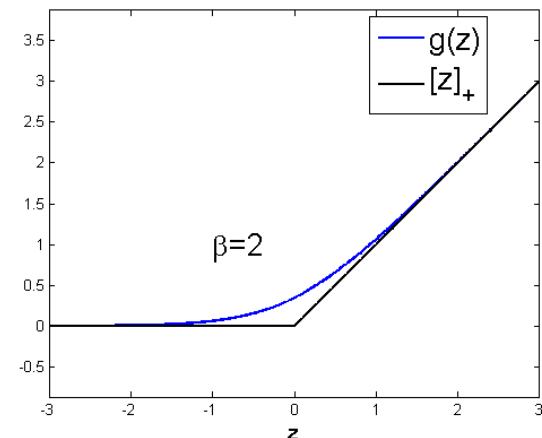


Intuitive illustration of the proposed DDML method

DDML as the following optimization problem:

$$\begin{aligned} \arg \min_f J &= J_1 + J_2 \\ &= \frac{1}{2} \sum_{i,j} g(1 - \ell_{ij}(\tau - d_f^2(\mathbf{x}_i, \mathbf{x}_j))) \\ &+ \frac{\lambda}{2} \sum_{m=1}^M (\|\mathbf{W}^{(m)}\|_F^2 + \|\mathbf{b}^{(m)}\|_2^2) \end{aligned}$$

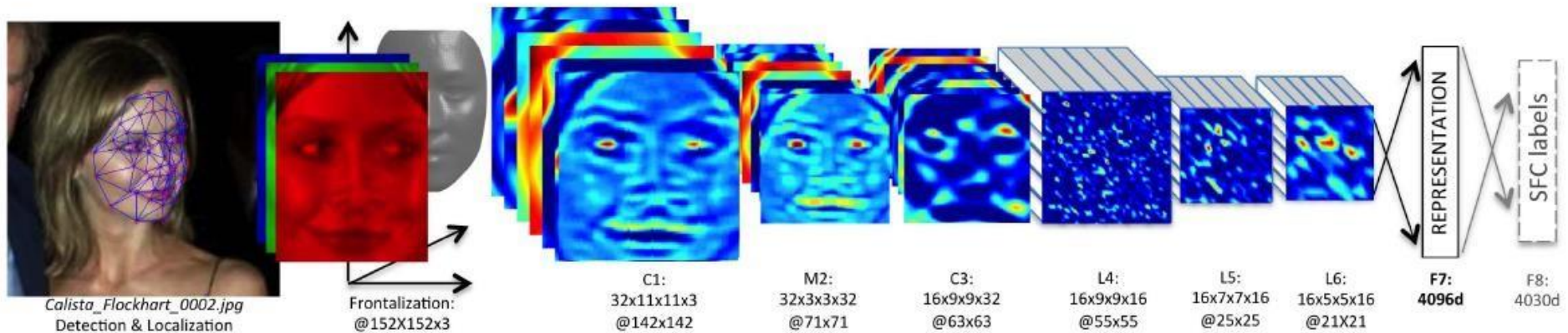
where $g(z) = \frac{1}{\beta} \log(1 + \exp(\beta z))$ is the generalized logistic loss function [25], which is a smoothed approximation of the hinge loss function $[z]_+ = \max(z, 0)$



Classification Network

Application in face verification(IV)

LFW:97.35%



Verification Metric:

1) Cosine similarity

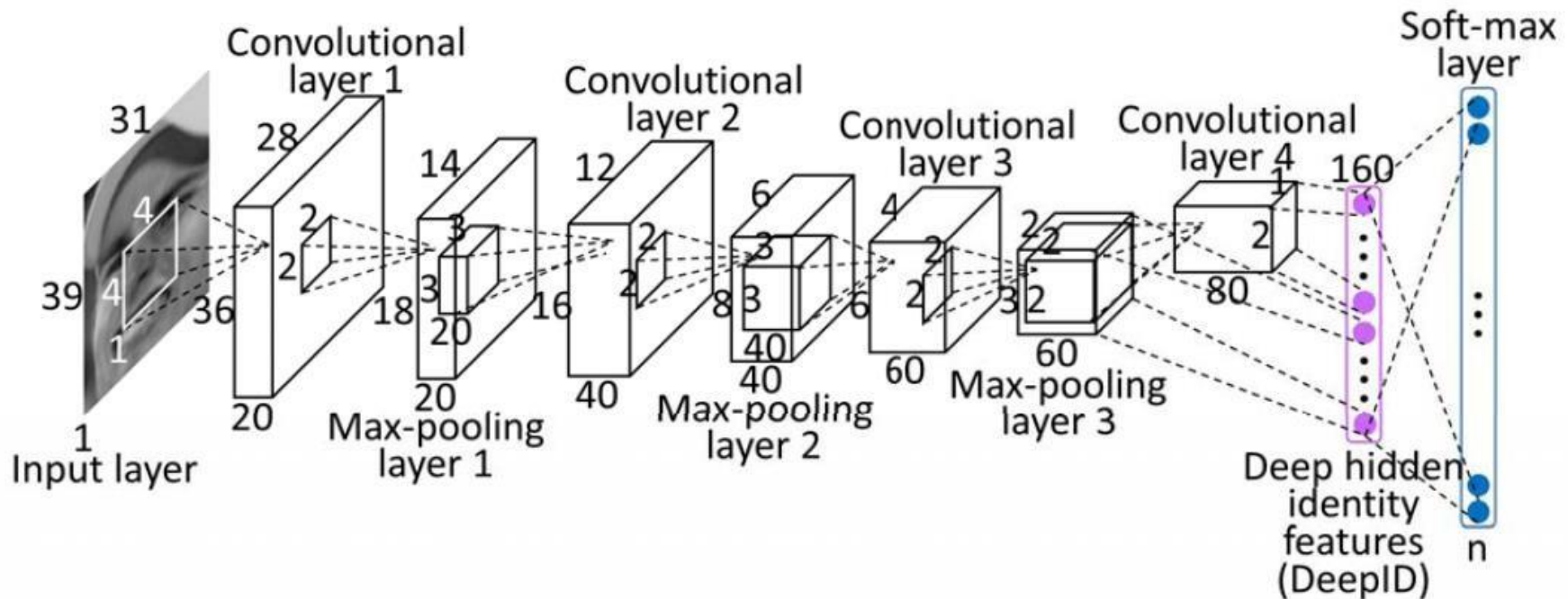
2) Weighted χ^2 distance $\chi^2(f_1, f_2) = \sum_i w_i (f_1[i] - f_2[i])^2 / (f_1[i] + f_2[i])$

3) Siamese network $d(f_1, f_2) = \sum_i \alpha_i |f_1[i] - f_2[i]|$

Classification Network

Application in face verification(III)

LFW:97.45%



Face Verification: Joint Bayesian

Classification & Siamese Network

Application in face verification(V)

LFW:99.15%

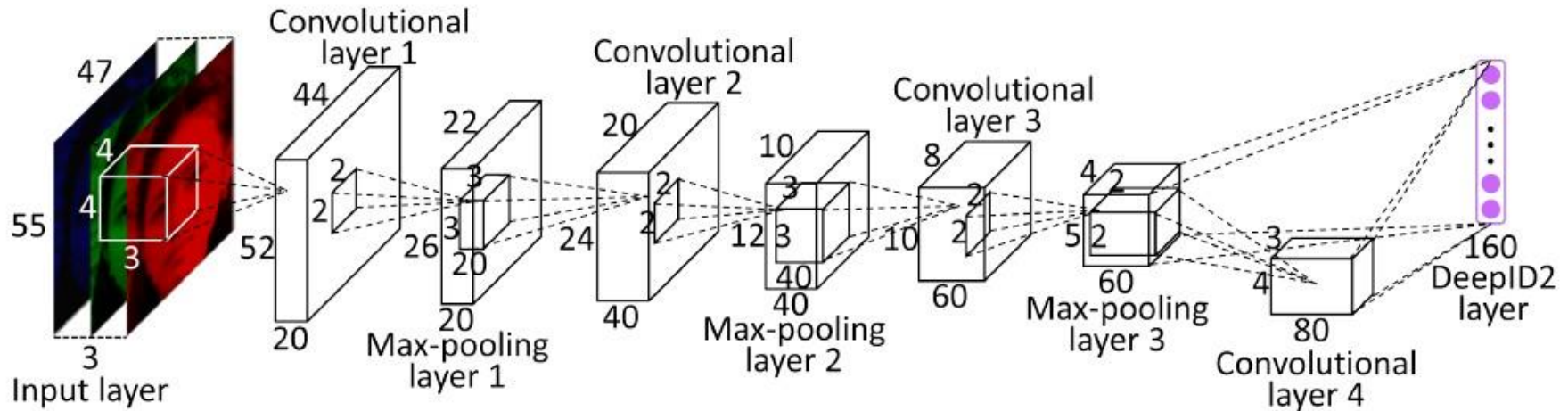


Figure 1: The ConvNet structure for DeepID2 extraction.

Deep Learning Face Representation by Joint Identification-Verification

Classification & Siamese Network

Application in face verification(V)

1. identification loss(cross-entropy)

$$\text{Ident}(f, t, \theta_{id}) = - \sum_{i=1}^n -p_i \log \hat{p}_i = - \log \hat{p}_t$$

2. verification loss (contrastive)

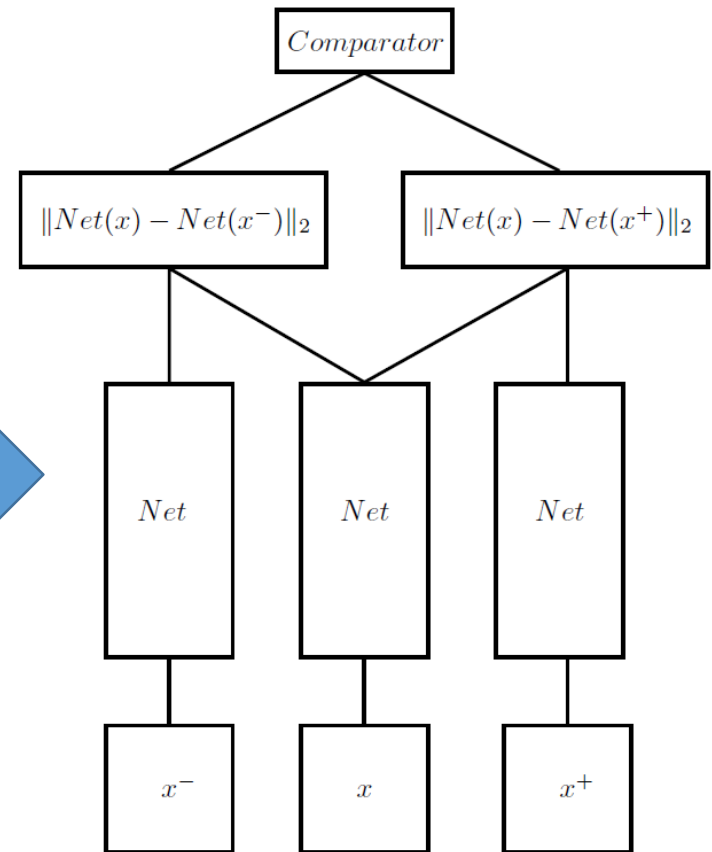
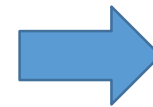
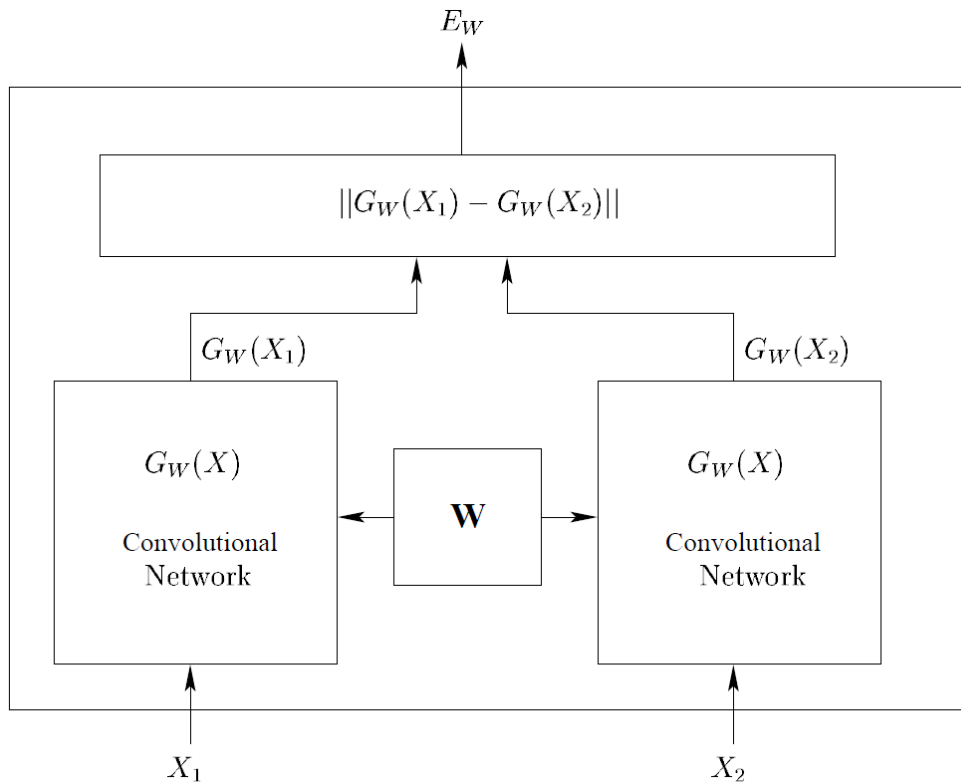
$$\text{Verif}(f_i, f_j, y_{ij}, \theta_{ve}) = \begin{cases} \frac{1}{2} \|f_i - f_j\|_2^2 & \text{if } y_{ij} = 1 \\ \frac{1}{2} \max(0, m - \|f_i - f_j\|_2)^2 & \text{if } y_{ij} = -1 \end{cases}$$

3. verification loss (cosine)

$$\text{Verif}(f_i, f_j, y_{ij}, \theta_{ve}) = \frac{1}{2} (y_{ij} - \sigma(wd + b))^2$$

where $d = \frac{f_i \cdot f_j}{\|f_i\|_2 \|f_j\|_2}$ is the cosine similarity

Triplet Network



From Siamese to Triplet Network

Triplet Network

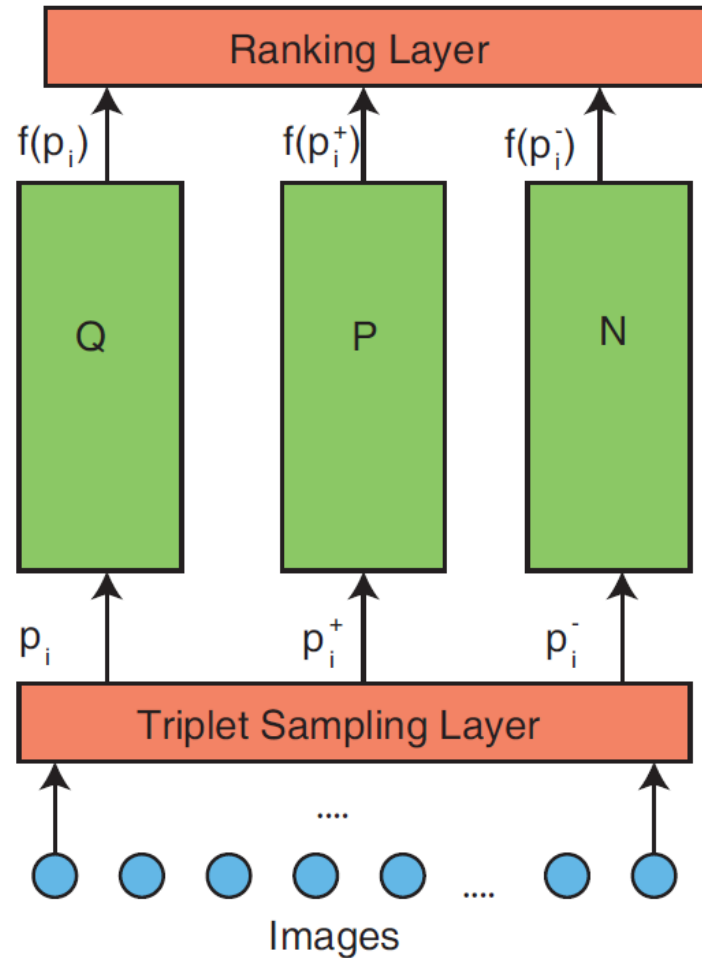
Application in Image ranking

Query					
Positive					
Negative					

Sample images from the triplet dataset

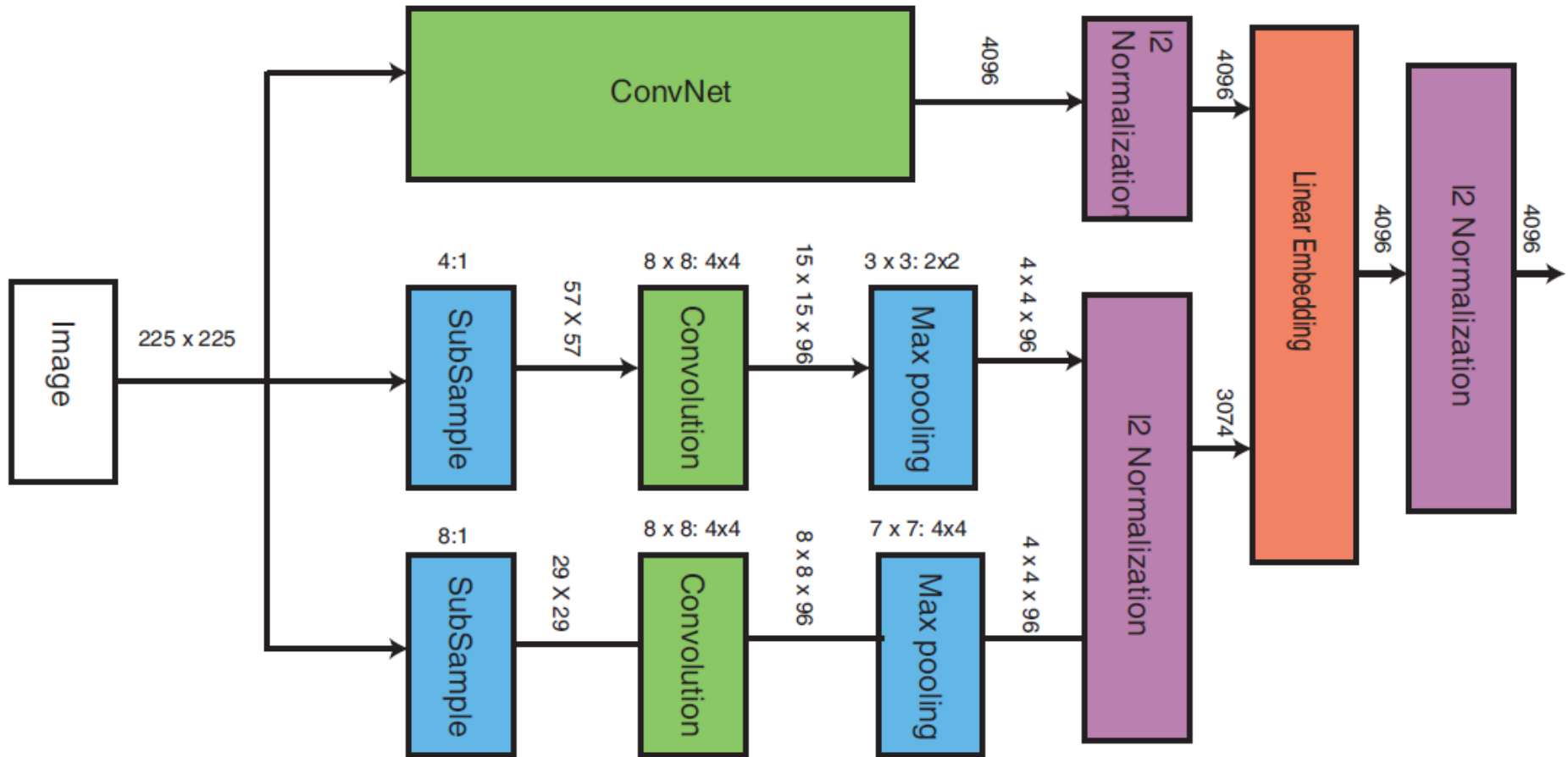
Triplet Network

Application in Image ranking



Triplet Network

Application in Image ranking



Triplet Network

Application in Image ranking

Distance $D(f(P), f(Q)) = \|f(P) - f(Q)\|_2^2$

$$D(f(p_i), f(p_i^+)) < D(f(p_i), f(p_i^-)),$$
$$\forall p_i, p_i^+, p_i^- \text{ such that } r(p_i, p_i^+) > r(p_i, p_i^-)$$

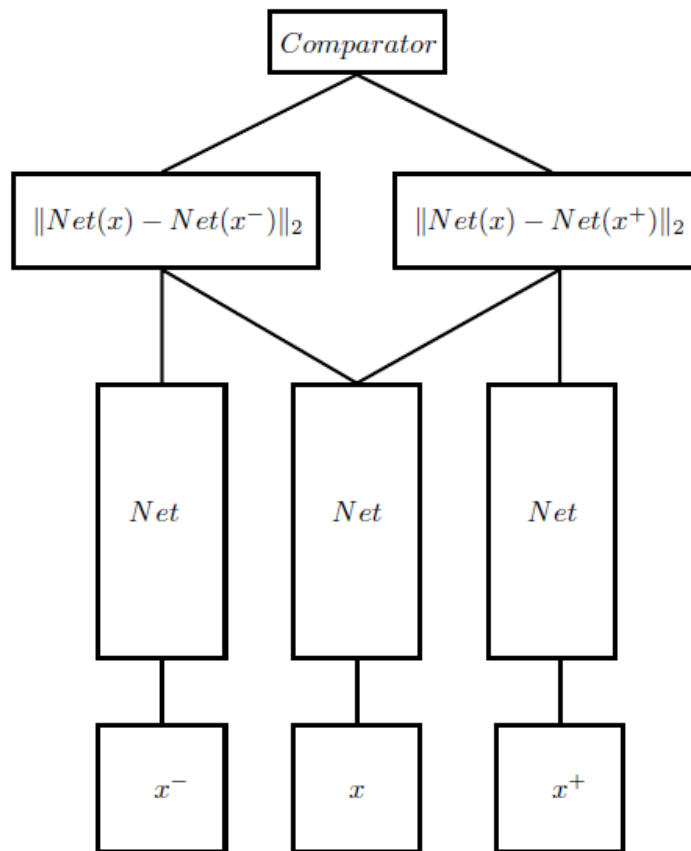
Hinge Loss $l(p_i, p_i^+, p_i^-) =$

$$\max\{0, g + D(f(p_i), f(p_i^+)) - D(f(p_i), f(p_i^-))\}$$

Triplet Network

Application in deep metric learning

$$\text{TripletNet}(x, x^-, x^+) = \begin{bmatrix} \|Net(x) - Net(x^-)\|_2 \\ \|Net(x) - Net(x^+)\|_2 \end{bmatrix} \in \mathbb{R}_+^2$$



SoftMax function is applied
on both outputs

Triplet Network

Application in deep metric learning



2D VISUALIZATION OF FEATURES of CIFAR10

Conclusion

- The loss function in Siamese Network is very important.
- Mixed Network Architecture can improve the performance.
- Caffe implementation of Siamese Network:
<http://caffe.berkeleyvision.org/gathered/examples/siamese.html>

Thank you!