# **Formulas from Geometry**

#### **Area Formulas**

#### Square

 $A = s^2$  where s is the side length

 $A = \frac{1}{2}d^2$  where d is the length of the diagonal

#### Triangle

 $A = \frac{1}{2}bh$  where b is the base and h is the altitude

 $A = \sqrt{s(s-a)(s-b)(s-c)}$  where s is the semiperimeter and a, b, and c are the sides

A = sr where s is the semiperimeter and r is the radius of the inscribed circle

 $A = \frac{1}{2}ab\sin\theta$  where a and b are two sides and  $\theta$  is the measure of the angle between a and b

#### Equilateral Triangle

 $A = \frac{1}{4}s^2\sqrt{3}$  where s is the side length

 $A = \frac{1}{3}h^2\sqrt{3}$  where h is the altitude

#### Parallelogram

A = bh where b is the base and h is the altitude

#### Rhombus

A = bh where b is the base and h is the altitude

 $A = \frac{1}{2}d_1d_2$  where  $d_1$  and  $d_2$  are the two diagonals

#### Kite

 $A = \frac{1}{2}d_1d_2$  where  $d_1$  and  $d_2$  are the two diagonals

#### Trapezoid

 $A = \frac{1}{2}(b_1 + b_2)h$  where  $b_1$  and  $b_2$  are the parallel bases and h is the distance between them

# $Cyclic\ Quadrilateral$

 $A = \sqrt{(s-a)(s-b)(s-c)(s-d)}$  where s is the semiperimeter and a, b, c, d are the sides

#### Regular Polygon

 $A = \frac{1}{2}ans$  where a is the apothem, n is the number of sides, and s is the side length

 $A = \frac{1}{2}ap$  where a is the apothem and p is the perimeter

#### Ellipse

 $A = ab\pi$  where a is half the major axis and b is half the minor axis

#### Circle

 $A = \pi r^2$  where r is the radius

 $A = \frac{1}{2}Cr$  where C is the circumference and r is the radius

 $A = \frac{1}{4}\pi d^2$  where d is the diameter

#### Sector of a Circle

 $A = \frac{1}{360^{\circ}} \pi a r^2$  where a is the angle (in degrees) that intercepts the arc and r is the radius

 $A = \frac{1}{2}ar^2$  where a is the angle (in radians) that intercepts the arc and r is the radius

#### **Surface Area Formulas**

Prism and Cylinder

S=2B+ph where B is the area of the base, p is the perimeter of the base, and h is the height

Pyramid and Cone

 $S = B + \frac{1}{2}ps$  where B is the area of the base, p is the perimeter of the base, and s is the slant height of a lateral face

Sphere

 $S = 4\pi r^2$  where r is the radius

### **Volume Formulas**

Prism and Cylinder

V = Bh where B is the area of the base and h is the height

Pyramid and Cone

 $V = \frac{1}{3}Bh$  where B is the area of the base and h is the height

Sphere

 $V = \frac{4}{3}\pi r^3$  where r is the radius

# **Greek Alphabet**

Upper	Lower		Upper	Lower	
case	case		case	case	
A	$\alpha$	alpha	N	$\nu$	nu
В	$\beta$	beta	Ξ	ξ	xi
$\Gamma$	$\gamma$	gamma	O	O	omicron
$\Delta$	$\delta$	delta	Π	$\pi$	pi
${ m E}$	$\epsilon$	epsilon	$\mathbf{R}$	ho	rho
$\mathbf{Z}$	$\zeta$	zeta	$\sum$	$\sigma$	sigma
Η	$\eta$	eta	Τ	au	tau
$\Theta$	$\theta$	theta	Υ	v	upsilon
I	$\iota$	iota	$\Phi$	$\phi$	phi
K	$\kappa$	kappa	X	$\chi$	chi
$\Lambda$	$\lambda$	lambda	$\Psi$	$\psi$	psi
M	$\mu$	mu	$\Omega$	$\omega$	omega

# **Trigonometric Values**

$$\sin 0 = 0$$

$$\sin\frac{\pi}{6} = \frac{1}{2}$$

$$\sin\frac{\pi}{4} = \frac{\sqrt{2}}{2}$$

$$\cos 0 = 1$$

$$\cos\frac{\pi}{6} = \frac{\sqrt{3}}{2}$$

$$\cos\frac{\pi}{4} = \frac{\sqrt{2}}{2}$$

$$\tan 0 = 0$$

$$\tan\frac{\pi}{6} = \frac{\sqrt{3}}{3}$$

$$\tan\frac{\pi}{4} = 1$$

$$\sin\frac{\pi}{3} = \frac{\sqrt{3}}{2}$$

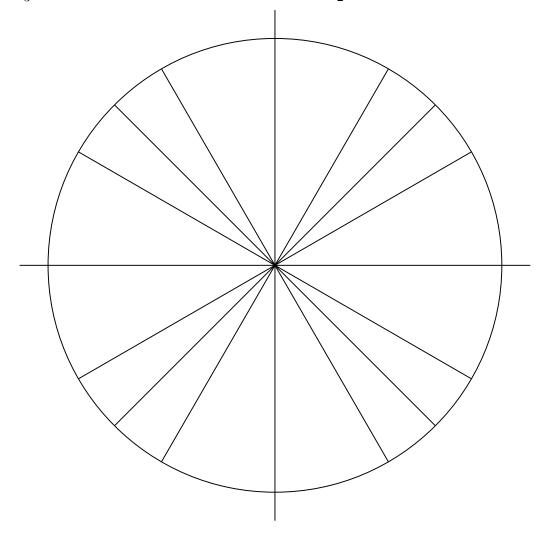
$$\sin\frac{\pi}{2} = 1$$

$$\cos\frac{\pi}{3} = \frac{1}{2}$$

$$\cos\frac{\pi}{2} = 0$$

$$\tan\frac{\pi}{3} = \sqrt{3}$$

 $\tan \frac{\pi}{2}$  is undefined



# **Useful Trigonometric Identities**

## **Triangle Ratios**

$$\sin x = \frac{\text{opposite}}{\text{hypotenuse}}$$

$$\csc x = \frac{1}{\sin x} = \frac{\text{hypotenuse}}{\text{opposite}}$$

$$\cot x = \frac{\cos x}{\sin x} = \frac{\text{adjacent}}{\text{opposite}}$$

$$\cos x = \frac{\text{adjacent}}{\text{hypotenuse}}$$

$$\sec x = \frac{1}{\cos x} = \frac{\text{hypotenuse}}{\text{adjacent}}$$

$$\tan x = \frac{\sin x}{\cos x} = \frac{\text{opposite}}{\text{adjacent}}$$

## **Pythagorean Identities**

$$\sin^2 x + \cos^2 x = 1$$

$$\tan^2 x + 1 = \sec^2 x$$

$$\cot^2 x + 1 = \csc^2 x$$

## **Double Angle Identities**

$$\sin 2x = 2\sin x \cos x$$

$$\cos 2x = \cos^2 x - \sin^2 x = 1 - 2\sin^2 x = 2\cos^2 x - 1$$

#### **Power Identities**

$$\sin^2 x = \frac{1 - \cos 2x}{2}$$

$$\cos^2 x = \frac{1 + \cos 2x}{2}$$

#### **Sum and Difference Identities**

$$\sin(x \pm y) = \sin x \cos y \pm \cos x \sin y$$

$$\cos(x \pm y) = \cos x \cos y \mp \sin x \sin y$$

#### **Law of Cosines**

$$c^2 = a^2 + b^2 - 2ab\cos\gamma$$

#### **Law of Sines**

$$\frac{\sin \alpha}{a} = \frac{\sin \beta}{b} = \frac{\sin \gamma}{c}$$