



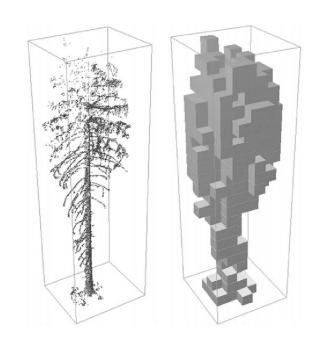
Differentiable Rendering

Abdullah Hamdi, IVUL group meeting

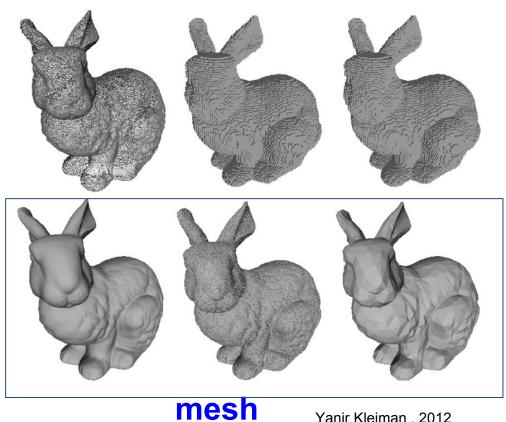


3D representation





point cloud vs Voxels



Yanir Kleiman, 2012

3D representation

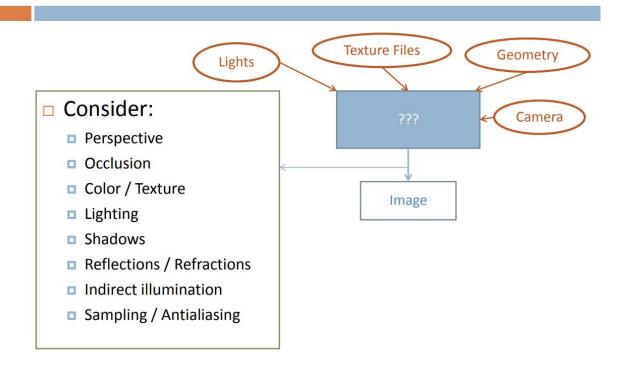


A Mesh is compact & useful for shading





What is Rendering?





Two Approaches

- Start from geometry
 - For each polygon / triangle:
 - Is it visible?
 - Where is it?
 - What color is it?

Rasterization

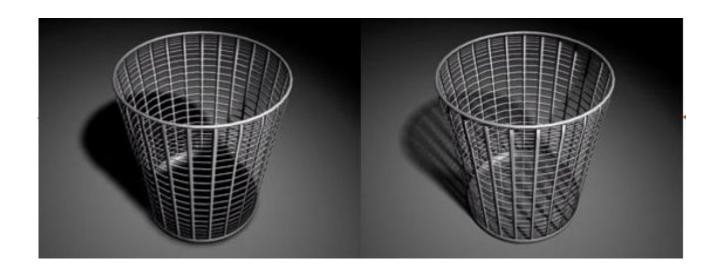
- Start from pixels
 - For each pixel in the final image:
 - Which object is visible at this pixel?
 - What color is it?

Ray Tracing

Shadows



Rasterization vs ray tracing



Degrees of realism





Polygonal model rendered in wire-frame (no visibility)



With visibility.



Shaded rendering. Note how the faces of the cube and cone have different intensities depending on their orientation relative to the light source.



Smooth patches and shading including highlights.

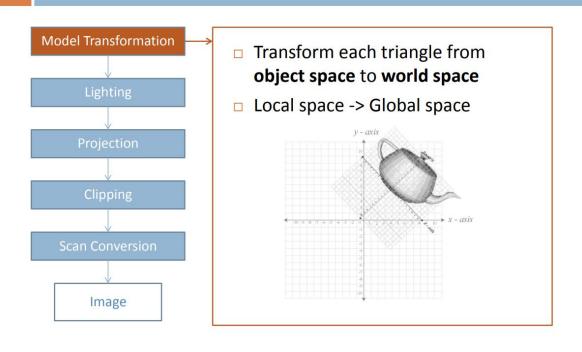


Texture-Mapping improves the appearance of surfaces (a better lighting is used too).

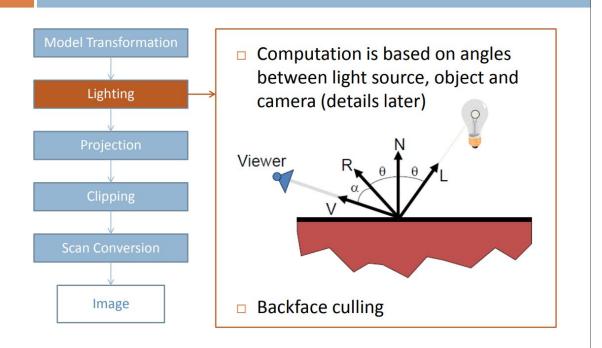


Shadows.

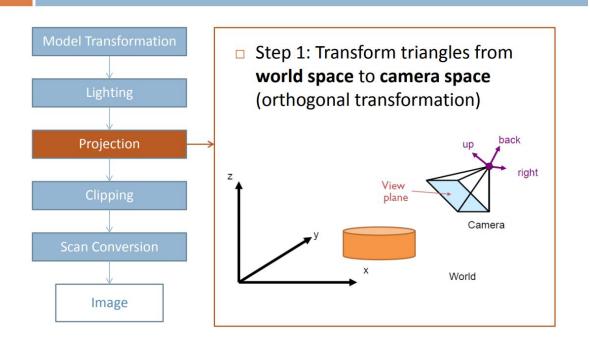




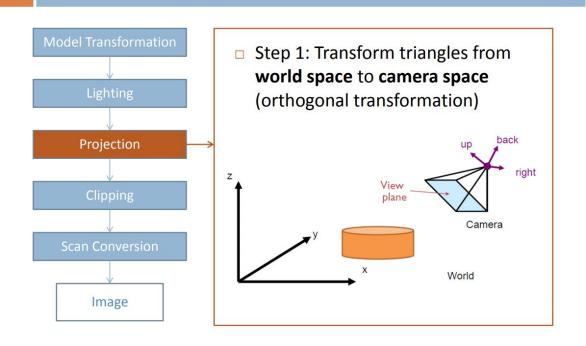






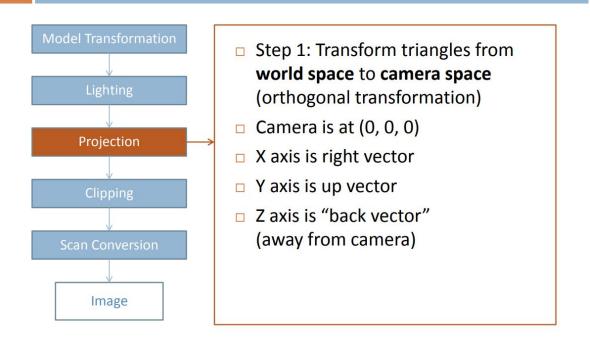






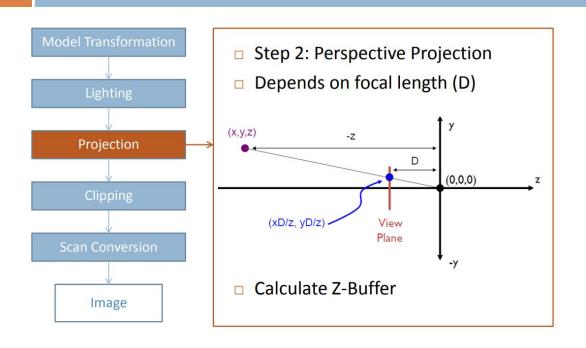


Rasterization – Graphics Pipeline



Yanir Kleiman, 2012



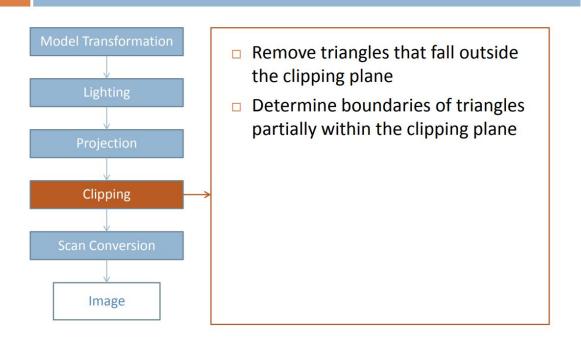




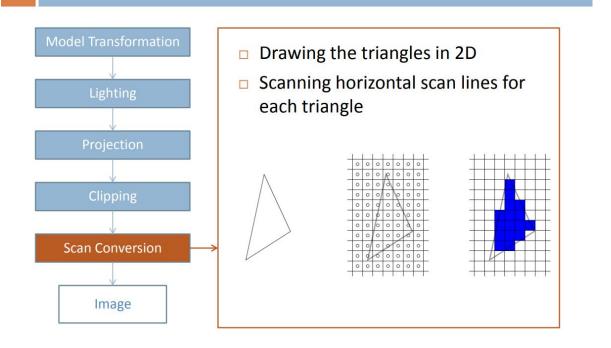
Projection equation

$$\lambda \begin{bmatrix} x \\ y \\ 1 \end{bmatrix} = \mathbf{P} \begin{bmatrix} u \\ v \\ w \\ 1 \end{bmatrix}, \quad \mathbf{P} = \mathbf{K} \begin{bmatrix} \mathbf{R} & \mathbf{t} \end{bmatrix}, \quad \mathbf{K} = \begin{bmatrix} f & 0 & c_x \\ 0 & f & c_y \\ 0 & 0 & 1 \end{bmatrix}$$





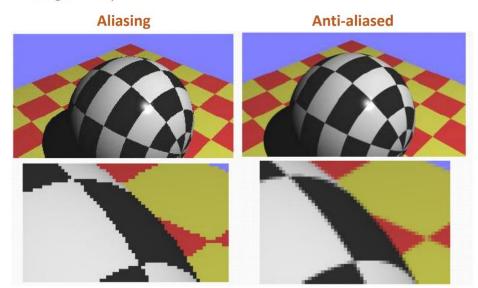






Rasterization – Antialiasing

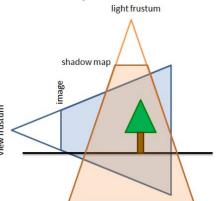
Aliasing examples





Rasterization – Shadow Maps

- Render an image from the light's point of view (the light is the camera)
- Shadow map
- Keep "depth" from light of every pixel in the map
- During image render:
 Calculate position and depth on the shadow map for each pixel in the final image (not vertex!)
- If pixel depth > shadow map depth the pixel will not receive light from this source





Rasterization – Shadow Maps

- This solution is not optimal
- Shadow map resolution is not correlated to render resolution – one shadow map pixel can span a lot of rendered pixels!
- Shadow aliasing
- Only allows sharp shadows
- Semi-transparent objects

Various hacks and complex solutions

Blurred hard shadows (shadow map)

True soft shadows (ray tracing)



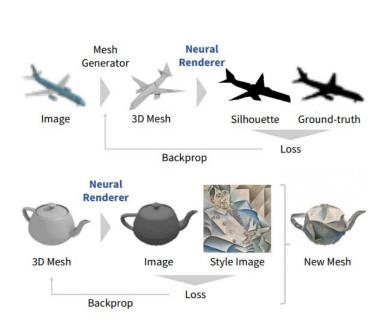
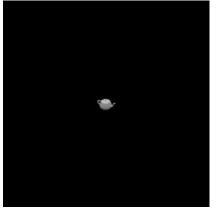


Figure 1. Pipelines for single-image 3D mesh reconstruction (upper) and 2D-to-3D style transfer (lower).







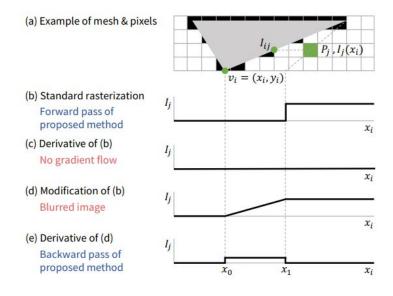


Figure 2. Illustration of our method. $v_i = \{x_i, y_i\}$ is one vertex of the face. I_j is the color of pixel P_j . The current position of x_i is x_0 . x_1 is the location of x_i where an edge of the face collides with the center of P_j when x_i moves to the right. I_j becomes I_{ij} when $x_i = x_1$.

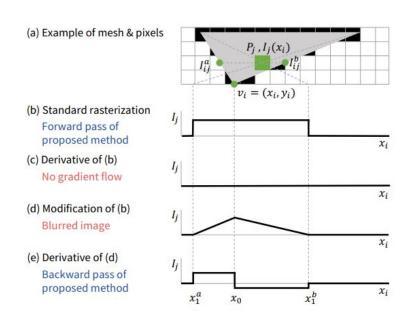


Figure 3. Illustration of our method in the case where P_j is inside the face. I_j changes when x_i moves to the right or left.



$$\frac{\partial I_j(x_i)}{\partial x_i}\Big|_{x_i=x_0} = \begin{cases} \frac{\delta_j^I}{\delta_i^x}; & \delta_j^P \delta_j^I < 0.\\ 0; & \delta_j^P \delta_j^I \ge 0. \end{cases}$$

$$\frac{\partial I_{j}(x_{i})}{\partial x_{i}}\Big|_{x_{i}=x_{0}} = \frac{\partial I_{j}(x_{i})}{\partial x_{i}}\Big|_{x_{i}=x_{0}}^{a} + \frac{\partial I_{j}(x_{i})}{\partial x_{i}}\Big|_{x_{i}=x_{0}}^{b}.$$

$$\frac{\partial I_{j}(x_{i})}{\partial x_{i}}\Big|_{x_{i}=x_{0}}^{a} = \begin{cases} \frac{\delta_{j}^{I^{a}}}{\delta_{x}^{a}}; & \delta_{j}^{P}\delta_{j}^{I^{a}} < 0.\\ 0; & \delta_{j}^{P}\delta_{j}^{I^{a}} \geq 0. \end{cases}$$

$$\frac{\partial I_{j}(x_{i})}{\partial x_{i}}\Big|_{x_{i}=x_{0}}^{b} = \begin{cases} \frac{\delta_{j}^{I^{b}}}{\delta_{x}^{b}}; & \delta_{j}^{P}\delta_{j}^{I^{b}} < 0.\\ 0; & \delta_{j}^{P}\delta_{j}^{I^{a}} \geq 0. \end{cases}$$

$$0; & \delta_{j}^{P}\delta_{j}^{I^{a}} \geq 0.$$



$$I_j^l = (l^a + (\boldsymbol{n}^d \cdot \boldsymbol{n}_j) l^d) I_j.$$

$$\mathcal{L}_{sl}(x|\phi_i, s_i) = -\frac{|\hat{s}_i \odot s_i|_1}{|\hat{s}_i + s_i - \hat{s}_i \odot s_i|_1}.$$

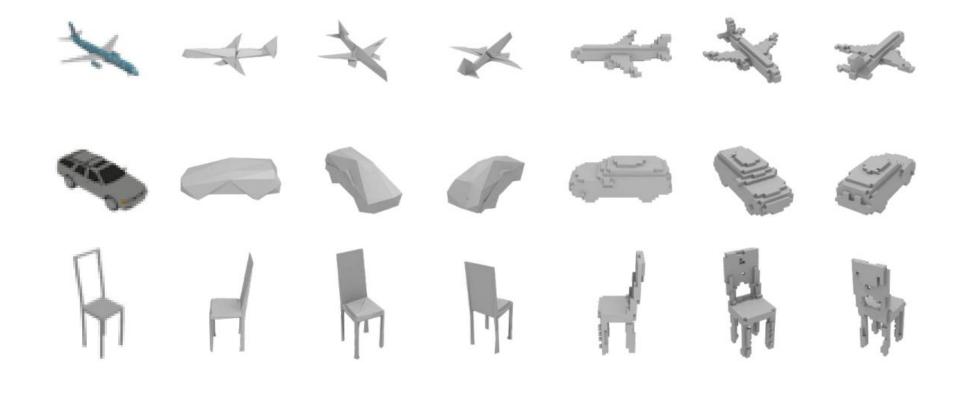
$$\mathcal{L}_{sm}(x) = \sum_{\theta_i \in \mathcal{E}} (\cos \theta_i + 1)^2.$$



	airplane	bench	dresser	car	chair	display	lamp	
Retrieval [36]	0.5564	0.4875	0.5713	0.6519	0.3512	0.3958	0.2905	
Voxel-based [36]	0.5556	0.4924	0.6823	0.7123	0.4494	0.5395	0.4223	
Mesh-based (ours)	0.6172	0.4998	0.7143	0.7095	0.4990	0.5831	0.4126	
	loudspeaker	rifle	sofa	table	telephone	vessel		mean
Retrieval [36]	0.4600	0.5133	0.5314	0.3097	0.6696	0.4078		0.4766
Voxel-based [36]	0.5868	0.5987	0.6221	0.4938	0.7504	0.5507		0.5736
Mesh-based (ours)	0.6536	0.6322	0.6735	0.4829	0.7777	0.5645		0.6016

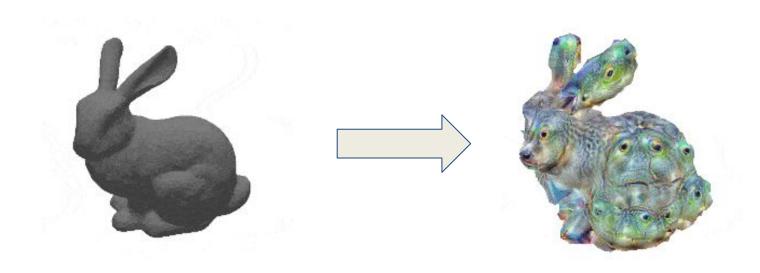
Table 1. Reconstruction accuracy measured by voxel IoU. Higher is better. Our mesh-based approach outperforms the voxel-based approach [36] in 10 out of 13 categories.







Deep dream





Style tansfer



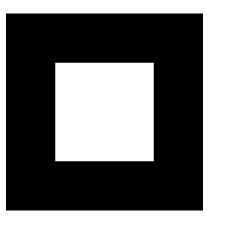






Optimizing mesh to match a projection



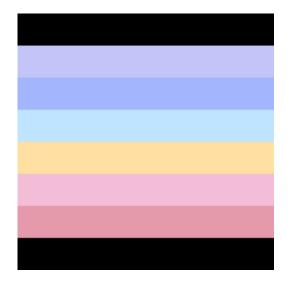








Optimizing texture

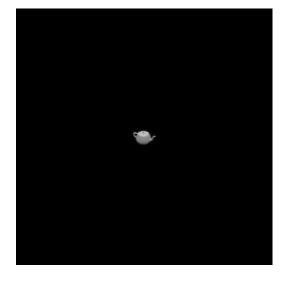






Optimizing view point





Jupyter Notebook!!



Let's all do it !!!

