## Homework 9

Austin Frownfelter

Matthew Bialecki

February 2, 2018

## 1 Problem 13

## 1.1 $M \rightarrow N$

Let N = M, b = 1.

Since M accepts x if  $x \in L$  in time T(|x|), N will accept x in time 1 \* T(|x|).

## 1.2 $N \rightarrow M$

To construct M from N, increase the alphabet size of M by a factor of b. Reconstruct M to be able to accept these larger alphabet symbols.

Construct a mapping of permutations of symbols of length 1 to b in N to the alphabet in M.

Begin at the start state of N

Search using a DFS to a depth of k \* b

Pause at this point and create a transition from the parent state ((k-1)\*b) to the current state using the single alphabet symbol mapped by the path used to get there.

If the DFS gets to a depth  $\neq k * b$  and cannot go farther, create a transition from the parent state to the current state using the single alphabet symbol mapped by the path used to get there.

M is a "sped up" version of N, since N's transitions are traversed b-at-a-time. Since there exists a mapping of  $M \to N$  and  $N \to M$ , the two definitions are equivalent.